



Article Mathematical Modeling and Simulation of a Compound Parabolic Concentrators Collector with an Absorber Tube

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Abstract: CPC solar collectors are a combination of new technologies that make it possible to generate heat from radiant solar energy by transferring heat between the absorber and the fluid. This study was performed based on heat transfer equations by proposing a mathematical model, as reported in the literature. A compound parabolic concentrators solar collector (CPC) numerical model was simulated and coded in Aspen HYSYS and MATLAB software and validated by comparing its results with other researchers and experimental results. The simulated mathematical model includes a twodimensional numerical model to describe the thermal and dynamic behavior of the fluid inside the CPC solar collector absorber tube. Numerical simulations of the fluid flow equations inside the CPC solar collector absorber tube, along with the energy equation for the absorber tube wall, coating, insulation and reflector, and solar collector heat analysis, were performed repeatedly in MATLAB and Aspen HYSYS software. This method is the most appropriate and reliable method for solving equations for numerical convergence. The experimental results of the parabolic concentrated solar collector (CPC) were used to evaluate and validate the numerical model. A solar compound parabolic concentrators collector (CPC) with short reflectors was used. This collector includes a cylindrical absorber with a real density ratio of 1.8, a reception angle of 22 degrees and a length of 2.81 m, a width of 0.32 m, and an opening of 0.1764 m. Analysis and uncertainty of the proposed model were performed with the measured sample. In the thermal efficiency analysis, the average deviation of the model from the experimental results of other researchers was equal to 7%, for increasing the temperature by 9 $^{\circ}$ C. According to these results, a good correlation between numerical results and experimental results for this proposed model has been obtained.

Keywords: compound parabolic concentrator solar collector (CPC); absorber tube; experimental study

1. Introduction

Originally used as radiation detectors in the early 1960s, compound parabolic concentrator solar collectors are more than 50 years old. Initially, Winston and Heinterberger described their use as sun-oriented collectors (1975) [1]. This technology has developed over time until solar water heaters became widely used. Using a flat solar receiver, a preliminary study was conducted on CPC solar collector technologies. Through advancements in technology, the receivers evolved to become tubes, which made it possible to use fluid as a heat transfer fluid [2]. The average reflection of solar radiation into the CPC solar collectors has been calculated analytically by Rübel (1976). CPC solar collectors were analyzed optically using the results of this study [3]. Using thermal analysis for solar collectors with absorber tubes, Hsieh (1981) developed a mathematical model [4]. A CPC collector absorber



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). tube was modeled with the finite element method by Chew et al. (1989), There was an isothermal coating on the absorber tube. Y. Trip Anagnostopoulos et al. (2000) designed two-faced solar collectors and presented them as CPC systems. According to the experimental findings, the proposed compound parabolic concentrator collector can achieve a maximum static temperature of 180 °C and an efficiency of 0.71 [5]. An axial heat flux solar collector was studied by China et al. (2006). Furthermore, Kim et al. (2008) designed and manufactured their own discharged-tube solar collectors, which they theoretically and experimentally evaluated [6]. Solar collectors with a tracking system that allows for a stable trajectory had a thermal Solar collector whose CPC had a 14.9% higher efficiency. An experimental solar collector based on CPC technology was proposed by Y. Kim et al. (2010). Its prototype accomplished a return of over 50% [7]. T. Beikircher et al. (2011) used geometrical concentration to investigate the optical performance of CPC solar collectors. After conducting simulation analyses, it was determined that the operating temperature was 0.35 degrees Celsius greater than the temperature of a flat plate collector [8] C. Tba and N. Fraidenraich (2013) employed a compound parabolic concentrator solar collector to activate a cooling system generator in a solar cooling project. CPC solar collectors achieved a temperature of 125 °C and an efficiency of 0.50 [9]. In their study, Z. S. Lu et al. (2013) developed and analyzed a numerical code for simulating the thermal behavior of storage systems with CPC solar collectors. It was determined that double glazing could increase efficiency by up to 47% by using it as a coating [10]. CPC solar collectors presented by C. Tíba and N. Fraidenraich, (2013) with U-shaped drained pipes reached an efficiency of up to 0.50 and a temperature of 150 °C [9]. Researchers at Gu et al. (2014) achieved a temperature range from 300 °C to 500 °C for a vacuum CPC solar collector [11]. Incorporating CPC solar collectors thermal and photovoltaic system was presented by X. Gu et al. (2014). A 5% difference in the results of the theoretical and experimental evaluations was found between these CPC solar collectors [12]. Figure 1 shows a CPC collector.



