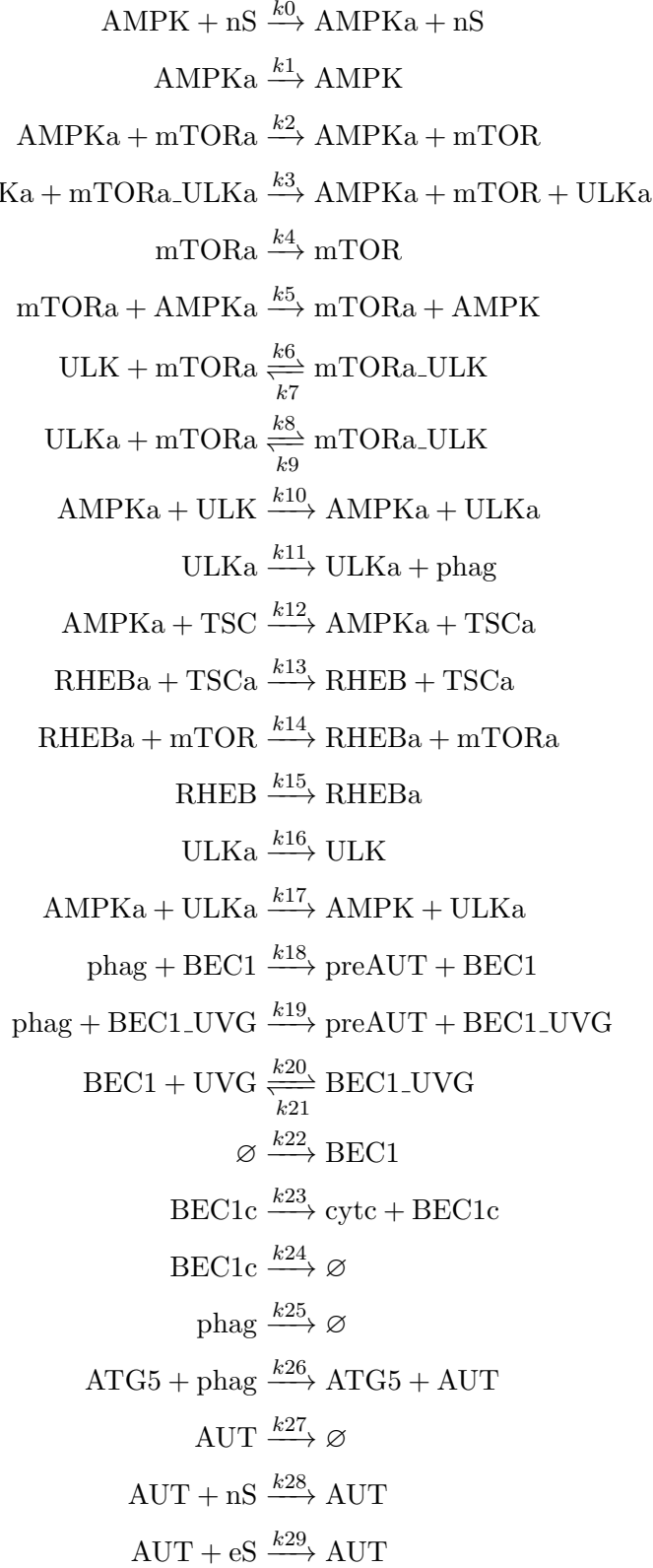
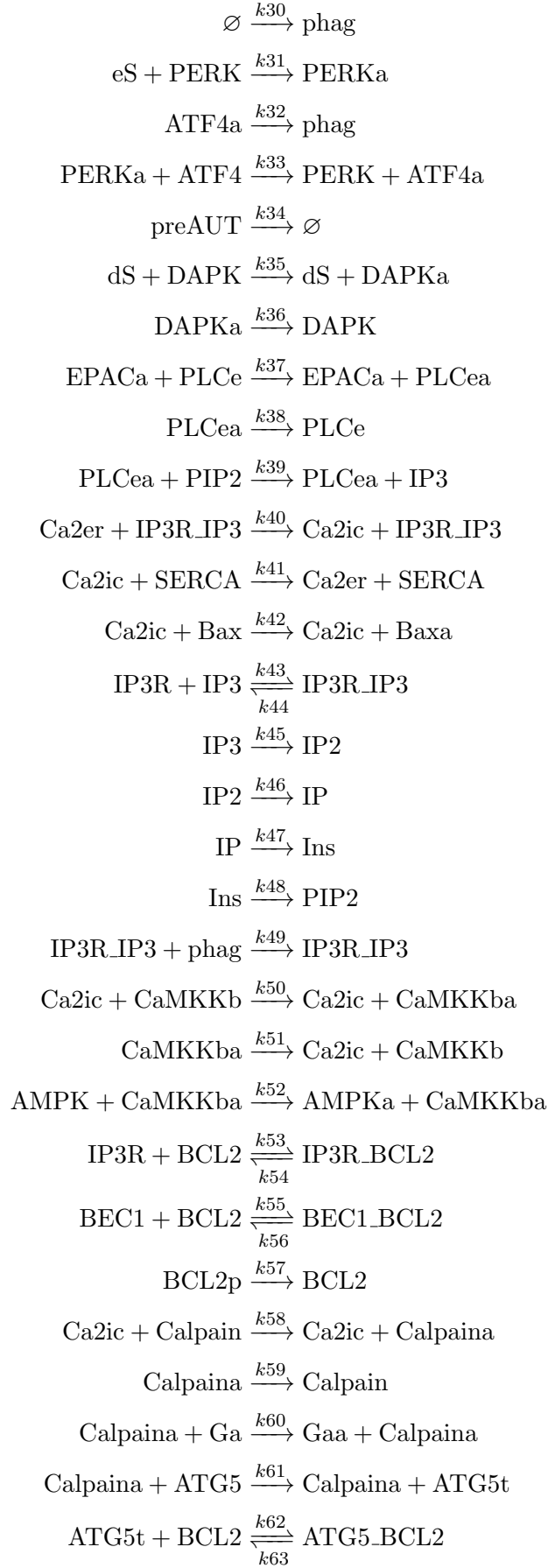
