

## **Supplementary Materials**

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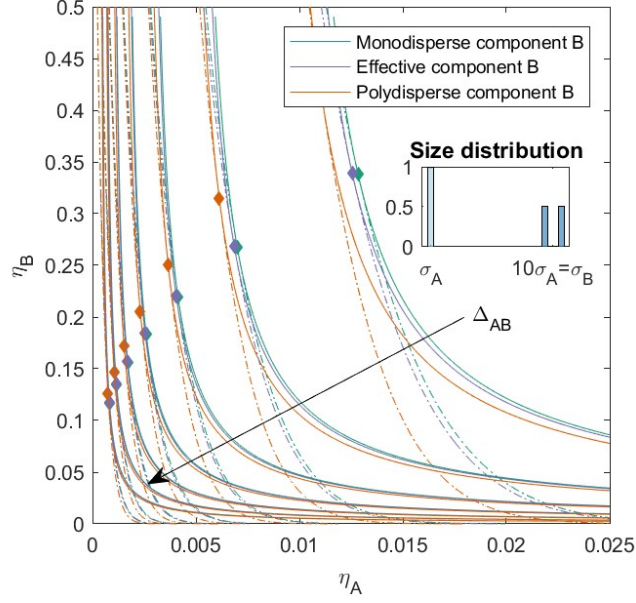
*Laboratory of Physics and Physical Chemistry of Foods,*

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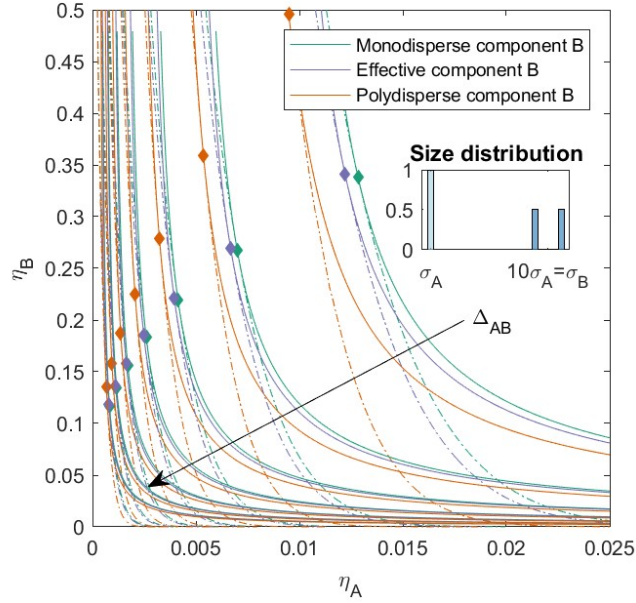
*The Netherlands*

## I. FIGURES

### A. Variation in $\Delta_{AB}$ between component A and B

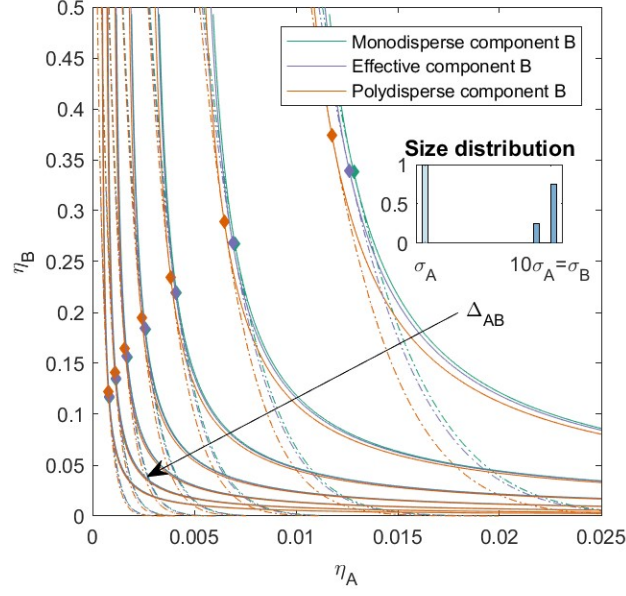


(a)  $PD = 8.00$

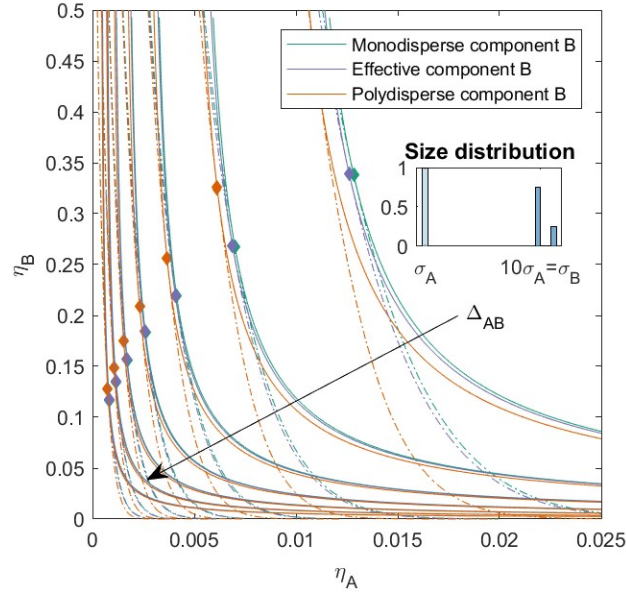


(b)  $PD = 12.00$

FIG. S 1. Phase diagram for binary (component  $A$  and  $B$ ) non-additive hard sphere mixture with size ratio  $q = \sigma_A/\sigma_B = 1/10$ , component  $A$  is monodisperse, component  $B$  is polydisperse, plotted as a function of the partial packing fractions,  $\eta_A$  and  $\eta_B$ . The interaction between components  $A$  and  $B$  is non-additive, the non-additivity parameter  $\Delta_{AB}$  was varied from -0.1 to 0.5 with a step size of 0.1 (the arrow indicates increasing  $\Delta_{AB}$ ). The interaction between the sub-components  $B$  is additive. The spinodal (solid line) and binodal (dashed line) meet each other at the critical point (diamond)

