Research on the Common Rail Pressure Overshoot of Opposed-Piston Two-Stroke Diesel Engines

Yi Lu, Changlu Zhao, Zhe Zuo *, Fujun Zhang and Shuanlu Zhang

School of Mechanical Engineering, Beijing Institute of Technology, Zhongguancun South Street No.5, Beijing 100081, China; luyi268@126.com (Y.L.); clzhao@bit.edu.cn (C.Z.); zfj123@bit.edu.cn (F.Z.); zhangshuanl@163.com (S.Z.)

* Correspondence: zuzeus@bit.edu.cn; Tel.: +86-10-6891-3637

Abstract: The common rail pressure has a direct influence on the working stability of Opposed-Piston Two-Stroke (OP2S) diesel engines, especially on performance indexes such as power, economy and emissions. Meanwhile, the rail pressure overshoot phenomenon occurs frequently due to the operating characteristics of OP2S diesel engines, which could lead to serious consequences. In order to solve the rail pressure overshoot problem of OP2S diesel engines, a nonlinear concerted algorithm adding a speed state feedback was investigated. First, the nonlinear Linear Parameter Varying (LPV) model was utilized to describe the coupling relationship between the engine speed and the rail pressure. The Linear Quadratic Regulator (LQR) optimal control algorithm was applied to design the controller by the feedback of speed and rail pressure. Second, cooperating with the switching characteristics of injectors, the co-simulation of MATLAB/Simulink and GT-Power was utilized to verify the validity of the control algorithm and analyze workspaces for both normal and special sections. Finally, bench test results showed that the accuracy of the rail pressure control was in the range of ± 1 MPa, in the condition of sudden 600 r/min speed increases. In addition, the fuel mass was reduced 76.3% compared with the maximum fuel supply quantity and the rail pressure fluctuation was less than 20 MPa. The algorithm could also be appropriate for other types of common rail system thanks to its universality.

Keywords: opposed-piston two-stroke diesel engine; common rail; pressure overshoot; LQR

1. Introduction

The Opposed-Piston Two-Stroke (OP2S) diesel engine concept, which has now been developed for more than a century, came to being in the end of 19th century. Gilles was the first to propose the OP2S engine scheme with only one cylinder. Based on his research, Witting manufactured the first opposed-piston engine using coal gas as fuel [1]. From then on, this technology was developed in many countries and widely applied to different domains such as aviation, shipping and trucks. However, its development was limited for a long time by the appearance of emission regulations [2]. In recent years, with the evolution of new materials, new techniques and internal combustion engine electronic control technology, many corporations including FEV, Advanced Propulsion Technologies (APT), EcoMotors and Achates Power have launched research on OP2S engines and obtained satisfactory results [3–5], hence people have come to focus on this high power density two-stroke diesel engine format once again [6,7].

Benefiting from the application of electronic control, OP2S engines show stronger competitiveness in emission reductions and energy savings, especially for the electronic control high pressure common rail system. This system had a more extensive practical value due to the superiority of its high injection pressure and flexible injection parameters [8,9]. In order to meet the anticipated higher emission

regulation requirements of the future, the common rail system has to supply a more accurate control method for the engine combustion process and reduce the pollution generation. The key point of controlling fuel injection quantity precisely is to realize the control of the combustion process. The fuel injection quantity of common rail systems is determined by both rail pressure and injection duration. Under the influence of high pressure operation conditions and the self-structure features of common rail systems, a major pressure fluctuation would be generated inside the injector chamber while the needle valve of the injector is opening or closing, and the pressure wave would spread inside the system. Catania et al. [10] studied the dynamic characteristics resulting from the pressure wave spread of common rail injection systems, and they found that the pressure fluctuation of the injector entrance caused by water hammer was remarkable and it took a long time to recover from it. Henein et al. [11] studied the injection characteristics and pressure fluctuation of the common rail injection system of diesel engines. They pointed out that practical injection duration was longer than the command duration with the rising rail pressure, which could have impact on the fuel quantity accuracy. Bianchi et al. [12] indicated the necessity of correcting the fuel injection quantity due to the pressure fluctuation characteristics inside the common rail system. On the other hand, it is also necessary to study rail pressure control strategies, for the reason that the accuracy of fuel-injection quantity can be grievously affected by the stability and responsiveness of the rail pressure. At present, rail pressure control strategies mainly adopt the methodology combining feedforward control, open loop control and fuzzy Proportion Integration Differentiation (PID) control, and it also adjusts relevant parameters by monitoring the system working conditions in real time. By utilizing the feedforward rail pressure control methodology based on the parameter self-regulation fuzzy PID algorithm, Ouyang [13,14] achieved good control effects and could satisfy the accuracy requirements of rail pressure control. Huang and Song from Shanghai Jiaotong University [15] developed a high pressure common rail system named GD-1 with their colleagues and studied control strategies in depth. Xu and Wang [16] came up with a composite control strategy which could switch automatically between cascade control and open loop control. Their strategy appropriately solved the problem that rail pressure varied with the change of engine working conditions, which made rail pressure respond rapidly and precisely. Zhou [17] developed a control system for high pressure common rail systems and put forward a new cylinder detection technology.

However, the OP2S diesel engine uses a hydraulic-mechanical hybrid output method, which has an impact on the control of common rail pressure. Engine speed suddenly increases while the load of the hydraulic pump falls sharply, then the engine speed control algorithm comes into action and immediately reduces the fuel injection quantity, thus the engine speed would drop to a reasonable range. In this situation, a prompt increase of speed causes an abrupt increase of fuel supply frequency of the high pressure pump leading to a sharp rise in rail pressure. Even if the switch range of a solenoid valve could be adjusted by a conventional rail pressure control PID algorithm, a severe delay would occur which results in a sudden rail pressure increase. Meanwhile, the engine control system would appropriately reduce the fuel injection quantity due to the speed rise. Under the synergy of these two aspects, the rail pressure would bump up and threaten the safety of the whole fuel system. Although the fuel injection quantity could be accurately maintained by the engine control system, depending on the injection adjustment characteristics as well as by adjusting the injection duration after the rail pressure increased rapidly, the increase of injection pressure and decrease of injection period would influence the injection rate, combustion and switching characteristics of the solenoid valve, thus immediately influencing the working conditions, combustion stability and exhaust gas deterioration. Although partial common rail systems could adjust their dynamic responsiveness by installing Pressure Control Valves (PCVs) at the exit of the high pressure pump, this slowed up the high-speed response characteristics. This technology is therefore not universally used yet. Meanwhile, the on-off of a proportional overflow valve would intensify the pressure fluctuation inside the rail and impact the injection accuracy. Therefore, it is significant to study how to come up with a control algorithm to decrease the rail pressure overshoot by using other types of control feedback structures,

without changing any oart of the existing structure of the common rail system components. Among the options optimal control algorithms might therefore be more suitable for common rail systems.

Through the feedback of state parameters of controlled objects, optimal control methods obtain optimal effects and broad stability margins by coordinating the control expense and state indexes. Nowadays they play a vital role in engine control applications. Li and his co-workers [18,19] controlled the engine speed and made it approach the expected value by making use of a linear prediction control method and quasi-infinite time domain nonlinear model prediction control method. Fialho et al. [20] designed a self-adaptive active suspension controller and achieved an ideal operation result via the combination of a linear parameter-variety controller and a nonlinear back-stepping controller. Kjergaard et al. [21] adopted an input-output linearization strategy and sliding mode control, and conducted elaborate comparative trails within classical PID control method and Linear Quadratic Regulator (LQR) control method. Yu et al. [22] demonstrated that engine torque control based on nonlinear model prediction control had good responsiveness, by means of comparing and analyzing the direct injection engine torque control precept under feedback linearization, nonlinear model prediction control as well as gain scheduling LQ optimal control. Furthermore, a direct relationship between the rise of rail pressure and the increase of engine speed in common rail systems was been found. By utilizing a double-parameter speed-pressure-pressure control algorithm rather than the primary single-parameter pressure-pressure control algorithm, the stability control requirement for rail pressure of an OP2S diesel engine could be better met. Therefore, optimal control theory, especially the LQR theory, could be appropriately applied to control the rail pressure. In the way of coordinating the control between different parameters such as engine speed and injection quantity, a decent control effect is implemented with broad stability margin and good performance.

