

Article

Modeling of Multiple Master–Slave Control under Island Microgrid and Stability Analysis Based on Control Parameter Configuration

Haifeng Liang 1,*, Yue Dong ¹ , Yuxi Huang ¹ , Can Zheng ² and Peng Li ¹

- ¹ Department of Electrical Engineering, North China Electric Power University, Baoding 071003, China; dy_foci99@163.com (Y.D.); dasaoli508@163.com (Y.H.); ncepulp@ncepu.edu.cn (P.L.)
- ² State Grid Jiaxing Power Supply Company, Jiaxing 314000, China; jxdl_zhengcan@163.com
- ***** Correspondence: hfliang@ncepu.edu.cn; Tel.: +86-139-3085-6912

Received: 16 July 2018; Accepted: 17 August 2018; Published: 24 August 2018

Abstract: The stable operation of a microgrid is crucial to the integration of renewable energy sources. However, with the expansion of scale in electronic devices applied in the microgrid, the interaction between voltage source converters poses a great threat to system stability. In this paper, the model of a three-source microgrid with a multi master–slave control method in islanded mode is built first of all. Two sources out of three use droop control as the main control source, and another is a subordinate one with constant power control which is also known as real and reactive power (PQ) control. Then, the small signal decoupling control model and its stability discriminant equation are established combined with "virtual impedance". To delve deeper into the interaction between converters, mutual influence of paralleled converters of two main control micro sources and their effect on system stability is explored from the perspective of control parameters. Finally, simulation and analysis are launched and the study serves as a reference for parameter setting of converters in a microgrid.

Keywords: islanded mode; multi-source microgrid; stability; small-signal model; multiple master–slave control

1. Introduction

Increasing exhaustion of fossil fuel and concerns about environmental pollution have led to extensive exploration of alternative energy sources. Of special interest are renewable energy sources (RES) such as solar and wind energy generation. This has resulted in the emergence of distributed generators (DGs) and the concept of microgrid (MG) has been introduced for proper utilization of DGs [\[1,](#page-16-0)[2\]](#page-16-1). As different DGs have different characteristics and natural uncertainty, their presence can have negative effects on MG. Deviations of voltage and frequency are larger when MG operates in islanded mode in comparison with grid-connected mode [\[3,](#page-16-2)[4\]](#page-16-3). Therefore, research on the stability of MG in islanded mode is of vital importance.

Usually, voltage source converters (VSCs) [\[5\]](#page-16-4) are used to interconnect different DGs, whose output is mostly in the form of direct or non-common frequency alternating current. Although the increasing number of power electronic converters improves the control speed, it brings fuzzy influence on stability owing to the mutual influence between them [\[6\]](#page-16-5). To address the abovementioned issue, various methods have been proposed in the literature. In [\[7,](#page-16-6)[8\]](#page-16-7), the sensitivity of load voltage and voltage compensation term are introduced to control the bus voltage as well as improve the response speed and accuracy. However, limitations in applicable scope of load and voltage reduce its practicality. In [\[9,](#page-16-8)[10\]](#page-16-9), energy storage devices are used not only to suppress the transient power fluctuations, but also to greatly improve MGs' stability thanks to a super-capacitor. However, this method affects

the entire system and declines its inertia. In [\[11](#page-16-10)[,12\]](#page-16-11), a model that contains converters, controllers and alternating current (AC) grids is built, and high order state space expressions are formulated to determine its stability. However, the mutual influence between converters is neglected and a large number of equations make stability analysis more complex. To improve the accuracy of analysis, the model of MG has been improved for higher accuracy [\[13](#page-16-12)[–16\]](#page-16-13), including a linear model of MG combined with a boost converters model [\[13\]](#page-16-12); a global model ignoring the change in rotating angles and coupling terms between DGs [\[14\]](#page-16-14); a dynamic model of multi-module comprising multi-class of DGs and loads [\[15\]](#page-16-15); and a new type of small-signal model containing secondary control that analyzed the stability of the system with eigenvalue [\[16\]](#page-16-13). However, the models established in the above literature didn't take into account the impact of electronic devices in grids. In view of this problem, some research delves deeper into the impact of control parameters on system stability [\[17\]](#page-16-16). It employs the root locus method to explore the reasonable ranges of control parameters by a small signal model. When multi-sources are paralleled, droop control can achieve coordination control without communication and the master–slave control method considers the power tracking of PV and wind power and the system stability [\[18,](#page-16-17)[19\]](#page-16-18). However, the influence in different control parameters on the system is not considered, for their parameters are partly or almost the same.

In view of the problem in [\[18\]](#page-16-17), this paper builds a model of multi-source MG, emphasizing the exploration of the mutual influence between converters on stability. To satisfy the decoupling condition, "virtual impedance" is introduced and a three-source decoupling small-signal model is built in addition to the characteristic polynomial also being deducted. On this basis, the mutual influence between converters on stability is analyzed on the level of control parameters by means of simulation studies. This method and the result can provide a reference for parameters' configuration of converters in MG with a large number of electronic devices plugged in.

2. The Structure of Multi-Source Microgrid and Analysis of Its Problems

The diversity of DGs is a common feature of MGs [\[15\]](#page-16-15). Therefore, adopting appropriate control methods is an accurate and fast way to achieve the stable operation of islanded MG.

2.1. Multi Master–Slave Control Structure of MG

The traditional master–slave control method consists of one master controller and several slave controllers, which forms the energy supply system (ESS), in order to take into account the power tracking the renewable energy and the system stability [\[19\]](#page-16-18). With the increase in the permeability and scale of MG, however, a single master controller can no longer maintain the regulation of voltage and frequency. Hence, several master control sources should be set up with a droop control method. This solution is adopted in DGs (e.g., diesel engine, micro gas turbine, fuel cell, etc.), which regulate bus voltage and frequency. Relatively, photovoltaic and wind turbines with PQ control methods run as slave sources. The use of droop control alone implements the peer-to-peer control method, and it realizes the peer-to-peer control method, which can achieve local control and coordination control without communication.

Figure [1](#page-2-0) shows a simplified structure of three-source MG in islanded mode. In Figure [1,](#page-2-0) $V_{\text{odn}} + jV_{\text{ogn}}$ and $R_n + jX_n$ are the output voltage of DGn and the equivalent impedance between bus and its converter; $i_{dn} + ji_{qn}$ is the output current of DG*n* ($n = 1, 2, 3$); $U_{Gd} + jU_{Gq}$ is the bus voltage of MG. DG1 and DG2 serve as master controllers adopting a droop control method, embodying the flexibility and redundancy of a peer-to-peer control method in power vacancy allocation; DG3 serves as a slave controller adopting the PQ control method, ensuring its constant output in islanded mode; Load is comprised of resistance and reactance. This system adopts a master–slave control method when three DGs work and it adopts a peer-to-peer control method when DG3 quits running.

Figure 1. System model of microgrid (MG) with multiple master–slave control method. **Figure 1.** System model of microgrid (MG) with multiple master–slave control method.

2.2. The Problem under Study 2.2. The Problem under Study

Fully symmetrical structure is mostly used in research on multi-source MG, whose parameters Fully symmetrical structure is mostly used in research on multi-source MG, whose parameters are the same in the same control method, ignoring the independence of control parameters of different DGs. The goal of this paper is to evaluate the following aspects: (1) whether there are interactions between $\frac{1}{2}$ control parameters to maintain stability when several converters operate in parallel; (2) whether there are interactions between control parameters of paralleled master controllers when a system's control strategy changes from single master–slave control to multiple master–slave control method; and (3) how these interactions influence the stability of MG.

