

Review



Field-Programmable Gate Array (FPGA)-Based Lock-In Amplifier System with Signal Enhancement: A Comprehensive Review on the Design for Advanced Measurement Applications

Jose Alejandro Galaviz-Aguilar ^{1,†}^(D), Cesar Vargas-Rosales ^{1,†}^(D), Francisco Falcone ^{1,2,†}^(D) and Carlos Aguilar-Avelar ^{3,*,†}^(D)

- ¹ Tecnologico de Monterrey, School of Engineering and Science, Monterrey 64849, Mexico; galaviz@tec.mx (J.A.G.-A.); cvargas@tec.mx (C.V.-R.); francisco.falcone@tec.mx (F.F.)
- ² Institute of Smart Cities, Universidad Pública de Navarra, Campus Arrosadía, E-31006 Pamplona, Spain
- ³ Facultad de Ingeniería, Universidad Autónoma de Baja California, Mexicali 21280, Mexico
- * Correspondence: aguilarav@uabc.edu.mx; Tel.: +52-686-841-8235 (ext. 44429)
- [†] These authors contributed equally to this work.

Abstract: Lock-in amplifiers (LIAs) are critical tools in precision measurement, particularly for applications involving weak signals obscured by noise. Advances in signal processing algorithms and hardware synthesis have enabled accurate signal extraction, even in extremely noisy environments, making LIAs indispensable in sensor applications for healthcare, industry, and other services. For instance, the electrical impedance measurement of the human body, organs, tissues, and cells, known as bioelectrical impedance, is commonly used in biomedical and healthcare applications because it is non-invasive and relatively inexpensive. Also, due to its portability and miniaturization capabilities, it has great potential for the development of new point-of-care and portable testing devices. In this document, we highlight existing techniques for high-frequency resolution and precise phase detection in LIA reference signals from field-programmable gate array (FPGA) designs. A comprehensive review is presented under the key requirements and techniques for single- and dual-phase digital LIA architectures, where relevant insights are provided to address the LIAs' digital precision in measurement system configurations. Furthermore, the document highlights a novel method to enhance the spurious-free dynamic range (SFDR), thereby advancing the precision and effectiveness of LIAs in complex measurement environments. Finally, we summarize the diverse applications of impedance measurement, highlighting the wide range of fields that can benefit from the design of high performance in modern measurement technologies.

Keywords: additive white Gaussian noise (AWGN); lock-in amplifiers (LIAs); field-programmable gate array (FPGA); phase sensitive detector (PSD); spurious-free dynamic range (SFDR)

1. Introduction

In many scientific and industrial applications, there is a need to measure or extract a signal with an amplitude that is much smaller than the noise component present in the environment [1–3]. The development in the design and manufacturing of sensors has led to a significant increase in their electronic sensitivity, such as that needed in integrated solutions based on lock-in amplifiers (LIAs), which is a rigorous yet practical framework for electronic measurements, considered fundamental for instrumentation, design applications, and characterization in modern physical environments. Field-programmable gate



Academic Editor: Evangelos V Hristoforou

Received: 8 November 2024 Revised: 10 January 2025 Accepted: 17 January 2025 Published: 20 January 2025

Citation: Galaviz-Aguilar, J.A.; Vargas-Rosales, C.; Falcone, F.; Aguilar-Avelar, C. Field-Programmable Gate Array (FPGA)-Based Lock-In Amplifier System with Signal Enhancement: A Comprehensive Review on the Design for Advanced Measurement Applications. *Sensors* **2025**, *25*, 584. https://doi.org/10.3390/s25020584

Copyright: © 2025 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https://creativecommons.org/ licenses/by/4.0/).

2 of 24

arrays (FPGAs) have emerged as indispensable tools in the design of advanced digital LIAs used in precision measurement applications. Their inherent flexibility, high-speed processing capabilities, and parallel architecture make FPGAs particularly well suited for the computational demands of digital signal processing and real-time analysis.

In addition to computational efficiency, FPGAs facilitate rapid prototyping and iterative design, which are essential for developing LIAs tailored to specific measurement requirements. For example, in biomedical applications, such as electrical impedance tomography or bioimpedance spectroscopy, the FPGA's ability to handle high-frequency signals and maintain signal integrity across multiple channels is pivotal. Furthermore, the scalability of FPGA-based designs supports their integration into portable and cost-efficient measurement systems, expanding the applicability of LIAs in diverse fields. Another approach is the development of biomedical databases, electronic health records (EHRs), and public health, which have been enhanced not only by availability and traceability but also by the liquidity of heterogeneous healthcare data obtained from several environment sensors [4]. One can find applications of LIAs in every sector of industrial electronics, including the service industry, such as in telecommunications systems, electronics design, healthcare devices, the manufacturing of measurement equipment, and any application where the signal to be measured is several times smaller than the background noise [5-7]. Lock-in amplifier circuit integration, along with the design of sensor elements, has seen a reduction in cost and power consumption [8–12]. Digital LIAs (DLIAs) have become increasingly popular in many experimental configurations due to the combination of flexibility, cost, and performance [13]. Current research efforts on signal acquisition provide solid foundations for the development of embedded design, VLSI systems, and applications with a special emphasis on application-specific integrated circuit (ASIC) integration, for instance, to build smart and fully embedded EEG sensing systems [14,15].

This paper aims to provide an overview to comparatively analyze LIA architectures from the perspective of their design, implementation, and applications to give the reader a general point of view of the importance of a functional digital design. This work discusses the practicality of features of cost-efficient, portable, and digital customizable LIA systems. Hence, the role of lock-in amplifiers and the state of the art of the FPGA system design implementations are reviewed. The rest of this paper is organized as follows. Section 2 describes the fundamentals of LIA systems. Section 3 provides comprehensive and detailed review for the single-phase and dual-phase LIAs architectures and their basic operation. In Section 4, the LIAs digital approach from the perspective of critical design issues and a phase-dithering technique for signal generation enhancement are discussed. Section 4 provides a detailed implementation review of FPGA-based systems. Section 5 presents an overview of the advancements in bioelectrical impedance measurements in biomedical applications. Section 6 provides a discussion of the reviewed systems aimed at feature classification model extraction and final remarks for future research. Finally, Section 7 concludes this paper.

2. Lock-In Amplifier Fundamentals

Mainly, in lock-in detection, a reference signal of the same frequency as the measured signal of interest is needed. The reference signal may be generated in the LIA or given as an external input. A phase-sensitive detector (PSD) identifies the phase difference between the input and reference signals, and phase shifting is performed to ensure that the two signals are in phase. Finally, the amplitude of the input signal that is in phase with the reference signal is obtained [16]. It is termed "lock-in" because it locks to and measures the particular frequency of the reference signal, ignoring all other signals in the input. The operating principle is that an input signal is demodulated by a synchronous

reference signal to produce in-phase or out-of-phase signals through a PSD [3]. In these applications, an LIA is able to perform phase measurements that determine the entire precision of the displacement measurement [17]. In the FPGA-based design, an LIA can provide phase estimate solutions on the accuracy of one reference signal oscillator period. Thus, an advantage of using FPGA-based designs is that, starting from a fixed system clock, the dynamic range of digital-to-time converter (DTC) only needs to cover the residual phase error within one cycle of the output clock [18].

Furthermore, correlation methods have been introduced, mainly to enhance the nonlinearity detrimental effects at the reference signal. This is an approximately linear operating range for the amplifier, and it is called the linear dynamic range (LDR). Some of the main criteria for the evaluation of LIA systems that include low-noise amplifiers and mixers are the maximum power level for which inter-modulation distortion becomes unacceptable and the noise-limited operation of the amplifier. The operating range for which spurious responses are minimal is called the spurious-free dynamic range (SFDR). In [19], H. Fan et al. report a recent study that provides limited digital control to achieve a significant improvement of SFDR in smart sensor systems. Several key performance parameters, such as signal-to-noise ratio (SNR), maximum operating frequency (freq_{max}), sampling frequency, clock frequency, and frequency resolution, are addressed in this paper. These capabilities, comparing both digital and analog LIAs from the current state-of-the-art, are illustrated in Figure 1 and defined in the following subsections.





The features of SFDR and SNR are used to demonstrate the trade-off between spectral leakage performance and hardware complexity, e.g., the direct digital frequency synthesizer (DDFS) design for fundamental signal generation. Similarly, the AC specifications are the most important in evaluating high-speed DAC/ADC settling time, glitch impulse area, distortion, SFDR, and SNR, since they play a critical role in the overall accuracy of the LIA system. The accuracy is a noteworthy advantage of the digital lock-in amplifiers instead of the analog ones, including the frequency synthesis, unwanted signal mitigation, and phase-sensitive detection [20–22]. The aforementioned approach to the DLIA structure has been used in a variety of real-time applications such as medical applications, optical spectroscopy, measuring multiple modulated frequency signals, electrical and electronic applications, and more [23]. The key capabilities outlined in Figure 1 summarize the revised LIA's designs analyzed in this manuscript. The chart highlights critical parameters for the

FPGA-based architecture, including metrics such as signal-to-noise ratio (SNR), maximum sampling frequency, maximum clock frequency, frequency resolution tailored to specific applications, and the operational frequency to low-, mid-, and high-range applications.