In order to meet the air-fuel mixture accuracy requirements under the impact of engine speed and load, the injection quantity must be measured precisely under the control of injection pressure and timing. That is, research on control algorithms is influenced by the whole fuel injection system, so it is necessary to establish a control-oriented model of a common rail injection system. Paolo et al. [23,24] built a flow nonlinear equilibrium model of common rail systems, and a simplified model of the internal rail flow from the perspective of engineering practice. They also came up with a simplified model of a sliding mode control method and figured that the method was appropriate for stability control of the common rail system nonlinear characteristics. Catania et al. [25] came up with a simple lumped parameter model of system vibration phenomena through a phenomenological analysis. They also put forward a referenced simplified model aiming at one-time fluctuation effect, based on which the fuel quantity could be amended. This method is representative fuel quantity control of common rail systems at present. Di Gaeta et al. [26,27] utilized a sliding mode method to control rail pressure as well. For the purpose of stability control of rail pressure, they established a more detailed mathematical model of a common rail system. Nevertheless, the most difficult part of the sliding mode control method is the control signal step, which results in chattering phenomenon. On account of the inherent fluctuation characteristics of rail pressure, the application of this method was partially limited.

In this paper, a common rail system mathematical model addressing the control strategy and a nonlinear Linear Parameter Varying (LPV) model used to reflect the coupling relationship between the engine condition and the rail pressure were established, which aimed at the problem that rail pressure might suddenly increase because of a sudden change of engine speed in an OP2S diesel engine. A LQR control algorithm for speed feedback optimal generalized scheduling control was put forward, which was based on the LPV model. In order to achieve a favorable control result on rail pressure, a MATLAB/Simulink and GT-Power co-simulation model was used to design referable control parameters in offline mode. In addition, the control parameters and engine speed as well as rail pressure were controlled concertedly. This turned out to achieve a wide stability margin and good consistency.

2. Experimental System

The development of the common rail system required original system experiments and calibrations on the component test bench, in order to accomplish some steady tests of the injection and pressure fluctuation characteristics. These processes could also verify and test the stability and performance of the common rail control algorithm. Generally, a common rail component test bench is composed of an injection system pump rig, pressure sensors with both high and low sensitivity, current clamp, a high-speed data acquisition system and fuel single injection equipment. After completing the component experiments and verification, the overall test could be conducted, which mainly focused on performance parameters, such as engine power, torque, dynamic variation and control performance indexes. Meanwhile, some other parameters like cooling water temperature, oil temperature, intake air temperature and pressure etc. ought to be monitored to adjust the control parameters in real time and protect the engine from malfunctions. The engine test bench was universally made up of a complete motor, dynamometer, cooling circulatory system and monitoring system. The experimental prototype test bench and measurement equipment are illustrated in Figure 1.
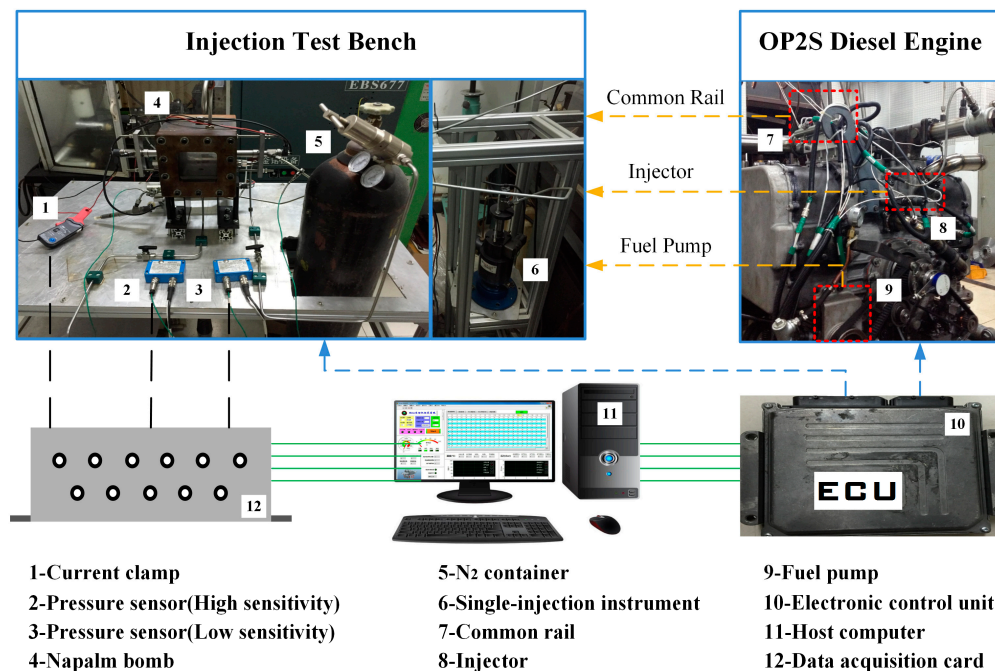

1-Current clamp	5-N$_2$ container	9-Fuel pump
2-Pressure sensor(High sensitivity)	6-Single-injection instrument	10-Electronic control unit
3-Pressure sensor(Low sensitivity)	7-Common rail	11-Host computer
4-Napalm bomb	8-Injector	12-Data acquisition card

Figure 1. Experimental prototype test bench and measurement equipment.

3. Common Rail System Model and Rail Pressure Control Algorithm

3.1. Common Rail System Model

3.1.1. OP2S Configuration

The OP2S diesel engine uses a hydraulic hybrid output method, which gets rid of the cylinder head. Each two pistons share one cylinder with a head in a level symmetrical layout and the flat combustion chamber is composed of two piston top surfaces and the cylinder wall. The injector, which injects the fuel into the combustion chamber from one side, was installed beside the cylinder jacket. It has only two strokes in a cycle and utilizes a uniflow scavenging system. The air inlet and outlet were both controlled by two pistons to accomplish the opening and closing motions, and these pistons promoted their own connecting rod mechanism respectively in order to drive the crankshaft by the synchronizing mechanism. The engine structure is shown in Figure 2 and the parameters of the engine are listed in Table 1.
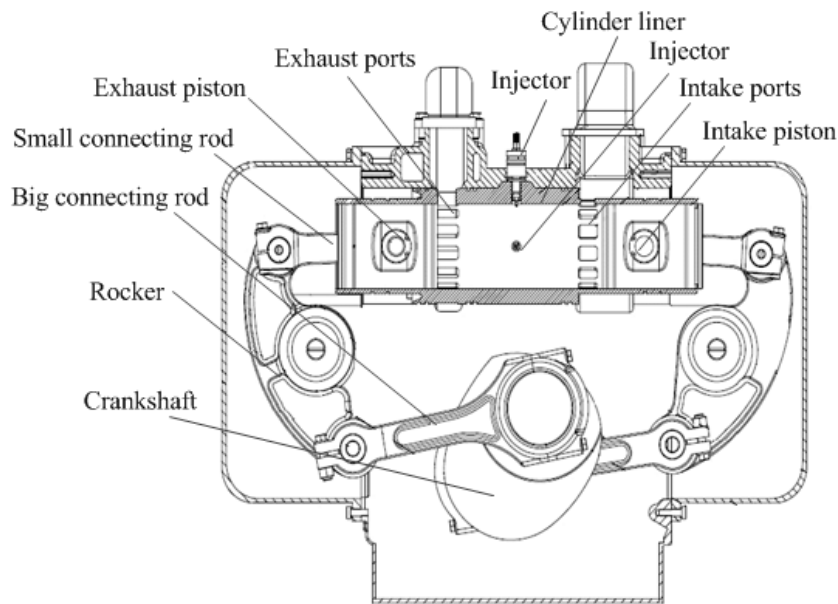
Figure 2. Configuration of OP2S diesel engine.

Table 1. Parameters of the OP2S diesel engine.

Parameter Item (Units)	Value
Number of cylinders (-)	2
Cylinder diameter (mm)	100
Stroke (mm)	110
Displacement (L)	3.4
Phase difference of the opposed-piston (°CA)	17
Maximum power (kW)	80 (2400 rpm)
Maximum torque (Nm)	420 (1600 rpm)
Nominal compression ratio (-)	22
Angle of intake valve open (°CA)	116
Angle of intake valve close (°CA)	110
Angle of exhaust valve open (°CA)	100
Angle of exhaust valve close (°CA)	113

