



# Article High-Efficiency Bidirectional LLC Resonant Converter with Primary Auxiliary Windings

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**Abstract:** In this paper, high-efficiency bidirectional LLC resonant converters with primary auxiliary windings in transformers of resonant circuits are proposed. Even though resonant capacitors are used on the primary and secondary sides, the proposed converter can operate, regardless of the direction of the power flow, with the high gain characteristics of the LLC resonant converter without the mutual coupling of resonant capacitors. The operation principles and gain characteristics of the proposed bidirectional DC–DC converters are described in detail. A 3.3 kW prototyped bidirectional LLC resonant converter for interfacing 750 V<sub>DC</sub> buses was built and tested to verify the effectiveness and applicability of this proposed converter.

Keywords: bidirectional converter; LLC resonant converter; CLLC resonant converter; DC-DC converter

## 1. Introduction

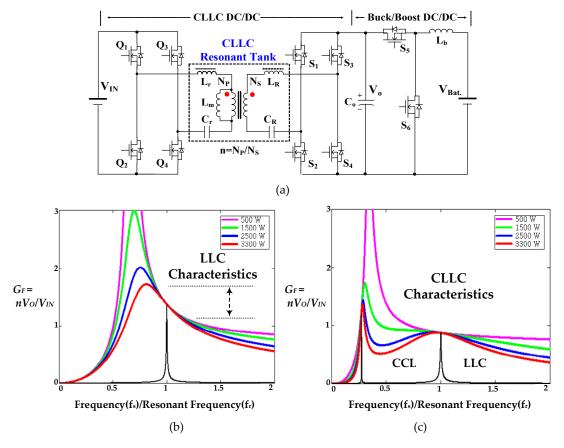
Voltage source-isolated or current source-isolated bidirectional DC–DC converters using a high-frequency transformer are generally used in energy storage systems for renewable energy sources and future electric vehicles [1–3]. To achieve a highly integrated power conversion circuit, the switching frequency should be increased. However, this has the drawback of hard switching, which can cause higher switching losses.

Recently, to minimize the size, switching losses, and Electromagnetic Interference (EMI) of a bidirectional DC–DC converter, CLLC resonant circuits with soft-switching characteristics, as shown in Figure 1a, were developed for the bidirectional DC–DC converter [4–7]. Due to the use of small resonant capacitors ( $C_r$ ,  $C_R$ ) in the primary and the secondary sides, the CLLC (CCL+LLC) shows gain characteristics as illustrated in Figure 1c, as compared to the high gain characteristics (at the frequency regions lower than the resonant frequency) of the conventional LLC resonant converter as illustrated in Figure 1b.

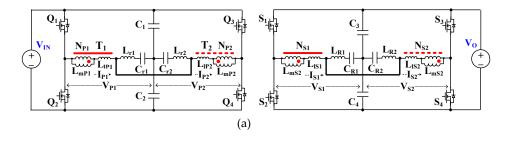
In heavy load conditions and frequency regions lower than the resonant frequency, the slope of the CLLC gain characteristics decreases, which means that zero voltage switching (ZVS) cannot be achieved. To increase the CLLC gain slope in frequency ranges below the resonant frequency, the transformer magnetization inductance (L<sub>m</sub>) must be significantly reduced, however, improving the efficiency is challenging because of the increase in conduction losses. To operate with the wide range of voltages in the bidirectional power transfer, a two-stage DC–DC converter (as shown in Figure 1a) composed of a hard-switched buck/boost converter for output voltage control and an unregulated LLC converter for electrical isolation has been used in various applications [7]. However, the two-stage bidirectional DC–DC converter not only causes high power losses but results in increased costs.

In this paper, bidirectional LLC resonant converters with a wide input and output voltage range are proposed, as shown in Figure 2 [8]. Compared to the operational characteristics of the conventional bidirectional CLLC resonant converter presented in Figure 1a, the proposed converters can be operated

with high gain characteristics without mutual coupling even though resonant capacitors are used on the primary and secondary sides. Therefore, without any additional buck/boost converter, the proposed bidirectional LLC resonant converter can be operated with high gain characteristics as a conventional LLC resonant converter, regardless of the direction of the power flow.



**Figure 1.** Two-stage bidirectional converter and gain characteristics: (**a**) Conventional two-stage bidirectional converter; (**b**) LLC gain characteristics; (**c**) CLLC gain characteristics.



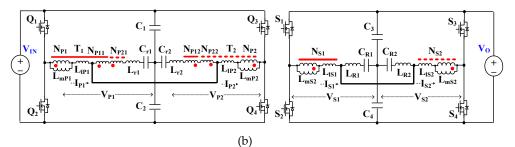
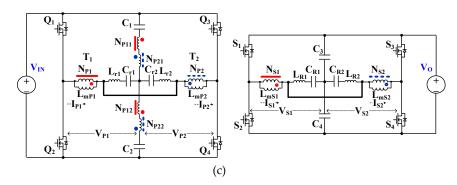


Figure 2. Cont.



**Figure 2.** Proposed bidirectional LLC resonant DC–DC converters: (a) Proposed converter 1; (b) Proposed converter 2; (c) Proposed converter 3.

