



Article Adaptive PI and RBFNN PID Current Decoupling Controller for Permanent Magnet Synchronous Motor Drives: Hardware-Validated Results

Xiaoli Zeng ^{1,2,*}, Weiqing Wang ¹ and Haiyun Wang ¹

- ¹ Department of Engineering Research Center of Ministry of Education for Renewable Energy Generation and Grid Connection Technology, Xinjiang University, Urumqi 830047, China
- ² Chongqing Jiangjin Shipbuilding Industry Co., Ltd., Chongqing 402263, China
- * Correspondence: 13669982941@163.com

Abstract: This study presents an adaptive proportional-integral (PI) and radial basis function neural network proportional-integral-derivative (PID) current control solution for permanent magnet synchronous motor (PMSM) drives. The proposed controller includes four controls: a decoupling term, a PI term, a supervision term, and a radial basis neural network-PID (RBFNN-PID) term. The first control term makes up the nonlinear factors, the second automatically adjusts the control gains, the third guarantees the system stability, and the fourth optimizes the PID parameters to achieve optimal system performance. Unlike off-line tuned PID controllers, the adaptive controller includes an adaptive tuning method for the on-line adjustment of control gain based on the gradient descent strategy. Therefore, it can be adjusted and handle the uncertainty of any system parameters. The program is not only simple and easy to be implemented but also ensures the accuracy and rapidity of the tracking speed. The control system has proven to be asymptotically stable. To verify the theory and application of the algorithm, a comparative experiment between the adaptive PI + RBFNN-PID controller and traditional PI + PID controller was conducted, demonstrating good robustness, which can effectively improve the PMSM. The results confirm that the proposed design achieves excellent control stability (i.e., quicker transient responding and smaller steady state error) in the presence of parametric uncertainty compared to conventional PID methods.

Keywords: adaptive control; parameter uncertainties; proportional-integral (PI) control; PID control; RBFNN-PID term; PMSM

1. Introduction

Currently, AC motors are widely used in household appliances and industrial fields, with examples including power cars, wind power systems, industrial robotics, air conditioning (ac), and washing machines. There are two main types of AC motors: asynchronous motor (IM) and PMSM. About 70% of industrial motors are IM because of its simplicity, durability, and low production cost [1-5]. However, the permanent magnet synchronous motor (PMSM) is gradually replaced by people because of its high efficiency, low maintenance cost and high power density. However, the permanent magnet synchronous motor (PMSM) system is a nonlinear multivariable system whose performance is not easy to control due to changes in operating parameters [6–9]. Therefore, it is necessary to develop a high-performance controller with a simple algorithm, quick response time, extremely high precision and strong robustness. The motor parameters and load torque variations of a proportional-integral-differential (PID) controller are used to operate permanent magnet synchronous motor (PMSM) system in industry because of its simplicity, definitude of function and high efficiency [10]. However, one of the main problems with conventional PID controllers is sensitivity to the uncertainties of the system. Therefore, the control performance of traditional PID methods is severely degraded due to parameter changes.



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). Some researchers surmount this shortcoming by designing mixed PID controllers or new adjusting rules [11–13]. As shown in [11], a mixed control system consisting of a transient fuzzy controller and a steady-state PI controller is proposed. Additionally [12] adjusted PI gain with fuzzy rules. However, these two methods both use off-line adjustment rules and lack adaptability to the uncertainty of time-varying systems in contrast to the adaptive PI controller with on-line regulation shown in [13]. Although the controller did not require any precise knowledge of motor parameters, there were no tested uncertain parameters. Recently, several researchers have proposed many advanced control strategies including fuzzy logic control (FLC) with nonlinear optimal control for the effective control of PMSM systems, nonlinear optimal control (NOC) with sliding mode control (SMC), neural network control, and adaptive control FLC [14]. Because of its fuzzy reasoning ability [15] has become a research hotspot. However, as the number of fuzzy rules adds, the control precision becomes greater, but the control algorithm becomes increasingly complex. NOC has been successfully introduced and applied to PMSM controllers [16,17]. Unfortunately, these controllers need sufficient knowledge and accuracy of motor parameters and has not yet been tested with drastic changes in mechanical parameters. Because of its robustness to external load disturbance and fast dynamic response, SMC is widely used in the speed control of permanent magnet synchronous motors [18–21]. Yet, the system dynamics are still susceptible to parameter changes and flutter problems. At the same time, another design method of speed control using NNC for permanent magnet synchronous motor system has been proposed [22–24]. One of the most important features of this technique is its advantage to approach linear or non-linear mappings by learning. Though its high complexity results in the control algorithm limits its implementation in practical applications. Adaptive control is another interesting approach because it can handle variable motor parameters and load torque for permanent magnet synchronous motor drives as shown in [25,26]. However, these two studies only considered changes in stator inductance and load torque. Other motor parameters present uncertainty such as stator resistance, moment of inertia, and viscous friction coefficient. In addition, convergence conditions for system dynamic errors are not guaranteed for the adaptive control algorithm [26].