This paper verified the influence of droop coefficient difference on a multi master–slave This paper verified the influence of droop coefficient difference on a multi master–slave control method based on the system model as shown in Figure [1.](#page-2-0) Set up the active droop coefficients of DG1, DG2 as 5×10^{-5} , 10×10^{-5} ; and the reactive droop coefficients of them as 0.003; other parameter settings are shown in Appendix [A;](#page-15-0) the waveform of bus voltage under different working conditions is shown in Figure [2.](#page-3-0) Figure [2a](#page-3-0) indicates the public bus bar voltage waveform when it works with DG1 and DG3, which contains only one master micro source; similarly, Figure [2b](#page-3-0) indicates the bus voltage Figure 2b indicates the bus voltage waveform when it works with DG2 and DG3. The bus voltage waveform when it works with DG2 and DG3. The bus voltage can be kept stable in the two cases. can be kept stable in the two cases. Under the same coefficient setting, when DG1, DG2 and DG3 Under the same coefficient setting, when DG1, DG2 and DG3 run together, the bus voltage waveform run together, the bus voltage waveform is oscillating and the microgrid is unstable as shown in is oscillating and the microgrid is unstable as shown in Figure [2c](#page-3-0). The cause of this phenomenon may be that the Cooperative operation of DG1 and DG2 makes the two controllers interact with each $\frac{1}{2}$ the two controls the two controllers interact with each other, so that the operation of the microgrid is deviated from its stable symphone point, and then the other, so that the operation of the microgrid is deviated from its stable running point, and then the
instability occurs. instability occurs.

Based on this conjecture, this paper delves deep into the interaction between control Based on this conjecture, this paper delves deep into the interaction between control parameters parameters under multiple master controllers' conditions, combining the case with the theoretical model. under multiple master controllers' conditions, combining the case with the theoretical model.

Figure 2. Waveforms of bus voltage under different working conditions in case of (a) DG1 and DG3 running; (b) DG2 and DG3 running; (c) DG1, DG2 and DG3 running together.

3. Theoretical Analysis of Control Methods 3. Theoretical Analysis of Control Methods 3. Theoretical Analysis of Control Methods

3.1. PQ Control Method 3.1. PQ Control Method 3.1. PQ Control Method

To improve the response speed and accuracy of power distribution, the PQ control method is To improve the response speed and accuracy of power distribution, the PQ control method is adopted [\[20–](#page-17-0)[22\]](#page-17-1). Double-loop control structure is employed: the inner loop uses current control to ensure response speed, thereby improving the operation characteristics of the system; the outer loop adopts power control [\[23\]](#page-17-2).

The structure of inner current loop is shown in Figure 3 [\[24\]](#page-17-3). The structure of inner current loop is shown in Figure [3 \[2](#page-3-1)4].

Figure 3. Structure of inner current loop. **Figure 3. Figure 3.** Structure of inner current loop. Structure of inner current loop.

In Figur[e 3](#page-3-1), V_{cd} and V_{cq} are the d,q axis voltage component of converters and V_{od} and V_{oq} are the d,q axis voltage components of the filter; L_f is the inductance of filter; K_{ip} and K_{ii} are the proportional and integral parameters of the proportional-integral (PI) controller. and integral parameters of the proportional-integral (PI) controller.

To satisfy the decoupling condition of the *d,q* axis, "virtual impedance" is introduced in To satisfy the decoupling condition of the *d,q* axis, "virtual impedance" is introduced in low-voltage AC MG [\[25](#page-17-4)[,26](#page-17-5)]. After decoupling, structure of the q axis is chosen to analyze because d,q share the same structure. Consider[in](#page-4-0)g the pulse-width modulation (PWM) and the sampling process,
the control diagram is shown in Figure 4. the control diagram is shown in Figure 4.

Figure 4. Control structure diagram of the inner current loop. **Figure 4.** Control structure diagram of the inner current loop.

As shown above, T_s is the time constant of sampling and its value is pretty small. $1/(T_s s + 1)$ and 1/(0.5*T*s*s* + 1) are the delay modules of sampling and PWM, and they can approximately merge into 1/(0.5*T*s*s* + 1) are the delay modules of sampling and PWM, and they can approximately merge into $1/(1.5T_s s + 1)$ [\[27\]](#page-17-6). Set up the switching frequency of the system as: $f_s = 20$ kHz, $T_s = 1/f_s = 0.05$ ms. The gain of the modulator is $K_{pwm} = U_{dc}/2 = 400$.

Then, the open-loop transfer function is as shown Then, the open-loop transfer function is as shown

$$
G_{iq0}(s) = \frac{K_{ip}K_{pwm}}{(1.5T_{s}s + 1)L_{f}s}.
$$
\n(1a)

Similarly, the open-loop transfer function of the *d*-axis is Similarly, the open-loop transfer function of the *d*-axis is

$$
G_{id0}(s) = \frac{K_{ip}K_{pwm}}{(1.5T_{s}s + 1)L_{f}s}.
$$
\n(1b)

In order to impose that the cut-off frequency of control is 0.1 times the switching frequency, following relations must be satisfied: the following relations must be satisfied:

$$
\begin{cases}\n\omega_x = \frac{2\pi f_s}{10} \\
20\lg|G_{iq0}(j\omega_x)| = 0\n\end{cases}
$$
\n(2)

where ω_x is the designed cut-off frequency.

If the switching frequency of the PWM modulator is 20 kHz, set up the inductor-capacitor (LC) passive filter's inductance *L_f* as 1.5 mH. $K_{ip} \approx 0.065$ can be obtained. The design principles of the converter output LC passive filter is

$$
\begin{cases}\n10f_n \le f_c \le f_s/5 \\
2\pi f_c L_f = 1/(2\pi f_c C_f)\n\end{cases} \tag{3}
$$

where f_c is the designed resonant frequency of filter, and f_n is the fundamental frequency. Setting up L_f $f(x)$ is the designed resonant frequency of filter, and $f(x)$ is the fundamental frequency. Setting up the is 1.5 mH and C_f is 20 μ F.

Based on the above analysis, the control structure of the PQ control method is shown in $\mathbf{e} \cup \mathbf{e}$ and \mathbf{e} and \mathbf{e} method is shown in the PQ. Figure [5](#page-5-0) [\[28\]](#page-17-7).