Lock-In Amplifier Classification

Addressing the review of LIA architectures is not an easy task, due to the broad range of approaches in their implementation: analog vs. digital, and within digital, based on DSPs, FPGAs, multicore controllers, etc. However, the type of system suited for LIAs can be classified based on the number of mixers used, the architecture incorporated, and the specific application [24]. Lock-in amplifiers in conjunction with PSD are used in instrumentation for their capability of detecting low-amplitude signals affected by interference or noise. FPGA, digital signal processors (DSPs), and microcontroller (MCU) technologies, among others, can help in rapid prototyping and the implementation of low-cost embedded systems while obtaining both high reliability and accuracy. Owing largely to the advancements in modern FPGA devices, which can provide highly integrated hardware resources, digital block features of complex DLIA architectures can be implemented in the same device, resulting in a compact and low-cost acquisition system that is well suited for applications requiring a large number of measurement channels [25,26]. Depending on the PSD method, the lock-in amplifier can be classified based on the architecture [27]. Here, we consider two classes as follows:

- Single-phase instrument: It has a single-PSD branch and a single reference signal. The method multiplies the excited signal by the lock-in reference using a PSD mixer or detector. Then, the PSD output is simply the product of two sine waves, and thus, the result is able to filter the removed unwanted AC signals.
- 2. Dual-phase instrument: It uses two PSD blocks along with two reference signals, one being phase-shifted ninety degrees with respect to the other. It is to be noted that with this configuration, the LIAs are capable of measuring both the in-phase and quadrature components. These components can greatly help in signal measuring and extraction in Cartesian or polar representations.

3. Single- and Dual-Phase Lock-In Amplifiers

The single-phase LIA operation is based on the frequency mixing, and a reference signal is used to single out the component of the input signal at the reference phase and frequency with known amplitudes. Thus, it can easily calculate the phase difference between these; otherwise, it may not be feasible to eliminate the AC component at the mixer output.

3.1. Basic Principle and Architecture

The general design of the lock-in amplifier could be represented at the system level with five building blocks, as shown in Figure 2. One can see the functional diagram block from the illustration, in which the basic architecture is compounded by (i) the stimulus input signal x_{in} , (ii) a reference signal x_{ref} , (iii) a phase-sensitive detector, (iv) a low-pass filter (LPF), and (v) output signal conversion x_{out} . Depending on the intended application and the technology applied, each element can be a custom-hardware, cost-effective, high-performance, and optimized solution. The reference signal x_{ref} will lock in to the input signal x_{in} , which usually comes from a sensor, a circuit previously implemented, a device under test (DUT), or an external input system. The phase-sensitive detector is a circuit that takes two signals at its input and produces an output that is the product of both signals, usually employing a mixer or multiplier. For certain sensor applications, dual-phase LIAs are demonstrated to be best suit, because it is not always possible to produce reference

signals with specific frequencies. In [26], Masciotti et al. proposed the analysis extended for multi-frequency that can be used to identify the limit (if any) to improve the noise immunity by increasing the sampling frequency.



Figure 2. Block diagram of the single-phase LIA: (**a**) overall system, (**b**) conceptual LIA process at the system level.

3.2. Dual-Phase Lock-In Amplifier

The dual-phase method for LIAs is capable of measuring both in-phase and quadrature components by using the mixing principle along with two reference signals, one being 90° shifted from the other. The dual-phase LIAs can obtain the amplitude and phase of the mixing frequency signals [28]. For sensor applications, dual-phase LIAs seem to be better, because sensors are deployed in real-life scenarios, and in some cases they will be prone to severe noise, for example, atmospheric disturbances in weather sensors. However, it is not always possible to produce matched frequency signals [24]. A LIA provides an extremely narrow band-pass filter, which, at the same time, does not suffer from 1/f noise when amplifying. Figure 3 shows a dual-phase block system based on the principle of an orthogonal signal decomposition. Let us consider the amplitude and phase components of an input V_{in} , as shown in Figure 3, and a reference signal V_{ref} , to derive the PSD given as

$$V_1 = V_{in} \cdot \sin(\omega_{in} + \theta_{in}) \cdot V_{ref} \cdot \sin(\omega_{ref}), \tag{1}$$

where ω_{in} is the input signal frequency, and ω_{ref} is the reference signal frequency. According to the trigonometric identity $\sin(x) \cdot \sin(y) = \frac{1}{2} [\cos(x - y) - \cos(x + y)]$, Equation (1) becomes

$$V_1 = \frac{V_{in} \cdot V_{ref}}{2} \bigg[\cos(\omega_{in} - \omega_{ref} + \theta_{in}) - \cos(\omega_{in} + \omega_{ref} + \theta_{in}) \bigg],$$

Then, the signals are applied to a low-pass filter to further signal conditioning, so higher-frequency components are neglected. Thus, the *X* is obtained as follows:

$$X = \frac{V_{in} \cdot V_{ref}}{2} \cos\left(\omega_{in} - \omega_{ref} + \theta_{in}\right),$$
(2)

Similarly, in the other branch of the system, we obtain

$$V_2 = V_{in} \cdot \sin(\omega_{in} + \theta_{in}) \cdot V_{ref} \cdot \cos(\omega_{ref}), \tag{3}$$

and using the trigonometric identity $\sin(x) \cdot \cos(y) = \frac{1}{2} \left[\sin(x - y) + \sin(x + y) \right]$, we can easily modify the Equation (3), to obtain

$$V_{2} = \frac{V_{in} \cdot V_{ref}}{2} \bigg[\sin(\omega_{in} - \omega_{ref} + \theta_{in}) + \sin(\omega_{in} + \omega_{ref} + \theta_{in}) \bigg], \tag{4}$$

The signals are applied to a low-pass filter, so higher-frequency components are neglected. Obtaining *Y* as

$$Y = \frac{V_{in} \cdot V_{ref}}{2} \sin\left(\omega_{in} - \omega_{ref} + \theta_{in}\right),\tag{5}$$

In theory, it is therefore sufficient to determine the expected value (relevant value to be measured), with the values of *X* and *Y*. The magnitude *A* is calculated as $A(t) = \sqrt{X(t)^2 + Y(t)^2}$ and the phase, $\tan(\varphi) = Y/X$, given by

$$\varphi(t) = \arctan\left(Y(t)/X(t)\right),\tag{6}$$

where $\varphi(t)$, is the phase that can be easily extracted from the DUT.



Figure 3. Block diagram of a basic dual-phase LIA design.

4. Digital Assessments: On the FPGA Critical Design Methodology for DLIAs

FPGAs play a critical role in addressing the leverage of modern signal processing algorithms to enhance frequency resolution, improve phase accuracy, and expand operational bandwidths in DLIAs by providing a customization platform for implementing tailored digital LIA architectures. Their capability to integrate direct digital synthesizers (DDS) for precise frequency generation, adaptive filters for noise reduction, and phase-sensitive detection algorithms ensures high-performance operation. Moreover, FPGAs allow for efficient resource utilization, enabling the realization of single- and dual-phase LIA systems with minimal hardware overhead while maintaining real-time processing capabilities. Since digital LIA platform performance needs to satisfy precise signal conditioning requirements, some numerical precision degree is mandatory. Thus, adequate methods for frequency stability, phase-sensitive multiplication, and filtering are also required. A digital approach can jointly provide a computationally much simpler implementation than an analog one such as in [29], which also yields a lower error estimation of the underlying signal amplitude. Furthermore, when designing LIAs in an analog implementation, some errors are difficult to mitigate due to the inherent characteristic of analog electronics, whereas in digital implementations, one can mitigate some of those error sources by modifying digital functional blocks or applying signal enhancement algorithms, thus improving accuracy. The FPGA-based digital LIA promises useful improvements for weak signal detection technology, such as those needed in the fields of electronic science, signal processing, and sensor technologies [30–32]. FPGAs are flexible and robust devices for this purpose, which, in addition to VHDL hardware description language, allow describing through behavior

models by the register-transfer level (RTL) and structure of digital components, such as precise DDS, which is a key component for ASIC design and implementation. For example, in sensors and measurement systems, finite precision controllability for the signal extraction is accomplished, thus reducing some error-phase measurement system imperfections [33,34]. In turn, intrinsic signal noise introduced by detectors, filters, and amplifiers features certain levels of unavoidable noise, and some can be eliminated by improving the generator and/or detector design. We summarize some of the critical reliability requirements with regard to the digital inaccuracy; these features are salient:

- DDS resolution (spectral purity DAC/ADC enhances).
- Low complexity in arithmetic logic (multiplications).
- Signal/noise power contributions (DDS-to-DAC).
- Clock synchronization to uncertainty reduction.
- Total harmonic distortion (mixing process) [35].

An FPGA-based LIA design enables flexible hardware adjustments in the field, resulting in significant cost savings. Note that in the proposed techniques, critical performance is dependent on the reference signal, which becomes of relevant for high precision. Figure 4 sketches a dual-phase DLIA platform with the main modules implemented in FPGA hardware. Thus, DDFS is a key component, especially in instrumentation and measurement, which becomes a functional part for high-precision systems (see [25,36–39]), which is crucial in both single- and dual-phase DLIAs architectures. In DDFS designs, the effect of finite precision on digital sinusoidal frequency synthesizers manifests itself as spurs in the spectral representation of the output sine wave. These effects are directly related to the phase angle precision limitations since the derived phase of the DDFS digital oscillator tends to be periodic in time and to contribute to the generation of harmonics and spurious. These drawbacks can be reduced by considering the following:

- Phase noise in DDS. In digital LIAs, the signal reference needs to determine DDS periodicity accordingly in order to appropriately reduce the phase noise at these frequencies. This can be accomplished by introducing a random signal of suitable variance into the derived phase, thus facilitating the reduction in the likelihood of identical values over time.
- SFDR strength ratio specifications. Spur-reduction techniques state that adding noise into the data path raises the overall noise level within the oscillator, which tends to reduce the noise localization and can provide significant SFDR enhancement.
- Frequency-phase likelihood in DDS. The requirements to reduce spur levels are dependent on many factors. The likelihood of repetition of derived phase values and resulting spurs, for a given angular precision, are closely linked to the ratio of the sampling frequency to the desired output frequency from any DDS source. An integral ratio clearly results in high-level spurious frequencies, while an irrational relationship is less likely to result in highly correlated noise at harmonic frequencies.