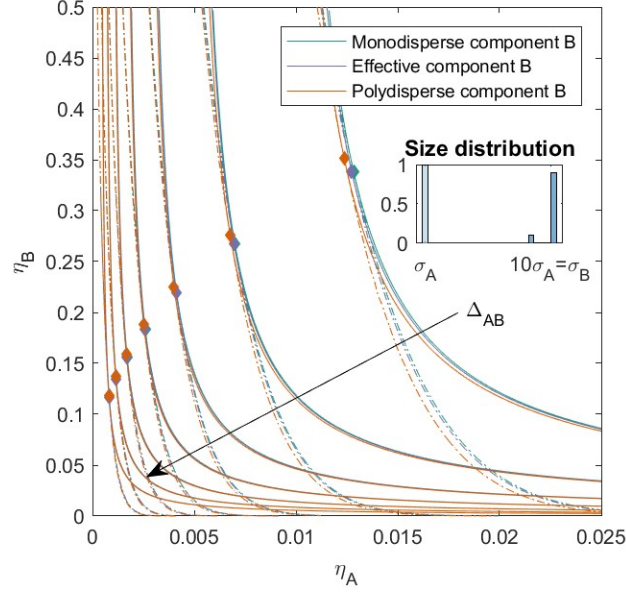


(a) Left skewed

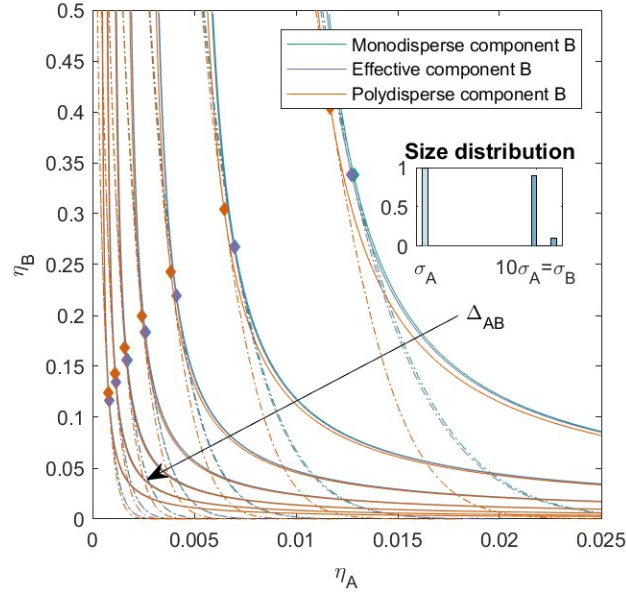


(b) Right skewed

FIG. S 2. Phase diagram for binary (component  $A$  and  $B$ ) non-additive hard sphere mixture with size ratio  $q = \sigma_A/\sigma_B = 1/10$ , component  $A$  is monodisperse, component  $B$  is polydisperse ( $PD = 6.93$ ), plotted as a function of the partial packing fractions,  $\eta_A$  and  $\eta_B$ . The interaction between components  $A$  and  $B$  is non-additive, the non-additivity parameter  $\Delta_{AB}$  was varied from  $-0.1$  to  $0.5$  with a step size of  $0.1$  (the arrow indicates increasing  $\Delta_{AB}$ ). The interaction between the sub-components  $B$  is additive. The spinodal (solid line) and binodal (dashed line) meet each other at the critical point (diamond)



(a) Left skewed



(b) Right skewed

FIG. S 3. Phase diagram for binary (component  $A$  and  $B$ ) non-additive hard sphere mixture with size ratio  $q = \sigma_A/\sigma_B = 1/10$ , component  $A$  is monodisperse, component  $B$  is polydisperse ( $PD = 4.80$ ), plotted as a function of the partial packing fractions,  $\eta_A$  and  $\eta_B$ . The interaction between components  $A$  and  $B$  is non-additive, the non-additivity parameter  $\Delta_{AB}$  was varied from  $-0.1$  to  $0.5$  with a step size of  $0.1$  (the arrow indicates increasing  $\Delta_{AB}$ ). The interaction between the sub-components  $B$  is additive. The spinodal (solid line) and binodal (dashed line) meet each other at the critical point (diamond)

**B. Variation in  $\Delta_{B_a B_b}$  between sub-components B at lower size ratio ( $q$ ) between component A and B for different  $\Delta_{AB}$**

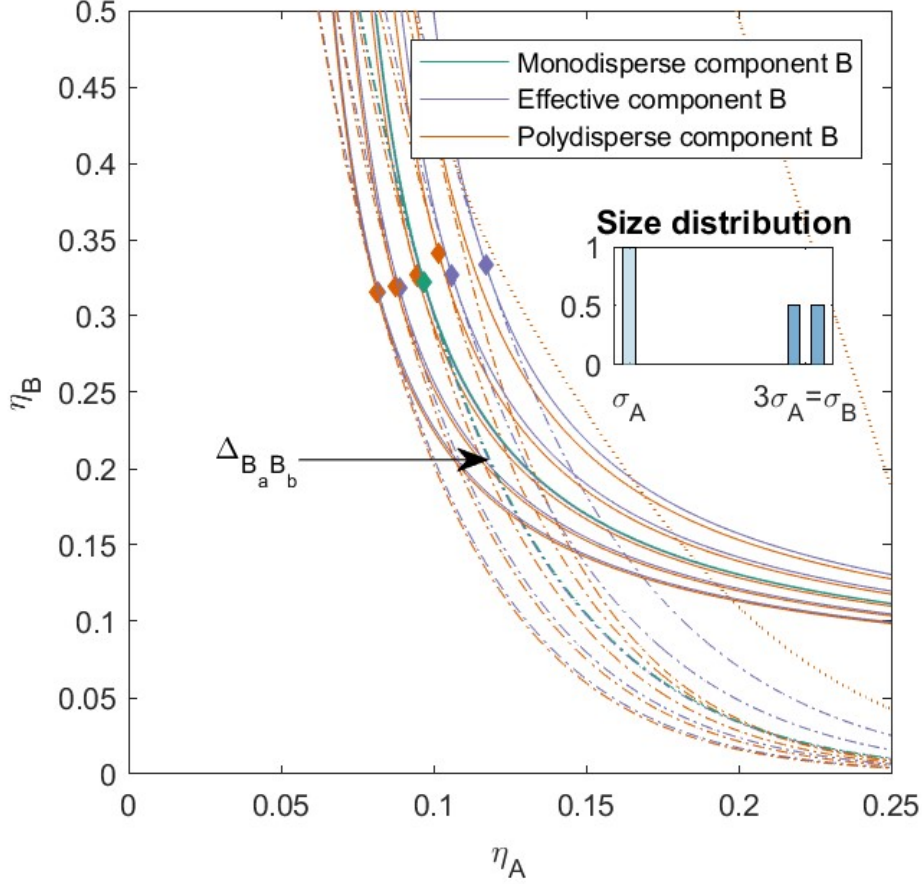


FIG. S 4. Phase diagram for binary (component  $A$  and  $B$ ) non-additive hard sphere mixture with size ratio  $q = \sigma_A/\sigma_B = 1/3$ , component  $A$  is monodisperse, component  $B$  is polydisperse ( $PD = 4.00$ ), plotted as a function of the partial packing fractions,  $\eta_A$  and  $\eta_B$ . The interaction between components  $A$  and  $B$  is non-additive with a non-additivity parameter  $\Delta_{AB} = 0.05$ , the interaction between the sub-components  $B$  is non-additive, the non-additivity parameter  $\Delta_{B_a B_b}$  was varied from  $-0.1$  to  $0.1$  with a step size of  $0.05$  (the arrow indicates increasing  $\Delta_{B_a B_b}$ ). The spinodal (solid line) and binodal (dashed line) meet each other at the plait point (diamond), the three phase boundary is indicated with a dotted line

