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Abstract: The paper presents the study of a three-phase system coupling a DC power source to a power grid. This study, based on an FPGA, implements a real-time control system and digital models of the power circuit. The proposed proportional–resonant (P+R) controller with a modified structure was part of the system, which can be used as an alternative controller to traditional ones, e.g., in photovoltaic systems. Due to difficulties in implementing resonant controllers, a P+R with a new structure using a PI controller was elaborated. With an appropriate approach to the generation of phase current patterns, it is possible to set the reactive current and, thus, compensate for the reactive power. The operation of the system for typical operating conditions (e.g., system startup, change in preset load) was characterized and compared with a classical solution using a PI controller.

Keywords: inverter; energy source; proportional–resonant; controller; FPGA

1. Introduction

Three-phase inverter control systems coupling energy sources to the power grid have traditionally used PI controllers and a natural system transformation to a rotating *dq* system [\[1\]](#page-15-0). To improve their performance, many variants have been proposed in the literature, including multistate feedback and increasing the proportional gain. The disadvantage of PI controllers is, among others, the distortion of the line current waveform caused by harmonics of the line voltage, inserted through feedback. For this reason, other solutions are sought, such as those based on fuzzy logic [\[2\]](#page-15-1).

Another solution is to use the proportional–resonant (P+R) controller [\[3\]](#page-15-2). The P+R controller has the ability to track sinusoidal varying signals and has selective amplitude– frequency characteristics. The P+R controller can be used in systems operating with a constant frequency of output voltage, e.g., in devices coupling renewable energy sources to the power grid [\[4\]](#page-15-3). This controller is designed for single-phase systems, but can be applied to three-phase systems, after their transformation to a two-phase orthogonal *αβ* stationary system [\[5\]](#page-15-4). In this case, two identical controllers operating independently in both axes are used. This solution allows also to control the reactive current of the supply line.

Among the advantages of $P+R$ controllers is that they can be tuned to the grid frequency for accurate tracking of the fundamental reference frequency and to some low-order harmonic frequencies for selective harmonic compensation. From an implementation point of view, a P+R controller requires less computational effort and does not require a grid voltage feedback loop, while achieving the same performance as a PI controller [\[2\]](#page-15-1). Due to the amplitude-frequency-selective characteristic, the power line current distortion is lower compared to control systems with PI structure [\[6](#page-15-5)[–8\]](#page-15-6).

In addition to the basic structure of the P+R controller, there are modifications described in the literature that improve its operation in grids with unstable voltage and

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frequency [\[9](#page-15-7)[,10\]](#page-15-8). The differences in their structures, compared to typical P+R controllers, are due to the different variants of the feedback loop and the change in the controller transmittance. Other solutions consist of a combination of a traditional PI regulator and a P+R regulator, which operate in *dq* [\[11\]](#page-15-9) and $\alpha\beta$ [\[12\]](#page-15-10) systems. The P+R controller can operate with different types of converters, e.g., matrix converters [\[13\]](#page-15-11) and multilevel inverters [\[14](#page-15-12)[,15\]](#page-15-13).

In the literature focused on simulation studies, implementations of structures composed of basic functional blocks are encountered [\[16–](#page-15-14)[18\]](#page-15-15). However, they mainly concern an ideal regulator with infinite gain for the reference frequency. The implementation of such a structure into a digital system is not indicated due to the natural limitation of signal ranges in such systems (such a limitation also applies to analog circuits). Due to the large slope of the characteristics in the resonant frequency range, even small changes in the line voltage frequency cause large and dangerous changes in the reference signals. This limits the functionality of the control system. To avoid these problems, the P+R controller in digital systems is made, for example, as a second-order generalized integrator (SOGI) [\[19\]](#page-15-16). A more common way is to implement the controller as a bandpass filter [\[4,](#page-15-3)[8,](#page-15-6)[20\]](#page-16-0). It has the same form as a gain-limited P+R regulator (called real [\[2\]](#page-15-1)). Such an implementation consists of an appropriate equation in the discrete signal domain, whose coefficients depend on the controller settings (gains of the proportional and resonant parts), the damping factor, and the grid frequency. Changing one of these parameters entails changing most of the parameters of the equation, which provides difficulties in implementing such a controller in grids with unstable voltage and frequency.