The proposed bidirectional LLC resonant converter 1 (Figure 2a) can be controlled at a nominal voltage that is close to the resonant frequency in the forward operation. However, in the reverse operation, it operates in the high switching frequency range above the resonance frequency with the charged battery voltage. Therefore, to control the charging/discharging voltage range ( $V_o$ : 270  $V_{DC}$ –430  $V_{DC}$ ) of a battery at the fixed input voltage ( $V_{IN}$ : 750  $V_{DC}$ ), it is necessary to adjust the gain in the forward and reverse power transfer operations. For this purpose, we propose bidirectional LLC resonant converters with auxiliary windings at the primary side of transformers, as shown in Figure 2b,c. In this paper, a 3.3 kW prototype bidirectional LLC resonant converter (Figure 2c) was designed and tested to confirm the validity and applicability of the proposed converter.

#### 2. Proposed Bidirectional LLC Resonant Converter

The proposed bidirectional LLC resonant converter shown in Figure 2c has two independent resonant circuits comprised of two transformers (T<sub>1</sub>, T<sub>2</sub>) including the primary main windings (N<sub>P1</sub>, N<sub>P2</sub>) with auxiliary windings (N<sub>P11</sub>/N<sub>P12</sub>, N<sub>P21</sub>/N<sub>P22</sub>), and resonant components (C<sub>r1</sub>/C<sub>r2</sub>, C<sub>R1</sub>/C<sub>R2</sub> & L<sub>r1</sub>/L<sub>r2</sub>, L<sub>R1</sub>/L<sub>R2</sub>), with common lines and voltage-divided capacitors (C<sub>1</sub>/C<sub>2</sub>, C<sub>3</sub>/C<sub>4</sub>) on the primary and secondary side. Even though resonant capacitors (C<sub>r1</sub>/C<sub>r2</sub>, C<sub>R1</sub>/C<sub>R2</sub>) are used on the primary and secondary sides, the proposed converters can be operated with the high gain characteristics of LLC resonant converters without mutual coupling. Depending on the status (on/off) of the switches (Q<sub>1</sub>-Q<sub>4</sub>/S<sub>1</sub>-S<sub>4</sub>) in the forward and reverse operation mode, the four modes that operate in the discontinuous mode below resonant frequency (f<sub>r</sub>) are described below.

#### 2.1. Forward Operation Mode

In the forward operation mode, as shown in Figure 3a,b,  $Q_1/Q_3$  and  $Q_2/Q_4$  are simultaneously turned on and off with a 50% duty cycle. The anti-parallel diodes of the secondary switches ( $S_1/S_4$ ,  $S_2/S_3$ ) are operated as rectifier diodes since secondary switches ( $S_1$ ,  $S_2$ ,  $S_3$ ,  $S_4$ ) are turned off. During the time interval  $t_0$ - $t_1$ , when the primary switches ( $Q_1/Q_3$ ) are turned on with ZVS, half of the input voltage ( $V_{IN}$ ) is applied to the resonant circuits including the transformer primary main windings ( $N_{P1}$ ,  $N_{P2}$ ) and auxiliary windings ( $N_{P11}$ - $N_{P21}$ ,  $N_{P12}$ - $N_{P22}$ ), the resonant inductors ( $L_{r1}$ ,  $L_{r2}$ ) and capacitors ( $C_{r1}$ ,  $C_{r2}$ ). Moreover, the voltages applied to the primary main windings and auxiliary windings of each transformer ( $T_1$ ,  $T_2$ ), are transferred to the transformer secondary windings ( $N_{S1}$ ,  $N_{S2}$ ) by the turn-ratio ( $n_F$ ) of each transformer. As shown in Figure 3c, the turn-ratio ( $n_F$ ) is set to adjust the charging voltage and the frequency control range. Here, the turn-ratio is the ratio of the transformer primary winding ( $N_{PF}$ ) to the secondary winding ( $N_S$ ) in the forward power transfer operation. At this time, the primary resonant currents  $I_{P1}(I_{P2})$  are flowing with the following paths: the voltage divided capacitor ( $C_1$ )  $\rightarrow Q_1(Q_3) \rightarrow$  primary main windings  $N_{P1}(N_{P2}) \rightarrow$  the resonant inductors  $L_{r1}(L_{r2})$  and capacitors  $C_{r1}(C_{r2}) \rightarrow$  the auxiliary windings  $N_{P1}-N_{P21} \rightarrow C_1$ , respectively. Furthermore, the primary resonant currents  $I_{P1}(I_{P2})$  are flowing through paths of the input voltage

 $(V_{IN}) \rightarrow Q_1(Q_3) \rightarrow primary main windings N_{P1}(N_{P2}) \rightarrow the resonant inductors L_{r1}(L_{r2}) and capacitors C_{r1}(C_{r2}) \rightarrow the auxiliary windings N_{P12}-N_{P22} \rightarrow the voltage divided capacitor (C_2), and back to the input voltage (V_{IN}), respectively. If there is a difference in the resonant current (I_{P1}, I_{P2}) flowing in each resonant circuit, the current flows through the primary common connection line by the voltage difference charged in the resonant capacitors (C_{r1}, C_{r2}) to suppress the resonant current unbalance. Due to the voltage polarity of secondary windings (N_{S1}/N_{S2}) in transformers (T_1, T_2), the sum voltage (V_{S1}+V_{S2}) of the secondary windings is transferred to the output side.$ 

