

## Article

# Distributionally Robust Optimization of an Integrated Energy System Cluster Considering the Oxygen Supply Demand and Multi-Energy Sharing

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**Abstract:** Regional integrated energy systems (IESs) have emerged to satisfy the increasing diversified energy demand in Tibet. However, limited resource allocation of a given IES can occur because of the uncertainty in the output and prediction error of distributed renewable energy (*DRE*). A distributionally robust optimization (DRO) model was proposed for the joint operation of multiple regional IESs, and multi-energy sharing and multi-energy flow coupling of electricity, heat, and oxygen were considered. The probability distribution of the *DRE* output was described using 1–norm and  $\infty$ –norm constraints, and the minimum operating cost under adverse scenarios was determined through DRO. Furthermore, on the premise of ensuring cluster profit, a pricing mechanism of the energy supply within the cluster was proposed. Finally, a typical model involving eight cases was established and analyzed. The results revealed that multi-energy sharing and multi-energy flow coupling improved the economy of IES cluster operation and realized the coordination of robustness and economy. The energy supply price within the cluster enhanced enthusiasm on the demand side.

**Keywords:** electricity; heat and oxygen; multi-energy sharing; double-norm constraints; distributionally robust optimization; pricing mechanism within the cluster



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## 1. Introduction

Altitude stress due to hypoxia has greatly affected the health and quality of life of residents in plateau areas. The government and researchers have explored how to solve the plateau oxygen supply problem. Tibet has proposed a universal oxygen supply in plateau urban areas as a development goal [1–3]; China has promoted and is working toward emission peak and carbon neutrality targets. As a clean energy base, Tibet has proposed a series of energy development plans. However, it is limited by inefficient energy utilization and increasing penetration of distributed renewable energy (*DRE*); the increasing electric and oxygen demand and low absorption rate of *DRE* pose new challenges to energy system construction in Tibet.

As a new energy system to promote sustainable energy development, an integrated energy system (IES) could effectively improve energy utilization efficiency while meeting diversified energy demands within the system. Compared with the existing energy framework in Tibet, the combination of source-network-load-storage modular interactions and integrated interactions in IESs has significantly altered the construction of energy systems and improved power grid resilience, and these benefits can be harnessed to meet the unique demand for a dispersed oxygen supply on the plateau. However, multi-energy flow coupling and the existence of multiple time scales result in IES operation difficulties. Current research mainly focuses on the optimal strategy of a single IES. In [4], system

investment and operation costs were reduced by considering source storage capacity allocation and operation optimization. In [5–7], power-to-gas (*P2G*) technology was used to realize the consumption of renewable energy and improve the economic benefits of the system. In [8,9], a dynamic energy hub and planning model was built, and an optimal planning and operation scheme of the IES was achieved. However, there is little research on the optimal scheduling problem of IES clusters. The existing research on *P2G* mainly focuses on the hydrogen energy of power-to-hydrogen (*P2H*) units and methanated natural gas utilization, but there is no research on *P2H* oxygen utilization in the *P2G* process.

Relevant research on plateau oxygen supply has shown that the feasibility and economic benefits of the vacuum pressure swing adsorption (*VPSA*) method in plateau areas are greater than those of the cryogenic air and membrane separation methods [10–12]. However, the disparities between oxygen supply demand, electric demand, and electric supply are becoming more pronounced as Tibet's economy continues to develop. The efficient use of energy cannot be facilitated by *VPSA* oxygen supply alone. Therefore, this study investigates a more effective oxygen supply mode that reduces *VPSA*'s electricity requirements.

The resource allocation capacity of a single IES is limited. The limitations of the energy framework create problems such as uncertainty in the *DRE* output, prediction error [13], and low consumption rates. Scholars have proposed combining multiple regional IESs, forming an alliance mechanism through multiple regional IESs, and building an IES cluster scheduling system. Energy sharing interactions among IESs could be realized to improve energy utilization efficiency and energy supply levels, achieve the best overall benefits, and reduce the impact of the energy framework on system scheduling. However, existing methods for the operation of multiple IESs do not accurately capture system operation characteristics in real time or highlight energy sharing among clusters [14]. Therefore, an IES cluster needs to account for the collaborative multi-energy interactions between multiple IESs, but the current study focuses on electricity sharing [15].

*DRE* output uncertainty significantly affects power system safety and economy. Currently, the main methods targeting uncertainty in power systems are stochastic optimization (SO) [16–18] and robust optimization (RO) [19–21]. However, SO and RO have shortcomings. Scholars have used distributionally robust optimization (DRO) to address uncertainty [22–24]. DRO is based on historical data and can be employed to determine the uncertainty set containing possible distributions and obtain the optimal solution when the prediction error of uncertainty factors follows the worst probability distribution. Through correlation transformation, the DRO can be converted into a deterministic mixed integer linear programming (MILP) model. This model can be directly solved by using Gurobi. Many studies have examined DRO applications in the IES [25–28], but DRO has not been applied in IES cluster optimization. Due to the difficulty of controlling electricity, heat, and oxygen coupling and the coordination and synergy among multiple clusters, IES clusters are highly uncertain. It is difficult to address IES cluster uncertainty using conventional RO and SO techniques. Therefore, research on IES cluster operation based on DRO is critical.

In this study, a DRO strategy for IES clusters was proposed, which considered the oxygen supply demand in plateau areas and multiple energy sharing. Under both 1– norm and  $\infty$ – norm constraints, a scheduling strategy for coordinating system robustness and model economy was constructed through multiple energy sharing mechanisms. The main contributions of this paper are as follows:

- (1) Based on the energy demand, energy framework and energy development planning in Tibet, a multi-energy flow coupling IES architecture of electricity, heat, oxygen, and other energy sources was established by coupling concentrated solar power (*CSP*), *P2H*, and other equipment.
- (2) The scenario uncertainty was described by combining the uncertainty probability distribution confidence set constrained by both the 1– norm and  $\infty$ – norm, and the worst scenario probability distribution was determined.

- (3) To minimize the IES cluster operation cost, a cooperative optimization strategy considering IES cluster robustness and economy was established through double-norm constraints and multiple energy sharing mechanisms. Furthermore, the comprehensive model effect was verified by comparing several cases.

The remainder of this paper is organized as follows: Section 2 introduces the IES cluster, Section 3 describes the structure and operation strategy of the two-stage DRO model, Section 4 presents the optimization framework, data, and model simulation results, and Section 5 summarizes the main findings, relevant limitations, and further research directions.

## 2. IES Cluster

### 2.1. IES Architecture

The IES architecture is shown in Figure 1. Dispatching of a single IES typically involves controllable units (*CSP*, hydropower (*HP*), *P2H*, hydrogen fuel cells (*HFC*), *VPSA*, demand response load, an electric furnace (*EF*), and other units), uncontrollable units (distributed wind/photovoltaic energy units, hydrogen charging stations, etc.), and energy storage equipment (hydrogen gas storage (*HGS*), etc.). To satisfy the energy demand and emission peak and carbon neutrality targets, a dispatching center was set up in the proposed regional IES to couple the various equipment and energy sources and convert the various renewable energy sources, such as external electric energy and hydrogen energy, into the required energy sources.

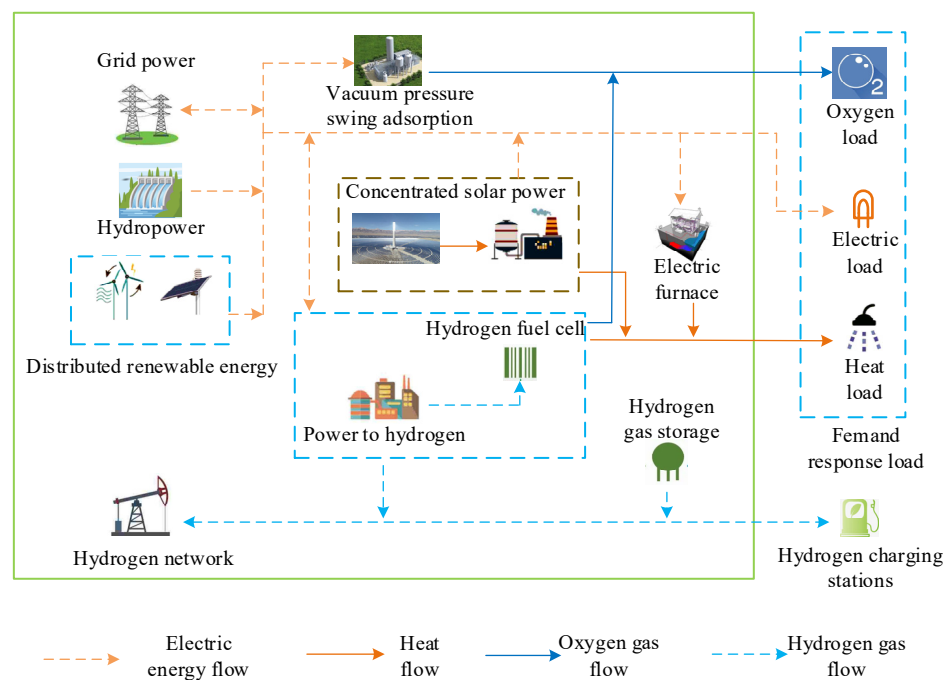


Figure 1. IES architecture.

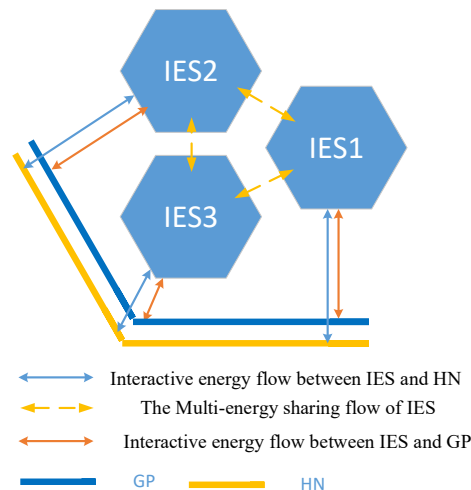
*P2H* and methanation reactors were included as traditional power-to-gas technology options, and the low efficiency of methanation reactors and carbon emissions associated with natural gas consumption were considered. Following the energy development plan of Tibet, this paper proposed the utilization of oxygen and hydrogen in *P2H* products according to local conditions. The heat supply was replaced by *HFC*, *EF*, and *CSP* units. Oxygen was supplied by collecting *P2H* oxygen combined with *VPSA* technology. Hydrogen was used by hydrogen charging stations, which could provide hydrogen energy for hydrogen internal combustion electric vehicles (HICEVs), and HICEVs were included among the buses, taxis, and official vehicles used in urban areas. This plan would not only

reduce carbon emissions, but also improve energy utilization efficiency and promote the consumption of the output of distributed wind/photovoltaic energy systems.

