

Article

Relaxation-Related Piezoelectric and Dielectric Behavior of Bi(Mg,Ti)O₃–PbTiO₃ Ceramic

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Abstract: Piezoelectric and dielectric materials have attracted much attention for their functional device applications. Despite its excellent piezoelectric properties, the content of lead in piezoelectric materials should be restricted to prevent future environmental problems. Therefore, reduced lead content in piezoelectric materials with similar piezoelectric properties is favorable. In our research, piezoelectric materials with decreased lead content will be studied and discussed. Even though the lead content is decreased in Bi(Mg_{0.5}Ti_{0.5})O₃–PbTiO₃ ceramics, they show piezoelectric properties similar to that of lead zirconate titanate (PZT)-based materials. We believe this high piezoelectric behavior is related to the relaxation behavior of Bi(Mg_{0.5}Ti_{0.5})O₃–PbTiO₃ (BMT–PT) ceramics. In this study, 0.62Bi(Mg_{0.5}Ti_{0.5})O₃–0.38PbTiO₃ ceramics were prepared by the conventional sintering process. These piezoelectric ceramics were sintered at varying temperatures of 975–1100 °C. Crystallinity and structural properties were analyzed and discussed. X-ray diffraction pattern analysis demonstrated that the optimal sintering temperature was around 1075 °C. A very high Curie temperature of 447 °C was recorded for 0.62BMT–0.38PT ceramics sintered at 1075 °C. For the first time, we found that the origin of the high Curie temperature, d_{33} , and the dielectric constant is the relaxation behavior of different dipoles in 0.62BMT–0.38PT ceramics.

Keywords: piezoelectric; BMT–PT; ceramic

1. Introduction

Since the discovery of Pb(Zr,Ti)O₃ (PZT) in the 1950s, it has been applied in piezoelectric transducers, actuators, and sensors because of its excellent piezoelectric properties [1]. PZT is also important in new high-precision switchable measurement methods, where dielectric properties are highly important. These methods compensate for environmental effects, voltage offset, frequency drift, and temperature influence, as previously reported in [2–4]. Due to its outstanding piezoelectric and mechanical properties, ceramic-based PZT actuators have received a great deal of attention in the industry. However, it is desirable to use materials with a low lead content to avoid environmental problems [5–8]. Therefore, there is a great need to discover piezoelectric materials that have a low lead content while still having favorable characteristics like those of PZT ceramics.

Recently, BiFeO₃-based (BF) perovskite materials have been intensively investigated, owing to their complex electric properties resulting from ferromagnetism and ferroelectricity [9–11]. For high temperature device applications, BF-based materials, (1 – x)BiMeO₃–xPbTiO₃ (Me³⁺ = Fe, Sc, Mg, In, Y, Yb, Ga), are attractive. These materials contain metallic components in a distorted perovskite structure, which has a higher Curie temperature between the ferroelectric and paraelectric states than that of PZT ceramics [12]. In particular, bismuth-based perovskite system Bi(Mg_{0.5}Ti_{0.5})O₃–PbTiO₃ (BMT–PT) ceramics are expected to have a higher Curie temperature with relative polarization and piezoelectric charge coefficient. Since the origin of the BiMeO₃–PTiO₃ system is multiferroic material,

it is expected to have weaker piezoelectric and dielectric properties than the PZT-based system. Despite the higher Curie temperature than that of the PZT system, lower piezoelectric and dielectric properties can be an obstacle for device applications. However, as a lead-containing material, BMT–PT piezoelectric material has similarly excellent piezoelectric properties as PZT, even though it has a low level of lead compared to PZT [13]. The multiferroic and relatively weak ferroelectric properties in the BiMeO₃–PTiO₃ system, which is usually observed in the electric field-dependent polarization process, can be the main obstacles for its future piezoelectric applications. However, as we have mentioned before, a relatively high piezoelectric charge coefficient of more than 200 pC/N with a higher Curie temperature range over 400 °C can improve its prospects for future multifunctional applications, including actuators and sensors.

In this study, we will prepare a BMT–PT system by optimizing the sintering temperature. The main advantages of a BMT–PT piezoelectric system are summarized in Table 1. As seen in Table 1, this system has high piezoelectric properties, a high Curie temperature, and a moderate price. However, as a representative lead content-reduced material, BiScO₃–PbTiO₃ also has a high piezoelectric coefficient and a high Curie temperature, but this material is very expensive and not feasible for application in electronic devices. The optimized composition of the BMT–PT system was selected through the phase diagram, and then the morphotropic phase boundary (MPB) was extracted to achieve the maximum piezoelectric properties [14]. In our assumption, we believe that 0.62Bi(Mg_{0.5}Ti_{0.5})O₃–0.38PbTiO₃ ceramics have a mixture of rhombohedra and tetragonal structures. This assumption will be tested and discussed after X-ray diffraction (XRD) analysis. Therefore, the composition of 0.62Bi(Mg_{0.5}Ti_{0.5})O₃–0.38PbTiO₃ was selected in this experiment [15]. Crystalline properties, including XRD patterns, and electrical properties, including piezoelectric and dielectric properties, will be investigated and discussed.