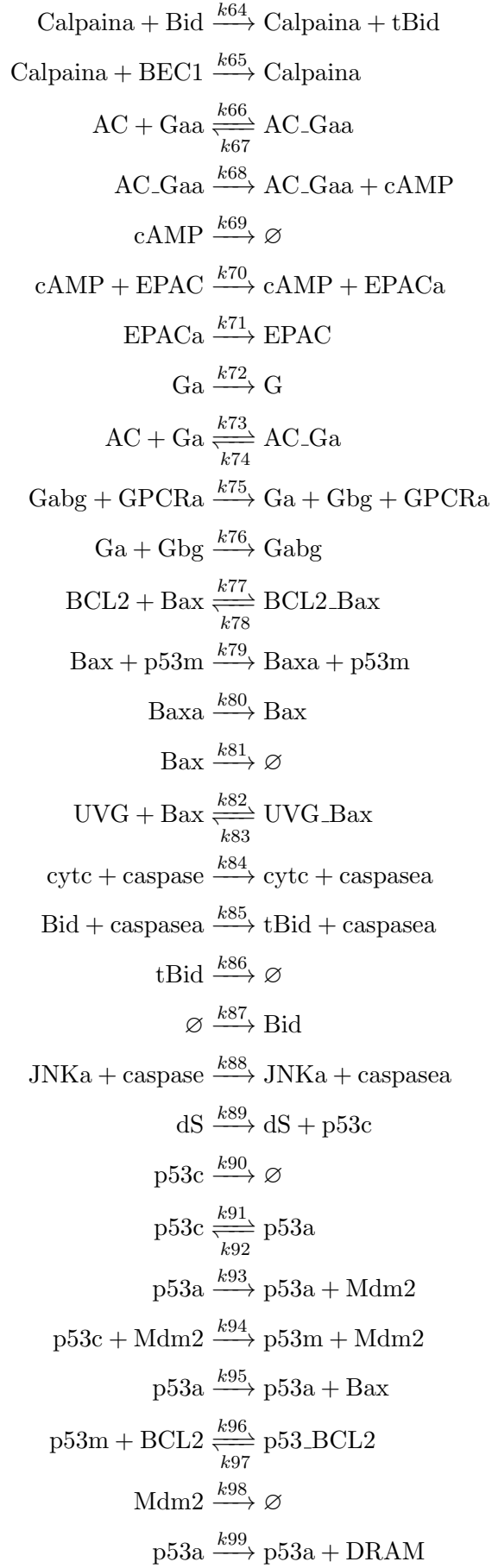