A dispatching center was used to coordinate and control the IES aggregation unit. Following the real-time situation of electric and hydrogen energy demands, this approach can implement energy sharing interactions among clusters, and excess electric energy or hydrogen can be sold to the grid power (GP) or hydrogen networks (HN), respectively. Figure 1 shows that the load of the IES cluster can be categorized into uncontrollable and demand response loads. Among these loads, an uncontrollable load is the load whose use considerably influences the demand side and cannot be controlled, for example, electric lights or computers. The demand response load can be categorized into transferable and adjustable loads. The adjustable load includes equipment that functions intermittently, e.g., water boilers and humidifiers. The transferable load refers to the load of other household equipment that can be transferred to other periods of work, for example, centralized laundry units and dishwashers. Considering that the transfer of electrical and heat loads slightly impacts the oxygen supply demand, only the adjustable amount was considered for the oxygen load.

## 2.2. Multi-Energy Sharing Architecture

The multi-energy sharing architecture of the IES cluster is shown in Figure 2. The sharing of electricity, oxygen, and hydrogen was included. However, due to the high heat pipe loss, heat interaction among IES clusters was not considered. The IES multi-energy interaction flow is based on traditional electric energy interactions. Energy sources such as oxygen and hydrogen are shared at very low transmission loss and can not only replace the role of energy storage to a certain extent, but also ensure deeper energy sharing among IES clusters, thus effectively improving the overall cluster scheduling flexibility.



**Figure 2.** Multi-energy sharing architecture.

To satisfy the demand for multiple types of energy loads, optimization of the dispatch of IES clusters is critical. However, uncontrollable units occur in the cluster, namely *DRE*, whose output uncertainty could adversely affect cluster scheduling.

## 2.3. Probability Scenario

In this study, 10 scenario and probability values were generated for each IES, based on 180 days of data through Copula joint scenario generation and the k-means clustering algorithm as the initial probability scenario generation method. The 1-norm and  $\infty$ -norm were simultaneously included to constrain the confidence set of the uncertainty probability distribution. The column and constraint generation (CCG) algorithm was used to design a DRO strategy for multiple cases, considering these double-norm constraints.

The relevant target values in the various cases were obtained via DRO, and the scenario probability values were modified according to the above double-norm constraints.

### 3. Distributionally Robust Optimization Model

The uncertainty in the DRE output and forecast error can adversely affect IES cluster planning and scheduling. Therefore, based on the above double-norm constraints, considering the energy demand in Tibet and the emission peak and carbon neutrality targets, a new IES cluster planning and scheduling strategy was constructed.

#### 3.1. Objective Function

The model was optimized considering the IES cluster. When the cluster economy and robustness are coordinated through DRO, the objective function is as follows:

$$\min \left\{ f_b^r + \max \sum_{i=1}^K \left( p_i^{T+1} \min f_r^i \right) \right\} \quad (1)$$

where  $p_i^T$  denotes the scenario probability value,  $f_b^r$  denotes the comprehensive equipment cost, and  $f_r^i$  denotes the total operation cost.

Following Equation (1), the objective function is the min–max–min form of DRO. In contrast to RO (RO can only optimize worst-scenario problems), DRO can solve worst-scenario one-stage planning schemes through the lower bound, estimate the economy of operation through  $\min f_r^i$ , determine the worst operation scenario that the cluster may encounter through  $\min f_r^i$ , and update the scenario probability value. The robustness and economy can be coordinated through continuous iteration.

The comprehensive cost  $f_b^r$  and operation cost  $f_r^i$  of the equipment are included in Equations (2) and (3), which can be calculated as follows:

$$\begin{cases} f_b^r = \frac{f_b}{(5 \cdot 365 \cdot (1+r))} \\ f_r^i = f_e^i + f_h^i + f_{DR}^i + f_{DRE}^i + f_{ES}^i \end{cases} \quad (2)$$

$$f_b = \sum_{i=1}^K \left( \begin{array}{l} P_{ri.CSP} M_{CSP}^i + P_{ri.P2H} M_{P2H}^i + P_{ri.hs} M_{hs}^i + P_{ri.VPSA} M_{VPSA}^i + \\ P_{ri.pip} L_{pip}^i + P_{ri.HP} M_{HP}^i + P_{ri.DRE} M_{DRE}^i + P_{ri.EF} M_{EF}^i + P_{ri.HFC} M_{HFC}^i + C_{HRS}^i \end{array} \right) \quad (3)$$

where  $P_{ri.CSP}$  denotes the unit comprehensive cost of CSP units (RMB/kW),  $P_{ri.P2H}$  denotes the unit comprehensive cost of P2H units (RMB/kW),  $P_{ri.hs}$  denotes the unit comprehensive cost of HGS units (RMB/m<sup>3</sup>),  $P_{ri.VPSA}$  denotes the unit comprehensive cost of VPSA technology (RMB/kW),  $P_{ri.pip}$  denotes the unit comprehensive cost of transmission pipelines (RMB/km),  $P_{ri.HP}$  denotes the unit comprehensive cost of HP (RMB/kW),  $P_{ri.DRE}$  denotes the unit comprehensive cost of DRE (RMB/kW),  $P_{ri.EF}$  denotes the unit comprehensive cost of EFs (RMB/kW),  $P_{ri.HFC}$  denotes the unit comprehensive cost of HFCs (RMB/kW),  $M_{P2H}^i$  denotes the P2H installed capacity,  $M_{hs}^i$  denotes the HGS installed capacity,  $M_{CSP}^i$  denotes the CSP installed capacity,  $M_{VPSA}^i$  denotes the VPSA installed capacity,  $M_{HP}^i$  denotes the HP installed capacity,  $M_{DRE}^i$  denotes the DRE installed capacity,  $M_{EF}^i$  denotes the EF installed capacity,  $M_{HFC}^i$  denotes the HFC installed capacity,  $L_{pip}^i$  denotes the construction length of hydrogen and oxygen transmission pipelines, and  $C_{HRS}^i$  denotes the cost of transforming gas stations into hydrogen charging stations, where  $f_e^i$  denotes the electricity purchase and sale cost from the GP,  $f_h^i$  denotes the hydrogen gas purchase and sale cost from the HN,  $f_{DR}^i$  denotes the cost of the demand response,  $f_{ES}^i$  denotes the cost of using energy storage, and  $f_{DRE}^i$  denotes the cost of discarding solar and wind energy.

(1) The electricity purchase and sale cost can be calculated as follows:

$$f_e = \sum_{t=1}^{24} \left( P_{ribuy}^t P_{buy.e}^t - P_{risell}^t P_{sell.e}^t \right) \quad (4)$$

where  $P_{ribuy}^t$  denotes the electric purchase price,  $P_{buy.e}^t$  denotes the electric purchase amount,  $P_{sell.e}^t$  denotes the electric sale amount, and  $P_{risell}^t$  denotes the electric sale price.

(2) The hydrogen gas purchase and sale cost can be calculated as follows:

$$f_h = \sum_{t=1}^{24} \left( P_{ri.h}^t P_{h.buy}^t - \delta_h P_{ri.h}^t P_{h.sell}^t \right) \quad (5)$$

where  $P_{ri.h}^t$  denotes the hydrogen purchase price,  $P_{h.buy}^t$  denotes the hydrogen purchase amount,  $P_{h.sell}^t$  denotes the hydrogen sale amount, and  $\delta_h$  denotes the conversion coefficient of the purchase price.

(3) The demand response cost can be calculated as follows:

$$f_{DR} = \delta_{tr} \sum_{t=1}^{24} (P_{tr}^t + H_{tr}^t) + \delta_{cut} \sum_{t=1}^{24} (P_{cut}^t + H_{cut}^t + O_{cut}^t) \quad (6)$$

where  $\delta_{tr}$  denotes the demand-side translation cost conversion coefficient and  $\delta_{cut}$  denotes the demand-side adjustment cost conversion coefficient.

(4) The cost of using energy storage can be calculated as follows:

$$f_{DRE} = \delta_{DRE} \sum_{t=1}^{24} (P_{P.DRE}^t - P_{DRE}^t) \quad (7)$$

where  $\delta_{DRE}$  denotes the conversion coefficient of discarding solar and wind energy,  $P_{P.DRE}^t$  denotes the DRE supply, and  $P_{DRE}^t$  denotes the DRE consumption electric power.

(5) The solar and wind costs can be calculated as follows:

$$f_{ES} = \delta_{HS} \sum_{t=1}^{24} (P_{HS.ch}^t + P_{HS.dis}^t) + \delta_{hs} \sum_{t=1}^{24} \rho_h (V_{hs.ch}^t + V_{hs.dis}^t) \quad (8)$$

where  $P_{HS.ch}^t$  denotes the charging heat power,  $P_{HS.dis}^t$  denotes the discharging heat power,  $V_{hs.ch}^t$  denotes the charging hydrogen volume,  $V_{hs.dis}^t$  denotes the discharging hydrogen volume,  $\delta_{HS}$  denotes the heat storage (HS) cost per unit power, and  $\delta_{hs}$  denotes the hydrogen storage cost per unit volume.

### 3.2. P2H-VPSA Combined Oxygen Supply Model

The overall product utilization efficiency of P2G is low, and the utilization of oxygen in the P2H process has not been previously considered. Therefore, P2H was combined with HFC, HS, and VPSA units. The hydrogen generated by P2H could be used by HFCs, HS units, and hydrogen charging stations, and the generated oxygen could be used combined with the VPSA, oxygen storage, and oxygen supply loads to achieve efficient product utilization and partially meet oxygen supply requirements.

(1) The P2H model can be expressed as follows:

$$\begin{cases} P_{EL.h}^t = \eta_{P2H} P_{EL}^t \\ V_{EL.h}^t = P_{EL.h}^t / P_{H.e} / \rho_h \\ V_{EL.O}^t = \eta_{P2H} P_{EL}^t / P_{O.e} / \rho_O \\ 0 \leq P_{EL}^t \leq M_{P2H} \\ \Delta P_{EL}^{lp} \leq P_{EL}^t - P_{EL}^{t-1} \leq \Delta P_{EL}^{up} \end{cases} \quad (9)$$

where  $P_{EL,h}^t$  and  $P_{EL}^t$  denote the hydrogen production power and electric power consumption, respectively, at the  $P2H$  stage (kW);  $V_{EL,h}^t$  denotes the volume of hydrogen produced via  $P2H$  ( $m^3/h$ );  $\eta_{P2H}$  denotes the  $P2H$  energy conversion efficiency;  $\rho_O$  denotes the oxygen density;  $P_{H,e}$  denotes the power consumption for hydrogen production per unit mass (kW/kg);  $V_{EL,O}^t$  denotes the  $P2H$  oxygen production volume;  $P_{O,e}$  denotes the power consumption for oxygen production per unit mass;  $M_{P2H}$  denotes the  $P2H$  installed capacity;  $P_{EL}^{\min}$  denote the electric power limit of  $P2H$ ; and  $\Delta P_{EL}^{up}$  and  $\Delta P_{EL}^{lp}$  denote the  $P2H$  limits of climbing power.