Furthermore, the secondary resonant currents  $(I_{S1}, I_{S2})$  do not flow through the secondary resonant capacitors (C<sub>R1</sub>, C<sub>R2</sub>), but flow through the secondary common connection line and anti-parallel diodes of the secondary switching devices  $(S_2/S_3, S_1/S_4)$ . Therefore, even when resonant capacitors are used on the primary and secondary sides, the proposed converter can operate with the high gain characteristics of the LLC resonant converter without mutual coupling. In the interval  $t_1-t_2$ , the primary switches  $(Q_1/Q_3)$  are kept turned on, which may look similar to the operation mode of the time interval  $t_0-t_1$ . However, interval  $t_1-t_2$  is where the resonant state terminates, and only the primary magnetizing currents (I<sub>Pm1</sub>, I<sub>Pm2</sub>) flow through the magnetizing inductance (L<sub>mP1</sub>, L<sub>mP2</sub>) of the transformers (T<sub>1</sub>,  $T_2$ ). When the primary switches ( $Q_1/Q_3$ ) are turned off at time  $t_2$ , due to the magnetizing current of the transformers (T<sub>1</sub>, T<sub>2</sub>), the output parasitic capacitance of Q<sub>1</sub>/Q<sub>3</sub> and Q<sub>2</sub>/Q<sub>4</sub> are charged and discharged to the input voltage ( $V_{IN}$ ) and zero voltage during the dead time ( $t_2-t_3$ ), respectively. At this point, the primary and secondary resonant currents ( $I_{P1}/I_{P2}$ ,  $I_{S1}/I_{S2}$ ) start to flow because of the change in voltage polarity of the transformers ( $T_1$ ,  $T_2$ ). After that, if the primary switches ( $Q_2/Q_4$ ) are turned on when the current is flowing in their anti-parallel diodes,  $Q_2$  and  $Q_4$  are operated with ZVS. Since the switching operation in the half cycle operation interval  $(t_3-t_6)$  is repeated, it is not described in this paper.

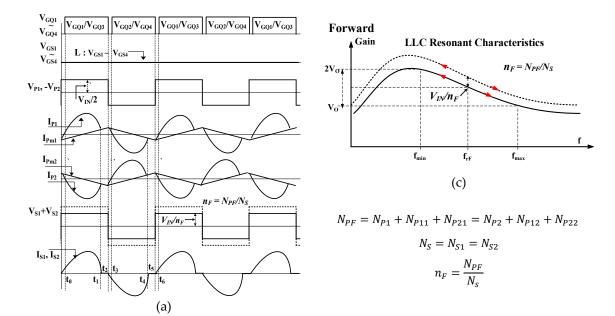
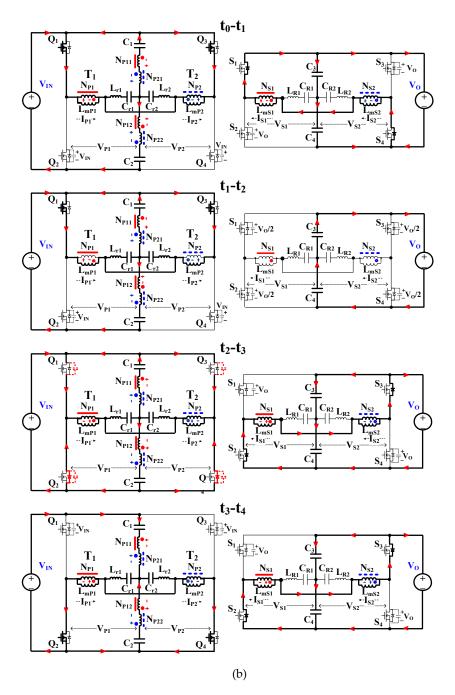


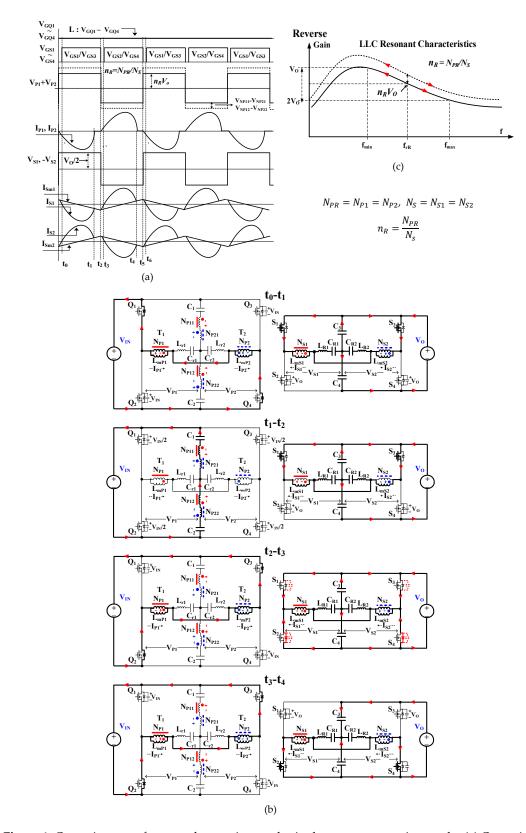
Figure 3. Cont.



**Figure 3.** Operating waveforms and operating modes in the forward operation mode: (**a**) Operating waveforms; (**b**) Operating modes; (**c**) Gain characteristics considering the turn-ratio ( $n_F$ ).

