







Communication

# Standing-Wave Feeding for High-Gain Linear Dielectric Resonator Antenna (DRA) Array

Kerlos Atia Abdalmalak <sup>1,2,\*</sup>, Ayman Abdulhadi Althuwayb <sup>3</sup>, Choon Sae Lee <sup>4</sup>, Gabriel Santamaría Botello <sup>5</sup>,  
Enderson Falcón-Gómez <sup>1</sup>, Luis Emilio García-Castillo <sup>1</sup> and Luis Enrique García-Muñoz <sup>1</sup>

- <sup>1</sup> Department of Signal Theory and Communications, Carlos III University of Madrid, 28903 Madrid, Spain; efalcon@pa.uc3m.es (E.F.-G.); luise@tsc.uc3m.es (L.E.G.-C.); legarcia@ing.uc3m.es (L.E.G.-M.)
- <sup>2</sup> Electrical Engineering Department, Aswan University, Aswan 81542, Egypt
- <sup>3</sup> Department of Electrical Engineering, College of Engineering, Jouf University, Sakaka 72388, Saudi Arabia; aalthuwayb@ju.edu.sa
- <sup>4</sup> Electrical and Computer Engineering Department, Southern Methodist University, Dallas, TX 75205, USA; csl@lyle.smu.edu
- <sup>5</sup> Electrical, Computer and Energy Engineering Department, University of Colorado, Boulder, CO 80309, USA; gasantam@pa.uc3m.es
- \* Correspondence: kerlos.atia@alumnos.uc3m.es

**Abstract:** A novel feeding method for linear DRA arrays is presented, illuminating the use of the power divider, transitions, and launchers, and keeping uniform excitation to array elements. This results in a high-gain DRA array with low losses with a design that is simple, compact and inexpensive. The proposed feeding method is based on exciting standing waves using discrete metallic patches in a simple design procedure. Two arrays with two and four DRA elements are presented as a proof of concept, which provide high gains of 12 and 15 dBi, respectively, which are close to the theoretical limit based on array theory. The radiation efficiency for both arrays is about 93%, which is equal to the array element efficiency, confirming that the feeding method does not add losses as in the case of standard methods. To facilitate the fabrication process, the entire array structure is 3D-printed, which significantly decreases the complexity of fabrication and alignment. Compared to state-of-the-art feeding techniques, the proposed method provides higher gain and higher efficiency with a smaller electrical size.

**Keywords:** antenna array feeds; dielectric resonator antenna (DRA); linear antenna arrays; standing wave; high-gain antennas; high radiation efficiency; 3D printing



**Citation:** Abdalmalak, K.A.; Althuwayb, A.A.; Lee, C.S.; Botello, G.S.; Falcón-Gómez, E.; García-Castillo, L.E.; García-Muñoz, L.E. Standing-Wave Feeding for High-Gain Linear Dielectric Resonator Antenna (DRA) Array. *Sensors* **2022**, *22*, 3089. <https://doi.org/10.3390/s22083089>

Academic Editor: Qammer Hussain Abbasi

Received: 24 February 2022

Accepted: 15 April 2022

Published: 18 April 2022

**Publisher's Note:** MDPI stays neutral with regard to jurisdictional claims in published maps and institutional affiliations.



**Copyright:** © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (<https://creativecommons.org/licenses/by/4.0/>).

## 1. Introduction

For decades, dielectric resonators (DRs) have been widely utilized as tuners or amplifiers in microwave-circuit applications [1] due to their high Q-factors. The utilization of antennas had to wait for a long time, until Long et al. presented the first cylindrical dielectric resonator antenna (DRA) in 1983 [2]. Ever since then, dielectric antennas have been intensively studied as potential substitutions of traditional less efficient metal radiators, which have serious problems at high frequencies [3–5]. There are some metal antennas such as lens [6] and slot [7] antennas that can avoid such losses and provide high gain with high efficiency, but they still have the drawbacks of being bulky and complex, respectively. From this perspective, DRAs come with numerous beneficial features such as high radiation efficiency, easy excitation scheme, light weight, and small size [8–11]. One of the main limitations of the DRA is its relatively low gain [12]; hence, dielectric resonator antenna (DRA) arrays are a preferred choice for many applications [13,14].

Several excitation schemes are used to feed DRA arrays [15], such as series or corporate microstrip lines [16,17], standard rectangular waveguide (RWG) [18–21], substrate integrated waveguide (SIW) [22–24], and dielectric image waveguide (DIG) [25–27]. Traditional corporate-feeding networks have a number of power dividers that cause spurious

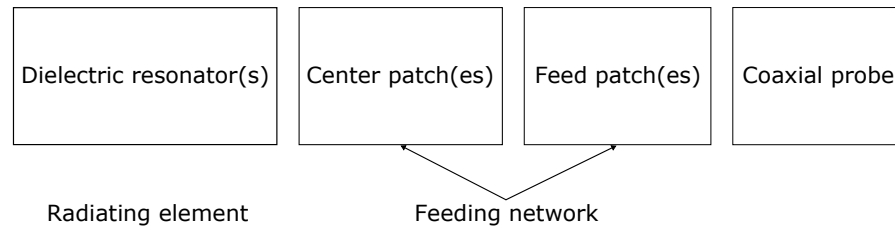
radiation, resulting in high losses [28]. Because of this, new feeding techniques focus on avoiding such losses, for example, in [29], the authors proposed the use of a single microstrip line to feed the whole array. Although this feeding technique is simple and of low cost, the resulting gain is relatively small (15 dBi using 9 elements), and its efficiency is below 80% [30]. Efficiency can be enhanced in the case of feeding only a single element and turning the rest of the array elements into parasitic elements, as in [31]; however, field distribution is not the same for all elements, which results in relatively low gain. For example, in [32], a gain of about 6.6 dBi was obtained using five elements. The RWG feeding scheme has two major drawbacks, high production costs and a bulky structure, which hinder array design [33]. Another feeding method is SIW, which results in significant leakage losses through multiple metallic vias [22] and extra complexity in the design. Lastly, in the DIG feeding scheme, considerable backradiation is a major issue [25]. Additionally, tapered rectangular waveguides are needed to launch the DIG that, in turn, renders the structure bulky and increases the fabrication cost [34].

Although state-of-the-art feeding methods provide some good characteristics, there is still a main research gap to find a novel feeding method that simultaneously illuminates the use of power dividers, transitions, or launchers with keeping uniform excitation to the array elements and low losses in the feeding network. This results in a high-gain DRA array with high efficiency, and renders the design simple, compact, and inexpensive, which are essential parameters for wireless applications such as sensing applications and 5G base station antennas. Hence, this paper presents a novel feeding scheme for linear arrays based on the standing-wave concept [35], compared to our previous standing-wave DRA array presented in [36] where the standing wave was formed by dielectric bridges with metal cover between elements. Here, it is formed within discrete metallic patches printed in the same substrate layer. This ensures more uniform excitation between elements, and could thus achieve performance close enough to the theoretical limit of the array, and achieve a similar gain with a lower number of elements compared to [36], which, in turn, would significantly decrease the size of the solution, as is demonstrated in Section 5.

This study is organized as follows. The detailed design procedure of the array element which acts as the unit cell of the array is presented in Section 2. A two-element array design based on a standing-wave feed is explained in Section 3 with the electric field distribution in the feeding network to confirm the forming of standing waves. Then, the concept is extended to a larger array of four elements in Section 4 with the theoretical calculations of the array factor to validate the feeding concept and confirm the uniform excitation of the array elements using the novel feeding method. Fabrication and measured results are given in Section 5 along with a comparison to DRA arrays fed by state-of-the-art feeding methods from different points of view. Lastly, the main remarks and future work are concluded in Section 6.

