

Article

# Optimal Capacity Estimation Method of the Energy Storage Mounted on a Wireless Railway Train for Energy-Sustainable Transportation

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**Abstract:** Although electric railway systems have gone through many technological innovations in their electrical, mechanical and structural engineering since the energy paradigm conversion to electrical energy, the conventional feeding system based on the catenary contact is still being applied. In order to solve the problems of the contact-based feeding system that arise and to build up the energy-sustainable electric railway system simultaneously, this paper considers the wireless railway train (WRT), which is fed by storages mounted on the board without catenary contact during driving and charged at a platform during a stop. In order to maximize the energy improvement of WRTs' operation, the optimal power and storage capacity estimation method considering the increased weight of the additional storage devices is proposed. Through case studies of the electrical and topographical conditions of the actual operating railway route, compared with the electrical performance of the existing railway trains, it is verified that the application of WRTs leads to facility capacity margin enlargement through the peak power reduction, and cost-effectiveness improvement through the reduction of catenary loss and driving energy.

**Keywords:** wireless railway train (WRT); electric railway system (ERS); optimal power and storage capacity; regenerative power; energy saving

## 1. Introduction

The electric railway systems (ERSs), which are a collection of electrical, mechanical, and structural engineering technologies, have contributed greatly to the development of human civilization through the rapid transport of passengers and cargo. Since the advancement in the energy paradigm from fossil fuels to electrical energy, the breakthrough development of each engineering technology, especially electrical engineering—which led to high-capacity, high-efficiency, miniaturization and weight reduction of the traction motor and converter and inverter (C/I)—has led to the current high-speed, high-efficiency, high-reliability and high-safety railway technology. There have been lots of advances in many technical areas, but the only thing that has not made technological advances in the structure of the early electric railway is the power feeding systems based on the catenary contact.

Since the existing contact-based feeding has been accepted for the electro-mechanical system with mobility, researches have been mainly conducted on minimizing contact loss during driving [1], analyzing mechanical wear and electrical impedance variation [2,3], detecting electrical arcs [4,5], and protecting the electric devices against AC arcs [6,7], etc. The only research to overcome the weaknesses of contact feeding focuses on the wireless power transfer inverter [8–11]. However, at a

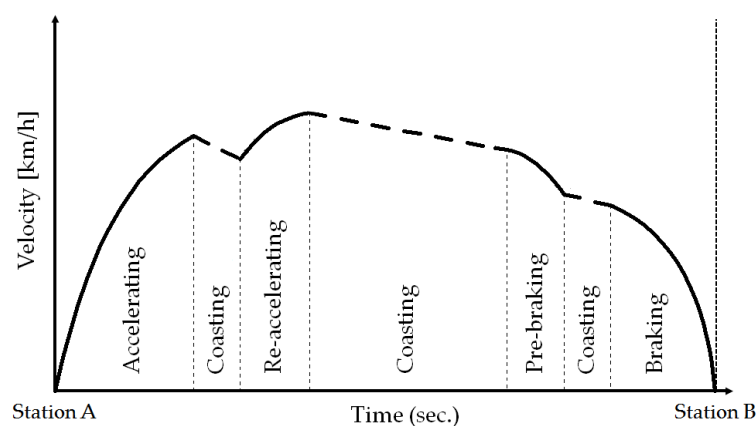
current technology level of power capacity of around 1 MW [11] and transmission efficiency of 80~90%, it is considered that the wireless power transfer technology is more practical for the auxiliary power supply of the magnetic levitation train [12,13] than as the main power source of the traction devices.

Another issue in ERS is the application of energy storage systems. Energy storage has wide applications and effectiveness in power systems, and in particular it has much higher effectiveness in terms of handling regenerative energy in ERSs. In ERSs, it has two types of applications: stationary installation in railway substations [14–16] and mounted on the train [17]. The stationary application has the advantage of saving the storage capacity since the stationary storage handles the remaining regenerative energy after consumption by the other accelerating train [18]. However, since the regenerative power is not the only cause of the catenary voltage fluctuation, it is difficult to pick up the regenerative energy only for charging. In addition, since the existing supply facility and the regenerative solution are at the same location, there is just a small change in the amount of current flowing through the catenary, and it is difficult to significantly improve the catenary losses. In the case of on-board application, since it is possible for it to handle the regenerative energy by itself in the train, it can maximize the use of regenerative energy and reduce the catenary loss significantly with the lowered load current flowing through the catenary [19,20]. However, the increase in the driving mass due to the on-board mounted storage may increase the driving energy itself. There is still a debate as to which type of storage application is better, and it is expected that the application type will be different depending on the structural, mechanical and operational conditions [21].

In spite of these controversies, this paper deals with the storage mounted wireless railway train (WRT), which has enough storage capacity not only to store regenerative energy but also to supply whole energy required for inter-station driving. This can be a solution to the weaknesses of the contact-based feeding system and a way to maximize energy efficiency simultaneously. In order to verify the system performance improvements of the optimal-designed WRT, this paper is organized as follows: Section 2 presents the basic formula to analyze the mechanical and electrical performance of railway trains; the optimal power and storage capacity estimation method is presented in Section 3; simulation results through case studies based on the actual track data are presented in Section 4; and finally, Section 5 presents our conclusions.

## 2. Basic Formula for Railway Train Performance Analysis

The electrical load characteristics of railway trains are determined by internal constraints based on the electrical specifications of the drive systems, such as traction motors and inverter, and topographical conditions, such as gradient and/or curvature sections. The internal constraint is used to derive the standard operating velocity curve between the two stations, as shown in Figure 1. In particular, within the allowable specification range of the driving system, the maximum rate of change in speed is set to 3.0 km/h/s and  $-3.5$  km/h/s for acceleration and braking, respectively.



**Figure 1.** Standard operating curve between two stations.

The gradient and/or curvature track conditions are reflected in the speed limit to prevent derailment of the train, resulting in a velocity profile deviating from the standard operating curve. These are the causes of the sudden acceleration and braking in the operating period other than the initial acceleration period and the final braking period. Combined with the train mobility characteristics, any peculiar power characteristic in substations is usually presented.

In this section, basic formulas of kinetic analysis for railway train motion are presented, taking into account the electrical specifications of the drive system and the topographical conditions of the track, and deriving the electrical load characteristics based on this analysis.

### 2.1. Kinetic Analysis Equations

The acceleration of the train is a physical quantity that must be calculated in order to calculate the speed and position of the wheel at every time step. Equation (1) shows the basic relations of total driving mass ( $m_{dr}$ ), effective traction force ( $F_{ET}^t$ ) and acceleration ( $a_{avg}^t$ ) of the train at a specific moment, time  $t$ . The total driving mass includes static mass ( $m_s$ ) and inertial mass ( $m_{iner}^t$ ) as shown in Equation (2):

$$a_{avg}^t = \frac{F_{ET}^t}{m_{dr}} \quad (1)$$

where  $a_{avg}^t$ : acceleration ( $m/s^2$ ) during time period  $t$ ;  $F_{ET}^t$ : effective traction force (kN) during time period  $t$  and  $m_{dr}$ : total driving mass (tonne):

$$m_{dr} = m_s + m_{iner} \quad (2)$$

where,  $m_s$ : static mass (tonne) and  $m_{iner}$ : inertial mass (tonne).