Figure 1. CPC collector [13].

Recently, researchers have looked at improving the performance of CPC concentrators by modifying their geometry, such as using materials that are better at transmitting light, creating better operating conditions, and using discharged tubes as adsorbents. Compared to the vacuum tube manufacturing process, it is easier and cheaper to make these other improvements. Table 1 summarizes the research conducted CPC solar collectors.

Reference	Year	Methodology Used/Applications
S. A. Waghmare et al. [14]		The solar flux density of the CPC collector was investigated using surface area radiation (surface area radiation) to design solar collectors based on thermal ratios and equations.
E. K. Nashine and P. Kishore [15]	2017	CPC solar collectors for different locations and compared them
R. L. Shrivastava, K. Vinod, and S. P. Untawale [16]	2017	They simulated transient systems and solar collectors.
Q. Li et al. [17]	2017	Technical-economic performance was analyzed by composite solar collectors (including prism arrays, fresnel lenses, and CPC collectors).
S. A. Waghmare et al. [18]	2017	The CPC solar collector and the surface area irradiation method corrected using the reflecting area to determine the dense flux designed by the solar collectors were examined.
C. Zheng et al. [19]	2017	They performed simulations and experimental studies on the semi-passive shape of the CPC solar collector beam conduction prism.
M. Moradi and M. Mehrpooya [20]	2017	Kalina cycle, which was technically and economically evaluated by a parabolic solar collector.
M. Mehrpooya, E. tosang, and A. Dadak [21]	2018	The combined solid oxide fuel cell and parabolic solar collector and combined cooling system optimally designed and economically designed the heating and power used for a large commercial tower.
A. B. Pouyfaucon et al. [22]	2018	Desalination technologies using solar energy using parabolic collectors were evaluated.
A. J. Expósito et al. [23]	2018	Using a solar CPC collector to investigate the intensity of disinfection of municipal wastewater from the sun. A new method of solar irradiation for the use of composite
P. R. Maddigpu et al. [24]	2018	membranes of carbon chitosan nanoparticles against Escherichia coli (a type of virus) that examined antimicrobial activity when used in a rotating composite solar collector reactor compared to solar disinfectant.
M. Antonelli et al. [25]	2018	They designed and built a medium temperature solar collector and then developed it and optimized the absorber shape of the collector by simulation.
M. Francesconi et al. [26]	2018	They numerically transferred heat in a configuration containing several CPC solar collectors and performed a sequential analysis in the solar field design to increase system efficiency.
N. I. Ibrahim et al. [27]	2018	They analyzed the effects of water-tube-nanoparticles on the thermal performance of CPC collectors.
R. Winston et al. [28]	2018	They simulated a new CPC with a modified adsorbent and optimized for applications in the environment.
M. Mehrpooya, E. tosang, and A. Dadak [21]	2019	They examined a combined cycle power plant with a solar field through a solar source and a high-temperature energy storage system.
V. Baranov [29]	2019	Examined curtain solar collectors.
V. Pranesh et al. [30]	2019	The desalination plant and the solar collector examined the combined parabolic
T. W. Smith et al. [31]	2019	They examined the optical geometry of linear sunlight compactors with CPC collectors as secondary reflectors.
B. Norton et al. [32]	2020	Study of an absorption solar refrigeration cycle with CPC collector based on an advanced mass transfer cycle.
A. F. Kothdiwala et al. [33]	2020	Organic Rankine cycles were thermodynamically analyzed using a
M Rönnelid and B Karlsson [34]	2020	solar parabolic thermal hybrid compaction system. A CPC collector was examined numerically and experimentally
N. Fraidenraich et al. [35]	2020	Parabolic solar light compactors for different heat transfer fluids
N. Frattenrach et al. [55]	2020	were modeled and analyzed based on their annual direct radiation.
H. Riaz, M. Ali, J. Akhtar, R. Muhammad, and M. Kaleem [36]	2020	in the average temperature range from 50 to 300 °C for industrial and domestic applications.
F. Masood et al. [37]	2020	The design and interrelationships between the design parameters of a low-density CPC concentrator (CPC) for photovoltaic applications.
A. B. Ortega, A. Terán-Franco, J. C. Castro, and J. A. del Río [38]	2021	Beam design, fabrication, and simulation of a new CPC concentrator based on a circular shape (TCPC).
Y. Li, F. Jiao, F. Chen, and Z. Zhang [39]	2021	optimization of a multi-part CPC concentrator (M-CPC) based on a comprehensive algorithm.
R. Shah and J. Patel [40]	2022	The hybrid solar system consisted of a photovoltaic cell (PV) module and a hybrid parabolic composite (CPC).