4.1. FPGA-Based Lock-In Amplifier System Signal Enhancement

It is well known that a digital LIA structure uses a synthesizer DDS-to-DAC output. DDS contains a digital block called a phase accumulator of 2^n -bit samples, which produces the digital sinusoidal signal. A large word size is needed to produce the low-hertz step size. Ultimately, the phase accumulator outputs to a sine look-up table (LUT). The large word size of the phase accumulator means that the word output to the DDS must be truncated to fit the limits of the DAC's input. This truncation leads to small discontinuities in the generated pattern, creating greater harmonic distortion [35]. These potential issues unavoidably cause deterministic timing errors, often referred to as deterministic jitter, that appear in the output spectrum as spurious tones. A preferred solution is using dither seed

in the generation of the phase accumulator output, which can reduce these "truncation spurs". Fortunately, these imperfections can be mitigated significantly with an efficient spread spectrum technique for a near-optimal spur-reduction performance. To extract enough useful information from the low signal-to noise ratio (SNR) signals, supposing a periodic waveform signal measured as in Equation (7), and, according to a given variance, modeled as the additive Gaussian, the white noise is:

$$x(t) = A \cdot \sin(\omega(t) + \phi) + n(t) \tag{7}$$

$$SNR = 10 \log_{10} \left(\frac{\Lambda}{2\sigma^2}\right) \tag{8}$$

As the approach of this work, we have concentrated on signal enhancement awareness to provide a digital signal conditioning stage as a key design consideration in the signal reference generation module of a typical DLIA. Notice that in the present work [40], the reference signal frequency resolution of 0.0291 Hz is ensured (calculated as $f_{min} = f_s/2^{32}$), and for specific bioelectrical signals under 10 KHz, this is more than enough for these applications. Please also note that in terms of the dynamic reserve (DR) and SFDR, those metrics have a strong relationship to the accuracy of measurement in the capabilities of any LIA system, and can be calculated as follows:

$$\mathrm{DR} = 20\log_{10} V_d / V_s \tag{9}$$

where V_d is the amplitude of the disturbance and V_s is the amplitude of the signal of interest.



Figure 4. DLIA block diagram with main modules.

4.1.1. FPGA-Based Lock-In Detection for Multi-Channel Chemical Species Tomography

A DLIA is based on a quadrature demodulation, by which both the amplitude and phase of the signal can be obtained [25]. The system is implemented using a Nexys 3 development board with an FPGA Xilinx Spartan-6. The LIA reference signals were tuned at 50 kHz. These results validate the feasibility of the proposed system to exploit the properties of FPGA platforms to implement low-profile, low-weight, and low-cost DLIAs. Figure 5 shows the design of the dual-phase lock-in amplifier. The input signal is then converted from analog to digital, and the two reference signals of the same amplitude are used, at the same angular frequency ω , but with 90° offset relative to each other; this to be able to obtain the signal amplitude and phase. By multiplying the input signal with amplitude *A*, with the two reference signals with amplitude *B*, we obtain the in-phase and quadrature components.



Figure 5. Block diagram of an FPGA-based LIA for multi-channel chemical species tomography.

4.1.2. Lock-In Amplifier for Atomic Force Microscopy Systems

In [39], a new efficient method for implementing the multichannel digital lock-in technique is presented, which is able to measure the amplitude and phase of multiple modulated frequency signals to solve the two most important problems in atomic force microscopy (AFM) systems, which are resolution and cost. Nonlinear contact between the tip and sample in tapping-mode AFM systems induces higher harmonics, which may be useful for the extraction of some characteristics of the sample [39]. The FPGA Xilinx Spartan-3 results demonstrate that the proposed architecture is superior to previous structures, especially in the hardware area and power consumption. The design is very similar to the basic dual-phase LIA system, where the reference signal comes from a DDS component on FPGA Xilinx Spartan-3. The input signal in this design is formed by the signal coming from the device under test (DUT), because it is a digital system, and the DUT may be an analog system. To measure the amplitude response of a nonlinear system, the probe should initially be excited by the sinusoidal signal. In a digital LIA, this signal can be realized by the DDS on FPGA and a DAC to convert it into analog form. It is worth mentioning that microscopy is one of the most popular applications of LIAs, used in experimental physics applications to design instruments that measure signals that are affected by a lot of noise [41,42].

4.1.3. FPGA-Based LIA with Sub-ppm Resolution

In [38], Gervasoni et al. reported a synchronous phase-sensitive architecture for sub-ppm resolution measurement system as shown in Figure 6. Here, the two branches are driven by a switch to sampling simultaneously at {ADC1, ADC2}, respectively. Note that gain fluctuations are canceled out by means of a ratio operation between the two amplitudes. The signals are reconstructed in real time using an FPGA to obtain their discrete-time sampled data as x(n)=I(n) + Qi(n) synchronously established by a PLL. The two signal amplitudes (and phases) are calculated with a dual-phase demodulation as in a standard LIA. The realized enhanced-LIA (ELIA) instrument comprises a generation channel, two acquisition channels, and an FPGA, and the measurement frequency can be up to 6 MHz. The design realization is based on a Spartan-6 FPGA from Xilinx (mounted on a module Opal Kelly XEM6010 that includes a PLL, external memory, and USB interface). A PGA provides an attenuation/gain in the range of (-22 to 20 dB). The realized enhanced LIA (ELIA) is a high-resolution replacement of standard LIAs, for example, in sensors or in device characterization applications, without requiring changes in the experimental setup or calibration.



Figure 6. Block diagram of an FPGA-based LIA with sub-ppm resolution working up to 6 MHz [38].

4.2. Low-Cost Accurate Phase Measurement System

In [36], Vandenbussche et al. reported a low-cost accurate phase measurement system based on a DLIA. In particular, we consider the structure with six stages depicted in Figure 7 for a conventional FPGA-based DLIA implementation. The blocks 1 and 6 depict the design built using an FPGA Xilinx Spartan 3A-DSP as a pre- and post-processing circuit to sending capture data. For the blocks 2 and 5, the system employs a NuHorizons Spartan 3A-DSP kit NH-SPAR3ADSP-EVL with a Maxim MAX11040K DAC/ADC to provide an adequate sampling procedure. The overall digital design is implemented in the FPGA NuHorizons kit, and a Xilinx Spartan 3A-DSP XC3SD1800A with an FPGA clock sampling at 80 MHz. At the blocks 1 and 6, the circuit also ensures a clock frequency that is divided by ten inside the FPGA and supplied to the Xilinx DDS IP Core using an 8 MHz reference clock. As noted in block 1; the reference signal is generated with a DDS component using a parameterized IP-block able to generate a cosine/sine signal of equal frequency. Both channels are converted from digital to analog by the DAC.



Figure 7. FPGA-based design of a digital phase measurement system [36].

The cosine signal, which is the input signal, passes the DAC reconstruction low-pass filter, the driver circuit, and the DUT. The reference signal passes a DAC reconstruction filter and driver circuit. For the blocks 3, 4, and 5, the input and the signal from the reference channel are both anti-aliasing filtered and simultaneously sampled by the ADC and sent back to the FPGA. Similarly, in blocks 5 and 6; the two signals, composed of the input signal and the reference signal, are sampled simultaneously and multiplied with each other in the PSD and low-pass-filtered. In the block 6, the product output is subsequently digitally low-pass-filtered. Also, the arc-tan function computes the associated angle difference by

using a Xilinx parametric CORDIC IP φ information at the output signal. Blocks 1 and 2 address the frequency resolution constrained by the hardware DAC's 24-bit limitations, resulting in an output SNR of approximately 6 dB per/bit, corresponding to a spurious-free dynamic range (SFDR) of around 96 dB/Hz.

5. Bioelectrical Impedance Measurement

Disregarding the method or architecture used to perform the measurement of the signal properties of different systems, there is no doubt that biomedical and healthcare applications of biological signal measurement have been responsible for continuously pushing the electronic hardware to their limits of performance and miniaturization. The measurement of the electrical bio-impedance (EBI) of the human body and its organs, tissues, and cells, better known as bioelectrical impedance analysis (BIA), has been widely used in medicine because of the relative simplicity of its technical implementation, its feature of being non-invasive, relatively inexpensive, and its property of performing in almost any subject because of its portability and miniaturization capabilities. These characteristics make this technique the most suitable method for monitoring the state of tissues and organs, both in vitro and in vivo, and it has great potential for the development of new applications.

EBI analyzers with acceptable accuracy, reliable measurements, and compact hardware implementations are needed for the most relevant clinical applications, for instance, to be suitable for on-chip realization in implantable devices [43–45]. A technique called Electric Cell-Substrate Impedance Sensing (ECIS) provides label-free and real-time detection of cells, which is emerging as an alternative or assistive method to traditional biochemical assays for diagnostic and pharmaceutical applications [46]. Its compatibility with a liquid environment combined with low cost and reduced size, with respect to optical techniques, makes bioimpedance measurements one of the most promising transducer mechanisms for lab-on-a-chip and biochip platforms [47]. This sensing methodology has been applied to different biomedical applications, such as cell growth monitoring, impedance-based flow cytometry [48], and impedimetric affinity biosensors, the latter being one of the most promising tools for point-of-care diagnostics [47]. The EBI analysis is widely used to quantify fat-free mass (FFM), body fat (BF), body cell mass (BCM), total body water (TBW), extracellular water (ECW), and intracellular water (ICW) in healthy and ill subjects [49]. It can be also used to perform several studies on body bigger parts (e.g., rheography and plethysmography) [50], the examination of particular organs, glands, or parts of the body (e.g., heart, liver, larynx, prostate, breast, blood, etc.), the examination of some selected fragments of tissues, and measurements of single-cell impedance [44,51]. More recently, it was also shown that EBI analysis has sufficient sensitivity to replace reference methods for the assessment of body composition in athletes [52], and it has great potential to be used to observe the proper body development in children and adolescents [53] and to predict risk for gestational diabetes mellitus by measuring maternal body composition [54], just to mention a few high-impact applications in the biomedical and health industry.

