

Article

The Integrated Energy Consumption Index for Energy Biomass Grinding Technology Assessment

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Abstract: The assessment of engineering objects in terms of energy consumption is an important part of sustainable development. Many materials, including those from the energy sector, need to undergo earlier processing, e.g., grinding. Grinding processes still demand a significant amount of energy, whereas current energy assessment methods do not take into account important parameters of the process, which makes it difficult to choose their optimal values. The study presents the analysis, testing, and assessment of mechanical engineering systems in terms of the energy consumption involved in the grinding of biomass intended for energy production purposes. A testing methodology was developed to improve the parameters of multi-disc grinding, including the reduction of energy consumption, power input, product quality improvement, and process efficiency. An original model of integrated energy consumption was developed. Tests were carried out on a five-disc grinder for five programs to assess the programmable angular speeds of the grinder discs. Output values, including specific energy demand, fragmentation degree, and integrated energy consumption, were assigned to each testing program. The test results were subjected to statistical analysis. Based on the authors' own research, it was found that the angular speed of the discs and, consequently, the linear speed of the grinding blades, have a significant influence on the values of the integrated energy consumption of the preliminary process.

Keywords: energy consumption; comminution; grinding; multi-disc mill; energy consumption index; energy assessment

1. Introduction

The simplest and the most common method of biomass utilization is its combustion, e.g., in the boilers of a power station [\[1\]](#page-22-0). There are also other forms of energy production that are increasing in popularity, including: gasification, biomethane production, esterification, the acquisition of bioethanol, etc. [\[2,](#page-22-1)[3\]](#page-22-2). Depending on the energy purpose and type of biomass, the comminution process will vary—in particular, in terms of the desired final dimension of the comminution product [\[4,](#page-22-3)[5\]](#page-22-4). In the case of anaerobic digestion, biomass is comminuted to several millimeter fractions [\[4\]](#page-22-3). Pellets are usually made of fibrous biomass ground to 2–4 mm or smaller, depending on the briquetting machine design, while briquettes, from particles smaller than 10 mm [\[6\]](#page-22-5). In the production of biofuels, in turn, biomass particles should be in the range of 100–500 µm, and for gasification and direct combustion processes, below 100 μ m [\[4\]](#page-22-3). Previous research has shown that the smaller the biomass particles are used for energy purposes, the greater the efficiency and easier control of biomass thermochemical transformation processes [\[5\]](#page-22-4).

Acquiring energy from biomass requires its earlier preparation: drying, grinding, palletizing, etc. [\[7\]](#page-22-6). These procedures require certain energy inputs (costs) which significantly decrease the energy and environmental balance in the entire lifecycle of the energy material (wood, grain biomass, etc.) [\[8–](#page-22-7)[13\]](#page-23-0). According to the idea of sustainable development concerning the design of systems, devices, and processes, in three areas—the environment, society, and economy—the biomass processing lines should be characterized by the lowest possible energy consumption and environmental impact [\[14](#page-23-1)[,15\]](#page-23-2). It also aims to improve the competitiveness of biomass fuels in relation to conventional fossil fuels [\[16,](#page-23-3)[17\]](#page-23-4).

Before being used for energy purposes, energy media need to be properly prepared, e.g., their dimensions need to be reduced by means of grinding [\[2\]](#page-22-1). Roller, drum, ball, hammer, and disc mills are used to grind granular biomaterials (biomass grains) [\[7](#page-22-6)[,18\]](#page-23-5). Tests have shown that the best relations between product quality, yield, and grinding energy consumption occur for hammer and disc mills [\[2,](#page-22-1)[7\]](#page-22-6). The quality of the grinding product is most often determined by the grinding degree, which is defined as the ratio of the characteristic dimensions of the particles before and after size reduction [\[19,](#page-23-6)[20\]](#page-23-7). Other indicators, e.g., bulk density, grain size distribution, specific surface area, energy value, and their relationship with the comminution process, are also important from the point of view of the final product quality [\[4](#page-22-3)[,21](#page-23-8)[–24\]](#page-23-9). Previous studies conducted by other researchers have shown that the reduction of biomass particles' sizes result in improved flowability and movement properties; the material moves better, e.g., on feeders [\[25\]](#page-23-10). Grinding processes also increase the bulk density of the product, which allows, among others, to reduce storage space [\[5\]](#page-22-4). In the case of biomass, there was also a trend of increasing energy demand along with an increase in the particle size of the grinding input material [\[26\]](#page-23-11). It has also been shown that the energy demand increases as the particle size of the comminution product decreases; i.e., the smaller the particles we want to achieve, the greater the energy input [\[5,](#page-22-4)[27\]](#page-23-12). The conducted analyzes have shown that the smaller the particles after comminution, the easier they are conducted; e.g., anaerobic digestion processes and the efficiency of biomass conversion into biofuels increases, due to the increase in the specific surface area of the particles in grinding processes [\[4](#page-22-3)[,28](#page-23-13)[,29\]](#page-23-14).

Current legislation imposes requirements which are supposed to reduce the energy consumption of technological lines, including energy material grinding. Unfortunately, currently used grinding machines and devices consume much energy and are inefficient [\[2,](#page-22-1)[30](#page-23-15)[–32\]](#page-23-16), which motivates researchers to take up research in order to reduce the energy consumption of grinders and mills. Thus, upon implementing innovative structural solutions, a multi-criteria analysis needs to be used. It should take into consideration such parameters as efficiency, energy consumption, fragmentation degree, and power consumption. The design of structural solutions should meet the criteria of sustainable development. Criteria to be used for the structure assessment should be matched in such a way that the choice of an optimal solution is possible.

Biomaterial grinding (e.g., granular biomass) is accompanied by many phenomena caused by the impact of the material, the machine elements, the internal structure of biomaterials, and their strength parameters [\[33\]](#page-23-17). Strength properties vary depending on the material and depend on, among others, internal structure, humidity, and biological features [\[34\]](#page-23-18), and in the case of biomass, a significant diversification of properties is observed even within one species [\[35–](#page-23-19)[37\]](#page-24-0). The increases in strength and hardness increase the energy demand for fragmentation [\[38–](#page-24-1)[40\]](#page-24-2). The increase in the humidity of the input material also contributes to the increase in energy demand during the size reduction process. The internal structure of biomass grains is not without significance—materials with greater glassiness are characterized by increased energy demands in size reduction processes; however, the fragmentation efficiency is greater, resulting in smaller particles [\[36,](#page-23-20)[38,](#page-24-1)[41,](#page-24-3)[42\]](#page-24-4). Wiercioch et al. [\[35\]](#page-23-19) showed proportionality of the grinding energy demand and mass of material. Other studies, conducted for single grains, have shown that the amount of grinding energy demand increases as grain thickness increases [\[37\]](#page-24-0). Thus, the criteria for the assessment of the structure and process need to be formulated. They must be adjusted both to the material and the grinding machine, as well as to the specificity of

the company. Hence, the identification of variables and factors affecting the process assessment in terms of energy consumption, efficiency, and product quality seems to be of key importance [\[7](#page-22-6)[,31\]](#page-23-21).