The thermoelectric ratio of HFCs can be adjusted to increase flexibility. The HFC model can be expressed as follows:

$$\begin{cases} P_{HFC,e}^t = \eta_{HFC} P_{HFC,h}^t \\ V_{HFC,h}^t = \eta_{H,e} P_{HFC,h}^t / P_{H,e} / \rho_H \\ P_{HFC,h}^{\min} \leq P_{HFC,h}^t \leq P_{HFC,h}^{\max} \\ 0 \leq P_{HFC,h}^t \leq M_{HFC} \\ \eta_{e,H}^{\min} P_{HFC,e}^t \leq P_{HFC,H}^t \leq \eta_{e,H}^{\max} P_{HFC,e}^t \\ \Delta P_{HFC,H}^{lp} \leq P_{HFC,H}^t - P_{HFC,H}^{t-1} \leq \Delta P_{HFC,H}^{up} \end{cases} \quad (10)$$

where  $P_{HFC,h}^t$  denotes the hydrogen consumption power of HFCs (kW),  $\eta_{HFC}$  denotes the energy conversion efficiency of HFCs,  $P_{HFC,e}^t$  denotes the HFC electric power (kW),  $P_{HFC,H}^t$  denotes the HFC heat power (kW),  $V_{HFC,h}^t$  denotes the hydrogen consumption volume of HFCs ( $m^3/h$ ),  $\eta_{e,H}^{\max}$  and  $\eta_{e,H}^{\min}$  denote the heat power limit coefficients,  $\Delta P_{HFC,H}^{up}$  and  $\Delta P_{HFC,H}^{lp}$  denote the HFC limits of climbing power, and  $M_{HFC}$  denotes the HFC installed capacity.

(2) The VPSA model can be expressed as follows:

$$\begin{cases} V_{VPSA}^t = \eta_{VPSA} P_{VPSA}^t / P_{VPSA,e} \\ P_{VPSA}^{\min} \leq P_{VPSA}^t \leq M_{VPSA} \\ \Delta P_{VPSA}^{lp} \leq P_{VPSA}^t - P_{VPSA}^{t-1} \leq \Delta P_{VPSA}^{up} \end{cases} \quad (11)$$

where  $P_{VPSA}^t$  denotes the VPSA power (kW),  $\eta_{VPSA}$  denotes the highest economic efficiency of oxygen production,  $P_{VPSA,e}$  denotes the unit power consumption ( $kW/m^3$ ),  $V_{VPSA}^t$  denotes the oxygen generation volume ( $m^3/h$ ),  $P_{VPSA}^{\max}$  and  $P_{VPSA}^{\min}$  denote the VPSA power limits, and  $\Delta P_{VPSA}^{up}$  and  $\Delta P_{VPSA}^{lp}$  denote the VPSA limits of climbing power.

### 3.3. Oxygen Load Model

The oxygen load is based on the unit volume of oxygen delivery required to correct the altitude from 3000 to 1000 m, and the electrical and heat loads can be considered to correct the building volume at the oxygen supply site. This ensures that the oxygen load can meet the oxygen supply requirements with a flexible response; please refer to [12].

(1) To simplify the calculation, the oxygen supply mode was divided into two cases based on the electrical and heat loads. When the electrical or heat load increases, it can be considered that there exists a new oxygen supply demand, the increment in the electrical or thermal load can be set to the oxygen delivery mode, and the invariant can be set to the maintenance mode. When the electrical or heat load decreases, it can be considered that there is no new oxygen supply demand, and the oxygen maintenance mode can be set. The oxygen delivery amount in the maintenance mode is the escape amount of oxygen. The oxygen load can be calculated as follows:

$$\begin{cases} V_{O_2} = w(\Delta_e) / \eta_{e,a} h C_{O_2} + (1-w)(\Delta_h) / \eta_{h,a} h C_{O_2} \\ \Delta_e = P \left( P_L^t - P_L^{t-1} \right) \\ \Delta_h = P \left( H_L^t - H_L^{t-1} \right) \end{cases} \quad (12)$$

$$O_L^t = w(P_L^t - P_{LB}^t) / \eta_{e.a} \cdot h \cdot C_{O_2} \cdot \eta_{esc} + (1 - w)(H_L^t - H_{LB}^t) / \eta_{h.a} \cdot h \cdot C_{O_2} \cdot \eta_{esc} + V_{O_2} \quad (13)$$

where  $V_{O_2}$  denotes the oxygen volume in the supply mode ( $m^3/h$ );  $P(\bullet)$  denotes the preserved positive numbers in the matrix;  $P_L^t$  denotes the electrical load;  $P_{LB}^t$  denotes the electrical load without the oxygen supply demand;  $H_L^t$  denotes the heat load;  $H_{LB}^t$  denotes the heat load without the oxygen supply demand;  $w$  denotes the weight, which is 0.5 in winter and 1 in the other seasons;  $\eta_{e.a}$  denotes the electricity consumption per unit area ( $W/m^2$ );  $\eta_{h.a}$  denotes the heat consumption per unit area ( $W/m^2$ ) (Table 1);  $C_{O_2}$  denotes the amount of oxygen delivered per unit area;  $h$  denotes the height of a single-story building, which is 3 m; and  $\eta_{esc}$  denotes the oxygen escape amount, which is 50%. Table 1 provides the conversion coefficient between the power or heat supply and unit area.

**Table 1.** Oxygen load-related parameters.

	Unit ( $W/m^2$ )		
	IES1	IES2	IES3
$\eta_{e.a}$	225	300	330
$\eta_{h.a}$	80	90	80

(2) The amount of oxygen delivered per unit area can be obtained as follows:

$$\begin{cases} C_{O_2} = \frac{m_0}{\rho_{O_2}^t} \\ m_0 = m_1 - m \end{cases} \quad (14)$$

where  $m_0$  denotes the oxygen content to be delivered ( $m^3/h$ ),  $t$  denotes the time,  $m_1$  denotes the corrected oxygen mass content, and  $m$  denotes the oxygen mass content before correction.

$$\begin{cases} m = \rho_O \lambda \eta_O \\ \lambda = P/P_0 \\ \ln P = a \left( \frac{H}{10000} \right)^3 + b \left( \frac{H}{10000} \right)^2 + c \left( \frac{H}{10000} \right) + d \end{cases} \quad (15)$$

where  $\eta_O$  denotes the average proportion of oxygen in the atmosphere;  $P_0$  denotes the atmospheric pressure at sea level;  $P$  denotes the atmospheric pressure at the current altitude;  $a$ ,  $b$ ,  $c$ , and  $d$  denote altitude correction factors (please refer to literature [29] for specific data); and  $H$  denotes the altitude.

$$\begin{cases} m_1 = \rho_O \lambda_1 \eta_O \\ \lambda_1 = P_1/P_0 \end{cases} \quad (16)$$

where  $H_1$  denotes the correct altitude of the target. Please refer to the literature 12 for specific data. Moreover,  $P_1$  denotes the correct atmospheric pressure of the target. Equation (15) can be employed to calculate  $\ln P$ .

### 3.4. CSP Assembly Unit and Energy Balance Constraints

Please refer to Equations (A1)–(A10) in Appendix A for the other equipment constraints.

(1) The heat fluid transmission loss at a CSP power plant is very low, so it was ignored. The CSP power plant constraints can be expressed as follows:

$$\begin{cases} P_{SF,HTF}^t + P_{HS,dis}^t = P_{HS,ch}^t + P_{CSP,H,e}^t \\ P_{SF,HTF}^t = \eta_{SF,HTF} S_{LP} D^t \rho_{P,LP} \\ P_{CSP,e}^t = \eta_{CSP} P_{CSP,H,e}^t \\ P_{CSP,H,e}^{min} \leq P_{CSP,H,e}^t \leq M_{CSP} \\ P_{CSP,H,e}^{lp} \leq P_{CSP,H,e}^t - P_{CSP,H,e}^{t-1} \leq P_{CSP,H,e}^{up} \end{cases} \quad (17)$$



where  $P_{SF,HTF}^t$  denotes the heat power of the heat collector to transfer the heated fluid;  $P_{CSP.H.e}^t$  denotes the CSP steam turbine heat power supply;  $\eta_{SF,HTF}$  denotes the photothermal efficiency of the heat collector;  $S_{LP}$  denotes the heat receiver area, at  $4 \times 1 \text{ m}^2$ ;  $D^t$  denotes the solar intensity;  $\rho_{P.LP}$  denotes the actual energy flow density irradiated to the heat receiver after superposition of the mirror surface;  $\eta_{CSP}$  denotes the steam turbine efficiency;  $P_{CSP.e}^t$  denotes the CSP electric power; and  $P_{CSP.H.e}^{lp}$  and  $P_{CSP.H.e}^{up}$  denote the CSP limits of climbing power.

(2) The CSP-HS constraints can be expressed as follows:

$$\left\{ \begin{array}{l} S_H^t = S_H^{t-1} + \eta_{SH}^{ch} P_{HS.ch}^t - (P_{CSP.H}^t + P_{HS.dis}^t) / \eta_{SH}^{dis} \\ S_H^{\min} \leq S_H^t \leq S_H^{\max} \\ p_{H.ch}^{\min} \leq P_{HS.ch}^t \leq \alpha_{H.ch} P_{H.ch}^{\max} \\ p_{H.dis}^{\min} \leq P_{HS.dis}^t \leq \alpha_{H.dis} P_{H.dis}^{\max} \\ \alpha_{H.dis} + \alpha_{H.ch} \leq 1 \\ S_H^{t=1} = S_H^{t=24} \\ (2 \leq t \leq 24) \end{array} \right. \quad (18)$$

where  $S_H^t$  denotes the HS capacity,  $S_H^{\max}$  and  $S_H^{\min}$  denote the limits of the HS capacity,  $\alpha_{H.dis}$  denotes the discharging heat power status parameters,  $\alpha_{H.ch}$  denotes the charging heat power status parameters,  $P_{H.ch}^{\max}$  and  $P_{H.ch}^{\min}$  denote the limits of the charging heat power,  $P_{H.dis}^{\max}$  and  $P_{H.dis}^{\min}$  denote the limits of the discharging heat power,  $\eta_{SH}^{ch}$  denotes the charging heat power efficiency,  $\eta_{SH}^{dis}$  denotes the discharging heat power efficiency, and  $P_{CSP.H}^t$  denotes the heat power supplied to the heat load.