#### 2.2. Reverse Operation Mode

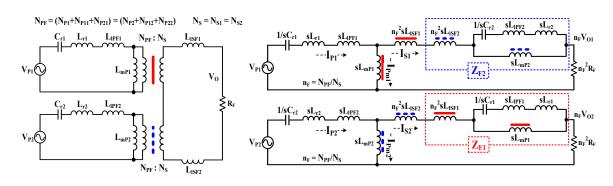
The reverse operation mode is shown in Figure 4a,b. The secondary switches  $(S_1/S_3 \text{ and } S_2/S_4)$ are simultaneously turned on and off with a 50% duty cycle. The anti-parallel diodes of the primary switches  $(Q_1/Q_3, Q_2/Q_4)$  are operated as rectifier diodes since the primary switches  $(Q_1, Q_2, Q_3, Q_4)$ are turned off. During the time interval  $t_0-t_1$ , when the secondary switches  $(S_1/S_3)$  are turned on with ZVS, half of the output voltage  $(V_0)$  is applied to each secondary resonant circuits, and in the reverse operation mode, as in the forward operation mode, the secondary resonant currents  $I_{S1}(I_{S2})$ flow through the paths of the voltage divided capacitor  $(C_3) \rightarrow S_1(S_3) \rightarrow$  secondary main windings  $N_{S1}(N_{S2}) \rightarrow$  the resonant inductors  $L_{R1}(L_{R2})$  and capacitors  $C_{R1}(C_{R2})$ , and back to the voltage divided capacitor ( $C_3$ ), respectively. Furthermore, the secondary resonant currents  $I_{S1}(I_{S2})$  flow through the paths of the output voltage  $(V_0) \rightarrow S_1(S_3) \rightarrow$  secondary windings  $N_{S1}(N_{S2}) \rightarrow$  the resonant inductors  $L_{R1}(L_{R2})$  and capacitors  $C_{R1}(C_{R2}) \rightarrow$  the voltage divided capacitor (C<sub>4</sub>), and back to the output voltage  $(V_O)$ , respectively. If there is a difference in the resonant current  $(I_{S1}, I_{S2})$  flowing in each secondary resonant circuit, the current flows through the secondary common connection line by the voltage difference charged in the resonant capacitors ( $C_{R1}$ ,  $C_{R2}$ ) to suppress the imbalance of the secondary resonant currents ( $I_{S1}$ ,  $I_{S2}$ ). At this point, the primary polarity of transformers ( $T_1$ ,  $T_2$ ) is changed by the secondary voltage applied to the secondary windings (N<sub>S1</sub>, N<sub>S2</sub>) of transformers, and the sum voltage  $(V_{P1} + V_{P2})$  of the primary windings  $(N_{P1}, N_{P2})$  is transferred to the input side  $(V_{IN})$ . As a result, the sum voltage of the auxiliary windings (NP11-NP21, NP12-NP22) connected to the primary resonance circuits is zero, which means that the primary resonant currents  $(I_{P1}, I_{P2})$  do not flow through the primary resonant capacitors ( $C_{r1}$ ,  $C_{r2}$ ), but flow through the primary common connection line and anti-parallel diodes of the primary switching devises ( $Q_2/Q_3$ ,  $Q_1/Q_4$ ). Thus, in reverse operation mode, high LLC gain characteristics can be obtained without mutual coupling even though resonant capacitors ( $C_{r1}/C_{r2}$ ,  $C_{R1}/C_{R2}$ ) are used on the primary and secondary sides. Also, by using the primary auxiliary windings (NP11-NP21, NP12-NP22) of transformers in the resonant circuits, the transferred voltage to the primary is lowered by the turn-ratio (n<sub>R</sub>: N<sub>P1</sub>/N<sub>S1</sub>, N<sub>P2</sub>/N<sub>S2</sub>) during the reverse power transfer operation. This can easily control the gain voltage range according to the battery charging and discharging voltage in the forward and reverse power transfer operation. In the interval  $t_1-t_2$ , the resonant state ends, and only the secondary magnetizing currents (I<sub>Sm1</sub>, I<sub>Sm2</sub>) flow through the magnetizing inductance ( $L_{mS1}$ ,  $L_{mS2}$ ) of the transformers ( $T_1$ ,  $T_2$ ). When the secondary switches ( $S_1/S_3$ ) are turned off at time  $t_2$ , due to the secondary magnetizing currents of the transformers ( $T_1$ ,  $T_2$ ), the output parasitic capacitance of  $S_1/S_3$  and  $S_2/S_4$  are charged and discharged to the output voltage  $(V_{O})$  and zero voltage, respectively, during the dead time  $(t_2-t_3)$ . During the dead time  $t_2-t_3$ , if the secondary switches  $(S_2/S_4)$  are turned on when the current is flowing in their anti-parallel diodes,  $S_2$ and S<sub>4</sub> are operated with zero voltage switching.

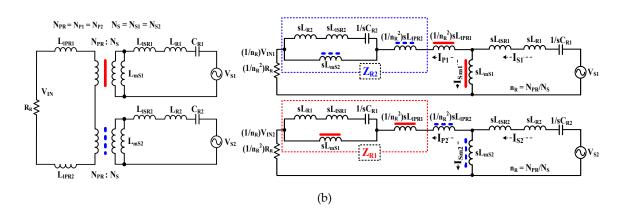


**Figure 4.** Operating waveforms and operating modes in the reverse operation mode: (**a**) Operating waveforms; (**b**) Operating modes; (**c**) Gain characteristics considering the turn-ratio ( $n_R$ ).