 Table 1. Summary of research on CPC collectors.

Reference	Year	Methodology Used/Applications
F. Chen and Q. Gui. [41]	2022	Propose a parabolic concentrator with a lip absorber (CPC) directly with a solar vacuum tube.
A. Ortega et al. [42]	2022	They built a CPC concentrator (CPC) to generate electricity and studied its performance.
S. Touré and M. Sidibé [43]	2022	They provided a solar oven equipped with a three-dimensional CPC reflector (CPC) where a solar beam enters the CPC at an angle θ .
V. Bhalla, V. Khullar, and R. V. Parupudi [44]	2022	They proposed a nanofluid-based volumetric adsorbent located in a new asymmetric CPC concentrator (NCPC).

Table 1. Cont.

This paper compares the mathematical relationships of a CPC with a tubular absorber with the practical results of a CPC collector. A mathematical model was developed and simulated in Span Hayes and MATLAB software, and a comparative study was performed between the results of the simulated CPC composite with the real sample and the samples of other researchers. In the solar collector, industrial oil is used as heat transfer fluid

2. Materials and Methods

2.1. Modeling of CPC Collectors

To calculate and design parabolic solar collectors, a Cartesian plane is used in which the two main parts of the geometry are drawn in a curve and a parabola based on the dimensions of the absorber tube [45,46]. For restricting the shape of CPC solar collectors in relation to angle, Baum (1984) proposed equations measured by rotating the absorber tube around its center point counterclockwise from the positive *x*-axis [47]. These equations can be used to calculate the geometry of CPC solar collectors in the coordinate plane, as well as their curves for parts in the plane and parabolas.

$$X = r(-\varphi\cos\varphi + \sin\varphi) \tag{1}$$

$$Y = -r(\cos\varphi + \varphi\sin\varphi) \tag{2}$$

To:

 $0 \le \varphi \le \frac{\pi}{2} + \theta_{max}$ $X = r(-A^* \cos \varphi + \sin \varphi)$ (3)

$$Y = -r(\cos\varphi + A^* \sin\varphi) \tag{4}$$

To:

To:

$$\frac{\pi}{2} + \theta_{max} \le \varphi \le \frac{3\pi}{2} - \theta_{max}$$

 $A^* = \frac{\frac{\pi}{2} + \theta_{max} + \varphi - \cos(\varphi - \theta_{max})}{1 + \sin(\varphi - \theta_{max})}$

With the values obtained on the Cartesian plate, the areas of coverage, reflectivity, and absorbency can be determined. The equations of coverage, absorber, and reflector are:

$$A_C = L \times W \tag{6}$$

(5)

$$A_a = 2\pi \times r_0 \times WL \tag{7}$$

$$A_r = \frac{L}{2} \left(\sqrt{4\dot{h^2} + W^2} + \frac{W^2}{2\dot{h}} \ln \frac{2\dot{h} + \sqrt{4\dot{h^2} + W^2}}{W} \right)$$
(8)

$$\acute{h} = \frac{W + D_0[\sin(180 + \theta) - (180 + \theta)\cos(180 + \theta)]}{2\tan\theta}$$
(9)

Aa refers to the diaphragm area, A_r to the lateral area of the receiver tube, and L to the length of the collector. The external absorption tube of CPC solar collectors made of 2.81 m has an inner diameter of 1.90 cm. Due to their large reception angle, CPC solar collectors combine solar radiation despite their lack of concentration. $\theta_{1/2} = 20$ is the angle between the openings of the solar collectors. The vertical axis is the angle between the CPCs. CPC solar collectors were designed using $\theta = 2.2$ and a cut of 0.5 of the height of the reflectance area. Carvalho et al. (1985) showed that incisions can result in significant gains in optical quality [48]. In particular, it increases the reception of the scattered beams and beams and reduces the average number of reflections. In addition, fewer materials are needed to make CPC solar collectors. After cutting, the acceptance half angle was $\theta_{1/2} = 22$ degrees. By this method, a 0.32 m wide and 0.29 m high CPC collector can be designed. The specified length for CPC solar collectors is 2.81 m. Figure 2 shows a CPC collector.



Figure 2. CPC solar collector [49].