3.1.2. Fuel System Model

The configuration of the fuel system of the engine is shown in Figure 3. It consists of a low and a high-pressure circuit, including the fuel tank, a low pressure gear pump connected with the crankshaft, a high-pressure plunger pump with an electro-hydraulic proportional delivery valve, a common rail and the injector. An inline electric low pressure gear pump takes the fuel out of the tank and injects it into a low-pressure cycle. After being throttled by an electronic-hydraulic proportional valve which was driven by a Pulse Width Modulation (PWM) square wave current, adequate fuel is supplied to the high pressure pump. The nominal rail pressure was reached during compression of the high pressure pump piston and the fuel was then delivered to the pump-to-rail pipe in order to maintain the common rail pressure stability. Subsequently, the injector, which was linked to the high pressure fuel pipe and common rail, would conduct the injection process under Electronic Control Unit (ECU) control according to the injection requirements.
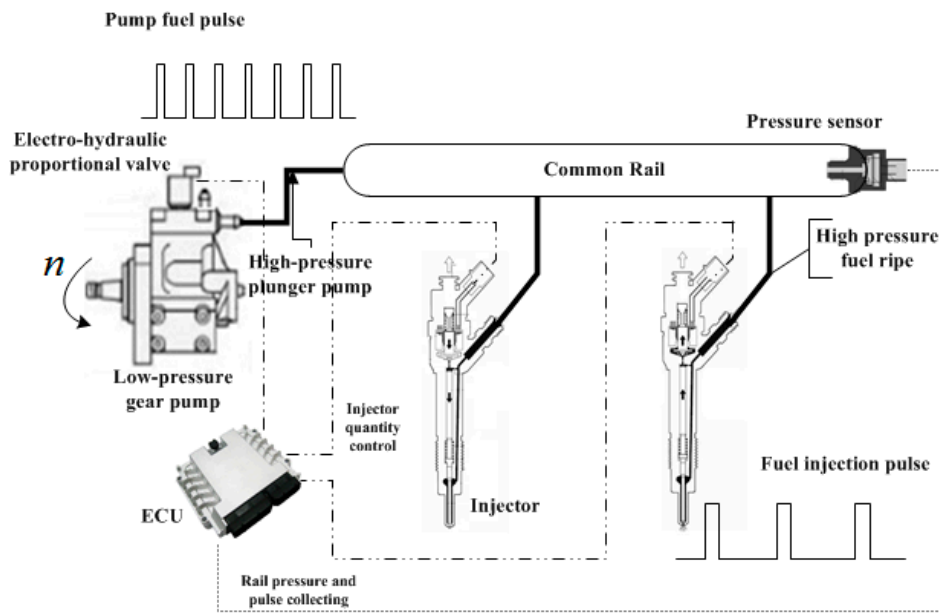
Figure 3. A block scheme of the common rail injection system for diesel engines.

Like in the common rail system of an OP2S diesel engine, the strong nonlinearities caused by the complex flow of fuel resulted in difficulties for designing the fluid dynamic model, and an excessively detailed consideration could not help us to design a control algorithm. Thus the choice of model parameters and empirical formulas during modeling was based on the adaptability of the control target. Referring to [23], the model was divided on account of control volume, fuel dynamic pressure was described through combining together Newton's motion law, the equation of continuity and the momentum equation. The bulk modulus formula of fluids was utilized to establish the flow-pressure differential equation, including high-pressure pump, common rail and fuel injector, based on the fuel pressure of different components in the common rail system [21]. Then, the relevant mathematical model was obtained. Fuel compressibility could be expressed by the bulk modulus formula:

$$K_f = -\frac{\mathrm{d}p}{\mathrm{d}v/v} \tag{1}$$

It could be approximated by an empirical formula as:

$$K_f = 1200 \cdot (1 + 0.6 \cdot \frac{p}{600}) \tag{2}$$

From (1), the following formula could be obtained:

$$\frac{dp}{dt} = -\frac{K_f}{v} \cdot \frac{\mathrm{d}v}{\mathrm{d}t} \tag{3}$$

where, $\mathrm{d}v/\mathrm{d}t$ took account of the inflow q_{in} and outflow q_{out}, and the volume changed $\mathrm{d}V/\mathrm{d}t$ resulted from mechanical motion. Thus, Formula (3) could be written as:

$$\frac{dp}{dt} = -\frac{K_f}{v} \cdot \left(\frac{\mathrm{d}V}{\mathrm{d}t} - q_{in} + q_{out}\right) \tag{4}$$

V is a constant volume for all the elements in the common rail system, except the high pressure pump, therefore, it could be canceled. Both q_{in} and q_{out} could be obtained from the law of conservation

of energy. The general flow formula of fuel flowing through the fuel orifice was as follows, which was based on Bernoulli's Equation:

$$q = \text{sgn}(\delta p) \cdot c \cdot A \sqrt{\frac{2|\delta p|}{\rho}} \tag{5}$$

where δp represents the pressure difference between both sides of the sectional area. The mathematical model of the high pressure pump, common rail and injector of the OP2S diesel engine common rail system could be established by using the above modeling principles.

3.1.3. High-Pressure Pump Model

A CP1H3 high pressure pump was chosen for this common rail system. Due to the complexity of its working principle, it should be simplified while modeling. Inside the triple plunger pump, pumping occurred three-times during one rotation of the camshaft. As a consequence, the rotation speed of the camshaft should rise up to three times while the fuel should be supplied by only one plunger in order to simplify it.

The plunger chamber volume of the high pressure pump varied with the camshaft rotation. Combined with the camshaft shape lines, the plunger chamber volume could be expressed as:

$$V_p(\alpha) = V_p{}^0 - A_p \cdot s_p(\alpha) \tag{6}$$

Considering the rate of change, the equation below could be obtained after taking the derivative of Equation (6):

$$\frac{dV_p}{dt} = -A_p \cdot \frac{ds_p}{dt} = -A_p \cdot 2\pi n \cdot \frac{ds_p}{d\alpha} \tag{7}$$

where $V_p{}^0$ represents the chamber volume when the plunger was at the Bottom Dead Center (BDC) position, and the engine crankshaft was driven by the belt at a 1.125-fold rotation speed.

On the basis of plunger distance variation curve related to camshaft shape lines, the fitting formula could be obtained as:

$$s_p(\alpha) = [2.85 - 2.85\cos(0.01745\alpha)] \times 10^{-3} \tag{8}$$

Taking the derivative of Equation (8), the following expression was obtained:

$$\frac{ds_p(\alpha)}{d\alpha} = 4.97\sin(0.01745\alpha) \times 10^{-5} \tag{9}$$

The pressure differential equations in each plunger chamber of the high pressure pump could be obtained as follows relating to the modeling principles:

$$\dot{p}_p = -\frac{K_f}{V}\left(-A_p \cdot 2\pi n \cdot \frac{dh_p}{d\theta} + q_s - q_r\right) \tag{10}$$

After the fuel flows past the gear pump, the stepped fuel returned to the valve and the high pressure fuel pump solenoid valve were connected in parallel, which kept the fuel pressure of the solenoid valve inlet stable and p_g was around 0.5 MPa. This insured that system could work normally. The flow via the solenoid valve is as follows:

$$q_s = \text{sgn}(p_p - p_g)c_p A_p \sqrt{\frac{2|p_p - p_g|}{\rho}} \cdot u_{\text{PWM}} \tag{11}$$

where q_r could be obtained from the following equation:

$$q_r = \text{sgn}(p_r - p_p)c_r A_r \sqrt{\frac{2|p_r - p_p|}{\rho}} \tag{12}$$

3.1.4. Common Rail Pipe Model

Essentially, a common rail is a long, tubular, high pressure container, which stores high pressure fuel inside and distributes high pressure fuel to each injector through a fuel injection pipe. Meanwhile, the rail reduces the pressure fluctuation caused by the fuel injection procedure and fuel supply procedure.

Considering that there is no rail deformation and no volume variation, two injectors installed in the circumferential direction in each cylinder of the OP2S diesel engine could inject fuel at the same time. The common rail pressure differential equation could then be obtained as:

$$\dot{p}_r = \frac{K_f(p_r)}{V_r}(q_r - 2 \cdot q_{i,k}) \tag{13}$$

where, k = 1, 2, 3, 4 represent four injectors, respectively.

Besides:

$$q_{i,k} = \text{sgn}(p_r - p_{i,k})c_{i,k}A_{i,k}\sqrt{\frac{2|p_r - p_{i,k}|}{\rho}} \tag{14}$$

3.1.5. Fuel Injector Model

In the injector modeling process, the pressure chamber volume was regarded as approximately constant. Thus, the pressure differential equation of injector pressure chamber could be obtained as:

$$\dot{p}_{i,k} = \frac{K_f(p_{i,k})}{V_{i,k}}(q_{i,k} - q_{cyl,k}) \tag{15}$$

and $q_{cyl,k}$ could be obtained by the following equation:

$$q_{cyl,k} = \text{sgn}(p_{i,k} - p_{cyl,k})c_{i,k}E_{T,k}A_{i,k}\sqrt{\frac{2|p_{i,k} - p_{cyl,k}|}{\rho}} \tag{16}$$

3.1.6. Fuel Quantity-Torque Transformation Model

The injection process of a common rail system is not totally independent from engine speed and load, and the fuel supply quantity is influenced by the engine speed and the injection quantity is influenced by load, which could cause a pressure fluctuation in the common rail. Therefore, the state of the common rail system is directly related to the engine working conditions. However, considering that the engine combustion process is complicated and it is difficult to control the combustion process timely and precisely in the actual control, it is thus quite significant to set up a simplified conversion model of the fuel quantity-torque faced with control implemention, which could satisfy the control requirements of the rail pressure overshoot problem of the common rail system. According to the relationship between engine speed and load, the conversion model of fuel quantity-torque of OP2S diesel engine could be simplified as:

$$\dot{n} = \frac{1}{J_{Engine}}\left(T_{Engine} - T_{load} - T_f\right) \tag{17}$$

where J_{Engine} represents the moment of inertia of the engine crankshaft, T_{Engine} represents the indicated torque, T_{load} represents the load caused by the fuel pump, oil pump, water pump and other attachments. T_f represents the load caused by friction and lubrication while the engine is working.