Research on energy-related aspects involved in grinding has been ongoing since the end of the 20th century. Since that time, many theories link energy consumption with product quality and the efficiency of the grinding process. These include the hypotheses of Rittinger, Kick, Holmes, Charles, Rebinder, Mielnikow, and Bond, as well as the statistical hypothesis. They, however, are based on certain simplifications regarding the similarity of particles and the failure to consider the forces of grinding. In addition, there are restrictions involved in their applicability [\[30](#page-23-15)[,43–](#page-24-5)[46\]](#page-24-6). Polish experiences in research on energy consumption include experiments conducted by: J. Flizikowski, Malewski, Tomporowski, Zawada, Brach, and Sidor [\[47](#page-24-7)[–55\]](#page-24-8), who have been involved in modeling the grinding process [\[56\]](#page-24-9).

The literature provides but only a few studies, including a comprehensive energy assessment of grinding machines and devices with a focus on the process parameters. A number of studies indicate energy consumption and the degree of grinding as basic assessment criteria [\[57,](#page-24-10)[58\]](#page-24-11).

The criteria for energy assessment provided in the literature (Table [1\)](#page-3-0) represent a machine-oriented approach to the grinding process. They can be considered to belong to the group of efficiency criteria proposed by M. Bielski [\[59\]](#page-24-12), presenting the ratio of profits to expenditures [\[60\]](#page-24-13). Dependences (1)–(8) indicate the energy "productivity" of the process; that is, they define the amount of energy needed to grind the material unit (unit of mass, volume). The function of adaptation (Equation (9)) proposed by J. Flizikowski [\[49\]](#page-24-14) views many grinding factors as a machine process and is designed for global assessment of the process in terms of biomass-processing for the needs of feeding animals. It combines the effects of material grinding—an increase in the processed grain assimilability by living organisms and the amount of energy used by the machine elements and power transmission system. Effectiveness understood in terms of the energy exchange efficiency (Equation (10)) has been discussed in paper [\[30\]](#page-23-15).

A criterion of a unit demand for energy is often used as an energy measure (dependence (6)). Depending on the material properties and the required grain dimensions, energy demands can be: from 20 kWh·Mg⁻¹ to 130 kWh·Mg⁻¹ for rough and medium grinding and up to 800 kWh·Mg⁻¹ for micro and nanogrinding.

For brittle materials such as glass, cement, and clinker, the energy required for very fine grinding is much lower than for polymer and biological fibrous materials. The energy demand for these materials is nearly two times higher, whereas the final particles are from 10 to 100 times larger. Hence, the grinding efficiency of fibrous materials is lower than that of brittle materials [\[61\]](#page-24-15).

An insufficient number and quality of grinding-process descriptions, ineffective technological solutions, and unsatisfying attempts to improve grinding system efficiency means major problems remain unsolved, such as the high energy costs of grinding, poor yield, and insufficient quality of the product represented by granulometric parameters. These problems should be solved by monitoring and supervising grinding parameters such as linear speed, the angular speed of discs, energy consumption, power input, etc. In view of the above, taking up research on this subject can bring numerous benefits.

There is an urgent need to provide an explanation of the essence of engineering and the control of granular biomass quasi-shearing by means of a multi-hole grinding unit with a focus on the process of energy consumption.

Hence, the following research goals were established:

The development of a mathematical model of energy consumption and granular biomass grinding for the needs of the integrated design of multi-hole (disc) grinding units. Experimental determination of the impact of selected parameters of the multi-disc grinding process on the sustainable energy consumption of granular biomass.

Research problems were formulated in the form of questions in relation to the research goals established herein:

- 1. Will the development of an adequate mathematical model of energy consumption considering basic parameters of the process such as the yield, fineness degree, unit energy consumption, and power input enable the integrated design of the structure, disc parameters, and hole movement in shearing culvert discs?
- 2. What is the impact of deliberately changed characteristics and relations of the unit motion on the yield, fineness degree, power input, unit energy consumption, and integrated index of sustainable granular biomass grinding energy consumption in a multi-hole grinding unit?

2. Materials and Methods

2.1. Integrated Energy Consumption Index

The introduction of energy and pro-environment-based assessment into the construction–optimization process of the technology of energy biomass grinding leads to the creation of new, better structural and process solutions. In a sense, it is a driving force for biomass-processing competitiveness and innovativeness [\[66,](#page-25-1)[67\]](#page-25-2). Paper [\[68\]](#page-25-3) indicates that energy efficiency assessments make it possible to improve the grinder process motion parameters and indicates technologies which are the best for a given product. It has also been proven that the developed efficiency models can be used not only for process verification but also for verification of the whole structure of grinding, particularly the working unit.

Developing an adequate mathematical model and finding functional dependences between the variables are important elements of each assessment (structural-optimization efficiency) [\[69\]](#page-25-4). The first step should involve the identification of the assessed processes and subprocesses and the determination of criteria [\[68\]](#page-25-3).

The assumption of the model of integrated energy consumption for grinding takes into account the most important grinding indexes, which are indirectly or directly connected with power and energy demand. First of all, the criteria for power consumption assessment, unambiguously characterizing the grinding device, were established. The following criteria were accepted as components of the model of integrated energy consumption, in accordance with the desired states of the grinding process [\[70,](#page-25-5)[71\]](#page-25-6):

• Yield of grinding *KQr*:

 $K_{Or} = Q_r$, (11)

, (12)

• Power demand *KP*:

• Unit energy demand
$$
K_{Ej}
$$
:

$$
K_{Ej} = 1/E_j,\tag{13}
$$

• Fragmentation degree K_i **:**

$$
K_i = i_{80},\tag{14}
$$

where *Qr*—yield of grinding, kg·h −1 ; *Pr*—average power consumption of grinding, kW; *Ej*—unit of energy consumption, kWh·kg⁻¹; and *i*₈₀—80% fragmentation degree.

 $K_P = 1/P_r$

The yield of grinding is indirectly related to the power and energy consumption of grinding. Increasing the yield is usually associated with an increase in the grinder dimensions and, subsequently, an increase in the power of the drive unit, which involves a change of energy parameters. In the machine conditions, grinding yield Q_r can be determined on the basis of a dependence of grinding product mass change ∆*m* in the intake hopper during the time of observation ∆*t* [\[19\]](#page-23-6):

$$
Q_r = \Delta m / \Delta t, \tag{15}
$$

which can further be written:

$$
Q_r = dm/dt, \tag{16}
$$

$$
Q_r = \int_0^t m dt. \tag{17}
$$

Power consumption for grinding changes in time, which is caused by an irregularity in the operation of the machine [\[72\]](#page-25-7). In the simplest way, it can be defined as a periodical occurrence of rises and falls in power consumption as a result of variable amounts of materials between the working elements, which causes momentary periods of the machine running idle during grinding (with no feed). In connection with this, the overall power consumption in time *t Ptoti* can be defined as [\[7](#page-22-6)[,73\]](#page-25-8):

$$
P_{toti} = P_{ui} + P_{ii},\tag{18}
$$

where *Pui*—power consumption for the medium grinding in a given moment *t*, kW and *Pii*—power consumption of the idle gear in a given moment *t*, kW.