The effective traction force is obtained by subtracting the train resistive force ( $F_{TR}$ ) from the motor traction force ( $F_{MT}$ ), as shown in Equation (3). The train resistive force is expressed by the sum of drag resistive force ( $F_{DR}$ ), curvature resistive force ( $F_{CV}$ ), and gradient resistive force ( $F_{GR}$ ), as shown in Equation (4). Each resistive force term can be expressed by Equations (5)–(7), respectively. The value of gradient resistive force might be negative according to the operating direction, and this is an important factor that causes a difference pattern in the load characteristics of the up-line and down-line trains.

$$F_{ET}^t = F_{MT}^t - F_{TR}^t \quad (3)$$

where,  $F_{ET}^t$ : effective traction force (kN) during time period  $t$ ;  $F_{MT}^t$ : motor traction force (kN) during time period  $t$  and  $F_{TR}^t$ : train resistive force (kN) during time period  $t$ .

$$F_{TR}^t = F_{DR}^t + F_{CV}^t + F_{GR}^t \quad (4)$$

where,  $F_{DR}^t$ : drag resistive force (kN) during time period  $t$ ;  $F_{CV}^t$ : curvature resistive force (kN) during time period  $t$  and  $F_{GR}^t$ : gradient resistive force (kN) during time period  $t$ .

$$F_{DR}^t = (\alpha + \beta \cdot v_{avg}^t) \cdot m_s \cdot a_g + \gamma \cdot (v_{avg}^t)^2 \quad (5)$$

where,  $\alpha$ ,  $\beta$ : kinetic friction coefficient ( ), ( $s/m$ );  $v_{avg}^t$ : average velocity of the railway train ( $m/s$ ) during time period  $t$ ;  $a_g$ : gravitational acceleration  $9.8$  ( $m/s^2$ ) and  $\gamma$ : air friction coefficient ( $tonne/m$ ):

$$F_{CV}^t = \frac{k}{R} \cdot m_s \cdot a_g \quad (6)$$

where,  $k$ : curvature friction coefficient (m) and  $R$ : radius of curvature (m)

$$F_{GR}^t = g \cdot m_s \cdot a_g \quad (7)$$

where  $g$ : gradient of the track (%).

The effective traction force, which is derived in Equation (3) using each resistive force from Equations (5)–(7), is used to calculate the average acceleration ( $a_{avg}^t$ ) in Equation (1). As shown in Equations (8) and (9), this acceleration value applied to the train during time step ( $\Delta t$ ) is applied to update the train speed and location from those values at the previous step:

$$v^t = v^{t-\Delta t} + a_{avg}^t \cdot \Delta t \tag{8}$$

where,  $v^t$ : train velocity (m/s) at time  $t$ ;  $v^{t-\Delta t}$ : train velocity (m/s) at time  $t - \Delta t$  and  $\Delta t$ : simulation time step (s).

$$x^t = x^{t-\Delta t} + v^{t-\Delta t} \cdot \Delta t + \frac{1}{2} \cdot a_{avg}^t \cdot (\Delta t)^2 \tag{9}$$

where,  $x^t$ : location (m) of the train at time  $t$  and  $x^{t-\Delta t}$ : location (m) of the train at time  $t - \Delta t$ .

The curvature resistive force and gradient resistive force are independent of train velocity, but drag resistive force is affected by velocity change during  $\Delta t$ , so the average of initial and final velocity of time period  $t$  should be applied to derive a more accurate acceleration value, as shown in Figure 2.

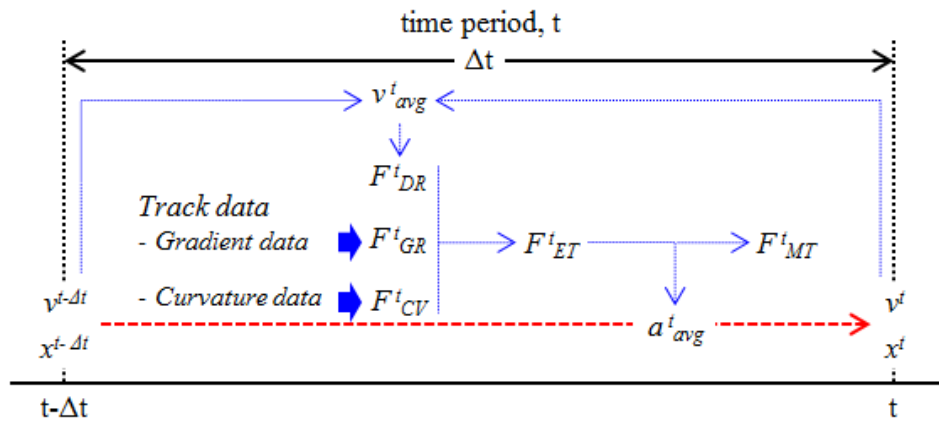


Figure 2. Iterative process to update the velocity and location of the train.

### 2.2. Electrical Power Analysis Equations

Railway trains that operate in an urban railway system with an inter-station distance of about 1 km have three modes of operation: acceleration, coasting and braking. In the section on coasting, only natural deceleration due to the three kinds of train resistive force is considered, and it is a section where there is no consumed or regenerative energy, that is, zero electrical power.

From the derived motor traction force in Equation (3), the mechanical power can be calculated as shown in Equation (10) since the work is the integral value of the force with respect to displacement and the power is the derivative of work with respect to time:

$$P_{mech}^t = F_{MT}^t \cdot v_{avg}^t \tag{10}$$

where  $P_{mech}^t$ : mechanical power (kW) during time period  $t$ .

In the section on acceleration with positive value of motor traction force, in consideration of the efficiency in the electric drive system (C/I, motor) and the mechanical drive system (gear box) in the train, the electric power for performing the mechanical demand operation must be calculated by applying the reciprocal of the efficiency of each apparatus, as shown in Equation (11):

$$P_{trac}^t = \frac{P_{mech}^t}{\eta_{gear} \cdot \eta_{inv} \cdot \eta_{MT}} = \left( \frac{1}{\eta_{gear} \cdot \eta_{inv} \cdot \eta_{MT}} \right) \cdot F_{MT}^t \cdot v_{avg}^t \tag{11}$$

where,  $P_{trac}^t$ : electrical tractive power (kW) during time period  $t$ ;  $\eta_{gear}$ : efficiency of gear box;  $\eta_{inv}$ : efficiency of C/I and  $\eta_{MT}$ : efficiency of the traction motor.

For the section on braking with negative value of motor traction force, since the regenerative power goes back into the catenary system through the electrical and mechanical drive apparatus, the electric power for braking is calculated as shown in Equation (12):

$$P_{regen}^t = (\eta_{gear} \cdot \eta_{inv} \cdot \eta_{MT}) \cdot F_{MT}^t \cdot v_{avg}^t \quad (12)$$

where  $P_{regen}^t$ : electrical regenerative power (kW) during time period  $t$ .

As a result, considering auxiliary power ( $P_{aux}$ ) such as lighting, air conditioning, heating, communication equipment and controller, the railway train has three electrical powers according to the operation modes, as shown in Equation (13):

$$P_{veh}^t = \begin{cases} P_{trac}^t + P_{aux} & \text{(accelerating)} \\ P_{regen}^t + P_{aux} & \text{(braking)} \\ P_{aux} & \text{(coasting)} \end{cases} \quad (13)$$

where,  $P_{veh}^t$ : train power (kW) during time period  $t$  and  $P_{aux}$ : auxiliary power (kW).

### 3. Optimal Design of ESS Specifications for WRT

The power and storage capacity of a typical on-board energy storage system (ESS) focuses on the handling of regenerative power to improve energy efficiency and minimize system loss, but those of the ESS mounted on the WRT considered in this paper should be determined to be at a level that enables inter-station operating without catenary contact because it drives without contact to the catenary and charges the energy storage only at the platform of the next station, as shown in Figure 3. That is, the moving WRT is electrically isolated from the feeding system and it operates as an electrical load only at the platform during a stop.



Figure 3. Operation scheme of wireless railway train (WRT).