#### 2.3. Equivalent Circuits of the Proposed Converter

In this section, voltage gain characteristics for both forward and reverse operation modes are discussed. To analyze the forward and reverse voltage gain characteristics, the converter can be simplified as T-shaped equivalent circuits since the proposed bidirectional LLC converter operates with the high gain characteristics of a conventional LLC resonant converter without the mutual coupling of resonant capacitors. Also, as the proposed bidirectional LLC resonant converter is operated by two resonant circuits in the forward and reverse operation modes, the converter's gain characteristics can be obtained by the superposition principle considering the individual voltage sources ( $V_{P1}/V_{P2}$ ,  $V_{S1}/V_{S2}$ ) as shown in Figure 5a,b.





(a)

**Figure 5.** Equivalent circuits considering the individual voltage sources  $(V_{P1}/V_{P2}, V_{S1}/V_{S2})$ : (a) Equivalent circuit in the forward operation mode; (b) Equivalent circuit in the reverse operation mode.

The converter's voltage gain equations (G<sub>F</sub>, G<sub>R</sub>) expressed by the turn-ratio ( $n_F = \frac{N_{PF}}{N_s}$ ,  $n_R = \frac{N_{PR}}{N_s}$ ) and the parameters of transformers are shown as the sum of individual voltage gains (G<sub>F1</sub> and G<sub>F2</sub>, G<sub>R1</sub> and G<sub>R2</sub>) in the forward and reverse operation mode. Figure 5a shows the equivalent circuit considering the individual primary voltage sources (V<sub>P1</sub>, V<sub>P2</sub>) in the forward operating mode. The voltage gain characteristics (G<sub>F1</sub>) of the primary voltage source 1 (V<sub>P1</sub>) and load voltage ( $n_FV_{O1}$ ) can be shown as Equation (1). Also, the voltage gain characteristics (G<sub>F2</sub>) of the primary voltage source 2 (V<sub>P2</sub>) and load voltage ( $n_FV_{O2}$ ) can be shown as Equation (2). Therefore, the final voltage gain (G<sub>F</sub>) in the forward operation mode of the proposed converter is the sum of Equation (1) and Equation (2), as shown in Equation (3). In the forward operation mode, as shown in the equivalent circuits of Figure 5a, the equations related to the individual primary resonant impedances (Z<sub>F1</sub>, Z<sub>F2</sub>), and transformer parameters are shown below. Here, L<sub>mP1</sub>/L<sub>mP2</sub> are the primary magnetizing inductance and L<sub>lPF1</sub>/L<sub>lPF2</sub>,  $L_{ISF1}/L_{ISF2}$  are the primary and secondary leakage inductance, respectively, in the forward operation mode, and  $L_{eqF1}/L_{eqF2}$  are the equivalent leakage inductance.

$$G_{F1} = \frac{n_F V_{O1}}{V_{P1}} = \frac{1}{2} \left[ \frac{n_F^2 R_F \frac{s L_{mP1} C_{r1}}{L_{mP1} + n_F^2 L_{lSF1}}}{\frac{n_F^2 R_F + Z_{F2}}{s(L_{mP1} + n_F^2 L_{lSF1})} \{1 + s^2 C_{r1} (L_{mP1} + L_{lPF1} + L_{r1})\} + (1 + s^2 C_{r1} L_{eqF1})} \right]$$
(1)

$$G_{F2} = \frac{n_F V_{O2}}{V_{P2}} = \frac{1}{2} \left[ \frac{n_F^2 R_F + Z_{F1}}{\frac{n_F^2 R_F + Z_{F1}}{s(L_{mP2} + n_F^2 L_{lSF2})}} \{1 + s^2 C_{r2} (L_{mP2} + L_{lPF2} + L_{r2})\} + (1 + s^2 C_{r2} L_{eqF2})} \right]$$
(2)

$$G_F = G_{F1} + G_{F2} = \frac{n_F V_o}{V_{IN}}$$
(3)

where  $Z_{F2} = s(L_{mP2} + n_F^2 L_{lSF2}) \frac{1 + s^2 C_{r2} L_{eqF2}}{1 + s^2 C_{r2} (L_{mP2} + L_{lPF2} + L_{r2})}; Z_{F1} = s(L_{mP1} + n_F^2 L_{lSF1}) \frac{1 + s^2 C_{r1} L_{eqF1}}{1 + s^2 C_{r1} (L_{mP1} + L_{lPF1} + L_{r1})};$  $N_{PF} = N_{P1} + N_{P11} + N_{P21} = N_{P2} + N_{P12} + N_{P22}, N_S = N_{S1} = N_{S2}; n_F = \frac{N_{PF}}{N_S}; L_{eqF1} = (L_{lPF1} + L_{r1}) + L_{mP1} / n_F^2 L_{lSF1}; L_{eqF2} = (L_{lPF2} + L_{r2}) + L_{mP2} / n_F^2 L_{lSF2};$ 