Experimental calibration for mechanical losses of the OP2S diesel engine was conducted by utilizing an indicator diagram. According to the experimental data obtained on the test bench shown in Table 2, the fitted equation of drag torque and engine speed is:

$$T_f = 0.23 \cdot n - 90.89 \tag{18}$$

Table 2. Experimental data of the OP2S diesel engine.

Engine Speed (r/min)	Indicated Torque (N·m)	Effective Power (KW)	Mechanical Losses (KW)	Torque Losses (N·m)
900	11.111	0	11.111	117.909
1200	20.962	4.712	16.250	166.823
1400	32.103	10.995	21.108	218.992
1600	46.007	18.848	27.159	274.606

The indicated power of the engine could be expressed as:

$$P_i = q_{cyl,k} \cdot i \cdot H_u \cdot \eta_{it} \cdot n / 60 \tag{19}$$

where H_u represents the low heating value of diesel, in kJ/mg units i represents the number of cylinders, η_{it} represents the indicated thermal efficiency, $q_{cyl,k}$ represents the cycle fuel injection quantity, in mg/cyc units.

Indicated torque was expressed as:

$$T_{Engine} = 9550 \cdot q_{cyl,k} \cdot i \cdot H_u \cdot \eta_{it} / 60 \tag{20}$$

From the formula, the indicated torque of the engine was proportional to the cycle fuel injection quantity. Considering that:

$$K_T = 9550 \cdot i \cdot H_u \cdot \eta_{it} / 60 \tag{21}$$

The expression could be transformed into:

$$T_{Engine} = K_T \cdot q_{cyl,k} \tag{22}$$

According to the parameters of the OP2S diesel engine, the equation could be integrated as:

$$\dot{n} = \frac{1}{J_{Engine}} \left[2 \cdot K_T E_T c_i A_i \sqrt{\frac{2p_r}{\rho}} - (0.23n - 90.89) - T_{load} \right] \tag{23}$$

3.2. Rail Pressure Control Algorithm

Considering that the common rail mathematical model has a high order and a complex form, and the nonlinear factors make it more difficult to design the control algorithm, therefore, a simplifying and linearizing model became a necessary objective in order to design the controller.

Currently, PID control algorithms have been widely applied for rail pressure control, but the control delay problem caused by the calculation of control parameters under the state of rail pressure overshoot still exists. According to the mathematical model, it could be found that rail state is influenced by parameters such as speed, pressure, etc. Reaction speed and precision of the control system could be enhanced with the speed feedback addition under the rail pressure control. The control type using both rail pressure and speed as double parameter feedback has the same construction as the classical optimal control.

Optimal control was the representative fruit of modern control theory, which gave the optimal control effect of both control cost and state index harmonization, so the LQR scheduling control

algorithm based on state space and the PID control algorithm optimized by optimal control are introduced as follows.

3.2.1. Simplification of Common Rail Mathematics Model

In this paper, the major research direction was the study of influence of the speed fluctuation on rail pressure. Rail pressure was established by balancing the fuel supply flow and fuel injection flow. The model of the high pressure fuel pump was simplified because of its complexity and tough computation process for fuel supply flow. The high pressure fuel pump supplied fuel three times in each cycle of the camshaft, and it was directly proportional to speed frequency. Meanwhile, it was influenced by the PWM signal which was used to control the solenoid valve so that the fuel supply flow from the pump could be simplified using Equation (24):

$$q_s = \frac{n}{60} \cdot 3 \cdot V_p \cdot u_{PWM} \tag{24}$$

Like the pump, the fuel injection flow from the injector was also simplified. The injection flow rate could be obtained as follows while the pressure in injector pressure chamber was considered to be approximately equal to that in the rail:

$$q_{cyl,k} = c_{i,k} E_{T,k} A_{i,k} \sqrt{\frac{2|p_r|}{\rho}} \tag{25}$$

where the rail pressure p_r and speed n were chosen as two states, and the system state equation could be obtained by:

$$\begin{cases} \dot{p}_r = \frac{K_f(P_r)}{V_r} \left(\frac{n}{60} \cdot 3 \cdot V_p \cdot u_{PWM} - 2 \cdot E_T c_i A_i \sqrt{\frac{2p_r}{\rho}} \right) \\ \dot{n} = \frac{1}{J_{Engine}} \left[2 \cdot K_T E_T c_i A_i \sqrt{\frac{2p_r}{\rho}} - (0.23n - 90.89) - T_{load} \right] \end{cases} \tag{26}$$

Considering the coupling relationship between state variables and control variables, a corresponding transformation should be conducted on Equation (24), so the rail fuel quantity was transformed into:

$$q_s = \frac{n}{60} \cdot 3 \cdot V_p - \frac{n}{60} \cdot 3 \cdot V_p \cdot u_{PWM} \tag{27}$$

After the transformation, the two state parameters, namely rail pressure p_r and speed n were respectively written as x_1, x_2. The output parameter was still rail pressure p_r, and it is written as y. Substituting other parameters of the OP2S diesel engine, the state space form of the system could be obtained as:

$$\begin{cases} \begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = a \begin{bmatrix} -0.088 \cdot E_T \sqrt{\frac{1}{p_r}} & 0.456 \\ 0.1 \cdot E_T \sqrt{\frac{1}{p_r}} & -0.29 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \\ + b \begin{bmatrix} -0.456n \\ 0 \end{bmatrix} u_{PWM} - \begin{bmatrix} 0 \\ 1.25 \end{bmatrix} T_{load} \\ y = \begin{bmatrix} 1 & 0 \end{bmatrix} \begin{bmatrix} p_r \\ n \end{bmatrix} \end{cases} \tag{28}$$

During the realization process of the OP2S rail pressure control, the integral error between reactive system current state and target state could be defined as the system error expansion, named ξ_e, according to the servo compensation design method. Coordination control of speed, fuel quantity and rail pressure without static error and using classical weight function-optimal control calculation method, the off-line design controller could be realized, by the influence of torque disturbance of

load, uncertainty and model simplification compensated by the state parameters. After designing the dimension expansion of servo compensation, the system state space equation was as follows:

$$
\begin{cases}
\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{\zeta}_e \end{bmatrix} = a \begin{bmatrix} -0.088 \cdot ET\sqrt{\frac{1}{p_r}} & 0.456 & 0 \\ 0.1 \cdot ET\sqrt{\frac{1}{p_r}} & -0.29 & 0 \\ -1 & 0 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \zeta_e \end{bmatrix} + b \begin{bmatrix} -0.456n \\ 0 \\ 0 \end{bmatrix} u_{\text{PWM}} \\
y = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \zeta_e \end{bmatrix}
\end{cases}
\tag{29}
$$

$$
u_{\text{LQR}} = -K_p \cdot x_1 - K_n \cdot x_2 - K_e \cdot x_3 + K_p \cdot p_d
\tag{30}
$$

3.2.2. LPV Linearization of the Common Rail Space Model

It could be found out that the state equation in a common rail system is influenced by the time-variant and nonlinear parameters p_r and ET via simplification of the rail model. With the control of state feedback, the classical linear control method guarantees the system stability, but no consistency of control effect. Therefore, the LPV method was adopted in this study for solving the problems of control system design that was affected by time-variant parameters, and achieving a stable control of the rail pressure. With the method, some foreign experts and scholars had made efforts on the vehicle control system modeling and control domain. This was applied in the air intake system of diesel engines in [28] and in the time-variant parameter identification of gasoline engines in [29]. In [30,31], a LPV-based scheduling method, specific to wetted wall engine parameters and engine speed time-variant parameters was put forward. By utilizing group design of PID and PID control parameters, the control problem of the influence of time-variant parameters to the nominal model during dynamic processes could be solved.

If the state matrix of a finite-dimensional system is the function of time-variant vector parameters, this sort of system is collectively called a LPV system. The time-variant vector parameter in LPV is a bounded set which can measure the specific values in real time without variety track prediction. In controller design problems of both linear time-invariant systems and linear time-variant systems, making the most of measurable information about the measurable time-variant parameters in the system and designing a control system with the study conclusion of linear control theory were the key points of utilizing the LPV system.