Table 1. Comparison of piezoelectric properties of BiMeO₃–PbTiO₃ and other lead content-reduced ceramics.

	Sintering Temperature	Dielectric Permittivity	Curie Temperature	Piezoelectric Charge Coefficient	Cost	Reference
BiFeO ₃ –PbTiO ₃	1100 °C	500 for 0.3BF–0.7PT	500 °C	165 pC/N	Moderate	[12,16]
BiScO ₃ –PbTiO ₃		1450 for 0.36BS–0.64PT	450 °C	460 pC/N	Very High	[12,17]
BiInO ₃ –PbTiO ₃		600 for 0.1BiInO ₃ –0.9TiO ₃	541 °C		Moderate	[12,18]
BiYbO ₃ –PbTiO ₃	1140 °C	650 for 0.1BY–0.9PT	590 °C	18 pC/N	Very High	[12,19]
BNT–PT 0.55Bi(Ni _{1/2} Ti _{1/2})O ₃ – 0.45PbTiO ₃	1050 °C		400 °C	293 pC/N	Moderate	[12,20]
BMT–PT (our samples)	1075 °C	625 for 0.62BMT–0.38PT	447 °C	237 pC/N	Moderate	

2. Materials and Methods

The 0.62Bi(Mg_{0.5}Ti_{0.5})O₃–0.38PbTiO₃ (0.62BMT–0.38PT) ceramics were prepared by a standard ceramic sintering technique using the blended oxides method. The raw materials, Bi₂O₃, 4MgCO₃·Mg(OH)₂·5H₂O, TiO₂, and PbO, were weighed and combined by ball-milling with a ZrO₂ ball in ethyl alcohol for 24 h. The blended powders were calcined at 900 °C for 2 h in a furnace. The desiccated powders were blended with polyvinyl alcohol (PVA) and compressed into a disk with a diameter of 10 mm and thickness of 1 mm. The sample was then sintered at various temperatures ranging from 975 to 1100 °C (975, 1000, 1025, 1050, 1075, and 1100 °C) for 2 h in a sealed alumina crucible to avoid loss of Bi₂O₃ and PbO due to sublimation. Silver electrodes were formed on both sides of the ceramic plates by screen printing. The poling process was performed in a silicon oil bath at

100 °C with an applied electric field of 1 kV/mm. The crystalline properties were analyzed by XRD using a Cu K α radiation source (Bruker ARS), and the electric properties were analyzed by an HP 4294 impedance analyzer. Field emission scanning electron microscopy (FESEM) was used to examine the microstructure. To characterize its piezoelectric and dielectric properties, the piezoelectric charge coefficient and electric field-dependent polarization processes were performed, in this experiment, by employing the Sawyer–Tower method with 0.1 Hz.

3. Results and Discussion

Figure 1 shows the XRD patterns for the 0.62BMT–0.38PT systems, which were sintered at various temperatures. The specimens were sintered from 975 to 1100 °C in steps of 25 °C. Figure 2 displays the (001) XRD peaks of 0.62BMT–0.38PT piezoelectric ceramics according to the sintering temperature range. As shown in Figures 1 and 2, the XRD patterns show very weak variation in peak intensities and positions. This means that the degree of crystallization and d-space of lattice parameters were slightly changed after the sintering process. As observed in Figure 2, the (001) peak position of 0.62BMT–0.38PT ceramics were shifted to lower angles as the sintering temperature increased. It means that the lattice parameter *c* increased as the sintering temperature increased. Furthermore, it seems that 0.62BMT–0.38PT piezoelectric systems have good crystalline structure without a pyrochlore phase.