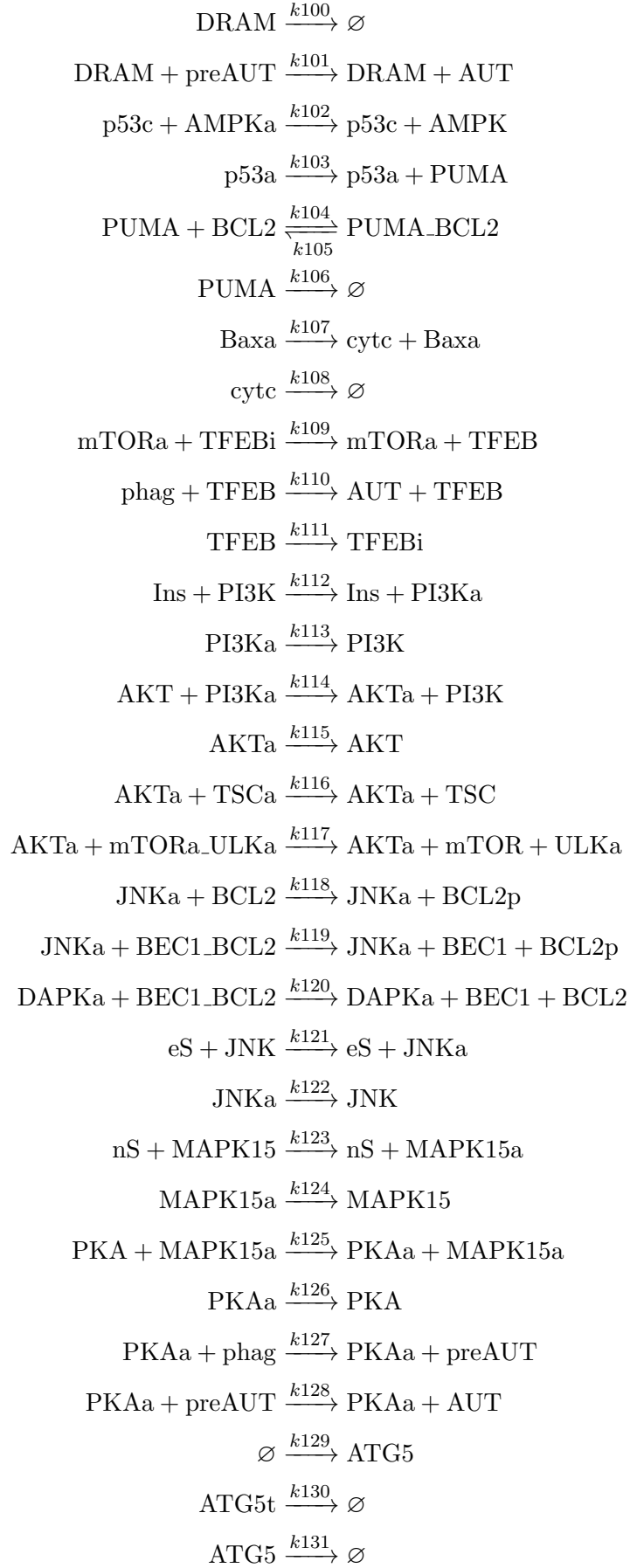
# 1 Liu et al. model's original reactions