Directed at the rail pressure control problem, the pressure is influenced by the injection quantity and supply quantity, where injection quantity is a nonlinear function of the rail pressure state p_r and the time-variant measurable fuel injection pulse width ET. The fuel injection pulse width has a time-variant characteristic because of its variation under different engine conditions. Meanwhile it was also influenced by wide rail pressure fluctuation and nonlinear variation under certain conditions. As a consequence, the rail pressure must be controlled by harmonizing the engine speed and injection quantity to guarantee a stable rail pressure and to restrain the impact of rail pressure overshoot. The control principle of LPV aimed at common rail systems is shown in Figure 4. The control system would detect the current pressure state p_r by a pressure sensor installed at the end of the common rail, and the control deviation e was obtained by subtracting the target pressure p_d from the current pressure p_r. Weighted integral calculations were made on control deviation e, and finally the results are summed up to get the control parameter. The control parameter could control the electric current of the throttle valve and adjust the opening angle of the valve through use of a duty cycle. Thus the goal of adjusting the pressure could be attained.
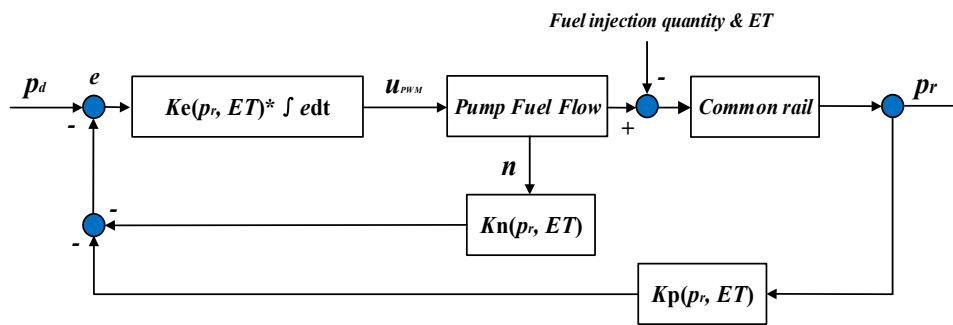
Figure 4. LPV control principle.

There were two nonlinear parameters (p_r, ET) in the 3×3 matrix of Equation (22), which present the time-varying problem of the coefficient matrix while using the previous solution method based on the original equation. A unit gain coefficient of control variable could not be obtained. However, both of the time-varying nonlinear parameters (p_r, ET) were measurable parameters. Referring to the LPV method, these measurable parameters could be substituted into the primary equation for solving, and the coefficient table, namely $K_p(p_r, ET)$, $K_n(p_r, ET)$, $K_e(p_r, ET)$, which was directly related to those two parameters (p_r, ET). This table could be updated by a look-up table program during the control implementation process, and the control equation can be shown as:

$$u_{LPV} = -K_p(p_r, ET) \cdot p_r - K_n(p_r, ET) \cdot n + K_e(p_r, ET) \cdot \int e \, dt + K_p(p_r, ET) p_d \qquad (31)$$

Hereby, for each certain condition of p_r and ET, there must be a corresponding control solution that can satisfy the control expectations. The control parameters confirmed the control characteristic parameter group of the state feedback control variable K and the time-variant measurable parameters p_r and ET via off-line design. The rail pressure could be controlled by different maps based on these parameters. In other words, on the basis of the LPV method, the controller parameters could be obtained by utilizing a linear control method to solve nonlinear control problems with the off-line design.

3.2.3. LQR Scheduling Control Algorithm Based on LPV Model

The LQR optimal control method possesses the advantage of computing the feedback control gain matrix [32] by providing a whole set of systems based on optimal control theory. Compared with general optimal control problems, linear quadratic type optimal control problems have two distinct features. First, most research objects of optimal control problems are multi-input multi-output dynamic systems, including single-input single-output types as an exceptional case. Second, the performance of the research system was comprehensive, flexible and practical.

The LQR scheduling control algorithm was designed to solve the rail pressure overshoot problems based on the LPV model. Simulation and validation experiments were completed to obtain the final controller by revising the weight function. Figure 5 shows the design process.

The OP2S diesel engine common rail system has a target pressure of 60~120 Mpa under different conditions. While $60 \leq p_r \leq 140$ MPa, the step value was chosen as 20. Fuel injection characteristics were between 500 to 2500 μs and the step was chosen as 500 μs. Each p_r and ET in different states were calculated with the LQR control parameter method. The rail pressure, speed and servo compensation state feedback parameter were respectively represented as K_p, K_n, K_e.
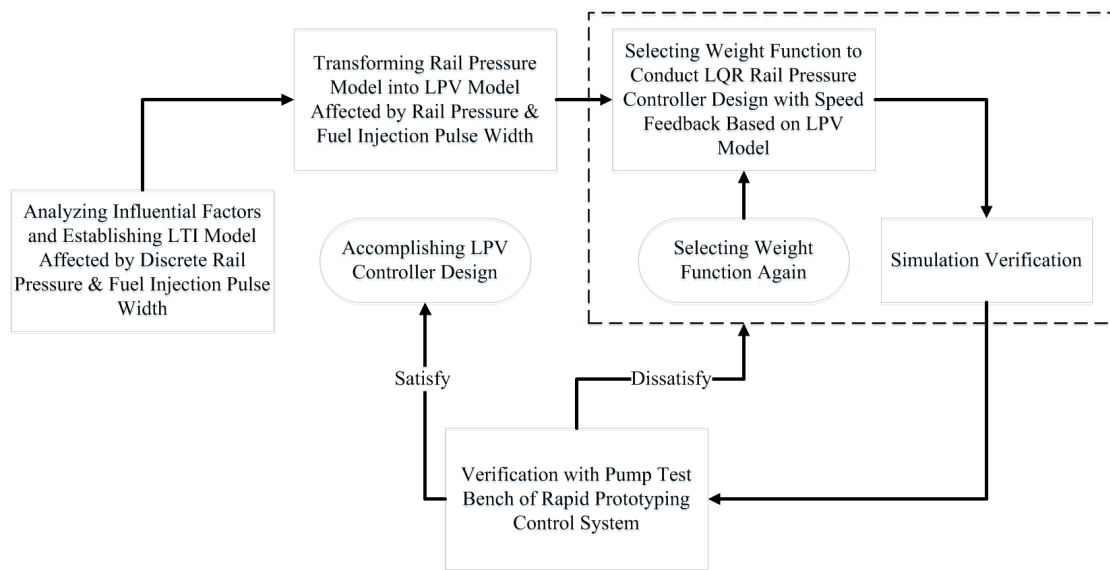
Figure 5. Design flow of the LQR scheduling control algorithm based on the LPV model.

The parameters *Q* and *R* were selected as:

$$Q = \begin{bmatrix} 1 & 0.1 & 0.1 \\ 0.1 & 1 & 0.1 \\ 0.1 & 0.1 & 1000 \end{bmatrix}, R = [1] \tag{32}$$

Then by substituting matrix *A*, *B*, *C* and *D* into the Riccati Equation, namely Equation (33), the positive definite matrix *P* could be obtained. By calculating the feedback matrix *K* with Equation (34), the LQR scheduling control parameters group was finally designed and obtained, as shown in Figures 6–8.

$$PA + A^T P - PBR^{-1}B^T P + C^T QC = 0 \tag{33}$$

$$K^T = R^{-1}B^T P \tag{34}$$
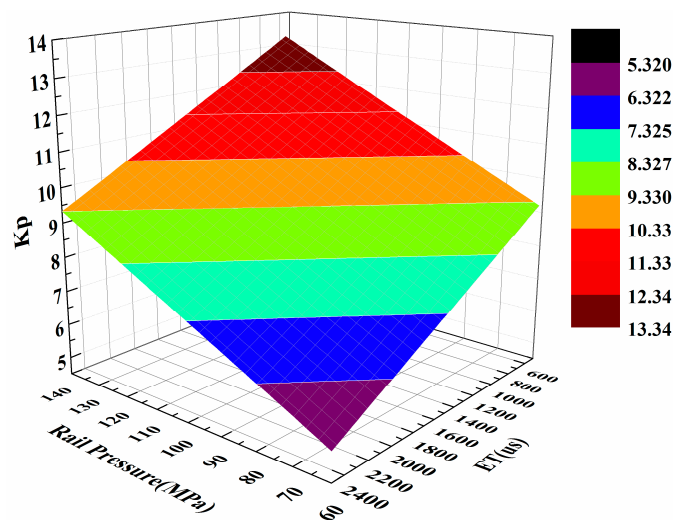
Figure 6. K_p distribution at different rail pressures and *ET*.
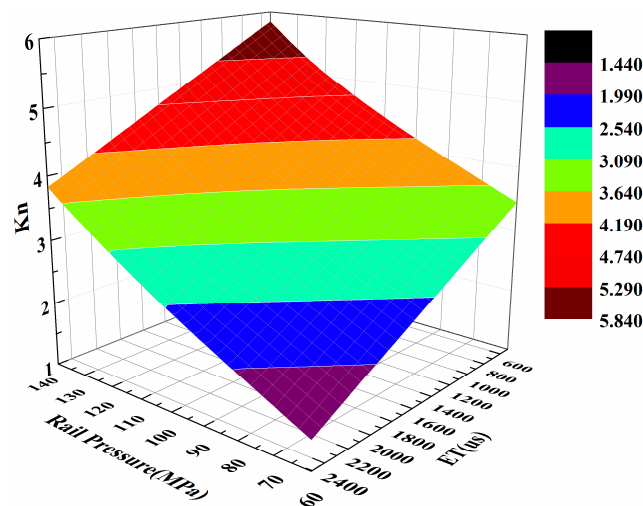
Figure 7. *K*n distribution at different rail pressures and *ET*.
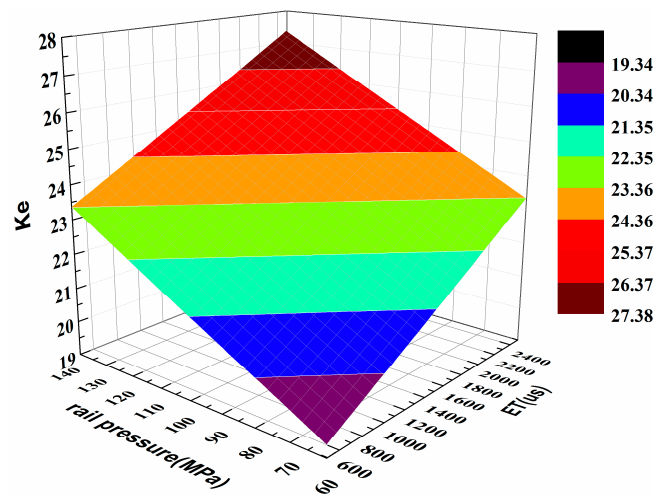
Figure 8. *K*e distribution at different rail pressures and *ET*.