As presented in the introduction, despite its advantages, the P+R controller is difficult to implement. Therefore, a new structure for the implementation of the controller is proposed using basic functional blocks and a PI regulator. The conducted tests confirmed the correct operation of the structure in single-phase systems [\[21](#page-16-1)[,22\]](#page-16-2). Section [2](#page-1-0) contains information on the P+R regulator, i.e., its structure and characteristics, as well as experimental studies comparing the continuous transmittance to the proposed one implemented in the FPGA. In Section [3,](#page-4-0) the assumptions for the performed tests in a three-phase system are presented. Section [4](#page-5-0) contains the results of these studies, especially a comparison of the PI and P+R controllers. In Section [5,](#page-9-0) conclusions are presented, formulated on the basis of the conducted tests.

2. Proportional–Resonant Controller

An ideal regulator has infinite gain for the frequency to which it is tuned. In practice, a controller with limited gain is used with transmittance (Equation (1)) [\[2\]](#page-15-1).

$$
G_{P+R}(s) = K_P + \frac{2K_I\xi\omega_r s}{s^2 + 2\xi\omega_r s + \omega_r^2}.
$$
\n(1)

In Figure [1,](#page-2-0) the amplitude–frequency characteristics are shown for the following parameters of the controller in Equation (1): *K^P* = 1, *K^I* = 100, *ω^r* = 100π, and *ξ* = 0.05. For signals with resonant frequency of the controller, gain is equal to *K^P + K^I* . It is much bigger than for other frequencies. The resonant part of the controller can expressed as shown in Equation (2) [\[19\]](#page-15-16).

$$
Y_R = \frac{1}{T_1 s} \left(X - k Y_R - \frac{1}{T_2 s} Y_R \right),
$$
 (2)

where Y_R is the resonant controller output signal, *X* is the resonant controller input signal, *T1, T²* are integration time constants, and *k* is the gain.

Figure 1. Bode plot of P+R controller with transmittance (Equation (1)). **Figure 1.** Bode plot of P+R controller with transmittance (Equation (1)).

Figure 1. Bode plot of P+R controller with transmittance (Equation (1)). The integral part with integration time T_2 and the proportional part with gain k form the parance structure of the *T* reontroller. The proposed structure of the T Tecontroller is shown
in Figure 2, where the reconnet part of the requister is highlighted by a dashed line [22] in Figure 2, where the resonant part of the regulator is highlighted by a dashed line [\[22\]](#page-16-2). Using Equation (2), a structure consisting of simple blocks (P or I) was obtained. Using Equation (2), a structure consisting of simple blocks (P or I) was obtained. The parallel structure of the PI controller. The proposed structure of the P+R controller is shown allel structure of the PI controller. The proposed structure of the P+R controller is shown

Figure 2. Proposed structure of the P+R controller [\[22\]](#page-16-2).

Figure 2. Proposed structure of the P+R controller [22].

 $F = 1.78$ measured that $T_1 = 72$ = T_1 , the relationship of the coefficients in Equations (1) can be expressed as If it is assumed that $T_1 = T_2 = T$, the relationship of the coefficients in Equations (1)

$$
k = \frac{1}{K_i}; \ \omega = \frac{1}{T}; \xi = \frac{1}{2K_i}.
$$

In order to verify the discretization of the P+R controller, the digital structure of this controller was tested for amplitude–frequency characteristics. A schematic diagram of the *Kollibner was lested for amphitude–frequency characteristics. A scriential diagram of the system that was implemented in the FPGA device is shown in Figure 3.* In order to verify the discretization of the F+K controller, the digital structure of this controller was tested for amplitude–frequency characteristics. A schematic diagram of the

Figure 3. Schematic diagram of a system to determine Bode plot. **Figure 3.** Schematic diagram of a system to determine Bode plot. **Figure 3.** Schematic diagram of a system to determine Bode plot.

Tests of amplitude–frequency characteristics were performed for the input signal frequency range from 40 to 60 Hz, while the regulator resonance frequency was 50 Hz. The results of these tests are shown in Figure 4. results of these tests are shown in Figure [4.](#page-3-1) results of these tests are shown in Figure 4.

Figure 4. Bode plot of the proposed controller structure. **Figure 4.** Bode plot of the proposed controller structure. **Figure 4.** Bode plot of the proposed controller structure.