CPC solar collectors with a Security glass coating are mathematically designed and modeled to cover the reflective surface and protect the environment. In Figure 2, we show schematically how to assemble the CPC solar collectors. A polystyrene insulating material was used that was coated with a resin for protection and strength. The polystyrene was glued to the reflective foil with special glue. An absorber tube is made of stainless steel, which is covered in matte black selective absorbers. The cover was constructed of Security glass and was attached to a framework that covered the edges of the solar collector with an aluminum frame. In order to test it, it must be put in a fixed position.

2.2. Simulation and Mathematical Modeling

The investigation of CPC solar collectors is based on a theory proposed by numerous authors. The mathematical model was created. When the CPC solar collectors are shortened, the reflector level is dropped by half, yet the composite performance stays about the same [4,50,51]. The correlations utilized in the mathematical model to evaluate the performance of incandescent (shortened) CPC solar collectors were expected to be applicable to sectional (abbreviated) parabolic solar collectors [52].

In Figure 3, the solar input flux is received by the absorber plate and the glass cover. Part of the heat absorbed by the outer part of the absorber plate surface is transferred to the inner part of the surface through the heat transfer mechanism and then to the working fluid through the heat transfer mechanism and the rest is transferred to the inner surface by heat transfer and radiation. The glass cover is transferred. The energy transmitted through displacement and radiation to the inner surface of the glass coating is first transferred to the outer surface by conduction and then wasted to the environment through radiation and displacement.



Figure 3. Heat distribution of CPC solar collectors.

Figures 4 and 5 of the network show the heat transfer mechanisms of CPC solar collectors. This network has been suggested for the analysis of solar collectors. The solar energy absorbed in the absorber tube of the solar collector increases the temperature of the tube. There are five main temperatures in the heat transfer process shown. These temperatures are fluid, adsorbent, coating, reflector, and environment.



Figure 4. Heat transfer network of CPC solar collectors.



Figure 5. Heat transfer network of CPC solar collectors for mathematical modeling.

Since CPC solar collectors are exposed to environmental conditions, CPC solar collectors are affected by environmental conditions, and energy is transferred from the collector to the environment. The absorbed solar energy is transferred to the absorber tube and from the absorber tube to the working fluid, which increases the temperature of the working fluid in the absorber tube and the fluid leaving the solar collector [53]. The following hypotheses are considered to analyze the thermal behavior of the CPC solar collector:

- Constant heat transfer.
- At the end of each depression, there is a slight conduction drop.
- Low iron glass coating with non-specific permeability is 0.90.
- One-dimensional flow is considered.
- The material of the reflector sheets is steel and its reflection coefficient is 0.9.
- The collector adsorbent is a corrosion resistant steel with an absorption coefficient of 0.94.
- It is considered zero by the absorption of solar radiation.
- The geometry of CPC solar collectors is without manufacturing errors.
- In the environment around the CPC solar collector, the thermodynamic properties, heat fluxes, and all temperatures are uniform.
- In a solar collector absorber tube, the heat resistance is negligible and neglected.

Radiation rays reach the absorber tube in several ways [54]. A portion of the rays entering the aperture from different directions of the light source reach the absorber tube directly, and after one or more reflections, the other rays reach the absorber tube. Hence, we can define an average radiation reflectance (*n*) for CPC solar collectors. Optical efficiency in the construction of solar collectors was estimated according to the materials used in an experimental study presented by Oommen and Jayaraman (2001) [55]. This method makes it possible to estimate the solar radiation in the absorber tube [56]. The relationship between the estimated optical efficiency is as follows.

$$\eta_{op} = \tau_{CPC} \rho r^n \alpha_a p \tag{10}$$

where τc crosses the cover. α_a is the lack of adsorbent. p is the reduction coefficient of the opening. Its formula $(1 - g/2\pi ro)$ in the formula the thickness of the gap is g (here, g = 1.00 cm was considered). ρr^n is the effective transmission of the CPC solar collectors. Here, ρ is the solar reflection of the reflective material of the CPC solar collectors. In Formula (10), the average number of reflections is obtained from the following equation:

$$n = \left(-\frac{1}{C}\right) + 1 \tag{11}$$

here:

$$C = \frac{1}{\sin \theta_{max}} = \frac{A_c}{A_a} \tag{12}$$

Fluid outlet temperature is equal to:

$$T_f = \left[\left(T_{fi} - T_{amb} \right) - \left(\frac{A_c}{A_a} \frac{S}{U_l} \right) \right] exp\left(-\frac{\dot{P}U_l}{mCp} \dot{F} \dot{X} \right) + \left(\frac{A_c}{A_a} \frac{S}{U_l} \right) + T_{amb}$$
(13)