#### 3.1. Optimal Power and Storage Capacity Estimation

During motion, that is, in an electrically isolated state, the energy required for acceleration and the regenerative energy generated during braking should be handled only by the energy storage mounted on the train. This means that an ESS with a storage capacity greater than the maximum energy required in the most severe driving conditions must be considered. Here, the most severe condition indicates the maximum static mass condition, that is, the maximum passenger boarding condition, which is reported as 30% of the train's mass. Considering the severe driving condition and additional devices related to the ESS, such as the storage power conversion system (PCS) and the energy storage packs (ESPs), the static mass applied to the formulas in Section 2 is modified, as shown in Equation (14):

$$m_s = m_{veh} + m_{psn} + m_{PCS} + m_{ESP} \quad (14)$$

where,  $m_{veh}$ : mass (tonne) of railway train;  $m_{psn}$ : mass (tonne) of maximum passengers;  $m_{PCS}$ : mass (tonne) of storage PCS and  $m_{ESP}$ : mass (tonne) of ESPs.

Assuming that it takes  $t_{max}$  to travel from the first station to the last station, the power capacity of the storage PCS must be greater than the maximum absolute value of the train power to implement the required acceleration or braking performance, and this can be expressed in Equation (15):

$$P_{PCS} = \max\{|P_{veh}^t|\} \quad (t : 0 \sim t_{max}) \quad (15)$$

where,  $P_{PCS}$ : power capacity (kW) of the storage PCS and  $t_{max}$ : total time (s) to travel whole railway track.

Assuming the whole railway track consisted of  $m$  stations, the optimal storage capacity can be estimated at the section where the depth of discharge is the greatest among the  $m - 1$  sections. Based on the load characteristics from Equation (13), the variation in the amount of energy stored in the ESS can be calculated as in Equation (16):

$$E_{sto}^t = \begin{cases} E_{sto}^{t-\Delta t} - \frac{1}{3600} \cdot \frac{P_{veh}^t}{\eta_{PCS}} \cdot \Delta t & (P_{veh}^t > 0) \\ E_{sto}^{t-\Delta t} + \frac{1}{3600} \cdot \eta_{PCS} \cdot P_{veh}^t \cdot \Delta t & (P_{veh}^t < 0) \end{cases} \quad (16)$$

where,  $E_{sto}^t$ : remaining energy (kWh) in ESS at time  $t$ ;  $E_{sto}^{t-\Delta t}$ : remaining energy (kWh) in ESS at time  $t - \Delta t$ ;  $\eta_{PCS}$ : efficiency of PCS;  $1/3600$ : scale factor for unit conversion from Joule to Wh.

The optimum storage capacity of a storage device required for reliable driving of a WRT makes the remaining amount zero at the maximum depth of the discharge state. Given that this value cannot be solved algebraically and is a value obtained through iterative calculations, the maximum difference between the minimum remaining energy and the storage capacity applied in each iteration step, as shown in Equation (17), is applied to the next iteration step as an optimal capacity:

$$E_{opt}(k) = \max\{E_{opt}(k-1) - E_{sto}^t\} \quad (t : 0 \sim t_{max}) \quad (17)$$

where,  $E_{opt}(k)$ : optimum storage capacity (kWh) at  $k$ th iteration step;  $E_{opt}(k-1)$ : optimum storage capacity (kWh) at  $k-1$ th iteration step.

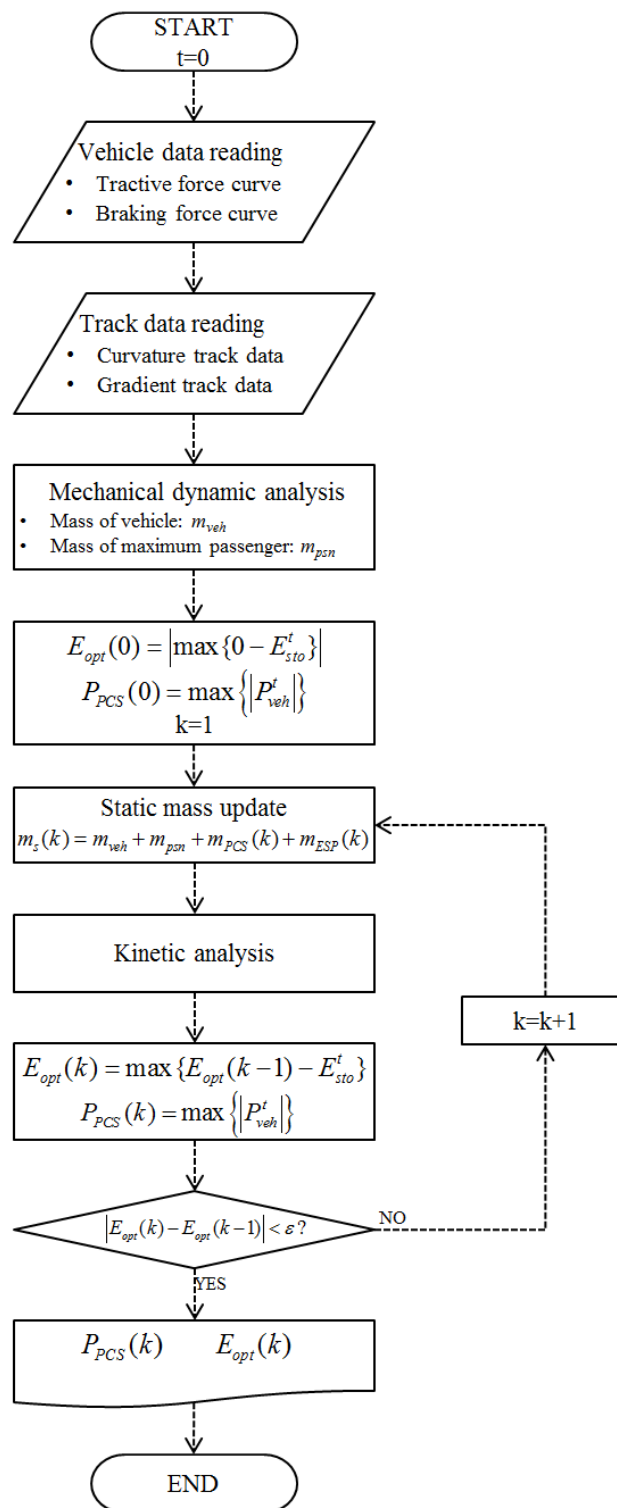
Figure 4 shows a flowchart of an iterative algorithm to solve the optimal storage capacity. The mass update process in the flowchart reflects the mass of the energy storage pack in Equation (18) and the storage PCS in Equation (19):

$$m_{ESP}(k) = E_{opt}(k-1) \cdot m_{uESP} \quad (18)$$

where,  $m_{ESP}(k)$ : total mass (tonne) of ESP at  $k$ th iteration step;  $m_{uESP}$ : mass of ESP per unit storage capacity (tonne/kWh):

$$m_{PCS}(k) = \left( \left[ \frac{P_{PCS}(k)}{P_{uPCS}} \right] + 1 \right) \cdot m_{uPCS} \quad (19)$$

where,  $m_{PCS}(k)$ : total mass (tonne) of PCS at  $k$ -th iteration step;  $m_{uPCS}$ : mass (tonne) of 1000 kW unit PCS;  $P_{PCS}(k)$ : PCS power capacity (kW) at  $k$ -th iteration step;  $P_{uPCS}$ : power capacity of unit PCS (=1000 kW) and  $[ ]$ : gauss function.