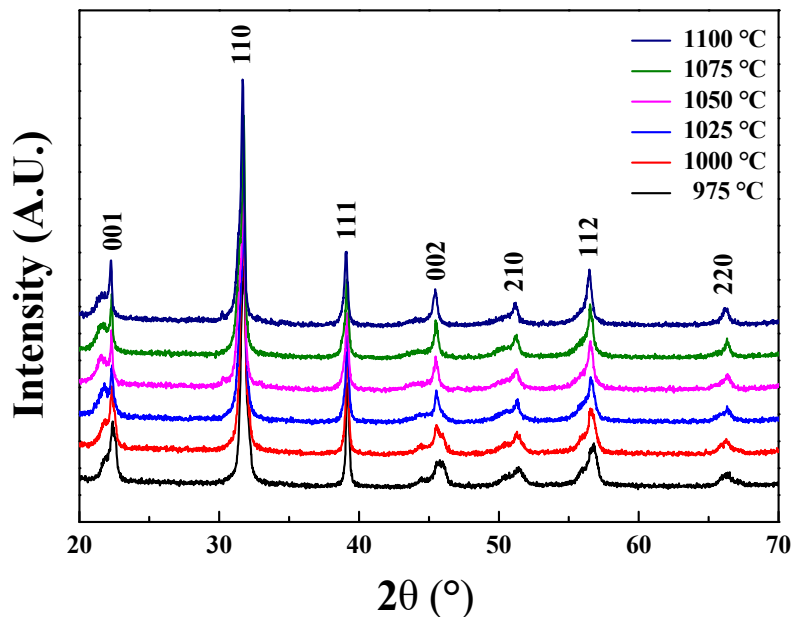


Figure 1. X-ray diffraction (XRD) patterns of $\text{Bi}(\text{Mg}_{0.5}\text{Ti}_{0.5})\text{O}_3\text{--PbTiO}_3$ ceramics according to sintering temperature.

Figure 3 depicts the degree of crystallization for the (001) direction in the 0.62BMT–0.38PT ceramic. The crystallization degree of (001) approached or even exceeded 10% at the sintering temperature of 1075 °C. This means that the distorted perovskite structure of 0.62BMT–0.38PT ceramics has a high degree of *c*-axis orientation as sintering temperature increases, which corresponds to the added thermal energy to form the crystalline structure. However, when the sintering temperature was increased beyond 1100 °C, the peak ratio of (001) decreased. We believe this maximum value of peak ratio (001) at 1075 °C and decreased peak ratio at 1100 °C are probably related with the crystallization degree. Therefore, we can argue that a sintering temperature of 1075 °C is the optimized sintering temperature owing to the increased (001) relative intensities.

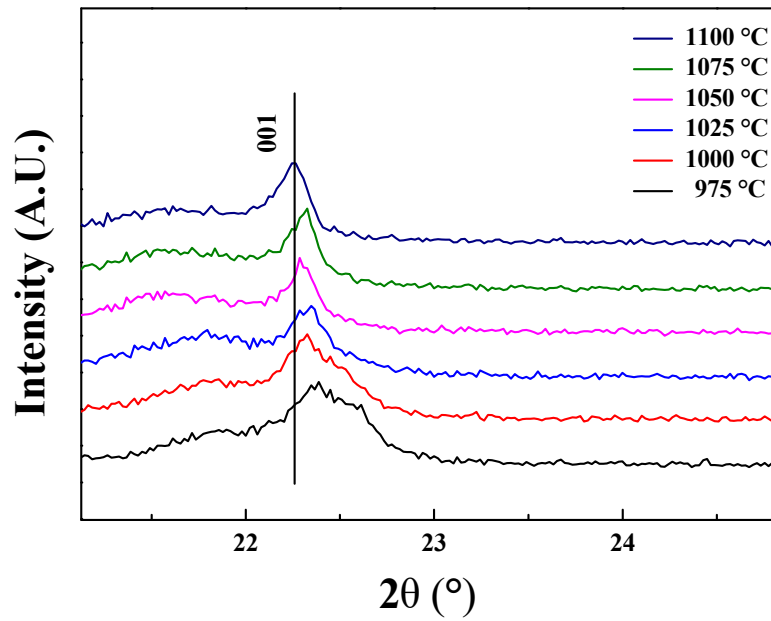


Figure 2. XRD (001) peak shifts of $\text{Bi}(\text{Mg}_{0.5}\text{Ti}_{0.5})\text{O}_3\text{-PbTiO}_3$ ceramics according to sintering temperature.

