

# Configurational Entropy of Folded Proteins and Its Importance for Intrinsically Disordered Proteins

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**Table S1.** Measures of similarity and dissimilarity of folded protein ensembles generated by non-polarizable and polarizable force fields. The similarity/dissimilarity metric and scaling law parameters are reported in Table S2. The  $\langle \text{RMSD} \rangle$  and  $\langle R_g \rangle$  are collected over 1  $\mu\text{s}$  simulation timescales. Proteins characterized are 1ARB [1], 1B6B [2], 1BSG [3], 1RII [4] 4XQ4 [5], 4R3F [6], and 2XR6 [7].

Protein (size)	1bsg (266 aa)	1arb (263 aa)	1rii (243 aa)	4r3f (196 aa)	4xq4 (188 aa)	1b6b (168 aa)	2xr6 (130 aa)
<b>Similarity and Dissimilarity Metric (<math>\text{\AA}</math>)</b>							
$D_{0,sim}$	6.16	6.11	5.80	5.00	4.86	4.47	3.63
$D_{0,dis}$	10.63	10.58	10.19	9.17	8.98	8.48	7.42
<b>Force Field/Protein</b>	<b><math>\langle \text{RMSD} \rangle \pm \langle \delta \text{RMSD} \rangle</math> (<math>\text{\AA}</math>)</b>						
ff99sb/TIP3P	$1.5 \pm 0.28$	$1.0 \pm 0.15$	$2.1 \pm 0.24$	$1.2 \pm 0.13$	$1.4 \pm 0.26$	$2.8 \pm 0.19$	$2.1 \pm 0.30$
ff99sb/TIP4P-Ew	$1.5 \pm 0.16$	$1.5 \pm 0.18$	$1.9 \pm 0.18$	$1.2 \pm 0.20$	$1.6 \pm 0.59$	$3.2 \pm 0.30$	$2.3 \pm 0.27$
C36m/TIP3P	$1.5 \pm 0.16$	$2.1 \pm 0.26$	$1.8 \pm 0.25$	$1.3 \pm 0.17$	$2.4 \pm 0.49$	$4.0 \pm 0.44$	$2.4 \pm 0.33$
C36m/TIP3Pm	$1.1 \pm 0.12$	$1.9 \pm 0.50$	$1.8 \pm 0.23$	$1.6 \pm 0.15$	$1.4 \pm 0.14$	$3.7 \pm 0.56$	$2.6 \pm 0.32$
AmPro13/AmW03	$3.3 \pm 0.77$	$3.1 \pm 0.56$	$4.9 \pm 0.70$	$1.5 \pm 0.39$	$4.1 \pm 0.53$	$5.9 \pm 0.28$	$2.6 \pm 0.20$
<b><math>R_g</math> Measures (<math>\text{\AA}</math>)</b>							
PDB	17.4	16.5	17.1	15.8	15.1	14.9	13.5
Scaling laws [8,9]	$18.9 \pm 0.4$	$18.7 \pm 0.4$	$18.2 \pm 0.5$	$16.8 \pm 0.5$	$16.6 \pm 0.5$	$16.0 \pm 0.5$	$14.6 \pm 0.6$
<b>Force Field/Protein</b>	<b><math>\langle R_g \rangle</math> (<math>\text{\AA}</math>)</b>						
ff99sb/TIP3P	$18.4 \pm 0.1$	$16.8 \pm 0.0$	$17.6 \pm 0.1$	$16.3 \pm 0.1$	$15.5 \pm 0.1$	$15.5 \pm 0.1$	$14.2 \pm 0.1$
ff99sb/TIP4P-Ew	$18.2 \pm 0.1$	$16.8 \pm 0.1$	$17.6 \pm 0.1$	$16.4 \pm 0.1$	$15.6 \pm 0.2$	$15.5 \pm 0.0$	$14.3 \pm 0.1$
C36m/TIP3P	$18.1 \pm 0.1$	$17.1 \pm 0.1$	$17.6 \pm 0.1$	$16.3 \pm 0.1$	$15.9 \pm 0.1$	$15.7 \pm 0.2$	$14.4 \pm 0.1$
C36m/TIP3Pm	$18.1 \pm 0.6$	$17.1 \pm 0.1$	$17.6 \pm 0.6$	$16.4 \pm 0.1$	$15.5 \pm 0.1$	$15.7 \pm 0.5$	$14.4 \pm 0.3$
AmPro13/AmW03	$18.8 \pm 0.5$	$17.2 \pm 0.1$	$18.7 \pm 0.6$	$16.5 \pm 1.3$	$16.3 \pm 0.1$	$15.6 \pm 0.1$	$14.3 \pm 0.1$

**Table S2.** Scaling Law Relationships used for folded states. The structural similarity  $D_{0,sim}$  and dissimilarity  $D_{0,dis}$  for globular proteins are from Maiorov and Crippen [10]. The  $R_g$  are measured from scaling laws derived over folded proteins in the PDB [8,9].