**Figure 4.** Flowchart to find optimal power and storage capacity.

### 3.2. Storage Charging Characteristic at Platform during Stop

After arriving at the station, the pantograph is lifted up to be electrically connected to the catenary and to charge the storages. Then the charger makes the storage charged with the constant charging current ( $I_{cha}$ ) until the amount of energy used in the previous inter-station section is charged. The charging current can be determined as in Equation (20). Considering pantograph lifting up and down times of 2 s each during 30-s dwell times, the effective time for charging is about 25 s, and the

charging current for full-charging can be calculated as shown in Equation (20). In Equation (20), the voltage value,  $V_{sto}^{min}$ , means the storage voltage with the lowest remaining energy at the start of charging at each station:

$$I_{cha} = \frac{C_{sto} \cdot (V_{sto}^{max} - V_{sto}^{min})}{t_{cha}} \quad (20)$$

where,  $C_{sto}$ : capacitance (F) of supercapacitor storage;  $I_{cha}$ : charging current (A);  $V_{sto}^{max}$ : storage voltage (V) at full-charged state;  $V_{sto}^{min}$ : storage voltage (V) at lowest-charged state and  $t_{cha}$ : maximum available time (s) for charging.

### 3.3. Modified Electrical Load Characteristic

Since the WRT is operated in such a manner that it is isolated from the feeding system during driving and connected to charge storage at the platform during stops, the electrical load characteristic of the WRT is completely different from the load of the existing train. Figure 5 shows graphs for location of the train, electrical load from kinetic analysis, variation of remaining energy in the WRT storage, and modified electrical power characteristic of the WRT for two inter-station sections. That is, from the viewpoint of the feeding system, the WRT has values as an electrical load only during charging at the platform and 0 value in other states. Physical operation for each section is as follows:

- State A Departure and initial accelerating: At the start of 'State A', the railway train departs to the next station. During this state, the ESS provides energy for accelerating. At this time, the WRT is electrically isolated from the feeding system and the electrical load for the feeding system is zero.
- State B Artificial braking by topographical track condition: Due to the curvature or gradient track condition, artificial braking may occur during driving. It can be seen that the regenerative energy generated at this time is charged by the storage and the stored energy increases.
- State C Re-acceleration: After artificial braking, there is a re-acceleration operation to increase the train velocity to within the normal driving velocity range.
- State D Coasting: This state is for the inertia operation. Generally, natural deceleration due to driving resistance occurs, but velocity may increase on some negative gradient track.
- State E Braking for arrival: A large amount of regenerative energy is usually generated, and the storage has the largest charge amount. At the end of 'State E', the WRT arrives at the station and starts to charge.
- State F Pantograph lifting-up: The pantograph is lifted up for storage charging. This takes around 2 s. At the end of 'State F', the WRT is electrically connected to the feeding system.
- State G Storage charging with constant current mode: The charging controller charges the storage with the constant charging current up to the full-charged state. During 'State G', the feeding system supplies electrical power to the WRT through the pantograph connected to the catenary. Charging operation lasts for up to 25 s.
- State H Pantograph lifting-down: After full charging at the end of 'State G', the pantograph takes several seconds to come down. At the end of 'State H', the WRT is electrically separated and departs to the next station.



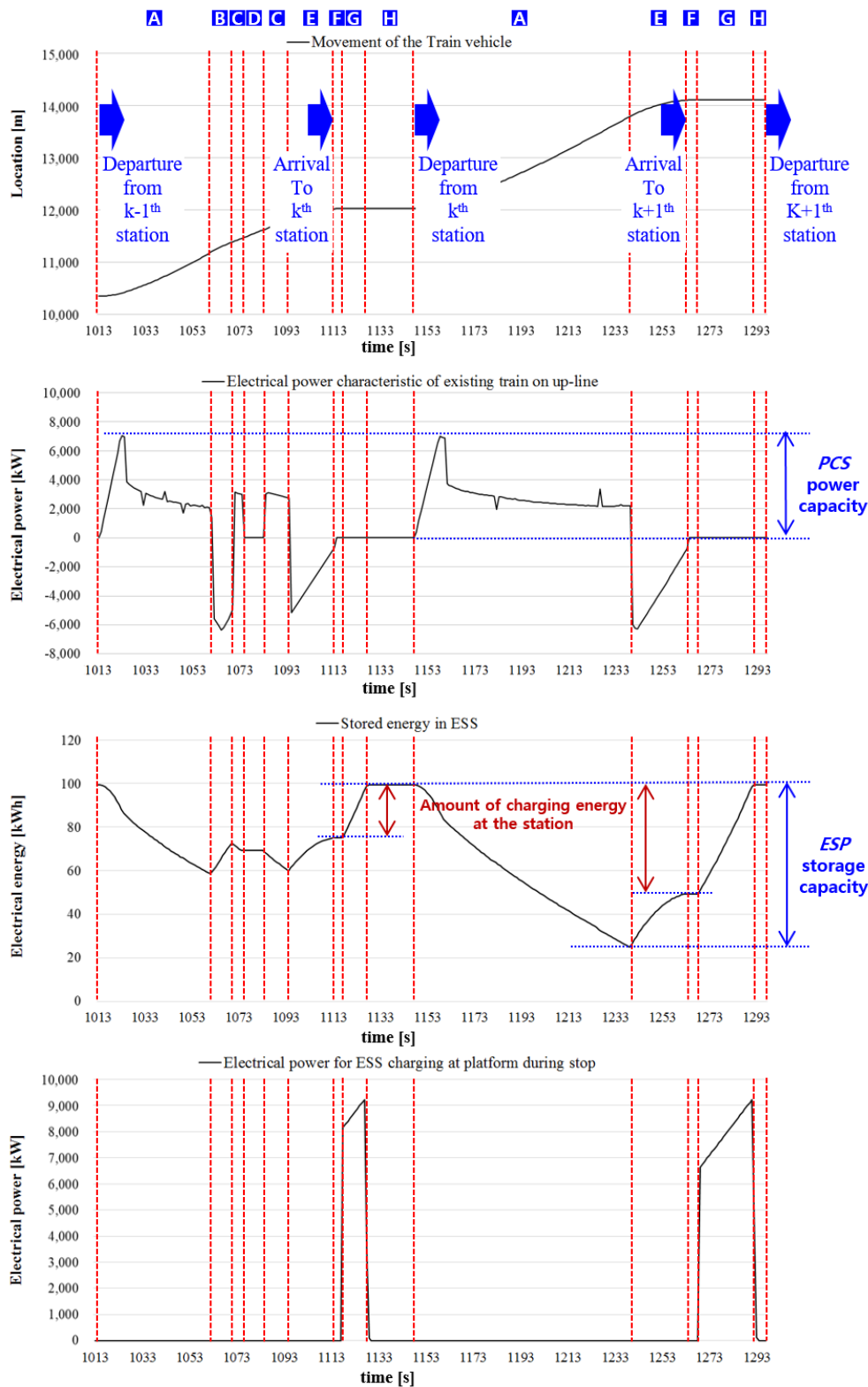


Figure 5. Operation mode of the railway train (location of the vehicle, power characteristics of the existing train, stored energy of the WRT storage, power characteristics of the WRT).

#### 4. Case Studies

The case studies have been carried out to analyze how much energy saving and peak power reduction can be achieved with the WRT on which an optimally designed energy storage system is

mounted. It is based on the track data of the actual service route and the driving system specifications of the actual service train.

#### 4.1. System Data

The route consists of 19 stations and five substations with rectifiers for converting AC to DC. Table 1 shows sets of operational data, structural data and electrical data. Curvature and gradient data of the track is presented in Appendixs A and B.