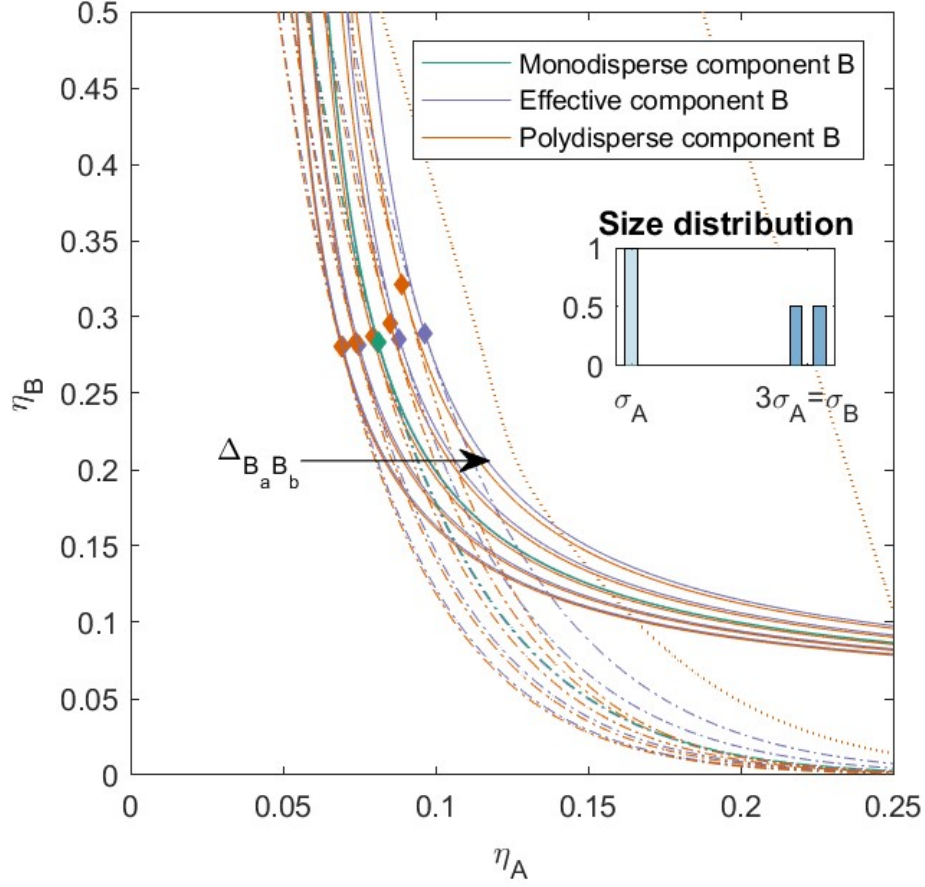


FIG. S 5. Phase diagram for binary (component  $A$  and  $B$ ) non-additive hard sphere mixture with size ratio  $q = \sigma_A/\sigma_B = 1/3$ , component  $A$  is monodisperse, component  $B$  is polydisperse ( $PD = 4.00$ ), plotted as a function of the partial packing fractions,  $\eta_A$  and  $\eta_B$ . The interaction between components  $A$  and  $B$  is non-additive with a non-additivity parameter  $\Delta_{AB} = 0.075$ , the interaction between the sub-components  $B$  is non-additive, the non-additivity parameter  $\Delta_{B_a B_b}$  was varied from  $-0.1$  to  $0.1$  with a step size of  $0.05$  (the arrow indicates increasing  $\Delta_{B_a B_b}$ ). The spinodal (solid line) and binodal (dashed line) meet each other at the plait point (diamond), the three phase boundary is indicated with a dotted line

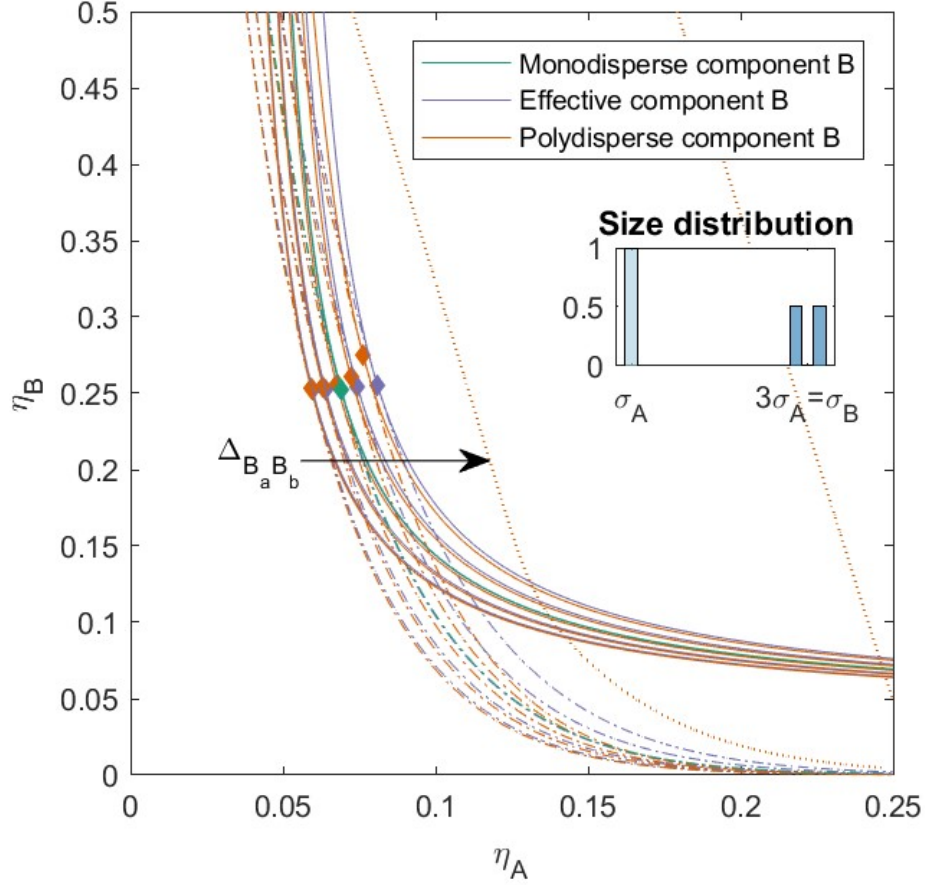


FIG. S 6. Phase diagram for binary (component  $A$  and  $B$ ) non-additive hard sphere mixture with size ratio  $q = \sigma_A/\sigma_B = 1/3$ , component  $A$  is monodisperse, component  $B$  is polydisperse ( $PD = 4.00$ ), plotted as a function of the partial packing fractions,  $\eta_A$  and  $\eta_B$ . The interaction between components  $A$  and  $B$  is non-additive with a non-additivity parameter  $\Delta_{AB} = 0.10$ , the interaction between the sub-components  $B$  is non-additive, the non-additivity parameter  $\Delta_{B_a B_b}$  was varied from  $-0.1$  to  $0.1$  with a step size of  $0.05$  (the arrow indicates increasing  $\Delta_{B_a B_b}$ ). The spinodal (solid line) and binodal (dashed line) meet each other at the plait point (diamond), the three phase boundary is indicated with a dotted line