Figure 5. Block diagram for PQ (real and reactive power) control. , *Q** are the reference values of active and reference power, respectively. After decoupling, the open-loop transfer

As shown, *Kpp* and *Kpi* are the proportional and integral parameters of the PI controller for As shown, K_{pp} and K_{pi} are the proportional and integral parameters of the PI controller for active power, respectively; K_{Op} and K_{Qi} are appropriate parameters for reactive power. Due to the symmetry
of the two parts, it makes $K_{De} = K_{O}$ and $K_{Di} = K_{Qi}$. In addition, P^* , O^* are the reference values of activ of the two parts, it makes $K_{Pp} = K_{Qp}$ and $K_{Pi} = K_{Qi}$. In addition, P^* , Q^* are the reference values of active and reference power, respectively. After decoupling, the open-loop transfer function is shown
 ϵ $_{Qp}$ and $K_{Pi} = K_{Qi}$. In a Γ *O'* \int_C \int_C

$$
\begin{cases}\nG_Q(s) = \frac{1.5U_{pcc}(K_{QP}s + K_{Qi})}{C_fXs^2} G_{id}(s) \\
G_P(s) = \frac{1.5U_{pcc}(K_{PP}s + K_{Pi})}{C_fXs^2} G_{iq}(s)\n\end{cases}.
$$
\n(4)

3.2. Inductive Droop Control

and control the operation of MG as the main control micro source. Its control structure still adopts Section [2.1.](#page-1-0) Likewise, the *q*-axis structure of voltage control loop after decoupling is shown in Figure [6.](#page-5-1) The DGs with droop control can independently adjust the balance of frequency and voltage voltage-current double loop structure, where the principle of its current control loop is similar to

and control the main control micro source. Its control micro source. It is control structure still adopts the main control α

Figure 6. Structure diagram of voltage loop control. **Figure 6.** Structure diagram of voltage loop control.

The open-loop transfer function in this structure is [29] The open-loop transfer function in this structure is [\[29\]](#page-17-8)

$$
G_{vqq}(s) = \frac{G_{iq}(s)(K_{vp}s + K_{vi})}{C_f(T_s s + 1)s^2}.
$$
\n(5)

It is necessary to instant an LC passive inter at the converter outlet to inter-right order narmonics,
h can be designed as Equation (3).
This paper adopts: $f_n = 50$ Hz, $f_s = 20$ kHz, $f_c = 1000$ Hz. Considering the voltag which can be designed as Equation (3). It is necessary to install an LC passive filter at the converter outlet to filter high order harmonics,

 \blacksquare is necessary to install an LC particle converter \blacksquare inductance, $L_f = 1.5$ mH, and $C_f = 16.89$ μ F can be obtained. At this point, the PI parameters of outer loop must be satisfied: loop must be satisfied:

$$
20\lg|G_{vq0}(j\omega_x)|=0.\t\t(6)
$$

 $2016|\Theta v_{qq}(\sqrt{\omega x})| = 0.$
Taking the stability and rapidity into account, $K_{vp} = 0.1$ and $K_{vi} = 407.65$ can be obtained; then, $K_{vi} = 400.$

The converter is connected to the point of common coupling (PCC). The voltage of this point is a planned constant and selected as the reference voltage, that is: U_{pcc} < 0 = U_{pcc} + j0, the output voltage of converter filter is: $V_0 < \theta = V_{0d} + jV_{0q}$. Supposing that the impedance of low-voltage MG is $R_l + jX_l$, where $X_l = \omega L_l$, ω is the AC signal frequency, L_l is the equivalent inductance of transmission line; then, the voltage and current relation of the *d* and *q* axes are line; then, the voltage and current relation of the *d* and *q* axes are

$$
\begin{cases}\nV_{0d} - U_{pcc} = (R_l + L_l s)I_{0d} - X_l I_{0q} \\
V_{0q} - 0 = (R_l + L_l s)I_{0q} + X_l I_{0d}\n\end{cases} (7)
$$

The expression of small signal quantity of the current as shown is The expression of small signal quantity of the current as shown is

$$
\begin{cases}\n\Delta I_{0q} = \Delta I_{0q1} + \Delta I_{0q2} = -H_a \times \Delta V_{0d} + H_b \times \Delta V_{0q} \\
\Delta I_{0d} = \Delta I_{0d1} + \Delta I_{0d2} = H_b \times \Delta V_{0d} + H_a \times \Delta V_{0q}\n\end{cases}
$$
\n(8)

where H_a and H_b can be expressed as

$$
H_a = \frac{X_l}{X_l^2 + (R_l + L_l s)^2}; \ H_b = \frac{(R_l + L_l s)}{X_l^2 + (R_l + L_l s)^2}.
$$
\n(9)

Actually, I_{0d} and I_{0q} are DC variables, and their differential results are negligible for L_{ls} and much smaller than X_l .

 $P + jQ = U_{pcc}(I_{0d} - jI_{0q})$ is the power equation in the *dq*0 coordinate system, and the power small signal model can be obtained: signal model can be obtained:

$$
\begin{cases}\n\Delta Q = -1.5U_{pcc}(\Delta I_{0q1} + \Delta I_{0q2}) \\
\Delta P = 1.5U_{pcc}(\Delta I_{0d1} + \Delta I_{0d2})\n\end{cases}.
$$
\n(10)

For double loop structure, the virtual impedance is equivalent to introducing a logical inductive For double loop structure, the virtual impedance is equivalent to introducing a logical feedback link in essence, which corrects the reference voltage of dual-loop control and controls the output power further.

Supposing that θ is quite small, then $V_{0q}^* = E^*$ sin $\theta \approx E^* \theta$, $V^*_{0d} \approx E^*$, where E^* is the reference voltage from reactive droop loop. Furthermore, it can be considered that $\Delta V^*_{\;\;0q}\approx E\Delta\theta$ because changes of E^* are much smaller than that of θ , where E is the reference voltage before reactive droop loop.
The control structure is shown in [Fig](#page-6-0)[ure](#page-17-5) 7 [26]. The control structure is shown in Figure 7 [26].

Figure 7. Droop control structure diagram in low-voltage MG. **Figure 7.** Droop control structure diagram in low-voltage MG.

After reasonable setting of virtual impedance, it is equivalent that the previous line impedance After reasonable setting of virtual impedance, it is equivalent that the previous line impedance connects in series with a reactance X_v , which satisfies the following relationship $X_v + X_v \gg R_l$, and then R_l in H_a and H_b can be neglected, that is $H_b = 0$, indicating the realization of decoupling in control. droop control.

4. Small Signal Modeling of Three-Source MG

Theoretical analysis of a three-source MG with all DGs working at the same time is performed on the basis of model built in Section 1.1. To help analyze the stability of system, the electrical quantities are expressed in steady state small signal equations [\[30](#page-17-9)[,31\]](#page-17-10), according to the relationship of voltage and current in *dq*0 coordinate system:

$$
\begin{cases}\n\Delta V_{odn} - \Delta U_{Gd} = (R_n + \frac{X_n}{\omega} s) \Delta i_{dn} - X_n \Delta i_{qn} \\
\Delta V_{ogn} - \Delta U_{Gq} = (R_n + \frac{X_n}{\omega} s) \Delta i_{qn} + X_n \Delta i_{dn}\n\end{cases}.
$$
\n(11)

Generally, the differential terms in Equation (11) has less influence and can be ignored. Therefore, the system model satisfies Equation (12):

$$
\begin{cases}\n\Delta V_{od1} - \Delta U_{Gd} = R_1 \Delta i_{d1} - X_1 \Delta i_{q1} \\
\Delta V_{og1} - \Delta U_{Gq} = R_1 \Delta i_{q1} + X_1 \Delta i_{d1} \\
\Delta V_{od2} - \Delta U_{Gd} = R_2 \Delta i_{d2} - X_2 \Delta i_{q2} \\
\Delta V_{og2} - \Delta U_{Gq} = R_2 \Delta i_{q2} + X_2 \Delta i_{d2} \\
\Delta V_{od3} - \Delta U_{Gd} = R_3 \Delta i_{d3} - X_3 \Delta i_{q3} \\
\Delta V_{og3} - \Delta U_{Gq} = R_1 \Delta i_{q3} + X_1 \Delta i_{d3} \\
0 - \Delta U_{Gd} = R_4 \Delta i_{d4} - X_4 \Delta i_{q4} \\
0 - \Delta U_{Gq} = R_2 \Delta i_{q4} + X_4 \Delta i_{d4} \\
\Delta i_{d1} + \Delta i_{d2} + \Delta i_{d3} + \Delta i_{d4} = 0 \\
\Delta i_{q1} + \Delta i_{q2} + \Delta i_{q3} + \Delta i_{q4} = 0\n\end{cases} (12)
$$