**Table 1.** System data of the Seoul Metro Line.

Type	System Data		Value
Operational Data	Total travel time		1854 (s)
	Dwell time		30 (s)
	Headway	Peak	240 (s)
		Non-peak	480 (s)
Total route length		19,902 (m)	
Structural Data	Station (substation) location	Station 1	0 (m)
		Station 2	860 (m)
		Station 3 (sub #1)	2243 (m)
		Station 4	3315 (m)
		Station 5	5004 (m)
		Station 6	5957 (m)
		Station 7 (sub #2)	6915 (m)
		Station 8	7973 (m)
		Station 9	8797 (m)
		Station 10	9543 (m)
		Station 11	10,350 (m)
		Station 12 (sub #3)	12,026 (m)
		Station 13	14,104 (m)
		Station 14	15,302 (m)
		Station 15 (sub #4)	16,063 (m)
		Station 16	16,882 (m)
		Station 17	17,763 (m)
		Station 18	18,731 (m)
		Station 19 (sub #5)	19,902 (m)
Electrical Data	Rated voltage		1500 (V)
	No-load voltage		1650 (V)
	Source impedance		0.02956 ( $\Omega$ )
	Feeder impedance		0.0203 ( $\Omega$ /km)
	Rail impedance		0.000464 ( $\Omega$ /km)

#### 4.2. Optimal Power and Storage Capacity of the Storage on the WRT

The initial value of power and storage capacity is calculated based on the results of the kinetic analysis of the train, including the mass of the train and the passengers only. Assuming the virtual 100 kWh storage, the maximum Depth of Discharge (DOD) of 56.54 kWh occurs in the 12th inter-station section in the upward direction and the maximum capacity of 5.485 MW occurs in the 7th inter-station section in the downward direction, as shown in Figure 6a,b, respectively. In particular, assuming supercapacitor storages which have only 75% of the stored energy as the available energy, the storage capacity gets to 4/3 times of the calculated required energy. That is, from the analysis results at the iteration Step 0, 6 (six) 1000 kW unit PCSs (for 5.485 MW PCS power) and 75.39 kWh (4/3 times of 56.54 kWh) are estimated, and these values are applied to the next step. From these results, the train load characteristic can be derived with the updated mass reflecting the mass of the energy storage packs and the PCS.

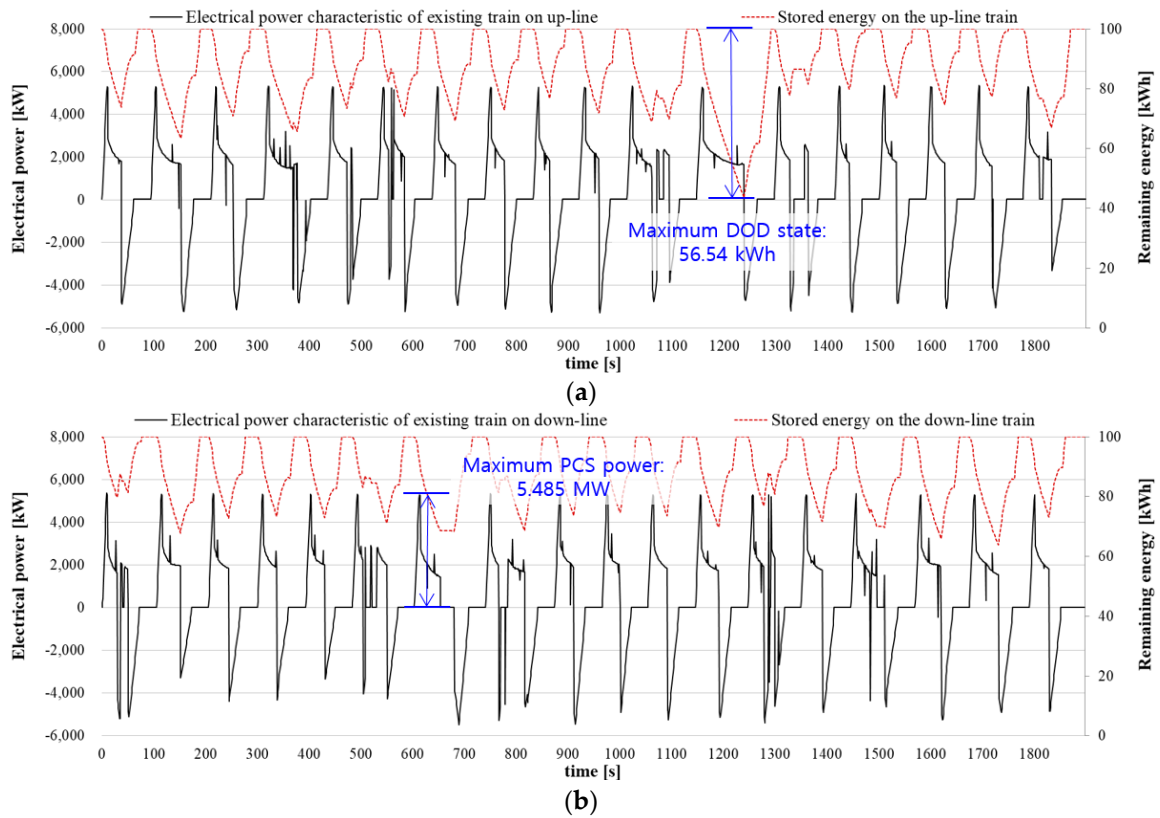


Figure 6. Electrical power characteristics and stored energy variation for the up- and down-line train at iteration step 0. (a) up-line train; (b) down-line train.

Table 2 shows the results of each iteration step. As the power capacity of the PCS and the storage capacity of the energy storage pack increase, the driving mass increases and, finally, the total mass converges to 352.7 tonnes. Then the optimal power and storage capacity of the storage set is estimated to be 7.276 MW and 99.66 kWh, which is effective energy of 74.745 kWh. Figure 7a,b show the final electrical power characteristic and modified load characteristic considering charging and discharging operation of the storage system.

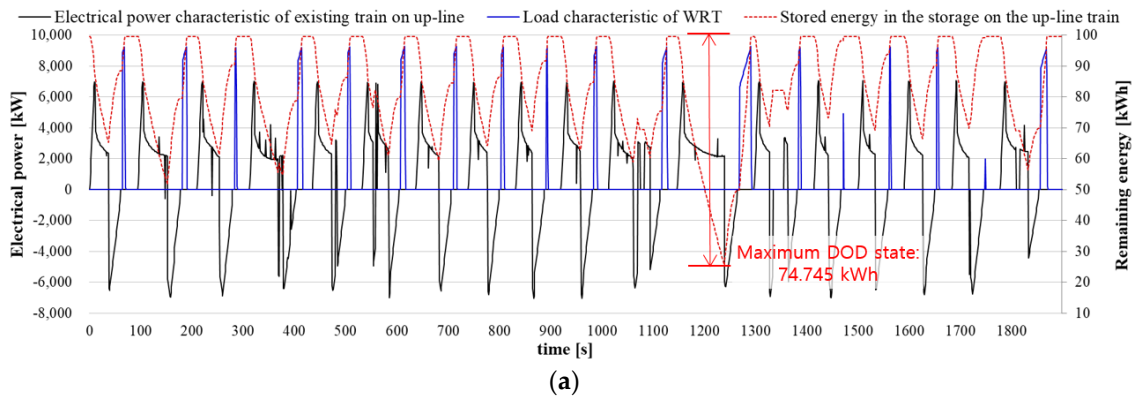
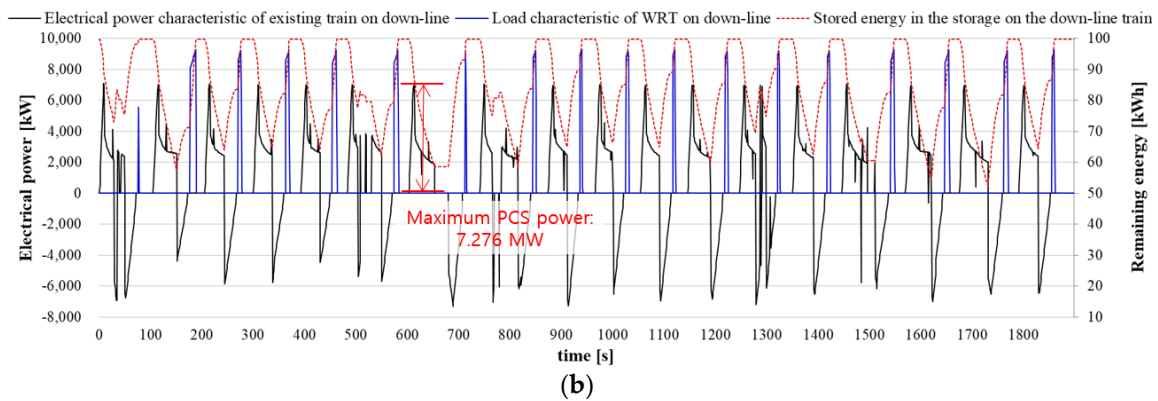


Figure 7. Cont.