Then, the total grinding power consumption P_r in a certain time interval T is an average of the momentary power consumption, according to the equation:

$$
Qr = \sum_{i=0}^{T} P_{toti}/T.
$$
 (19)

Grinding processes are characterized by the parameters of the unit energy demand; therefore, they were accepted to be a component of the integrated energy consumption index model. Generally, a unit energy demand is defined as the amount of energy per mass unit of the material (volume) [\[2,](#page-22-1)[7,](#page-22-6)[20](#page-23-7)[,63](#page-24-17)[,64\]](#page-25-9). For the grinding machine unit, demand *E^j* is expressed as a ratio of average power consumed by the grinder *P^r* to yield *Q^r* [\[19](#page-23-6)[,63](#page-24-17)[,73\]](#page-25-8):

$$
E_j = P_r / Q_r \tag{20}
$$

The last criterion of the model of integrated energy consumption was accepted to be the fragmentation degree, being a determiner of the product quality and effectiveness of the grinding process [\[20,](#page-23-7)[74\]](#page-25-10). Most generally, the fragmentation degree is defined as a ratio of the material mean dimensions before grinding to its mean dimensions after grinding [\[21](#page-23-8)[,75\]](#page-25-11). So far, it has been proven that increasing the frequency of the machine element contact (by increasing the rotational, angular, and linear speeds of the grinding elements) and repetitions of grinding provides an output product with smaller dimensions—that is, with a higher fragmentation degree [\[72,](#page-25-7)[76\]](#page-25-12). Unfortunately, it causes higher energy consumption [\[27,](#page-23-12)[77,](#page-25-13)[78\]](#page-25-14). The energy consumption model assumes a fragmentation degree of 80% *i*₈₀, defined as [\[19\]](#page-23-6):

$$
i_{80} = D_{80}/d_{80} \tag{21}
$$

where *D*₈₀—dimension of the sieve hole through which 80% of the feed material passes and *d*₈₀—dimension of the sieve hole through which 80% of the grinding product passes.

The model of integrated energy consumption was constructed in the same way as the model of efficiency described in paper [\[68\]](#page-25-3). This made it possible to establish a quantitative relation between the most important grinding indexes in terms of energy consumption. Integrated energy consumption was described in the criteria-based approach proposed by J. Zawada in the following way [\[79\]](#page-25-15):

$$
E_{zint} = K_{Qr} \cdot K_P \cdot K_{Ej} \cdot K_i
$$
\n(22)

Bearing in mind dependences (11)–(14) and (22), integrated energy consumption depends, in direct proportion, on the yield and fragmentation degree and, in an inverse proportion, to the power consumption and unit energy demand. Assuming that the state to be desired is that in which $Q \rightarrow \infty$, $i_{80} \rightarrow \infty$, $P_r \rightarrow 0$, and $E_i \rightarrow 0$, then $E_{zint} \rightarrow \infty$. In the sustainable approach, a better process will be the one with a higher integrated energy consumption index value (22).

2.2. Raw Materials

Rice and corn grains that are unsuitable for food purposes due to having been stored in inappropriate conditions that were used for the production of pellets underwent grinding in the experimental tests, verifying the correctness of the integrated energy consumption model. Both crops are extensively grown, and both of them have found applications in the energy sector due to their good energy characteristics, which make them suitable for the production of pellets whose calorific value is similar to that of a wooden biomass [\[80\]](#page-25-16). Grain moisture was determined on a moisture balance MAC 210/NP (RADWAG, Radom, Poland) by means of the weight method. Rice grains were balance MAC 210/NP (RADWAG, Radom, Poland) by means of the weight method. Rice grains were characterized by moisture at the level of 13.47% \pm 0.02%, whereas corn was at the level of 12.68% \pm 0.02%. The characteristic dimension of grain D_{80} for corn was 8.15 mm and, for rice, 2.14 mm (Figu[re](#page-6-0) 1). These values were obtained on the basis of a granulometric analysis carried out on a Camsizer (Retsch Technology GmbH, Haan, Germany) design according to the ISO norm 13322-2:2006 [\[81\]](#page-25-17). value is similar to that of a wooden biomass [80]. Grain moisture was determined on a moisture balance MAC 210/NP (RADWAG, Radom, Poland) by means of the weight method. Rice grains were

Figure 1. Granulometric distribution of (a) rice grains (b) corn grains.

2.3. Test Stand *2.3. Test Stand* 2.3. Test Stand

Verification of the model of integrated energy consumption was performed on a test stand for the intelligent monitoring of performance characteristics of a multi-disc grinder. The test stand was composed of: a five-disc mill, a control panel with a performance monitoring system, and an integrated system for analysis of the grinding product's particle [siz](#page-6-1)e (Figure 2).

Figure 2. Test stand for the intelligent monitoring of granular mass characteristics: 1-five-disc grinder, 2—worm feeder, 3—hopper, 4—control unit, 5—reception basket of the product of grinding, 6—weight of the product of grinding, and 7—integrated system for the analysis of the grinding product's particle $size [28]$.

A five-disc mill was equipped with a special integrated system for feed-dosing with a screw conveyor feeder, which makes it possible to control the feeding of the grain material into the grinding chamber. The grinding unit consists of five multi-hole discs fixed on the grinder shaft (Table [2\)](#page-7-0). Each disc is powered individually by means of a dedicated motor which enables \mathcal{O}

disc is powered individually by means of a dedicated motor which enables precise control of the angular speed of each disc. The final product is collected in the intake hopper with a scale fixed angular speed of each disc. The final product is collected in the intake hopper with a scale fixed underneath, by means of which, the mass of the fragmented material is weighed. This makes it possible differentiality by means of which, the mass of the magneticed material is weighed. This makes it possible to determine the actual yield of the process. The integrated system of the particle size analysis makes it possible to assess the grinding product's granulometric composition and to determine the degree of fragmentation. The whole system is equipped with a set of sensors and archive modules. Control of the grinder and data reading is included in the control panel by means of the authors' own application
(MMM) 2010) (MŁYN, 2019). possible to determine the actual yield of the process. The integrated system of the particle size $\frac{1}{2}$ the particle size $\frac{1}{2}$ d fragmentation. The degree of σ fragmentation is equipped with a set of sensors and the with a set of sensors and indicated (0.0111) 2019).

Parameter	Unit	Disc ₁	Disc ₂	Disc ₃	Disc ₄	Disc ₅
Disc diameter D_n	mm	274	274	274	274	274
Number of holes l_n	pcs.	14	22	27	33	39
Holes diameter d_n	mm	30	23	21	17.5	17,5

Table 2. Structural parameters of the five-disc grinder. **Table 2.** Structural parameters of the five-disc grinder.

2.4. Research Methodology 2.4. Research Methodology

Verification of the integrated energy consumption index model was carried out consistently with
Les secondo din Figure 2 the plan presented in Figure [3.](#page-7-1) the plan presented in Figure 3.

Figure 3. Research plan. *Vp*—feed dosing capacity, *Pi*—power consumption on the *i*-th disc, ∆*m*—mass increase in the intake hopper, *d*₈₀—dimension of the sieve hole through which 80% of the grinding intervalsed in the sieve hole through which 80% of the grinding product passes, i_{80} —80% fragmentation degree, E_j —unit energy consumption, Q_r —yield of grinding, *Pr*—power consumed by the grinder, and *Ezint*—integrated energy consumption. *Pr*—power consumed by the grinder, and *Ezint*—integrated energy consumption. **Figure 3.** Research plan. *Vp*—feed dosing capacity, *Pi*—power consumption on the *i*-th disc, ∆*m*—mass

for each of them on a moisture balance MAC 210/NP (RADWAG, Radom, Poland) in accordance with ISO norm 1446 [\[82\]](#page-25-18), and, additionally, average grain size before grinding on a CAMSIZER (Retsch Technology GmbH, Haan, Germany) device was also determined in accordance with ISO norm 13322-2:2006 [\[81\]](#page-25-17). Next, the prepared material was subjected to grinding on a five-disc grinder for 20 different grinding disc angular speed settings in accordance with the accepted test program [\[28](#page-23-13)[,79\]](#page-25-15) in $\begin{bmatrix} 0 & 0 & 0 & 1 \end{bmatrix}$ disc angular speed setting in accordance with the accep First, 20 one-kilogram samples of rice and corn were prepared. The moisture level was determined

order to investigate the dependence of the integrated energy consumption index on the total increase in the grinder disc angular speed *S*∆ω (Table [3\)](#page-8-0). The minimal speed of the grinder discs accepted to be the point of reference was 20 rad·s⁻¹. The accepted settings of the disc angular speed were different in terms of the angular speed gradient $\Delta \omega$. The feed was delivered by means of a screw conveyor feeder with the speed of 112 kg⋅h⁻¹. Changes in the time of parameters such as power consumption, product mass in the intake hopper, angular speeds of the grinder discs, torques, and size of the product particles were recorded (with a sampling frequency every 0.5 s) in order to determine the values of the integrated energy consumption model criteria (components)—that is, power consumption, yield, fragmentation degree, and unit energy consumption.