Assuming that ΔV_{od1} , ΔV_{og1} , ΔV_{od2} , ΔV_{og2} , ΔV_{od3} , ΔV_{og3} , R_1 , X_1 , R_2 , X_2 , R_3 , X_3 , R_4 , X_4 are known, ∆*id*1, ∆*iq*1, ∆*id*2, ∆*iq*2, ∆*id*3, ∆*iq*3, ∆*id*4, ∆*iq*⁴ can be expressed with the above quantities by solving Equation (12), ΔU_{Gd} , $\Delta j U_{Gq}$ by Equation (13):

$$
\begin{cases}\n\Delta U_{Gd} = J_1 \Delta V_{od1} + J_2 \Delta V_{od2} + J_3 \Delta V_{od3} + J_4 \Delta V_{og1} + J_5 \Delta V_{og2} + J_6 \Delta V_{og3} \\
\Delta U_{Gq} = J_7 \Delta V_{od1} + J_8 \Delta V_{od2} + J_9 \Delta V_{od3} + J_{10} \Delta V_{og1} + J_{11} \Delta V_{og2} + J_{12} \Delta V_{og3}\n\end{cases}.
$$
\n(13)

It is clear that $X_1 \gg R_1$, $X_2 \gg R_2$ [\[25,](#page-17-4)[26\]](#page-17-5) when DG1 and DG2 adopt the droop control method, and then the influence of line resistance can be ignored, that is: $R_1 = R_2 = 0$. Suppose that the load is mostly active and then: $X_4 = 0$. Therefore, the coefficients in Equation (13) can be expressed as

$$
\begin{cases}\nI_1 = J_{10} = [R_3^2 R_4^2 (X_1 X_2 + X_2^2) + R_4^2 X_2 X_3 (X_1 X_2 + X_1 X_3 + X_2 X_3)]/D_d \\
I_2 = J_{11} = [R_3^2 R_4^2 (X_1 X_2 + X_1^2) + R_4^2 X_1 X_3 (X_1 X_2 + X_1 X_3 + X_2 X_3)]/D_d \\
I_3 = J_{12} = [R_3 R_4 X_1^2 X_2^2 + R_4^2 X_1 X_2 (X_1 X_2 + X_1 X_3 + X_2 X_3)]/D_d \\
I_4 = -J_7 = [R_4 X_1 X_2^2 (R_3^2 + R_3 R_4 + X_3^2)]/D_d \\
I_5 = -J_8 = [R_4 X_1^2 X_2 (R_3^2 + R_3 R_4 + X_3^2)]/D_d \\
I_6 = -J_9 = [-R_3 R_4^2 X_1 X_2 (X_1 + X_2) + R_4 X_1^2 X_2^2 X_3]/D_d \\
D_d = R_3^2 R_4^2 (X_1 + X_2)^2 + (R_1 + R_2)^2 X_1^2 X_2^2 + X_1^2 X_2^2 X_3^2 + 2R_4^2 X_1 X_2 X_3 (X_1 + X_2 + X_3) + R_4^2 X_3^2 (X_1^2 + X_3^2)\n\end{cases}
$$
\n(14)

After ignoring the differential terms, model of droop control is shown by Equations (13) and (14) is obtained from model of PQ control:

$$
\begin{cases}\n[\Delta E_1^* - \frac{3n_1 U_{pcc}}{2X_1} (\Delta V_{od1} - \Delta U_{Gd})] G_{vd1}(s) = \Delta V_{od1} \\
[\Delta \omega_{01}^* - \frac{3m_1 U_{pcc}}{2X_1} (\Delta V_{og1} - \Delta U_{Gq})] G_{vq1}(s) = \Delta V_{og1} \\
[\Delta E_2^* - \frac{3n_2 U_{pcc}}{2X_2} (\Delta V_{od2} - \Delta U_{Gd})] G_{vq2}(s) = \Delta V_{od2} \\
[\Delta \omega_{02}^* - \frac{3m_2 U_{pcc}}{2X_2} (\Delta V_{og2} - \Delta U_{Gq})] G_{vq2}(s) = \Delta V_{og2}\n\end{cases} (15)
$$

$$
\begin{cases}\nG_Q(s)\{\Delta Q_3^* + 1.5U_{pcc}[-X_3M + R_3N]\} = \Delta V_{od3} \\
G_P(s)\{\Delta P_3^* - 1.5U_{pcc}[R_3M + X_3N]\} = \Delta V_{od3} \\
M = \frac{(\Delta V_{od3} - \Delta U_{Gd})}{X_3^2 + R_3^2} \\
N = \frac{(\Delta V_{od3} - \Delta U_{Gq})}{X_3^2 + R_3^2}\n\end{cases} (16)
$$

To simplify the equations, setting up $H_1 = 1.5n_1U_{pcc}/X_1$, $H_2 = 1.5m_1U_{pcc}/X_1$, $H_3 = 1.5n_2U_{pcc}/X_2$, $H_4 = 1.5 m_2 U_{pcc}/X_2$, $H_5 = 1.5 U_{pcc} X_3/(X_3^2 + R_3^2)$, $H_6 = 1.5 U_{pcc} R_3/(X_3^2 + R_3^2)$, by solving simultaneously Equations (15) and (16), Equation (17) is obtained.

$$
\begin{cases}\n[\Delta E_{1}^{*} - H_{1}(\Delta V_{od1} - \Delta U_{Gal})]G_{vd1}(s) = \Delta V_{od1} \\
[\Delta \omega_{01}^{*} - H_{2}(\Delta V_{og1} - \Delta U_{Gq})]G_{vd1}(s) = \Delta V_{og1} \\
[\Delta E_{2}^{*} - H_{3}(\Delta V_{od2} - \Delta U_{Gal})]G_{vd2}(s) = \Delta V_{od2} \\
[\Delta \omega_{02}^{*} - H_{4}(\Delta V_{og2} - \Delta U_{Gq})]G_{vd2}(s) = \Delta V_{og2} \\
G_{Q}(s)[\Delta Q_{3}^{*} - H_{5}(\Delta V_{od3} - \Delta U_{Gal}) + \\
H_{6}(\Delta V_{og3} - \Delta U_{Gq})] = \Delta V_{od3} \\
G_{P}(s)[\Delta P_{3}^{*} - H_{6}(\Delta V_{od3} - \Delta U_{Gal}) + \\
H_{5}(\Delta V_{og3} - \Delta U_{Gq})] = \Delta V_{od3}\n\end{cases}
$$
\n(17)

where Δ*E*^{*}₁ and Δ*ω*_{0*i*}^{*} are the reference voltage and reference frequency of DG*i* (*I* = 1, 2), which adopts droop control.