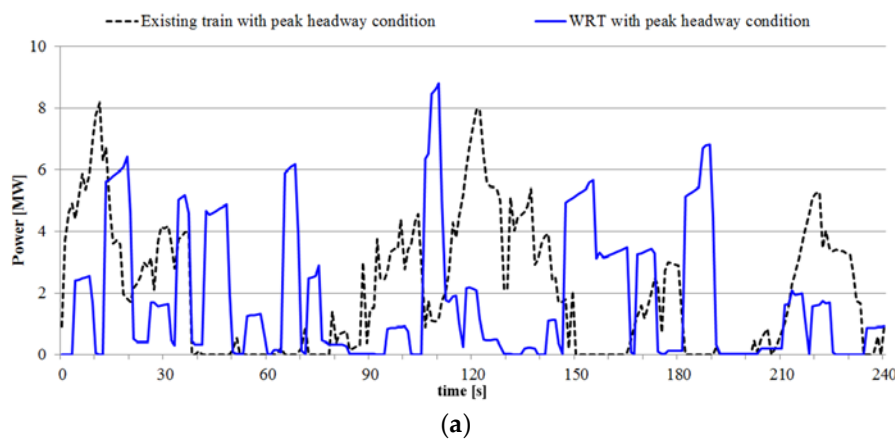
**Figure 7.** Final electrical power characteristics, remaining energy, and modified load characteristics for the up- and down-line driving train at final iteration step. (a) up-line train; (b) down-line train.

**Table 2.** Results of each iteration step for power and storage capacity optimization ( $m_{uESP} = 0.7$  tonne/kWh,  $m_{uPCS} = 2.1$  tonne).

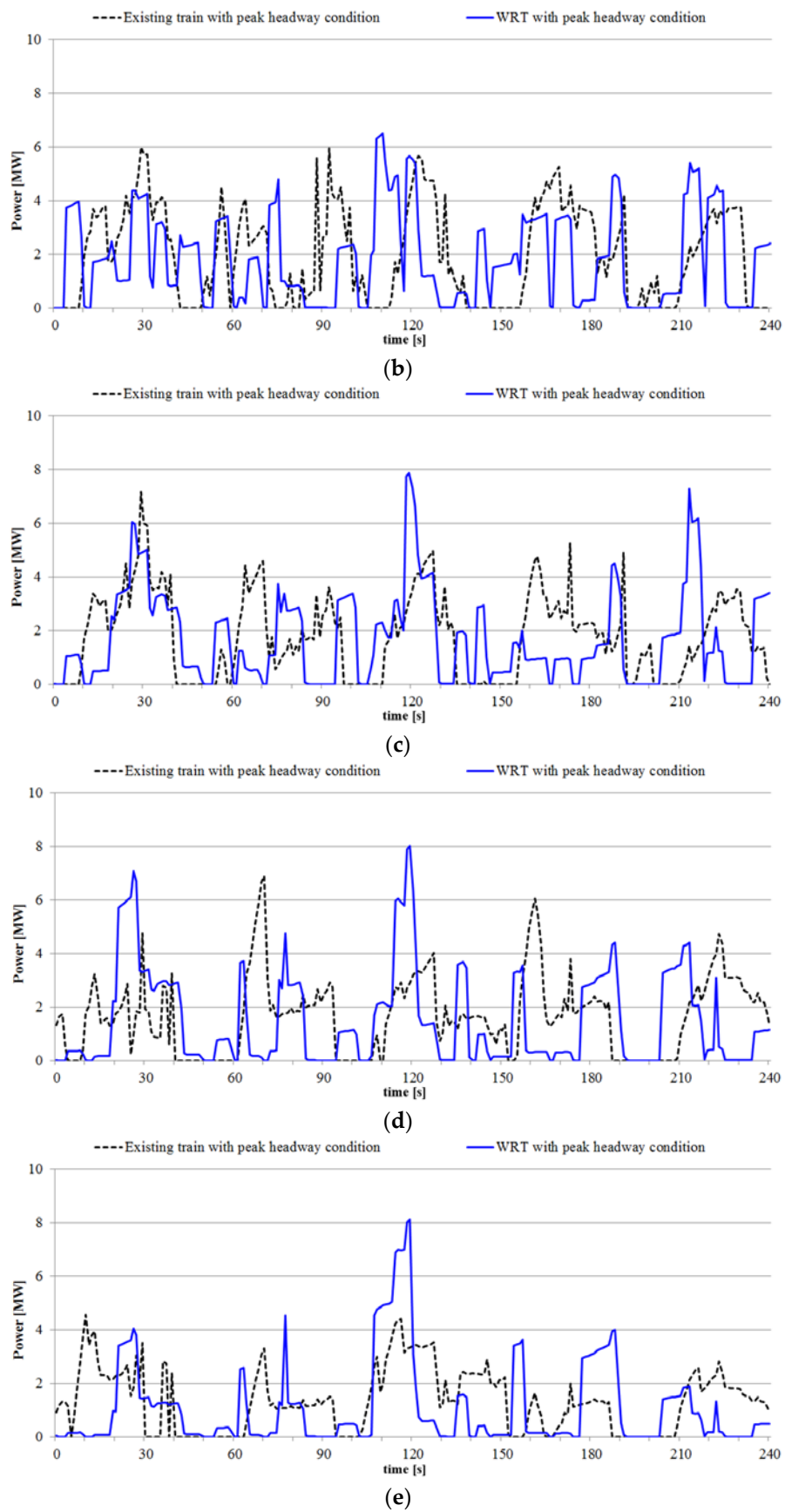
Iteration	$m_{veh}$ (tonne)	$m_{psn}$ (tonne)	$P_{aux}$ (MW)	$P_{PCS}$ (MW)	$m_{PCS}$ (tonne)	$E_{STO}$ (kWh)	$m_{STO}$ (tonne)
Step 0	204.7	61.4	0.02	-	-	-	-
Step 1	204.7	61.4	0.02	5.485	12.6	75.39	52.8
Step 2	204.7	61.4	0.02	6.837	14.7	93.73	65.6
Step 3	204.7	61.4	0.02	7.251	16.8	97.92	68.5
Step 4	204.7	61.4	0.02	7.271	16.8	99.33	69.5
Step 5	204.7	61.4	0.02	7.275	16.8	99.60	69.7
Step 6	204.7	61.4	0.02	7.276	16.8	99.66	69.8
Step 7	204.7	61.4	0.02	7.276	16.8	99.66	69.8

### 4.3. Peak Headway Operating Condition

The peak headway during rush hour is set to 240 s and a maximum of 8 trains in each direction are driven. Based on these operating conditions, comparison studies of electrical performance of each substation according to the operation of the WRTs and the existing trains have been carried out based on the DC electric railway powerflow analysis method [14]. Figure 8 shows the power supplied at each substation by the WRTs and existing trains' operation. From the perspective of energy, although the power consumption increases due to the increased weight, since the regenerative energy is handled by the train itself, the total effective energy supplied from the substation can be lowered.



**Figure 8.** Cont.



**Figure 8.** Results of substation power for the peak headway condition. (a) Electrical power of Substation 1; (b) Electrical power of Substation 2; (c) Electrical power of Substation 3; (d) Electrical power of Substation 4; (e) Electrical power of Substation 5.

