

Article

Simulation and Experimental Study on the Use of Ventilation Air for Space Heating of a Room in a Low-Energy Building

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Abstract: In thermally modernised buildings, sharing of ventilation heat loss becomes more significant. In the case of the application of ventilation with heat recovery, especially during transitional periods, there arises a question of whether an air system makes it possible to maintain the required indoor air temperature without the necessity of using a basic hydronic heating system. This paper presents the application of a simple thermal network model of a building zone to simulate indoor air temperature in a single room of a multi-storey building with a mechanical ventilation system with heat recovery. Ventilation air was supposed to be the only heat source and its ability to maintain the required indoor air temperature was checked in simulations and then compared with measurements. The 5R1C thermal network model of a building zone was used for simulations. Comparison with measurements showed the Mean Absolute Error (MAE) and Root Mean Square Error (RMSE) of indoor air calculation to be 2.37 °C and 2.45 °C, respectively. When including heat flux from the bottom storey through the floor, MAE = 1.28 °C and RMSE = 1.38 °C were obtained.

Keywords: indoor air temperature; heat recovery; thermal network model; 5R1C; air heating system



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1. Introduction

A dominating share of total energy use in Polish residential buildings belongs to space heating [1]. Therefore, thermal refurbishment of buildings in Poland has focused, so far, mainly on external walls, roofs, and windows [2–4]. However, in thermally modernised objects, the energy required to warm up cold external air supplied to the building's interior is more important [5–7]. For this reason, various solutions of ventilation heat recovery are applied both in new and thermally modernised buildings [8–10] resulting in lower heating energy demand [11–14].

At the design stage of each thermal refurbishment, the design heat load is calculated following the procedure provided in EN 12831 [15,16] for the external design temperature given in that standard. It depends on the climatic conditions of the area of interest [17]. The efficiency of the ventilation heat recovery, assumed by the system's designer, is also taken into account [18]. The calculated design load is the minimum thermal power that has to be supplied to the building zone to ensure thermal comfort during the heating season [19]. However, one should remember that the design external air temperature is an extreme value that may occur only for a short period of time in the year. Hence, the designed thermal power is not utilised permanently, which can be noticed in any thermal load duration curve of a single building or a heating network [20]. For two or more installed heat sources, this means the possibility to choose the most effective one in certain conditions. Therefore, in a building with a hydronic heating system and ventilation with heat recovery, there is a possibility to use only the latter under favourable outdoor weather conditions. It can be especially interesting in buildings after thermal retrofitting or in other energy efficient objects.

Numerous studies confirmed good indoor conditions in buildings with air handling units with cooling and heating coils combined with various, both low- and high-temperature, hydronic heating systems [21–24]. Several authors have also presented relevant case studies recently.

Harsem et al. [25] proposed a heating system for a hospital consisting of a ground source heat pump, gas boiler, borehole thermal energy storage, hydronic radiators, and an air handling unit. Calculations, performed in a developed simulation tool, allowed the selection of thermal capacity of heat pumps for their highest seasonal performance effectiveness. The authors also studied the impact of ventilation heat recovery efficiency and ventilation coil supply/return temperatures on the annual effectiveness of a system.

Javed et al. [26] studied an application of displacement ventilation to provide heating to a passive school building located in Norway. At first, experimental tests in a test cell and simulations in the IDA-ICE tool were performed to ensure that the simulation program is capable of computing thermal and contaminant stratification in a room with displacement ventilation. Field tests in the classroom revealed that the ventilation system was able to maintain an indoor operative temperature within the acceptable comfort range during winter conditions (outdoor temperature from $-7\text{ }^{\circ}\text{C}$ to $+3\text{ }^{\circ}\text{C}$).

Mao et al. [27] presented an application of stratum ventilation for space heating in a single room. Using CFD simulations in the Airpak 3.0.16 tool, they analysed the impact of room dimensions on air distribution, thermal comfort, and ventilation performance, obtaining the maximum suitable dimensions for the room. Temperature effectiveness of ventilation and dimensionless temperature were used as energy efficiency indicators of heating. Experiments in a test room confirmed the accuracy of simulations.