By solving Equations (13) and (17), Equation (18) can be obtained:

$$
\left[\begin{array}{cc} \Delta U_{Gd} & \Delta U_{Gq} \end{array}\right]^T = H_G^{2 \times 6} \left[\begin{array}{cc} \Delta E_1^* & \Delta \omega_{01}^* & \Delta E_2^* & \Delta \omega_{02}^* & \Delta Q_3^* & \Delta P_3^* \end{array}\right]^T. \tag{18}
$$

On the premise of guaranteeing the stability of the inner loop, $G_{id}(s) = G_{iq}(s) = 1$ is reasonable [\[21,](#page-17-11)[32\]](#page-17-12); therefore, $G_{\textit{vd}}(s) = G_{\textit{va}}(s) = 1$. In addition, H_G is a matrix of 2 \times 6, whose simplified one is shown in Equation (19):

$$
\begin{bmatrix}\n\Delta U_{Gd} \\
\Delta U_{Gq}\n\end{bmatrix} = \begin{bmatrix}\n\frac{C_1(s)}{D(s)} & \frac{C_2(s)}{D(s)} & \frac{C_3(s)}{D(s)} & \frac{C_4(s)}{D(s)} & \frac{C_5(s)}{D(s)} & \frac{C_6(s)}{D(s)} \\
\frac{F_1(s)}{D(s)} & \frac{F_2(s)}{D(s)} & \frac{F_3(s)}{D(s)} & \frac{F_4(s)}{D(s)} & \frac{F_5(s)}{D(s)} & \frac{F_6(s)}{D(s)} \\
\times \begin{bmatrix}\n\Delta E_1^* & \Delta \omega_{01}^* & \Delta E_2^* & \Delta \omega_{02}^* & \Delta Q_3^* & \Delta P_3^* \\
\times \begin{bmatrix}\n\Delta E_1^* & \Delta \omega_{01}^* & \Delta E_2^* & \Delta \omega_{02}^* & \Delta Q_3^* & \Delta P_3^*\n\end{bmatrix}^T.\n\end{bmatrix} (19)
$$

As shown above, Equation (19) is the small-signal control model of the islanded MG, elements of whose coefficient matrix share the same denominator named *D*(*s*). By analyzing the characteristic equation $D(s) = 0$, the stability of the system can be determined.

5. Simulation and Stability Analysis

5.1. Parameter Setting and Calculation

Based on Figure [1,](#page-2-0) DG1 and DG2 should satisfy: *P*¹ = 30,000 − (*f* − 50)/*m*1, *P*² = 30,000 − (*f* − 50)/*m*2, $Q_1 = 5000 - (E_1 - 311)/n_1$, $Q_2 = 5000 - (E_2 - 311)/n_2$.

Using the parameters in Appendix [A,](#page-15-0) H_1 - H_6 can be obtained: $H_1 = 466.5n_1$, $H_2 = 466.5m_1$, $H_3 = 466.5n_2$, $H_4 = 466.5m_2$, $H_5 = 208.6$ and $H_6 = 417.2$.

5.2. Influence of Active Droop Coefficient m¹ and m² on Stability

To explore the impact of single variable m_1 on system stability, a priority assignment is first implemented: $n_1 = n_2 = 0.001 \text{ V}/\text{var}, K_{Pp} = K_{Qp} = 0.0005, K_{Pi} = K_{Qi} = 0.5.$

(1) When $m_2 = 5 \times 10^{-5}$ Hz/W, the characteristic equation $D(s) = 0$ is $\frac{1}{1}$ (125 $\frac{1}{2}$ *m sm sm s*

$$
(m_1 + 0.00242)s^5 + (234m_1 + 0.542)s^4 + (125m_1 + 0.392)s^3
$$

+
$$
(9860m_1 + 42.3)s^2 + (3790m_1 + 15.7)s + (58,000m_1 + 122) = 0
$$
 (20)

The root locus equation as Equation (20) whose gain is *m*¹ can be acquired by processing Equation (21): Ine root

$$
m_1 W_1(s) + 1 = 0,\t\t(21)
$$

where *W*1(*s*) and the similar expressions hereafter in this paper can be found in Appendix B. where *W*1*(s)* and the similar expressions hereafter in this paper can be found in Appendix [B.](#page-15-1)

The root locus of *D*(*s*) when m_1 varies from 0 to + ∞ is shown in Figure [8.](#page-9-0)

Figure 8. The root locus of *D*(s) following *m*₁ changes when $m_2 = 5 \times 10^{-5}$ Hz/W.

There are five branches, S_1 starts from (-233.8x, 0) to (-225.3, 0) and always stays in left half-plane and far away from the imaginary axis, so it is not shown in the picture; S_2 and S_3 locate in left half-plane and have no impact on stability; S_4 and S_5 move towards the positive direction with the change of m_1 , leading to the decline in stability, they finally cross the imaginary axis ($m_1 = 3.2 \times 10^{-5}$) and enter the 10−5) and enter the right half-plane indicating that the system is no longer stable. Therefore, the right half-plane indicating that the system is no longer stable. Therefore, the proper range of *m*¹ to ensure system stability is $[0, 3.2 \times 10^{-5})$ in this condition.

Theoretically, the smaller m_1 is, the weaker the impact of change in DG1's output power on system's frequency is, especially when $m_1 = 0$, DG1 works in constant frequency control mode and has the strongest stability. At this point, DG1 has theoretically infinite power supply, which owns the $\frac{1}{2}$ absolute frequency stability and peak regulating ability. However, this assumption is not consistent with the energy attributes of MG. That is, MG's output power is limited and relies on other MGs' cooperation, so *m*¹ cannot be too small. On the other hand, a large value of *m*¹ also results in the fast oscillation of system frequency under small power fluctuation, which is harmful to system stability and this situation is shown in Figure [8](#page-9-0) when $m_1 > 3.2 \times 10^{-5}$.

When $m_1 = 2.5 \times 10^{-5}$ Hz/W and $m_2 = 5 \times 10^{-5}$ Hz/W, the bus voltage waveform is shown in Figure [9.](#page-10-0) Because 2.5 × 10⁻⁵ ∈ [0, 3.2 × 10⁻⁵) and the bus voltage is stable, it means that the m_1 in this range ensures microgrid stable operation, which can verify the correctness of above analysis.

Figure 9. The bus voltage waveform when $m_1 = 2.5 \times 10^{-5}$ Hz/W and $m_2 = 5 \times 10^{-5}$ Hz/W.

(2) When $m_2 = 10 \times 10^{-5}$ Hz/W, the root locus equation whose gain is m_1 is

$$
m_1 W_2(s) + 1 = 0.
$$
 (22)

The root locus of *D*(*s*) when m_1 varies from 0 to +∞ is shown in Figure [10.](#page-10-1)

 T_{S} is so similar to Figure 8 that it won't be described again. The proper range of T_{S} is the proper range of T_{S} **Figure 10.** The root locus of *D*(s) following *m*₁ changes when $m_2 = 10 \times 10^{-5}$ Hz/W.