The calculations were carried out in  $\frac{mol}{cm^3}$ , thus the rate coefficients values for the first and second order reactions are taken in  $\frac{1}{s}$  and  $\frac{cm^3}{mol*s}$  units, respectively.



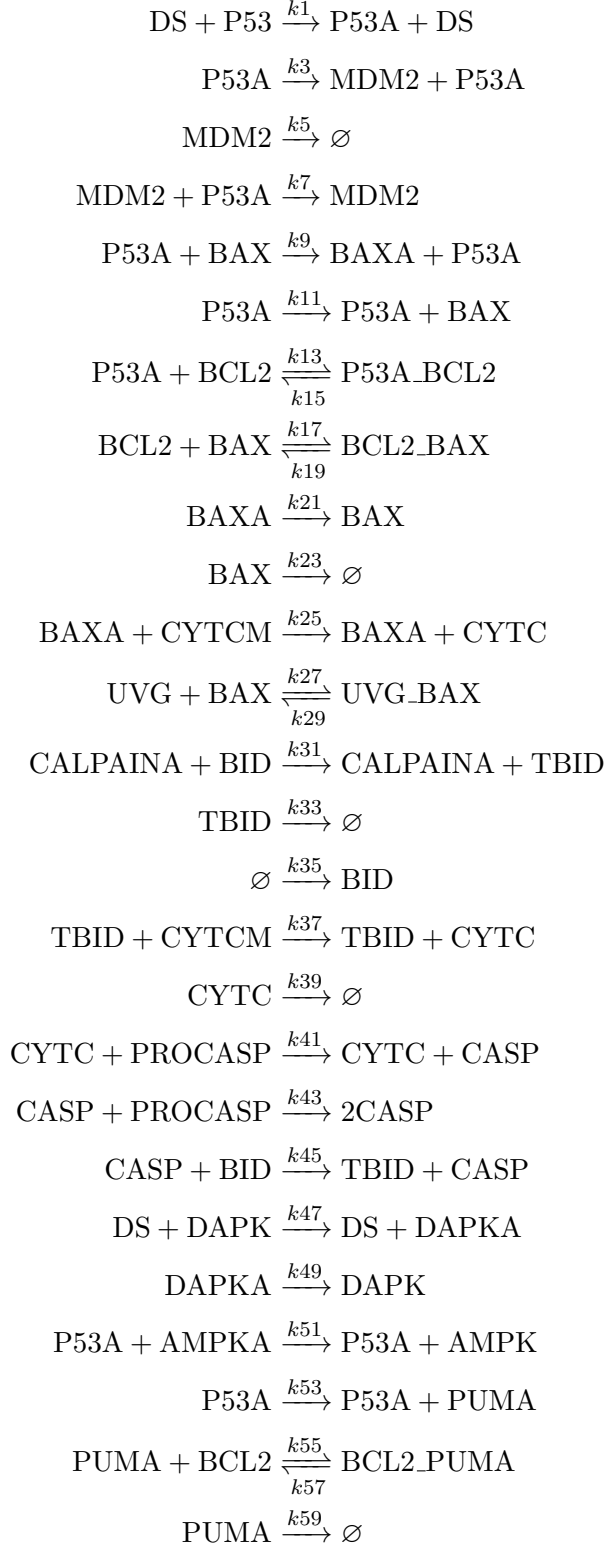


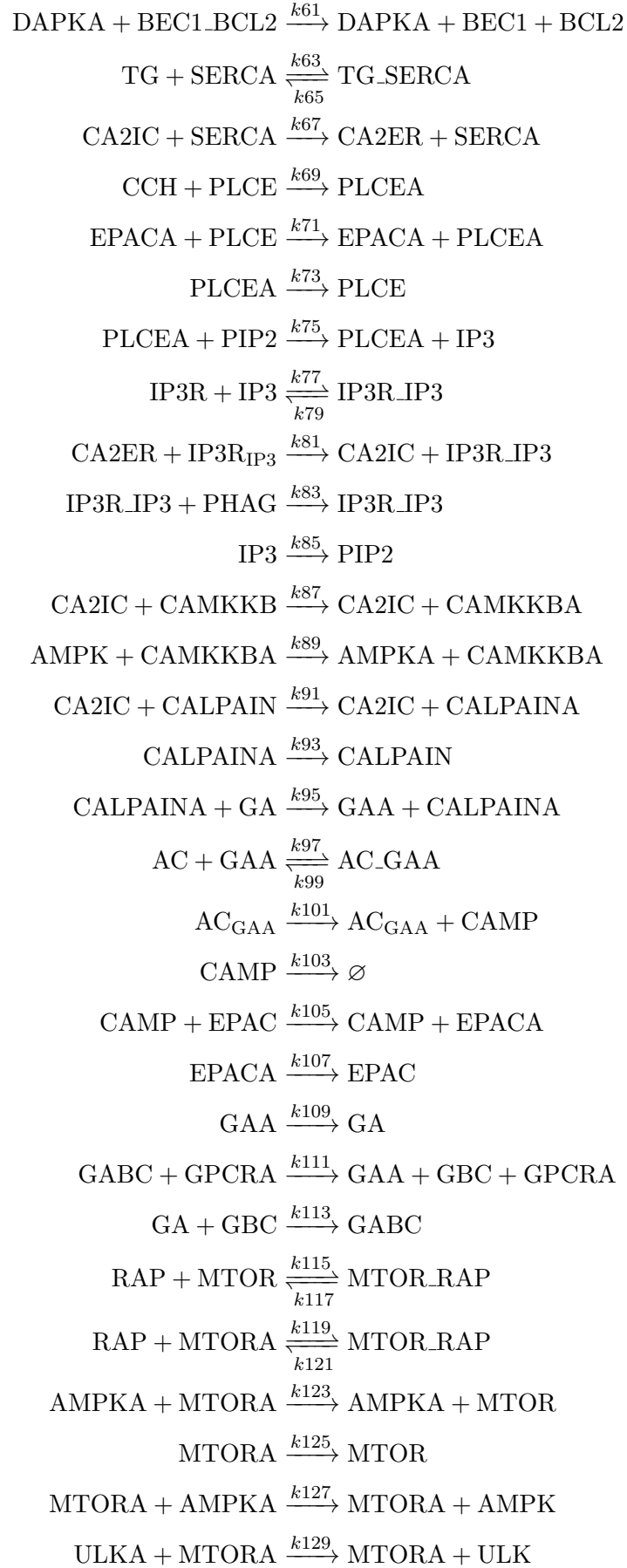