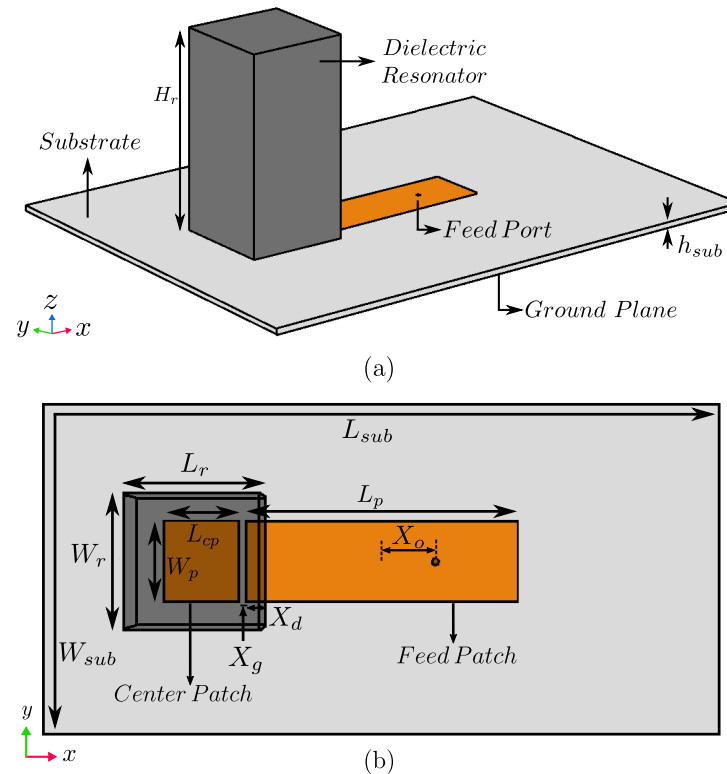
## 2. Design of DRA Array Unit Cell

Figure 1 presents a general high-level block diagram of DRA array fed by the proposed standing wave feeding method. The design consists of discrete metallic patches called feed and center patches transferring the signal from the coaxial probe to the dielectric resonator which acts as the radiating element. The feed patch was designed to form a standing wave under the stripline to feed the antenna element. Then, another smaller patch (called a center patch) is inserted with a gap distance to control the field excitation under the dielectric resonator. Lastly, a dielectric resonator (radiating element) is introduced above the center patch. The total distance between neighboring elements is about one and a half guided wavelengths for maximal array gain. It is clear here that the proposed feeding method excited the radiating element without the need for any power dividers, transitions, or launchers, which would significantly affect DRA array performance, as is demonstrated in the rest of the paper.



**Figure 1.** Block diagram of DRA array based on the proposed feeding method.

As an initial step of the array design, the radiating element was designed, which is a rectangular dielectric resonator as shown in Figure 2. Here, a higher-order mode  $TE_{113}$  is excited at a frequency of 3.9 GHz to obtain higher gain than that of the fundamental mode of  $TE_{111}$  (enhancement of about 2 dB). The optimized dimensions of the resonator were  $L_r = 26.2$  mm,  $W_r = 26.2$  mm, and  $H_r = 45.8$  mm. It was composed of polylactic acid (PLA) with dielectric constant  $\epsilon_r = 3.549$  [37,38]. High-permittivity resonators ( $\epsilon_r$  up to 140 [12]) can be used if compact sizes are needed, but at a high cost. The feed-network substrate was Arlon 25N with dielectric constant  $\epsilon_{r(\text{sub})} = 3.38$ , loss tangent  $\delta_{\text{sub}} = 0.0015$ , thickness  $h_{\text{sub}} = 1.5$  mm, and surface area  $120 \times 160$  mm<sup>2</sup> ( $W_{\text{sub}} \times L_{\text{sub}}$ ).



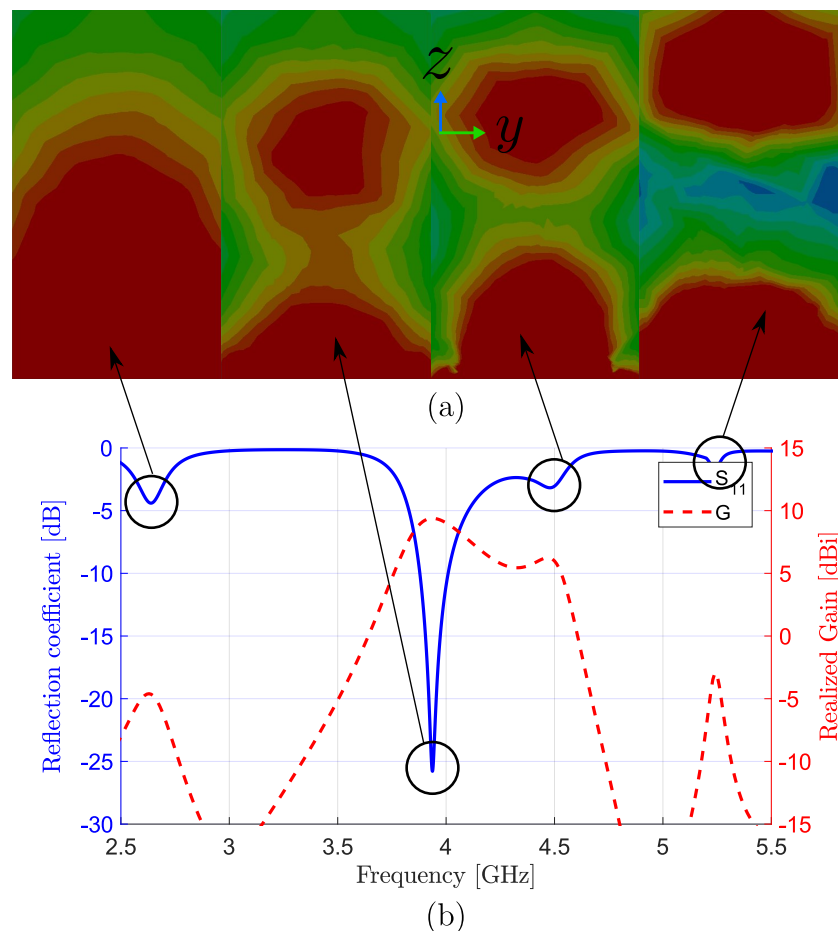
**Figure 2.** (a) 3D view of DRA Unit cell and (b) top view with transparent resonator.

The next step is to add the feeding network to have the unit cell for the linear DRA array. To create such a unit cell, feed and center patches with dimensions of  $61.5 \times 17$  mm ( $L_p \times W_p$ ) and  $15 \times 17$  mm ( $L_{cp} \times W_p$ ) were introduced with a gap of  $X_g = 1.4$  mm between them, as shown in Figure 2. The designed dielectric resonator was placed above the center patch with an overlapping distance ( $X_d = 4.2$  mm) between resonator and feed patch, which is needed for sufficient coupling between resonator and feed patch. A  $50 \Omega$  coaxial probe was placed at an offset distance of  $X_o = 7.6$  mm from the center of the feed patch for proper impedance matching.

The simulated field distribution of  $TE_{113}$  mode in the H-plane ( $y$ - $z$  plane) inside the DRA at the resonance frequency of 3.9 GHz is shown in Figure 3, along with the reflection coefficient and gain as a function of frequency. Figure 3a shows interested mode  $TE_{113}$

excited at 3.9 GHz and three other neighbor resonant modes at frequencies of 2.6, 4.5, and 5.2 GHz, which correspond to  $TE_{111}$ ,  $TE_{113}$ , and a hybrid mode, respectively. The design and coaxial probe can be easily readjusted to match any of these resonances. The second and third modes were a single  $TE_{113}$ , which was split into two resonances due to the impedance mismatching. Hence, by changing the antenna element, matching can be enhanced, and modes come closer which needs a larger bandwidth; however, this is omitted here, as the main contribution for the paper is array feeding and not element design. The antenna produced a peaked gain of 9.3 dBi in the boresight direction ( $\theta = 0^\circ$ ), which outperformed DRA elements operating at  $TE_{113}$  [39,40]. This illustrates the efficient feeding scheme of the standing wave, even for a single-element DRA antenna.

The dimensions were optimized for maximal gain using high-frequency structure simulator (HFSS) [41]. The design was simulated under the driven modal on the basis of the finite element method (FEM) and adaptive meshing. The convergence condition was set to achieve target delta S-parameters below 2%, which implied dividing the structure into 20 to 40 thousand tetrahedral meshes for single and four elements, respectively. The used boundary conditions are absorbing boundary condition (ABC) for a surrounding air box that is a quarter wavelength farther away than the antenna edges. Metal feed and center patches were approximated with the perfect electric conductor (PEC) boundary condition during optimization, and were replaced by normal copper units with a thickness of 35  $\mu\text{m}$  at the final simulations.