This study combines the simple and effective traditional PI + PID controller with the self-tuning capabilities of adaptive control to designed a better adaptive PI + RBFNN-PID controller for permanent magnet synchronous motor drives. The controller contains an adaptive tuning law designed to tune the control gain on-line using the method of gradient descent. Thus, when the parameters are changed, the PI + PID-RBFNN gain will be auto-adjusted to the optimal value. Therefore, good dynamic response can be obtained even when the system parameters are uncertain. The Lyapunov stability theory describes the stability analysis of the proposed control strategy in detail. The experimental results for the current fluctuation and current response time show that the proposed adaptive PI + RBFNN-PID control scheme is effective and feasible when compared with the traditional PI + PID control scheme under the condition of uncertain parameters. In Section 2, the model is defined. In Section 3, the adaptive PI and PID controllers are defined, and the performance is analyzed. In Section 4, the RBFNN-PID controller is defined, and the performance and advantage of the NN compensator from RBFNN-PID is verified. In Section 5, a comparison between the conventional PI + PID method and the proposed adaptive PI + RBFNN-PID method for the current fluctuation and current response time is completed.

2. System Dynamic Error and Model Description

2.1. The Model Description from the System

The torque balance equation of a PMSM [27] is:

$$\tau_{em} = J_{eq} d\omega_m / dt + B_a \omega_m + T_L, \tag{1}$$

where J_{eq} is the inertia of the motor; ω_m is the motor rotational speed; B_a is the friction coefficient; T_L is the load torque; and τ_{em} is the electromagnetic drive torque, which depends on the type of PMSM. For a PM motor, τ_{em} can be expressed as follows:

$$\tau_{em} = P(\psi_f i_{sq}) \text{PM motor}$$
⁽²⁾

where *P* represents the number of motor pole pairs. Finally, the relationship between ω_m and ω_e is given by:

$$\omega_e = \omega_m \cdot P. \tag{3}$$

A mathematical model of a SMT permanent rotating reference frame motor driver can be described by the following equations in the d, q rotating reference frame

$$\begin{cases} \dot{i}_d = -\frac{R_s}{L_d}i_d + \frac{1}{L_d}V_d + \omega_e i_q \\ \dot{i}_q = -\frac{R_s}{L_q}i_q - \frac{\psi_f}{L_q}\omega_e + \frac{1}{L_q}V_q - \omega_e i_d \end{cases}$$
(4)

where ω_e is the rotor speed of PMSM; i_d and i_q are the *d* and *q* stator current, respectively; V_q and V_d are the *d* and *q* voltage input, respectively; L_d and L_q is the *d* and *q* stator inductance, respectively; R_s is the stator resistance; and ψ_f is the flux linkage.

2.2. The Dynamic Error System

To improve the stability of a PMSM, the errors and integral of errors are joined. The dynamic errors between i_d and its reference value, i_d^* , and between i_q and its reference value, i_d^* , are defined as:

$$\begin{cases} e_d = i_d^* - i_d \\ e_q = i_q^* - i_q \end{cases}.$$
(5)

The integrals of e_q and e_d are defined as:

$$\begin{cases} \delta_d = \int_0^t e_d dt \\ \delta_q = \int_0^t e_q dt \end{cases}$$
(6)

A positive definite Lyapunov function is constructed as:

$$V = \frac{1}{2}e_d^2 + \frac{1}{2}e_q^2 + \frac{1}{2}k_{id}\delta_d^2 + \frac{1}{2}k_{iq}\delta_q^2.$$
 (7)

The derivative of *V* to *t* gives the following result:

$$\dot{V} = e_d [\dot{i}_d^* - \frac{1}{L_d} (u_d - R_s i_d + \omega_e L_q i_q) + k_{id} \delta_d] + e_q [\dot{i}_q^* - \frac{1}{L_q} (u_q - R_s i_q - \omega_e L_d i_d - \omega_e \psi_f) + k_{iq} \delta_q],$$
(8)

$$\begin{cases} V_d = L_d \dot{i}_d^* + R_s i_d + k_1 L_d e_d + k_{id} L_d \delta_d \\ -\omega_e L_q i_q \\ V_q = L_q \dot{i}_q^* + R_s i_q + k_2 L_q e_q + k_{iq} L_q \delta_q \\ +\omega_e L_d i_d + \omega_e \psi_f \end{cases}$$
(9)

$$\begin{cases} V_d = L_d i_d + R_s i_d + L_d e_d + k_1 L_d e_d + k_{id} L_d \delta_d - \omega_e L_q i_q \\ V_q = L_q i_q + R_s i_q + L_q e_q + k_2 L_q e_q + k_{iq} L_q \delta_q \\ + \omega_e L_d i_d + \omega_e \psi_f \end{cases}$$
(10)