(3) The energy balance constraints can be expressed as follows:

$$\begin{aligned} P_{CSP.e}^t + P_{HP}^t + P_{DER}^t + P_{HFC.e}^t + P_{buy.e}^t &= P_{sell.e}^t + P_{ia.e}^t + P_{EL.DR}^t + P_{EF.e}^t + P_{VPSA}^t + P_{EL}^t \\ P_{CSP.H}^t + P_{EF.H}^t + P_{HFC.H}^t &= P_{HL.DR}^t \\ V_{VPSA}^t + V_{EL.O}^t &= V_{OL.DR}^t + P_{ia.O}^t \\ V_{EL.h}^t + V_{hs.dis}^t + P_{h.buy}^t &= V_{HFC.h}^t + V_{hs.ch}^t + P_{h.sell}^t + P_{ia.h}^t \end{aligned}$$

$$s.t. \left\{ \begin{array}{l} 0 \leq P_{buy.e}^t \leq p_{buy.e}^{\max} \\ 0 \leq P_{sell.e}^t \leq p_{sell.e}^{\max} \\ 0 \leq P_{h.sell}^t \leq p_{h.sell}^{\max} \\ 0 \leq P_{h.buy}^t \leq p_{h.buy}^{\max} \\ p_{ia.e}^{\min} \leq P_{ia.e}^t \leq p_{ia.e}^{\max} \\ p_{ia.h}^{\min} \leq P_{ia.h}^t \leq p_{ia.h}^{\max} \\ p_{ia.O}^{\min} \leq P_{ia.O}^t \leq p_{ia.O}^{\max} \end{array} \right. \quad (19)$$

where  $P_{ia.e}^t$ ,  $P_{ia.O}^t$ , and  $P_{ia.h}^t$  denote the energy sharing of electric, oxygen, and hydrogen, respectively;  $P_{HP}^t$  denotes the HP electric power;  $P_{EF.H}^t$  denotes the EF heat power;  $P_{EF.e}^t$  denotes the EF electric power;  $P_{EL.DR}^t$ ,  $P_{HL.DR}^t$ , and  $V_{OL.DR}^t$  denote the electrical, heat, and oxygen loads, respectively, after the demand response;  $P_{buy.e}^{\max}$  and  $P_{sell.e}^{\max}$  denote the upper limit of electric purchase and sale;  $p_{h.sell}^{\max}$  and  $p_{h.buy}^{\max}$  denote the upper limit of hydrogen purchase and sale;  $p_{ia.e}^{\max}$  and  $p_{ia.e}^{\min}$  denote the electric sharing constraints;  $p_{ia.h}^{\max}$  and  $p_{ia.h}^{\min}$  denote the hydrogen sharing constraints; and  $p_{ia.O}^{\max}$  and  $p_{ia.O}^{\min}$  denote the oxygen sharing constraints.

### 3.5. Double-Norm Constraint Model

(1) With the initial probability distribution as the center, and the 1-norm and  $\infty$ -norm as the constraint conditions, the probability distribution values of the discrete case can be constrained, and their feasible regions are  $\Omega_1$  and  $\Omega_\infty$ , respectively.

$$\Omega = \begin{cases} p_i \geq 0, i = 1, 2, \dots, K \\ \sum_{i=1}^K p_i = 1 \\ \Pr\left\{\sum_{i=1}^K |p_i - p_i^0| \leq \theta_1\right\} \geq \alpha_1 \\ \Pr\left\{\max |p_i - p_i^0| \leq \theta_\infty\right\} \geq \alpha_\infty \end{cases} \quad (20)$$

where  $p_i$  denotes the scenario probability;  $\sum_{i=1}^K |p_i - p_i^0| \leq \theta_1$  denotes  $\Omega_1$  (1 - norm);  $\max |p_i - p_i^0| \leq \theta_\infty$  denotes  $\Omega_\infty$  ( $\infty$  - norm);  $\theta_1$  and  $\theta_\infty$  denote the maximum deviation values of the probability; and  $\alpha_1$  and  $\alpha_\infty$  denote the degree of confidence of the probability distribution values.

(2)  $\{P_k\}$  satisfies the following confidence levels according to the literature [29]:

$$\{P_k\} = \begin{cases} \Pr\left\{\sum_{i=1}^K |p_i - p_i^0| \leq \theta_1\right\} \geq 1 - 2Ke^{-\frac{2M\theta_1}{K}} \\ \Pr\left\{\max |p_i - p_i^0| \leq \theta_\infty\right\} \geq 1 - 2Ke^{-2M\theta_\infty} \end{cases} \quad (21)$$

where  $M$  denotes the case number,  $K$  denotes the maximum value of  $i$ , and  $i$  denotes the cluster number.

(3) According to Equations (20) and (21), Equation (22) can be obtained as follows:

$$\begin{cases} \theta_1 = \frac{K}{2M} \ln \frac{2K}{1-\alpha_1} \\ \theta_\infty = \frac{1}{2M} \ln \frac{2K}{1-\alpha_\infty} \end{cases} \quad (22)$$

#### 4. Case Simulation

##### 4.1. Model Optimization Framework

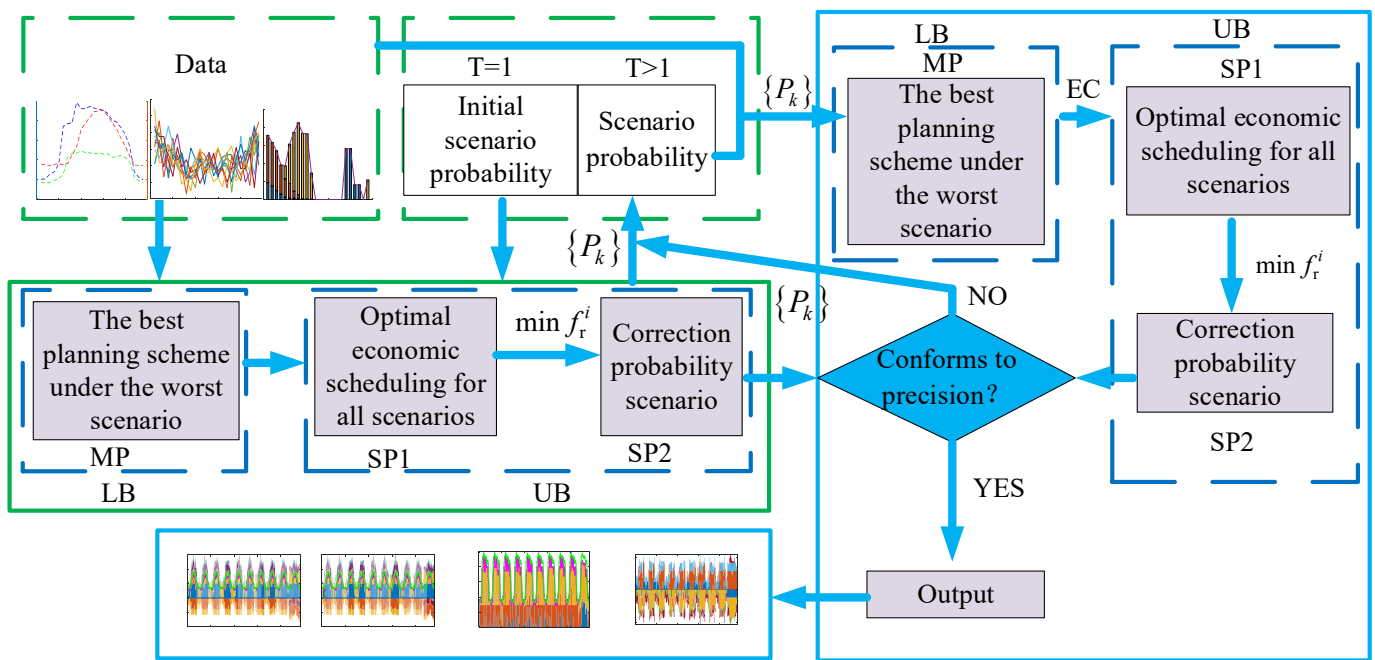
In this study, the model is decomposed into the main problem (MP) and two subproblems (SP1 and SP2). MP solves the lower bound of the objective function ( $LB$ ), SP1 solves  $\min f_r^i$  in  $\max \sum_{i=1}^K (p_i^{T+1} \min f_r^i)$ , and SP2 solves  $\{P_k\}$  through double-norm constraints and  $\max \sum_{i=1}^K (p_i^{T+1} \min f_r^i)$ ; Equations (20)–(22) are the double-norm constraints.

$$\begin{cases} LB = \{\min(f_b^r + \eta), LB\} \\ UB = \left\{f_b^r + \max \sum_{i=1}^K (p_i^{T+1} \min f_r^i), UB\right\} \\ \eta \geq \sum_{i=1}^K p_i^T f_r^i \\ p_i^T = p_i^0 \quad \text{if } T = 1 \end{cases} \quad (23)$$

where  $LB$  denotes the lower bound of the objective function,  $UB$  denotes the upper bound of the objective function, and  $p_i^0$  denotes the initial scenario probability value (Table A1 in Appendix A).

The model optimization process is shown in Figure 3. In an iteration, according to the initial scenario probability,  $LB$  in Equation (23) calculates the best equipment capacity (EC) under the worst scenario, SP1 solves the most economical operation state according to the equipment capacity obtained from  $LB$ , and the SP2 correction probability scenario is obtained through Equations (20)–(24). In the next iteration, we use the corrected scenario probability value obtained from the previous iteration. Through continuous iteration,  $re$  converges to the minimum value and conforms to precision.  $re$  denotes the residual.

$$re = |(UB - LB)/UB| \quad (24)$$



EC denotes equipment capacity    MP denotes main problem    LB denotes The lower bound of the objective function  
 SP1 denotes subproblem1    SP2 denotes subproblem2    UB denotes the upper bound of the objective function

Figure 3. Flow chart of the model optimization process.

4.2. Data Description

Three adjacent areas in Lhasa, Tibet, including medical, office, and commercial areas, were used for numerical simulation. The load in these three areas and relevant data of typical DRE scenarios are provided below.

Figure 4 shows a typical electric power, heat load forecast, and oxygen load diagram of the IES cluster. Figure 5 shows the DRE in 10 scenarios of the IES cluster. As shown in Figure 5, IES1 refers to wind power, IES2 refers to wind and photovoltaic power, and IES3 refers to photovoltaic power. Figure 6 shows the charging hydrogen prediction results for HICEVs, including hydrogen buses, taxis, and business vehicles.

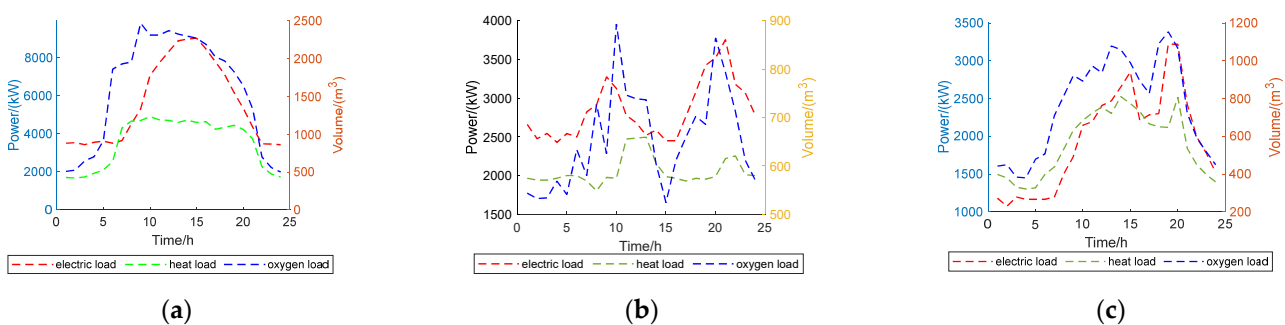


Figure 4. IES1 (a), IES2 (b), and IES3 (c) loads.