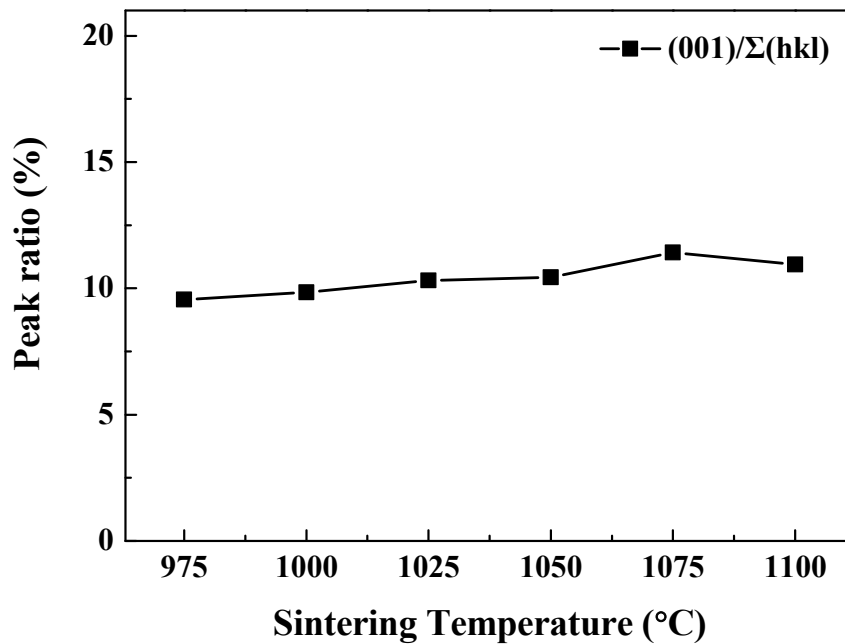


Figure 3. Peak ratio (001) of $\text{Bi}(\text{Mg}_{0.5}\text{Ti}_{0.5})\text{O}_3\text{-PbTiO}_3$ ceramics according to sintering temperature.

Figure 4 shows the FESEM images for the 0.62BMT–0.38PT ceramics, which were sintered at various temperatures. As shown in the FESEM images, the grain size of 0.62BMT–0.38PT ceramics increased as the sintering temperature increased. At a sintering temperature of 1075 °C, 0.62BMT–0.38PT ceramics showed a large grain size with a dense structure. Due to this highly dense structure, 0.62BMT–0.38PT ceramics that were sintered at 1075 °C showed the highest piezoelectric and dielectric properties among the specimens. However, as the sintering temperature of 1100 °C was attained, the grain shape was distorted, and the size was decreased.

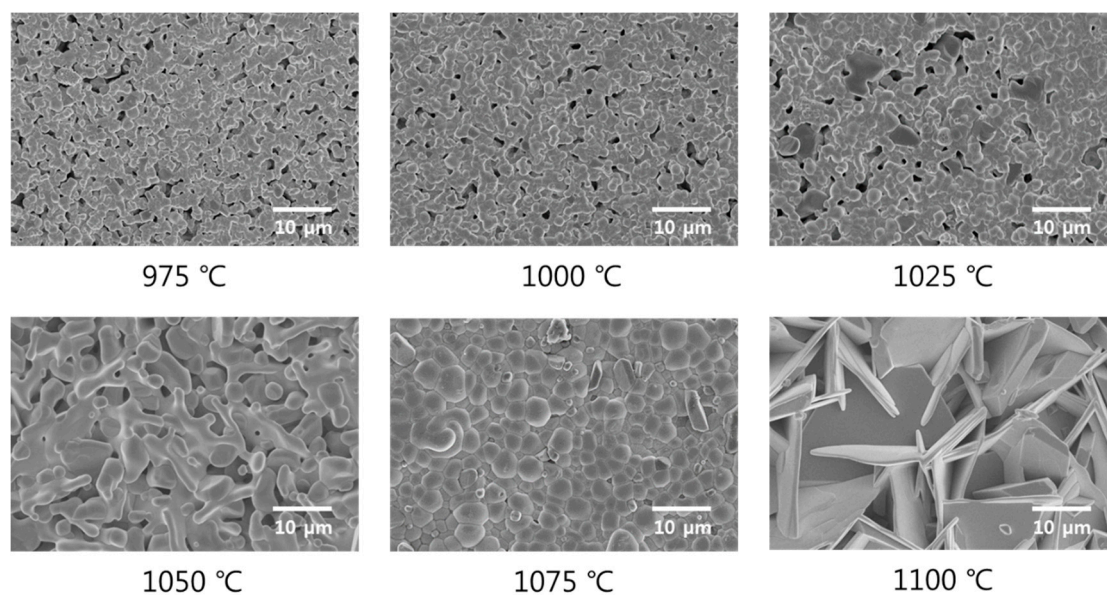


Figure 4. Field-emission scanning electron microscopy (FESEM) images of $\text{Bi}(\text{Mg}_{0.5}\text{Ti}_{0.5})\text{O}_3\text{-PbTiO}_3$ according to sintering temperature.

Figure 5 reveals the bulk and theoretical density of 0.62BMT–0.38PT ceramics depending on the sintering temperature. As the sintering temperature increased, the density increased up to 1075 °C and then decreased. This behavior is similar to that of grain size as observed in the FESEM images. As the sintering temperature increased, 0.62BMT–0.38PT ceramics became crystallized, therefore, the density was increased. However, as the sintering temperature was further increased up to 1100 °C, the density decreased. We believe that this decreased bulk density comes from the oversintered phase of 0.62BMT–0.38PT ceramics. It also seems that the bulk density of 0.62BMT–0.38PT ceramics correlated with the FESEM images, which is described in Figure 4.