Scaling Law	a	b	c
$D_{0,sim} = a + bN^c$ folded states	-5.74	1.85	1/3
$D_{0,dis} = a + bN^c$ folded states	-4.54	2.36	1/3
$R_g = a + bN^c$ folded states	0.0	2.2	0.38
$R_g = a + bN^c$ folded states	0.0	3.0	1/3

**Table S3.** Average root mean square fluctuation around average simulated structure ( $\langle \text{RMSF} \rangle$ ).

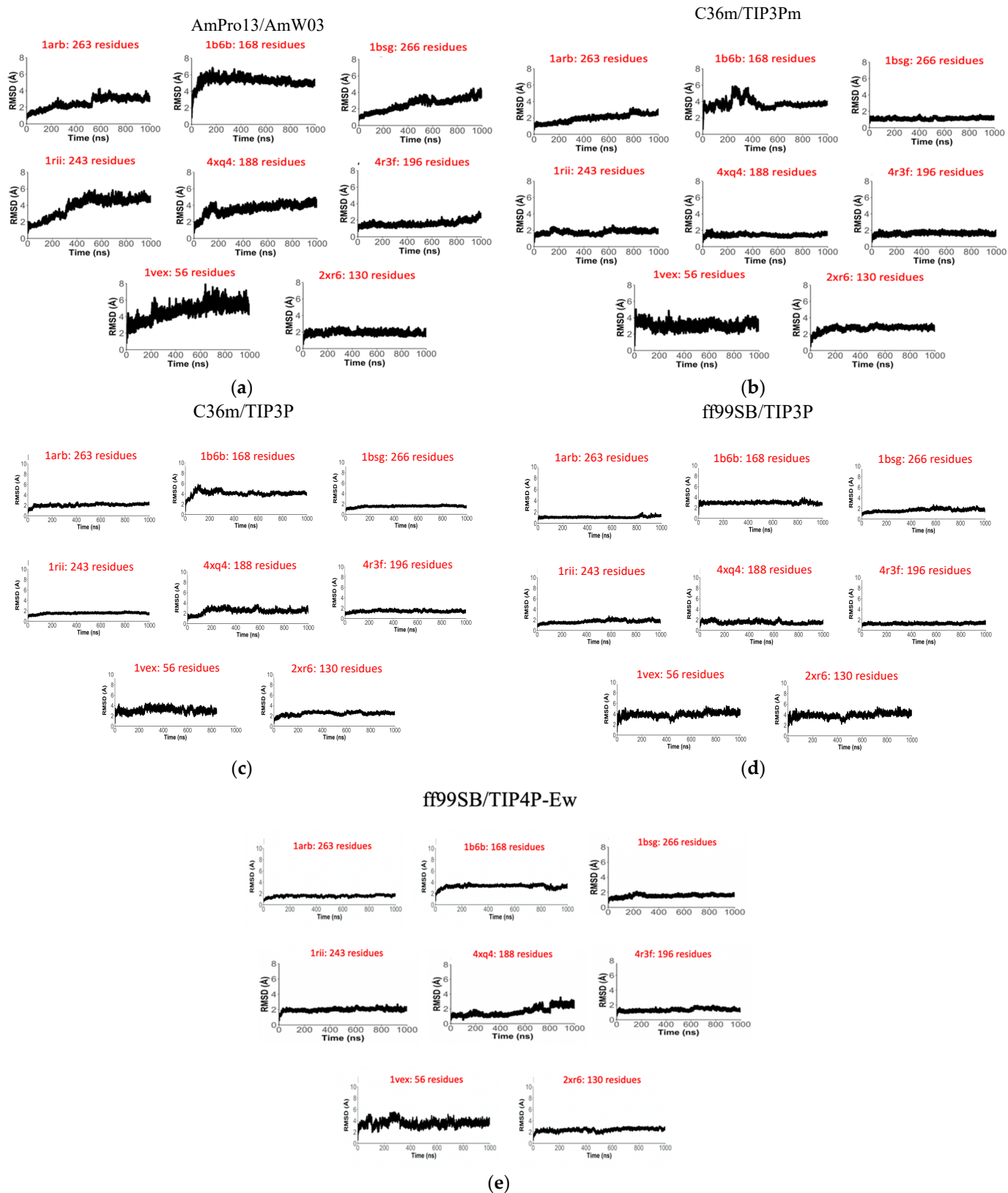
Protein/Force Field	$\langle \text{RMSF} (\text{\AA}) \rangle$						
	1bsg (266 aa)	1arb (263 aa)	1rii (243 aa)	4r3f (196 aa)	4xq4 (188 aa)	1b6b (168 aa)	2xr6 (130 aa)
ff99sb/TIP3P	0.60	0.43	0.58	0.47	0.54	0.62	0.47
ff99sb/TIP4P-Ew	0.52	0.46	0.54	0.53	0.50	0.58	0.47
C36m/TIP3P	0.47	0.50	0.51	0.53	0.61	0.61	0.49
C36m/TIP3Pm	0.46	0.54	0.55	0.51	0.53	0.80	0.63
AmPro13/AmW03	0.81	0.59	0.95	0.68	0.75	0.70	0.58