[0, 2.9 × 10−5), and system stability declines with the increase of *m*1. nocus is so similar to Figure 8 that it won t be described again. The proper range of *i* [0, 2.9 \times 10⁻⁵), and system stability declines with the increase of m_1 . The locus is so similar to Figure 8 that it won't be described again. The proper range of *m*¹ is The locus is so similar to Figure [8](#page-9-0) that it won't be described again. The proper range of *m*₁ is

When $m_1 = 2 \times 10^{-5}$ Hz/W and $m_2 = 10 \times 10^{-5}$ Hz/W, the bus voltage waveform is shown in Figure [11.](#page-10-2) The waveform is similar to Figure [9,](#page-10-0) without more detailed analysis.

Figure 11. The bus voltage waveform when $m_1 = 2 \times 10^{-5}$ Hz/W and $m_2 = 10 \times 10^{-5}$ Hz/W.

(3) When $m_2 = 2.5 \times 10^{-5}$ Hz/W, the root locus equation whose gain is m_1 is

$$
m_1 W_3(s) + 1 = 0. \t\t(23)
$$

The root locus of *D*(*s*) when m_1 varies from 0 to +∞ is shown in Figure [12.](#page-11-0)

Figure 12. The root locus of *D*(s) following *m*₁ changes when $m_2 = 2.5 \times 10^{-5}$ Hz/W.

The locus is so similar to Figure [8](#page-9-0) that it won't be described again. The proper range of m_1 is [0, 7.21 \times 10⁻⁵), and system stability declines with the increase of m_1 . who many securities with the mercuse of m₁.

When $m_1 = 5 \times 10^{-5}$ Hz/W and $m_2 = 2.5 \times 10^{-5}$ Hz/W, the bus voltage waveform is shown in Figure [13.](#page-11-1) The waveform is similar to Figure 9, without more detailed analysis. Figure 13. The waveform is similar to Figur[e 9](#page-10-0), without more detailed analysis.

Figure 13. The bus voltage waveform when $m_1 = 5 \times 10^{-5}$ Hz/W and $m_2 = 2.5 \times 10^{-5}$ Hz/W.

In summary, the comparison of range for m_1 when m_2 is different is shown in Table [1.](#page-11-2) In Table [1,](#page-11-2) m_1 is less than 2.9 \times 10⁻⁵ when m_2 is 10 \times 10⁻⁵. It is the reason why bus voltage is unstable in Section 1.2. The allowable range of m_1 narrows with the increase of m_2 . From the perspective of system stability, the active droop coefficients of two DGs are supposed to be coordinated and restricted in a lower range so that the unit power loss won't cause large change in frequency and system frequency collapse.

Table 1. The influence of active droop coefficients between DG1 and DG2.

m_2 (Hz/W)	Range of m_1 (Hz/W)
2.5×10^{-5}	$[0, 7.21 \times 10^{-5})$
5×10^{-5}	$[0, 3.2 \times 10^{-5}]$
10×10^{-5}	$[0, 2.9 \times 10^{-5})$

5.3. Influence of Reactive Droop Coefficient n¹ and n² on Stability

To explore the impact of single variable n_1 on system stability, a priority assignment is first implemented: *m*¹ = *m*² = 2.5 × 10−⁵ Hz/W, *KPp* = *KQp* = 0.0005, *KPi* = *KQi* = 0.5.

(1) When $n_2 = 0.002 \text{ V}/\text{var}$, the root locus of the equation $D(s) = 0$ whose gain is n_1 is implemented: *m*¹ = *m*² = 2.5 × 10−⁵ Hz/W, *KPp* = *KQp* = 0.0005, *KPi* = *KQi* = 0.5. (1) When *n*² = 0.002 V/var, the root locus of the equation *D*(*s*) = 0 whose gain is *n*¹ is

$$
n_1 W_4(s) + 1 = 0. \t\t(24)
$$

The root locus when n_1 varies from 0 to +∞ is shown in Figure [14.](#page-12-0)

Figure 14. The root locus of *D*(s) following n_1 changes when $n_2 = 0.002 \text{ V}/\text{var}.$

There are six branches, *S*¹ first moves towards left and then turns right and always stays in the There are six branches, S_1 first moves towards left and then turns right and always stays in the left half-plane, indicating that the system stability first enhances and then degrades; S_2 and S_3 are located in the left half-plane and have no impact on stability; S_4 and S_5 move towards the positive direction with the change of n_1 , leading to the decline in stability, they finally cross the imaginary axis $(n_1 = 0.00147)$ and enter the right half-plane indicating that the system is no longer stable. Therefore, the proper range of n_1 to ensure system stability is $[0, 0.00147)$ in this condition.

Theoretically, the smaller *n*₁ is, the weaker the impact of change in DG1's output reactive power on system's voltage is. Especially when *n*₁ = 0, DG1</sub> works in constant voltage control mode and has which owns the absolute voltage stability and reactive power compensation ability. However, this the strongest stability. At this point, DG1 has theoretically infinite reactive power supply, which owns the absolute voltage stability and reactive power compensation ability. However, this assumption is not consistent with the energy attributes of MG. That is, MG's output reactive power is limited and relies on other MGs' cooperation, so n_1 cannot be too small. On the other hand, a large value of n_1 also results in voltage collapse under small reactive power fluctuation, and this instable situation is shown in picture when $n_1 > 0.00147$.

When $n_1 = 0.001$ V/var and $n_2 = 0.002$ V/var, the bus voltage waveform is shown in Figure [15.](#page-12-1) Because 0.001 ∈ [0, 0.00147) and the bus voltage is stable, it means that the *n*₁ in this range ensures microgrid stable operation, which can verify the correctness of the above analysis. microgrid stable operation, which can verify the correctness of the above analysis.

Figure 15. The bus voltage waveform when $n_1 = 0.001 \text{ V}/\text{var}$ and $n_2 = 0.002 \text{ V}/\text{var}$.

(2) When $n_2 = 0.001 \text{ V}/\text{var}$, the root locus equation is

$$
n_1 W_5(s) + 1 = 0. \t\t(25)
$$

The root locus of *D*(*s*) when *n*₁ varies from 0 to +∞ is shown in Figure [16.](#page-13-0)

Figure 16. The root locus of *D*(s) following n_1 changes when $n_2 = 0.001$ V/var.

Because this locus is similar to Figure 14 , it won't be described again. The proper range of n_1 is $[0, 0.00169)$, and system stability declines with the increase of n_1 .

When $n_1 = 0.001$ V/var and $n_2 = 0.001$ V/var, the bus voltage waveform is shown in Figure 17. The waveform is similar to Figure [15,](#page-12-1) without more detailed analysis.

Figure 17. The bus voltage waveform when $n_1 = 0.001 \text{ V}/\text{var}$ and $n_2 = 0.001 \text{ V}/\text{var}$.

(3) When $n_2 = 0.004 \text{ V}/\text{var}$, the root locus equation is

$$
n_1 W_6(s) + 1 = 0. \t\t(26)
$$

The root locus of *D*(*s*) when n_1 varies from 0 to +∞ is shown in Figure [18.](#page-14-0)

Figure 18. The root locus of $D(s)$ following n_1 changes when $n_2 = 0.004 \text{ V}/\text{var}.$

Because this locus is similar to Figure [14,](#page-12-0) it won't be described again. The proper range of n_1 is [0, 0.00133), and system stability declines with the increase of n_1 .

When $n_1 = 0.001$ V/var and $n_2 = 0.004$ V/var, the bus voltage waveform is shown in Figure 19. The waveform is similar to Figure 15, without more detailed analysis. The waveform is similar to Figure [15,](#page-12-1) without more detailed analysis. The waveform is similar to Figure 15, without more detailed analysis.