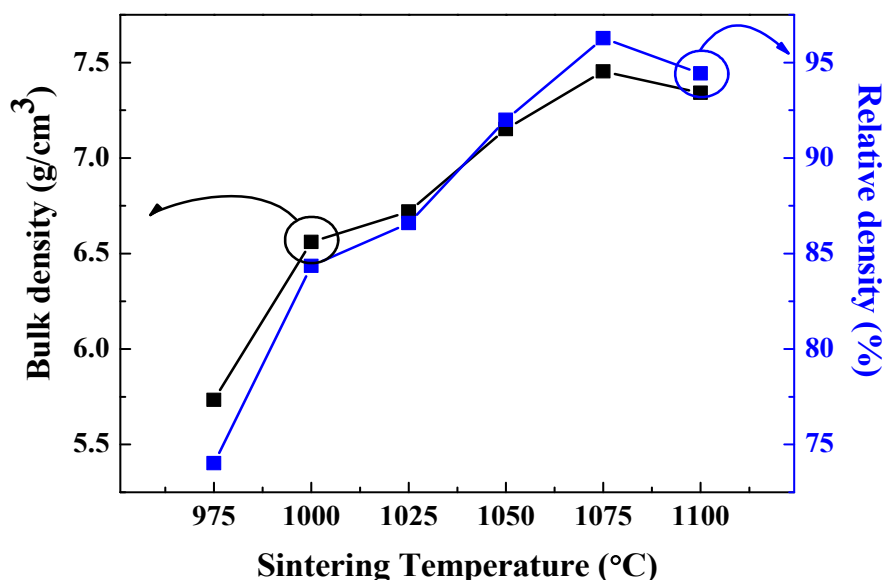


Figure 5. Bulk density and relative density of $\text{Bi}(\text{Mg}_{0.5}\text{Ti}_{0.5})\text{O}_3\text{-PbTiO}_3$ ceramics according to sintering temperature.

Figure 6 shows the frequency-dependent dielectric permittivity of 0.62BMT–0.38PT ceramics from 1 kHz to 1 MHz. Clearly, 0.62BMT–0.38PT ceramics sintered at the 1075 °C showed the highest

dielectric permittivity of 625 at 1 kHz, whereas those sintered at 975 °C showed the lowest dielectric permittivity of 480 at 1 kHz.

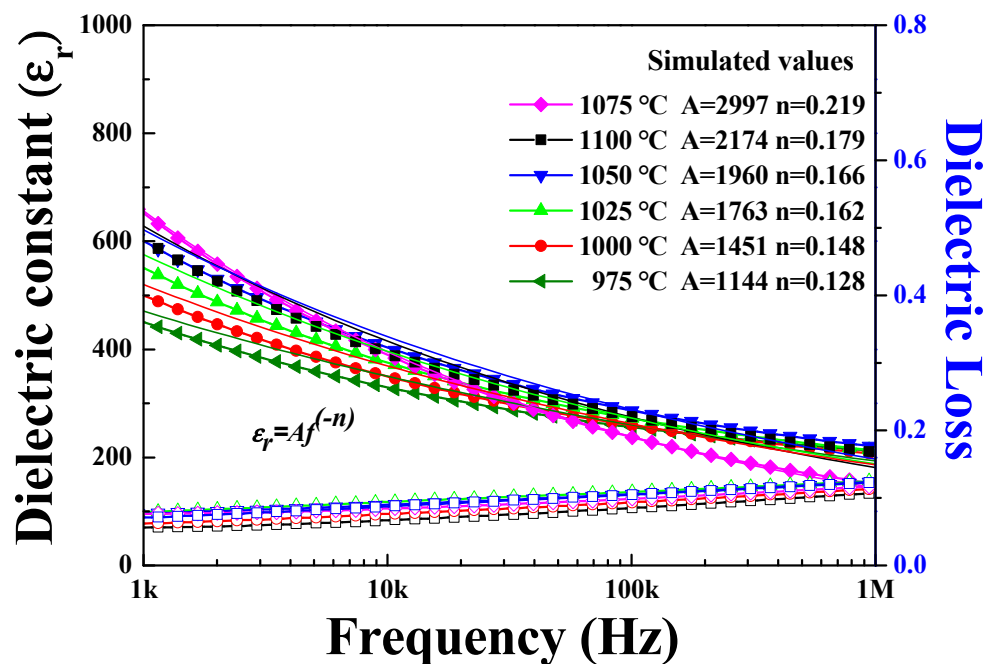


Figure 6. Frequency-dependent dielectric permittivity of $\text{Bi}(\text{Mg}_{0.5}\text{Ti}_{0.5})\text{O}_3\text{-PbTiO}_3$ ceramics according to sintering temperature.