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3. Design of the Adaptive PI and PID Controller

3.1. Traditional PI and PID Compound Control with Decoupling Technology

The equation for V_{dq} and the conventional adaptive PI design are as follows:

$$V_{dq} = u_1 + u_2 + u_{nn}, \tag{11}$$

The voltage equation of the mathematical model of SPMSM is as follows:

$$\begin{cases} u_{1d} = L_d i_d + R_s i_d - \omega_e L_q i_q \\ u_{1q} = L_q i_q + R_s i_q + \omega_e L_d i_d + \omega_e \psi_f \end{cases}$$
(12)

Depending on R_s , L_d , L_q , and ψ_f , the system parameters $\beta_1 - \beta_5$ can be expressed as:

$$\beta_1 = \frac{R_s}{L_d}, \ \beta_2 = \frac{1}{L_d}, \ \beta_3 = \frac{R_s}{L_q}, \ \beta_4 = \frac{1}{L_q}, \ \beta_5 = \frac{\psi_f}{L_q}$$
 (13)

The mathematical model of the current equation obtained by combining Equations (12) and (13) is:

$$\begin{cases} \dot{i}_d = -\beta_1 i_d + \beta_2 u_{1d} + \omega_e i_q \\ i_q = -\beta_3 i_q + \beta_4 u_{1q} - \beta_5 \omega_e - \omega_e i_d \end{cases}$$
(14)

where u_1 , as shown in Equation (11), is as follows:

$$u_1 = u_0 + u_{PI} + u_s \tag{15}$$

From Equations (12) and (13), the models of the error system are as follows:

$$\begin{cases} u_{1d} = (\beta_1 i_d - \omega_e i_q)/\beta_2 \\ u_{1q} = (\beta_3 i_q + \beta_5 \omega_e + \omega_e i_d)/\beta_4 \end{cases}$$
(16)

From Equations (12), (14), and (16), Equation (14) is expressed as:

$$\begin{cases} \dot{i}_d = \beta_2(u_{1d} - u_{0d}) \\ i_q = \beta_4(u_{1q} - u_{0q}) \end{cases}$$
 (17)

 u_{1dq} can be rewritten in vector form as:

$$u_{1dq} = \begin{bmatrix} \beta_2 u_{1d} \\ \beta_4 u_{1q} \end{bmatrix} = A \begin{bmatrix} u_{1d} \\ u_{1q} \end{bmatrix} = u_0 + u_{PI}, \tag{18}$$

The value of the coefficient *A* is as follows:

$$A = \begin{bmatrix} \beta_2 & 0\\ 0 & \beta_4 \end{bmatrix},\tag{19}$$

The value of the coefficient u_{PI} is as follows:

$$u_{PI} = \begin{bmatrix} u_{1PI} \\ u_{2PI} \end{bmatrix} = \begin{bmatrix} -K_{1P}i_d - K_{1I}\int_0^t i_d dt \\ -K_{2P}i_q - K_{2I}\int_0^t i_q dt \end{bmatrix},$$

$$= EK$$
(20)

where K_{1P} , K_{1I} , K_{2P} , K_{2I} are the proportional gain, integral gain and differential gain of the PI controller, respectively. The equation of state and gain matrices are expressed as:

$$E = \begin{bmatrix} \int_0^t i_d dt & i_d & 0 & 0\\ 0 & 0 & \int_0^t i_q dt & i_q \end{bmatrix},$$
 (21)

$$K = \begin{bmatrix} -K_{1I} & -K_{1P} & -K_{2I} & -K_{2P} \end{bmatrix}^{T},$$
(22)

It is important to note that the derivative of the current model is usually convoluted and, therefore, was excluded in Equation (22).

Adaptive PI relies on on-line parameter tuning, which solves the problem of matching the motor's internal parameters and enables a rapid response system. The proposed adaptive PI controller can be expressed as:

$$u_{1dq} = u_0 + u_{PI} - u_{PI0} + u_s. ag{23}$$

3.2. The Proposed Adaptive PI Controller

The latest trajectory error vectors under the reduced-order dynamics of SMC are used to obtain an adaptive tracking error rule.

$$s(t) = \begin{bmatrix} s_1(t) \\ s_2(t) \end{bmatrix} = \begin{bmatrix} i_d \\ i_q \end{bmatrix}.$$
(24)

From the viewpoint of sliding mode control, the conditions for the existence of sliding mode and collision mode are derived according to Lyapunov. In general, the Lyapunov candidate function for the SMC is expressed by $V_1 = 1/2s^Ts$. Then, the slip can be derived from the Lyapunov theory that can verify the slip of the system, which is given by:

$$\dot{V}_1(t) = s^T \dot{s} < 0.$$
 (25)