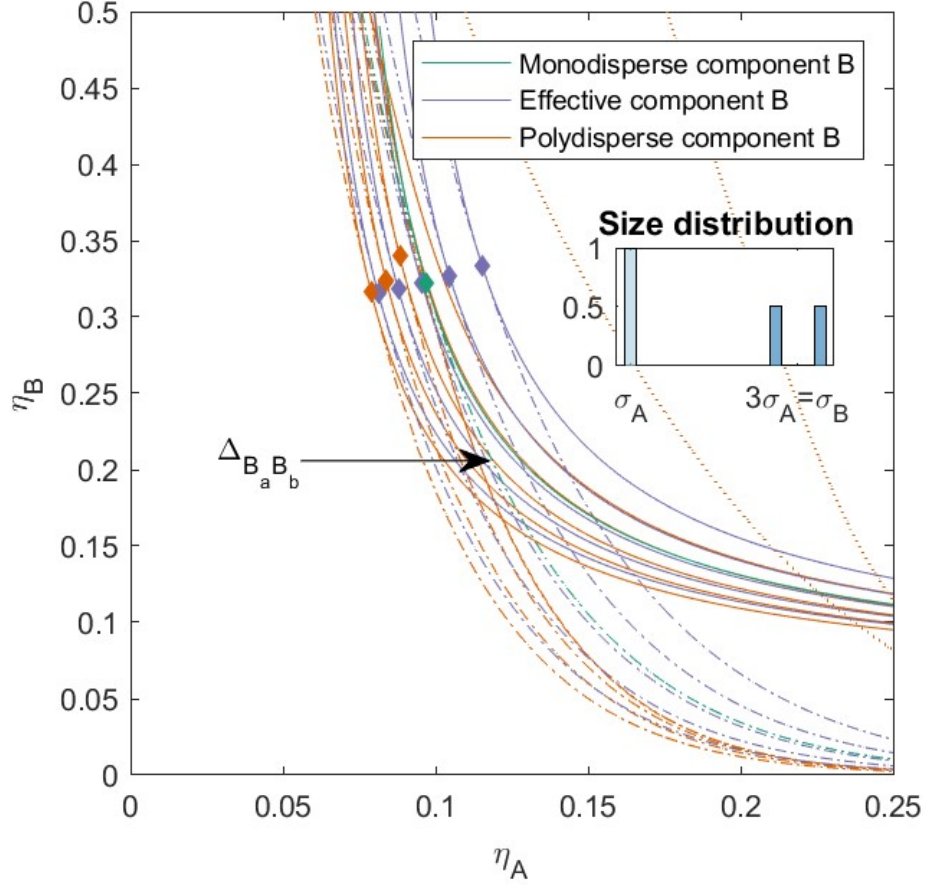


FIG. S 7. Phase diagram for binary (component  $A$  and  $B$ ) non-additive hard sphere mixture with size ratio  $q = \sigma_A/\sigma_B = 1/3$ , component  $A$  is monodisperse, component  $B$  is polydisperse ( $PD = 8.00$ ), plotted as a function of the partial packing fractions,  $\eta_A$  and  $\eta_B$ . The interaction between components  $A$  and  $B$  is non-additive with a non-additivity parameter  $\Delta_{AB} = 0.05$ , the interaction between the sub-components  $B$  is non-additive, the non-additivity parameter  $\Delta_{B_a B_b}$  was varied from  $-0.1$  to  $0.1$  with a step size of  $0.05$  (the arrow indicates increasing  $\Delta_{B_a B_b}$ ). The spinodal (solid line) and binodal (dashed line) meet each other at the plait point (diamond), the three phase boundary is indicated with a dotted line

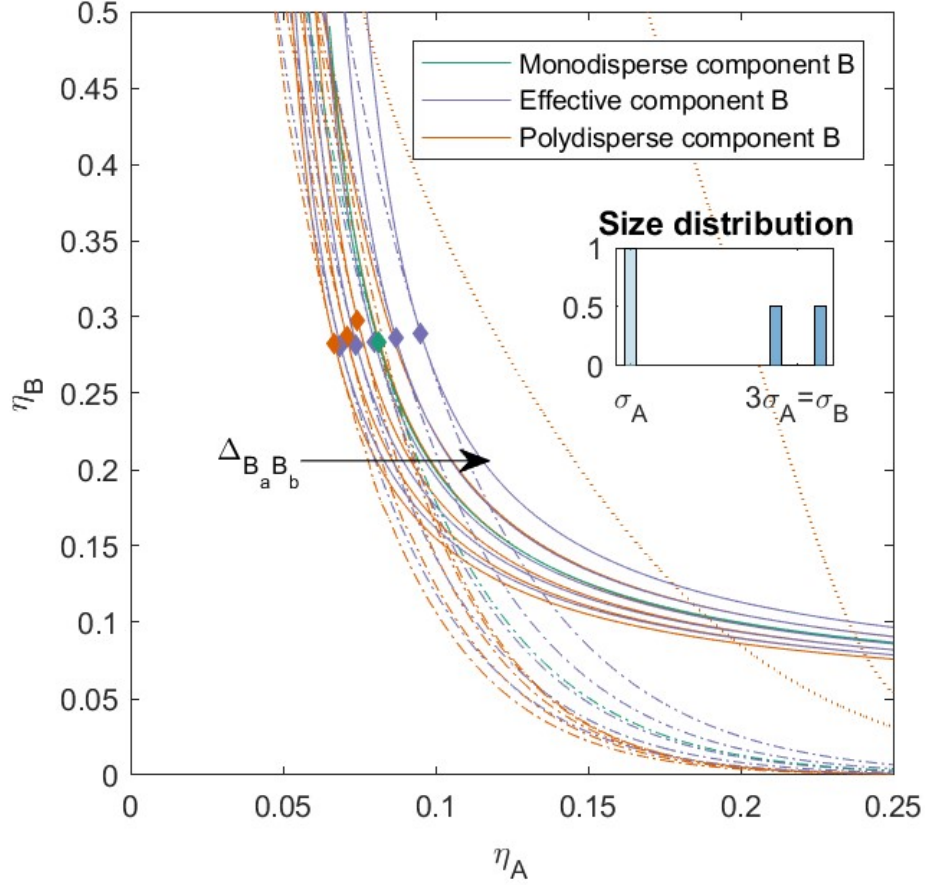


FIG. S 8. Phase diagram for binary (component  $A$  and  $B$ ) non-additive hard sphere mixture with size ratio  $q = \sigma_A/\sigma_B = 1/3$ , component  $A$  is monodisperse, component  $B$  is polydisperse ( $PD = 8.00$ ), plotted as a function of the partial packing fractions,  $\eta_A$  and  $\eta_B$ . The interaction between components  $A$  and  $B$  is non-additive with a non-additivity parameter  $\Delta_{AB} = 0.075$ , the interaction between the sub-components  $B$  is non-additive, the non-additivity parameter  $\Delta_{B_a B_b}$  was varied from  $-0.1$  to  $0.1$  with a step size of  $0.05$  (the arrow indicates increasing  $\Delta_{B_a B_b}$ ). The spinodal (solid line) and binodal (dashed line) meet each other at the plait point (diamond), the three phase boundary is indicated with a dotted line