It seems that 0.62BMT–0.38PT ceramics have high dielectric permittivity ranges at room temperature. The solid lines indicate the simulation fitting from the measured samples with the power law. The power law of $\epsilon_r = Af^{-n}$ was employed to fit dielectric relaxation behavior [21]. Ceramics of 0.62BMT–0.38PT sintered at 1075 °C showed the highest exponent of 0.219 among the specimens. Compared to other specimens, this means that the variance of dielectric permittivity for 0.62BMT–0.38PT ceramics sintered at 1075 °C has the highest exponent of 0.219 and highest dielectric permittivity of 625. The high exponent value of 0.219 from the power law equation means that many different dipoles were involved in the relaxation process with continuous freezing out of dipoles with increasing frequency range. Therefore, 0.62BMT–0.38PT piezoelectric ceramics showed rapid change in the dielectric constant when increasing the frequency range. Owing to this high relaxation behavior, 0.62BMT–0.38PT ceramics sintered at 1075 °C have the highest piezoelectric properties. The dielectric permittivity of 0.62BMT–0.38PT ceramics sintered at 1075 °C also have the highest dielectric permittivity values.

Figure 7 shows the electric field-dependent polarizations for 0.62BMT–0.38PT ceramics with different sintering temperatures. As the sintering temperature was increased, the polarization increased. In particular, 0.62BMT–0.38PT ceramics sintered at 1075 and 1100 °C showed higher ferroelectric properties compared to other specimens. It seems that the higher the sintering temperature, the larger the polarization behavior. In the case of the electric field-dependent polarization case, sintering temperature dependencies are more clearly observed.

Figure 8 shows the piezoelectric charge coefficient and electromechanical coupling coefficient of 0.62BMT–0.38PT ceramics depending on the sintering temperature range. The piezoelectric charge coefficient and electromechanical coupling coefficient of 0.62BMT–0.38PT ceramics sintered at 1075 °C showed the highest values of 240 pC/N and 47%, respectively. These high piezoelectric charge coefficient and electromechanical coupling coefficient coincided well with the dense behavior observed in FESEM images and bulk densities.

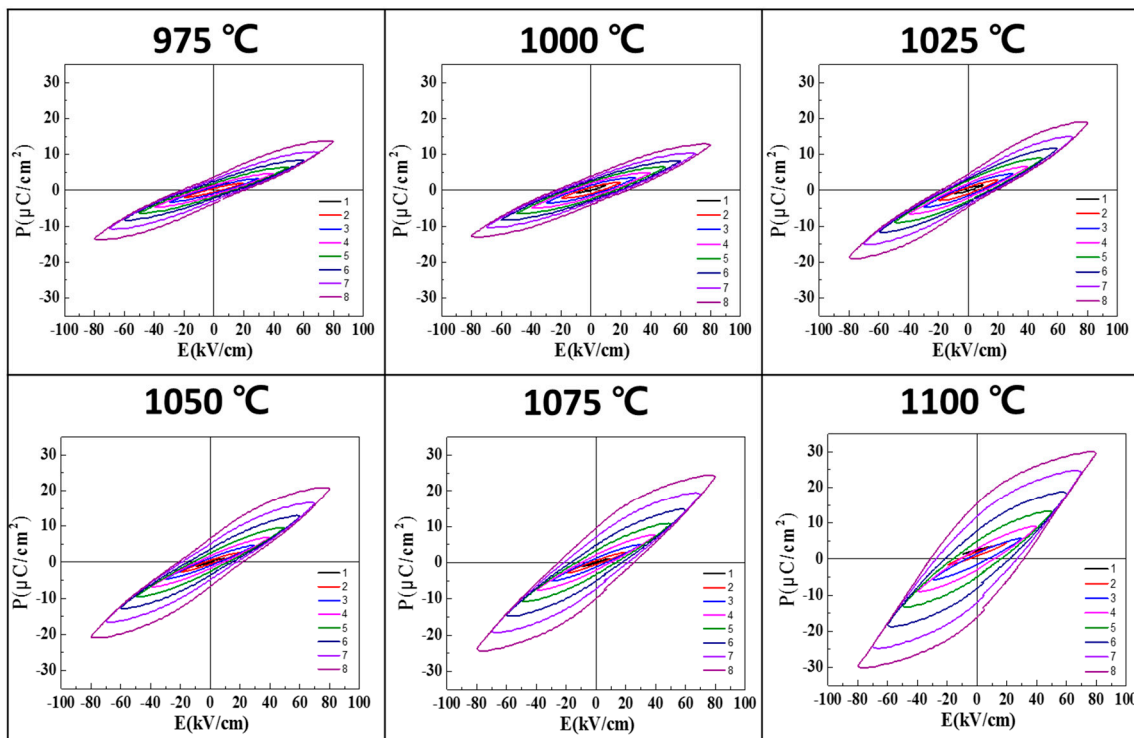


Figure 7. Electric field-dependent polarization properties of $\text{Bi}(\text{Mg}_{0.5}\text{Ti}_{0.5})\text{O}_3\text{-PbTiO}_3$ according to sintering temperature.