 ϵ comparing the characteristics of the continuous form of the regulator with those of the regulator with the regulator ϵ μ in a digitally implemented regulator, the digital P+R controller has significantly less signals signals are signal point of μ $\mu_{\rm B}$ at the resonant frequency (ideal— $\mu_{\rm B}$) decays discussed— $\mu_{\rm B}$ decays discussed $\mu_{\rm B}$ and $\mu_{\rm B}$ and $\mu_{\rm B}$ its phase shift is smaller for signals with frequencies other than resonant (ideal—around Comparing the characteristics of the continuous form of the regulator with those of the digitally implemented regulator, the digital P+R controller has significantly less gain at the resonant frequency (ideal—40 dB, implemented—25 dB). Furthermore, its signal gain at the resonant frequency (ideal—40 dB, implemented—25 dB). Furthermore,

80°, implemented—70°). This is due to the accuracy of the calculations and the rounding
transformation from the natural coordinate system to *αβ* following the relationship in Equainvolved. These features allow for more stable operation following small changes in line
voltage frequency. voltage frequency.

3. P+R Operation in Three-Phase System

The P+R controller can be used in three-phase systems. The control system operates *i* in the *αβ* coordinate system, and patterns of the current waveform are obtained similarly in the *αβ* coordinate system, and patterns of the current waveform are obtained similarly to the single-phase system from the phase voltage waveforms as described in [\[21,](#page-16-1)[22\]](#page-16-2).
The transformation from the natural coordinate system to $\alpha\beta$ follows the relationship in to the single-phase system from the phase voltage waveforms as described in [21,22]
The transformation from the natural coordinate system to *αβ* follows the relationship in Equation (4). This is the version of the *αβ* transformation in which the natural and *αβ* 3 system waveforms have equal amplitudes.

$$
\begin{array}{c}\nv_{\alpha} = v_{a} \\
v_{\beta} = \frac{v_{b} - v_{c}}{\sqrt{3}}\n\end{array} \tag{4}
$$

in the *αβ coordinate system, and patterns of the current waveform are obtained similar lying are obtained* similar

In this system, it is possible to independently set the active and reactive components of the supply line currents. In Figure 5, the alpha-beta frame is presented with the current space vector Im and the voltage space vector Um. Both the voltage and the current space
wectors were calculated wing Faustion (4). Assuming that the voltage vector is rotating vectors were calculated using Equation (4). Assuming that the voltage vector is rotating with angular velocity wt, the current vector rotates with the same angular velocity but is delayed by an angle *φ* for inductive load. In this case, the component of the current vector corresponds to the component *IP*, and *IP*, an lying in the direction of the voltage vector corresponds to the active component *IP*, and that in the orthogonal direction corresponds to the reactive component *IQ*. that in the orthogonal direction corresponds to the reactive component *IQ*.

Figure 5. Graphical interpretation of reference active and reactive currents. **Figure 5.** Graphical interpretation of reference active and reactive currents.

By analyzing Figure [5,](#page-4-1) We can deduce that

$$
i_{P\alpha} = (I_m \cos \varphi) \cos \omega t = Y V_m \cos \omega t = Y v_\alpha
$$

\n
$$
i_{P\beta} = (I_m \cos \varphi) \sin \omega t = Y V_m \sin \omega t = Y v_\beta
$$

\n
$$
i_{Q\alpha} = (I_m \sin \varphi) \cos(\frac{\pi}{2} - \omega t) = I_m \sin \varphi \sin \omega t = Y V_m \sin \omega t = Y v_\beta
$$

\n
$$
i_{Q\beta} = (-I_m \sin \varphi) \cos \omega t = -Y V_m \cos \omega t = -Y v_\alpha
$$
\n(5)

The equations presented are the control rules implemented in the control system. From these, the orthogonal reference currents are determined as follows:

$$
i_{\alpha REF} = k_P v_\alpha + k_Q v_\beta
$$

\n
$$
i_{\beta REF} = k_P v_\beta - k_Q v_\alpha
$$
\n(6)

where k_P and k_Q are arbitrarily preset components corresponding to the active and reactive component of the current, respectively. Therefore, it is possible to use an inverter in which the reference currents are also obtained as in Equation (6) as a reactive power compensator. This could compensate for both inductive and capacitive reactive power, thereby implementing voltage control at the point of connection to the line.

The primary role of the system is to transfer energy from the renewable energy source to the grid. Therefore, the level of compensated reactive power depends on the current load of the device with active power. The reactive power that can be generated is limited by the following equation: 2 2 *QSP ^K* ≤ − Max , (7)

$$
Q_K \le \sqrt{S_{\text{Max}}^2 - P^2},\tag{7}
$$

where S_{Max} is the maximum apparent power, and P is the actual active power value.