Test	No. of	$S\Delta\omega$	$\Delta\omega$	ω_1	ω_2	ω_3	ω_4	ω_5
Program	Configuration	rad $\cdot {\rm s}^{-1}$	rad \cdot s $^{-1}$	rad \cdot s ⁻¹				
	1	50	5	20	25	30	35	40
	$\overline{2}$	100	10	20	30	40	50	60
I	3	150	15	20	35	50	65	80
	4	200	20	20	40	60	80	100
	$\mathbf{1}$	200	20	100	80	60	40	20
	$\overline{2}$	150	15	80	65	50	35	20
$\rm _{II}$	3	100	10	60	50	$40\,$	30	$20\,$
	4	50	5	40	35	30	25	20
	$\mathbf{1}$	40	20	20	40	20	40	20
	$\overline{2}$	85	20	45	25	45	25	45
$\rm III$	3	225	25	75	50	75	50	75
	$\overline{4}$	360	20	100	80	100	80	100
	$\mathbf{1}$	40	20	20	40	20	40	20
	$\overline{2}$	80	40	20	60	20	60	$20\,$
IV	3	120	60	20	80	20	80	20
	$\overline{4}$	160	80	20	100	20	100	20
	$\mathbf{1}$	240	80	100	20	100	20	100
	2	280	60	100	40	100	40	100
V	3	320	40	100	60	100	60	100
	4	360	20	100	80	100	80	100

Table 3. Settings of the five-disc mill control parameters [\[28\]](#page-23-13).

RP—research program; ω_1 , ω_2 , ω_3 , ω_4 , and ω_5 —angular speeds of discs, rad·s⁻¹; $\Delta\omega$ —increase in angular speeds, rad·s⁻¹; and *S*∆ω—total increase in angular speeds, rad·s^{-1.}

The next step involved both statistical and substantive analyses. The values of the integrated energy consumption were determined for each setting of the grinder disc according to dependence (22). Statistical analysis of the results was carried out by means of MS EXCEL (Microsoft, Redmond, WA, USA) and Statistica software (TIBCO Software Inc., Palo Alto, CA, USA). A general statistical analysis of the results, including the determination of the characteristics of the integrated energy consumption distribution and its variable components, was performed. Tests of the distribution of the normality of the variables were conducted by means of a Shapiro-Wilk test. This test is used to assess the distribution of the results. The null hypothesis of this test is that the population is normally distributed [\[83\]](#page-25-19). Thus, if the *p*-value is less than the chosen alpha level (in this study, $p > 0.05$), then the null hypothesis is rejected, and it can be assumed that the data are not characterized by normal distribution. When the p-value is greater than the chosen alpha level, it cannot be rejected that the data are characterized by normal distribution [\[83\]](#page-25-19). A correlation analysis using the Pearson method was performed for variables whose distribution was close to normal, while a Spearman correlation analysis was applied for the remaining ones. Next, a regression analysis was used. The results of the statistical analyses were found to be significant for $p < 0.05$.

3. Results and Discussion $\frac{1}{\sqrt{2}}$ such that the study, the study, the integration index variables $\frac{1}{\sqrt{2}}$

In this part of the study, the test results of the integrated energy consumption index variables are described along with an analysis of their relations with the independent variable: the increase in the grinder disc angular speed *S*∆*ω*. The results of the tests performed for the settings of the accepted grinder disc angular speed configurations for rice grinding are presented in Table S1 and, for corn, in Table S2.

3.1. Test Results of the Integrated Energy Consumption Model Variables and Their Analysis

The analysis included general descriptive characteristics of the resultant variables of power consumption, fragmentation degree, unit energy consumption, yield, the Shapiro-Wilk test for the normality of distribution, and correlation analysis with the Pearson method.

3.1.1. Power Consumption Figure 4 shows the test results of the power consumption for rice and corn grinding on a five-

Figure 4 shows the test results of the power consumption for rice and corn grinding on a five-disc grinder. The results indicate that the disc angular speed changes do affect power consumption. An increase in power consumption along with an increase in the grinder disc angular speed was observed. It can also be noticed that the power consumption for each disc setting was different depending on the material used (Figure 4). The power consumption f[or](#page-9-0) rice grinding was lower than the power consumption for corn grinding for all cases, which is mostly connected with the differing properties and internal structures of these materials [\[34\]](#page-23-18).

Figure 4. Test results of the power consumption for rice and corn grinding. **Figure 4.** Test results of the power consumption for rice and corn grinding.

corn grains, which is reflected by the power demand of grinding machines, due to the necessity of overcoming the higher resistance of moving elements [\[37\]](#page-24-0). An increased demand for power and operation the gase of a higher strength grinding motorial was confirmed by $[28, 40]$ among athers. An energy in the case of a higher-strength grinding material was confirmed by [38–40], among others. energy in the case of a higher-strength grinding material was confirmed by [\[38–](#page-24-1)[40\]](#page-24-2), among others. AnEarlier analyses of rice and corn strength indicated that higher forces are needed to grind

increased demand for power for corn grinding is also the effect of differences in the internal structure thereof [\[38–](#page-24-1)[40\]](#page-24-2). Rice grains deprived of husks were used in the tests, whereas corn grains had the seed coat. Moreover, corn grains differ from rice grains in terms of endosperm structure. Grains with higher endosperm glassiness have been observed to need more energy and power in the process of grinding [\[36](#page-23-20)[,41,](#page-24-3)[42\]](#page-24-4). $\frac{1}{\sqrt{6}}$ $\frac{1}{\sqrt{6}}$ higher $\frac{1}{\sqrt{6}}$ have $\frac{1}{\sqrt{6}}$ and power in the power in t

On the basis of the Shapiro-Wilk test (Appendix [A,](#page-20-0) Tables [A1](#page-20-1) and [A2\)](#page-21-0) and the values of skewness and kurtosis (Appendix [A,](#page-20-0) Tables [A3](#page-21-1) and [A4\)](#page-21-2) of the distribution of the power consumption test results, it was found that this distribution is approximately normal. Subsequently, the Pearson method was used for the analysis of correlation between the power consumption of grinding P_R and total speed increase *S∆*ω. Correlation analysis revealed that there was a strong relation between the power consumption in grinding P_R and a total speed increase $S\Delta\omega$ during both rice grinding (R = 0.9658, Appendix A, Table [A5\)](#page-21-3) and corn grinding ($R = 0.9847$, Appendix [A,](#page-20-0) Table A6). ω the basis of the Shapiro-Wilk test (Appendix A, Tables A1 and A2) and the values of shearing

On the basis of the linear regression analysis, equations describing the dependence of power On the basis of the linear regression analysis, equations describing the dependence of power consumption as a function of total speed increase were determined. It was found that power consumption as a function of total speed increase were determined. It was found that power consumption for grinding can be described by means of a linear model with a high match (Figure [5\)](#page-10-0). consumption for grinding can be described by means of a linear model with a high match (Figure 5). Both the coefficient in the equations and the regression models themselves were statistically significant Both the coefficient in the equations and the regression models themselves were statistically (Tables 4 and 5).