Furthermore, the equivalent circuits considering the individual secondary voltage sources ( $V_{S1}$ ,  $V_{S2}$ ) in the reverse operation mode can be shown in Figure 5b. Moreover, the voltage gain characteristics ( $G_{R1}$ ,  $G_{R2}$ ) of the secondary voltage sources ( $V_{S1}$ ,  $V_{S2}$ ) and primary voltages ( $(1/n_R)V_{IN1}$ ,  $(1/n_R)V_{IN2}$ ) can be found with Equation (4) and Equation (5). Therefore, the final voltage gain ( $G_R$ ) in the reverse operation mode of the proposed converter is the sum of Equation (4) and Equation (5), as shown in Equation (6). Here,  $L_{mS1}/L_{mS2}$  and  $L_{ISR1}/L_{ISR2}$  are the secondary magnetizing inductance and leakage inductance, and  $L_{IPR1}/L_{IPR2}$  and  $L_{eqR1}/L_{eqR2}$  are the primary leakage inductance and the equivalent leakage inductance in the reverse operation mode.

$$G_{R1} = \frac{V_{IN1}}{n_R V_{S1}} = \frac{1}{2} \left[ \frac{\left(1/n_R^2\right) R_R \frac{sL_{mS1}C_{R1}}{L_{mS1} + (1/n_R^2)L_{IPR1}}}{\frac{(1/n_R^2)R_R + Z_{R2}}{s(L_{mS1} + (1/n_R^2)L_{IPR1})} \{1 + s^2 C_{R1}(L_{mS1} + L_{ISR1} + L_{R1})\} + \left(1 + s^2 C_{R1}L_{eqR1}\right)} \right]$$
(4)

$$G_{R2} = \frac{V_{IN2}}{n_R V_{S2}} = \frac{1}{2} \left[ \frac{\left(1/n_R^2\right) R_R \frac{sL_{mS2}C_{R2}}{L_{mS2} + (1/n_R^2)L_{lPR2}}}{\frac{(1/n_R^2) R_R + Z_{R1}}{s(L_{mS2} + (1/n_R^2)L_{lPR2})} \{1 + s^2 C_{R2}(L_{mS2} + L_{lSR2} + L_{R2})\} + \left(1 + s^2 C_{R2}L_{eqR2}\right)} \right]$$
(5)

$$G_R = G_{R1} + G_{R2} = \frac{V_{IN}}{n_R V_o}$$
(6)

where  $Z_{R2} = s(L_{mS2} + (1/n_R^2)L_{lPR2}) \frac{1+s^2C_{R2}L_{eqR2}}{1+s^2C_{R2}(L_{mS2}+L_{lSR2}+L_{R2})}; Z_{R1} = s(L_{mS1} + (1/n_R^2)L_{lPR1}) \frac{1+s^2C_{R1}L_{eqR1}}{1+s^2C_{R1}(L_{mS1}+L_{lSR1}+L_{R1})}; Z_{R1} = s(L_{mS1} + (1/n_R^2)L_{lPR1}) \frac{1+s^2C_{R1}L_{eqR1}}{1+s^2C_{R1}(L_{mS1}+L_{lSR1}+L_{R1})}; N_{PR} = N_{P1} = N_{P2}; N_S = N_{S1} = N_{S2}; n_R = \frac{N_{PR}}{N_S}; L_{eqR1} = (L_{lSR1} + L_{R1}) + \frac{L_{mS1}}{(1/n_R^2)L_{lPR1}}; L_{eqR2} = (L_{lSR2} + L_{R2}) + \frac{L_{mS2}}{(1/n_R^2)}L_{lPR2}.$ 

Equation (7) and Equation (8) show the corner frequency ( $f_{oF}$ ,  $f_{oR}$ ) and resonant frequency ( $f_{rF}$ ,  $f_{rR}$ ) in the forward and reverse operation mode, respectively.

$$f_{oF} = \frac{1}{2\pi\sqrt{C_{r1}(L_{mP1} + L_{lPF1} + L_{r1})}} = \frac{1}{2\pi\sqrt{C_{r2}(L_{mP2} + L_{lPF2} + L_{r2})}}, \quad f_{rF} = \frac{1}{2\pi\sqrt{C_{r1}L_{eqF1}}} = \frac{1}{2\pi\sqrt{C_{r2}L_{eqF2}}}$$
(7)

$$f_{oR} = \frac{1}{2\pi \sqrt{C_{R1}(L_{mS1} + L_{lSR1} + L_{R1})}} = \frac{1}{2\pi \sqrt{C_{R2}(L_{mS2} + L_{lSR2} + L_{R2})}}, \ f_{rR} = \frac{1}{2\pi \sqrt{C_{R1}L_{eqR1}}} = \frac{1}{2\pi \sqrt{C_{R2}L_{eqR2}}}$$
(8)

In the voltage gain characteristics ( $G_F$ ,  $G_R$ ) shown in Figures 6a and 7a, the corner frequency ( $f_{oF}$ ,  $f_{oR}$ ) represents the frequency when the load in the forward and reverse operation mode are open ( $n_F^2 R_F = (1/n_R^2) R_R = \infty$ ). The  $f_{rF}$  and  $f_{rR}$  are the resonant frequency when the load in the forward and reverse operation mode are shorted ( $n_F^2 R_F = (1/n_R^2) R_R = 0$ ). The peaking at corner frequency ( $f_{oF}$ ,  $f_{oF}$ )

 $f_{oR}$ ) is generated due to the different values in the inductance of transformers (T<sub>1</sub>, T<sub>2</sub>). This peak will disappear when each transformer has the same inductance parameters.