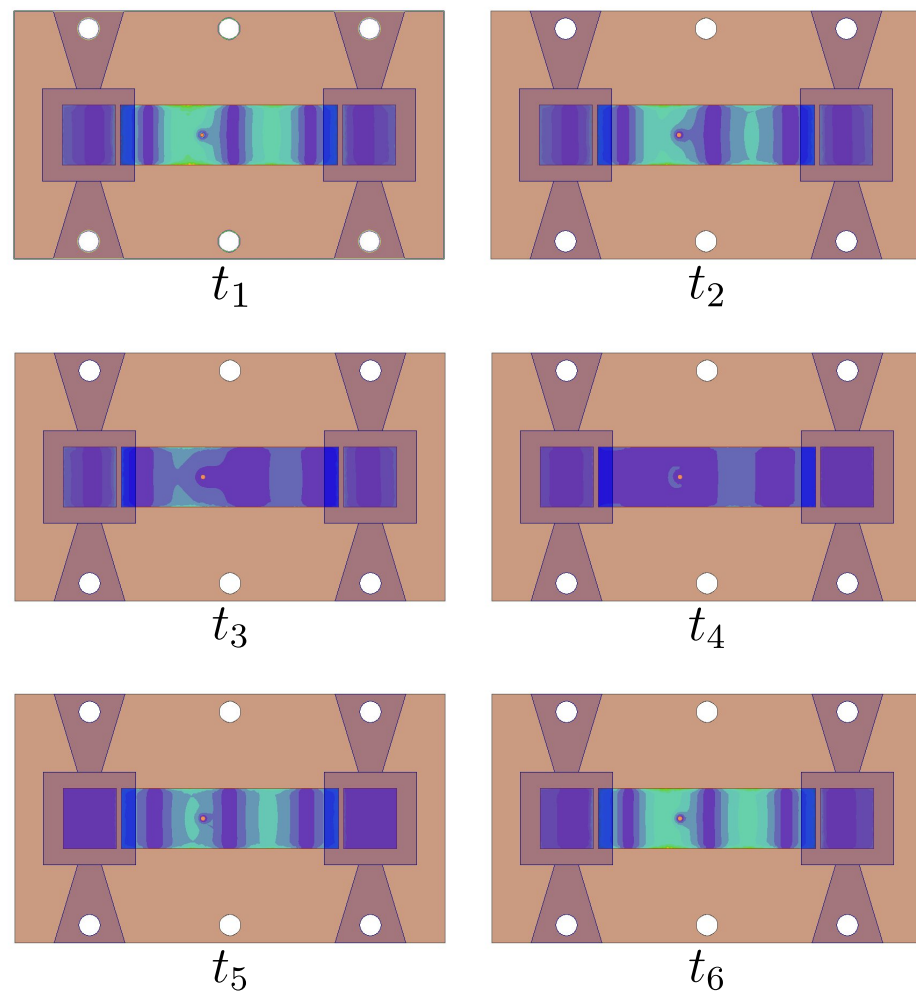
**Figure 3.** (a) Field distribution of  $TE_{113}$  mode at 3.9 GHz and neighboring resonant modes inside DRA. (b) Simulated  $S_{11}$  and gain vs. frequency of antenna element.

### 3. Two-Element Standing-Wave Linear Array

In this section, a  $1 \times 2$  linear array based on the standing-wave feed method is presented. To form the two-element array, the unit cell in Figure 2 is replicated twice. Since the

second cell was the end element of the array, there was no need to add another feed patch at the right of the second element, as the feed patch at the middle would already feed the two elements. Hence, for a general  $1 \times N$  element array, we needed  $N$  center patches lying underneath each dielectric resonator and  $N - 1$  feed patches to uniformly deliver energy to all elements.

A standing wave is formed when two waves travel in opposite directions with an equal magnitude within the feeding network, where null locations do not move. Figure 4 shows the fixed places of null field points in the feeding network. Simulation results are shown in Figure 5, where a maximal realized gain of about 12 dBi was obtained at the resonant frequency. Such a high gain is 2.7 dB over the single-element gain.



**Figure 4.** Snapshots of electric field distribution in proposed array demonstrating standing-wave excitation in the feed network.

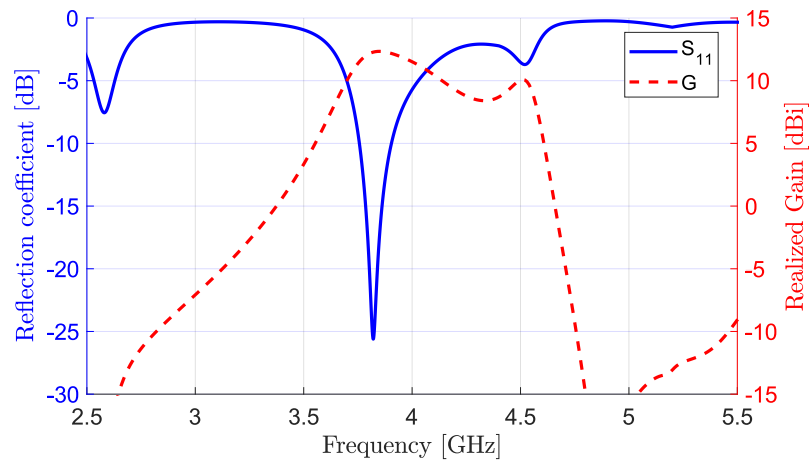


Figure 5. Simulated  $S_{11}$  and gain vs. frequency of the proposed two-element standing-wave DRA array.

#### 4. Four-Element Standing-Wave Linear Array

The proposed configuration was extended to create a four-element linear array by adding two more unit cells to the two-element design as shown in Figure 6. Considering that the number of elements ( $N$ ) was 4, and following our discussion above, the four-element array consists of 4 dielectric resonators lying above 4 center patches with 3 connecting feed patches. The optimized geometrical parameters, as summarized in Table 1, remained almost the same as the number of array elements increased. Such a feature provides a convenient design procedure for various array sizes.

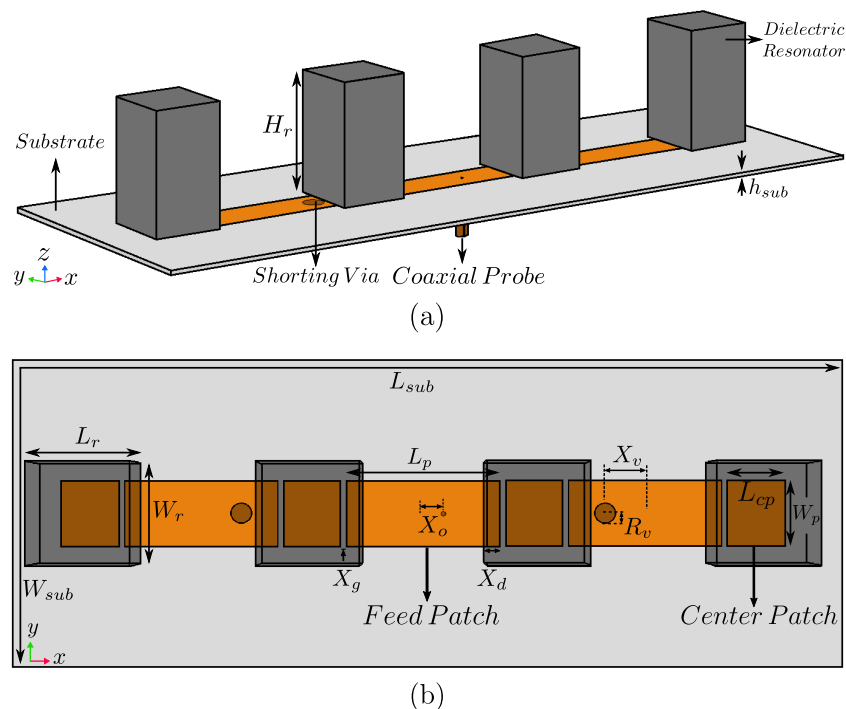


Figure 6. Schematic diagram of proposed four-element standing-wave DRA array: (a) 3D view and (b) top view with transparent resonators.