The SMC condition requires that $s \to 0$ as $t \to \infty$. To obtain the adaptive regulation of the PI gain, the supervised gradient method is used to decrease the SMC condition. The method of the gradient descent algorithm is computed in the opposite direction of the power flows and yields the stable characteristics of the PID gains. Therefore, the four adaptive laws governing the gain, K_{1P} , K_{1I} , K_{2P} , and K_{2I} , are easily obtained under the supervisory gradient method, that is as follows:

$$\dot{K}_{1P} = -\gamma_{1P} \frac{\partial V_1}{\partial K_{1P}} = -\gamma_{1P} \frac{\partial V_1}{\partial u_{1PI}} \frac{\partial u_{1PI}}{\partial K_{1P}} = -\gamma_{1P} s_1 i_d,$$

$$\dot{K}_{1I} = -\gamma_{1I} \frac{\partial V_1}{\partial K_{1I}} = -\gamma_{1I} \frac{\partial V_1}{\partial u_{1PI}} \frac{\partial u_{1PI}}{\partial u_{1PI}} = -\gamma_{1I} s_1 \int_0^t i_d dt,$$

$$\dot{K}_{2P} = -\gamma_{2P} \frac{\partial V_1}{\partial K_{2P}} = -\gamma_{2P} \frac{\partial V_1}{\partial u_{2PI}} \frac{\partial u_{2PI}}{\partial K_{2P}} = -\gamma_{2P} s_2 i_q,$$

$$\dot{K}_{2I} = -\gamma_{2I} \frac{\partial V_1}{\partial K_{2I}} = -\gamma_{2I} \frac{\partial V_1}{\partial u_{2PI}} \frac{\partial u_{2PI}}{\partial K_{2I}} = -\gamma_{2I} s_2 \int_0^t i_q dt,$$

(26)

where γ_{1P} , γ_{1I} , γ_{2P} , γ_{2I} are the learning rates that are positive.

The adaptive adjusting method can be expressed in the following vector form:

$$\dot{K} = \phi E^T s, \tag{27}$$

where $\phi = diag(\gamma_{1I}, \gamma_{1P}, \gamma_{2I}, \gamma_{2P})$.

Remark 1. Using on-line adjustment, the control gain can be adjusted automatically with the change of system parameters. Thus, the designed adaptive PID controller can overcome the drawbacks of all off-line adjustment methods and provide good performance without being affected by the uncertainty of the system parameters.

Next, a monitor is required to pull the dynamic error back to a predetermined bounded area and guarantee the stability of the system. Suppose there is an optimized PI control (u_{PI}^*) such that:

$$t_{PI}^* = u_{PI0} + \varepsilon, \tag{28}$$

where $K^* = \begin{bmatrix} -K_{1I}^* & -K_{1p}^* & -K_{2I}^* & -K_{2P}^* \end{bmatrix}^T$ is the optimal gain matrix and $\varepsilon = \begin{bmatrix} \varepsilon_1 & \varepsilon_2 \end{bmatrix}^T$, where ε_1 and ε_2 are the approximation inaccuracies, and they are assumed to be bounded

by $0 \le |\varepsilon_1| \le \alpha_1$ and $0 \le |\varepsilon_2| \le \alpha_2$, in which α_1, α_2 are the positive constants. Then, the projection for the regulatory controls is as follows:

$$u_s = \begin{bmatrix} -\alpha_1 * \operatorname{sgn}(s_1) \\ -\alpha_2 * \operatorname{sgn}(s_2) \end{bmatrix}.$$
(29)

Through integrating the decoupling control terms, the PID control terms with adaptive laws, and the supervisory control terms, the desired controller is obtained as $u_{1dq} = u_{0dq} + u_{PI} + u_s$.

4. RBFNN-PID Controller Design

4.1. The Proposed Adaptive RBFNN-PID Controller

RBFNN incremental PID trajectory tracking is superior to traditional PID control in terms of adaptability, robustness and real-time performance. Unlike the conventional PID controller, it has a highly adaptive learning ability and meets the requirements for a nonlinear controller.

The expression of u_2 is:

$$u_2 = u_{PID} + u_{2s}, (30)$$

 $\dot{e} = \sigma$, (31)

$$\begin{cases} u_{2d} = L_d \sigma_d + k_1 L_d e_d + k_{id} L_d \delta_d \\ u_{2q} = L_q \sigma_q + k_2 L_q e_q + k_{iq} L_q \delta_q \end{cases}$$
(32)

$$M = \begin{bmatrix} \delta_d & e_d & \sigma_d & 0 & 0 & 0 \\ 0 & 0 & 0 & \delta_q & e_q & \sigma_q \end{bmatrix}.$$
 (33)

$$Z = \begin{bmatrix} Z_{3I} & Z_{3P} & Z_{3D} & Z_{4I} & Z_{4P} & Z_{4D} \end{bmatrix}^{T}.$$
 (34)