Electrical impedance spectroscopy (EIS) applied to biological tissues, also known as bioimpedance spectroscopy, is a powerful and versatile technique used to study the frequency response of the electrical properties of biological materials noninvasively. In this test, a low-amplitude electrical signal is injected into the tissue sample or body parts to characterize the sample in terms of its bioimpedance. Since biological tissues are developed with biological cells, which exhibit complex electrical responses, under an alternating electrical excitation, the bioimpedance varies with the tissue anatomy and composition, and the applied signal frequency modifies the current penetration and conduction paths [55]. The variation of bioimpedance as a function of frequency is a valuable source of information about an examined tissue. This technique has been widely used to assess the condition of organic tissues in vivo, in vitro, and ex vivo and for various applications in many areas of research and clinical practice [56–60].

For instance, bioimpedance measurement using EIS has been applied to differentiate cancerous tissues in a variety of organs, including breast, cervix, skin, bladder, and prostate [60], to assess skin hydration, to detect breast cancer, to measure fluid volumes on limbs, for respiratory monitoring [61], to detect subjects with cardiovascular disease risk factors, and to improve the prediction accuracy for measuring abdominal fat distribution using machine-learning-based algorithms [62]. Bioimpedance measurement in tissue is one of the parameters that allow ischemia monitoring in living bodies [63]. This measurement was also used to show the influence of skin impedance on biological potential measurement, to measure skin moisturization using skin admittance, and to analyze gait analysis using lower-leg electrical impedance [64]. Many biomedical, immunological, and pharmaceutical studies require highly homogeneous populations of biological particles separated from heterogeneous mixtures such as peripheral blood or even clonal cell lines with differing characteristics. Impedance-activated microseparation is a very sensitive technique, which can size, count, and isolate particles based on the bioimpedance measurement [65].

Thus, the understanding of the electrical current conduction in biological tissues and the development of new methodologies for the quantification of this phenomenon are of great relevance to improve techniques like bioelectrical impedance analysis (BIA) and electrical/electrochemical impedance spectroscopy (EIS).

Computational Prediction: A Robust Machine Learning Approach

The underlying embedded technology aims to make optimal use of hardware realizations to address more complex and flexible circuit architectures that can be applied to improve the digital signal acquisition and conditioning performance with practical limitations. This notion is faced by DSP algorithms for implementing the complex processing of biological systems acquired from reading sensor signals that present intrinsic properties with highly irregular, non-stationary, and heterogeneous morphologies. This complexity implies the necessity of suitable methods, such as the supervised and unsupervised classification of machine learning (ML) algorithms, which contribute to providing several promising results to modern medicine devices [66]. The goal of the classification algorithm is to distinguish different signal states accurately [14]. Thus, the performance of classification algorithms can help to acquire high-quality signals to characterize true and false positives to provide further metrics and figures of merit such as receiver operating characteristic (ROC) curve and area under the curve (AUC) analysis. In [67], N. Dey et al. reported several models based on clustering and classification approaches such as convolutional neural networks (CNNs), decision trees, and support vector machines (SVM) that have been successfully applied to medical imaging. However, biomedical signal analysis has yet to fully benefit from this novel approach. Figure 8 shows the block diagram of the analog components and digital hardware building blocks based on FPGA-based design blocks for the analysis of bioelectrical signals with sources of multiple wire connection frequencies with channel selection [68]. The block diagram shown in Figure 9 denotes the two procedures associated with an automated process for the extraction of the main features in a given adaptive processing and classification of sensor signals, following a step-by-step parameterization. The model classification provided in procedure 1 in Figure 9 integrates various techniques, including ensemble learning approaches and artificial neural networks (ANNs), serving as examples for feature extraction. Additionally, parameter optimization is performed using metrics such as the mean squared error (MSE), mean absolute error (MAE), normalized mean squared error (NMSE), and the coefficient of determination. These metrics evaluate the model's performance in regression analysis and assess its effectiveness in minimizing prediction errors.

In [69], a system is reported to determine the optimal biosignal characteristics from recorded sampled data points over time periods for the detection of driving stress from electrocardiogram (ECG) signals. An extensive review is addressed in [70] to compare the accuracy of classification, implementation complexity, invasiveness, and targeted application for electromyography (EMG), electroencephalogram (EEG), and rapid eye movement (REM). An approach guided by learning paradigms can successfully aid in the development of advanced healthcare diagnostic systems for biosignal analysis [71].



Figure 8. Block diagram classification with analog components and digital FPGA-based design blocks for the analysis and digital conditioning of bioelectrical signals.



Figure 9. Block diagram of the procedure for signal extraction, selection, and model classification for feature optimization.

Figure 10 shows different types of signals with typical frequency, amplitude, and 1/f noise relationship levels. Figure 11 summarizes the implementation building blocks to

continuously sample and process the various types of bioelectrical signals from electrodes shown in Figure 8. The concept of developing the architecture in the digital domain enables us to reach an adequate algorithmic and digital processing circuits, which in turn analyze and classify the stream of digital signals using well-suited pre-defined algorithms to provide dedicated FPGA/ASIC hardware. The AUC classification captures key signal characteristics in the time domain, which can be transformed into frequency representations via a fast Fourier transform. Calculating the AUC of the power spectral density quantifies the energy distribution of EEG, EMG, and ECG signals across frequency bands [72], offering insights into signal power and facilitating the analysis of physiological or pathological processes within specific frequency ranges, as illustrated in Figure 10.



Figure 10. Signal characteristics with the frequency/amplitude relationship.



Figure 11. System key building blocks for the processing signals at the hardware integrated circuit.

6. Discussion

We have introduced a comprehensive summary of applications, including industrial electronics [73], telecommunications, and healthcare biomedical circuits [12,21,43,44,66,69,74]. The design implementation for these applications has attracted the attention of the industry and the scientific community, starting from a few basic assumptions on the design [29], analysis [26,68], measurement, and modeling techniques which are important to address rigorously engineered LIA systems [34]. Moreover, a key lack of these architectures in voltage resolution control for the detectable instrument has to be fixed by an input range for both the single and dual-phase and is independent of the input signal amplitude [38]. Note, however, that the dual-phase LIA usually deals with an unavoidable and intrinsic 1/f flicker noise

of the reference voltage (either used by the DAC and ADC), and most applications result in signal amplitude modulation [17,24,26,38,39,75]. LIAs are strongly affected by cyclostationary effects that mainly originate from circuits such as the ADC and DAC, which are also correlated with conversion gains and fluctuations. In [38] a standard implementation is demonstrated to provide benefits in sub-ppm measurements, i.e., filtering bandwidth of 1 Hz to switching frequency greater than 1 kHz so that the resolution will be flat at sub-ppm values. However, by lowering the switching frequency [21,76], the resolution suffers from spectral degradation due to the overlapping with the side harmonics of the 1/f noise components. Then signalconditioning measurements become dependent on the frequency of the input's spectral density, which can be compensated with an operation where a finite frequency response exists. Furthermore, some noise effects on digital LIA architectures can be scaled or shifted using convolution [75], which helps to keep SNR at maximum levels. In this context, it is well known that lower phase noise is achieved with a larger size or by paralleling several devices. Thus, FPGA digital components that operate with main clock synchronization, (i.e., if a frequency synthesis is dependent on clock-aware routability, some issues such as the sampling clock jitter can be removed given the time base) are an overall cost [34,77]. The convenience of the digital alternatives is that it benefits the accuracy of detecting quantitative noise contributions.

The assumption behind the methods of quantization errors and resolution in signal generation lie in the achievable digital LIAs performance, which shares a strong relationship with the optimization methods, such as in terms of numerical precision problems. To the extent of our knowledge, in [26] Masciotti et al. introduced a great advance in the analysis of a digital lock-in technique for practical noise reduction and discrimination, where the design can detect multiple signals at different modulation frequencies. Consider that for the enabling technologies that involve medical applications comprising several IoTs providing smart healthcare devices into one SoC, measurements present fundamental limits that are related to the lock-in amplifier relative resolution. Similarly, it should not be ignored that practical sensor-stimuli systems (EEG, gas, audio, etc.) have lagged far behind the application flexibility given their steady-state discrete-time conditions [76]. Despite the capabilities provided for analog lock-in amplifiers, a few examples from the literature of proof-of-concept experiment design CMOS technologies provide flexible functionalities or enable interoperability between the measurement system and the sensor. In other words, the supporting process of signal extraction is in most cases limited to specific technical restrictions related to the signal conditioning stage, extraction, and the measurement process [21,76,78].

6.1. Challenges and Future Directions for Driven Machine Learning Architectures

Bioelectrical impedance sensors are pivotal tools in the domain of health monitoring, providing valuable insights into various physiological parameters. The review concludes by addressing the challenges encountered in employing machine learning algorithms for feature extraction from bioelectrical impedance sensors. The extraction of meaningful features from impedance data is a critical step in enhancing the accuracy and reliability of health-related predictions. Additionally, potential future directions, including the integration of deep learning techniques and real-time applications, are outlined to provide a roadmap for further research in this domain. The incorporation of AUC analysis enhances the precision of feature extraction processes, thus contributing significantly to the advancement of health monitoring technologies. Emphasis is placed on algorithms' ability to exploit the enhanced impedance signals obtained through lock-in amplifiers, as explained in the procedure extraction and the model feature classification in Figure 9. Thus, this review provides some key comparative metrics such as accuracy, sensitivity, and specificity to quantify their performance. The development of compact instrumentation and

the measurement and analyses of the observed data use multiple stochastic and machine learning techniques to bring out the best correlation fit between the glucose concentration and a specific feature of the electrical signal ML techniques applied to the extraction of data from LIAs [79] to provide pioneers with compact photoacoustic spectroscopy systems with a lock-in amplifier as basis circuit that also can integrated with machine learning, marking a significant step toward wearable glucose monitoring devices.