Tables 3 and 4 show the comparison results of the power simulation for the peak headway condition. Comparing the simulation results of each type of train, it can be seen that the maximum power is at a similar level except for substation 5. In substation 5, the maximum power is about double, but it can be handled with the existing electrical facilities. The application of WRTs also has the advantage of reducing energy consumption. Total supply energy is analyzed as 88.88% compared with the case of an existing train. This is because not only is the required energy amount reduced by increasing the utilization rate of the regenerative energy but also the system loss is reduced due to the smaller load current.

**Table 3.** Power simulation results for railway substation at peak headway condition.

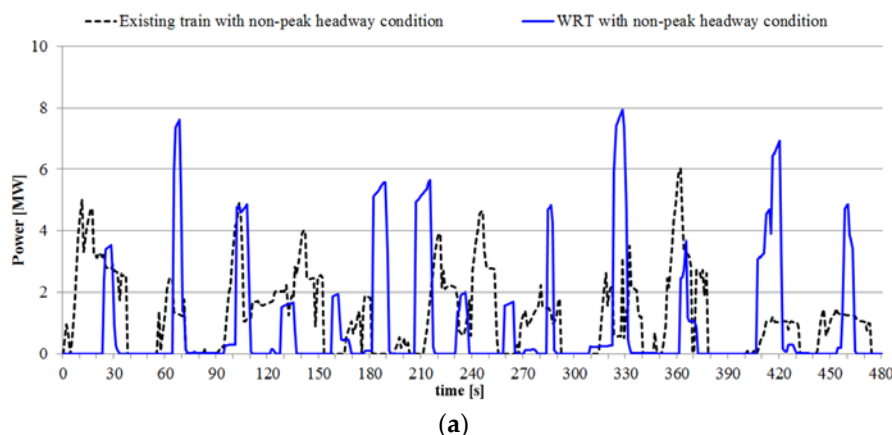
Sub. No.	Existing Train		WRT		Ratio of Supplied Energy (%)
	Maximum Power (MW)	Total Supplied Energy (kWh)	Maximum Power (MW)	Total Supplied Energy (kWh)	
1	8.17	136.80	8.78	120.83	88.32
2	6.00	130.95	6.52	121.31	92.65
3	7.17	118.66	7.87	110.35	93.00
4	6.90	110.79	8.02	99.08	89.43
5	4.56	90.14	8.13	70.43	78.13
Total		587.34		522.01	88.88

**Table 4.** Train energy analysis results at peak headway condition.

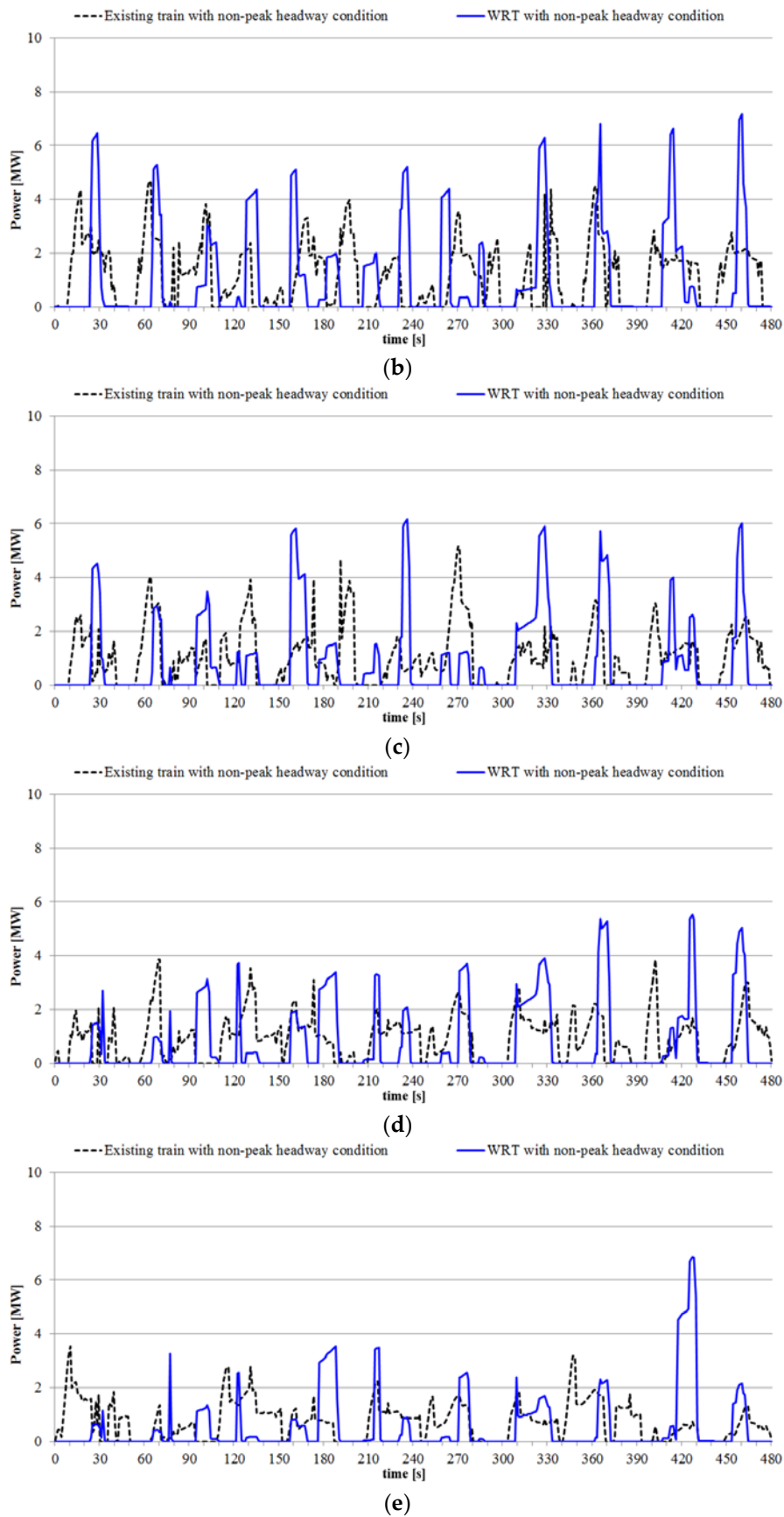
Train	Analysis Results	Results	Remarks
Existing Train	Total energy for traction (kWh)	1031.74	
	Total regenerative energy (kWh)	−669.78	
	Total energy for auxiliary loads (kWh)	21.10	
	System loss (kWh)	204.28	Losses, regenerative energy dissipation
	Total supplied energy of substation (kWh)	587.34	
WRT	Total energy for traction (kWh)	479.52	
	Total regenerative energy (kWh)	-	No regenerative energy into the catenary
	Total energy for auxiliary loads (kWh)	21.10	
	System loss (kWh)	21.39	Only system losses
	Total supplied energy of substation (kWh)	522.01	

4.4. Non-Peak Headway Operating Condition

At times other than the rush hour, the headway time of 480 s is set and a maximum of four trains in each direction operate. For the non-peak headway condition, the simulation results of electrical power for each substation are shown in Figure 9a–e. The peak power values of the substations are slightly increased, but those values are under the system capacity of the existing electrical facilities.



**Figure 9.** Cont.



**Figure 9.** Results of substation power for the non-peak headway condition. (a) Electrical power for Substation 1; (b) Electrical power for Substation 2; (c) Electrical power for Substation 3; (d) Electrical power for Substation 4; (e) Electrical power for Substation 5.

Tables 5 and 6 show the comparison results of the power simulation for the non-peak headway condition. Since the electrical load and simulation time at the non-peak headway condition are half and twice that of the peak headway operating condition, respectively, it is easy to expect that total supplied energy will be calculated at a similar level. However, in the case of existing trains, the difference between the two values is considerably large. This is because the utilization rate of regenerative energy is lowered due to the lower number of trains which usually consume that energy.