The latest error tracking vector based on PID with the dynamics of SMC is given as:

$$\Omega(t) = \begin{bmatrix} \Omega_1(t) \\ \Omega_2(t) \end{bmatrix} = \begin{bmatrix} \frac{1}{s}e_d + e_d + se_d \\ \frac{1}{s}e_q + e_q + se_q \end{bmatrix}.$$
(35)

Then, the transfer function from s_3 is obtained by strictly positive real functions:

$$G(p) = \frac{e_d}{s_3} = \frac{1}{\frac{1}{\frac{1}{s} + s + 1}},$$
(36)

where *s* is regarded as the Laplace variable. Therefore, it is to be stated that e_d be astringent to zero when the condition of $s \rightarrow 0$ is satisfied.

$$\begin{aligned} \dot{Z}_{1P} &= -\eta_{1P} \frac{\partial V_2}{\partial K_{3P}} = -\eta_{1P} \Omega_1 e_d, \\ \dot{Z}_{1I} &= -\eta_{1I} \frac{\partial V_2}{\partial K_{3I}} = -\eta_{1I} \Omega_1 \delta_d, \\ \dot{Z}_{1D} &= -\eta_{1D} \frac{\partial V_2}{\partial K_{3D}} = -\eta_{1D} \Omega_1 \sigma_d, \\ \dot{Z}_{2P} &= -\eta_{2P} \frac{\partial V_2}{\partial K_{4P}} = -\eta_{2P} \Omega_2 e_q, \\ \dot{Z}_{2I} &= -\eta_{2I} \frac{\partial V_2}{\partial K_{4I}} = -\eta_{2I} \Omega_2 \delta_q, \\ \dot{Z}_{2D} &= -\eta_{2D} \frac{\partial V_2}{\partial K_{4D}} = -\eta_{2D} \Omega_2 \sigma_q, \end{aligned}$$

$$(37)$$

where η_{1p} , η_{1I} , η_{1D} , η_{2p} , η_{2I} , η_{2D} are the positive learning rates.

$$\dot{Z} = \xi M^T \Omega,$$
 (38)

where $\xi = diag(\eta_{3I}, \eta_{3P}, \eta_{3D}, \eta_{4I}, \eta_{4P}, \eta_{4D})$.

Remark 2. With on-line regulation, the control gain can be auto-adjustment as the system parameters change. Hence, the proposed RBFNN-PID controller can overcome the drawbacks of all off-line regulation methods and show good performance while ignoring the uncertainty of the system parameters.

$$u_{2s} = \begin{bmatrix} -\alpha_3 \times \operatorname{sgn}(s_3) \\ -\alpha_4 \times \operatorname{sgn}(s_4) \end{bmatrix}$$
(39)

4.2. NN Compensator in RBFNN-PID

RBFNN is an efficient feedforward neural network, which has the characteristics of good approximation and generalization performance, a simple structure and fast learning speeds [28,29]. RBF neural network is used in the compensator, but it is not suitable for the multilayer neural network proposed in references [30–32]. The main structure of the RBFNN shown in the orange frames of Figure 1 consists of three layers [33]: an input layer with five variables, an output layer, u^* , and a hidden layer governed by a Gaussian function.

$$V^* = V_{qds} + u^*. (40)$$



Figure 1. PID control diagram of the RBF neural network.

Layer one is the input layer. In this layer, inputs *x* are to be used in the next layer.

$$\begin{aligned} x &= \begin{bmatrix} \int_0^t i_d & i_d & \delta_d & e_d & \dot{e}_d \int_0^t i_q & i_q & \delta_q & e_q & \dot{e}_q \end{bmatrix}, \\ x &= \begin{bmatrix} \int_0^t i_d & i_d & \delta_d & e_d & \dot{e}_d \int_0^t i_q & i_q & \delta_q & e_q & \dot{e}_q \end{bmatrix}, \end{aligned}$$
(41)

Layer two is the hidden layer—this layer consists of a series of computational cells of hidden neurons. Each neuron is activated by an RBF. The output of the hidden layer is computed by:

$$h_j(x,c,d) = \exp(-\frac{\|x-c_j\|^2}{2d_j^2}), j = 1...m,$$
(42)

where *m* is the number of neurons; $c_j = \begin{bmatrix} c_{j1} & c_{jn} \end{bmatrix}$ is the center vector of neuron *j*; d_j is the standard deviation of the *j*th RBF, $d = \begin{bmatrix} d_1 & d_m \end{bmatrix}^T$; and h_j is the Gaussian function for neuron *j*.

Layer three is the export layer. The output indicator at this level is a linear weighted portfolio:

$$f(x) = \sum_{j=1}^{m} W_{ji} h_j(x, c, d), i = 1 \dots n,$$
(43)

where W_{ji} refers to the weight, which connects the *jth* hidden node to the *ith* output, and *n* is the number of inputs.