Table 2 lists the purchase and sale price of the power grid; the median value of the purchase and sale price was adopted as the power load price on the demand side. Table 3 summarizes select system parameters, including the comprehensive cost, equipment efficiency, energy consumption ratio, and climbing power. Among these parameters, the installed capacity of HP stations and DRE is the construction capacity, without considering the efficiency and energy consumption ratio, and hydrogen storage does not consider the

energy consumption ratio. *DRE* is the grid-connected amount, without considering the climbing power, and only the amount of abandoned wind/solar power was considered. The scheduling cycle included 10 scenarios, 24 h for each scenario, and the step size was 1 h.

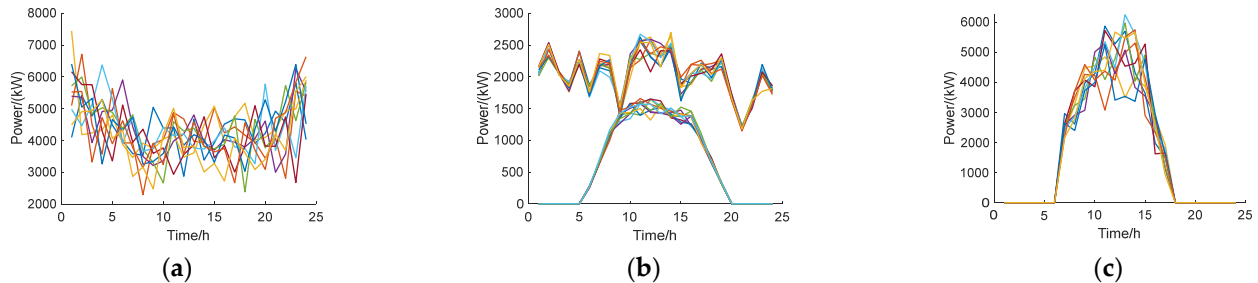


Figure 5. *DRE* of IES1 (a), IES2 (b), and IES3 (c).

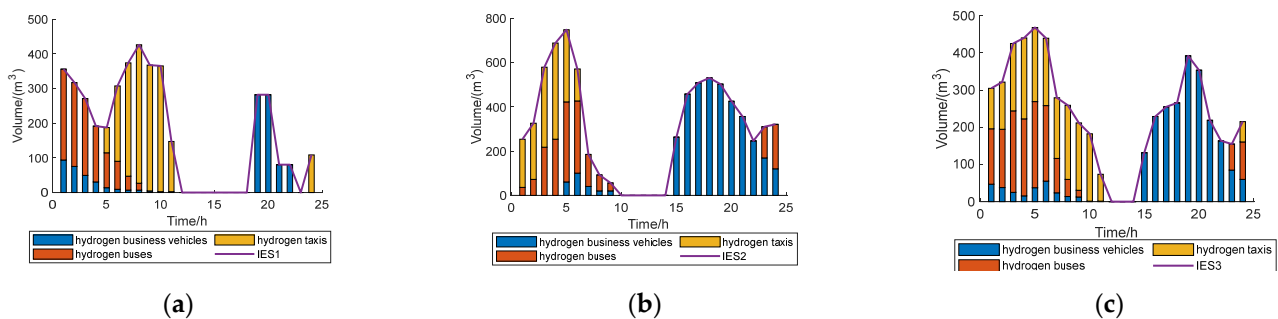


Figure 6. IES cluster charging hydrogen prediction for HICEVs, IES1 (a), IES2 (b), and IES3 (c).

Table 2. Purchase and sale price of the power grid.

	Time/(h)					
	1–7	8–11	12–14	15–18	19–22	23–24
Purchase/RMB	0.4	0.75	1.2	0.75	1.2	0.4
Sale/RMB	0.2	0.4	0.6	0.4	0.6	0.2

Table 3. Relevant parameters.

Equipment	Comprehensive Cost	Efficiency	Energy Consumption Ratio	Climbing Power
(Polymer electrolyte membrane (PEM)) P2H	10,000 (RMB/kW)	0.7	35 (kW/kg)	20%
HFC	1000 (RMB/kW)	0.95	3.3 (kW/Nm <sup>3</sup> )	20%
VPSA	4500 (RMB/kW)	0.85	0.45 (kW/Nm <sup>3</sup> )	20%
HP	12,000 (RMB/kW)	/	/	20%
WT	22,000 (RMB/kW)	/	/	/
PV	9600 (RMB/kW)	/	/	/
HGS	3000 (RMB/kg)	0.95	/	250 (Nm <sup>3</sup> /h)

The equipment price and equipment construction, operation, and maintenance costs are included in the comprehensive cost in Table 3. By default, the service life of all equipment was set to 20 years, so only the operation and maintenance cost of 20 years was considered.

Among the *CSP* parameters listed in Table 4, the combined cost of *CSP* and *HS* units was 30,000 RMB/kW, and the *CSP* efficiency was the efficiency of steam turbine generation.

As indicated in Table 5,  $P_{CSP1,e}^{\max}$ ,  $P_{CSP2,e}^{\max}$ , and  $P_{CSP3,e}^{\max}$  denote the installed capacity of the CSP generation stations of IES, IES2, and IES3, respectively.

**Table 4.** CSP.

Equipment	Comprehensive Cost	Efficiency	Heated Fluid Transmission	Climbing Power
CSP	30,000 (RMB/kW)	0.8 (electric)	0.72	20%
HS		0.95	/	2000 (kW/h)

**Table 5.** CSP installed capacity.

Equipment	Installed Capacity/(MW)		
	IES1	IES2	IES3
CSP	$P_{CSP1,e}^{\max}$	$P_{CSP2,e}^{\max}$	$P_{CSP3,e}^{\max}$
HS	10	10	10

The equipment purchase, equipment installation, and 20-year maintenance costs of gas transmission stations and pipelines are included in the pipeline construction cost in Table 6. The default laying length of each IES pipeline was 10 km.

**Table 6.** Pipeline and hydrogen charging station parameters.

	Oxygen Transmission Pipeline	Hydrogen Transmission Pipeline	Hydrogen Charging Stations
Cost	500,000 (RMB/km)	630,000 (dollar/km)	3 × 5 million
Length/(km)	3 × 10	3 × 10	/

To verify the advantages of the IES cluster considering multiple energy sharing and the effects of the *P2H-VPSA* joint oxygen supply, CSP power stations, and double-norm constraints on the demand response, various cases were set (‘×’ denotes elements that are not considered in a specific case) in Table 7.

**Table 7.** Case set.

	Case 1	Case 2	Case 3	Case 4	Case 5	Case 6	Case 7	Case 8
DR		×						
CSP			×					
Oxygen sharing				×				
Hydrogen sharing					×			
<i>P2H</i>						×		
1 – norm							×	
∞ – norm								×

In the above eight cases, Case 1 simulates the model built in this study, and Cases 2–8 are comparative cases. We verified the effect of the proposed model by adjusting various conditions in Case 1.

In Case 2, we deleted the demand response, and verified the role of the electricity, oxygen, and heat demand responses via a comparison to Case 1. In Case 3, we deleted CSP, and we verified the role of the CSP energy supply via comparison. Cases 4 and 5 were designed to compare and verify the effect of multiple energy sharing. Case 6 was set to compare and verify the effect of the *P2H-VPSA* combined oxygen supply. We established Cases 7 and 8 to compare and verify the comprehensive effect of the double-norm constraints.

The model entails a mixed integer linear programming problem. In this study, we used the Yalmip toolbox to call Gurobi in MATLAB software to solve this problem. The computer parameters were as follows: Intel (R) core (TM) i5 2.90 GHz and 16 GB RAM.

### 4.3. Data Analysis

#### 4.3.1. Cluster Optimization Result Analysis

Based on the above parameter settings, a DRO model was built to consider multiple energy sharing scenarios of the IES cluster. Case 1 was set as  $\alpha_1 = 0.5$  and  $\alpha_\infty = 0.99$ .

Table 8 provides the optimal planning capacity of the equipment. Table 9 indicates that as  $f_b^r$  was the daily average comprehensive cost and the operating cost was the cost of 10-scenario operation optimizations, the total cost was 10 times the comprehensive cost plus the operating cost. Figure 7 and Equations (4) and (5) reveal that the energy sold by the IES exceeded the energy purchased, resulting in negative values of  $f_e^i$  and  $f_h^i$ . The abandoned wind and solar rate of the IES cluster was 0, and  $R_{DRE}$  denotes the penetration rate of the DRE installed capacity.

**Table 8.** Equipment planned capacity.

	VP SA /(kW)	P2H /(kW)	EF /(kW)	HP /(kW)	HGS /(m <sup>3</sup> )	HFC /(kW)
IES1	121.63	4931.43	2453.75	5772.99	1640.15	3378.40
IES2	150.49	2236.97	1427.28	2945.48	1500	1186.28
IES3	683.73	2793.84	1572.92	4035.47	1000	1331.90

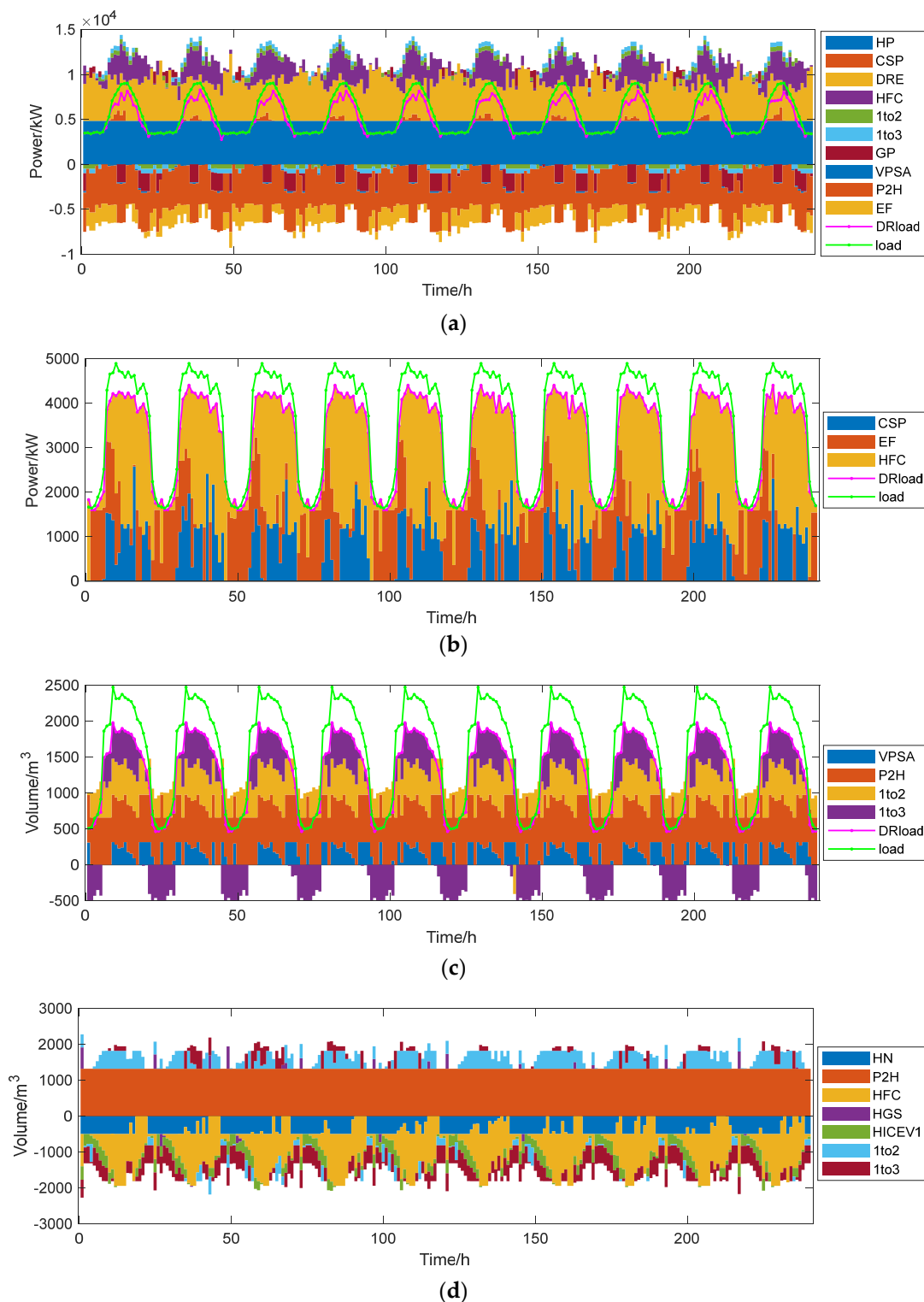
**Table 9.** Model optimization results.