**Table S4.** Lindemann criteria for core and surface residues. Core residues are defined as residues with C-alpha atoms within  $0.5 \cdot R_g$  of the center residue in the crystal structure. Surface residues are all protein residues not characterized as core residues. A value of  $a = 4.375 \text{\AA}$  was used to calculate the Lindemann Criteria.

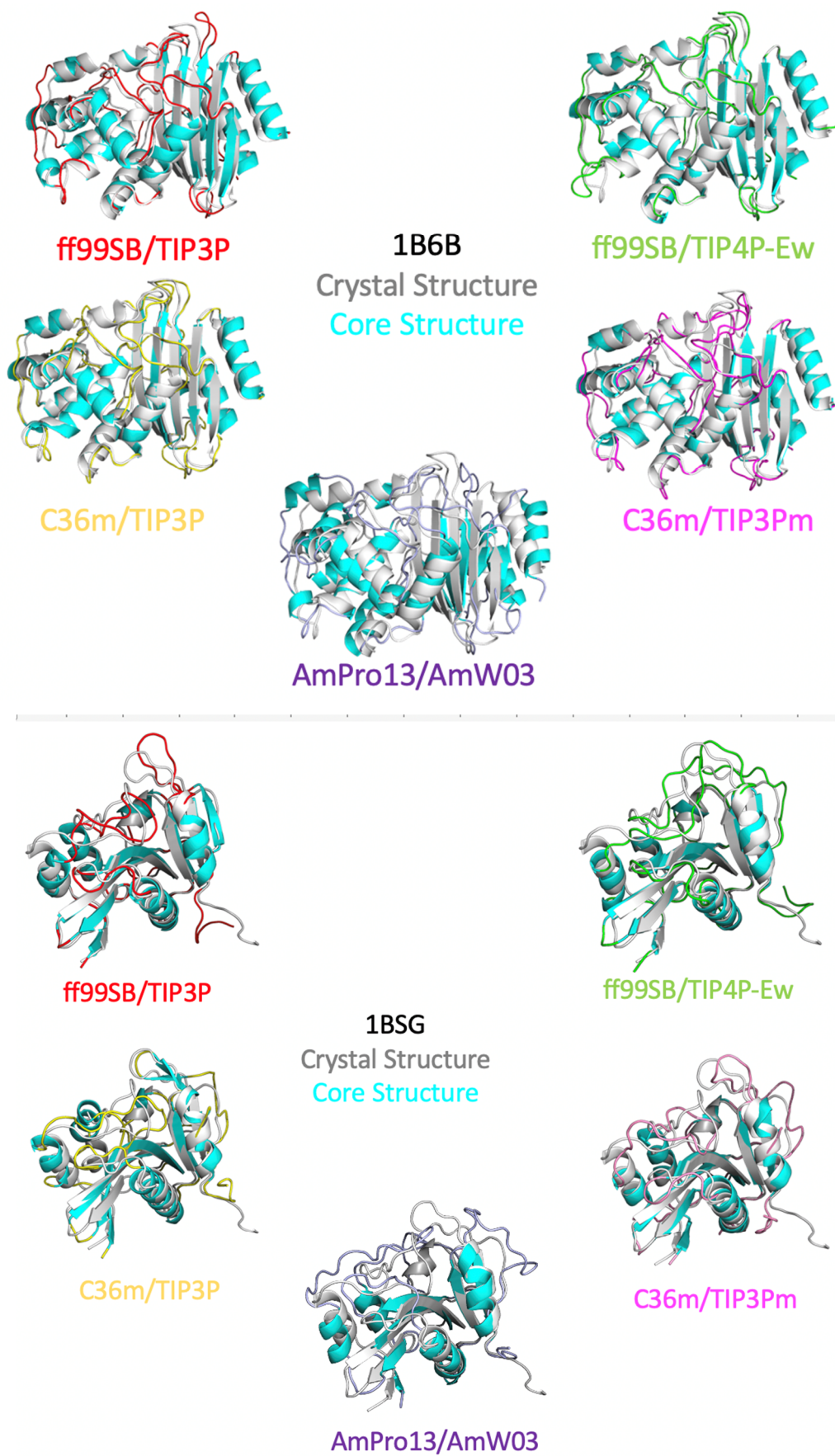
$\Delta_l^{sim} (300 \text{ K}) \text{ Core}$								
Force Field/Protein	1bsg	1arb	1rii	4r3f	4xq4	1b6b	2xr6	Average
ff99sb/TIP3P	0.11	0.07	0.10	0.08	0.08	0.09	0.08	0.09
ff99sb/TIP4P-Ew	0.09	0.08	0.09	0.09	0.08	0.09	0.08	0.09
C36m/TIP3P	0.09	0.08	0.08	0.09	0.11	0.10	0.08	0.09
C36m/TIP3Pm	0.09	0.10	0.09	0.08	0.08	0.13	0.09	0.09
AmPro13/AmW03	0.16	0.09	0.17	0.12	0.11	0.11	0.09	0.12
$\Delta_l^{sim} (300 \text{ K}) \text{ Surface}$								
Force Field/Protein	1bsg	1arb	1rii	4r3f	4xq4	1b6b	2xr6	Average
ff99sb/TIP3P	0.16	0.12	0.17	0.13	0.16	0.19	0.14	0.15
ff99sb/TIP4P-Ew	0.15	0.13	0.16	0.15	0.13	0.17	0.13	0.15
C36m/TIP3P	0.13	0.15	0.15	0.16	0.17	0.18	0.15	0.16
C36m/TIP3Pm	0.11	0.15	0.16	0.15	0.16	0.17	0.19	0.16
AmPro13/AmW03	0.21	0.18	0.27	0.19	0.23	0.20	0.18	0.21