In the designed neural network compensator, the input signal from layer one is the referred track vector, and the output from layer three is used for modeling difference, external disturbance and no modeling part. The NN compensator is used to create the non-linear projections between the referred track and the non-modeled dynamics, but it cannot achieve the whole optimal approximation. The center vector *c* and the standard deviation *d* are unchanged within the reference trajectory and the number of neurons. Because the radial basis function has the ability of nonlinear approximation, the best approximation u^* can be described by:

$$u^* = f^*(x) - \varepsilon_2 = W^* h(x) - \varepsilon_2, \tag{44}$$

where $f^*(x)$ is the output vector from the hidden layer; W^* is the optimal weight value vector; and ε_2 is a minimum approximating error. Due to the characteristics of the RBFNN, the following practical assumptions hold.

Assumption 1. The approximation error ε_2 is a small real constant. If the hidden layer has enough neurons, that is, the absolute value of ε_2 can be any small number, i.e.,

$$\hat{f}(x) = \hat{W}h(x),\tag{45}$$

$$u^* = \hat{f}(x) + Wh(x) - \varepsilon_2. \tag{46}$$

There is an optimal value u_{nn} *that satisfies the following conditions* u^* *:*

$$\begin{cases} u^* + f_d \le \varepsilon_1 \\ u^*(e+\delta+\sigma) \le 0 \\ (e+\delta+\sigma)(u^*+f_d) \le \varepsilon \end{cases}$$
(47)

$$\hat{f}(x) + \tilde{W}h(x) + f \le \varepsilon_1 + \varepsilon_2 = \varepsilon,$$
(48)

where $\widetilde{W} = W^* - \hat{W}$ refers to the estimation error of the weight vector. u_{nn} from Equation (11) satisfies the condition as:

$$u_{nn} = \hat{f}(x) - v \tanh\left\lfloor \frac{v}{\sigma + e + \delta} \right\rfloor v > 0,$$

$$\dot{\hat{W}}_{i} = -\Theta_{i}h_{i}p, i - 1, 2, \dots m,$$

$$p = \delta + e + \sigma,$$

(49)

where $\Theta_i = diag[\Theta_1, \Theta_2 \dots \Theta_m]$ is a positive symmetry theorem.

4.3. Stability and Analysis

To analyze system stability, the tracking theorem is as follows:

Theorem 1. Regarding the dynamic error system represented by Equation (16). On the condition of applying with an adaptive PI + RBFNN-PID current controller, Equation (23), which having adaptive tuning method, Equation (26), the dynamic error system expresses asymptotically being stability.

Proof. The next equation can be deduced from Equations (16), (23), and (28):

$$\dot{s} = B(u_{PI} + u_s - u_{PI}^* + u_{PI}^* - u_{PI0}) = B(E\tilde{K} + u_s - \varepsilon),$$
(50)

where $\widetilde{K} = K - K^*$.

The control gain error is defined as follows:

$$\widetilde{K}_{1P} = K_{1P} - K^*_{1P}, \ \widetilde{K}_{1I} = K_{1I} - K^*_{1I}
\widetilde{K}_{2P} = K_{2P} - K^*_{2P}, \ \widetilde{K}_{2I} = K_{2I} - K^*_{2I}.$$
(51)

On the basis of Equations (50) and (51), the following Lyapunov candidate functions were selected:

$$V_{2}(t) = \frac{1}{2}s^{I}B^{-1}s + \frac{1}{\gamma_{1P}}K_{1P}^{2} + \frac{1}{\gamma_{1I}}K_{1I}^{2} + \frac{1}{\gamma_{1I}}K_{1I}^{2} + \frac{1}{\gamma_{2P}}\tilde{K}_{2P}^{2} + \frac{1}{\gamma_{2I}}\tilde{K}_{2I}^{2}$$
(52)

The Lyapunov function, $V_2(t)$, derivative of time is given by:

$$\dot{V}_{2}(t) = \frac{1}{2}s^{T}B^{-1}\dot{s} + \frac{1}{\gamma_{1p}}\tilde{K}_{1p}\dot{k}_{1p} + \frac{1}{\gamma_{1I}}\tilde{K}_{1I}\dot{k}_{1I}
+ \frac{1}{\gamma_{2p}}\tilde{K}_{2p}\dot{k}_{2p} + \frac{1}{\gamma_{2I}}\tilde{K}_{2I}\dot{k}_{2I}
= s^{T}B^{-1}B(E\tilde{K} + u_{s} - k) + \tilde{K}^{T}\phi^{-1}\dot{K}
= s^{T}(E\tilde{K} - \begin{bmatrix} \alpha_{1}\mathrm{sgn}(s_{1}) \\ \alpha_{2}\mathrm{sgn}(s_{2}) \end{bmatrix} - \varepsilon) - \tilde{K}^{T}\phi^{-1}\phi E^{T}s
= -\alpha_{1}|s_{1}| - \alpha_{2}|s_{2}| - \varepsilon_{1}s_{1} - \varepsilon_{2}s_{2}
\leq -(\alpha_{1} - |\varepsilon_{1}|)|s_{1}| - (\alpha_{2} - |\varepsilon_{2}|)|s_{2}|
\leq 0.$$
(53)