To predict the collector performance, \hat{F} , which represents the collector efficiency coefficient, must be calculated. To evaluate the energy survival in the solar collector according to the fluid inlet temperature, the removal factor of the solar collector \hat{F} is used. Given that the highest value of high temperature can not be defined on the surface of the adsorbent tube, Equation (14) is used [57]:

$$\dot{F} = \frac{\left(\frac{1}{U_l}\right)}{\left(\frac{1}{U_l} + \frac{1}{U_{L/a}}\right)} \tag{14}$$

Here, without considering the heat transfer mechanism in the fluid, the heat transfer coefficient of all CPC solar collectors U_l is calculated. The method uses the relationship between the experimental expression proposed by Duffy and Beckman 1991. The coefficient

of heat transfer losses of the solar energy receiver is calculated from Formula (15). Here U_l is the total coefficient of heat loss [58]:

$$\dot{F} = \frac{\left(\frac{1}{U_l}\right)}{\left(\frac{1}{U_l} + \frac{1}{U_{L/a}}\right)}$$
(15)

$$U_{l} = \left\{ \left(h_{tot,c-amb}^{-1}\right) + \frac{h_{tot,a-c}^{-1} \left[h_{tot,r-amb}^{-1} + \left(h_{tot,r-c}^{-1} + h_{tot,a-r}^{-1}\right)^{-1}\right]}{h_{tot,a-c}^{-1} + h_{tot,r-amb}^{-1} + \left(h_{tot,rad-c}^{-1} + h_{tot,a-r}^{-1}\right)^{-1}}\right\}^{-1}$$
(16)

Heat transfer between hot and enclosed air and the radiation receiver tube is referred to as internal heat transfer, and its value is obtained by the formula of instantaneous energy balance on the receiver tube [59,60].

$$G(\tau_{\mathcal{C}}\alpha_r) = q_{u-r} + q_{cover, r-c} + q_{rad, r-c}$$
(17)

where $G(\tau_C \alpha_r)$ is the solar energy passing through the glass coating and τ_C is the absorption coefficient of the glass coating and α_r is the absorption coefficient of the receiver.

$$q_{cover, r-c} = h_{cov, r-c}(T_r - T_c)$$
(18)

where the convective heat transfer coefficient is $h_{cov, r-c}$ and is calculated from Formula (18) [61,62]. 1 1

$$h_{tot,c-amb} = h_{cove,a-amb} + h_{rad,c-sky}$$
(19)

$$h_{tot,r-amb} = h_{cove,r-amb} + h_{rad,r-sky}$$
⁽²⁰⁾

$$h_{tot,a-r} = h_{cove,a-r} + h_{rad,a-r} \tag{21}$$

In the above formulas, the convective heat transfer coefficient between the environment and the glass coating is displayed with $h_{cov, c-amb}$ and is calculated from the following formula. Duffy and Beckman (1991) calculated the convective heat transfer coefficient between the environment and the glass coating [63]. The radiation heat transfer coefficient $h_{rad, c-amb}$ is calculated using the following equation [62,64,65].

$$h_{cove,r-amb} = (5.7 + 3.8V)\frac{A_r}{A_a}$$
⁽²²⁾

$$h_{cove,c-amb} = \frac{A_c}{A_a} (3.8V + 5.7)$$
(23)

In the formulas, the wind speed is V. The equations presented by Hsieh (1981) were used to calculate the convective heat transfer coefficient between the reflector and the absorber tube and the cover and the adsorbent tube [4]:

$$h_{cove,a-c} = (3.25 + 0.0085) \left(\frac{T_a - T_c}{4r_O}\right)$$
(24)

$$h_{cove,a-r} = (3.25 + 0.0085) \left(\frac{T_a - T_r}{4r_O}\right)$$
(25)

Given that the input of the current collector is considered to be fully developed, the outer diameter of the receiver tube of the solar collector is r_0 [66].

$$q_{cover, r-c} = h_{cov, r-c} (T_r - T_c)$$
(26)

where the average temperature of the receiver tube is T_r and the radiant heat transfer coefficient is $h_{cover, r-c}$.