6.2. Comparative Table: A Systematic Review

Some practical considerations of the state of the art for LIA architectures are summarized in Table 1. The discussion in Section 4 was devoted to detailing the applications available for a wide range of frequencies. In the same way, some underlying aspects of LIA technology such as the design, application, and signal reference generation were addressed. In the literature, Chighine et al. [25], Vandenbussche et al. [36], and Ayat et al. [39], proposed some FPGA-based architectures where an overall LIA system is conceived. The most relevant features ofn the FPGA devices are in the requirements and reliability of signal conditioning aspects, which are crucial for these specific sensor applications. In most cases, the digital DDS architecture [16,18,26,34,37,77] requires a precise tuning frequency control, which sometimes makes critical to apply a sampling rate for an equivalent sampling frequency. Tables 1 and 2 present an overview of works that attain a good synchronization and frequency resolution for each platform/device design for several LIAs systems. As an example, such a design principle is to ensure the Nyquist criterion, and the optimal detection process is simple and can ensure a reliable and straightforward characterization if the maximum output frequency is provided on a factor of 1/3for a sampling frequency [38,40]. These limitations on critical sensor applications tend to result in inaccurate sub-Hertz frequencies at the extraction method and thus do not provide a precise normalized amplitude at the stimulus signal [34,38]. Recent developments present attractive solutions to address the digital precision of LIA system-level requirements. In [80], Pfeiffer et al. proposed a module for biomedical health issues over the terahertz range to constitute a sequential system implementation with clocking control and a lock-in amplifier-based digital readout mode. Likewise, the implementation of silicon technology, such as the approach using DSP, has advanced to the point of providing special signal conditioning functions on LIAs, thus enabling high-precision measurements on sensor systems through FPGA devices [16,25,26,33,34,36,38]. In [36], Vandenbussche et al. proposed a practical investigation to calculate the causes of inaccuracy from a system derivation that considers aspects like linearity, quantization effects [18], differentiation, logarithmic and anti-logarithmic conversion, and peak-to-peak and phase-sensitive detection [11,33,34,36], in which signal quality improvements are closely related to phenomena, such as cross-sensitivity, non-linearity [19], and unwanted signals. In [19], Fan et al. proposed a technique to detect physical, chemical, or biological quantities in sensors by optimizing SFDR from the ADC signal extraction to smart sensor systems, which can enhance the inaccuracy of the delayed measured phase for conventional LIA architectures [19,33,81]. On the other hand, the knowledge of the experimental designs in which non-idealities for synthesizing frequency limits for the signal recovery process are strongly dependent on systematic errors due to harmonics [43]. In this context a study with the reference frequencies is validated in [11] and for the designs reported in Table 1. Another aspect that occurs with successive measurements is related to phase distortion that is highly dominant; thus, it becomes crucial to apply calibration methods to reduce the uncertainty in the experimental system [82]. Gervasoni et al. [38] experimentally demonstrated an LIA system based on a dual-channel ADCs full-duplex, which can acquire the signal from the DUT and the stimulus signal. In this architecture, the LIA enhancements allow the compensation of the

slow gain fluctuations of both the DAC and ADC, which can considerably reduce phase mismatch effects at the extraction chain. In [83], Sarma et al. presented an analysis of theoretical SFDR resolutions \geq 12-bit ADCs. A key aspect is related to the convenience of the DDS resolution accuracy for the designs summarized in Table 2, which also determines precision in the output signal. Such a key condition is difficult to fulfill in the case of high-frequency digital LIAs, with sampling rates of tens or hundreds of MS/s.

 Table 1. Comparison of DDS performance in seminal works on digital LIA systems.

Digital Architectures					
LIA Class, References	Freq. clk.	Device/Platform	Key Feature: Ref. Description		
Single-phase, [36]	250 MHz	FPGA Xilinx Spartan-3	A low-cost digital LIA system to accurate phase measurement.		
Single-phase, [84]	100 MHz	TI TMS320 DSP series	A low-power operation DSP for remote and battery-powered operations.		
Dual-phase, [12]	250 MHz	FPGA Xilinx SoC XC7Z100	A system application for microfluidic impedance measurement		
Dual-phase, [25]	100 MHz	FPGA Xilinx Spartan-6	A multichannel optical chemical tomography system.		
Dual-phase, [39]	500 kHz	FPGA Xilinx Spartan-3	A digital LIA to measure the amplitude and phase of multichannel modulated frequency signals.		
Dual-phase, [75]	70 kHz	Microcontroller DSP-based	A low-cost LIA, that recovers the weak signal under extremely noisy conditions.		
Different approaches [38]	6 MHz	FPGA Xilinx Spartan-6	A DLIA architecture that allows to compensate low-frequency gain fluctuations added by the DAC/ADC.		
Analog Architectures: Seminal Works					
LIA Class, References	Freq. clk.	Technology	Key Feature: Ref. Description		
Single-phase, [21]	14.64 MHz	CMOS 0.35-µm	A LIA for optical sensing and spectroscopy applications.		
Single-phase, [76]	10 kHz	CMOS analog multipliers	A system for electroencephalogram biomedical applications.		
Single-phase, [78]	25 Hz	CMOS 0.35-μm	A detector for measurement of small, slow, and noisy signals.		

Table 2. Comparison of DDS performance with several digital LIAs systems.

Reference	DDS Resolution [bits]	Operating Freq _{max} [Hz]	SNR [dB]
Huang et al. [12]	14-bit	30 MHz	20
Chighine et al. [25]	12-bit	50 kHz	-
Vandenbussche et al. [36]	16-bit	15.62 kHz	90
Ayat et al. [39]	14-bit	500 kHz	2
Gervasoni et al. [38]	14-bit	6 MHz	42
Proposed work, [40] [†]	14-bit	12.5 MHz	90

Reference	DDS Resolution [bits]	Operating Freq _{max} [Hz]	SNR [dB]
Sonnaillon, et al. [85]	10-bit	5 MHz	50
Milhem et al. [76]	_	10 kHz	15
Das et al. [84]	10-bit	5 kHz	_
Rahmannuri et al. [86]	12-bit	10 kHz	15.6
Bhattacharyya et al. [75]	16-bit	5 kHz	24.09
Liu et al. [87]	16-bit	100 kHz	_
Cheng et al. [88]	12-bit	1 MHz	_

Table 2. Cont.

⁺ Considering the DDS signal reference with phase dithering enhancement (up-to four tones), $Freq_{max}$ is given with a 1/10 factor for a 125 MHz clock.

6.3. Final Remarks and Future Research

The overview of LIAs in this paper emphasizes the digital design capabilities to enable the LIA instruments interfacing with sensor devices [8,10,30–32]. In general, some critical LIA requirements for higher-level applications that interact with a sensor, such as their topological arrangement, can be related to voltage phenomena associated with the amplification, filtering, and digitization. Most digital LIAs use a PLL to generate a stable frequency. This indicates that in the phase domain that governs the reference and input signal, a phase relation and its frequency are responsible for the progression of phase locking for both the stimuli and the reference signals [26]. Some frequency-dependent key attributes in LIAs are related to three considerations:

- Frequency-commensurate support: It is important to emphasize that for the commensurate agreement lock-in frequencies (i.e., working at precisely 10 MHz on a lock-in with 100 MHz sampling rate), a frequency with a factor of 1/10-th of the sampling rate has to be ensured [40].
- Uniformly sampled signal rational samples: In digital LIA instruments, it is often necessary to consider incommensurate frequencies [89], where the ratio of the two signal frequencies is irrational. This is an important sub-case of a commensurate frequency relationship, namely $f_1/f_2 = n/m$ for the integers *n* and *m*.
- Time-invariant, phase normalization, and commensurate signals: A signal conditioning stage must be present on a quick verification of the DUT response that treats the nonlinear stimuli.

In addition to the signal conditioning and integrity techniques, some LIA systems where signal processing is compounded with correlation methods are certainly valid and sufficient to identify and count events where the SNR is already good, even if these electrical signals become noisy due to severe conditions of temperature, pressure, humidity, and drift [18,26,29]. In some LIA applications under very noisy environments, it sometimes becomes impossible to apply correlation techniques; however, digital adaptive filtering techniques can help to recover the data (see Ref. [74]). This also facilitates a more accurate estimation given the subsequent dependence at the inter-stage quantization process (e.g., DDS, DAC-ADC, filtering) [83]. Thus, for a noisy measurement environment, improving the reattained SNR (assuming a reasonable calibration procedure) of the system is crucial. In some cases, SNR reduction can modify the filtering so that any correlation method can be subsequently applied to the filtered data [26,30,34].