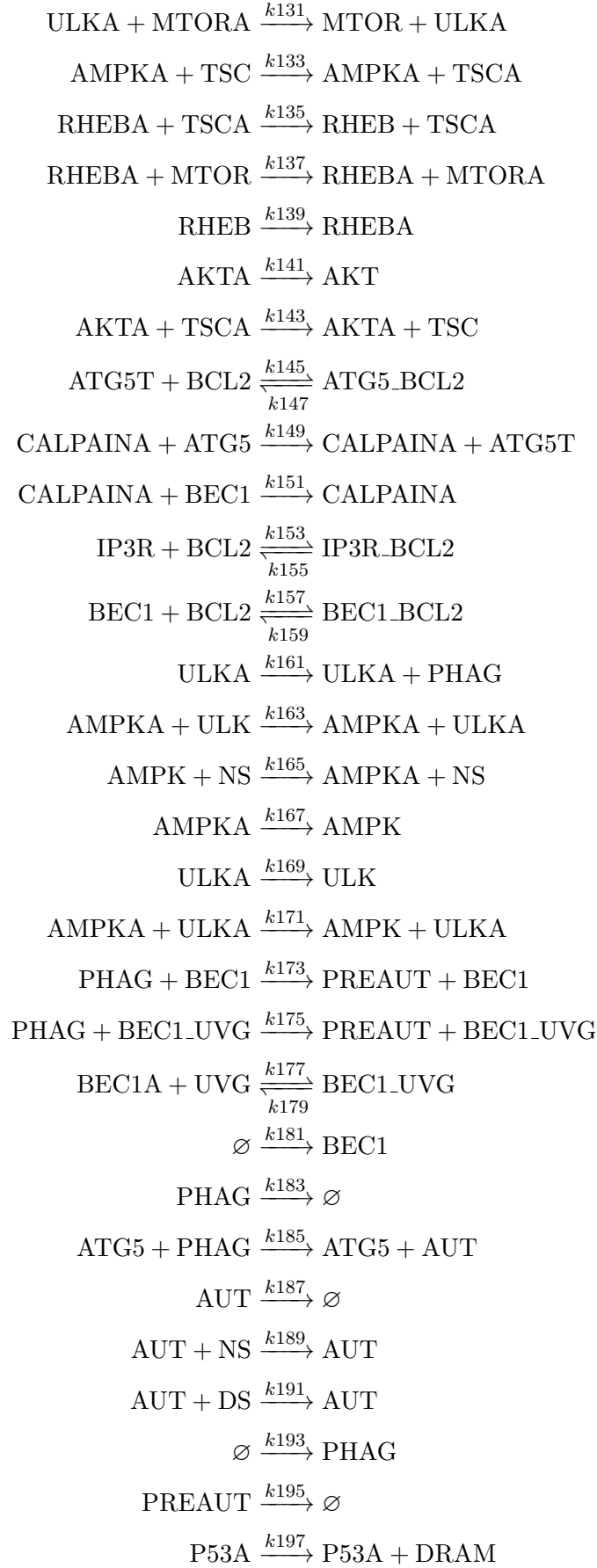


## 2 Revised reactions

The calculations were carried out in  $\frac{mol}{cm^3}$ , thus the rate coefficients values for the first and second order reactions are taken in  $\frac{1}{s}$  and  $\frac{cm^3}{mol*s}$  units, respectively.