Figure 19. The bus voltage waveform when $n_1 = 0.001$ V/var and $n_2 = 0.004$ V/var.

In summary, the comparison of range of *n*¹ when *n*² is different is shown in Table [2.](#page-14-2) The allowable range of *n*¹ narrows with the increase of *n*2. From the perspective of system stability, the reactive droop coefficients of two DGs are supposed to be coordinated because it is restricted in such a low value range that the unit reactive power loss won't cause large change in voltage—thus avoiding the vicious cycle: "change in voltage-reactive power loss-enlargement change in voltage—larger reactive power loss".

Table 2. The influence of reactive droop coefficients between DG1 and DG2.

n_2 (V/var)	Range of n_1 (V/var)
0.001	[0, 0.00169)
0.002	[0, 0.00147)
0.004	[0, 0.00133)

6. Conclusions

In this paper, research on influence of the wide application of electronic devices on system stability is done by a three-source MG with a multiple master-slave control method.

Different from the traditional master–slave control model, this paper established a model where several master controllers coordinate and control the system in islanded mode. Then, the "virtual impedance" was introduced to satisfy the decoupling condition and the small-signal decoupling control model, which contains two main control sources and subordinate one, was also developed on the basis of theory. Finally, the interaction between various DGs with droop control from the perspective of control parameters was explored with the aid of the root locus method. The results show that the value range of the droop coefficient for the two main DGs has mutual influence and the coordinated allocation of parameters also affects the stability of microgrid operation. This research could serve as a reference for parameter setting and contributed to study on stability of multi-source MG.

Author Contributions: All of the authors contributed to this work. H.L. and P.L. provided important comments on the modeling and designed the experiments; Y.D. and C.Z. performed the experiments and analyzed the data; Y.D. and Y.H. wrote the whole paper.

Funding: This research was funded by the National Natural Science Foundation of China (No. 51577068) and the National High Technology Research and Development Program of China (No. 2015AA050101). And the APC was funded by North China Electric Power University.

Acknowledgments: The authors gratefully acknowledge the support from the National Natural Science Foundation of China (No. 51577068) and the National High Technology Research and Development Program of China (No. 2015AA050101).

Conflicts of Interest: The authors declare no conflict of interest.

Appendix A

Table A1. System basic parameter value.

Appendix B

The expressions of coefficients $W_1(s)$ – $W_6(s)$ in Equations (21)–(26) are shown in (A1)–(A6).

$$
W_1(s) = \frac{412.78s^5 + 96,596s^4 + 51,663s^3 + 4,069,653s^2 + 1,562,487s + 23,925,000}{s^5 + 223.78s^4 + 161.64s^3 + 17,462s^2 + 6492s + 50,574},\tag{A1}
$$

$$
W_2(s) = \frac{413.2s^5 + 96,818s^4 + 51,322s^3 + 3,997,107s^2 + 1,536,776s + 24,028,925}{s^5 + 224.3s^4 + 161.2s^3 + 17,340s^2 + 6450s + 50,785},
$$
 (A2)

$$
W_3(s) = \frac{412.7s^5 + 96,558s^4 + 51,863s^3 + 4,110,238s^2 + 1,576,956s + 23,890,375}{s^5 + 223.67s^4 + 162s^3 + 17,538s^2 + 6519s + 50,501},
$$
 (A3)

$$
W_4(s) = \frac{128,449s^5 + 32,460,140s^4 + 17,352,828s^3 + 2,532,328,040s^2 + 490,885,015s + 7,337,660,287}{s^6 + 257.04s^5 + 173.83s^4 + 29,655.7s^3 + 8295s^2 + 952,419s}, \quad (A4)
$$

$$
W_5(s) = \frac{128,449s^5 + 16,237,480s^4 + 16,087,143s^3 + 1,266,640,229s^2 + 483,547,355s + 3,668,830,143}{s^6 + 128.6s^5 + 159s^4 + 14,834s^3 + 7342s^2 + 476,209s}, \quad (A5)
$$

$$
W_6(s) = \frac{128,449s^5 + 64,905,460s^4 + 19,884,196s^3 + 5,063,703,661s^2 + 505,560,336s + 14,675,320,574}{s^6 + 513.9s^5 + 203.5s^4 + 59,299s^3 + 10,200s^2 + 1,904,839s}.
$$
 (A6)