Using the adaptive PI controller, Equation (23), with adaptive tuning laws, Equation (26), for non-zero values, the relevant inequalities can be obtained for the tracking error vector \dot{s} , satisfied that $\dot{V}_2(t)$ is a negative semi-infinite function [i.e., $V_2(t) \leq V_2(0)$], and s and \tilde{K} must be bounded. The $\Omega(t)$ can be expressed as $\Omega(t) \equiv (\alpha_1 - |\gamma_1|)|s_1| + (\alpha_1 - |\gamma_1|)|s_2|$, and the following inequality can be obtained from Equation (23):

$$\int_{0}^{t} \Omega(\tau) d\tau \le V_{2}(0) - V_{2}(t), \tag{54}$$

Since $V_2(0)$ and $V_2(t)$ are bounded and non-increasing, the following inequalities are deduced to be:

$$\lim_{t \to \infty} \int_0^t \Omega(\tau) d\tau \le \infty.$$
(55)

Meanwhile, as long as *s* is bounded, Equation (25) indicates that *V* is also bounded. Then, $\Omega(\tau)$ is uniform and continuous. By applying Barbalat's lemma [34], it can be found that $\lim_{t\to\infty} \Omega(\tau) = 0$. Therefore, $s \to 0$ as $t \to \infty$ and the adaptive PI + RBFNN-PID controller will keep asymptotic stability even if the parameters of the motor change and external load disturbance occurs.

Remark 3. It should be noted that the adaptive PI control strategy proposed in this paper is suitable for various electrical systems, and its mathematical form is shown in Equation (16). The general design process of the designed control strategy can be overviewed as follows.

Step one: Use the pole placement method [35,36] to select the initial value of the PI gain. Step two: Structure the decoupling control term u_{0d} , and term u_{0q} as Equation (14) and the supervision and control term u_s as Equation (29).

Step three: Organize the PI control term u_{PI} as Equation (20) with the self-adaptive control as Equation (26).

Step four: The desired laws from Equation (23) are obtained by combining the three controls in Equations (14), (20) and (29).

The stability analysis of RBFNN-PID is the same as the adaptive PI.

5. Experimental Validation

5.1. Drive System Settings

An experimental platform was set up with the core controller (TMS320F28335) from the TI company. The decoupling control of the PMSM was verified based on the current deviation control effect of the sliding mode control strategy. The program of the designed adaptive PI + RBFNN-PID control algorithm was followed as shown in Figure 2. The general design process of the control scheme was followed as shown in Figure 3, as proposed by F28335DSP, and the hardware was set up following the structure diagram of the all-digital control system based on the DSP as shown in Figure 4. The PMSM was a 400 W stepper motor drag model (YH57BYGH56). The PWM switching frequency of the DSP processor was set to 10 kHz, and the DC bus voltage provided by the output DC regulated power supply was set to 30V. The EPWM and RC filter circuit equivalent for the analog-to-digital conversion chip (ADC) and current analog signal output to the oscilloscope. The given parameters from the SPMSM controller are shown in Table 1.



Figure 2. The program of the designed adaptive PI + RBFNN-PID control algorithm.



Figure 3. General structure diagram of the sPMSM drive system using the designed adaptive PI + RBFNN-PID controller.



Figure 4. Hardware design of the permanent magnet synchronous motor control system based on DSP.

Parameter	Symbol	Value
Rated power	P_e	400 W
Rated phase-to-phase voltage	V_r	220 V
Rated phase current	Ir	2.8 A
Rated torque	T_r	2.7 N.M
Number of poles	P	8
Stator resistance	R_s	2.875 Ω
Stator inductance	L_d , L_q	0.22 mH, 0.61 mH
Magnet flux	ψ_f	0.085 V·s/rad
Equivalent inertia	Ĭ	$0.0018 \text{ kg} \cdot \text{m}^2$
Viscous friction coefficient	В	0.0002 N·m·s/rad

Table 1. Nominal SPMSM Parameters.

5.2. Research Program

To evaluate the characteristics of the theory and application of the proposed control strategy, it was tested under two research scenarios including susceptible load torque and under inductance parameter variations. The adjusting performance of the designed control strategy was evaluated by the current response time in response to stepwise changes in load torque. In addition, the robust nature of the motor parameters to the control system was verified by the magnitude of current fluctuation as the electrical parameters vary with the temperature and stator current during system operation.