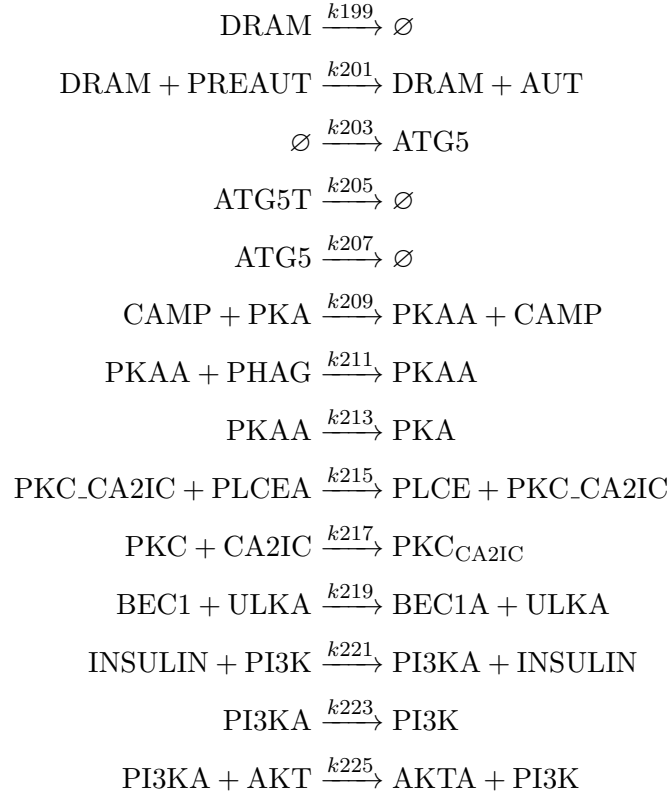


Table S1: List of the species found in the models, and their full names

Short Notation	Full Name
AMPK	AMP-activated protein kinase
nS	Nuclear Stress
AMPKa	Active AMP-activated protein kinase
mTORa	Active mammalian target of rapamycin
mTOR	mammalian target of rapamycin
mTOR.ULK	mTOR ULK complex
ULKa	Active Unc-51 like autophagy activating kinase
ULK	Unc-51 like autophagy activating kinase
phag	Phagophore
TSC	Tuberous sclerosis complex
TSCa	Active tuberous sclerosis complex
RHEBa	Active Ras homolog enriched in brain
RHEB	Ras homolog enriched in brain
BEC1	Beclin 1
preAUT	Pre-autophagosome
BEC1.UVG	Beclin 1 UVRAG complex
UVG	UV radiation resistance-associated gene
BEC1c	Cytosolic Beclin 1
cytc	Cytochrome c



Table S1: List of the species found in the models, and their full names

Short Notation	Full Name
ATG5	Autophagy-related protein 5
AUT	Autophagosome
eS	ER Stress
PERK	Protein kinase R-like endoplasmic reticulum kinase
PERKa	Active PERK
ATF4a	Active Activating Transcription Factor 4
ATF4	Activating Transcription Factor 4
dS	DNA Stress
DAPK	Death-associated protein kinase
DAPKa	Active death-associated protein kinase
EPACa	Active exchange protein directly activated by cAMP
PLCe	Phospholipase C epsilon
PLCea	Active phospholipase C epsilon
PIP2	Phosphatidylinositol 4,5-bisphosphate
IP3	Inositol trisphosphate
Ca2er	Endoplasmic reticulum calcium ion
IP3R_IP3	IP3 receptor IP3 complex
Ca2ic	Intracellular calcium
SERCA	Sarcoplasmic/endoplasmic reticulum calcium ATPase
Bax	Bcl-2-associated X protein
Baxa	Active Bcl-2-associated X protein
IP3R	IP3 receptor
IP2	Inositol bisphosphate
IP	Inositol phosphate
Ins	Insulin
CaMKKb	Calcium/calmodulin-dependent protein kinase kinase beta
CaMKKba	Active calcium/calmodulin-dependent protein kinase kinase b
BCL2	B-cell lymphoma 2
IP3R_BCL2	IP3 receptor BCL2 complex
BEC1_BCL2	Beclin 1 BCL2 complex
BCL2p	Phosphorylated BCL2
Calpain	Calpain
Calpaina	Active calpain
Ga	G protein alpha subunit
Gaa	Active G protein alpha subunit
ATG5t	truncated ATG5
ATG5_BCL2	ATG5 BCL2 complex
Bid	BH3 interacting-domain death agonist
tBid	Truncated Bid