**Table S5.** Percentage of  $\alpha$ -helix as a function of temperature for the  $(\text{AAQAA})_3$  peptide using the sequential definition. The  $\alpha$ -helix percentage is defined as 3 consecutive residues within the  $\alpha$ -helix basin as described in Methods [11]. Aggregate simulation timescales for each non-polarizable force field is  $1.0 \mu\text{s}$  for 300 K and 320 K, and  $0.5 \mu\text{s}$  for 340 K, 360 K, and 380 K. For the polarizable model we simulated for  $0.5 \mu\text{s}$  for all temperatures. All simulations started from a folded  $\alpha$ -helix.

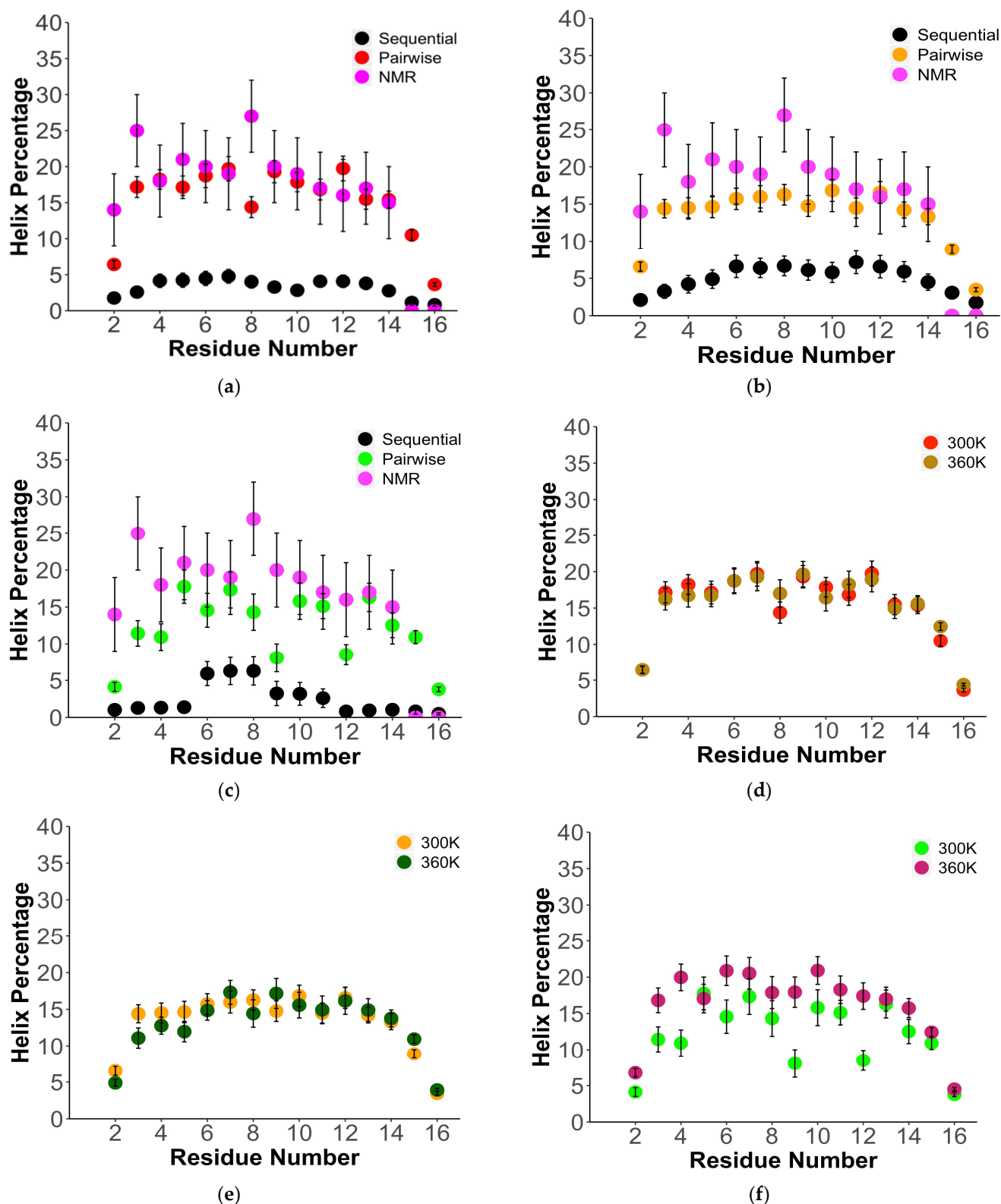
Force Field/Temp	300 K	320 K	340 K	360 K	380 K
C36/TIP3Pm	4.98 (0.74)	4.01 (0.51)	3.28 (0.63)	3.72 (0.90)	4.75 (0.81)
C36m/TIP3Pm	4.70 (0.61)	4.11 (0.57)	4.60 (0.80)	4.97 (1.14)	5.31 (1.05)
ff99SB/TIP4P-Ew	3.25 (0.42)	2.64 (0.30)	2.92 (0.44)	2.77 (0.39)	2.69 (0.41)
ff99SB-ildn/TIP4P-D	2.44 (0.65)	3.75 (0.75)	2.80 (0.59)	4.15 (1.03)	2.89 (0.43)
AmPro13/AmW03	3.71 (1.55)	3.32 (1.04)	2.59 (1.59)	1.85 (0.98)	1.12 (0.52)



**Figure S1.** Protein RMSD when simulated with polarizable and non-polarizable force fields. Root mean square deviation (RMSD) vs. simulation time for 1  $\mu$ s MD simulations for (a) AmPro13/AmW03, (b) C36m/TIP3Pm, (c) C36m/TIP3P, (d) ff99SB/TIP3P, (e) ff99SB/TIP4P-Ew. Proteins characterized are 1ARB [1], 1B6B [2], 1BSG [3], 1RII [4], 4XQ4 [5], 4R3F [6], 1VEX [12] and 2XR6 [7].



**Figure S2.** Comparison of core structure and loop restructuring of the simulated force fields against the crystal structure for 1B6B [2] and 1BSG [3].



**Figure S3.** Structural properties for (AAQAA)<sub>3</sub> of other non-polarizable force fields. Comparison of estimated helical propensities from simulation assuming 3 sequential residues (black) vs average over any presence of  $\alpha$ -helix,  $\pi$ -helix, and  $3_{10}$  helix for all force fields at 300 K compared to NMR estimates (pink). In the SI we consider not only ff99SB/TIP4P-Ew, but other force fields not considered in the main study including C36/TIP3Pm and ff99SB-ildn/TIP4P-D to validate TCW. Comparison of helix definitions for (a) ff99SB/TIP4P-Ew (red), (b) C36/TIP3Pm (orange), and (c) ff99SB-ildn/TIP4P-D (green). Comparison of two temperatures of 300 K and 360 K for average presence of  $\alpha$ -helix,  $\pi$ -helix, and  $3_{10}$  helix for (d) ff99SB/TIP4P-Ew, (e) C36/TIP3Pm, and (f) ff99SB-ildn/TIP4P-D. See main text and Figure 4 caption for definitions.

## References

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