7. Conclusions

In this paper, we have provided an overview of recent digital LIA application developments. We emphasized in this investigation the context of a tailor-made real-time embedded system, where the stimulus frequency and acquisition can provide a stable operation above Hz up to tens of MHz. Thus, by knowing the capabilities of the application of signal processing techniques, lock-in amplifiers' performance can be improved rapidly from an RTL digital design perspective. For the reviewed applications, DDS digital frequency controllability can accelerate the embedded LIA design applications, which in turn can provide an effective and efficient tradeoff between accuracy and hardware consumption. Similarly, from the digital point of view, large systematic errors in both single- and dual-phase of the described lock-in phase's system applications tend to decrease the conditioning signal methods' performance for most practical sensors, which in turn influence the interoperability features for the measurements and design limitations. As we highlighted, for the critical design features for DLIA's architectures, the SFDR performance is a critical characteristic in FPGA-based design and is especially vital in applications requiring high sensitivity and specificity, such as biomedical signal processing and advanced sensor systems. Therefore, we also emphasize that the optimization of SFDR to DLIA's designs not only enhances measurement accuracy but also increases the applicability of these systems across diverse and complex use cases. This enhancement can not only improve the calibration stage for digital dual-phase LIAs, but it can also improve linearity in the DUT signal extraction. From this perspective, an accelerated FPGA-based LIA digital architecture implementation can be improved by ensuring enhancements of spectral purity. Also, our findings from the actual needs of the far-reaching significance of frequency-dependent LIAs operation has a good compromise among resolution, control, switching, and system implementations, such as in sensors that need high specificity and sensitivity.

Author Contributions: Conceptualization, J.A.G.-A. and C.A.-A.; methodology, J.A.G.-A., F.F., C.V.-R. and C.A.-A.; software, J.A.G.-A. and C.V.-R.; validation, J.A.G.-A., C.A.-A., F.F. and C.V.-R.; formal analysis, J.A.G.-A. and C.A.-A.; investigation, J.A.G.-A., F.F. and C.A.-A.; resources, C.A.-A. and C.V.-R.; data curation, J.A.G.-A. and C.A.-A.; writing—original draft preparation, C.A.-A. and J.A.G.-A.; writing—review and editing, J.A.G.-A., C.V.-R., F.F. and C.A.-A.; visualization, J.A.G.-A. and C.A.-A.; writing—review and editing, J.A.G.-A., C.V.-R., F.F. and C.A.-A.; visualization, J.A.G.-A. and C.A.-A.; writing—review and editing, J.A.G.-A., C.V.-R., F.F. and C.A.-A.; visualization, J.A.G.-A. and C.A.-A.; supervision, C.V.-R.; project administration, J.A.G.-A. and C.A.-A.; funding acquisition, C.V.-R. All authors have read and agreed to the published version of the manuscript.

Funding: This research received no external funding

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Not applicable.

Conflicts of Interest: The authors declare no conflicts of interest.

Abbreviations

ADC	analog-to-digital converter
AFM	Atomic force microscopy
ARM	advanced RISC machines
ASIC	application-specific integrated circuit
BPF	band-pass filter
CMOS	complementary metal-oxide-semiconductor
DAC	digital-to-analog converter

DDFS	direct digital frequency synthesizer
DDS	direct digital synthesis
DLIA	digital lock-in amplifier
DSP	digital signal processor
DTC	digital-to-time converter
DUT	device under test
FPGA	field programmable gate array
HDL	hardware description language
HPF	high-pass filter
IP	intellectual property
LDR	linear dynamic range
LFSR	linear-feedback shift register
LIA	lock-in amplifier
LNA	low-noise amplifier
LPF	low-pass filter
LUT	look-up table
MCU	microcontroller unit
NCO	numerically controlled oscillator
PGA	programmable gain amplifier
PLL	phase-locked loop
PMD	phase-modulation-demodulation
PSD	phase sensitive detection
PXI	PCI eXtensions for Instrumentation
RISC	reduced instruction set computer
RMS	root mean square
RTL	register-transfer level
SFDR	spurious-free dynamic range
SINAD	signal-to-noise-and-distortion
SNR	signal-to-noise ratio
SoC	system on a chip
THD	total harmonic distortion
VHDL	VHSIC hardware description language
IoT	internet of things

References

- Sigmund, M. Short-Term Entropy of Signal Energy Used for Effective Detecting of Weak Gunshots in Noisy Environments. Sensors 2024, 24, 4933. [CrossRef] [PubMed]
- Zhang, Q.; Jeong, W.; Kang, D.J. Lock-in amplifiers as a platform for weak signal measurements: Development and applications. *Curr. Appl. Phys.* 2024, *66*, 95–109. [CrossRef]
- 3. Bhagyajyoti, J.; Sudheer, L.; Bhaskar, P.; Parvathi, C. Review on lock-in amplifier. Int. J. Sci. Eng. Technol. 2012, 1, 40–45.
- Zhang, Y.; Qiu, M.; Tsai, C.; Hassan, M.M.; Alamri, A. Health-CPS: Healthcare Cyber-Physical System Assisted by Cloud and Big Data. *IEEE Syst. J.* 2017, 11, 88–95. [CrossRef]
- Meng, Z.; He, X.; Li, Y.; Huang, J.; Chen, D.; Wang, Z. A Multi-contaminants Detection Sensor Based on Digital Lock-in Amplifier Module with High Sensitivity and High Detectability. *IEEE Sens. J.* 2023, 23, 16123–16135. [CrossRef]
- 6. Devasagayam, J.; Leclerc, C.A.; Bosma, R.; Wood, L.; Collier, C.M. Lock-in Amplifier Dairy Sensor for Detection of Ciprofloxacin. *IEEE Access* 2023, *11*, 41697–41707. [CrossRef]
- Hernandez, P.M.M.; Pascual, M.T.S.; Calvo, B. Micropower CMOS lock-in amplifier for portable applications. *Electron. Lett.* 2016, 52, 828–830. [CrossRef]
- 8. Davidovic, M.; Seiter, J.; Hofbauer, M.; Gaberl, W.; Zimmermann, H. Monolithically integrated dual-lock-in optical sensor. *Electron. Lett.* **2014**, *50*, 306–308. [CrossRef]
- 9. Kishore, K.; Akbar, S.A. Evolution of Lock-in Amplifier as Portable Sensor Interface Platform: A Review. *IEEE Sens. J.* 2020, 20, 10345–10354. [CrossRef]
- 10. De Marcellis, A.; Palange, E.; Liberatore, N.; Mengali, S. Low-cost portable 1 mhz lock-in amplifier for fast measurements of pulsed signals in sensing applications. *IEEE Sens. Lett.* **2017**, *1*, 7000104. [CrossRef]