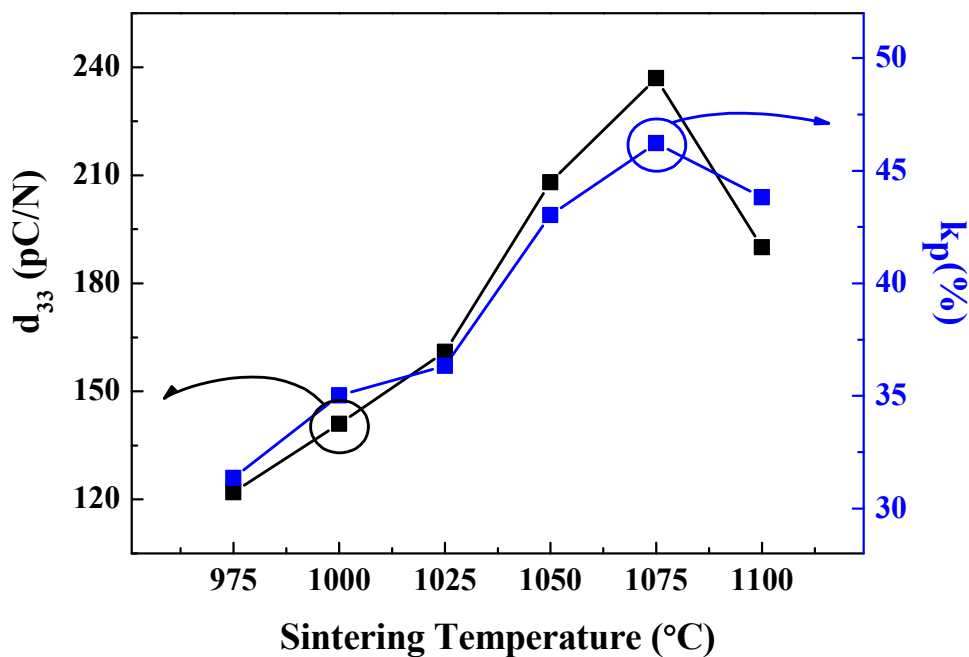


Figure 8. Piezoelectric coefficient d_{33} and k_p of $\text{Bi}(\text{Mg}_{0.5}\text{Ti}_{0.5})\text{O}_3\text{-PbTiO}_3$ according to sintering temperature.

Figure 9 displays the piezoelectric voltage coefficient and figure of merit (FoM) of 0.62BMT–0.38PT ceramics. As shown in Figure 9, the highest value of the piezoelectric voltage coefficient of 41×10^{-3} Vm/N and FoM of $9.8 \text{ pm}^2/\text{N}$ were obtained for the 0.62BMT–0.38PT ceramics. Since the piezoelectric voltage coefficient was derived from the piezoelectric charge coefficient and dielectric constant, $g_{33} = d_{33}/\epsilon_r$, we can expect that the piezoelectric voltage coefficient of 0.62BMT–0.38PT ceramics sintered at 1075 °C has the highest values of 41×10^{-3} Vm/N and FoM of $9.8 \text{ pm}^2/\text{N}$.

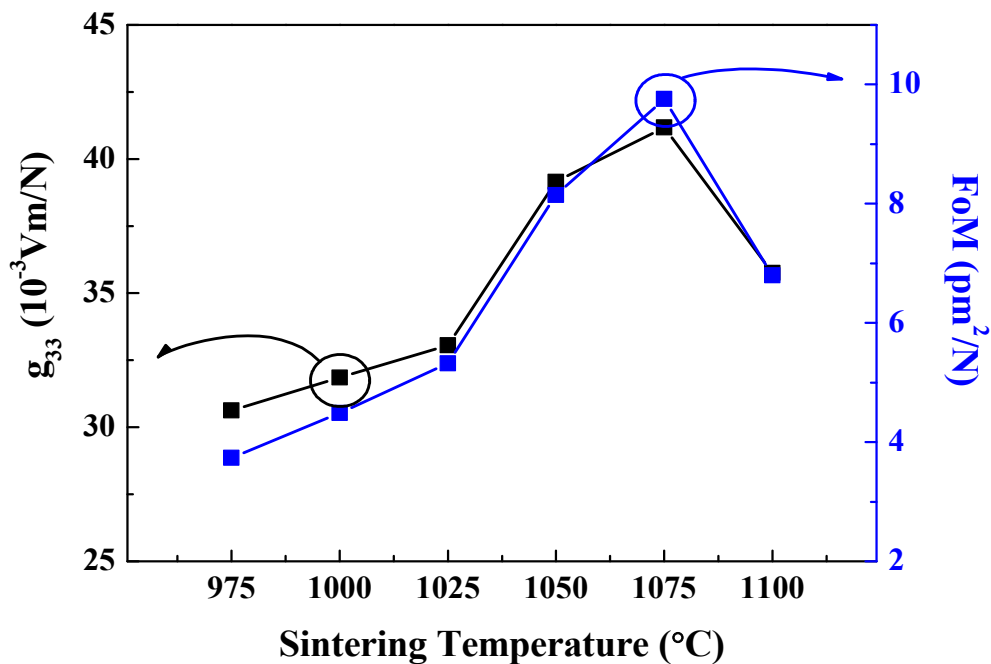


Figure 9. Piezoelectric voltage coefficient and figure of merit (FoM) of $\text{Bi}(\text{Mg}_{0.5}\text{Ti}_{0.5})\text{O}_3\text{-PbTiO}_3$ according to sintering temperature.