**Table 5.** Power simulation results for railway substation at non-peak headway condition.

Sub. No.	Existing Train		WRT		Ratio of Supplied Energy (%)
	Maximum Power (MW)	Total Supplied Energy (kWh)	Maximum Power (MW)	Total Supplied Energy (kWh)	
1	6.01	163.50	7.93	121.63	74.39
2	4.70	157.12	7.17	122.81	78.16
3	5.17	137.55	6.17	111.93	81.37
4	3.86	122.79	5.53	99.49	81.02
5	3.53	100.03	6.87	70.72	70.71
Total	680.98		526.57		77.33

**Table 6.** Train energy analysis results at non-peak headway condition.

Train	Analysis Results	Results	Remarks
Existing Train	Total energy for traction (kWh)	1031.74	Losses, regenerative energy dissipation
	Total regenerative energy (kWh)	−669.78	
	Total energy for auxiliary loads (kWh)	21.10	
	System loss (kWh)	297.92	
	Total supplied energy of substation (kWh)	680.98	
WRT	Total energy for traction (kWh)	479.52	No regenerative energy into the catenary Only system losses
	Total regenerative energy (kWh)	-	
	Total energy for auxiliary loads (kWh)	21.10	
	System loss (kWh)	25.95	
	Total supplied energy of substation (kWh)	526.57	

## 5. Conclusions

In order to verify the electrical merits of the WRT application, this paper proposed a method for estimating the optimum power and storage capacity of the energy storage system mounted on the WRT and presented comparative analysis results of power simulation for existing trains and WRT. Since the WRTs dealt with in this paper apply the contactless method during motion, the proposed optimal capacity estimation method finds the optimal power capacity capable of coping with the demand operation of the train considering the increased driving power by the additional mass of PCS and energy storage packs.

Through the case studies, the electrical performance of WRTs designed to improve the energy-sustainability by maximizing the utilization of regenerative energy and minimizing the system loss has been verified. In terms of electrical performance, the advantages of the WRT application include the full utilization of regenerative energy for high energy-sustainability, and driving energy and system loss reduction for reduced operating cost without any additional electrical facilities in the railway substation. In addition to its electrical benefits, there are several other advantages, such as preventing mechanical wear of the catenary, enhancing reliability of the electrical device due to electrical arc removal, enhancing operational reliability of the train against system failure, increasing transportation capacity without additional power equipment, etc.

Despite maximizing the utilization rate of regenerative energy, the reason why the energy efficiency improvement effect of the WRT application stays at around 20% is because of the increase in the driving mass of about 33% by the energy storage mount. In other words, the greater energy



saving can be expected through the weight reduction of the storage devices, that is, improvement in the energy density of the *ESPs* and power density of the *PCSs*. Also, based on the estimation of the overall benefits, including the electrical benefits, it is expected that more accurate cost/benefit analyses for WRT applications will be achieved.

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**Conflicts of Interest:** The authors declare no conflict of interest.

## Appendix A

**Table A1.** Track Curvature Data.

From (m)	To (m)	Cur. Radius (m)	Speed Limit (km/h)	From (m)	To (m)	Cur. Radius (m)	Speed Limit (km/h)	From (m)	To (m)	Cur. Radius (m)	Speed Limit (km/h)
1249	1270	60,000	100	5745	6042	250	65	11,800	11,828	10,000	100
1299	1360	5497	100	6263	6327	542	50	12,204	12,228	3000	100
1394	1428	4502	100	6513	6636	1000	100	12,264	12,288	3000	100
1449	1470	5497	100	6880	6900	20,000	100	12,644	12,810	1202	100
1877	1921	3002	100	7064	7090	12,000	100	13,217	13,304	2000	100
2042	2171	2997	100	8322	8342	22,000	100	13,342	13,429	2000	100
2265	2357	2702	100	8722	8850	670	90	13,686	14,021	800	100
2814	2970	3397	100	8930	8952	50,000	100	14,669	15,002	248	55
3068	3251	1212	100	9222	9243	40,000	100	15,831	16,260	602	90
3325	3345	18,000	100	9373	9393	46,000	100	16,568	16,690	2002	100
3375	3395	18,000	100	9472	9509	50,000	100	16,961	17,704	997	100
3623	3733	1199	100	10,408	10,736	802	100	17,900	18,237	1002	100
4220	4318	3000	100	10,938	10,958	999	100	18,624	18,668	1198	100
4515	4945	602	90	11,088	11,111	999	100	19,166	19,322	362	75
5254	5317	1200	100	11,378	11,633	298	65				

## Appendix B

**Table A2.** Track Gradient Data.

From (m)	To (m)	Gradient [%]		Speed Limit (km/h)		From (m)	To (m)	Gradient [%]		Speed Limit (km/h)	
		Up	Down	Up	Down			Up	Down	Up	Down
485	860	-3	3	100	100	8797	9039	3	-3	100	100
860	1280	3	-3	100	100	9039	9096	-12	12	105	100
1280	1410	3	-3	100	100	9096	9357	-19	19	105	100
1410	1530	3	-3	100	100	9357	9534	3	-3	100	100
1530	1813	15	-15	100	105	9534	9663	19	-19	100	105
1813	2160	-15	15	105	100	9663	9800	19	-19	100	105
2160	2243	0	0	100	100	9800	9934	19	-19	100	105
2243	2338	-2	2	100	100	9934	10,213	-14	14	105	100
2338	2620	14	-14	100	105	10,213	10,350	-3	3	100	100
2620	2985	-27	27	95	100	10,350	10,550	3	-3	100	100
2985	3315	-7	7	105	100	10,550	10,718	-10	10	105	100
3315	3570	-29	29	90	100	10,718	10,884	-3	3	100	100
3570	3830	-15	15	105	100	10,884	11,190	-10	10	105	100
3830	4090	-4	4	100	100	11,190	11,439	10	-10	100	105

Table A2. Cont.

From (m)	To (m)	Gradient [‰]		Speed Limit (km/h)		From (m)	To (m)	Gradient [‰]		Speed Limit (km/h)	
		Up	Down	Up	Down			Up	Down	Up	Down
4090	4347	17	−17	100	105	11,439	12,026	10	−10	100	105
4347	4402	30	−30	100	90	12,026	12,492	22	−22	100	100
4402	4654	29	−29	100	90	12,492	13,465	10	−10	100	105
4654	4895	5	−5	100	100	13,465	13,785	22	−22	100	100
4895	5004	−4	4	100	100	13,785	14,104	3	−3	100	100
5004	5163	−2	2	100	100	14,104	15,143	−6	6	105	100
5163	5620	−3	3	100	100	15,143	15,302	3	−3	100	100
5620	5957	4	−4	100	100	15,302	15,592	−28	28	95	100
5957	6296	10	−10	100	105	15,592	15,892	−17	17	105	100
6296	6573	14	−14	100	105	15,892	16,063	3	−3	100	100
6573	6760	−10	10	105	100	16,063	16,352	−16	16	105	100
6760	6915	3	−3	100	100	16,352	16,741	−4	4	100	100
6915	7083	10	−10	100	105	16,741	16,882	−3	3	100	100
7083	7213	10	−10	100	105	16,882	17,589	−8	8	105	100
7213	7353	−10	10	105	100	17,589	17,763	8	−8	100	105
7353	7503	−7	7	105	100	17,763	18,399	−25	25	95	100
7503	7674	−7	7	105	100	18,399	18,731	−3	3	100	100
7674	7973	3	−3	100	100	18,731	19,210	3	−3	100	100
7973	8173	16	−16	100	105	19,210	19,501	12	−12	100	105
8173	8483	−3	3	100	100	19,501	19,902	32	−32	100	90
8483	8797	−3	3	100	100						

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