**Table 1.** Geometrical parameters of DRA array (unit: mm).

$L_{\text{sub}}$	$W_{\text{sub}}$	$h_{\text{sub}}$	$L_r$	$W_r$	$H_r$	$L_p$
280	70	1.52	26.2	26.2	45.8	61.5
$L_{\text{cp}}$	$W_p$	$X_g$	$X_o$	$X_d$	$R_v$	$X_v$
15	17	1.4	7.6	4.2	4	22

In a standing-wave array, the entire array acts as a single large resonator; hence, more than one mode can be strongly excited near the operating frequency, especially in a large array. Unfortunately, some of the excited modes do not produce radiation in the intended direction. Figure 7a presents the field distribution and 3D radiation pattern of the array, being red, yellow, green, and blue colors represent the strength from the max to the minimum. It shows such an example where the fields of the two end elements are in the opposite direction to those of the two inner elements, producing diminished radiation in the boresight direction. To eliminate such unwanted modes, shorting pins are used. Figure 7b shows that the added pins suppress those undesirable modes to give more uniform fields among all array elements for maximal directivity.

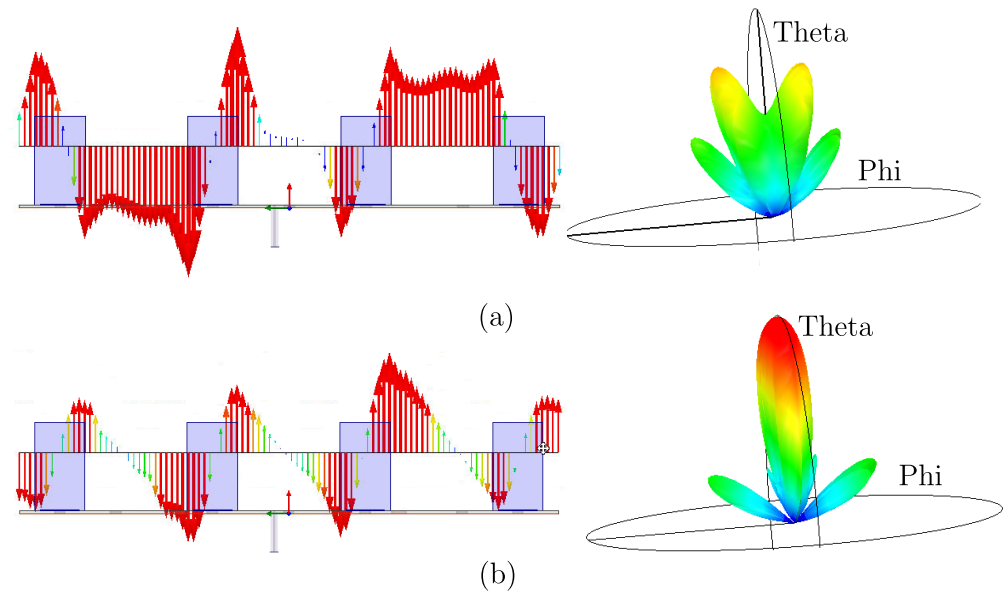
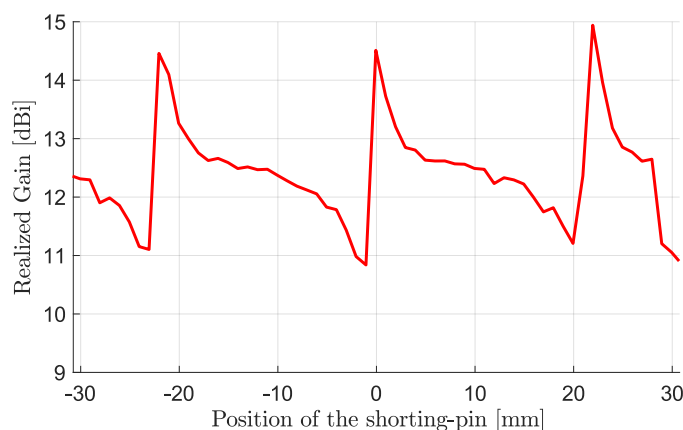
**Figure 7.** Field distribution and radiation pattern of proposed four-element DRA array (a) without and (b) with shorting pins.

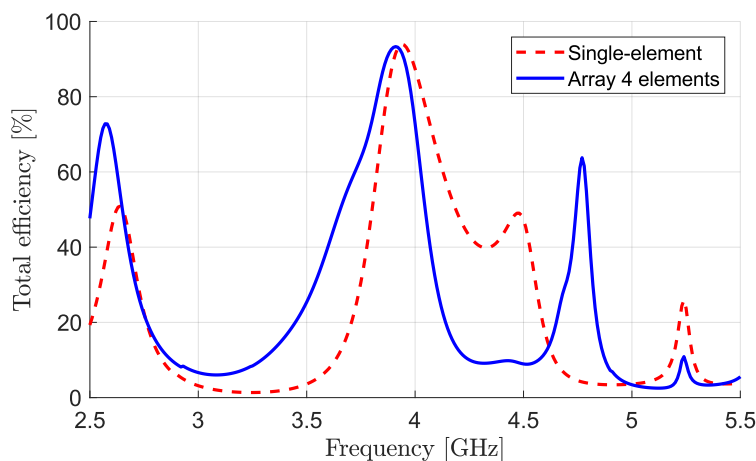
Figure 8 presents the effect of the shorting-pin position on the array gain. The three pin positions for maximal gain indicate three null electric-field points of the desired mode under the patch because the presence of the pins does not affect the field distribution optimal for gain, but puts down other undesirable modes with finite field strength at the pin location. The radius of the shorting pins was also optimized, so that the undesired modes become eliminated as much as possible, while the selected mode is least affected by the vias.





**Figure 8.** Gain of four-element antenna vs. position of shorting pin along feed patch.

The simulated total efficiency of the four-element design is shown in Figure 9. High efficiency of about 93% was achieved for the four-element array at the resonant frequency, which was only 1% less than that of the single-element design. This demonstrates the benefit of the proposed feeding technique compared to other feeding methods that introduce extra losses in the array structure, resulting in a reduction in antenna efficiency.