To improve the gain characteristics of the forward and reverse operation based on voltage gain equations ( $G_F$ ,  $G_R$ ), the switching frequency and the transformer's turn-ratio at the nominal voltage conditions of the battery must be set to operate in the vicinity of the resonant frequency ( $f_{rF}$ ,  $f_{rR}$ ). In this condition, primary auxiliary windings ( $N_{P11}/N_{P12}$ ,  $N_{P21}/N_{P22}$ ) used to adjust the gain characteristics have a very important role in achieving high voltage gain characteristics for the whole load range variation in both forward operation mode and reverse operation mode.

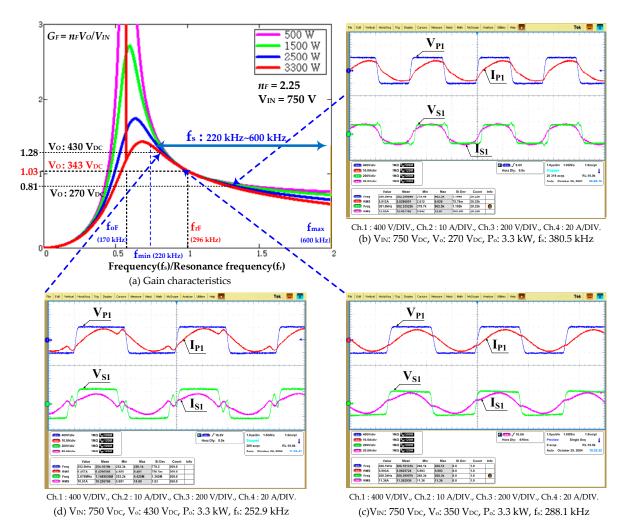


Figure 6. Experimental waveforms and voltage gain characteristics in the forward operation mode.

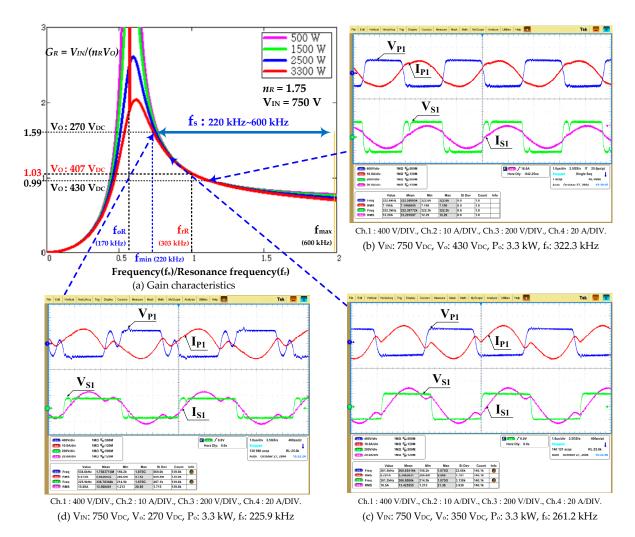


Figure 7. Experimental waveforms and voltage gain characteristics in the reverse operation mode.

## 3. Experimental Results

In this paper, a 3.3 kW prototyped LLC resonant converter for bidirectional power conversion with a 750  $V_{DC}$  input voltage and an output voltage range of 270–430  $V_{DC}$  was built and tested to verify the validity of the proposed converter. The experimental conditions and specifications are shown in Table 1. Note that T represents the number of turns.

Figures 6 and 7 show the results of our experiment, describing the waveforms of each circuit component in the forward and reverse operation mode, respectively. The experimental waveforms of the primary terminal voltage/current ( $V_{P1}$ ,  $I_{P1}$ ) and the secondary terminal voltage/current ( $V_{S1}$ ,  $I_{S1}$ ) are given for a capacity of 3.3 kW with an input voltage (750  $V_{DC}$ ) and output voltage (270  $V_{DC}$ /350  $V_{DC}$ /430  $V_{DC}$ ), in the forward and reverse operation, respectively.

The results of the experiment and simulation (Math-Cad) in both the forward and reverse operations confirmed that the proposed bidirectional LLC resonant converter for wide output voltage control (270–430  $V_{DC}$ ) operates with LLC resonant gain characteristics in the frequency control range of 220 kHz to 600 kHz. Therefore, we proved that the proposed bidirectional LLC resonant converter can operate with the same high gain characteristics as a conventional LLC resonant converter without the mutual coupling of resonant capacitors.