- 11. Patou, F.; Dimaki, M.; Kjrgaard, C.; Madsen, J.; Svendsen, W.E. System-level sensitivity analysis of sinw-biofet-based biosensing using lock-in amplification. *IEEE Sens. J.* 2017, *17*, 6295–6311. [CrossRef]
- 12. Huang, K.; Geng, Y.; Zhang, X.; Chen, D.; Cai, Z.; Wang, M.; Zhu, Z.; Wang, Z. A Wide-Band Digital Lock-in Amplifier and Its Application in Microfluidic Impedance Measurement. *Sensors* **2019**, *19*, 3519. [CrossRef] [PubMed]
- 13. Harvie, A.J.; de Mello, J.C. OLIA: An open-source digital lock-in amplifier. Front. Sens. 2023, 4, 1102176. [CrossRef]
- Yang, J.; Sawan, M. From Seizure Detection to Smart and Fully Embedded Seizure Prediction Engine: A Review. *IEEE Trans. Biomed. Circuits Syst.* 2020, 14, 1008–1023. [CrossRef]
- 15. Yazicioglu, R.F.; Merken, P.; Puers, R.; Van Hoof, C. A 200 μ W Eight-Channel EEG Acquisition ASIC for Ambulatory EEG Systems. *IEEE J. Solid-State Circuits* **2008**, *43*, 3025–3038. [CrossRef]
- 16. Gaspar, J.; Chen, S.F.; Gordillo, A.; Hepp, M.; Ferreyra, P.; Marqués, C. Digital lock in amplifier: Study, design and development with a digital signal processor. *Microprocess. Microsyst.* **2004**, *28*, 157–162. [CrossRef]
- 17. Aguirre, J.; Medrano, N.; Calvo, B.; Celma, S. Lock-in amplifier for portable sensing systems. *Electron. Lett.* **2011**, 47, 1172–1173. [CrossRef]
- Palattella, C.; Klumperink, E.A.M.; Alink, M.S.O.; Nauta, B. Digital-to-Frequency Converters with a DTC: Theoretical Analysis of the Output SFDR. *IEEE Trans. Circuits Syst. I Regul. Pap.* 2019, *66*, 3761–3774. [CrossRef]
- 19. Fan, H.; Li, J.; Feng, Q.; Diao, X.; Lin, L.; Zhang, K.; Sun, H.; Heidari, H. Exploiting Smallest Error to Calibrate Non-Linearity in SAR Adcs. *IEEE Access* 2018, *6*, 42930–42940. [CrossRef]
- 20. Aguirre, J.; García-Romeo, D.; Medrano, N.; Calvo, B.; Celma, S. Square-Signal-Based Algorithm for Analog Lock-In Amplifiers. *IEEE Trans. Ind. Electron.* 2014, *61*, 5590–5598. [CrossRef]
- 21. Hu, A.; Chodavarapu, V.P. CMOS Optoelectronic Lock-In Amplifier with Integrated Phototransistor Array. *IEEE Trans. Biomed. Circuits Syst.* **2010**, *4*, 274–280. [CrossRef] [PubMed]
- 22. Maya-Hernández, P.M.; Sanz-Pascual, M.T.; Calvo, B. CMOS Low-Power Lock-In Amplifiers with Signal Rectification in Current Domain. *IEEE Trans. Instrum. Meas.* 2015, 64, 1858–1867. [CrossRef]
- Hintenaus, P.M.; Trinker, H. Multifrequency Lock-In Detection with Nonsinusoidal References. *IEEE Trans. Instrum. Meas.* 2013, 62, 785–793. [CrossRef]
- Akshaya, S.; Rao, S.N.; Bennaceur, K. A survey of low-cost lock-in amplifiers for sensor applications. In Proceedings of the 2018 International Conference on Advances in Computing, Communications and Informatics (ICACCI), Bangalore, India, 19–22 September 2018; pp. 2486–2490.
- Chighine, A.; Tsekenis, S.; Fisher, E.; Polydorides, N.; Wilson, D.; Lengden, M.; Johnstone, W.; McCann, H. Tdlas using fpgabased lock-in detection for multichannel chemical species tomography. In Proceedings of the 2015 IEEE SENSORS, Busan, Republic of Korea, 1–4 November 2015; pp. 1–4.
- 26. Masciotti, J.M.; Lasker, J.M.; Hielscher, A.H. Digital Lock-In Detection for Discriminating Multiple Modulation Frequencies with High Accuracy and Computational Efficiency. *IEEE Trans. Instrum. Meas.* **2008**, *57*, 182–189. [CrossRef]
- 27. Belea, R.; Epure, S. Low cost lock-in amplifier solutions. In Proceedings of the 2017 IEEE 23rd International Symposium for Design and Technology in Electronic Packaging (SIITME), Constanta, Romania, 26–29 October 2017; pp. 118–121.
- Wu, D.; Wang, C.; Sun, H.; Wang, H. A novel digital lock-in amplifier with dual channels. In Proceedings of the 2009 International Asia Conference on Informatics in Control, Automation and Robotics, Bangkok, Thailand, 1–2 February 2009; pp. 464–468.
- 29. Leis, J.; Martin, P.; Buttsworth, D. Simplified digital lock-in amplifier algorithm. Electron. Lett. 2012, 48, 259–261. [CrossRef]
- 30. Faller, L.; Mitterer, T.; Leitzke, J.P.; Zangl, H. Design and Evaluation of a Fast, High-Resolution Sensor Evaluation Platform Applied to MEMS Position Sensing. *IEEE Trans. Instrum. Meas.* **2018**, *67*, 1014–1027. [CrossRef]
- 31. Mauch, S.; Reger, J. Real-Time Spot Detection and Ordering for a Shack–Hartmann Wavefront Sensor with a Low-Cost FPGA. *IEEE Trans. Instrum. Meas.* **2014**, *63*, 2379–2386. [CrossRef]
- 32. Athi, M.V.; Zekavat, S.R.; Struthers, A.A. Real-Time Signal Processing of Massive Sensor Arrays via a Parallel Fast Converging SVD Algorithm: Latency, Throughput, and Resource Analysis. *IEEE Sens. J.* **2016**, *16*, 2519–2526. [CrossRef]
- 33. Macias-Bobadilla, G.; Rodríguez-Reséndiz, J.; Mota-Valtierra, G.; Soto-Zarazúa, G.; Méndez-Loyola, M.; Garduno-Aparicio, M. Dual-phase lock-in amplifier based on FPGA for low-frequencies experiments. *Sensors* **2016**, *16*, 379. [CrossRef]
- 34. Vandenbussche, J.; Lee, P.; Peuteman, J. On the Accuracy of Digital Phase Sensitive Detectors Implemented in FPGA Technology. *IEEE Trans. Instrum. Meas.* **2014**, *63*, 1926–1936. [CrossRef]
- Ould-Bachir, T.; Blanchette, H.F.; Al-Haddad, K. A Network Tearing Technique for FPGA-Based Real-Time Simulation of Power Converters. *IEEE Trans. Ind. Electron.* 2015, 62, 3409–3418.
- Vandenbussche, J.; Peuteman, J.; Lee, P. Development of a low-cost accurate phase measurement system. In Proceedings of the 2014 Information and Communication Technologies Innovation and Application (ICTIA), Sousse, Tunisia, 6–8 March 2014; pp. 1–7.
- 37. Ashrafi, A.; Adhami, R. Theoretical Upperbound of the Spurious-Free Dynamic Range in Direct Digital Frequency Synthesizers Realized by Polynomial Interpolation Methods. *IEEE Trans. Circuits Syst. I Regul. Pap.* **2007**, *54*, 2252–2261. [CrossRef]

- Gervasoni, G.; Carminati, M.; Ferrari, G. FPGA-based lock-in amplifier with sub-ppm resolution working up to 6 MHz. In Proceedings of the 2016 IEEE International Conference on Electronics, Circuits and Systems (ICECS), Monte Carlo, Monaco, 11–14 December 2016; pp. 117–120.
- 39. Ayat, M.; Karami, M.A.; Mirzakuchaki, S.; Beheshti-Shirazi, A. Design of multiple modulated frequency lock-in amplifier for tapping-mode atomic force microscopy systems. *IEEE Trans. Instrum. Meas.* **2016**, *65*, 2284–2292. [CrossRef]
- Galaviz-Aguilar, J.A.; Vargas-Rosales, C.; Falcone, F. Reliable Methodology to FPGA Design Verification and Noise Analysis for Digital Lock-In Amplifiers. *IEEE Embed. Syst. Lett.* 2024, 16, 307–310. [CrossRef]
- 41. Pollastrone, F.; Piccinini, M.; Pizzoferrato, R.; Palucci, A.; Montereali, R.M. Fully-digital low-frequency lock-in amplifier for photoluminescence measurements. *Analog. Integr. Circuits Signal Process.* **2023**, *115*, 67–76. [CrossRef]
- Dorsa, A.; Xie, Q.; Wagner, M.; Xu, X.G. Lock-in amplifier based peak force infrared microscopy. *Analyst* 2023, 148, 227–232. [CrossRef]
- Min, M.; Parve, T. An Electrical Bio-Impedance Analyzer for Implantable Medical Devices. In Proceedings of the 2005 IEEE Instrumentation and Measurement Technology Conference Proceedings, Ottawa, ON, Canada, 16–19 May 2005; pp. 1823–1828.
- Min, M.; Parve, T. Improvement of Lock-in Electrical Bio-Impedance Analyzer for Implantable Medical Devices. *IEEE Trans.* Instrum. Meas. 2007, 56, 968–974. [CrossRef]
- 45. Allegri, D.; Donida, A.; Malcovati, P.; Barrettino, D. CMOS-Based Multifrequency Impedance Analyzer for Biomedical Applications. *IEEE Trans. Biomed. Circuits Syst.* **2018**, *12*, 1301–1312. [CrossRef]
- 46. Park, I.-H.; Hong, Y.; Jun, H.-S.; Cho, E.-S.; Cho, S. DAQ based Impedance Measurement System for Low Cost and Portable Electrical Cell-Substrate Impedance Sensing. *BioChip J.* **2018**, *12*, 18–24. [CrossRef]
- 47. Carminati, M.; Ferrari, G.; Bianchi, D.; Sampietro, M. Impedance spectroscopy for biosensing: Circuits and applications. In *Handbook of Biochips*; Sawan, M., Ed.; Springer Science + Business Media: New York, NY, USA, 2015; pp. 1–24.
- 48. Tang, T.; Liu, X.; Kiya, R.; Shen, Y.; Yuan, Y.; Zhang, T.; Suzuki, K.; Tanaka, Y.; Li, M.; Hosokawa, Y.; et al. Microscopic impedance cytometry for quantifying single cell shape. *Biosens. Bioelectron.* **2021**, *193*, 113521. [CrossRef]
- Kyle, U.G.; Bosaeus, I.; De Lorenzo, A.D.; Deurenberg, P.; Elia, M.; Gómez, J.M.; Heitmann, B.L.; Kent-Smith, L.; Melchior, J.C.; Pirlich, M.; et al. Bioelectrical impedance analysis—Part II: Utilization in clinical practice. *Clin. Nutr.* 2004, 23, 1430–1453. [CrossRef] [PubMed]
- 50. Annus, P.; Land, R.; Priidel, E.; Metshein, M.; Min, M.; Märtens, O. Quantization of the response signal differences for the electrical bioimpedance measurement. *IFMBE Proc.* **2018**, *65*, 290–293.
- 51. Frączek, M.; Kręcicki, T.; Moron, Z.; Krzywaźnia, A.; Ociepka, J.; Rucki, Z.; Szczepanik, Z. Measurements of electrical impedance of biomedical objects. *Acta Bioeng. Biomech.* 2016, *18*, 11–17. [PubMed]
- 52. Campa, F.; Gobbo, L.A.; Stagi, S.; Cyrino, L.T.; Toselli, S.; Marini, E.; Coratella, G. Bioelectrical impedance analysis versus reference methods in the assessment of body composition in athletes. *Eur. J. Appl. Physiol.* **2022**, 122, 561–589. [CrossRef] [PubMed]
- 53. Orsso, C.E.; Gonzalez, M.C.; Maisch, M.J.; Haqq, A.M.; Prado, C.M. Using bioelectrical impedance analysis in children and adolescents: Pressing issues. *Eur. J. Clin. Nutr.* **2022**, *76*, 659–665. [CrossRef]
- 54. Zhang, R.Y.; Wang, L.; Zhou, W.; Zhong, Q.M.; Tong, C.; Zhang, T.; Han, T.L.; Wang, L.R.; Fan, X.; Zhao, Y.; et al. Measuring maternal body composition by biomedical impedance can predict risk for gestational diabetes mellitus: A retrospective study among 22,223 women. *J. Matern.-Fetal Neonatal Med.* **2022**, *35*, 2695–2702. [CrossRef]
- Bera, T.K. Bioelectrical Impedance and The Frequency Dependent Current Conduction Through Biological Tissues: A Short Review. In Proceedings of the 3rd International Conference on Communication Systems (ICCS-2017), Rajasthan, India, 14–16 October 2017; Volume 331.
- 56. Kim, J.; Abbasi, M.A.; Kim, T.; Park, K.D.; Cho, S. Lock-in Amplifier-Based Impedance Detection of Tissue Type Using a Monopolar Injection Needle. *Sensors* **2019**, *19*, 4614. [CrossRef]
- 57. Quoc, T.V.; Ngoc, V.N.; Hoang, B.-A.; Jen, C.-P.; Duc, T.C.; Bui, T.T. Development of a Compact Electrical Impedance Measurement Circuit for Protein Detection Two-electrode Impedance Micro-sensorg. *IETE J. Res.* **2023**, *69*, 2478–2486. [CrossRef]
- 58. Tang, J.; Yin, W.; Lu, M. Bio-impedance spectroscopy for frozen-thaw of bio-samples: Non-contact inductive measurement and finite element (FE) based cell modelling. *J. Food Eng.* **2020**, *272*, 109784. [CrossRef]
- Viswam, V.; Bounik, R.; Shadmani, A.; Dragas, J.; Urwyler, C.; Boos, J.A.; Obien, M.E.; Müller, J.; Chen, Y.; Hierlemann, A. Impedance Spectroscopy and Electrophysiological Imaging of Cells with a High-Density CMOS Microelectrode Array System. *IEEE Trans. Biomed. Circuits Syst.* 2018, *12*, 1356–1368. [CrossRef]
- 60. Deana, D.A.; Ramanathan, T.; Machado, D.; Sundararajan, R. Electrical impedance spectroscopy study of biological tissues. *J. Electrost.* **2008**, *66*, 165–177. [CrossRef] [PubMed]
- Tsunami, D.; McNames, J.; Colbert, A.; Pearson, S.; Hammerschlag, R. Variable Frequency Bioimpedance Instrumentation. In Proceedings of the 26th Annual International Conference of the IEEE EMBS, San Francisco, CA, USA, 1–4 September 2004; pp. 2386–2389.