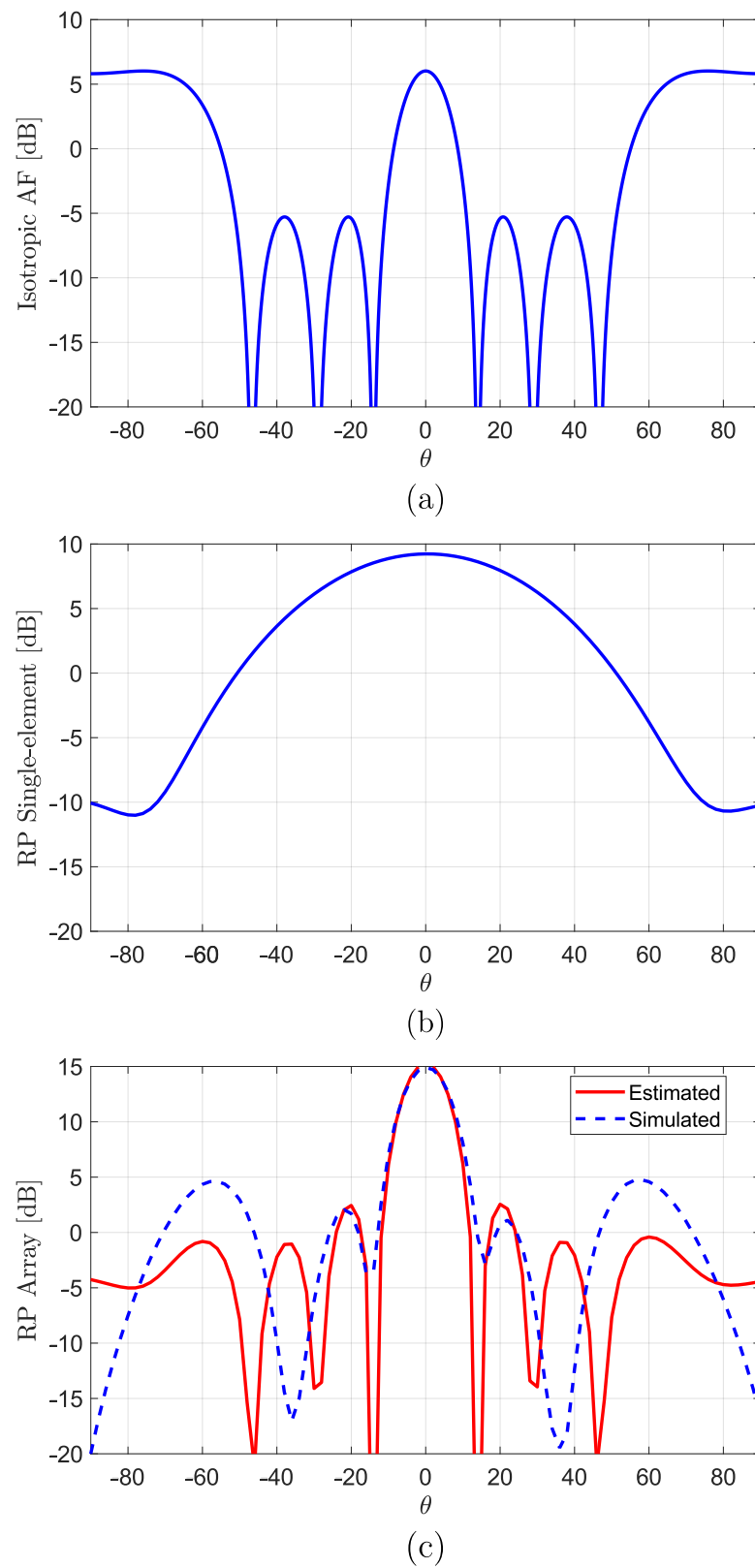


**Figure 9.** Efficiency of proposed DRA array.

For comparison purposes and to validate the performance of the proposed array feeding method, the array factor for an ideal array was estimated, as is shown in Figure 10a. Hence, four equispaced isotropic elements with the same element spacing as the proposed array and fed with the same amplitude and phase. With this, an upper limit of the gain improvement could be estimated.

Such array factor can be added (in dB) to the actual radiation patterns of the array element (Figure 10b) to compute the estimated total pattern of the array in such an ideal case (uniform feeding to all antenna elements). Figure 10c demonstrates that the proposed feeding method efficiently excites the four elements as the actual simulated radiation patterns of the array are in excellent agreement with the theoretical estimated especially near the boresight. It is clear that the simulated one provided a peak gain of about 15 dBi, which was almost equal to the upper theoretical limit. In other words, the gain enhancement for the four-element array over that of a single element is 5.7 dB, which is approximately equal to the theoretical array gain of a four isotropic-element array with the same element spacing of  $1.03 \lambda_0$  [42].





**Figure 10.** (a) Theoretical array factor of four isotropic sources; (b) simulated element factor; and (c) simulated and estimated radiation pattern of proposed DRA array.

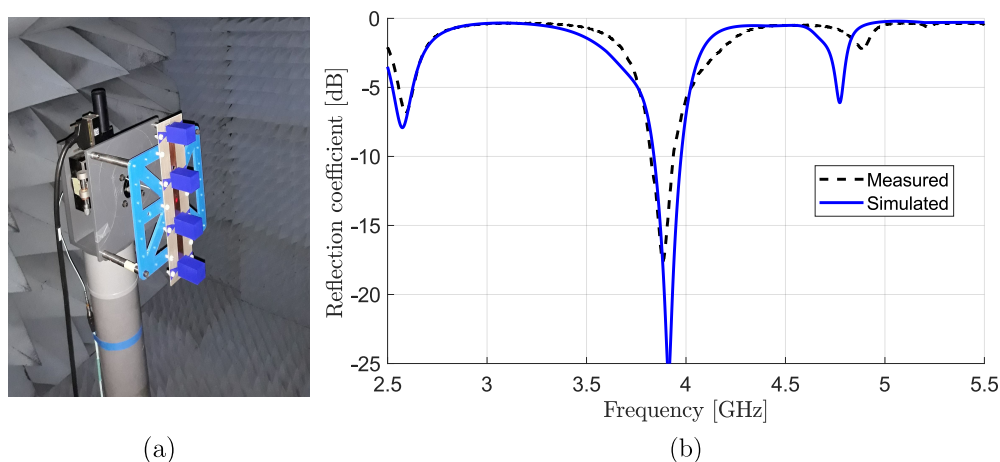
## 5. Fabrication and Measurements

A four-element standing-wave DRA array was fabricated (Figure 11a) using 3D printing, which is a promising technique for antennas at microwave ranges [43,44]. Two small arms were included in each dielectric element to ensure accurate alignment. Simulated and measured reflection coefficients, and realized gain were in excellent agreement, as shown in Figure 11b.

For gain and radiation pattern measurements, the DRA array was adjusted in an anechoic chamber in the receiving mode with transmitting the signal from the vector network analyzer (VNA) through a standard commercial horn. The spacing between the two antennas was selected to ensure that the tested antenna would be in the far-field region. The signal was amplified using a power amplifier before delivering to the horn to compensate the free space and cables losses, and ensure good receiving power levels above the noise floor of the measurement setup [45]. On the basis of the direct comparison method using a third horn with known gain vs. frequency values, the realized gain as a function of frequency of the proposed DRA array was measured, as shown in Figure 12. Compared to a maximal simulated realized gain of 15 dBi, the measured gain showed a value of 14 dBi at the resonant frequency. The difference in gains was due to uncertainties in material properties, as is explained later in this section. The array had an impedance and 3 dB gain bandwidth product of about 4%, which was equal to those of the single-element antenna. In other words, the proposed array feeding method did not reduce either impedance or gain bandwidths.

The simulated and measured radiation patterns of the dielectric array at the resonance frequency in both E- and H-planes were in relatively good agreement (Figure 13). The simulated sidelobe level was about  $-10$  dB, which was the best achievable value of DRA working in  $TE_{113}$  mode [40,46]; however, the measured sidelobe level was lower than that of the simulated. Investigating the possible sources for the mismatching more, and Figures 11 and 12 show that there was a frequency shift up to higher frequency. From this point, it appeared that the reason behind this mismatching was the difference in the dielectric properties of polylactic acid (PLA) due to 3D printing conditions.

Despite the fact that PLA dielectric constant should be about 3.5 at a frequency range around 4 GHz [37,38], the value practically depends on 3D manufacturing properties such as printing temperature [47] and printing resolution [48]. Hence, by considering actual manufacturing conditions (printing temperature of  $220$  °C and layer thickness of  $50$   $\mu\text{m}$ ) and at the used frequency band, the dielectric constant would be affected to be slightly smaller (around 2.7) [47–50].



**Figure 11.** (a) Manufactured prototype of four-element DRA array. (b) Measured and simulated  $S_{11}$  of manufactured four-element standing-wave DRA array prototype.

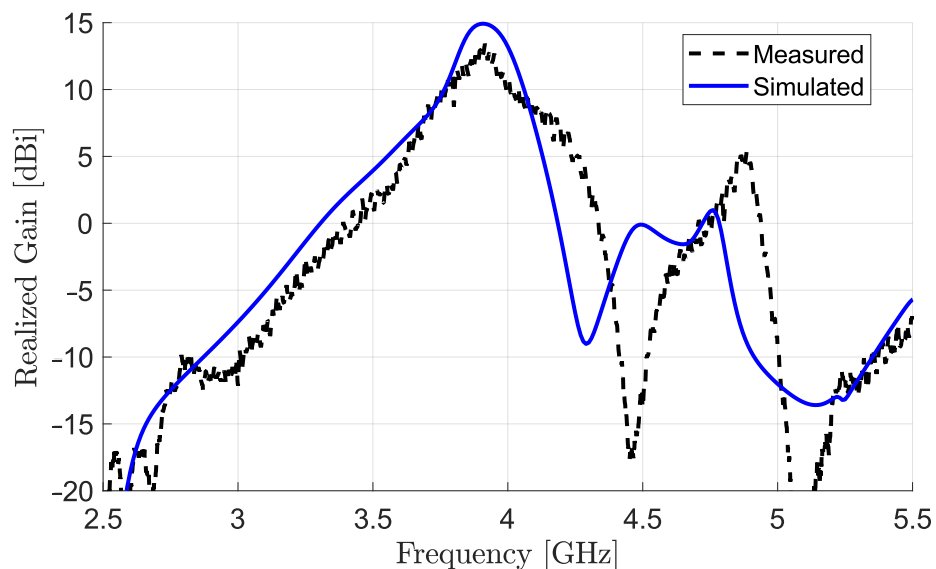


Figure 12. Simulated and measured realized gain of four-element standing-wave DRA array.