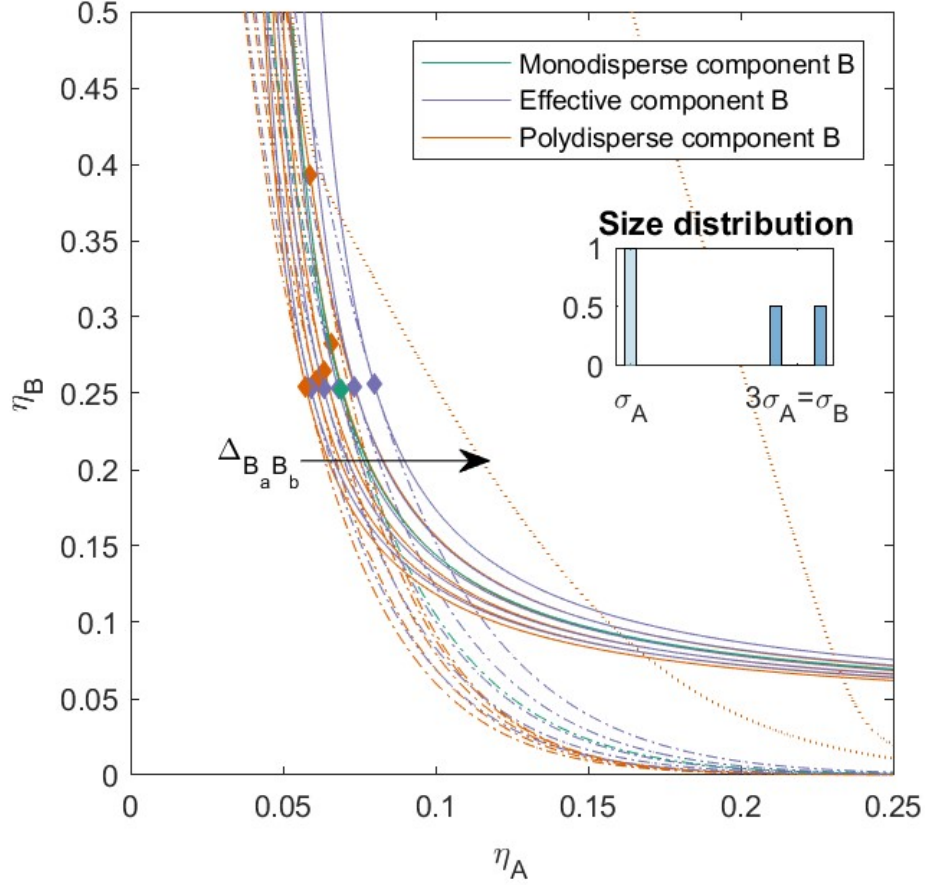


FIG. S 9. Phase diagram for binary (component  $A$  and  $B$ ) non-additive hard sphere mixture with size ratio  $q = \sigma_A/\sigma_B = 1/3$ , component  $A$  is monodisperse, component  $B$  is polydisperse ( $PD = 8.00$ ), plotted as a function of the partial packing fractions,  $\eta_A$  and  $\eta_B$ . The interaction between components  $A$  and  $B$  is non-additive with a non-additivity parameter  $\Delta_{AB} = 0.1$ , the interaction between the sub-components  $B$  is non-additive, the non-additivity parameter  $\Delta_{B_a B_b}$  was varied from  $-0.1$  to  $0.1$  with a step size of  $0.05$  (the arrow indicates increasing  $\Delta_{B_a B_b}$ ). The spinodal (solid line) and binodal (dashed line) meet each other at the plait point (diamond), the three phase boundary is indicated with a dotted line

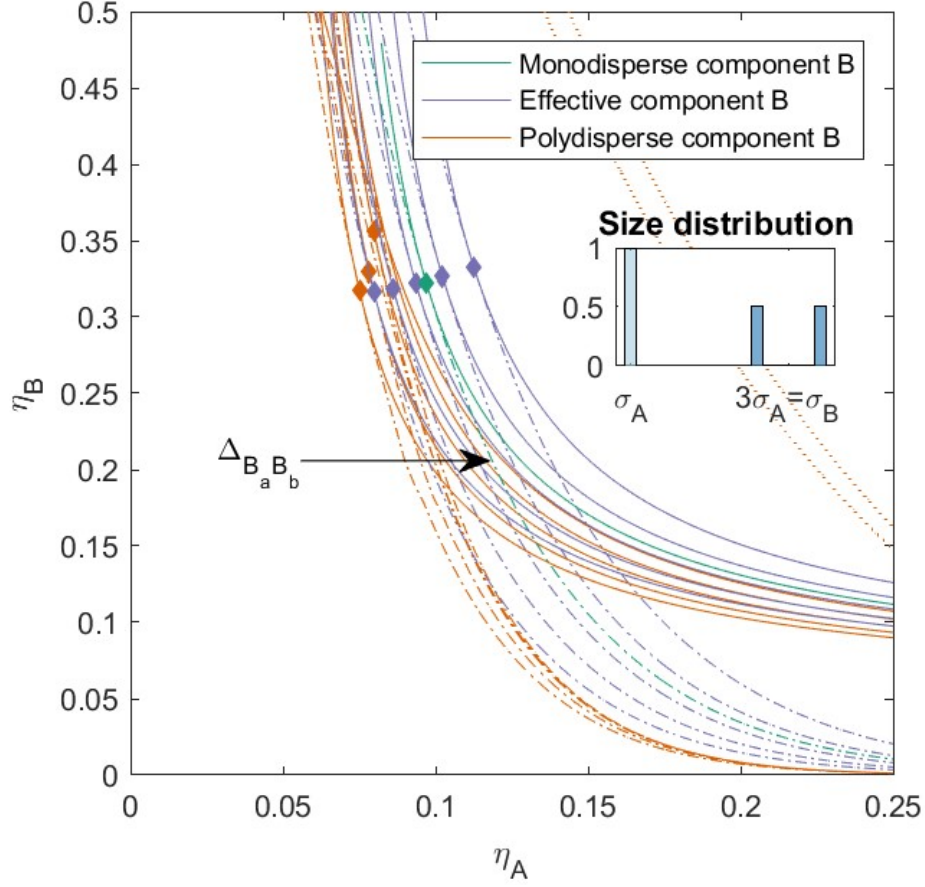


FIG. S 10. Phase diagram for binary (component  $A$  and  $B$ ) non-additive hard sphere mixture with size ratio  $q = \sigma_A/\sigma_B = 1/3$ , component  $A$  is monodisperse, component  $B$  is polydisperse ( $PD = 12.00$ ), plotted as a function of the partial packing fractions,  $\eta_A$  and  $\eta_B$ . The interaction between components  $A$  and  $B$  is non-additive with a non-additivity parameter  $\Delta_{AB} = 0.05$ , the interaction between the sub-components  $B$  is non-additive, the non-additivity parameter  $\Delta_{B_a B_b}$  was varied from  $-0.1$  to  $0.1$  with a step size of  $0.05$  (the arrow indicates increasing  $\Delta_{B_a B_b}$ ). The spinodal (solid line) and binodal (dashed line) meet each other at the plait point (diamond), the three phase boundary is indicated with a dotted line