- 62. Santhanam, P.; Nath, T.; Peng, C.; Bai, H.; Zhang, H.; Ahima, R.S.; Chellappa, R. Artificial intelligence and body composition. *Diabetes Metab. Syndr. Clin. Res. Rev.* **2023**, *17*, 102732. [CrossRef] [PubMed]
- 63. Yufera, A.; Leger, G.; Rodriguez-Villegas, E.O.; Muñoz, J.M.; Rueda, A.; Ivorra, A.; Gomez, R.; Noguera, N.; Aguiló, J. An Integrated Circuit for Tissue Impedance Measure. In Proceedings of the 2nd Annual International IEEE-EMBS Special Topic Conference on Microtechnologies in Medicine & Biology, Madison, WI, USA, 24 May 2002.
- 64. Yamamoto, Y.; Yamamoto, T. Measurement of electrical bio-impedance and its applications. *Med. Prog. Through Technol.* **1987**, 12, 171–183.
- 65. Han, S.-I.; Joo, Y.-D.; Han, K.-H. Impedance-activated microseparator based on amplitude modulation sensing and dielectrophoretic switching methods. *Sens. Actuators Chem.* **2012**, 171–172, 1312–1320. [CrossRef]
- Ganapathy, N.; Swaminathan, R.; Deserno, T.M. Deep Learning on 1-D Biosignals: A Taxonomy-based Survey. Yearb. Med. Inform. 2018, 27, 98–109. [CrossRef]
- 67. Dey, N.; Borra, S.; Ashour, A.S.; Shi, F. *Machine Learning in Bio-Signal Analysis and Diagnostic Imaging*; Academic Press: Cambridge, MA, USA, 2019.
- 68. Mesa, I.; Rubio, A.; Tubia, I.; De No, J.; Diaz, J. Channel and feature selection for a surface electromyographic pattern recognition task. *Expert Syst. Appl.* **2014**, *41*, 5190–5200. [CrossRef]
- 69. Elgendi, M.; Menon, C. Machine Learning Ranks ECG as an Optimal Wearable Biosignal for Assessing Driving Stress. *IEEE Access* 2020, *8*, 34362–34374. [CrossRef]
- 70. Kassiri, H.; Chemparathy, A.; Salam, M.T.; Boyce, R.; Adamantidis, A.; Genov, R. Electronic Sleep Stage Classifiers: A Survey and VLSI Design Methodology. *IEEE Trans. Biomed. Circuits Syst.* **2017**, *11*, 177–188. [CrossRef]
- 71. Schizas, C.N.; Pattichis, C.S. Learning systems in biosignal analysis. Biosystems 1997, 41, 105–125. [CrossRef]
- 72. Wang, L.; Song, F.; Zhou, T.H.; Hao, J.; Ryu, K.H. EEG and ECG-Based Multi-Sensor Fusion Computing for Real-Time Fatigue Driving Recognition Based on Feedback Mechanism. *Sensors* **2023**, *23*, 8386. [CrossRef]
- 73. Paz, F.; Ordonez, M. High-Performance Solar MPPT Using Switching Ripple Identification Based on a Lock-In Amplifier. *IEEE Trans. Ind. Electron.* **2016**, *63*, 3595–3604. [CrossRef]
- 74. Sun, T.; van Berkel, C.; Green, N.G.; Morgan, H. Digital signal processing methods for impedance microfluidic cytometry. *Microfluid Nanofluid* **2009**, *6*, 179–187. [CrossRef]
- 75. Bhattacharyya, S.; Ahmed, R.N.; Purkayastha, B.B.; Bhat-tacharyya, K. Implementation of digital lock-in amplifier. *J. Phys. Conf. Ser.* **2016**, 759, 012096. [CrossRef]
- Milhem, S.F.; Mahmoud, S.A. CMOS digitally programmable lock-in amplifier for eeg detection system. In Proceedings of the 2017 International Conference on Electrical and Computing Technologies and Applications (ICECTA), Ras Al Khaimah, United Arab Emirates, 21–23 November 2017; pp. 1–4.
- 77. Hou, Y.; Li, C.; Tang, S. An Accurate DDS Method Using Compound Frequency Tuning Word and Its FPGA Implementation. *Electronics* **2018**, *7*, 330. [CrossRef]
- 78. De Marcellis, A.; Ferri, G.; D'Amico, A. One-Decade Frequency Range, In-Phase Auto-Aligned 1.8 V 2 mW Fully Analog CMOS Integrated Lock-In Amplifier for Small/Noisy Signal Detection. *IEEE Sens. J.* **2016**, *16*, 5690–5701. [CrossRef]
- Shaikh, F.; Haworth, N.; Wells, R.; Bishop, J.; Chatterjee, S.K.; Banerjee, S.; Laha, S. Compact Instrumentation for Accurate Detection and Measurement of Glucose Concentration Using Photoacoustic Spectroscopy. *IEEE Access* 2022, 10, 31885–31895. [CrossRef]
- Pfeiffer, U.R.; Hillger, P.; Jain, R.; Grzyb, J.; Bucher, T.; Cassar, Q.; MacGrogan, G.; Guillet, J.P.; Mounaix, P.; Zimmer, T. Ex Vivo Breast Tumor Identification: Advances Toward a Silicon-Based Terahertz Near-Field Imaging Sensor. *IEEE Microw. Mag.* 2019, 20, 32–46. [CrossRef]
- Holub, J.; Aumala, O. Data Processing and Dither Enhancement of ADC Parameters—Trends, Applications, Limits. In Proceedings of the 4th International Conference on Advanced A/D and D/A Conversion Techniques and Their Applications & 7th European Workshop on ADC Modelling and Testing, Prague, Czech Republic, 26–28 June 2002; pp. 127–134.
- 82. Corminboeuf, D. Calibration of the Absolute Linearity of Lock-In Amplifiers. *IEEE Trans. Instrum. Meas.* **2019**, *68*, 2060–2065. [CrossRef]
- Sarma, V.; Ravi, C.; Sahoo, B.D. Achieving Theoretical Limit of SFDR in Pipelined ADCs. *IEEE Trans. Very Large Scale Integr. Syst.* 2017, 25, 3175–3185. [CrossRef]
- Das, A.; Yaswanth, T. A low-cost, portable alternative for a digital lock-in amplifier using TMS320C5535 DSP. In Proceedings of the 2015 Annual IEEE India Conference (INDICON), New Delhi, India, 17–20 December 2015; pp. 1–4.
- Sonnaillon, M.O.; Urteaga, R.; Bonetto, F.J.; Ordonez, M. Implementation of a high-frequency digital lock-in amplifier. In Proceedings of the Canadian Conference on Electrical and Computer Engineering, Saskatoon, SK, Canada, 1–4 May 2005; pp. 1229–1232.

- Rahmannuri, H.; Rivai, M.; Sardjono, T.A. Design of digital lock-in amplifier for low concentration gas detection. In Proceedings of the 2017 International Seminar on Intelligent Technology and Its Applications (ISITIA), Surabaya, Indonesia, 28–29 August 2017; pp. 319–322.
- Liu, Z.; Zhu, L.; Koffman, A.; Waltrip, B.C.; Wang, Y. Digital lock-in amplifier for precision audio frequency bridge. In Proceedings of the 2012 Conference on Precision Electromagnetic Measurements, Washington, DC, USA, 1–6 July 2012; pp. 586–587.
- Cheng, J.; Xu, Y.; Wu, L.; Wang, G. A Digital Lock-in Amplifier for Use at Temperatures of up to 200 °C. Sensors 2016, 16, 1899.
 [CrossRef]
- Herley, C.; Wong, P.W. Efficient Minimum Rate Sampling of Signals with Frequency Support over Non-Commensurable Sets. In Modern Sampling Theory. Applied and Numerical Harmonic Analysis; Benedetto, J.J., Ferreira P.J.S.G., Eds.; Birkhäuser: Boston, MA, USA, 2001.

Disclaimer/Publisher's Note: The statements, opinions and data contained in all publications are solely those of the individual author(s) and contributor(s) and not of MDPI and/or the editor(s). MDPI and/or the editor(s) disclaim responsibility for any injury to people or property resulting from any ideas, methods, instructions or products referred to in the content.