Power *S*Max in this case is equal to the nominal active power of the converter. Power *S*Max in this case is equal to the nominal active power of the converter.

4. Laboratory Model 4. Laboratory Model

The laboratory model tests of a three-phase, three-wire, three-leg, two-level inverter The laboratory model tests of a three-phase, three-wire, three-leg, two-level inverter with a P+R controller were performed in real time (RT) using the Quartus II software package. The P+R controller was part of an inverter control system coupling a three-phase package. The P+R controller was part of an inverter control system coupling a three-phase power line to a renewable energy source. In practice, controllers are commonly tested using real-time models implemented in the same structure as the control system. This is possible due to the high computational capabilities of programmable systems, e.g., FPGAs. Using previously verified models allows testing controllers in similar conditions as in cases with a real power system. This method of controller testing is [ill](#page-5-1)ustrated in Figure 6. The basic currents and the voltage waveform during hardware startup registered when the active current component changed from 21 A to 16 A are [sh](#page-6-0)own in Figure 7. This case refers to a reactive current component equal to zero.

Figure 6. Figure 6. Laboratory stand with RT modeling in FPGA. Laboratory stand with RT modeling in FPGA.

Figure 7. Grid currents i_a , i_b , i_c in A and grid voltage u_a in V for proposed P+R controller during startup process and active current change $I_{\alpha ref}$ in A, measured for reactive current $I_{\beta ref} = 0$.

In the next level of research, the waveforms of currents and voltages, active and reactive power for a constant reference value $i_{\alpha ref}$ equal to 10 A, and zero, positive, and negative reactiv[e c](#page-6-1)omponents of current $i_{\beta ref}$ were registered. Figure 8 shows the case when the active component of the reference current was equal to 20 A with zero reactive component.

igure 8. Registered data for reference active current $I_{\text{surf}} = 10$ A and reference reactive current **Figure 8.** Registered data for reference active current $I_{\text{areff}} = 10$ A and reference reactive current *Iβref* = 0 A: reactive power in var (**a**); active power in W (**b**); grid currents and voltage waveforms (**c**).

It can be seen from Figure 8 that the reactive power value is close to zero within the limits resulting from the accuracy of the measuring systems and parasitic reactance. limits resulting from the accuracy of the measuring systems and parasitic reactance.

As shown in Figures [9](#page-7-0) and [10,](#page-8-0) the inverter can generate both types of reactive power, As shown in Figures 9 and 10, the inverter can generate both types of reactive power, at the same active power, transferring it from the energy source to the grid. at the same active power, transferring it from the energy source to the grid.

Figure 9. Registered data for reference active current $I_{\text{aref}} = 10$ A and reference reactive current $I_{\beta ref} = 1$ A: reactive power in var (a); active power in W (b); grid currents and voltage waveforms (c).

The blocks implemented in the software were divided into two parts: the simulator of the power circuit (energy source, inverter, and power line) and the control system (controller, modulation system, and current pattern signal generation). In Table [1,](#page-7-1) the assumptions made during the experimental verification of the system with a digital P+R controller are given.

The reference waveform of the line current was obtained according to Equation (5). The coefficients k_P and k_Q were limited by software such that the maximum current value was not exceeded. An appropriately scaled (by *k^v* coefficient) *αβ* reference voltage signal was added to the controller output signal. The amplitude of these signals was chosen in

such a way that the output voltage of the inverter was equal to the supply line voltage when the controller output signal was zero. As a result, no current flowed in the line during in each of caling inverter startup.

Figure 10. Registered data for reference active current $I_{\alpha ref} = 10$ A and reference reactive current $I_{\beta ref}$ = -1 A: reactive power in var (a); active power in W (b); grid currents and voltage waveforms (c).

The line current is the result of the voltage difference between the inverter and the grid. Its waveform in one line is described by the following equation:

$$
i(t) = \frac{v_C - v_f}{R} \left(1 - e^{-Rt/L} \right) + i(0)e^{-Rt/L},
$$
\n(8)

where v_c is the inverter voltage, v_f is the phase voltage in the supply line, R is the line resistance, and *L* is the total inductance of the system.