3.2.4. Optimal Control PID Control Algorithm

The PID control algorithm has been optimized and the control principle is shown in Figure 9. The control system would detect the current pressure state p_r by a pressure sensor installed at the end of the common rail, and the control deviation e was obtained by subtracting the desired pressure p_d and the current pressure p_r. Multiplication and integral calculations were made on control deviation e with different weights, and the results finally summed to get the control parameter. The control parameter could control the electric current of the throttle valve and adjust the opening angle of valve through the form of a duty cycle. Thus the goal of adjusting the pressure could be reached. The characteristic was that the integral coefficient was defined as the dimension expansion coefficient K_i, the proportionality coefficient was defined as K_p, which was the same as the system setup, and controller design was conducted by utilizing state feedback theory. Because that variable design parameters only contained the output state feedback and the integral of output state feedback, other state control effects are lacking in some aspects compared with an n-dimensional full-state feedback controller. Zhu [33] has studied in depth optimal control with PID control algorithms. Referring to his method, the PID and LQR control algorithms were combined in this paper. While Proportion (P) has the same definition as the pressure feedback coefficient K_p, integration (I) has the same definition as the error integral feedback coefficient K_e. Because of the lack of feedback loop, the engine speed feedback coefficient K_n

could only be 0, and the system could perform the calculations by setting K_n as a constant 0. Thus the optimal PID control parameters could be theoretically obtained.
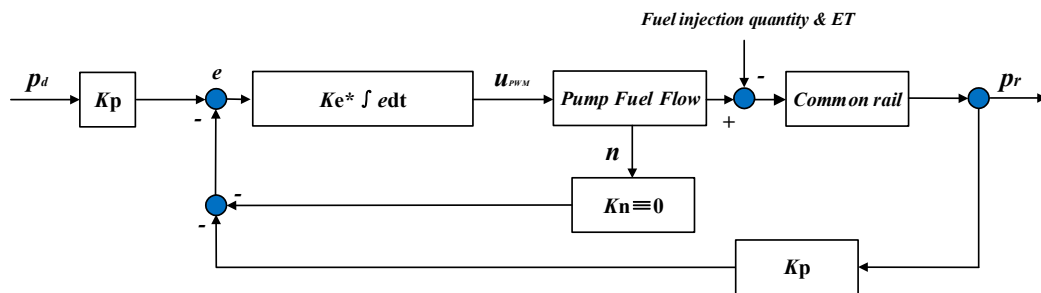

Figure 9. Control principle of PID optimized by optimal control.

3.3. Analysis of Rail Pressure Overshoot

3.3.1. Co-Simulation Model

According to the common rail system mathematical model, a simulation model could be established in MATLAB/Simulink, as shown in Figure 10. After analyzing and calculating the model, partial parameters such as rail pressure, engine speed and fuel mass could be obtained and appropriately served as the input parameters of GT-Power [34] for the following 1D in-cylinder process simulation. Both MATLAB/Simulink and GT-Power are widely used in engine design because of their flexibility [35,36].
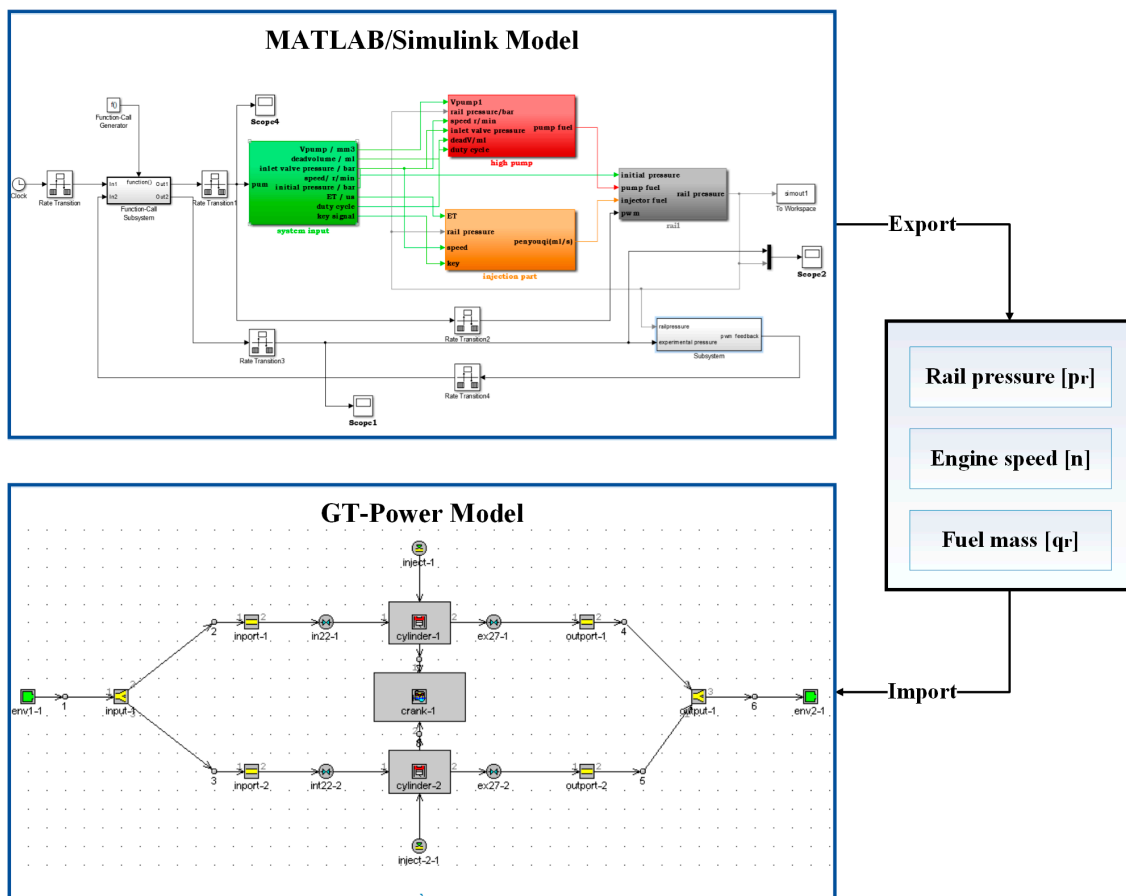

Figure 10. Co-simulation of OP2S engine using MATLAB/Simulink & GT-Power.