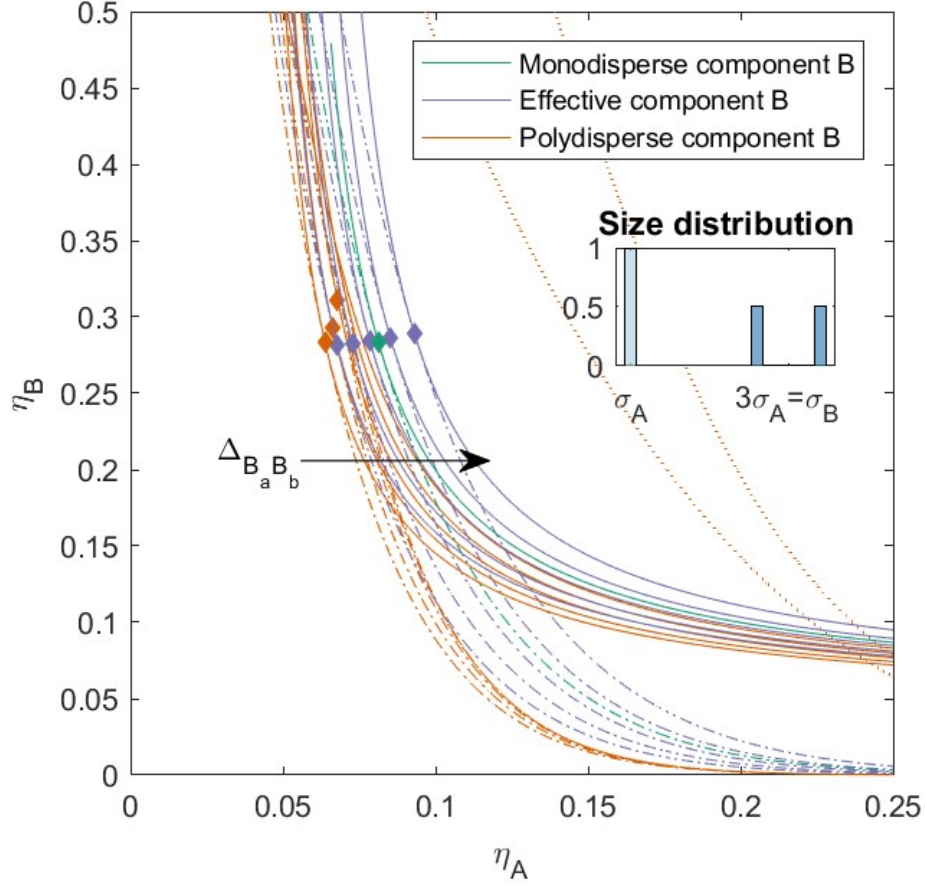


FIG. S 11. Phase diagram for binary (component  $A$  and  $B$ ) non-additive hard sphere mixture with size ratio  $q = \sigma_A/\sigma_B = 1/3$ , component  $A$  is monodisperse, component  $B$  is polydisperse ( $PD = 12.00$ ), plotted as a function of the partial packing fractions,  $\eta_A$  and  $\eta_B$ . The interaction between components  $A$  and  $B$  is non-additive with a non-additivity parameter  $\Delta_{AB} = 0.075$ , the interaction between the sub-components  $B$  is non-additive, the non-additivity parameter  $\Delta_{B_a B_b}$  was varied from  $-0.1$  to  $0.1$  with a step size of  $0.05$  (the arrow indicates increasing  $\Delta_{B_a B_b}$ ). The spinodal (solid line) and binodal (dashed line) meet each other at the plait point (diamond), the three phase boundary is indicated with a dotted line

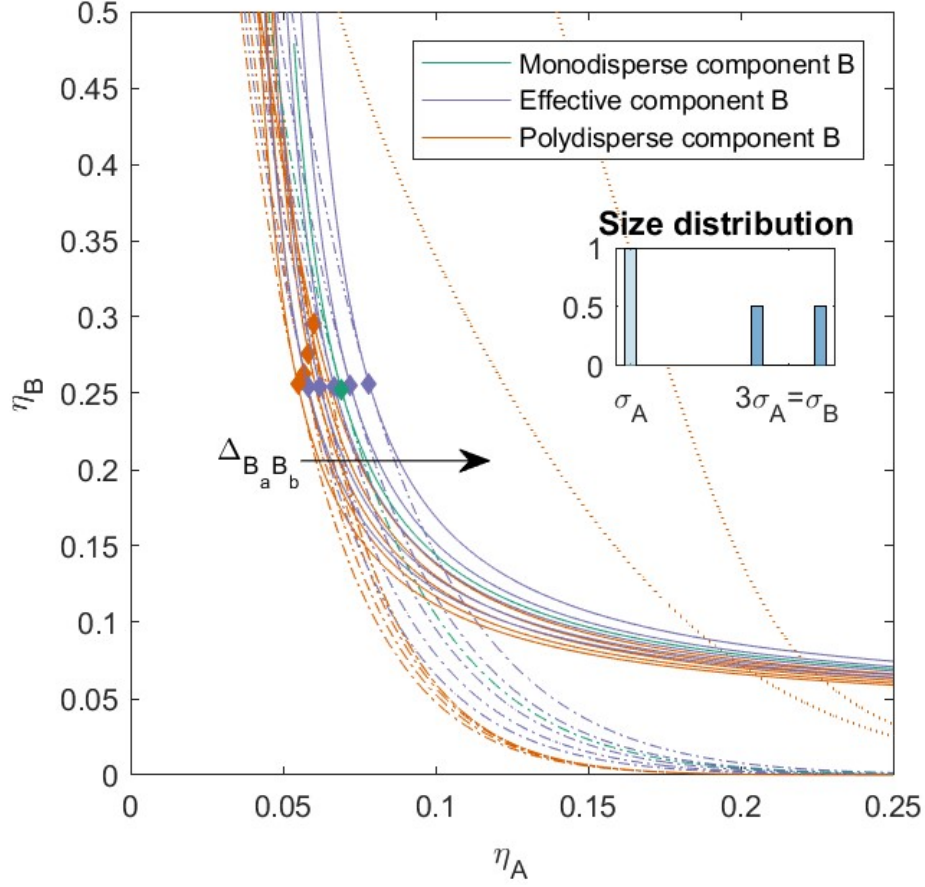


FIG. S 12. Phase diagram for binary (component  $A$  and  $B$ ) non-additive hard sphere mixture with size ratio  $q = \sigma_A/\sigma_B = 1/3$ , component  $A$  is monodisperse, component  $B$  is polydisperse ( $PD = 12.00$ ), plotted as a function of the partial packing fractions,  $\eta_A$  and  $\eta_B$ . The interaction between components  $A$  and  $B$  is non-additive with a non-additivity parameter  $\Delta_{AB} = 0.1$ , the interaction between the sub-components  $B$  is non-additive, the non-additivity parameter  $\Delta_{B_a B_b}$  was varied from  $-0.1$  to  $0.1$  with a step size of  $0.05$  (the arrow indicates increasing  $\Delta_{B_a B_b}$ ). The spinodal (solid line) and binodal (dashed line) meet each other at the plait point (diamond), the three phase boundary is indicated with a dotted line

## II. FRACTIONATION

Table S I. Critical points for the different binary mixtures depending on the non-additivity of component  $B$ , and phase separated concentrations and fractionation of the different mixtures for specific parent concentration ( $\eta_{A_{parent}} = 0.010, \eta_{B_{parent}} = 0.200$ ), depending on the non-additivity of component  $B$ ,  $PD = 8.00$

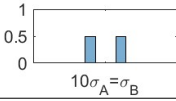
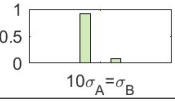
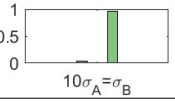
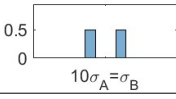
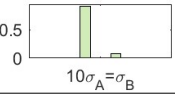
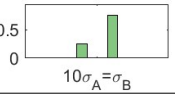
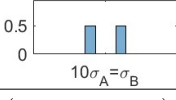
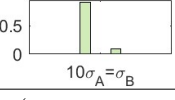
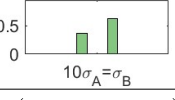
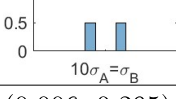
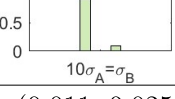
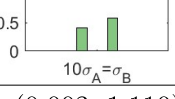
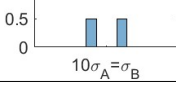
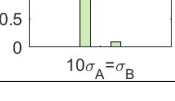
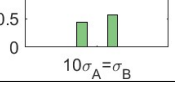
$\Delta_{B_a B_b}$	$\eta_{crit}$	Top phase	Bottom phase
0.100	-	$\eta$ (0.011, 0.092) PD: 4.65, Size: 0.93, PD: 3.10, Size: 1.07, $\alpha : 0.903$	$\eta$ (0.003, 1.206) $\alpha : 0.097$
			