Figure 10 shows the temperature-dependent dielectric permittivity ϵ_r of the 0.62BMT–0.38PT ceramic sintered from 975 to 1100 °C. At sintering temperatures of 975, 1000, 1025, 1050, 1075, and 1100 °C, the Curie temperature was 346.9, 374.5, 386.5, 389.2, 447.2, and 428.5 °C, respectively. As the sintering temperature increased from 975 to 1075 °C, the Curie temperature increased from 346.9 to 447.2 °C. As the sintering temperature reached 1100 °C, the Curie temperature suddenly decreased. Compared to other specimens, BMT–PT ceramics sintered at 975 °C had the lowest Curie temperature of 346.9 °C, whereas those sintered at 1075 °C had the highest Curie temperature of 447.2 °C.

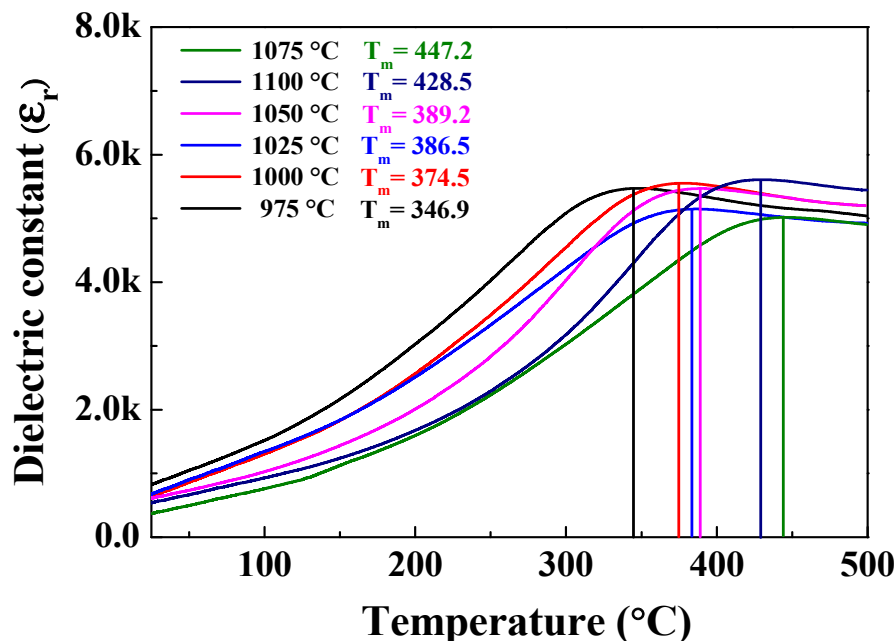


Figure 10. Temperature-dependent relative dielectric constant ϵ_r of $\text{Bi}(\text{Mg}_{0.5}\text{Ti}_{0.5})\text{O}_3\text{-PbTiO}_3$ ceramic according to sintering temperature.

4. Conclusions

In this research, the piezoelectric and dielectric properties of 0.62BMT–0.38PT ceramics with different sintering temperatures were investigated and discussed. A very high Curie temperature of 447 °C was recorded for 0.62BMT–0.38PT ceramics sintered at 1075 °C. 0.62BMT–0.38PT piezoelectric ceramics have a reduced lead content and high piezoelectric charge coefficient of 237 pC/N and can, therefore, be used in piezoelectric applications where the environment is harsh. Even though 0.62BMT–0.38PT ceramics had a lower lead content compared to Pb(Zr_{0.5}Ti_{0.5})O₃-based conventional piezoelectric ceramics, 0.62BMT–0.38PT piezoelectric ceramics still have excellent piezoelectric and dielectric properties with a high Curie temperature. We believe that the high piezoelectric properties of 0.62BMT–0.38PT are related to relaxation behavior. We believe 0.62BMT–0.38PT ceramics, with their lower lead content, can act as alternative materials for lead-based piezoelectric materials. Reducing the lead content of piezoelectric materials is expected to help not only by preventing environmental pollution on Earth but, also, by being more useful as a piezoelectric material because of its excellent characteristics compared to lead-free piezoelectric material. For example, 0.62BMT–0.38PT ceramics can be applied in piezoelectric transducers or as a sintering aid, using ferroelectricity, that does not change at a high temperature.

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Conflicts of Interest: The authors declare no conflict of interest.

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