3.3.2. Results and Analysis

The PID control algorithm could adjust the opening for the electro-hydraulic proportional throttle valve by detecting the error between the practical and target rail pressure. The amount of adjustment amount is related to the rail pressure error. The process for adjusting the rail pressure with the PID algorithm is as follows:

Before the sudden increase of engine speed, there is no significant rise for pressure since the injection quantity had no obvious reduction. Because of the small rise in the detected pressure, the solenoid valve closes a little, thus the inlet fuel flow mass decreases a little. On account of the influence of the different parameters and the update period of the controlled quantity, the latter has had a weak impact on the fuel pump and the fuel supply quantity varies inconspicuously. The rail pressure rises rapidly with the prompt reduction of the injection quantity resulting from engine speed overshoot. When the pressure overshoot is perceived and the solenoid valve is closed by the PID controller, a large pressure overshoot has already occurred inside the rail. In conclusion, the adjustment of the PID controlled quantity has a lag and the pressure varies without a quick response. The simulation result of PID control is shown in Figure 11. According to the results, a fast rise of rail pressure, a large amount of overshoot and a slow adjustment response result, with the load quickly decreasing and the engine speed suddenly increasing. While the power system is working or in the simulation, there might be some special working conditions. Several parameters exceeded their normal working sections and this leads to some special working states (usually malfunction states) in the actual power system. By means of simulation, the special state section was demonstrated in area marked as ① in Figure 11, characterized by a small quantity injection under high rail pressure.
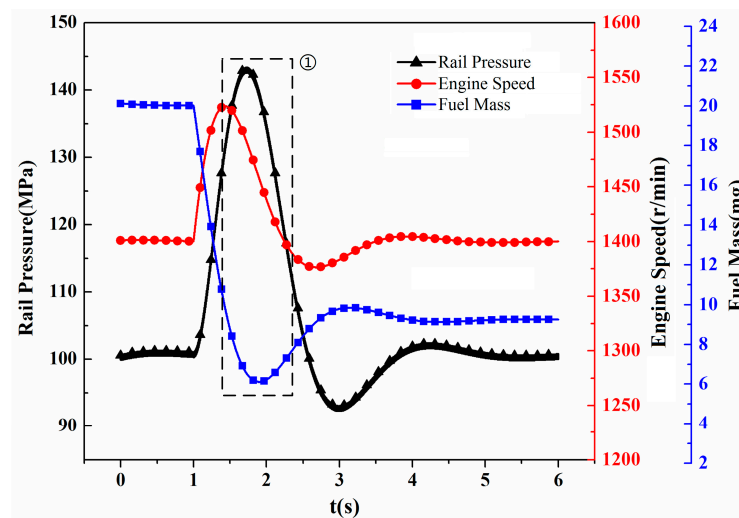

Figure 11. Rail pressure, engine speed and fuel mass vs. time controlled by PID.

According to the working principles and operating requirements of the injector of a common rail system, it can control the fuel injection quantity by using a time-pressure control method. That is, by looking up the injection characteristics curve on the basis of the current rail pressure and target fuel quantity to obtain an injection duration *ET* and to control the cycle injection quantity. The injection characteristics curve shown in Figure 12 was obtained from the test bench shown in Figure 1. During the experiment, the first step was to adjust the rail pressure to the test value (100–140 MPa) by using the control system. After that, the injection period should be set to a constant (0.5–3.5 ms). By recording the fuel injection quantities 100 times with the single-injection instrument and taking an average, the injection characteristics curve could be obtained. The operating features of the injector of the common rail system are shown in Figure 12. When the rail pressure was 140 MPa, the minimum stable injection duration was 0.5 ms and minimum fuel mass was 9 mg. When the calculated fuel mass equaled 6.5 mg,

the opening time for the injector was 0.35 ms and the expected in-cylinder pressure was 5.2 MPa. Under the working situation of a short opening time, the injector might not open normally and no fuel would be injected. Another situation is that the injector might not close regularly after opening and the fuel mass might jump to a large quantity. In the working principle of the injector of the common rail system [11], the current action time was the injector working time.
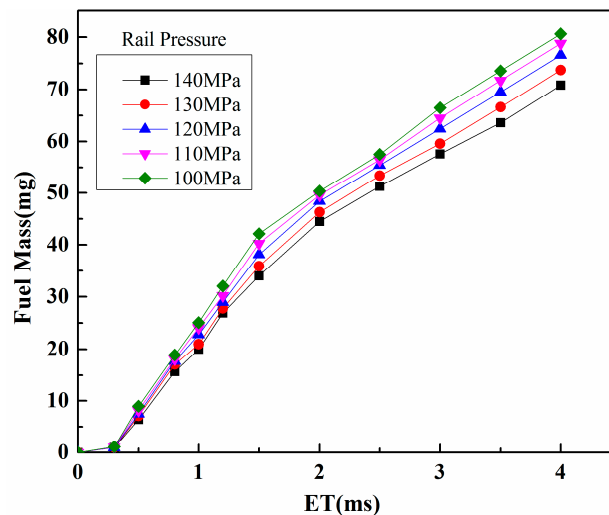

Figure 12. Map for injector characteristics.

As shown in region B of Figure 13, at first, the electric current of the solenoid valve of common rail injector rose to more than 20 A within 0.1 ms, and the static friction and static pressure inside of injector could be overcome by the solenoid valve. Then, the electric current would be kept at 20 A in order to guarantee that the needle valve could move to a fully opened state at 0.5 ms. Finally, the electric current would be kept at 10 A to reduce the power consumption of the solenoid valve until injection ends. If the injection duration was too short, that is less than 0.5 ms, the needle valve and control plunger could not open completely, then there it would occur that the injector could not open normally or the needle valve could not close normally after opening while the electric current supply had already finished. The closing of the injector is controlled by the displacement of a ball valve depending on the elastic force of the return spring. Under different injector pressures, the acting force controlling the solenoid valve is not the same. If the rail pressure were higher, the return resistance would be larger and there would be a great impact on the closing speed of the solenoid valve which could also cause an injection closing delay, and the fuel injection quantity would rise high, as shown in Table 3. The region A of Figure 13 showed that water hammer turning up along with the closing of the ball valve would result in a sudden pressure increase, which represents the closing point of the ball valve. Aiming at a fuel injection expectation of 0.35 ms, just like the target operating conditions mentioned above, this could generate an improper fuel injection of 0.5–1.2 ms and cause several problems such as the overtopping of in-cylinder pressure, decline of component reliability and deterioration of emissions. The specific in-cylinder pressure curve is shown in Figure 14.

Table 3. Injector opening period variation with the rail pressure under different injection durations.

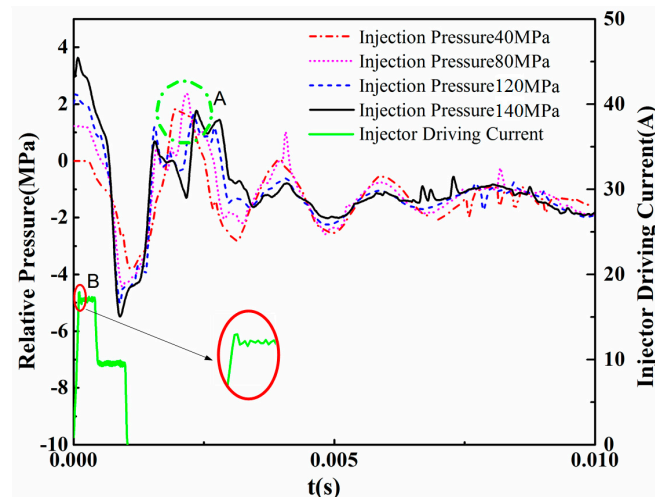| *ET*/ms Rail Pressure/MPa	1.0	1.5	2.0
40	1.95 ms	2.97 ms	3.95 ms
80	2.14 ms	3.24 ms	4.38 ms
120	2.28 ms	3.39 ms	4.44 ms
140	2.35 ms	3.43 ms	4.61 ms

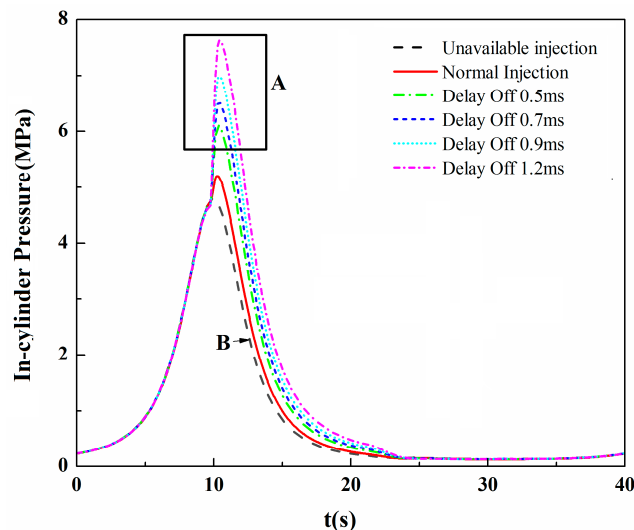**Figure 13.** Off-delay characteristics of the injector.

Figure 14. In-cylinder pressure in the special section.

The LQR method obtains feedback information from the state of the fuel pump rotation speed as well as the rail pressure. The controlled quantity was adjusted by detecting the state of the rotation speed and pressure directly. Namely, the rail pressure remained stable while the opening of throttle valve was changing with variation of rotation speed and pressure. The specific pressure adjustment process was as follows.