Figure 5. Power consumption for grinding as a function of total speed increase; marking the **Figure 5.** Power consumption for grinding as a function of total speed increase; marking the confidence interval and values predicted for (a) rice grinding and (b) corn grinding.

$\overline{}$	$\,$	Value	Standard Error	t-Value	Prob > t
Rice	Intercept Slope	0.73234 0.00497	0.06115 3.14735×10^{-4}	11.97547 15.80313	5.21551×10^{-10} 5.36891×10^{-12}
Corn	Intercept Slope	0.74508 0.00666	0.05392 2.77525×10^{-4}	13.8175 23.98018	5.05108×10^{-11} 4.11081×10^{-15}

Table 5. Test results of the significance of the power consumption linear regression equation.

3.1.2. Yield

Figure 6 shows the results of rice and corn gr[in](#page-11-0)ding yield tests performed on a five-disc grinder. The results indicate that the disc angular speed changes have an impact on this parameter change. As in the case of power consumption, it was observed that grinding yields increased along with an increase in the disc angular speeds. It could also be observed that, for the settings of the grinder disc angular speeds at which the first disc speed was the lowest, the rice grinding yield was significantly higher than that of the corn (Figure 6). For the remaining settings, the yield was similar though slightly higher for corn. This might result from the relations between the structural characteristics of working discs, speed, and the size of the grain used. The average size of rice grains was definitely lower than that of corn; hence, more of them can be introduced into the open space of the grinding discs.

Figure 6. Test results of rice and corn grinding. **Figure 6.** Test results of rice and corn grinding.

On the basis of the Shapiro-Wilk test (Appendix A, Tables A1 and A2) and the values of On the basis of the Shapiro-Wilk test (Appendix A, Tables A1 and A2) and the values of skewness and kurtosis (Appendix [A,](#page-20-0) Tables [A3](#page-21-1) and [A4\)](#page-21-2) of the distribution of the performance test results, it was found that this distribution is approximately normal. Subsequently, the Pearson method was used in the analysis of correlation between grinding yield Q_r and the total speed increase. A correlation A correlation analysis showed that the correlation between the yield of grinding Qr and the total analysis showed that the correlation between the yield of grinding *Q^r* and the total speed increase *S*∆ω during both rice grinding (Appendix [A,](#page-20-0) Table [A5\)](#page-21-3) and corn grinding was poor (Appendix A, Table [A6\)](#page-22-8).

Poor correlations between the disc total angular speed increased, and the yield might be the result of the grain strength properties and their relations and interactions with the grinding unit. The phenomena accompanying the flow of granular materials through the grinding chamber, the inter-hole space, and inter-disc space of the quasi-shearing unit are not without importance. There can occur, among other things, periods when the material lingers in the grinding chamber due to the adhesion of wet grains, which can be observed, e.g., in the case of corn and the poor results in the fourth test program.

3.1.3. Unit Energy Consumption

Figure [7](#page-12-0) shows the test results of the unit energy consumptions for rice and corn grain grinding. For all the considered settings of the five-disc grinder angular speeds, the unit energy demand was higher for corn grinding (Figure [7\)](#page-12-0), which was mostly connected with a higher power consumption during corn grinding, which, in turn, results from the grain strength properties which are discussed in Section [3.1.1.](#page-9-1) Earlier research also indicated a higher unit energy consumption for corn grinding [19]. The results indicate that an increase in the angular speed of discs caused an increase in energy consumption (Figure 7). 3.1.3. Unit Energy Consumption

Figure 7. Test results of the unit energy consumption for rice and corn grinding. **Figure 7.** Test results of the unit energy consumption for rice and corn grinding.

On the basis of the Shapiro-Wilk test (Appendix A, Tables A1 and A2) and the values of On the basis of the Shapiro-Wilk test (Appendix A, Tables A1 and A2) and the values of skewness and kurtosis (Appendix [A,](#page-20-0) Tables [A3](#page-21-1) and [A4\)](#page-21-2) of the distribution of the results of the unit energy $\frac{1}{2}$ consumption tests, it was found that this distribution is approximately normal for the grinding of rice, while for the grinding of corn, it deviated from normal. Subsequently, the Pearson method was used was used in an analysis of correlation between unit energy consumption E_j for rice grinding and total speed and total speed increase S∆ω; whereas, in the case of corn, the Spearman method was used to assess increase *S*∆ω; whereas, in the case of corn, the Spearman method was used to assess these relations. Correlation analysis showed that there was a very strong positive correlation between the unit energy \sim the unit energy consumption Ej and total speed increase S∆ω for rice grinding (R = 0.95332, Appendix consumption *E^j* and total speed increase *S*∆ω for rice grinding (R = 0.95332, Appendix [A,](#page-20-0) Table [A5\)](#page-21-3). In the case of corn grinding, the correlation of these two variables was moderate (R = 0.5963, Appendix [A,](#page-20-0) $\overline{}$ $\frac{0.5}{0.5}$ and $\frac{0.5}{0.5}$. Table [A8\)](#page-22-9).

An equation describing the dependence of the unit energy consumption for rice grinding as a An equation describing the dependence of the unit energy consumption for rice grinding as a function of the total speed increase was determined based on a linear regression analysis. It was function of the total speed increase was determined based on a linear regression analysis. It was found found that the unit energy demand can be described by means of a linear model with a high match that the unit energy demand can be described by means of a linear model with a high match (Figure [8a](#page-13-0)).

In the case of the unit energy consumption involved in corn grinding, after the removal of outstanding values (results for settings IV3, IV4, and V1), it was the exponential model that provided \overline{a} the best match (Figure [8b](#page-13-0)) when compared to the others. This model was chosen on the basis of t fainting of the unferent nothing at models. As a selection chieffon, the value of the model match coefficient R^2 (the higher the value, the better the model) and the value of the standard error of the model coefficients (the lower the error, the better the model) were used. Unfortunately, the chosen model explained the variability of the unit energy consumption as a function of the total speed increase merely partially—slightly over 46% of the variability was explained by means of the chosen function. a ranking of the different nonlinear models. As a selection criterion, the value of the model match

Both the coefficients in the equations and the regression models were statistically significant (Tables [6](#page-13-1) $\,$ and [7\)](#page-13-2). The standard error of the coefficients in the equations did not exceed 12%. with the yield in the yield in the case of corn grinding was presented in Section 3.1.2 and was also reported i rue coemcients in

Figure 8. Unit energy consumption for grinding as a function of the total speed increase with **Figure 8.** Unit energy consumption for grinding as a function of the total speed increase with indication of the confidence interval and predicted values for: (**a**) rice grain grinding and (**b**) corn grinding.