To see the effect of such changes in the dielectric constant, the array was resimulated using the new estimated dielectric constant. The resimulated and measured gain and radiation patterns were in excellent agreement, as shown in Figure 14.

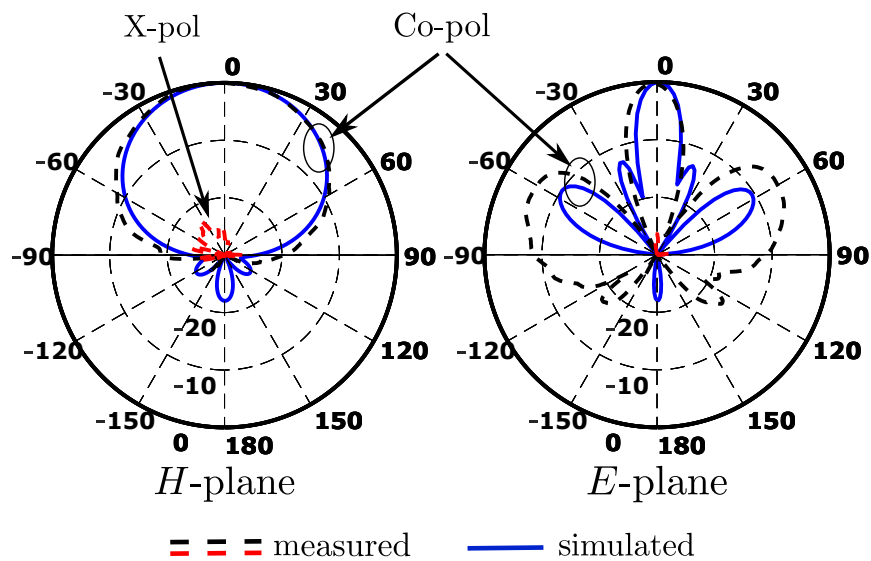
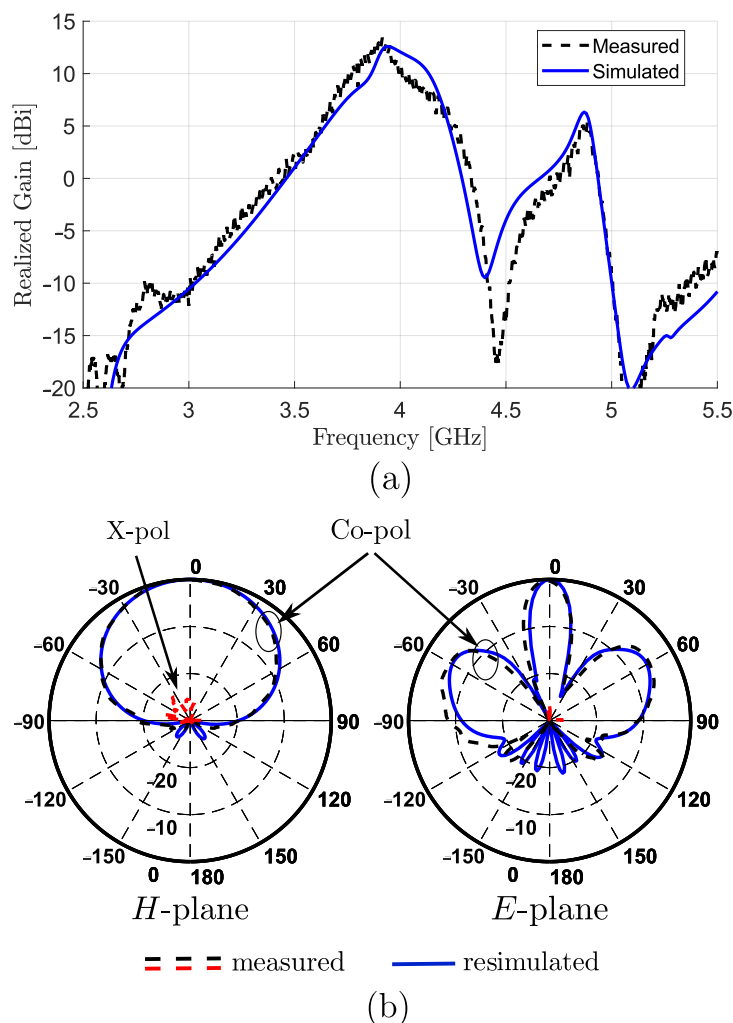


Figure 13. Simulated and measured radiation patterns of four-element standing-wave DRA array.



**Figure 14.** Resimulated and measured: (a) realized gain; (b) radiation patterns after considering mismatching in dielectric characteristics.

Table 2 shows a comparison of the four-element dielectric array based on the proposed feeding scheme with those of the state-of-the-art feeding techniques for DRA arrays with highlighting their drawbacks in red. The proposed feeding method showed a significant gain improvement of about 3 to 6.5 dB compared with recently reported designs of other feeding schemes. It also remarkably enhanced efficiency compared to standard microstrip lines or DIG feeds. Moreover, in comparison to DIG or SIW, the proposed feeding produced a comparable gain that was provided by the 4 times greater number of elements, which resulted in a very compact design of about 10% of the size of other feeds, in addition to a decrease in cost and complexity. Even for our previous work based on standing-wave feeding [36] which successfully achieved most of the previously mentioned advantages, the feed in this paper is more compact as a similarly high gain of 14 dBi was achieved here by 4 elements ( $2\lambda^3$ ), while 9 elements ( $18.7\lambda^3$ ) are needed for the previous feeding method to achieve a comparable gain of 14 dBi. Regarding the impedance and 3 dB gain bandwidth (BW) product, the proposed feed showed comparable BW to SIW, microstrip lines, and standing-wave feeding methods with lower BW compared to DIG and parasitic methods. However, due to the previously mentioned advantage, the proposed feeding still presented the best overall performance. Additionally, as confirmed in Section 5, this feeding did not degrade array performance, so larger BW could easily be achieved by updating the array element using any standard DRA bandwidth enhancement techniques, as is briefly discussed in Section 6; the proposed array would then have as large a bandwidth as that of the array element.

**Table 2.** Comparison of proposed standing-wave DRA array with arrays based on state-of-the-art feeding techniques.

Ref	DRA Array Feeding Method	No. of Elements	Gain @ $f_0$ (dBi)	Antenna Size ( $\lambda^3$ )	Impedance/Gain BW Product (%)	Efficiency @ $f_0$ (%)
[31]	Parasitic	3	9.25	0.89(1.5 × 1 × 0.59)	9	92
[23]	SIW	4	10.6	1(1.13 × 3.5 × 0.26)	5	93
[16]	Microstrip lines	4	10	0.9(2.5 × 2.13 × 0.17)	3	85
[25]	DIG	7	7.61	15.4(4.66 × 9.77 × 0.34)	10	64.6
[24]	SIW	8	11.5	11(8.4 × 6.3 × 0.21)	2	85
[36]	Standing-wave	9	15	18.7(4.11 × 3.73 × 1.22)	7	91
[25]	DIG	15	12.46	25.2(4.66 × 16 × 0.34)	15	63
This work	Standing-wave	2	12	0.9(0.91 × 1.58 × 0.61)	4	93
This work	Standing-wave	4	14	2(0.91 × 3.64 × 0.61)	4	93

## 6. Conclusions and Future Work

In this paper, a high-gain linear DRA array with a standing-wave feed network is presented without the need of using power dividers, transitions, or launchers. The proposed feed technique provided relatively high gain and excellent efficiency compared with those of standard feeding methods. Such attractive features come in addition to a simple and compact design with a straightforward impedance-matching procedure, similar to that of regular microstrip antennas. Arrays based on the proposed feeding method with a different number of elements were presented with manufacturing a four-elements array with low-cost 3D-printing technology. Good agreement was realized between the simulated and measured results with a peak measured gain of 14 dBi. The small deviation between theory and experiments was investigated and was due to changes in the dielectric properties of the resonator material depending on 3D manufacturing properties.