Using Equation (8), the line current values at discrete time intervals were determined (calculations for $T_p = 4 \mu s$ and $T_{RL} = 0.021$).

$$
i(n) = i(n-1)e^{\frac{-T_p}{T_{RL}}} + \frac{v_S(n-1)}{R}(1 - e^{\frac{-T_p}{T_{RL}}}),
$$
\n(9)

where *i(n)* is the current value at the *n*-th sample time, *i(n* − 1) is the current value at the previous sample time, and $v_s(n - 1)$ is the value of the voltage difference between inverter and line voltages.

The blocks that make up the control system are a P+R controller, a modulator consisting of a triangular waveform generator (24 kHz), and three numerical comparators. The numerical comparators compare the output signal of the controller with the triangular waveform and, on this basis, generate control signals for the switches of the inverter legs. In Figure [11,](#page-9-1) the block diagram of the individual modules implemented in the FPGA for the study is shown.

Figure 11. Block diagram of the implemented system.

Figure 11. Block diagram of the implemented system. **5. Results and Analysis**

The conducted studies investigated the following issues:

- Startup of the device with a preset active power,
- The change in the preset active load,
- Startup of the device with a preset active and reactive power,
- The change in the preset reactive load,
- Phase modulation of grid voltages, ϵ
- Step phase shift of grid voltages,
- \mathfrak{e} and \mathfrak{e} . Grid voltage drop.

Example waveforms of these operating states are presented in Figures [12](#page-10-0)[–18.](#page-11-0) For simplicity, the waveforms illustrate voltages and currents in the *αβ* axes after transformation from the natural reference system. The values marked on the graphs are amplitude values
of suggests and reduced system the graphics and second the hard graphs are amplitude values or currents and voltages. Inverter operation and associated phase current calculations were
performed in the RT system and implemented for a three-phase line. The waveforms were mation from the internation from the natural reference system. The waveforms were observed with the Quartus II environment tool using the JTAG protocol to transfer samples
of selected cignals to a semputor of currents and voltages. Inverter operation and associated phase current calculations were of selected signals to a computer.

recede signals to a comparent
For all operating conditions, the controller operation was stable. In Figures [12–](#page-10-0)[15,](#page-10-1) the for an operating conditions, the contention operation was station in righter in 1980. components of the current reached set values. In Figures [16–](#page-11-1)[18,](#page-11-0) a grid operation with unstable parameters was shown. As in previous cases, the response to these changes in the control system was correct and quickly reached the reference waveforms. In the case of phase modulation (Figure [16\)](#page-11-1), no significant phase shift was observed. During step phase change (Figure [17\)](#page-11-2), the time needed to achieve the reference waveform was about 10 ms. In the case study with voltage drop, the current change was not significant.

Figure 12. Startup of the device-change in the active component of the current to the nominal P_N .

Figure 14. Device startup-change in active and reactive component of the current to $0.7P_N$.

0.7*PN.* Figure 15. Change in reactive power character into the opposite one at constant active 0.7*PN.* 0.7*PN.* component 0.7*PN.*

Figure 16. Phase modulation of grid voltages (from -30° to $+30^{\circ}$ within 100 ms interval) at constant active component $0.7P$. active component 0.7*PN.*

Figure 17. Step phase change of grid voltages (+30°) at constant active component 0.7*PN.* **Figure 17.** Step phase change of grid voltages (+30◦) at constant active component 0.7*PN.* **Figure 17.** Step phase change of grid voltages (+30°) at constant active component 0.7*PN.*

Figure 18. The 10% voltage drop at constant active component $0.7P_N$.

In the next step of the study, control systems with the proposed $P+R$ controller and
leader life controllar means compared. In Table 2, the means steps of these controllers are compared. In traditional solutions, a large gain is used in the proportional path of the 21 Controller; however, for the purpose of this study, it was set equal to the proportional stable parameters was shown. As in process was shown in previous cases, the response of the response μ and μ part of the P+R controller. This allowed comparing the operation of the controllers under cimilar conditions. p_{intra} conduction (Figure 16), no significant phase shift was observed. During step phase shift was obs the classical PI controller were compar[ed](#page-11-3). In Table 2, the parameters of these controllers similar conditions.

Fable 2. Overview of tested controllers. **Table 2.** Overview of tested controllers.

Both types of controllers were operated in the $\alpha\beta$ reference system. Characteristics were plotted for the following operating states:

- Startup of the device with the preset active power (from 0 to the preset power),
- Change in the preset active load (from $0.5P_N$ to the preset power, where P_N is the nominal power of the inverter),
- Change in the character of active power,
	- Change in the preset reactive load with constant active power load (constant 0.5*PN*, reactive power from 0 to the preset power).