$\overline{}$		Value	Standard Error	t-Value	Prob > t
Rice	Intercept	0.02809	0.00235	11.93399	5.5149×10^{-10}
	Slope	1.62274×10^{-4}	1.21157×10^{-5}	13.39367	8.44112×10^{-11}
Corn	a	0.10313	0.01227	8.40195	4.68401×10^{-7}
	b	0.9881	0.00401	246.4428	0
			a, b—coefficients of regression model (Figure 8b).		

Table 6. Test results of the significance of the coefficients of the unit energy consumption regression model.

Table 7. Test results of the significance of the equations of the unit energy consumption regression model.

$\overline{}$	Sum of Squares	Mean Square	F-Value	Prob > F
Rice	0.00546	0.00546	179.39049	8.44112×10^{-11}
Corn	0.10853	0.05427	97.41927	2.55003×10^{-9}

The unit (specific) energy consumption depend on two factors: the energy consumed for the grinding process and the mass of grinded material, and it described the amount of energy needed for $\frac{1}{2}$ shows the test results of rice and corn grain fragmentations at $\frac{1}{2}$ and $\frac{1}{2}$ after grinding on a $\frac{1}{2}$ and $\frac{1$ ratio of power demand and grinding yield. For grinded materials, the dependence between the yield and discs' total speed increase was not specified, and as it is one of the unit energy components, it influences the dependence between the unit energy consumption and the discs' total speed increase. For corn, the yield values spread was significant; that is why the fitting is very low. The problems grinding one kg of material. According to [\[19\]](#page-23-6), the unit energy consumption can be expressed as the with the yield in the case of corn grinding was presented in Section [3.1.2](#page-11-1) and was also reported in the previous study [\[28\]](#page-23-13).

3.1.4. Fragmentation Degree

Figure [9](#page-14-0) shows the test results of rice and corn grain fragmentations at 80% after grinding on a five-disc mill. A higher fragmentation degree was found for corn grain grinding for all analyzed disc angular speed settings (Figure [9\)](#page-14-0), which was connected with the ratio of the grain dimension and the inter-disc gap. The grains of rice and corn had similar average dimensions in all tests, and this value depended on the value of the inter-disc gap—the size of a particle after grinding will always be smaller than the gap. Due to the fact that the characteristic size of corn grains was bigger before grinding than

the size of rice grains (Table S1 and Table S2 in the Supplementary Materials) and their dimensions decreased down to those comparable to rice grains, the fragmentation degree of the corn grains was higher. It was observed, like in other studies [\[5,](#page-22-4)[26\]](#page-23-11), that for grinding bigger particles (corn has bigger particles than rice), the energy consumption is higher. It was also reported that the higher the disc speed (so the contacts between materials and cutting edges are more intensive), the grinding product has smaller particles [\[4,](#page-22-3)[84\]](#page-25-20). On the basis of the Shapiro-Wilk test (Appendix [A,](#page-20-0) Tables A1 and [A2\)](#page-21-0) and the values of the skewness and kurtosis (Appendix [A,](#page-20-0) Tables [A3](#page-21-1) and [A4\)](#page-21-2) of the distribution of the grinding results, it was found that this distribution is approximately normal for both rice and corn grinding. Subsequently, the Pearson method was used in an analysis of the correlation between the grain fragmentation degree *i₈₀* and summary speed increase *S*∆ω. Correlation analysis showed that there was a very strong positive relation between the rice fragmentation degree i_{80} and the total speed increase $S\Delta\omega$ (R = 0.93237, Appendix A, Table A5). In the case of corn grinding, the positive correlation between these two variables was moderate ($R = 0.6893$, Appendix A, Table A6). distribution of the grinding results, it was found, it was found that the grinding for the corresponding $10a$ and $10a$. The obtained linear model was able to provide a 90 explanation of $10a$

Figure 9. Test results of an 80% fragmentation degree for rice and corn grinding. **Figure 9.** Test results of an 80% fragmentation degree for rice and corn grinding.

The equation describing the dependence of an 80% degree of rice fragmentation as a function of the total speed increase was determined based on an analysis of linear regression. It was found that an 80% fragmentation degree can be described with a high match by means of a linear model (Figure [10a](#page-14-1)). The obtained linear model was able to provide a 90% explanation of the fragmentation degree as a function of the total angular speed increase *S*∆ω.

Figure 10. An 80% fragmentation degree as a function of the total speed increase with the markings **Figure 10.** An 80% fragmentation degree as a function of the total speed increase with the markings of the of the confidence interval and values predicted for: (a) rice grain comminution and (b) corn grain confidence interval and values predicted for: (**a**) rice grain comminution and (**b**) corn grain comminution.

For the case of the 80% fragmentation degree of corn, the linear model explained the fragmentation degree changes as a function of the total speed increase *S*∆*ω* only to a small extent ($R^2 = 0.47513$). Thus, the decision was made to check nonlinear models. As in the case of the unit energy demand, a ranking of models which took into account the value of the match coefficient $R²$ and the value of the standard error of the model coefficients was used. It was the exponential model which best explained the highest percent of the 80% corn fragmentation degree variability as compared to the other models (Figure [10b](#page-14-1)). Unfortunately, the chosen model did not sufficiently explain the variability of the 80% fragmentation degree as a function of the total speed increase. Both the coefficients in the equations and the regression models themselves were statistically significant (Tables [8](#page-15-0) and [9\)](#page-15-1). The standard error of the coefficients in the equations did not exceed 10%.

$\overline{}$	$\overline{}$	Value	Standard Error	t-Value	Prob > t
Rice	Intercept	1.02074	0.01376	74.17752	7.73924×10^{-24}
	Slope	7.74976×10^{-4}	7.08224×10^{-5}	10.94254	2.19489×10^{-9}
Corn	a	4.46488	0.13804	32,34576	
	b	0.97486	0.00357	273.12834	

Table 8. Test results of the regression model coefficient significance for an 80% fragmentation degree.

a, b—coefficients of regression model (Figure [10b](#page-14-1)).

Table 9. Test results of the regression equation significance for an 80% fragmentation degree.

$\overline{}$	Sum of Squares	Mean Square	F-Value	Prob > F
Rice	0.12447	0.12447	119.73909	2.19489×10^{-9}
Corn	335.73877	167.86938	864.38272	1.31021×10^{-18}

3.2. Analysis of the Integrated Energy Consumption Results

The next step of the tests involved an analysis of the integrated energy consumption for rice and corn grain comminution. Figure [11](#page-16-0) shows the results of the integrated energy consumption tests for both grains. In the case of corn, the highest values of the integrated energy consumption were found for setting no. 4 with RP II and, next, for setting no. 1 with RP III and setting no. 1 with RP IV. For rice grinding, the highest values of the integrated energy consumption were found for setting no. 1 in RP IV and, next, for setting no. 1 in RP III, setting no. 4 in RP II, and setting no. 2 in RP IV.

An analysis of the relations between the integrated energy consumption made it possible to determine the yield ranges, power consumption, unit energy consumption, and fragmentation degree for which the integrated efficiency is the highest (Figures [12](#page-17-0) and [13,](#page-18-0) red color). The integrated energy consumption for rice grinding on a five-disc grinder assumes values within the interval (928–1420) when the grinding yield is included in the range (25.2–30.6) kg \cdot h⁻¹, unit energy consumption in the range (0.027–0.049) kWh·kg−¹ , power consumption in the range (0.88–1.02) kW, and fragmentation degree in the range (1.04–1.13) (Figure [12\)](#page-17-0). The integrated energy consumption of corn grinding on a five-disc grinder assumes values in the range (1592–2640) when the grinding yield is within (19.8–32.4) kg⋅h⁻¹, unit energy consumption within (0.037-0.061) kWh⋅kg⁻¹, power consumption within (0.91-1.31) kW, and fragmentation degree in the range (2.75–4.21) (Figure [13\)](#page-18-0).