(10)

On the collector cover, heat transfer occurs between the glass and the environment, which is the external heat transfer, in the form of various independent forms of heat transfer, such as convection and radiation, which is a large amount of heat loss. The instantaneous energy balance formula on the composite parabolic collector glass cover is as follows:

$$G(\alpha_c) + q_{rad,r-c} + q_{cover, r-c} = q_{cover, c-amb} + q_{rad,c-amb} + C_C \frac{dI_c}{dt}$$
(27)

where the CPC solar collector glass cover is absorbed by the absorption coefficient α_c and $G(\alpha_c)$ is the amount of radiant solar energy.

$$q_{cover, c-amb} = h_{cov, c-amb}(T_c - T_{amb})$$
(28)

$$q_{rad, c-amb} = h_{rad, c-amb}(T_c - T_{amb})$$
⁽²⁹⁾

where the radiant heat transfer coefficient is $h_{rad, c-amb}$ [67]. According to Hsieh (1981), the radiative heat transfer coefficient between the reflector and the absorber, the coating and the absorber, the coating and the reflector, the cover and the sky, can be evaluated by the following equations [64,65]

$$h_{rad,r-sky} = \varepsilon_c \sigma \left(T_r^2 + T_{sky}^2 \right) \left(T_c + T_{sky} \right) \left(\frac{A_r}{A_a} \right)$$
(30)

$$h_{rad,c-sky} = \varepsilon_c \sigma \left(T_c^2 + T_{sky}^2 \right) \left(T_c + T_{sky} \right) \left(\frac{A_c}{A_a} \right)$$
(31)

 ε_c is the diffusion coefficient of glass, σ is the Stephen Boltzmann's constant, T_c is the glass coating temperature, and Tsky is the sky temperature. The sky temperature is 6 degrees Celsius lower than the ambient temperature [68,69].

Where the glass temperature is T_c , the peripheral area of the receiver tube is A_r , and the diaphragm area A_a is [70].

$$h_{rad,a-c} = \frac{\sigma \left(T_a^2 + T_c^2\right) \left(T_a + T_c\right)}{\frac{1}{\varepsilon_c} + \left(\frac{A_c}{A_r}\right) \left(\frac{1}{\varepsilon_a} - 1\right)}$$
(32)

$$h_{rad,a-r} = \frac{\sigma \left(T_r^2 + T_a^2\right) \left(T_r + T_a\right)}{\frac{\left(1 - \varepsilon_r\right)}{\varepsilon_r} + \frac{1}{F_{a-r}} + \left(\frac{A_r}{A_a}\right) \frac{\left(1 - \varepsilon_a\right)}{\varepsilon_a}}$$
(33)

$$h_{rad,r-c} = \frac{\sigma(T_r^2 + T_c^2)(T_r + T_c)}{\frac{(1-\varepsilon_c)}{\varepsilon_c} + \frac{1}{F_{c-r}} + \left(\frac{A_c}{A_r}\right)\frac{(1-\varepsilon_r)}{\varepsilon_r}} \left(\frac{A_r}{A_a}\right)$$
(34)

$$F_{c-r} = \left(\frac{1}{2}\right) \left[\frac{A_r}{A_c} - \frac{(1 - \sec\theta_{1/2})(1 + 2\sec\theta_{1/2})}{\sec\theta_{1/2}}\right]$$
(35)

$$F_{a-r} = \left(\frac{A_r}{2A_a}\right) \left[1 - \left(\frac{A_c}{A_r}\right) \frac{(1 - \sec\theta_{1/2})(1 + 2\sec\theta_{1/2})}{\sec\theta_{1/2}}\right]$$
(36)

The first method is to use the relation of the total heat loss coefficient U_L . Hsieh (1983) used a CPC solar collector to obtain a relation for determining the total heat loss coefficient. The total heat loss coefficient U_L can be calculated from it [4,57,71]:

$$U_{L/a} = \left(\frac{r_0}{h_i r_i} + \frac{r_0}{k} \ln \frac{r_0}{r_i}\right)^{-1}$$
(37)

In this paper, a cpc collector is a tube for the solar energy absorber. Beer et al. (2014) conducted a study to analyze a coaxial lobe. They obtained the total heat loss coefficient using the thermal resistance analysis of a pipe. This is exactly the analogy presented by Hsieh (1981) [4]. This resistor consists of the sum of the convection heat transfer layer of

the tube wall resistor and the two sides of the tube inner wall. The coefficient of fluid convection in the inner and outer part of the tube is analyzed using the Gnielinski correlation. For the pipes, the diameter is equal to D = 2r [72].

$$h_f = 0.023 R^{0.8} P r^{0.4} \frac{k}{D} \tag{38}$$

The correlations are written in terms of the Nusselt number, the Prandtl number and the Reynolds number. $Nu = [(f/2)(R - 1000)Pr]/[1 + 12.7(f/2)(1/2) (\mathbb{Z} Pr\mathbb{Y}(2/3) - 1)]$ the mean value for use as hI was estimated in Equation (32) [73–76].