For the last point, it is important to keep in mind the limitation resulting from Equation (7). When the active power load is $0.5P_N$, the maximum reactive component is limited to $0.8P_N$. The changes in the set quantities were triggered at random moments of the supply voltage period. For this reason, the presented results are an average of 10 measurements for each set point of operation. As a criterion for a properly operating controller, a moment at which the deviation of the regulation was no more than 10% of the instantaneous value of the set waveform was assumed.

Figures 19-[22](#page-14-0) illustrate the characteristics of control systems with the P+R or PI controller for various operating conditions. They show how the regulation time $(t_r$ in ms) changes depending on the set value of active or reactive component. The value of the set component (as well as for other cases) expressed as a function of the characteristics as a percentage refers to the rated power of the device. In Figure [19,](#page-12-0) the dependence of the adjustment time on the set active component during the startup of the device is shown. adjustment time on the set terms component atting the startup of the device is shown
With the increase in the set point value, the regulation time in both variants increased. For the P+R controller, for $0.5P_N$ and higher values, the regulation time oscillated around 30 ms. In the case of the PI regulator, on the other hand, the adjustment time was significantly longer and was characterized by an increase across the entire range of parameter changes. The largest difference was observed for the rated power, and it was about 20 ms. The smallest was observed for $0.6P_N$, and it was about 8 ms. via are mercase in the set point value, the set of \mathbb{R}^n

The graph in Figure 20 shows the dependence of the adjustment time on the set value of the active component for a step change of the set load. The study assumes that the power changes from $0.5P_N$ to the set point. As in the previous case, the adjustment time In the system with the PI controller was significantly longer. The smallest difference was between for the change to maximum power, and it was 27 ms. The smallest difference was 15 ms for $0.3P_N$. T_{max} (see the enarge to maximum power, and it was about 20 ms. The enarget among \sim *PM* corrected for \sim *PN*.

Figure 19. Comparison of adjustment times of P+R and PI controllers in the tested system for startup **Figure 19.** Comparison of adjustment times of P+R and PI controllers in the tested system for startup with the set active component. with the set active component.

set reactive component for both controllers. The differences in this case were the smallest

Figure 20. Comparison of adjustment times of P+R and PI controllers in the tested system for **Figure 20.** Comparison of adjustment times of P+R and PI controllers in the tested system for changes in the set active component (from $0.5P_N$ to the set one). changes in the set active component (from 0.5*PN* to the set one).

Figure 21. Comparison of adjustment times of P+R and PI controllers in the tested system, for changes in the character of the reactive component.

The remaining characteristics, illustrated in Figures [21](#page-13-1) and [22,](#page-14-0) concern the operation of the system when the reactive component of the line currents was also set. Figure [21](#page-13-1) illustrates the changes in the adjustment time upon changing the character of the reactive power. In both cases, this time increased with the initial value of the reactive component. The largest difference was about 15 ms for a reactive component equal to 10% of the rated power. The adjustment time of both systems stabilized at about $Q = 0.4P_N$, achieving values of about 36 ms for P+R and 43 ms for PI. The dependence of the adjustment time while the set reactive component was changed in the case of a constant active component is presented in Figure [22.](#page-14-0) In this case, the adjustment time increased with the increase in the

 $\mathbf{r}_\mathbf{S}$ reactive component for both controllers. The differences in this case were the smallest and did not exceed 10 ms.

Figure 22. Comparison of adjustment times of P+R and PI controllers in the tested system for **Figure 22.** Comparison of adjustment times of P+R and PI controllers in the tested system for changes in the reactive component at a constant active component $(0.5P_N)$.

In each of the cases studied, the PI controller had a steady-state error, which was not In each of the cases studied, the PI controller had a steady-state error, which was not observed for the P+R controller. For this reason, the PI controller in such systems is used observed for the P+R controller. For this reason, the PI controller in such systems is used after transformation to a *dq* system, where it operates on constant signals. after transformation to a *dq* system, where it operates on constant signals.