Figure 11. Test results of the integrated energy consumption for rice and corn grinding. **Figure 11.** Test results of the integrated energy consumption for rice and corn grinding. 0

The results of the integrated energy consumption tests are characterized by a higher value scatter for corn grinding, and the scatter of results for power consumption, yield, fragmentation degree, and for corn grinding, and the scatter of results for power consumption, yield, fragmentation degree, and unit energy consumption were also higher for corn grinding than for rice grinding (Figures 12 and 13). Thus, by knowing the components of the integrated energy consumption, its values can be predicted 0420) when the grinding than to complements. In the range of range (25.2–30.6) kg/h−1, unit energy consumption in tensor with a higher accuracy for rice grinding than for corn grinding.

Next, a basic statistical analysis of the variable was performed. On the basis of the Shapiro-Wilk test (Appendix [A,](#page-20-0) Tables [A1](#page-20-1) and [A2\)](#page-21-0) and the values of the skewness and kurtosis (Appendix A, Tables [A3](#page-21-1) and [A4\)](#page-21-2) of the distribution of the results, it was found that the distribution of the integrated energy consumption deviated from normal; therefore, in the correlation analysis, the Spearman coefficient was used to describe the monotonic relationships between the variables. Correlation analysis showed that there is a very strong negative correlation between the integrated energy consumption of rice grinding the range (1592-2640) when the grinding yield is with $\frac{1}{2}$. and total speed increase *S*∆w (R = −0.95554, Appendix [A,](#page-20-0) Table [A7\)](#page-22-10). In the case of corn grinding, the negative correlation of these two variables was moderate ($R = -0.51131$, Appendix [A,](#page-20-0) Table [A8\)](#page-22-9). degree in the range of the range of the variables. Correlation analysis showed a

Figure 12. *Cont.*

Figure 12. The integrated energy consumption of rice grinding as a function of the model components. **Figure 12.** The integrated energy consumption of rice grinding as a function of the model components.

Nonlinear regression analysis was used to determine the equations describing the dependence of the rice and corn grinding's integrated energy consumption as a function of the total speed increase. In this case, the best-matched model was determined on the basis of the value of matching coefficient \mathbb{R}^2 and the error values of the standard coefficients of the determined dependencies. It was found that the integrated energy consumption of rice grinding is best explained, nearly 77%, by an exponential model (Figure 14a). As regards corn, the best match was an exponential model, though it accounted for only 46% of the integrated energy consumption variability (Figure [14b](#page-18-1)). Both coefficients in the equations and the regression models themselves were statistically significant (Tables [10](#page-19-0) and [11\)](#page-19-1). The standard error of coefficients did not exceed 11% in the rice grinding's integrated energy consumption equations, and, in the case of corn, it did not exceed 26%.

Figure 13. The integrated energy consumption for corn grinding as a function of the model components. variable components.

Figure 14. The integrated energy consumption as a function of the total speed increase with the indication of the confidence interval and predicted values for: (a) rice grain comminution and (b) corn grain comminution.

The results of the analyses indicate that the rice and corn grinding processes differ in terms of yield, power consumption, fragmentation degree, unit energy consumption, and integrated energy consumption. In the case of corn, the process of grinding has more of a random character, which is mostly the result of the large differentiation of the grains of one species, which was also observed in other tests [\[20,](#page-23-7)[28,](#page-23-13)[85\]](#page-25-21). Hence, the match of models of unit energy consumption, yield, and fragmentation other tests [20,20,00]. Tiente, the materior models or unit energy consumption, yield, and magmentation
degree as a function of corn grinding speed increases, and subsequently, the models of the integrated energy consumption, which include the above-listed components, is rather poor.

$\overline{}$	$\qquad \qquad$	Value	Standard Error	t-Value	Prob > t
Rice	a	1325.48108	155.50266	8.52385	9.81711×10^{-8}
	b	0.99266	0.00124	802.86997	
Corn	a	2895.65796	776.51222	3.72906	0.00154
	b	0.98979	0.00339	292,34877	

Table 10. Results of significance tests for the coefficients of the integrated energy consumption regression model.

a, b—coefficients of regression model (Figure [14a](#page-18-1),b).

Table 11. Results of the significance tests for the equations of the integrated energy consumption regression.

	Sum of Squares	Mean Square	F-Value	Prob > F
Rice	6,691,362.97097	3,345,681.48549	125.99749	2.60167×10^{-11}
Corn	2.09017×10^{7}	1.04509×10^{7}	28.02063	2.96612×10^{-6}

Analyzing the values of the integrated energy consumption for the two grain species considered herein, it can be said that, from the point of view of the accepted criterion, a smaller increase in the angular speeds in relation to the reference speed on each disc (20 rad·s⁻¹) provides higher values of integrated energy consumption; e.g., the process of grinding is characterized by a low power consumption while maintaining the remaining parameters of grinding at a satisfactory level.

Verification of the integrated energy consumption model was performed for granular materials. It should be expected that, for a different type of biomass, e.g., wooden biomass, the value of the energy consumption index and its relations with the grinder disc total angular speeds would be different from the materials used in the study.

The proposed index of the integrated energy consumption can successfully be used to assess the grinding process and to select the grinder angular speeds to provide a low energy consumption, high yield, and a high fragmentation degree of the product. This index can find applications in automatic and control systems for industrial lines grinding energy materials, e.g., biomass, coal, and post-use polymer materials.

4. Summary and Conclusions

The aim of the study was achieved by developing and verifying the model of integrated energy consumption for grinding a biomass, which takes into account the fundamental parameters of the process: power consumption, unit energy consumption, yield, and the determination of the impact of changes in the grinding unit motion parameters on the values of the index developed herein.

The analyses of this study have proven that the index developed herein can be used successfully to assess a biomass grinding's energy consumption in an integrated approach—that is, one which includes not only energy consumption but also other parameters important from the point of view of the grinding process (yield, fragmentation degree, power consumption, and unit energy consumption). The verification of the model on a real object—a five-disc grinder—made it possible to determine the dependencies of the integrated energy consumption index and the motion parameters of the grinder discs for the total increase in disc annular speeds. Based on the analyses, it was found that the total speed increased, and thus, the increase in the disc angular speeds causes an increase in power consumption, in the fragmentation degree, and the unit energy consumption for both rice and corn grinding. In the case of rice grinding, these dependencies can be described with a high match by means of linear models. In the case of corn, a linear dependence was found only for power consumption. Nonlinear models were used for the unit energy consumption and fragmentation degree, though they accounted for only 60% of the studied parameter variability. The yield did not correlate with the total increase in angular disc speeds for either rice or corn grinding. This results mainly from physical

mechanical properties of the grains and grain-grinding unit relations and confirms the variety and variability of grains observed so far within one type of grain and, in addition, confirms the randomness of the grinding process.

The test results prove that integrated energy consumption is negatively correlated with a total increase in the grinder angular speeds. The models which best represent the variability of the integrated energy consumption were exponential models; though, in the case of corn, this model was characterized by a lower matching coefficient ($R^2 = 0.45896$) than the energy consumption model for rice grinding $(R^2 = 0.76749)$. Upon analyzing the values of the integrated energy consumption for two grain species, it can be observed that, in terms of the criterion accepted herein, a smaller angular speed increase in relation to the reference speed on each disc of the grinder (20 rad·s⁻¹) causes higher values of integrated energy consumption; that is, the process of grinding is characterized by a low power consumption while sustaining the remaining parameters of grinding at a satisfactory level.