0.05	(0.006, 0.376)	$\eta$ (0.011, 0.070) PD: 4.77, Size: 0.93, PD: 6.63, Size: 1.04, $\alpha : 0.865$	$\eta$ (0.003, 1.032) $\alpha : 0.135$
			
0	(0.006, 0.314)	$\eta$ (0.011, 0.045) PD: 4.86, Size: 0.93, PD: 7.58, Size: 1.02, $\alpha : 0.837$	$\eta$ (0.003, 0.994) $\alpha : 0.163$
			
-0.05	(0.006, 0.300)	$\eta$ (0.011, 0.033) PD: 4.86, Size: 0.93, PD: 7.78, Size: 1.01, $\alpha : 0.835$	$\eta$ (0.003, 1.043) $\alpha : 0.165$
			
-0.1	(0.006, 0.295)	$\eta$ (0.011, 0.025) PD: 4.84, Size: 0.93, PD: 7.86, Size: 1.01, $\alpha : 0.839$	$\eta$ (0.003, 1.110) $\alpha : 0.161$
			



Table S II. Critical points for the different binary mixtures depending on the non-additivity of component  $B$ , and phase separated concentrations and volume fraction  $\alpha$  of the different mixtures for specific parent concentration ( $\eta_{A_{parent}} = 0.010, \eta_{B_{parent}} = 0.200$ ), depending on the non-additivity of component  $B$ ,  $PD = 12.00$

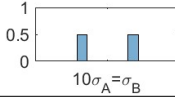
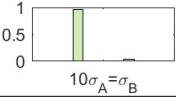
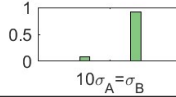
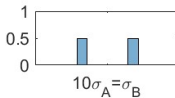
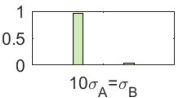
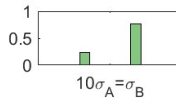
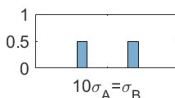
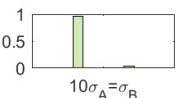
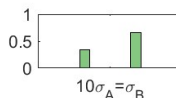
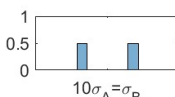
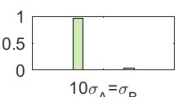
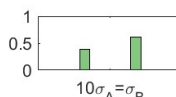
$\Delta_{B_a B_b}$	$\eta_{crit}$	Top phase	Bottom phase	
0.05	-	$\eta$ (0.011, 0.071) PD: 4.80, Size: 0.89, PD: 6.08, Size: 1.10, $\alpha : 0.897$	$\eta$ (0.002, 1.319) $\alpha : 0.103$	
				
0	(0.005, 0.359)	$\eta$ (0.011, 0.056) PD: 4.84, Size: 0.89, PD: 9.58, Size: 1.06, $\alpha : 0.875$	$\eta$ (0.003, 1.210) $\alpha : 0.125$	
				
-0.05	(0.005, 0.322)	$\eta$ (0.011, 0.041) PD: 4.80, Size: 0.89, PD: 10.90, Size: 1.04, $\alpha : 0.861$	$\eta$ (0.003, 1.184) $\alpha : 0.139$	
				
-0.1	(0.005, 0.308)	$\eta$ (0.011, 0.031) PD: 4.73, Size: 0.89, PD: 11.37, Size: 1.03, $\alpha : 0.857$	$\eta$ (0.003, 1.214) $\alpha : 0.143$	
				



Table S III. Critical points for the different binary mixtures depending on the non-additivity of component  $B$ , and phase separated concentrations and volume fraction  $\alpha$  of the different mixtures for specific parent concentration ( $\eta_{A_{parent}} = 0.010, \eta_{B_{parent}} = 0.200$ ), depending on the non-additivity of component  $B$ ,  $PD = 6.93$

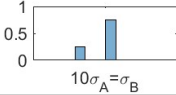
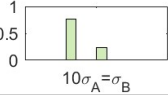
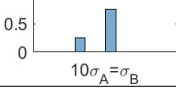
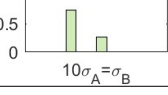
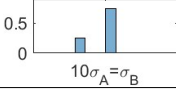
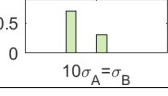
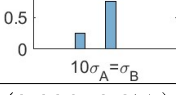
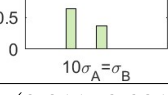
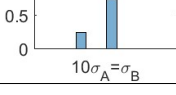
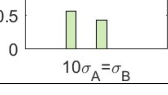
$\Delta_{B_a B_b}$	$\eta_{crit}$	Top phase	Bottom phase
0.100	(0.006, 0.374)	$\eta$ (0.011, 0.055) PD: 7.41, Size: 0.92, PD: 2.55, Size: 1.04, $\alpha : 0.850$	$\eta$ (0.003, 1.024) $\alpha : 0.159$
			
0.05	(0.006, 0.314)	$\eta$ (0.011, 0.048) PD: 7.62, Size: 0.92, PD: 4.28, Size: 1.03, $\alpha : 0.837$	$\eta$ (0.004, 0.978) $\alpha : 0.163$
			
0	(0.006, 0.290)	$\eta$ (0.011, 0.037) PD: 7.92, Size: 0.93, PD: 5.57, Size: 1.02, $\alpha : 0.822$	$\eta$ (0.004, 0.951) $\alpha : 0.178$
			
-0.05	(0.006, 0.279)	$\eta$ (0.011, 0.028) PD: 8.20, Size: 0.94, PD: 6.21, Size: 1.01, $\alpha : 0.816$	$\eta$ (0.004, 0.967) $\alpha : 0.184$
			
-0.1	(0.006, 0.277)	$\eta$ (0.011, 0.021) PD: 8.35, Size: 0.95, PD: 6.53, Size: 1.01, $\alpha : 0.818$	$\eta$ (0.003, 1.002) $\alpha : 0.182$
			

Table S IV. Critical points for the different binary mixtures depending on the non-additivity of component  $B$ , and phase separated concentrations and volume fraction  $\alpha$  of the different mixtures for specific parent concentration ( $\eta_{A_{parent}} = 0.010, \eta_{B_{parent}} = 0.200$ ), depending on the non-additivity of component  $B$ ,  $PD = 6.93$

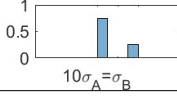
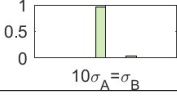
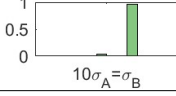
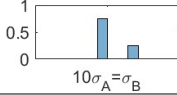
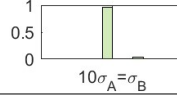
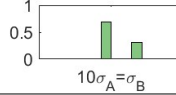
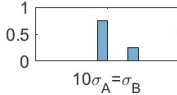
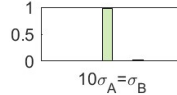
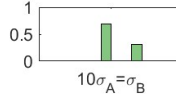
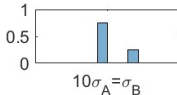
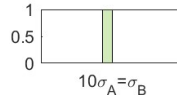
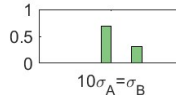
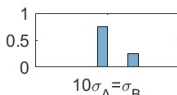
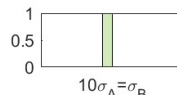
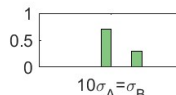
$\Delta_{B_a B_b}$	$\eta_{crit}$	Top phase	Middle phase	Bottom phase
0.100	-	$\eta$ (0.011, 0.065) PD: 3.05, Size: 0.97, $\alpha : 0.819$	$\eta$ (0.005, 0.643) PD: 4.43, Size: 0.97, $\alpha : 0.097$	$\eta$ (0.002, 1.376) PD: 2.88, Size: 1.11, $\alpha : 0.04$
				