Specification/Parameters	Values
Input voltage (V <sub>IN</sub> )	750 V <sub>DC</sub>
Output voltage $(V_{IN})$	270 V <sub>DC</sub> -430 V <sub>DC</sub> /3.3 kW
Switching Devices (Q <sub>1</sub> –Q <sub>4</sub> )	UJ3C120040K3S(1200 V, 65 A, R <sub>DS</sub> : 35 mΩ, SiC)
Switching Devices $(S_1-S_4)$	UJ3C065030K3S(650 V, 85 A, R <sub>DS</sub> : 27 mΩ, SiC)
Resonant Capacitors [(C <sub>r1</sub> ,C <sub>r2</sub> )/C <sub>R1</sub> ,C <sub>R2</sub> )] Resonant Inductors [(L <sub>r1</sub> ,L <sub>r2</sub> )/L <sub>R1</sub> ,L <sub>R2</sub> )]	10.5 nF/56 nF 22.1 uH/4 uH
Resonant Frequency [f <sub>rF</sub> /f <sub>rR</sub> : Forward/Reverse] Switching Frequency Range (f <sub>s</sub> )	296.3 kHz/303.7 kHz 220 kHz–600 kHz
Forward ope	eration mode
Primary self-inductance [T <sub>1</sub> /T <sub>2</sub> : L <sub>lPF1</sub> + L <sub>mP1</sub> /L <sub>lPF2</sub> + L <sub>mP2</sub> ]	61.4 uH/61.1 uH
Secondary self-inductance $[T_1/T_2: L_{ISF1} + (1/n_F^2)L_{mP1}/L_{ISF2} + (1/n_F^2)L_{mP2}]$	11.73 uH/11.65 uH
Primary magnetizing Inductance [T <sub>1</sub> /T <sub>2</sub> : L <sub>mP1</sub> /L <sub>mP2</sub> ]	57.65 uH/57.28 uH
Turn-ratio $[N_{PF}/N_S = n_F]$	2.25 [18 T(14 T + 2 T + 2 T)/8 T]
Reverse ope	ration mode
Primary self-inductance $[T_1/T_2:L_{IPR1} + n_R^2 L_{mS1}/L_{IPR2} + n_R^2 L_{mS2}]$	35.06 uH/35.28 uH
Secondary self-inductance [T <sub>1</sub> /T <sub>2</sub> : L <sub>ISR1</sub> +L <sub>mS1</sub> /L <sub>ISR2</sub> + L <sub>mS2</sub> ]	11.73 uH/11.65 uH
Secondary magnetizing Inductance [T <sub>1</sub> /T <sub>2</sub> : L <sub>mS1</sub> /L <sub>mS2</sub> ]	11.04 uH/11.13 uH
Turn-ratio $[N_{PR}/N_S = n_R]$	1.75 [14 T/8 T]

Table 1. Major ratings and parameters of the proposed converter.

Figure 8a,b show the efficiency characteristics of the proposed bidirectional LLC resonant converter in the forward and reverse operation modes, respectively. In the forward operation mode, as shown in Figure 8a, the efficiency at maximum power (3.3 kW) with an input voltage of 750 V<sub>DC</sub> and output voltage of 350 V<sub>DC</sub> was 98.48%, and the maximum efficiency was 98.75% at an input voltage of 350 V<sub>DC</sub> and power capacity of 2.5 kW because the switching operation was close to the resonant frequency ( $f_{rF}$ : 296 kHz). In the reverse operation mode, the maximum efficiency with an input voltage of 750 V<sub>DC</sub> and output voltage of 350 V<sub>DC</sub>, 2.5 kW was 97.78%, as shown in Figure 8b.

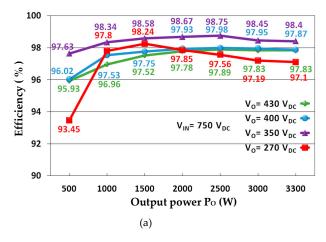
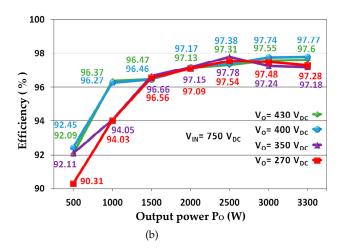


Figure 8. Cont.



**Figure 8.** Efficiency characteristics in forward and reverse operating conditions: (**a**) Forward operation mode; (**b**) Reverse operation mode.

The experimental setup for the laboratory prototype 3.3 kW bidirectional LLC resonant converter is shown in Figure 9.

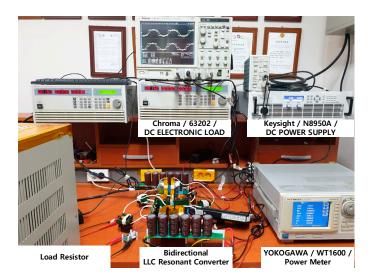


Figure 9. Photograph of the converter experiment.

#### 4. Discussion

A bidirectional DC–DC converter with high power density and efficiency has been proposed for on-board chargers (OBC) for EVs and as a DC micro-grid for an electrical storage system. As shown in Figure 1, the CLLC resonant converter has recently been developed for the electric vehicle OBC, but to improve the gain characteristics below the resonant frequency is challenging, as mentioned above. To overcome these problems, a topology comprised of a Power Factor Correction (PFC) AC–DC converter operating with variable DC-link voltage and a CLLC resonant DC–DC converter operating with fixed switching frequency is considered as key for various applications [4]. However, PFC AC–DC converters are hard-switching, which limits the switching frequency for integration and increases the voltage rating of switching devices and DC link capacitors according to the increased DC link voltage.

To overcome these limitations, we show that the proposed bidirectional LLC resonant converter could be implemented with a wide output voltage range.

## 5. Conclusions

In this paper, a simple scheme for a bidirectional LLC resonant DC–DC converter using the primary auxiliary windings and two resonant circuits was proposed, and this shows the LLC resonant characteristics for both forward and reverse directional operations. Experiments with a fabricated 3.3 kW prototype were conducted to evaluate the proposed bidirectional LLC resonant converter. The experimental results show that the proposed topology is a viable solution for the design of bidirectional DC–DC converters.

## 6. Patents

E.S Kim. Bidirectional LLC Resonant Converter. Patent-pending (No: 10-2019-0011426), South Korea, 2019.1.29.

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Conflicts of Interest: The authors declare no conflict of interest.

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