Since the speed rise is discovered by the control system, the solenoid valve would be shut down in order to reduce the fuel supply quantity. The simulation result is shown in Figure 15. It could be seen that under normal conditions, the control precision was within the 20 MPa limit by utilizing a rotation speed feedback control strategy and the LQR scheduling control method of the rail pressure. When the rail pressure was 120 MPa, the minimum fuel mass was 8 mg, which both match the injection Map and the injection process could be conducted regularly. Compared with the conventional PID control, the amount of rail pressure overshoot with LQR could be more indistinctive, while the load decreased quickly and the engine speed increased suddenly under some certain conditions.
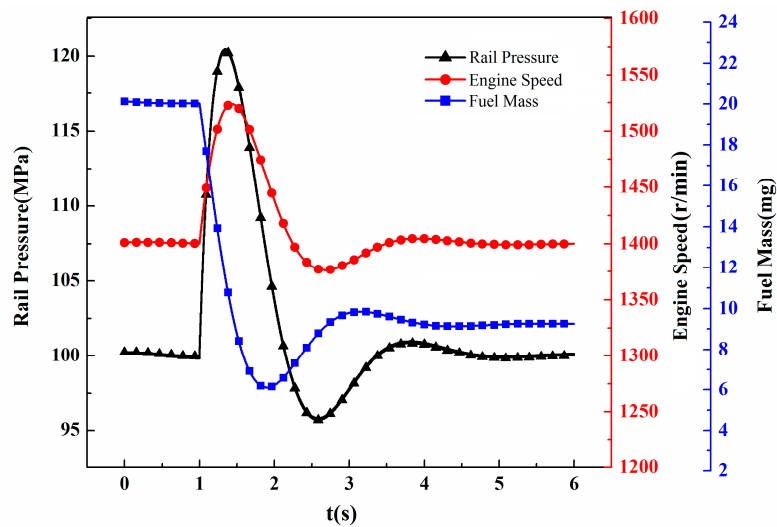
Figure 15. Rail pressure, engine speed and fuel mass vs. time controlled by LQR.

The rail pressure comparison resulting from utilizing two different control algorithms is illustrated in Figure 16. Compared with PID control, LQR added a state feedback controlled quantity for adjusting the rail pressure according to the engine speed, which leads to a faster response speed with the variation of engine speed. The rail pressure overshoot is jointly caused by the increase of fuel supply frequency of the high pressure plunger pump and the decrease of fuel injection quantity. Under the working conditions of high rail pressure and small injection quantity, the injector could not be switched steadily. Besides, the combustion process could be impacted, thus possibly causing malfunctions like flameouts. Armed with speed feedback, the LQR algorithm reduced the absolute value of the rail pressure overshoot and stabilized the injector in the working conditions. Furthermore, it also reduced the failure probability of the engine. By using PID control, the rail pressure suddenly increased 40 MPa as the variation of the quantity of fuel was 14 mg. While the fuel quantity was abruptly changing under a higher level of the working pressure (120~140 MPa), the rail pressure might directly rise and even exceed the maximum allowable rail pressure (160 MPa) without a prompt adjustment. All the above are possible reasons for causing structure malfunctions in the common rail system, such as leaks, abrasion, overheating of components and carbon deposition.
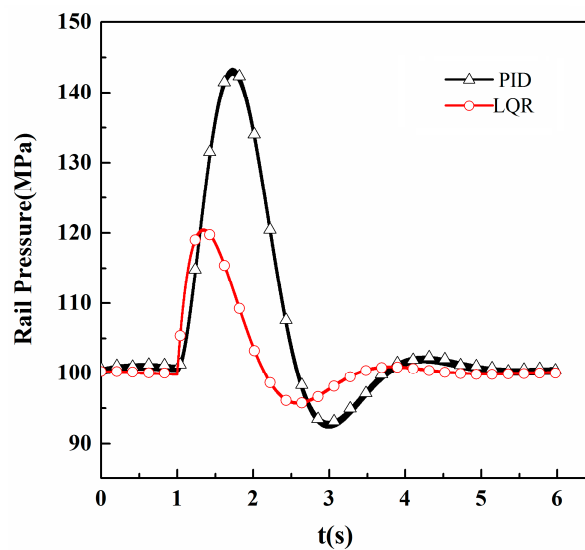

Figure 16. Comparison of rail pressure overshoot controlled by PID & LQR.

The design algorithm was written in the OP2S diesel engine control system. Rail pressure optimal control experiments was performed on the experimental prototype. The experimental results are shown in Figure 17. The engine worked continually under steady conditions at the state of 1400 r/min and 120 N·m. Due to a sudden outage, the dynamometer unloaded instantaneously which led to a 600 r/min variation of engine speed and the fuel quantity decreased by 76.3% compared with the maximum fuel supply. After adopting the speed feedback control strategy, the rail pressure fluctuation was less than 20 MPa. Besides, it took less than 3.5 s for the pressure to return to a stable value, thus the control expectations were achieved.
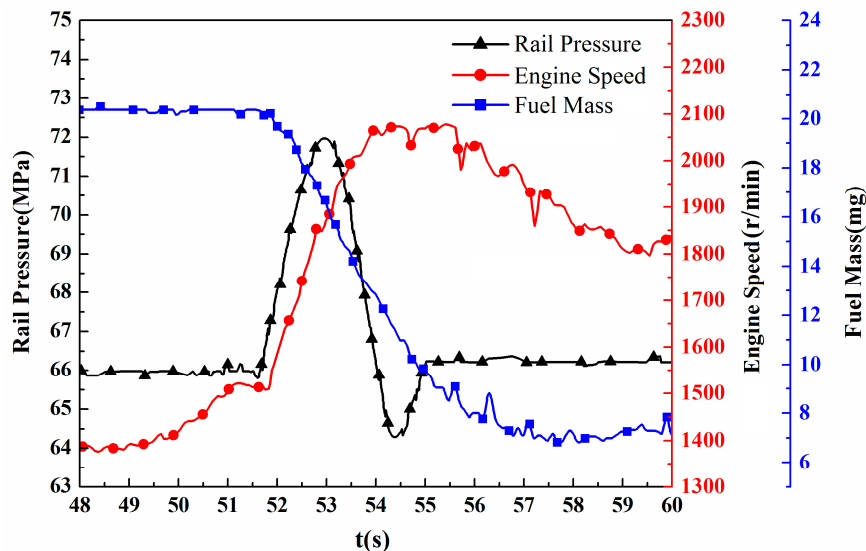

Figure 17. Rail pressure, engine speed and fuel mass vs. time on the experimental prototype.

4. Conclusions

(1) After adopting a speed feedback control strategy, the control precision stays within the range of ±1 MPa. When that engine speed undergoes a 600 r/min variation, the fuel quantity decreases by 76.3% compared with the maximum fuel supply. The rail pressure fluctuation is less than 20 MPa and the time before the pressure returns to a stable value is less than 3.5 s. The control method restraining pressure overshoot problems is thus proved to be valid.

(2) While using the LQR control system group on the basis of the LPV model design as well as the state feedback and servo compensation design, an ideal control effect results. The format of multi-state and coordinated control parameters could be applied to a multi-parameter control design of a multi-state complicated control system. Control parameters are designed off-line, thus reducing the calibration workload.

(3) Aiming at the specific dynamic control problem of an OP2S diesel engine, the engine speed feedback, complex working conditions and nonlinear multi-parameter exponential equation family are added to the pressure control algorithm. The sensitivity of the dynamic fuel quantity variation characteristics of the OP2S diesel engine and the impact on the system dynamics from nonlinear parameters are preferably reduced. Finally, the algorithm is verified.

(4) Although the control strategy in this study is designed for the rail pressure overshoot problem of OP2S diesel engines, the method could also be appropriate for other types of common rail systems thanks to its universality.

Nomenclature

Abbreviation

BDC	Bottom Dead Center
ECU	Electronic Control Unit
LPV	Linear Parameter Varying
LQR	Linear Quadratic Regulator
OP2S	Opposed-Piston Two-Stroke
PCV	Pressure Control Valves
PWM	Pulse Width Modulation
PID	Proportion Integration Differentiation

Symbols

α	Crank angle, deg
ρ	Fuel density, kg/m^3
a	Correction coefficient
b	Correction coefficient
c	Discharge coefficient
ET	Injection pulse width
J_{Engine}	Moment of inertia in engine, kg $\cdot$ m^2
k	Injector number
K_f	Fuel bulk modulus of elasticity, MPa
K_T	Model constants
K_p	Rail pressure state feedback parameter
K_n	Speed state feedback parameter
K_e	Servo compensation state feedback parameter
n	Crankshaft speed, r/min
p	Time varying fuel pressure, MPa
p_g	Constant fuel pressure,0.5MPa
q	Fuel flow, m^3/s
s_p	Plunger instantaneous axial displacement, m
T_{load}	Load torque, N $\cdot$ m
u	Control signals
v	Instantaneous fuel volume, m^3
V	Constant volume, m^3

Subscripts

0	Initial value
cyl	cylinder
i	injector
in	flow direction
out	flow direction
p	pump
r	rail
s	solenoid valve of pump
d	desired rail pressure

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