The increase in heat in the fluid is calculated by the energy balance in the collector suction pipe relative to the temperature difference of the suction pipe temperature difference with Formula (39):

$$Qu_a = SA_c - A_a U_l (T_a - T_{amb}) \tag{39}$$

Increasing the temperature of the fluid can be obtained by using the difference between the temperature of the adsorbent tube and the temperature of the working fluid with Formula (40):

$$Qu_f = U_{L/a} \left(T_a - T_f \right) \tag{40}$$

Figure 6 shows the calculation method for solving the mathematical model.



Figure 6. CPC solar collector simulation algorithm.

The simulated system is shown in Figure 7.



Figure 7. Simulated system.

The installed CPC collector system with the high-temperature heat pump is shown in Figure 8.



Figure 8. CPC collector system with high-temperature heat pump.

First, it is necessary to enter the meteorological data of the equipment installation site and the optical and thermal properties of the solar collector materials. CPC solar collectors are divided into specific control volumes according to the length of their tube to evaluate the fluid temperature and thermal properties along the tube. Here, just to calculate the convective heat transfer coefficients of the fluid, the average pipe heat loss (hl) must be calculated. Before continuing the thermal analysis of the solar collector, it is necessary to estimate the collector coating temperature, the absorber temperature, and the reflector. When the useful fluid temperature is calculated by iteration and the coating temperatures of the solar collector, absorber tube, and parabolic reflectors are equal to the initial estimated temperature, the simulation software stops the temperature calculation iterations. The next volume control simulation considers the fluid outlet temperature as the inlet temperature. Mathematical models were simulated and coded in Span Hayes and MATLAB.

2.3. CPC Collectors Installed

Figure 9 shows the installation diagram of the CPC solar collector and high-temperature heat pump and the piping equipment and CPC solar collector temperature control instrument that comply with the standard [ASHRAE 2014] [77].



Figure 9. Process status of the modeled system.

The CPC collector, which is installed as a hot water production system in a pipe manufacturing company, is shown in Figure 9. Installing CPC solar collectors in series or in parallel with the working fluid flow allows them to perform fluid circulation operations when the valves are opened or closed and to increase heat transfer. Additionally, to produce more hot fluid, several solar CPC collectors with specific capacities can be connected in series or in parallel.

3. Results and Discussion

In this study, the CPC solar collector system with oil working fluid with specific characteristics was used to transfer radiant energy heat. For one year, all experiments were performed daily, and the output temperatures were measured. The outlet temperatures of the tube are a function of the weather conditions and the amount of radiation. In the following, the amount of temperature and radiation is checked.

Environmental Conditions and Air Temperature

Due to the fact that Ahvaz is located in a hot and humid region and the temperature is warm in most months of the year, the high amount of air temperature and the temperature difference play important roles on the efficiency and power of the solar collectors. Solar collectors have different capacities on air temperature [58,78,79]. Table 2 shows the minimum and maximum air temperature of Ahvaz city. Figure 10 shows the daily changes in air temperature and Figure 11 shows the monthly changes.

Table 2. Minimum and maximum air temperature in Celsius [80].

Month	January	February	March	April	May	June	July	August	Septembe	r October	November	December
Max temperature °C	23	29	32	40	49	49	51.5	49	48	44	34	24
Min temperature °C	5	3	9	14	19	26	28	27	23	12	9	5.6
Ave temperature °C	14	16	20.5	27	34	37.5	39.8	38	35.5	28	21.5	14.8
		50 50 0 45 0 40 35 30 25 20 20		Www	N	mpenh	Minin	m	Mullin			

150

180 210

Day

240

270 300

330

360

Figure 10. Daily temperature in Ahvaz [80].

90 120

10

30

60



Figure 11. Monthly temperature in Ahvaz [80].

The normal direct radiation on the ramp for all months of the year is shown separately in Table 3 and the daily radiation in Figure 11. The daily radiation is compared in Figure 12 and the outlet temperature from the collector in similar researches in different lengths of the absorber tube in Figure 13.