Table S1: List of the species found in the models, and their full names

Short Notation	Full Name
AC	Adenylate cyclase
AC_Gaa	Adenylate cyclase G protein alpha subunit complex
cAMP	Cyclic adenosine monophosphate
EPAC	Exchange protein directly activated by cAMP
G	G protein
AC_Ga	Adenylate cyclase G protein alpha subunit complex
Gabg	G protein alpha, beta, gamma subunits
GPCRa	Active G protein-coupled receptor
Gbg	G protein beta and gamma subunits
BCL2_Bax	BCL2 Bax complex
p53m	Mitochondrial p53
UVG_Bax	UVG bound to Bax
caspase	Procaspase
caspasea	Cleaved caspase
JNKa	Active c-Jun N-terminal kinase
p53c	Cytosolic p53
p53a	Active p53
Mdm2	Mouse double minute 2 homolog
p53_BCL2	p53 BCL2 complex
DRAM	DNA damage-regulated autophagy modulator
PUMA	p53 upregulated modulator of apoptosis
PUMA_BCL2	PUMA BCL2 complex
TFEBi	Inactive transcription factor EB
TFEB	Transcription factor EB
PI3K	Phosphoinositide 3-kinase
PI3Ka	Active phosphoinositide 3-kinase
AKT	Protein kinase B
AKTa	Active protein kinase B
JNK	c-Jun N-terminal kinase
MAPK15	Mitogen-activated protein kinase 15
MAPK15a	Active mitogen-activated protein kinase 15
PKA	Protein kinase A
PKAa	Active protein kinase A

### 3 Initial protein concentrations

Table S2: Initial species concentration ranges in nM

species	min	max	source
AC	100	400	[1, 2]
AC_Ga	0	100	assumed
AC_Gaa	0	100	assumed
AKT	0	100	[3, 4]
AKTa	50	200	[3, 4]
AMPK	187.5	750	[5, 6]
AMPKa	0	100	[5, 6]
ATG5	100	400	[7]
ATG5_BCL2	0	100	assumed
ATG5t	15	60	assumed
AUT	0	100	[8]
BCL2	25	100	[9, 10]
BCL2_Bax	10	40	[9]
BCL2_PUMA	25	100	[9]
BEC1	50	200	[11]
BEC1_BCL2	0	100	assumed
BEC1_UVG	0	100	assumed
Bax	10	40	[9, 10]
Baxa	0	0	[9, 10]
Bid	10	40	[9, 10]
Ca2er	500	2000	[12, 13, 14]
Ca2ic	50	200	[12, 13, 14]
CaMKKb	50	200	[12]
CaMKKba	0	100	[12]
Calpain	10	40	[15]
Calpaina	0	100	[15]
DAPK	50	200	[11]
DAPKa	0	100	[11]
DRAM	0	100	[11]
EPAC	5	20	assumed
EPACa	0	100	assumed
GPCRa	5	20	[16]
Ga	5	20	[16, 17, 13]
Gaa	0	100	[16, 17, 13]
Gabc	0	100	[16, 17, 13]
Gbc	5	20	[16, 17, 13]
IP3	65	260	[12]
IP3R	5	20	[12]
IP3R_BCL2	0	100	assumed

IP3R_IP3	0	100	assumed
MDM2	0	100	[18, 19]
P53a_BCL2	0	100	assumed
PLCea	0	100	[12]
PLCe	5	20	[12, 14, 20]
PIP2	250	1000	[12]
PKA	75	300	[2]
PKAa	0	100	assumed
PUMA	0	100	assumed
RHEB	0	100	assumed
RHEBa	150	600	assumed
SERCA	0	100	[12]
TSC	112.5	450	[5, 6]
TSCa	0	100	[5, 6]
ULK	35	140	[8]
ULKa	0	100	assumed
UVG	50	200	assumed
UVG_Bax	0	100	assumed
cAMP	0	100	[1, 2]
casp	0	0	assumed
cytc	0	100	[9, 10]
cytcm	10	40	[9, 10]
mTOR	0	100	[5, 11]
mTORa	187.5	750	[5, 11]
mTORa_ULK	0	100	assumed
mTORa_ULKa	0	100	assumed
p53	12.5	50	[18, 19]
p53a	0	100	assumed
phag	0	100	assumed
preAUT	0	100	assumed
procasp	12	48	[9, 21]
tBid	0	100	[9]

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