	Cost/(RMB)						Abandonment DRE Rate	$R_{DRE}$	
	$10 \times f_b^r$	$f_e^i$	$f_h^i$	$f_{DR}^i$	$f_{DRE}^i$	$f_{ES}^i$			Total Cost
IES1	195,254.30	−79,402.76	−230,194.49	1466.54	0	19,874.01	3,369,750.5	0	40.02%
IES2	110,220.13	−73,772.37	−243,107.03	999.13	0	20,695.12	3,369,750.5	0	37.79%
IES3	119,101.72	−60,178.25	−253,665.72	3389.98	0	17,885.06	3,369,750.5	0	42.76%

Table 10 provides the total energy sharing results under the 10 scenarios and demonstrates that electricity, oxygen, and hydrogen interactions were included. Regarding the overall interaction of energy sharing, the higher the renewable energy power generation, the higher the energy sharing value. Conversely, the lower the power generation, the lower the energy sharing value.

**Table 10.** Multi-energy sharing.

	Electricity Sharing/(kW)	Volume/(m <sup>3</sup> )	
		Oxygen Sharing	Hydrogen Sharing
1 to 2	50,407.58	1939.34	25,911.81
2 to 1	57,586.23	87,531.07	53,536.94
2 to 3	48,736.95	862.84	6008.74
3 to 2	51,212.07	40,071.93	87,791.24
1 to 3	58,749.58	100,320.40	84,184.06
3 to 1	54,415.72	59,353.21	7527.67



**Figure 7.** IES1 energy balance. (a) IES1 electric power balance. (b) IES1 heat power balance. (c) IES1 oxygen balance. (d) IES1 hydrogen balance.

The scheduling cycle of a given cluster scenario encompassed 24 h, and the scheduling results for the 10 typical scenarios of IES1 in the three adjacent IESs are shown in Figure 7. In the *DRE* scenario depicted in Figure 5, the scenario data dispersion of IES1 was the highest, whereas the scenario data dispersion of IES2 and IES3 was low; please refer to Appendix B for the scheduling results of IES2 and IES3.

As shown in Figure 7, electric energy mainly originated from *HP*, *DRE*, *HFC*, *GP*, and energy sharing, and was mainly consumed by the *P2H* and electrical load. In IES1, compared with the traditional utilization mode, *P2H* provided 86.91% of the oxygen supply instead of *VPSA*, and the provided hydrogen energy was interactively used by the *HFCs*, hydrogen charging stations, and hydrogen energy systems. *P2H* was no longer simply a device to absorb excess renewable energy, but an energy hub for electricity, heat, oxygen, and hydrogen.

In the cluster, the *HFC* electricity supply was concentrated during peak load hours, and the *EF* electricity consumption was concentrated at night, corresponding to the heat balance. The transmission of electric energy to IES2 and IES3 was concentrated at night, and during daytime peak hours, IES2 and IES3 transmitted electric energy to IES1. In terms of heat supply, *CSP*, together with *HFCs* and *EFs*, flexibly adjusted the heat power. The *EF* and *CSP* models are complementary models. *EFs* were used to supply heat at night, *CSP* was used to supply heat during the day, and *HFCs* were used to supply heat during peak hours. With regard to the oxygen supply, *P2H* combined *VPSA* and oxygen sharing, with *P2H* providing the main oxygen supply and *VPSA* and oxygen sharing providing auxiliary oxygen supplies. Oxygen sharing in the cluster occurred as follows: IES3 sent oxygen to IES1 during the day, IES1 sent oxygen to IES3 at night, and IES2 sent oxygen to IES1 most of the time. With regard to the hydrogen supply, the hydrogen production of *P2H* basically remained constant. During the peak period of hydrogen demand, IES2 delivered hydrogen to IES1. In the afternoon, IES2 delivered hydrogen to IES2 by reducing hydrogen sales in the afternoon and at night. Due to the minimum hydrogen production of *P2H*, IES3 produced hydrogen during the middle period. IES1 delivered hydrogen to IES3 to bridge the peak period of the hydrogen demand of IES3. IES3 delivered hydrogen to IES2 to bridge the peak period of the hydrogen demand of IES2.

A comparison of the IES cluster energy supply price and market price is shown in Figure 8, and a comparison of the cluster energy supply revenue is provided in Table 11. The price fluctuations in the 10 scenarios were basically the same, so only the price of the 10th scenario was given.

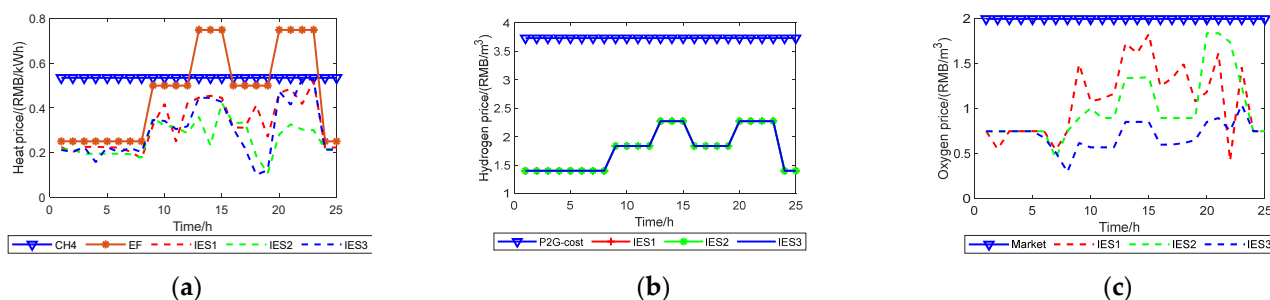


Figure 8. IES cluster energy supply and market prices. (a) Heat price. (b) hydrogen price. (c) Oxygen price.

Table 11. Energy supply income.

	Income/(RMB)			
	Electricity Supply	Heat Supply	Oxygen Supply	Hydrogen Supply
Market price	1,645,868.40	961,179.10 (G) 921,750.00 (E)	1,185,047.03	705,210.02
IES cluster price	1,552,777.50	537,174.10	317,194.00	308,350.30

According to Figure 8 and Equations (A11)–(A14), the energy supply price in the cluster should be lower than the market price based on ensuring a 10% profit, and lower prices could enhance demand-side activity. The market price of hydrogen includes the



transportation price (7.79 RMB/kg), hydrogen injection price (8.73 RMB/kg), and production cost (25 RMB/kg). The price of hydrogen in the cluster is the pipeline transportation cost. Only the transportation cost of the booster station and the cost after *P2H* allocation should be considered. The hydrogen supply object is the hydrogen charging station.

As indicated in Table 11, the electricity price in the cluster was the median value of the electricity purchase and sale price of the cluster. The market price to purchase electricity accounts for 0.66 kWh/RMB of the electricity price in Lhasa. The market price of heating income includes the income of natural gas heating (G) and electric heating €. Although the total income of the cluster under the 10 scenarios was lower than the market price income, the pricing mechanism in the cluster maintained a 10% profit, which did not reduce the interests of the IES cluster.

#### 4.3.2. Equipment Effect Analysis

To verify the effect of the *P2H* oxygen supply, *CSP*, and demand response, a comparison of relevant cases was performed, as summarized in Table 12. Table 13 provides the specific optimization results without *CSP* in Case 3, and Table 14 lists the specific optimization results for the *P2H* oxygen supply in Case 6. Table 15 provides the total number of IES cluster demand responses under the 10 scenarios.

**Table 12.** Comparison of the results of Cases 1–3 and 6.

	Cost/(RMB)			
	Case 1	Case 2	Case 3	Case 6
IES1	1,664,286.00	1,680,287.08	1,935,782.59	1,670,702.04
IES2	807,016.30	886,898.42	981,657.05	948,911.43
IES3	898,448.20	1,038,758.88	950,317.00	1,013,862.14

**Table 13.** Case 3 results.

	Cost/(RMB)					
	$10 \times f_b^r$	$f_e^i$	$f_h^i$	$f_{DR}^i$	$f_{DRE}^i$	$f_{ES}^i$
IES1	1,945,546.92	154,771.28	−170,195.81	3457.96	0	2202.24
IES2	1,218,976.59	−42,413.58	−197,561.30	1488.78	0	1166.56
IES3	1,164,351.28	−36,194.57	−183,101.66	4144.47	0	1117.48

**Table 14.** Case 6 results.

	Cost/(RMB)					
	$10 \times f_b^r$	$f_e^i$	$f_h^i$	$f_{DR}^i$	$f_{DRE}^i$	$f_{ES}^i$
IES1	1,945,546.92	−91,629.17	−206,761.48	2239.84	0	19,643.03
IES2	1,218,976.59	−89,677.82	−210,365.62	1071.29	0	21,161.27
IES3	1,164,351.28	−74,542.60	−206,665.40	3322.16	0	18,084.26

**Table 15.** IES1 DR.

	Electrical Load Response/(kW)	Volume/(m <sup>3</sup> )	
		Heat Load Response	Oxygen Load Response
		IES1	134,012.0
IES2	68,319.00	49,354.50	25,713.35
IES3	47,043.00	45,667.00	33,216.26

Compared with Case 3, the operation cost in Case 1 was reduced by 12.88%. Without *CSP*, the impact on cluster cost optimization was the greatest. Compared with the specific results provided in Table 9, the electricity purchase and sale cost, hydrogen purchase and sale cost, and demand response cost of the cluster increased. Compared with Case 6, the operating cost in Case 1 was reduced by 7.26%. Without the *P2H* oxygen supply, the *P2H* energy consumption was reduced, and the electricity purchase and sale cost of the cluster were reduced, but the hydrogen purchase and sale cost increased. As there was no *P2H* oxygen supply, the cost of *P2H* could not be shared, and the oxygen supply and hydrogen sale prices increased, which reduced the enthusiasm on the demand side from Case 1 levels. Compared with Case 2, the operation cost in Case 1 was reduced by 6.55%. Compared with Cases 3 and 6, the impact was minimal without the demand response.