The model of integrated energy consumption considered in this study can be a useful tool for integrated design and to select structural and process grinding parameters in preimplementation tests for grinders. Moreover, it can find an application in the automation and control systems of industrial lines' grinding energy materials, such as biomass, coal, and post-use polymers.

Further research on the structures and operations of biomass grinders in terms of their energy consumptions should be focused on finding the relations between selected structural characteristics of the grinding unit and negative environmental factors such as $CO₂$ emissions and natural resource depletion, as well as operation potentials.

Supplementary Materials: The following are available online at http://[www.mdpi.com](http://www.mdpi.com/1996-1073/13/6/1417/s1)/1996-1073/13/6/1417/s1: Table S1: The test results of rice grinding's integrated energy consumption and particular components of the model. Table S2: Test results of the integrated energy consumption for rice grinding and particular components of the model

Author Contributions: Conceptualization: W.K.; methodology, W.K. and J.F.; software, W.K.; validation, A.T. and J.F.; formal analysis, R.K. and P.B.-W.; investigation, W.K. and A.T.; resources, W.K.; data curation, W.K.; writing—original draft preparation, W.K.; writing—review and editing, W.K., A.T., J.F., R.K., and P.B.-W.; visualization, W.K.; supervision, J.F. and A.T.; project administration, W.K.; and funding acquisition, W.K. All authors have read and agreed to the published version of the manuscript.

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Appendix A

Table A1. Tests results of the normality of the Shapiro-Wilk distribution of variables for the process of rice comminution.

P^{*r*}—grinding power consumption, kW; Q^{*r*}—grinding yield, kg⋅h⁻¹; *E_j*—unit energy consumption, kWh⋅h⁻¹; *i*₈₀—80% fragmentation degree; E_{zint} —integrated energy consumption; and S∆ω—total increase in angular speeds, rad·s^{−1}.

	DF	Statistic	<i>p</i> -Value	Decision at Level (5%)
P_R	20	0.93699	0.21026	Cannot reject normality
Q_r	20	0.91059	0.06541	Cannot reject normality
E_i	20	0.65731	1.22879×10^{-5}	Reject normality
180	20	0.95111	0.38428	Cannot reject normality
E_{zint}	20	0.83526	0.00305	Reject normality
$S\Delta\omega$	20	0.91736	0.08817	Cannot reject normality

Table A2. Test results of the normality of the Shapiro-Wilk distribution of variables for the process of corn grinding.

P^{*r*}—power consumption for grinding, kW; *Q*^{*r*}—grinding yield, kg⋅h⁻¹; *E*_{*j*}—unit energy consumption, kWh⋅h⁻¹; *i*80—80% fragmentation degree; *Ezint*—integrated energy consumption; and *S*∆ω—total angular speed increase, rad \cdot s⁻¹.

Table A3. Results of the descriptive statistical analysis of variables for the process of rice grinding.

$\qquad \qquad$	Mean	Standard Deviation	Sum	Skewness	Kurtosis	Minimum	Median	Maximum	Range $(Max-Min.)$
P_R	1.5555	0.53786	31.11	0.31892	-1.15303	0.84	1.425	2.48	1.64
Q_r	28.165	1.69528	563.3	-0.02646	-1.28024	25.2	28.3	30.6	5.4
E_i	0.05495	0.01778	1.099	0.2127	-1.26079	0.027	0.052	0.083	0.056
i_{80}	1.149	0.08681	22.98	0.50272	-0.89842	1.04	1.14	1.31	0.27
E_{zint}	505.65	328.92877	10113	1.32281	1.62855	190	422	1417	1227
$S\Delta\omega$	165.5	104.43961	3310	0.60399	-0.72265	40	150	360	320

P^{*r*}—power consumption for grinding, kW; *Q*^{*r*}—yield of grinding, kg⋅h⁻¹; *E*_j—unit energy consumption, kWh⋅h⁻¹; *i*80—80% fragmentation degree; *Ezint*—integrated energy consumption; and *S*∆ω – total increase in angular $\frac{1}{2}$ speeds, rad \cdot s^{-1}.

$\overline{}$	Mean	Standard Deviation	Sum	Skewness	Kurtosis	Minimum	Median	Maximum	Range $(Max-Min.)$
P_R	1.8465	0.70585	36.93	0.41186	-0.92384	0.91	1.755	3.11	2.2
Q_r	21.725	8.82627	434.5	-0.74904	-0.4979	4.3	24	32.4	28.1
E_i	0.118	0.11051	2.36	2.23553	4.35658	0.037	0.0905	0.422	0.385
i_{80}	4.0685	0.65617	81.37	-0.77544	1.47486	2.29	4.125	5.11	2.82
E_{zint}	872.15	807.93116	17443	1.12497	0.13387	24	511.5	2639	2615
$S\Delta\omega$	165.5	104.43961	3310	0.60399	-0.72265	40	150	360	320

Table A4. Results of the descriptive statistical analysis of variables for the process of corn grinding.

P^{*r*}—power consumption for grinding, kW; *Q*^{*r*}—yield of grinding, kg⋅h⁻¹; *E*_{*j*}—unit energy consumption, kWh⋅h⁻¹; *i*80—80% fragmentation degree; *Ezint*—integrated energy consumption; and *S*∆ω—total increase in angular $\frac{1}{2}$ speeds, rad \cdot s^{-1}.

Table A5. Results of the analysis of variable correlation using the Pearson method for the process of rice grinding.

Two-tailed test of significance is used and * correlation is significant at the 0.05 level. *Pr*—power consumption for grinding, kW; Q_r—yield of grinding, kg·h⁻¹; E_j—unit energy consumption, kWh·h⁻¹; i₈₀—80% fragmentation degree; and *S*Δω—total angular speed increase, rad·s⁻¹.

Table A6. Results of the analysis of variable correlation using the Pearson method for the process of corn grinding.

		P_R	$\mathcal{L}r$	180
$S\Delta\omega$	r-Pearson	$0.98471*$	0.25495	$0.6893*$
	<i>p</i> -value	4.11081×10^{-15}	0.27801	7.741×10^{-4}

Two-tailed test of significance is used and * correlation is significant at the 0.05 level. *Pr*—power consumption for grinding, kW; Q_r—yield of grinding, kg·h⁻¹; *i*₈₀—80% fragmentation degree; and *S*∆ω—total angular speed increase, rad·s −1 .

Table A7. Results of the correlation analysis with the Spearman method for the process of rice grinding.

$\overline{}$	$\overline{}$	E_{zint}
$S\Delta\omega$	Spearman Corr.	$-0.95554*$
	p -value	5.48274×10^{-11}

Two-tailed test of significance is used and * correlation is significant at the 0.05 level. *Ezint*—integrated energy consumption and *S*∆ω—total angular speed increase, rad·s −1 .

Table A8. Results of the analysis of variable correlation with the Spearman method for corn grinding.

Two-tailed test of significance is used and * correlation is significant at the 0.05 level. *Ej*—unit energy consumption, kWh·h⁻¹; *E_{zint}*—integrated energy consumption; and *S*∆ω—total angular speed increase, rad·s⁻¹.

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