Table 3. Normal direct radiation on the r	amp for all months of the year separately.
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Month	D	D DNI		I _O	I _T	I _T	
	Day of Year	kWh/m²/day	-	kW/m ²	kWh/m²/day	MJ/m²/day	
January	17	3.2	1.6896	5.7606	4.6579	16.7685	
February	45	4.33	1.4669	6.9832	5.7655	20.7559	
March	75	4.84	1.2127	8.6897	5.4931	19.7753	
April	105	5.44	1.0089	10.1974	5.4192	19.5091	
May	135	6.48	0.8772	11.1336	5.8823	21.1761	
June	162	7.31	0.8222	11.4671	6.3233	22.7639	
July	198	7	0.8463	11.2703	6.1864	22.2711	
August	228	6.67	0.9498	10.5255	6.3945	23.0203	
September	258	5.44	1.1262	9.2097	5.8837	21.1812	
Öctober	288	4.24	1.3664	7.541	5.2589	18.9321	
November	318	3.09	1.622	6.062	4.2809	15.4114	
December	344	2.83	1.7684	5.3768	4.2161	15.1781	



Figure 12. Daily radiation MJ/m².



Figure 13. Outlet temperature from the collector in similar research in different lengths of absorber tube.

The temperature of the fluid at the inlet point of the CPC collector adsorbent can be continuously measured with a thermometer. The results of the water outlet temperature at the adsorbent outlet point depend on the length of the CPC solar collector. In all diagrams, the temperature of the working fluid tends to increase, and this is related to the increase in the ambient temperature and solar energy that constantly appears on the receiver tube and is directly related to the length of the absorber tube. CPC solar collectors increase the inlet temperature of the working fluid by an average of 10 to 18 degrees depending on the calculated day number. This temperature is transferred to the heat pump after the heat and at the outlet of the heat pump. The temperature of the hot water increases and is transferred more than the temperature of the working fluid leaving the collector. In the characteristic curve of any CPC solar collector system, its efficiency curve allows the thermal efficiency to be measured based on the inlet temperature of the absorber tube, the ambient temperature at the collector installation site, and the solar radiation at the CPC solar collector installation site.

Figure 14 shows the effects of the absorber length and efficiency of CPC solar collector and the outlet temperature of the working fluid. According to the comparison and analysis of the results, the presented mathematical model is a logical result and in the experimental range of other researchers. Figures 15–17 show the characterization results of a CPC solar collector operating at a flow rate. The simulation results of the CPC solar collector in MAT-LAB and Aspen HYSYS software were evaluated and compared with the experimental results and the results of other researchers.



Figure 14. The efficiency of the collector in different lengths of the absorber tube has been compared in similar researches.



Figure 15. Absorption coefficient of CPC solar collector efficiency.



Figure 16. The efficiency of the collector has been compared with the maximum ambient temperature and with similar researches.



Figure 17. The efficiency of the collector has been compared with the minimum ambient temperature and with similar researches.

4. Conclusions

In this paper, the mathematical heat transfer network modeling and CPC solar collector simulation with an absorber tube were performed and evaluated. This study was performed using a CPC solar collector and a mathematical model with a length of 2.81 m and a width of 0.32 m and an inside diameter of 0.01 m. This study was performed based on a CPC solar collector installed in a pipe company during one year. The proposed simulator showed a difference of 5 °C with other results. The comparison of the results of other studies showed that under the same parameters, shortened CPC solar collectors with an absorber tube achieve a 10% higher efficiency.

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Nomenclature

- a absorber
- A CPC area (m²)
- amb environment
- Con convective heat transfer
- Cp specific heat of the fluid (kJ $\circ C^{-1}$ kg)
- D diameter (m)
- ex external
- f fluid
- F form factor
- F₀ elimination coefficient (-)
- fi inlet fluid
- fo effluent
- g coverage
- G solar radiation (W m²)
- h heat transfer coefficient (W m² K⁻¹)
- h₀ CPC height (m)
- hf coefficient of heat transfer coefficient of the fluid to the pipe wall (W m K^{-1})
- i internal
- k conductive heat transfer coefficient (W m K^{-1})
- L CPC length (m)
- m mass flow (kg s⁻¹)
- n number of reflections
- O optical
- o outlet
- P pressure (bar)
- Pr Prandtl number
- r absorber radius (m);
- r reflector
- Rad radiation
- Re Reynolds number
- S absorbed radiation per unit area (W m^{-2})
- sk sky
- T temperature (°C)
- Ul total heat transfer coefficient (W m² K⁻¹)
- Ula total heat transfer coefficient in the fluid (W $m^2 K^{-1}$)
- W CPC width (m)
- x₀ "x" point coordinate axis of CPC geometry
- y₀ "y" point coordinate axis of CPC geometry
- α CPC absorption coefficient
- γ interception factor
- ε cover release
- η optical efficiency
- θ wide angle
- ρ reflection
- σ Stephen Boltzmann constant
- τ transfer
- ϕ angle to determine

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