The *CSP* and *CSP-HS* scheduling processes in Scenario 10 were used to analyze the effectiveness of *CSP*, as shown in Figures 9 and 10, respectively. Figure 9 shows that with the help of the *CSP* high-density heat tank, the *CSP* delayed the period of heating and power generation, further improving cluster flexibility. In terms of the electricity supply, cooperation with other equipment in the power supply was realized to simultaneously cut peaks and bridge valleys; in terms of the heat supply, *HFCs* were used to supply the peak heat load in coordination with *EFs* and *HFCs*, and *EFs* and *CSP* were used to provide the remainder.

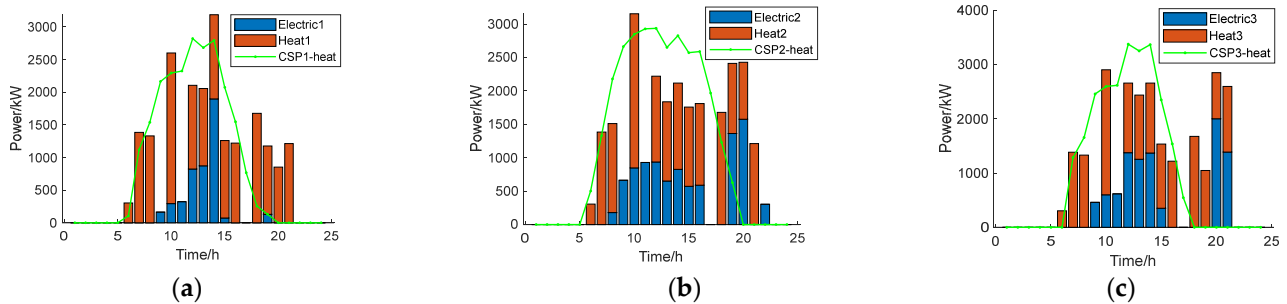


Figure 9. *CSP* scheduling results of IES1 (a), IES2 (b), and IES3 (c).

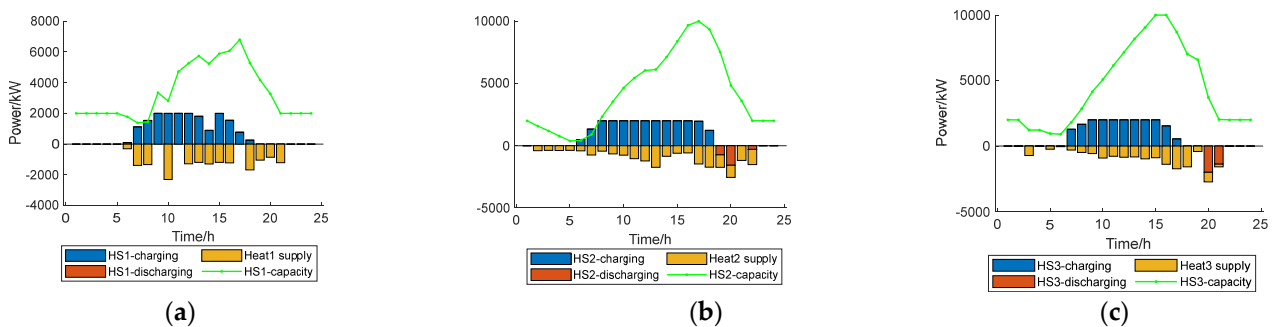


Figure 10. *CSP-HS* scheduling results of IES1 (a), IES2 (b), and IES3 (c).

Comparing Figures 7 and A1 in Appendix B and Table 16, it is evident that, compared with Case 1, part of the oxygen load in IES1 in Case 6 was supplied by *P2H*, replacing 78.39% of the *VPSA* oxygen supply. A total of 81,505.68 kW of electricity was saved under the 10 scenarios. In IES2, under the combined *P2H-VPSA* oxygen supply, the output of *P2H* basically remained stable, replacing 65.22% of the *VPSA* oxygen supply and saving 53,180.39 kW of electricity under the 10 scenarios. In IES3, under the combined *P2H-VPSA* oxygen supply, the output of *P2H* basically remained constant, replacing 42.88% of the *VPSA* oxygen supply, and 54,963.07 kW of electricity was saved under the 10 scenarios.

**Table 16.** Percentage of the *P2H* oxygen supply in the combined *P2H-VPSA* oxygen supply.

	IES1	IES2	IES3
Percentage (%)	78.39	65.22	42.88

#### 4.3.3. Multiple Energy Sharing Analysis

In a conventional IES, when *DRE* cannot be consumed in real time, energy is discarded, and the absorption rate of *DRE* is reduced. Therefore, the energy sharing mode was adopted and hydrogen and oxygen sharing was assessed. To verify the advantages of multiple energy sharing, Table 17 provides a comparison of three scenarios, and the specific results are as follows: compared with Case 4 (oxygen sharing), the cost of IES1 in Case 1 decreased by 0.9%, the cost of IES2 decreased by 10.3%, and the cost of IES3 increased by 6.3%. Case 5 (hydrogen sharing) was similar to Case 4, and compared with Cases 4 and 5, the total cost decreased by 1.61 and 3.99%, respectively. Combined with Figures 7 and A1, the results show that in hydrogen or oxygen sharing, IES3 was mainly responsible for the transmission of hydrogen and oxygen from IES1 to IES2. This occurred because the generation capacity of *DRE* was the main impact factor of multiple energy sharing. Overall, the *DRE* generation capacity decreased, and under the multiple energy sharing mode, the overall economy of the IES cluster improved.

**Table 17.** Comparison of the results of Cases 1, 4, and 5.

	Cost/(RMB)		
	Case 1	Case 4	Case 5
IES1	1,664,286.00	1,680,196.64	1,694,205.04
IES2	807,016.30	899,993.33	924,279.15
IES3	898,448.20	844,621.54	891,407.86

#### 4.3.4. Different Confidence Levels for Cluster Result Comparison

In DRO, different confidence levels could yield varying degrees of conservatism of the cluster. In this paper, we analyzed the model calculation results by setting different confidence intervals. The parameter settings are listed in Table 18. Regarding the conservative responses of uncertain systems, the higher the system cost, the higher the degree of conservatism, and the lower the risk preference and the higher the adjusted reserve capacity of the system, to balance the larger error and higher energy consumption of the *DRE* output. However, considering the high uncertainty in *DRE* in Tibet, we selected the most conservative of the defined confidence levels in this paper.

**Table 18.** Comparison of the results at different confidence levels.

$\alpha_1$	$\alpha_\infty$		
	0.5	0.9	0.99
0.20	3,325,749.92	3,330,083.26	3,336,340.05
0.50	3,329,127.75	3,333,823.71	3,369,750.50
0.90	3,320,367.90	3,337,569.98	3,349,257.23

Furthermore, the 1– norm with  $\alpha_1 = 0.2, 0.5, 0.9$  and the  $\infty$ – norm with  $\alpha_\infty = 0.5, 0.9, 0.99$  were selected for comparison with the double-norm constraints, as summarized in Table 19 and Table 20, respectively. The results indicate that, at the same confidence level, the operation costs under the double-norm constraints were lower than under single-norm constraints.

**Table 19.** Comparison of the results of Cases 1 and 8.

	Double Norm	1 – Norm
0.20	3,336,340.05	3,432,631.62
0.50	3,369,750.50	3,434,569.65
0.90	3,349,257.23	3,468,672.31

**Table 20.** Comparison of the results of Cases 1 and 7.

	Double Norm	$\infty$ – Norm
0.50	3,336,340.05	3,430,380.45
0.90	3,369,750.50	3,445,127.40
0.99	3,349,257.23	3,446,824.83

## 5. Conclusions

In this study, considering multiple energy sharing and multi-energy coupling, a DRO model of IES clusters was built. The DRO method based on double-norm constraints was introduced to address the uncertainty in *DRE*. The main conclusions are as follows:

- (1) Based on the demand for a dispersed oxygen supply and energy development planning in the plateau region, an IES was built by coupling electricity, heat, oxygen, and hydrogen. Considering the current energy situation in Tibet and the emission peak and carbon neutrality targets of China, the traditional IES was improved by introducing clean energy units to achieve extremely low carbon emissions and improve *DRE* consumption levels. The enthusiasm on the demand side was enhanced through a reasonable pricing mechanism without reducing the cluster profit level. The scenario comparison showed that the cluster economy was higher than in other scenarios.
- (2) DRO optimization under double-norm constraints achieved a better balance between robustness and economy. Therefore, DRO was more effective in addressing the uncertainty in the *DRE* output in IES cluster optimization. At the same time, the two confidence intervals of the double-norm constraints were parameters reflecting the decision-maker's risk preference. The lower the degree of conservatism, the lower the operating cost and the higher the benefits of the double-norm constraint strategy. Decision-makers must choose different confidence intervals according to their risk preferences.
- (3) The multiple energy sharing mechanism of the IES cluster provided a higher economic advantage than that provided by the single electricity sharing mechanism. Due to the various energy consumption habits and *DRE* installation levels of each IES, the energy consumption in each IES may considerably vary, which may lead to an energy surplus and energy waste. However, the multiple energy sharing mechanism solved this problem. The scenario comparison revealed that the multiple energy sharing mechanism effectively reduced the cluster cost, planned capacity, and energy storage usage.

To satisfy energy sharing among clusters and the interconnection with electricity and hydrogen markets, multi-energy sharing mechanisms were used in this study to make connections among multiple regional IESs. Although the demand for a dispersed oxygen supply is unique to plateau areas, oxygen is widely used in situations such as oxygen-rich combustion and medical care. Therefore, this model can have generalizable value. The DRO model sets the energy interaction price of adjacent IESs as the energy supply price. Energy sharing price design should be considered in the future to further enhance the economic benefits of the cluster. Furthermore, it is vital to consider energy network optimization (electricity, hydrogen, and heat) in the optimization of multi-energy systems to ensure the feasibility of the obtained dispatch solutions. Therefore, research on energy network optimization should be the focus of future work.

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### Appendix A

1. The other equipment constraints can be expressed as follows:

$$\begin{cases} P_{HP}^{\min} \leq P_{HP}^t \leq M_{HP} \\ \Delta P_{HP}^{lp} \leq P_{HP}^t - P_{HP}^{t-1} \leq \Delta P_{HP}^{up} \\ P_{EF,h}^t = \eta_{EF} P_{EF,e}^t \\ P_{EF,e}^{\min} \leq P_{EF,e}^t \leq M_{EF} \\ \Delta P_{EF,e}^{lp} \leq P_{EF,e}^t - P_{EF,e}^{t-1} \leq \Delta P_{EF,e}^{up} \end{cases} \quad (A1)$$

where,  $P_{HP}^{\min}$  denotes the lower power limit of  $HP$ ,  $M_{HP}$  denotes the  $HP$  installed capacity,  $\Delta P_{HP}^{up}$  and  $\Delta P_{HP}^{lp}$  denote the  $HP$  limits of climbing power,  $\eta_{EF}$  denotes the heat supply of  $EFs$ ,  $P_{EF,e}^{\min}$  denotes the lower power limit of  $EFs$ ,  $M_{EF}$  denotes the  $EF$  installed capacity, and  $\Delta P_{EF,e}^{up}$  and  $\Delta P_{EF,e}^{lp}$  denote the  $EF$  limits of climbing power.