6. Conclusions 6. Conclusions

The presented experimental results of the studies prove the functionality of the P+R The presented experimental results of the studies prove the functionality of the P+R controller in systems of three-phase inverters coupling energy sources to the power grid. controller in systems of three-phase inverters coupling energy sources to the power grid. For all the tests carried out, the P+R controller was characterized by better dynamics of For all the tests carried out, the P+R controller was characterized by better dynamics of operation than the PI regulator. The differences were even more than one period of supply operation than the PI regulator. The differences were even more than one period of supply voltage in favor of the P+R controller. In the case of reactive power control, when the system played an additional role in compensating for reactive power, the differences were not so significant, but the P+R controller was still characterized by better dynamics of operation. Since both controllers had the same proportional gain, it can be concluded that the resonant part of the proposed P+R controller provides better dynamic performance. the resonant part of the proposed P+R controller provides better dynamic performance. The possibility of using a lower gain in the feedback will also reduce the harmonic transfer The possibility of using a lower gain in the feedback will also reduce the harmonic transfer when the voltage is distorted. when the voltage is distorted.

Real-time testing was performed using an FPGA-based platform. This allowed the Real-time testing was performed using an FPGA-based platform. This allowed the control system to be tested as it might be used in a real device. During such tests, the control system to be tested as it might be used in a real device. During such tests, the control system cooperated with the blocks, in which the parameters were artificially generated for the power grid, inverter, and energy source. The high frequency of operation and, thus, the calculations allow assuming that the control system will work properly in cooperation with a real device and grid, without requiring many improvements.