0.05	(0.006, 0.325)	$\eta$ (0.011, 0.050) PD: 2.96, Size: 0.97, $\alpha : 0.813$		$\eta$ (0.004, 0.854) PD: 7.35, Size: 1.01, $\alpha : 0.187$
				
0	(0.006, 0.326)	$\eta$ (0.011, 0.044) PD: 2.36, Size: 0.96, $\alpha : 0.826$		$\eta$ (0.004, 0.941) PD: 7.33, Size: 1.01, $\alpha : 0.174$
				
-0.05	(0.006, 0.331)	$\eta$ (0.011, 0.040) PD: 1.84, Size: 0.96, $\alpha : 0.837$		$\eta$ (0.003, 1.025) PD: 7.31, Size: 1.01, $\alpha : 0.163$
				
-0.1	(0.005, 0.337)	$\eta$ (0.011, 0.037) PD: 1.42, Size: 0.96, $\alpha : 0.848$		$\eta$ (0.003, 1.106) PD: 7.29, Size: 1.01, $\alpha : 0.142$
				

Table S V. Critical points for the different binary mixtures depending on the non-additivity of component  $B$ , and phase separated concentrations and volume fraction  $\alpha$  of the different mixtures for specific parent concentration ( $\eta_{A_{parent}} = 0.010, \eta_{B_{parent}} = 0.200$ ), depending on the non-additivity of component  $B$ ,  $PD = 4.80$

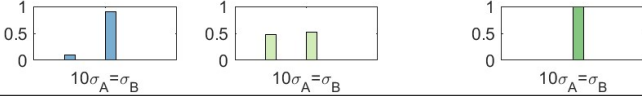
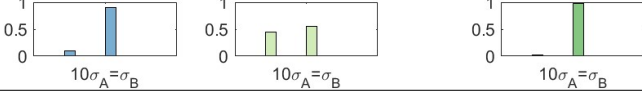
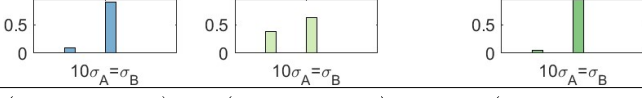
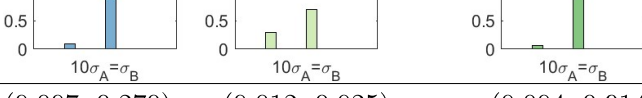
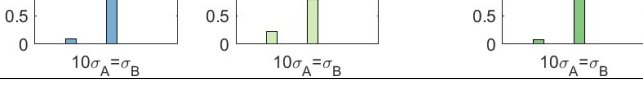
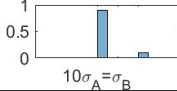
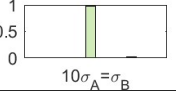
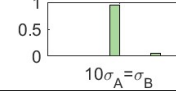
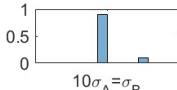
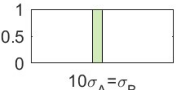
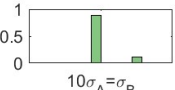
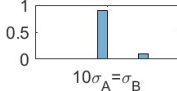
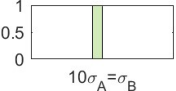
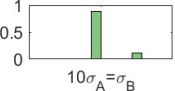
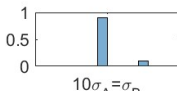
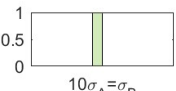
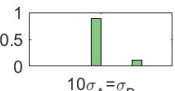
$\Delta_{B_a B_b}$	$\eta_{crit}$	Top phase	Bottom phase
0.100	(0.007, 0.295)	$\eta$ (0.011, 0.039) PD: 8.51, Size: 0.94, PD: 1.77, Size: 1.01, $\alpha : 0.817$	$\eta$ (0.004, 0.918) $\alpha : 0.183$
			
0.05	(0.007, 0.284)	$\eta$ (0.011, 0.036) PD: 8.40, Size: 0.95, PD: 2.69, Size: 1.01, $\alpha : 0.811$	$\eta$ (0.004, 0.904) $\alpha : 0.189$
			
0	(0.007, 0.276)	$\eta$ (0.011, 0.032) PD: 8.12, Size: 0.96, PD: 3.53, Size: 1.01, $\alpha : 0.805$	$\eta$ (0.004, 0.895) $\alpha : 0.195$
			
-0.05	(0.007, 0.271)	$\eta$ (0.012, 0.028) PD: 7.58, Size: 0.97, PD: 4.11, Size: 1.00, $\alpha : 0.803$	$\eta$ (0.004, 0.899) $\alpha : 0.197$
			
-0.1	(0.007, 0.270)	$\eta$ (0.012, 0.025) PD: 6.79, Size: 0.98, PD: 4.46, Size: 1.00, $\alpha : 0.803$	$\eta$ (0.004, 0.914) $\alpha : 0.197$
			

Table S VI. Critical points for the different binary mixtures depending on the non-additivity of component  $B$ , and phase separated concentrations and volume fraction  $\alpha$  of the different mixtures for specific parent concentration ( $\eta_{A_{parent}} = 0.010, \eta_{B_{parent}} = 0.200$ ), depending on the non-additivity of component  $B$ ,  $PD = 4.80$

$\Delta_{B_a B_b}$	$\eta_{crit}$	Top phase	Middle phase	Bottom phase
0.100	(0.007, 0.262)	$\eta$ (0.011, 0.040) PD: 2.47, Size: 0.99, $\alpha : 0.791$	$\eta$ (0.005, 0.767) PD: 3.71, Size: 0.99, $\alpha : 0.198$	$\eta$ (0.002, 1.472) PD: 2.57, Size: 1.14, $\alpha : 0.011$
				
0.05	(0.007, 0.279)	$\eta$ (0.011, 0.037) PD: 1.90, Size: 0.99, $\alpha : 0.795$		$\eta$ (0.004, 0.832) PD: 5.10, Size: 1.00, $\alpha : 0.205$
				
0	(0.006, 0.304)	$\eta$ (0.011, 0.036) PD: 1.20, Size: 0.98, $\alpha : 0.807$		$\eta$ (0.004, 0.885) PD: 5.13, Size: 1.00, $\alpha : 0.193$
				
-0.05	(0.006, 0.335)	$\eta$ (0.011, 0.036) PD: 0.75, Size: 0.98, $\alpha : 0.818$		$\eta$ (0.004, 0.935) PD: 5.15, Size: 1.00, $\alpha : 0.182$
				
-0.1	(0.006, 0.369)	$\eta$ (0.011, 0.037) PD: 0.47, Size: 0.98, $\alpha : 0.828$		$\eta$ (0.003, 0.982) PD: 5.17, Size: 1.00, $\alpha : 0.172$
		