2. Demand response

(1) The limit of the adjustable oxygen load can be obtained as follows:

$$O_{cut}^{\min} \leq O_{cut}^t \leq O_{cut}^{\max} \quad (A2)$$

where  $O_{cut}^t$  denotes the adjustable oxygen load volume and  $O_{cut}^{\max}$  and  $O_{cut}^{\min}$  denote the limits of the adjustable oxygen load volume. The oxygen load after the demand response can be calculated as follows:

$$V_{OL,DR}^t = O_L^t - O_{cut}^t \quad (A3)$$

(2) The limit of the transferable electrical load can be determined as follows:

$$\begin{cases} -\mu_P P_L^t \leq P_{tr}^t \leq \mu_P P_L^t \\ \sum_{t=1}^{24} P_{tr}^t = 0 \end{cases} \quad (A4)$$

where  $P_{tr}^t$  denotes the transferable electrical load power,  $\mu_P$  denotes the percentage of the translatable electrical load in the electrical load, and  $P_L^t$  denotes the electrical load. The limit of the adjustable electrical load can be expressed as follows:

$$P_{cut}^{\min} \leq P_{cut}^t \leq P_{cut}^{\max} \quad (A5)$$

where  $P_{cut}^t$  denotes the adjustable electrical load power and  $P_{cut}^{\max}$  and  $P_{cut}^{\min}$  denote the limits of the adjustable electrical load power. The electrical load after the demand response can be obtained as follows:

$$P_{EL,DR}^t = P_L^t + P_{tr}^t - P_{cut}^t \quad (A6)$$

- (3) The limit of the transferable heat load can be calculated as follows:

$$\begin{cases} -\mu_H H_L^t \leq H_{tr}^t \leq \mu_H H_L^t \\ \sum_{t=1}^{24} H_{tr}^t = 0 \end{cases} \quad (A7)$$

where  $H_{tr}^t$  denotes the transferable heat load power,  $\mu_H$  denotes the percentage of the translatable heat load in the heat load, and  $H_L^t$  denotes the heat load. The limit of the adjustable heat load can be expressed as follows:

$$H_{cut}^{\min} \leq H_{cut}^t \leq H_{cut}^{\max} \quad (A8)$$

where  $H_{cut}^t$  denotes the adjustable heat load power and  $H_{cut}^{\max}$  and  $H_{cut}^{\min}$  denote the limits of the adjustable heart load power. The heat load after the demand response can be obtained as follows:

$$P_{HL,DR}^t = H_L^t + H_{tr}^t - H_{cut}^t \quad (A9)$$

3. The HGS constraints can be expressed as follows:

$$\begin{cases} S_{hs}^t = S_{hs}^{t-1} + \eta_{sh}^{ch} V_{hs,ch}^t - V_{hs,dis}^t / \eta_{sh}^{dis} \\ S_{hs}^{\min} \leq S_{hs}^t \leq M_{hs}^i \\ V_{h,ch}^{\min} \leq V_{hs,ch}^t \leq \alpha_{h,ch} V_{h,ch}^{\max} \\ V_{h,dis}^{\min} \leq V_{hs,dis}^t \leq \alpha_{h,dis} V_{h,dis}^{\max} \\ \alpha_{h,dis} + \alpha_{h,ch} \leq 1 \\ S_{hs}^{t=1} = S_{hs}^{t=24} \\ (2 \leq t \leq 24) \end{cases} \quad (A10)$$

where  $S_{hs}^t$  denotes the HGS capacity,  $M_{hs}^i$  denotes the HGS installed capacity,  $S_{hs}^{\min}$  denotes the lower limit of the HGS capacity,  $\alpha_{h,dis}$  denotes the discharging hydrogen status parameters,  $\alpha_{h,ch}$  denotes the charging hydrogen status parameters,  $V_{h,ch}^{\max}$  and  $V_{h,ch}^{\min}$  denote the limits of the charging hydrogen volume,  $V_{h,dis}^{\max}$  and  $V_{h,dis}^{\min}$  denote the limits of the discharging hydrogen volume,  $\eta_{sh}^{ch}$  denotes the charging hydrogen efficiency, and  $\eta_{sh}^{dis}$  denotes the discharging hydrogen efficiency.

4. IES cluster energy supply price Through Equations (A11)–(A14), the P2H cost can be apportioned to the P2H hydrogen and P2H oxygen supplies. HFCs can be divided into power and heat supplies, and the intra-cluster electricity price is the average electricity purchase and sale price. As the hydrogen purchase cost is included in the operating cost, the hydrogen price only considers the transmission cost and cost of hydrogen energy sharing.

- (1) The heat supply price can be obtained as follows (hydrogen shares 60% of the P2H power consumption cost, and the profit is 10%):

$$\begin{cases} P_{ri,hot} = 1.1(P_{CSP,H}^t P_{ri,CSP} + G_{sell}^t P_{EF,e}^t + w_h w_{h,e} E_{P2H,H_2}) / (P_{CSP,H}^t + P_{EF,H}^t + P_{HFC,H}^t) \\ \eta_H = V_{HFC,H}^t / V_{EL,H}^t \\ E_{P2H,H_2} = G_{sell}^t V_{HFC,H}^t P_{H,e} \rho_H / \eta_{P2H} / \eta_H \end{cases} \quad (A11)$$

where  $w_h$  denotes the P2H cost allocation weight, which is 0.6;  $G_{sell}^t$  denotes the electricity sale price;  $E_{P2H,H_2}$  denotes the power consumption cost for P2H hydrogen production;  $w_{h,e}$  denotes the real-time thermoelectric proportion of HFCs; and  $P_{ri,CSP}$  denotes the CSP heat supply price.

- (2) The oxygen supply price can be determined as follows (the profit is 10%):

$$P_{ri,o} = 1.1 G_{sell}^t (V_{VPSA}^t P_{VPSA,e} / \eta_{VPSA} + w_o E_{P2H,O_2}) / (V_{VPSA}^t + V_{EL,O}^t) \quad (A12)$$

$$E_{P2H.O_2} = G_{sell}^t V_{EL.O}^t P_{O.e} \rho_O / \eta_{P2H} \quad (A13)$$

where  $w_0$  denotes the  $P2H$  oxygen supply cost allocation weight, which is 0.6;  $E_{P2H.O_2}$  denotes the power consumption cost for  $P2H$  oxygen production; and the value is the same as that of  $E_{P2H.H_2}$ .

(3) The hydrogen supply price can be obtained as follows (the profit is 10%):

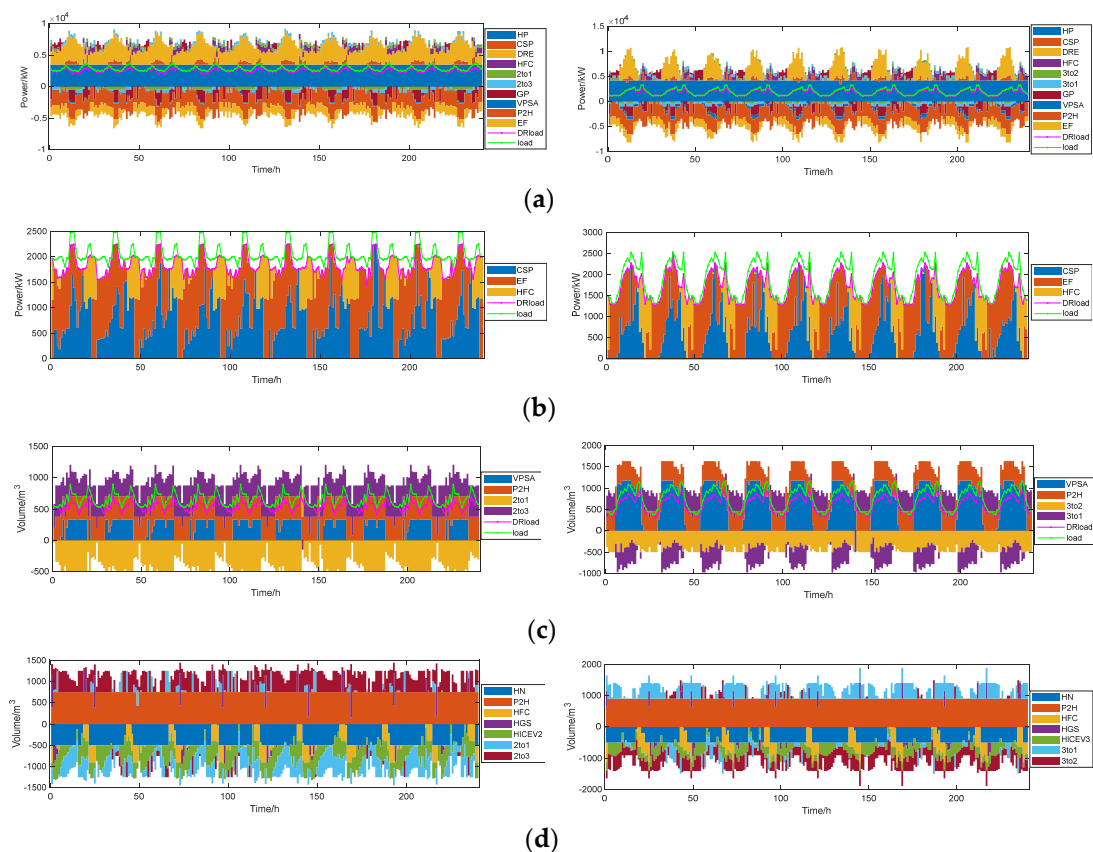
$$P_{ri.H_2} = P_{ri.tran} + 1.1(1 - w_0)E_{P2H.H_2} / V_{EL.h}^t \quad (A14)$$

where  $P_{ri.tran}$  denotes the price of hydrogen pipeline transportation, at 10.73 RMB/kg.

**Table A1.** Initial scenario probability.

	Scenario 1	Scenario 2	Scenario 3	Scenario 4	Scenario 5	Scenario 6	Scenario 7	Scenario 8	Scenario 9	Scenario 10
IES1	0.17	0.10	0.09	0.11	0.07	0.09	0.05	0.12	0.12	0.08
IES2	0.07	0.05	0.12	0.04	0.06	0.04	0.07	0.05	0.31	0.09
IES3	0.06	0.1	0.12	0.16	0.09	0.08	0.08	0.06	0.09	0.16

## Appendix B



**Figure A1.** IES2 and IES3 energy balance. (a) IES2 and IES3 electric power balance. (b) IES2 and IES3 heat power balance. (c) IES2 and IES3 oxygen balance. (d) IES2 and IES3 hydrogen balance.

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