Possible extensions for the work are divided into three main research lines. First, improving the bandwidth, which can be achieved by designing an array on the basis of the same feeding method but using different DRA array element shapes. For example, using an element consisting of multiple dielectric slabs instead of the standard rectangle one to increase the bandwidth (can provide an improvement around 3 times) or using metallic patches as the superstrate. Second, improving the gain even further by using pyramidal horns instead of rectangle resonators. Lastly, scaling the design to work at higher frequencies such as mm wave ranges.

**Author Contributions:** K.A.A., simulation, manufacturing and measurements, writing, A.A.A.; simulation and writing, C.S.L.; analysis methodology, supervision, funding, G.S.B.; manufacturing, E.F.-G. and L.E.G.-C.; review and editing, and funding, L.E.G.-M.; supervision. All authors have read and agreed to the published version of the manuscript.

**Funding:** This research was funded by Fundación SENER (REFTA), Comunidad de Madrid MARTINLARA-CM (P2018/NMT-4333), Agencia Estatal de Investigacion (PID2019-109984RB-C41), and RTC2017-6394-7 projects.

**Institutional Review Board Statement:** Not applicable.

**Informed Consent Statement:** Not applicable.

**Data Availability Statement:** Not applicable.

**Conflicts of Interest:** the authors declare no conflict of interest.

## References

1. Kajfez, D.; Guillon, P. *Dielectric Resonators*; Artech House Microwave Library, Artech House: London, UK, 1986.
2. Long, S.; McAllister, M.; Shen, L. The resonant cylindrical dielectric cavity antenna. *IEEE Trans. Antennas Propag.* **1983**, *31*, 406–412. [[CrossRef](#)]
3. Brown, E.R.; Abdalmalak, K.A.; Zhang, W. Effect of Metal Resistive Losses on the Gain of a THz Planar Spiral Antenna. In Proceedings of the 2020 14th European Conference on Antennas and Propagation (EuCAP), Copenhagen, Denmark, 15–20 March 2020; pp. 1–4.
4. Kesavan, A.; Al-Hassan, M.; Ben Mabrouk, I.; Denidni, T.A. Wideband Circular Polarized Dielectric Resonator Antenna Array for Millimeter-Wave Applications. *Sensors* **2021**, *21*, 3614. [[CrossRef](#)] [[PubMed](#)]
5. Rivera-Lavado, A.; García-Muñoz, L.E.; Lioubtchenko, D.; Preu, S.; Abdalmalak, K.A.; Santamaría-Botello, G.; Segovia-Vargas, D.; Räsänen, A.V. Planar Lens-Based Ultra-Wideband Dielectric Rod Waveguide Antenna for Tunable THz and Sub-THz Photomixer Sources. *J. Infrared Millim. Terahertz Waves* **2019**, *40*, 838–855. [[CrossRef](#)]
6. García-Muñoz, E.; Abdalmalak, K.A.; Santamaría, G.; Rivera-Lavado, A.; Segovia-Vargas, D.; Castillo-Aranibar, P.; Dijk, F.V.; Nagatsuma, T.; Brown, E.R.; Guzman, R.C.; et al. Photonic-based integrated sources and antenna arrays for broadband wireless links in terahertz communications. *Semicond. Sci. Technol.* **2019**, *34*, 054001. [[CrossRef](#)]
7. Warmowska, D.; Abdalmalak, K.A.; Muñoz, L.E.G.; Raida, Z. High-Gain, Circularly-Polarized THz Antenna with Proper Modeling of Structures with Thin Metallic Walls. *IEEE Access* **2020**, *8*, 125223–125233. [[CrossRef](#)]
8. Petosa, A. *Dielectric Resonator Antenna Handbook*; Artech House Antennas and Propagation Library, Artech House: London, UK, 2007.
9. Leung, K.W.; Lim, E.H.; Fang, X.S. Dielectric Resonator Antennas: From the Basic to the Aesthetic. *Proc. IEEE* **2012**, *100*, 2181–2193. [[CrossRef](#)]
10. Gaya, A.; Jamaluddin, M.H.; Ali, I.; Althuwayb, A.A. Circular Patch Fed Rectangular Dielectric Resonator Antenna with High Gain and High Efficiency for Millimeter Wave 5G Small Cell Applications. *Sensors* **2021**, *21*, 2694. [[CrossRef](#)]
11. Petosa, A.; Ittipiboon, A. Dielectric Resonator Antennas: A Historical Review and the Current State of the Art. *IEEE Antennas Propag. Mag.* **2010**, *52*, 91–116. [[CrossRef](#)]
12. Luk, K.; Leung, K. *Dielectric Resonator Antennas*; Antennas, S., Ed.; Research Studies Press: New York, NY, USA, 2003.
13. Abdalmalak, K.A.; Santamaría-Botello, G.; Lee, C.S.; Rivera-Lavado, A.; García-Castillo, L.E.; Segovia-Vargas, D.; García-Muñoz, L.E. Microwave Radiation Coupling into a WGM Resonator for a High-Photonic-Efficiency Nonlinear Receiver. In Proceedings of the 2018 48th European Microwave Conference (EuMC), Madrid, Spain, 23–27 September 2018; pp. 781–784. [[CrossRef](#)]
14. Abdalmalak, K.A.; Botello, G.S.; Suresh, M.I.; Falcón-Gómez, E.; Lavado, A.R.; García-Muñoz, L.E. An Integrated Millimeter-Wave Satellite Radiometer Working at Room-Temperature with High Photon Conversion Efficiency. *Sensors* **2022**, *22*, 2400. [[CrossRef](#)]
15. Petosa, A.; Mongia, R.; Ittipiboon, A.; Wight, J. Investigation of various feed structures for linear arrays of dielectric resonator antennas. In Proceedings of the IEEE Antennas and Propagation Society International Symposium, 1995 Digest, Newport Beach, CA, USA, 18–23 June 1995; Volume 4, pp. 1982–1985. [[CrossRef](#)]
16. Mishra, N.K.; Das, S.; Vishwakarma, D.K. Beam steered linear array of Cylindrical Dielectric Resonator Antenna. *AEU Int. J. Electron. Commun.* **2019**, *98*, 106–113. [[CrossRef](#)]
17. Petosa, A.; Ittipiboon, A.; Cuhaci, M. Array of circular-polarised cross dielectric resonator antennas. *Electron. Lett.* **1996**, *32*, 1742–1743. [[CrossRef](#)]
18. Leung, K.W.; So, K.K. Rectangular waveguide excitation of dielectric resonator antenna. *IEEE Trans. Antennas Propag.* **2003**, *51*, 2477–2481. [[CrossRef](#)]
19. Zhang, Y.; Kishk, A.A.; Yakovlev, A.B.; Glisson, A.W. Analysis of Wideband Dielectric Resonator Antenna Arrays for Waveguide-Based Spatial Power Combining. *IEEE Trans. Microw. Theory Tech.* **2007**, *55*, 1332–1340. [[CrossRef](#)]
20. Eshrah, I.A.; Kishk, A.A.; Yakovlev, A.B.; Glisson, A.W. Excitation of dielectric resonator antennas by a waveguide probe: modeling technique and wide-band design. *IEEE Trans. Antennas Propag.* **2005**, *53*, 1028–1037. [[CrossRef](#)]
21. Leung, K.W.; Lo, H.Y.; So, K.K.; Luk, K.M. High-permittivity dielectric resonator antenna excited by a rectangular waveguide. *Microw. Opt. Technol. Lett.* **2002**, *34*, 157–158. [[CrossRef](#)]
22. Xu, F.; Wu, K. Guided-wave and leakage characteristics of substrate integrated waveguide. *IEEE Trans. Microw. Theory Tech.* **2005**, *53*, 66–73. [[CrossRef](#)]
23. Abdel-Wahab, W.M.; Busuioc, D.; Safavi-Naeini, S. Millimeter-Wave High Radiation Efficiency Planar Waveguide Series-Fed Dielectric Resonator Antenna (DRA) Array: Analysis, Design, and Measurements. *IEEE Trans. Antennas Propag.* **2011**, *59*, 2834–2843. [[CrossRef](#)]
24. Abdallah, M.S.; Wang, Y.; Abdel-Wahab, W.M.; Safavi-Naeini, S. Design and Optimization of SIW Center-Fed Series Rectangular Dielectric Resonator Antenna Array with 45 Linear Polarization. *IEEE Trans. Antennas Propag.* **2018**, *66*, 23–31. [[CrossRef](#)]
25. Al-Zoubi, A.S.; Kishk, A.A.; Glisson, A.W. A Linear Rectangular Dielectric Resonator Antenna Array Fed by Dielectric Image Guide with Low Cross Polarization. *IEEE Trans. Antennas Propag.* **2010**, *58*, 697–705. [[CrossRef](#)]
26. Al-Zoubi, A.; Kishk, A.; Glisson, A.W. Slot-aperture-coupled linear dielectric resonator array fed by dielectric image line backed by a reflector. In Proceedings of the 2008 IEEE Antennas and Propagation Society International Symposium, San Diego, CA, USA, 5–11 July 2008; 2008; pp. 1–4. [[CrossRef](#)]