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References

- 1. Patel, H.; Mishra, N. Modelling and Analysis of Grid Connected Three-Phase Photovoltaic Inverter. *SSRN J.* **2019**. [\[CrossRef\]](http://doi.org/10.2139/ssrn.3442520)
- 2. Binkowski, T. Photovoltaic Inverter Control Using Programmable Logic Device. *SN Appl. Sci.* **2019**, *1*, 596. [\[CrossRef\]](http://doi.org/10.1007/s42452-019-0598-x)
- 3. Teodorescu, R.; Blaabjerg, F.; Liserre, M.; Loh, P.C. Proportional-Resonant Controllers and Filters for Grid-Connected Voltage-Source Converters. *IEE Proc. Electr. Power Appl.* **2006**, *153*, 750. [\[CrossRef\]](http://doi.org/10.1049/ip-epa:20060008)
- 4. Cha, H.; Vu, T.-K.; Kim, J.-E. Design and Control of Proportional-Resonant Controller Based Photovoltaic Power Conditioning System. In Proceedings of the 2009 IEEE Energy Conversion Congress and Exposition, San Jose, CA, USA, 20–24 September 2009; pp. 2198–2205.
- 5. Tarasantisuk, C.; Suyata, T.; Tarateeraseth, V.; Witheephanich, K. Active and Reactive Power Control for Three-Phase Grid Inverters with Proportional Resonant Control Strategies. In Proceedings of the 2016 13th International Conference on Electrical Engineering/Electronics, Computer, Telecommunications and Information Technology (ECTI-CON), Chiang Mai, Thailand, 28 June–1 July 2016; pp. 1–6.
- 6. Makhloufi, S. Comparative Study Between PI and Resonant Controllers for PV Grid-Connected Inverter. *Int. J. Grid Distrib. Comput.* **2014**, *7*, 135–142. [\[CrossRef\]](http://doi.org/10.14257/ijgdc.2014.7.3.13)
- 7. Zammit, D.; Spiteri Staines, C.; Apap, M. Comparison between Pi and Pr Current Controllers in Grid Connected Pv Inverters. *Int. J. Electr. Electron. Sci. Eng.* **2014**, *8*, 221–226. [\[CrossRef\]](http://doi.org/10.5281/ZENODO.1090617)
- 8. Rufa'I, N.A.; Zhang, L.; Chong, B. Comparison of PI and PR Controllers with Adaptive Notch Filter for LCL Filtered Grid-Tie Converters under Weak Grid. In Proceedings of the 2019 IEEE PES/IAS PowerAfrica, Abuja, Nigeria, 20–23 August 2019; pp. 650–655.
- 9. Xie, Z.; Chen, Y.; Wu, W.; Wang, Y.; Gong, W.; Guerrero, J.M. Frequency Coupling Admittance Modeling of Quasi-PR Controlled Inverter and Its Stability Comparative Analysis under the Weak Grid. *IEEE Access* **2021**, *9*, 94912–94922. [\[CrossRef\]](http://doi.org/10.1109/ACCESS.2021.3093465)
- 10. Zeng, C.; Li, S.; Wang, H.; Miao, H. A Frequency Adaptive Scheme Based on Newton Structure of PRRC for LCL-Type Inverter Connected with Weak Grid. *Energies* **2021**, *14*, 4225. [\[CrossRef\]](http://doi.org/10.3390/en14144225)
- 11. Liserre, M.; Teodorescu, R.; Blaabjerg, F. Multiple Harmonics Control for Three-Phase Grid Converter Systems with the Use of PI-RES Current Controller in a Rotating Frame. *IEEE Trans. Power Electron.* **2006**, *21*, 836–841. [\[CrossRef\]](http://doi.org/10.1109/TPEL.2006.875566)
- 12. Stojic, D.; Milinkovic, M.; Veinovic, S.; Klasnic, I. Novel Proportional-Integral-Resonant Current Controller for Three Phase PWM Converters. In Proceedings of the 2016 4th International Symposium on Environmental Friendly Energies and Applications (EFEA), Belgrade, Serbia, 14–16 September 2016; pp. 1–4.
- 13. Zhang, J.; Li, L.; Dorrell, D.G.; Guo, Y. Space Vector Modulation Based Proportional Resonant Current Controller with Selective Harmonics Compensation for Matrix Converter Systems. In Proceedings of the 2017 20th International Conference on Electrical Machines and Systems (ICEMS), Sydney, Australia, 11–14 August 2017; pp. 1–6.
- 14. Uddin, W.; Busarello, T.D.C.; Zeb, K.; Khan, M.A.; Yedluri, A.K.; Kim, H.-J. Control Strategy Based on Arm-Level Control for Output and Circulating Current of MMC in Stationary Reference Frame. *Energies* **2021**, *14*, 4160. [\[CrossRef\]](http://doi.org/10.3390/en14144160)
- 15. Tariq, M.; Iqbal, M.T.; Meraj, M.; Iqbal, A.; Maswood, A.I.; Bharatiraja, C. Design of a Proportional Resonant Controller for Packed U Cell 5 Level Inverter for Grid-Connected Applications. In Proceedings of the 2016 IEEE International Conference on Power Electronics, Drives and Energy Systems (PEDES), Trivandrum, India, 14–17 December 2016; pp. 1–6.
- 16. Ramesh, V.; Mandava, S. Microgrid Design and Control Using a Discrete Proportional Resonant Controller. *Int. J. Renew. Energy Res.* **2015**, *5*, 1041–1048.
- 17. Husev, O.; Roncero-Clemente, C.; Makovenko, E.; Pimentel, S.P.; Vinnikov, D.; Martins, J. Optimization and Implementation of the Proportional-Resonant Controller for Grid-Connected Inverter with Significant Computation Delay. *IEEE Trans. Ind. Electron.* **2020**, *67*, 1201–1211. [\[CrossRef\]](http://doi.org/10.1109/TIE.2019.2898616)
- 18. Sreekumar, P.; Danthakani, R.; Veettil, S.P. Implementation of Proportional-Resonant Controller in an Autonomous Distributed Generation Unit. In Proceedings of the 2018 Advances in Science and Engineering Technology International Conferences (ASET), Abu Dhabi, United Arab Emirates, 6 February–5 April 2018; pp. 1–5.
- 19. Tarraso, A.; Candela, J.I.; Rocabert, J.; Rodriguez, P. Proportional-Resonant Current Controller with Orthogonal Decoupling on the Aβ-Reference Frame. In Proceedings of the IECON 2017—43rd Annual Conference of the IEEE Industrial Electronics Society, Beijing, China, 29 October–1 November 2017; pp. 1453–1458.
- 20. Khalfalla, H.; Ethni, S.; Al-Greer, M.; Pickert, V.; Armstrong, M.; Phan, V.T. An Adaptive Proportional Resonant Controller for Single Phase PV Grid Connected Inverter Based on Band-Pass Filter Technique. In Proceedings of the 2017 11th IEEE International Conference on Compatibility, Power Electronics and Power Engineering (CPE-POWERENG), Cadiz, Spain, 4–6 April 2017; pp. 436–441.
- 21. Nowak, M.; Piróg, S. Simulation Studies of the Proportional Resonant Controller. Przegląd Elektrotechniczny 2018, 6, 130-133. [\[CrossRef\]](http://doi.org/10.15199/48.2018.06.24)
- 22. Nowak, M.; Piróg, S. Implementation of the Proportional Resonant Controller in the FPGA System. *Przegląd Elektrotechniczny* **2019**, *7*, 87–90. [\[CrossRef\]](http://doi.org/10.15199/48.2019.07.18)