5.3. Experimental Results

Scenario One: In this scenario, the given speed (ω_d) was set to 2000 r/min with inductance parameters of $L_d = 1.2 \hat{L}_d$, $L_q = 0.8 \hat{L}_q$. At 0.3 s, the load torque (T_L) was suddenly changed from 3 N.m to 6 N·m. Figure 5 shows the experimental waveform of the designed adaptive PI + RBFNN-PID controller is compared with the conventional PI controller experimental waveform shown in Figure 6. Figures 5 and 6 show the changes by the d-axis stator current (i_{ds}) and q-axis current (i_{qs}). It was found from Figures 5 and 6 that after applying the adaptive whole law, the adjustment performance of the traditional PI + PID control system was apparently improved. That is, the proposed control scheme stabilized quickly with a fast dynamic time response (settling time: 123 ms) in the case of sudden changes of load torque. Conversely, as can be seen from Figure 6, the conventional PI + PID controller still performed poorly with the load torque step changes due to the adjusting time of 417 ms and poor waveform. It is worth noting that the gain of the conventional PI + PID controller can be adjusted to rated parameters through widely simulation several times. As shown in Figure 6, the stability performance varies widely because it lacks the NN tuning that enhances system stability under parameter uncertainty. What is more, under the condition of the same variation of motor inductance parameters, the fluctuation range of the current in Figure 5 is much smaller than the fluctuation range of the current in Figure 6, which shows the robustness of the proposed control strategy to parameter changes. Scenario Two: In this scenario, the value of the given speed (ω_d) was set to 2000 r/min with inductance parameters of $L_d = 0.8L_d$, $L_q = 1.2L_q$. At 0.6 s the load torque (T_L) suddenly changed from 6 N·m to 3 N·m under system motor inductance parameter variations. From Figures 7 and 8, the experimental waveform of the designed adaptive PI + RBFNN-PID controller is compared with that of the conventional PI controller. In detail, Figures 7 and 8, each display the changes of the d-axis stator current and q-axis stator current. In these data, the proposed adaptive PI + RBFNN-PID control scheme (regulation time: 313 ms) had a faster dynamic performance than the traditional PI + PID control scheme (regulation time: 441 ms), which shows very poor stability under the parameter uncertainties and load torque step. What is more, under the condition of the same variation of motor inductance parameters, the fluctuation range of the current in Figure 7 is much smaller than the fluctuation range of the current in Figure 8. At the same time, this shows the robustness of the proposed control strategy to parameter changes.



Figure 5. The validation results of the adaptive PI + RBFNN-PID control for the abrupt load torque change of system parameters under inductance parameters $L_d = 1.2\hat{L}_d$, $L_q = 0.8\hat{L}_q$. The top plot displays the *q*-axis stator current (i_{qs}), and the bottom plot displays the *d*-axis stator current (i_{ds}).



Figure 6. The validation results of the traditional PI + PID control for the abrupt load torque change of system parameters under inductance parameters $L_d = 1.2\hat{L}_d$, $L_q = 0.8\hat{L}_q$. The top plot displays the *q*-axis stator current (i_{qs}), and the bottom plot displays the *d*-axis stator current (i_{ds}).



Figure 7. The validation results of the adaptive PI + RBFNN-PID control strategy for the load torque of the system abruptly changing under inductance parameters $L_d = 0.8\hat{L}_d$, $L_q = 1.2\hat{L}_q$. The top plot displays the *q*-axis stator current (i_{qs}), and the bottom plot displays the *d*-axis stator current (i_{ds}).



Figure 8. The validation outcomes of the traditional PI + PID control strategy for the load torque of the system abruptly changing under inductance parameters $L_d = 0.8\hat{L}_d$, $L_q = 1.2\hat{L}_q$. The top plot displays the *q*-axis stator current (i_{qs}), and the bottom plot displays the *d*-axis current (i_{ds}).

6. Conclusions

In this study, an adaptive PI + RBFNN-PID control strategy for current was designed for PMSM drives using a simple and easy control algorithm. This paper presents an adaptive tuning method, which can automatically adjust the gain of PI+ PID controls so as to obtain a good current response performance. The method used the gradient descent adaptive tuning method. Therefore, the control scheme proposed in this paper can ensure the accuracy and rapidity of current in the case of system inductor parameter changes and load interference from outside. The control system stability was analyzed exhaustively. The effectiveness of the control strategy was verified through experiments. As a comparison, the traditional PI + PID controller and proposed controller were tested under the same conditions. The experimental results showed that compared with the traditional PI + PID control method, the proposed adaptive PI + RBFNN-PID control algorithm significantly improved control performance. The main results of the study are the following:

- 1. A new adaptive PI + RBFNN-PID control strategy was proposed, and detailed design steps were given.
- 2. The Lyapunov method provided mathematical proof of control system stability, zero convergence and the pertinent lemmas.
- 3. We verified the adaptive PI + RBFNN-PID control method and showed that we tested the adaptive PI + RBFNN-PID control scheme and the SPMSM driver can accurately track the speed under the change of motor parameters and external load disturbance.
- 4. The results were given and the traditional PI + PID controller results were compared. Currently, many researchers are developing new PI + PID gain analysis and tuning methods, and the proposed adaptive PI + RBFNN-PID control method contributes to reducing the difficulty of these tasks.

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