References

- 1. Marzband, M.; Javadi, M.; Pourmousavi, S.A.; Lightbody, G. An advanced retail electricity market for active distribution systems and home microgrid interoperability based on game theory. *Electr. Power Syst. Res.* **2018**, *157*, 187–199. [\[CrossRef\]](http://dx.doi.org/10.1016/j.epsr.2017.12.024)
- 2. Chendan, L.; Savaghebi, M.; Guerrero, J.M.; Coelho, E.A.; Vasquez, J.C. Operation cost minimization of droop-controlled AC microgrids using multiagent-based distributed control. *Energies* **2016**, *9*, 717. [\[CrossRef\]](http://dx.doi.org/10.3390/en9090717)
- 3. Amoateng, D.O.; Hosani, M.A.; Moursi, M.S.E.; Turitsyn, K.; Kirtley, J.L. Adaptive voltage and frequency control of islanded multi-microgrids. *IEEE Trans. Power Syst.* **2017**, *33*, 4454–4465. [\[CrossRef\]](http://dx.doi.org/10.1109/TPWRS.2017.2780986)
- 4. Kosari, M.; Hosseinian, S.H. Decentralized reactive power sharing and frequency restoration in islanded microgrid. *IEEE Trans. Power Syst.* **2017**, *32*, 2901–2912. [\[CrossRef\]](http://dx.doi.org/10.1109/TPWRS.2016.2621033)
- 5. Divshali, P.H.; Hosseinian, S.H.; Abedi, M. A novel multi-stage fuel cost minimization in a VSC-based microgrid considering stability, frequency, and voltage constraints. *IEEE Trans. Power Syst.* **2013**, *28*, 931–939. [\[CrossRef\]](http://dx.doi.org/10.1109/TPWRS.2012.2210449)
- 6. Bonfiglio, A.; Brignone, M.; Invernizzi, M.; Labella, A.; Mestriner, D.; Procopio, R. A simplified microgrid model for the validation of islanded control logics. *Energies* **2017**, *10*, 1141. [\[CrossRef\]](http://dx.doi.org/10.3390/en10081141)
- 7. Guo, Q.; Cai, H.; Wang, Y.; Chen, W. Distributed secondary voltage control of islanded microgrids with event-triggered scheme. *J. Power Electron.* **2017**, *17*, 1650–1657.
- 8. Farrokhabadi, M.; Cañizares, C.A.; Bhattacharya, K. Frequency control in isolated/islanded microgrids through voltage regulation. *IEEE Trans. Smart Grid* **2017**, *8*, 1185–1194. [\[CrossRef\]](http://dx.doi.org/10.1109/TSG.2015.2479576)
- 9. Serban, I. A control strategy for microgrids: Seamless transfer based on a leading inverter with supercapacitor energy storage system. *Appl. Energy* **2018**, *221*, 490–507. [\[CrossRef\]](http://dx.doi.org/10.1016/j.apenergy.2018.03.122)
- 10. Lin, P.; Wang, P.; Xiao, J.; Wang, J.; Jin, C.; Tang, Y. An integral droop for transient power allocation and output impedance shaping of hybrid energy storage system in DC microgrid. *IEEE Trans. Power Electron.* **2017**, *33*, 6262–6277. [\[CrossRef\]](http://dx.doi.org/10.1109/TPEL.2017.2741262)
- 11. Etemadi, A.H.; Davison, E.J.; Iravani, R. A generalized decentralized robust control of islanded microgrids. *IEEE Trans. Power Syst.* **2014**, *29*, 3102–3113. [\[CrossRef\]](http://dx.doi.org/10.1109/TPWRS.2014.2312615)
- 12. Pogaku, N.; Prodanovic, M.; Green, T.C. Modeling, analysis and testing of autonomous operation of an inverter-based microgrid. *IEEE Trans. Power Electron.* **2007**, *22*, 613–625. [\[CrossRef\]](http://dx.doi.org/10.1109/TPEL.2006.890003)
- 13. Herrera, L.; Inoa, E.; Guo, F.; Wang, J.; Tang, H. Small-signal modeling and networked control of a PHEV charging facility. *IEEE Trans. Ind. Appl.* **2014**, *50*, 1121–1130. [\[CrossRef\]](http://dx.doi.org/10.1109/TIA.2013.2272912)
- 14. Zhu, M.; Li, H.; Li, X. Improved state-space model and analysis of islanding inverter-based microgrid. In Proceedings of the 2013 IEEE International Symposium on Industrial Electronics, Taipei, Taiwan, 28–31 May 2013; pp. 1–5.
- 15. Makrygiorgou, D.I.; Alexandridis, A.T. Distributed stabilizing modular control for stand-alone microgrids. *Appl. Energy* **2018**, *210*, 925–935. [\[CrossRef\]](http://dx.doi.org/10.1016/j.apenergy.2017.07.085)
- 16. Wu, T.; Liu, Z.; Liu, J.; Liu, B.; Wang, S. Modeling and stability analysis of the small-AC-signal droop based secondary control for islanded microgrids. In Proceedings of the 2016 IEEE Energy Conversion Congress and Exposition (ECCE), Milwaukee, WI, USA, 18–22 September 2016.
- 17. Cao, W.; Ma, Y.; Yang, L.; Wang, F.; Tolbert, L.M. D-Q impedance based stability analysis and parameter design of three-phase inverter-based ac power systems. *IEEE Trans. Ind. Electron.* **2017**, *64*, 6017–6028. [\[CrossRef\]](http://dx.doi.org/10.1109/TIE.2017.2682027)
- 18. Yu, Z.; Ai, Q.; He, X.; Piao, L. Adaptive droop control for microgrids based on the synergetic control of multi-agent systems. *Energies* **2016**, *9*, 1057. [\[CrossRef\]](http://dx.doi.org/10.3390/en9121057)
- 19. Ghalebani, P.; Niasati, M. A distributed control strategy based on droop control and low-bandwidth communication in DC microgrids with increased accuracy of load sharing. *Sustain. Cities Soc.* **2018**, *40*, 155–164. [\[CrossRef\]](http://dx.doi.org/10.1016/j.scs.2018.04.011)
- 20. Khayamy, M.; Ojo, O. A power regulation and droop mode control method for a stand-alone load fed from a PV-current solurce inverter. *Int. J. Emerg. Electr. Power Syst.* **2015**, *16*, 83–91.
- 21. Shuai, Z.; Shen, C.; Yin, X.; Liu, X.; Shen, Z.J. Fault analysis of inverter-interfaced distributed generators with different control schemes. *IEEE Trans. Power Deliv.* **2017**, *33*, 1223–1235. [\[CrossRef\]](http://dx.doi.org/10.1109/TPWRD.2017.2717388)
- 22. Meng, X.; Liu, Z.; Liu, J.; Wu, T.; Wang, S.; Liu, B. A seamless transfer strategy based on special master and slave DGs. In Proceedings of the 2017 IEEE Future Energy Electronics Conference and Ecce Asia, Kaohsiung, Taiwan, 3–7 June 2017.
- 23. Chen, H.; Xu, Z.; Zang, F. Nonlinear control for VSC based HVDC system. In Proceedings of the 2006 IEEE Power Engineering Society General Meeting, Montreal, QC, Canada, 18–22 June 2006.
- 24. Lang, H.; Yue, D.; Cao, D. Research on VSC-HVDC double closed loop controller based on variable universe fuzzy PID control. In Proceedings of the 2017 IEEE China International Electrical and Energy Conference, Beijing, China, 25–27 October 2017.
- 25. Dou, C.; Zhang, Z.; Yue, D.; Song, M. Improved droop control based on virtual impedance and virtual power source in low-voltage microgrid. *Iet Gener. Transm. Distrib.* **2017**, *11*, 1046–1054. [\[CrossRef\]](http://dx.doi.org/10.1049/iet-gtd.2016.1492)
- 26. Wu, X.; Shen, C.; Iravani, R. Feasible range and optimal value of the virtual impedance for droop-based control of microgrids. *IEEE Trans. Smart Grid* **2017**, *8*, 1242–1251. [\[CrossRef\]](http://dx.doi.org/10.1109/TSG.2016.2519454)
- 27. Ramos-Fuentes, G.A.; Melo-Lagos, I.D.; Regino-Ubarnes, F.J. Odd harmonic high order repetitive control of single-phase PWM rectifiers: Varying frequency operation. *Techno Lógicas* **2016**, *19*, 63–76.
- 28. Tripathi, R.N.; Singh, A.; Hanamoto, T. Design and control of LCL filter interfaced grid connected solar photovoltaic (SPV) system using power balance theory. *Int. J. Electr. Power Energy Syst.* **2015**, *69*, 264–272. [\[CrossRef\]](http://dx.doi.org/10.1016/j.ijepes.2015.01.018)
- 29. Shuai, Z.; Sun, Y.; Shen, Z.J.; Tian, W.; Tu, C.; Li, Y.; Yin, X. Microgrid stability: Classification and a review. *Renew. Sustain. Energy Rev.* **2016**, *58*, 167–179. [\[CrossRef\]](http://dx.doi.org/10.1016/j.rser.2015.12.201)
- 30. Coelho, E.A.A.; Cortizo, P.C.; Garcia, P.F.D. Small-signal stability for parallel-connected inverters in stand-alone AC supply systems. *IEEE Trans. Ind. Appl.* **2002**, *38*, 533–542. [\[CrossRef\]](http://dx.doi.org/10.1109/28.993176)
- 31. Rasheduzzaman, M.; Mueller, J.A.; Kimball, J.W. An accurate small-signal model of inverter-dominated islanded microgrids using dq reference frame. *IEEE J. Emerg. Sel. Top. Power Electron.* **2017**, *2*, 1070–1080. [\[CrossRef\]](http://dx.doi.org/10.1109/JESTPE.2014.2338131)
- 32. Ellabban, O.; Mierlo, J.V.; Lataire, P. A DSP-based dual-loop peak DC-link voltage control strategy of the Z-source inverter. *IEEE Trans. Power Electron.* **2012**, *27*, 4088–4097. [\[CrossRef\]](http://dx.doi.org/10.1109/TPEL.2012.2189588)

© 2018 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license [\(http://creativecommons.org/licenses/by/4.0/\)](http://creativecommons.org/licenses/by/4.0/.).