27. Wyville, M.; Petosa, A.; Wight, J. DIG feed for DRA arrays. In Proceedings of the 2005 IEEE Antennas and Propagation Society International Symposium, Washington, DC, USA, 3–8 July 2005; Volume 2A, pp. 176–179. [CrossRef]
28. Petosa, A.; Ittipiboon, A.; Antar, Y.M.M.; Roscoe, D.; Cuhaci, M. Recent advances in dielectric-resonator antenna technology. *IEEE Antennas Propag. Mag.* **1998**, *40*, 35–48. [CrossRef]
29. Elkarkraoui, T.; Delisle, G.Y.; Hakem, N.; Coulibaly, Y. High gain cross DRA antenna array for underground communications. In Proceedings of the 2014 IEEE Antennas and Propagation Society International Symposium (APSURSI), Memphis, TN, USA, 6–11 July 2014; pp. 1942–1943. [CrossRef]
30. Elkarkraoui, T.; Hakem, N.; Delisle, G.Y.; Coulibaly, Y. A Novel Design Approach for a 60 GHz Circularly Polarized EBG Antenna. *Prog. Electromagn. Res.* **2016**, *69*, 37–51. [CrossRef]
31. Shahadan, N.H.; Jamaluddin, M.H.; Kamarudin, M.R.; Yamada, Y.; Khalily, M.; Jusoh, M.; Dahlan, S.H. Steerable Higher Order Mode Dielectric Resonator Antenna With Parasitic Elements for 5G Applications. *IEEE Access* **2017**, *5*, 22234–22243. [CrossRef]
32. Movahedinia, R.; Sebak, A.R.; Chaharmir, M.R.; Ranjbar Nikkhah, M.; Kishk, A.A. X-Band Circularly Polarized Electronically Steerable Parasitic Array Radiator of DRA. *IEEE Trans. Antennas Propag.* **2018**, *66*, 721–728. [CrossRef]
33. Rivera-Lavado, A.; García-Muñoz, L.E.; Generalov, A.; Lioubtchenko, D.; Abdalmalak, K.A.; Llorente-Romano, S.; García-Lampérez, A.; Segovia-Vargas, D.; Räisänen, A.V. Design of a Dielectric Rod Waveguide Antenna Array for Millimeter Waves. *J. Infrared Millim. Terahertz Waves* **2017**, *38*, 33–46. [CrossRef]
34. Bhartia, P.; Bahl, I. *Millimeter Wave Engineering and Applications*; A Wiley-Interscience Publication; Wiley: Seoul, Korea, 1984.
35. Lakshmanan, A.; Lee, C.S. A Standing-Wave Microstrip Array Antenna. *IEEE Trans. Antennas Propag.* **2011**, *59*, 4858–4861. [CrossRef]
36. Althuwayb, A.A.; Abdalmalak, K.A.; Lee, C.S.; Santamaría-Botello, G.; García-Castillo, L.E.; Segovia-Vargas, D.; García-Muñoz, L.E. 3-D-Printed Dielectric Resonator Antenna Arrays Based on Standing-Wave Feeding Approach. *IEEE Antennas Wirel. Propag. Lett.* **2019**, *18*, 2180–2183. [CrossRef]
37. Huber, E.; Mirzaee, M.; Bjorgaard, J.; Hoyack, M.; Noghianian, S.; Chang, I. Dielectric property measurement of PLA. In Proceedings of the 2016 IEEE International Conference on Electro Information Technology (EIT), Grand Forks, ND, USA, 19–21 May 2016; pp. 0788–0792. [CrossRef]
38. Kumar, P.; Dwari, S.; Utkarsh.; Singh, S.; Kumar, J. Investigation and Development of 3D Printed Biodegradable PLA as Compact Antenna for Broadband Applications. *IETE J. Res.* **2020**, *66*, 53–64. [CrossRef]
39. Fang, X.S.; Chow, C.K.; Leung, K.W.; Lim, E.H. New single-/dual-mode design formulas of the rectangular dielectric resonator antenna using covariance matrix adaptation evolutionary strategy. *IEEE Antennas Wirel. Propag. Lett.* **2011**, *10*, 734–737. [CrossRef]
40. Petosa, A.; Thirakoune, S. Rectangular Dielectric Resonator Antennas With Enhanced Gain. *IEEE Trans. Antennas Propag.* **2011**, *59*, 1385–1389. [CrossRef]
41. ANSYS Simulation Driven Product Development, HFSS. Available online: <https://www.ansys.com/> (accessed on 1 February 2022).
42. Balanis, C.A. *Antenna Theory: Analysis and Design*; John Wiley & Sons: Hoboken, NJ, USA, 2016.
43. Kremer, H.I.; Leung, K.W.; Wong, W.C.; Lo, K.K.W.; Lee, M.W.K. Design of Dielectric Resonator Antenna Using Dielectric Paste. *Sensors* **2021**, *21*, 4058. [CrossRef] [PubMed]
44. Abdalmalak, K.A.; Botello, G.S.; Llorente-Romano, S.; Rivera-Lavado, A.; Flygare, J.; Fernández, J.A.L.; Puente, J.M.S.; García-Castillo, L.E.; Segovia-Vargas, D.; Pantaleev, M.; et al. Ultrawideband Conical Log-Spiral Circularly Polarized Feed for Radio Astronomy. *IEEE Trans. Antennas Propag.* **2020**, *68*, 1995–2007. [CrossRef]
45. Lamkaddem, A.; El Yousfi, A.; Abdalmalak, K.A.; Posadas, V.G.; Segovia-Vargas, D. Circularly Polarized Miniaturized Implantable Antenna for Leadless Pacemaker Devices. *IEEE Trans. Antennas Propag.* **2022**, *1*. [CrossRef]
46. Petosa, A.; Thirakoune, S.; Ittipiboon, A. Higher-order modes in rectangular DRAs for gain enhancement. In Proceedings of the 2009 13th International Symposium on Antenna Technology and Applied Electromagnetics and the Canadian Radio Science Meeting, Banff, AB, Canada, 15–18 February 2009, pp. 1–4. [CrossRef]
47. Dichtl, C.; Sippel, P.; Krohns, S. Dielectric properties of 3D printed polylactic acid. *Adv. Mater. Sci. Eng.* **2017**, *2017*, 6913835. [CrossRef]
48. Veselý, P.; Tichý, T.; Šefl, O.; Horynová, E. Evaluation of dielectric properties of 3D printed objects based on printing resolution. *IOP Conf. Ser. Mater. Sci. Eng.* **2018**, *461*, 012091. [CrossRef]
49. Abdalmalak, K.A. Analysis and Design of Antennas and Radiometers for Radio Astronomy Applications in Microwave, Mm-wave, and THz Bands. Ph.D. Thesis, Universidad Carlos III de Madrid, Madrid, Spain, 2022.
50. Zhang, S.; Njoku, C.C.; Whittow, W.G.; Vardaxoglou, J.C. Novel 3D printed synthetic dielectric substrates. *Microw. Opt. Technol. Lett.* **2015**, *57*, 2344–2346. [CrossRef]