Ameen et al. [28] experimentally studied the usability of a corner-placed stratum ventilation system to provide cooling and heating in a medium test room. A total of 15 cases with three nominal supply air temperature setpoints of $17.7\text{ }^{\circ}\text{C}$, $21\text{ }^{\circ}\text{C}$, and $25\text{ }^{\circ}\text{C}$ and five different airflow rates from 30 to 70 L/s were investigated. The measured vertical temperature gradients and the velocity conditions satisfied the requirements of Category A of ISO7730 in all cases. Similar conclusions were given in the case of corner-impinging jet ventilation, corner-mixing ventilation, and displacement ventilation in the cooling and heating modes [29,30].

Kong et al. [31] investigated mixing and stratum ventilation for space heating in a test chamber. Experimental results confirmed good energy performance of stratum ventilation while maintaining required indoor thermal conditions. Ventilation effectiveness was also higher in this case: 0.98 in comparison to 0.74 for mixing ventilation.

In a simulation study [32], authors simulated in TRNSYS the use of exhaust ventilation air and the air-to-water compressor heat pump for space heating of a multifamily building. The proposed solution showed its potential for energy consumption reduction in five analysed locations in Poland. However, indoor comfort was not studied.

The presented studies proved the ability of ventilation to provide space heating while maintaining indoor thermal comfort during the heating season. Several authors noticed that this concept fits well with low-energy and passive houses [33–36]. However, the focus on the technical aspects of ventilation has made the issue of the building's heat balance and thermal dynamics recede into the background.

While considering the use of ventilation for space heating of a building, mainly professional and sophisticated simulation tools were used such as IDA ICE in the case of a municipal building [37–39]. Markiewicz-Zahorski et al. [40] analysed the conversion of an office building into a multi-family residential building based on monthly and hourly energy simulations in OZC and EnergyPlus simulation tools, respectively. Ventilation loss was included in the energy demand for space heating and cooling, but no information on considered ventilation systems was provided. Veršić et al. [41] simulated night passive cooling in an office building depending on the wind velocity using the building model of 3D Studio MAX 2016 and CFD Simscale software. Hourly energy simulations were performed implementing the hourly method of EN ISO 52016-1 [42] in Visual Basic 2017. Authors

not only analysed indoor thermal conditions but estimated cooling energy savings as well. They also presented selected waveforms of hourly indoor and outdoor air temperature, wind speed, and cooling load.

A simpler solution was used in [43] for the simulation of the hourly internal air temperature in a free-running building with a double skin façade. For this application, authors accordingly modified the 5R1C (five resistors and one capacitor) thermal network model of a building zone from EN ISO 13790 [44]. It is intended only for the calculation of sensible heating and cooling power, so the humidification and dehumidification processes of air cannot be considered here.

That standard has been replaced recently by EN ISO 52016 [42] which, among others, introduced a more detailed hourly simulation method [45]. However, despite its complexity, authors reported differences in output results between this new method and more sophisticated professional simulation tools [46–48]. Hence, it was decided to apply the simpler method of EN ISO 13790, still used in practice [49,50].

This model is of special interest because of several important advantages, such as low computational requirements [51–53], allowing it to be implemented in a spreadsheet [54,55], and easy modification for various applications [56–59]. Despite the used simplifications, such as lumping all partitions into single thermal capacitance, it provides reliable results [60].

Thanks to these features, it was also used in studies related to various aspects of ventilation in buildings. Costantino et al. [61] analysed the indoor climate in broiler houses and the required ventilation flow rate dependent on the broiler's age. Hedegaard et al. [62] simulated the district heating consumption of large groups of residential buildings. Natural ventilation in the 5R1C network was modelled by infiltration and window opening by occupants. The latter component was described by a relationship between the outdoor air temperature and the window openings. In [63], energy use in mechanically ventilated greenhouses was modelled. The 5R1C scheme was applied to solve the sensible energy balance and then indoor air humidity was computed. Depending on the resulting thermal conditions, various ventilation strategies of a greenhouse were introduced. Buonomano et al. [64] modified the model to simulate the behaviour of a building with integrated solar thermal collectors. The building's occupancy schedule assumed two values of ventilation airflow depending on the season and indoor temperature. Jędrzejuk and Rucińska [1] proposed a method to assess the need for artificial cooling of residential buildings. It was based on hourly indoor operative temperature, calculated by the 5R1C model, and then compared with the defined limit.

Two conclusions emerge from the review presented. Firstly, the assessment of ventilation use for space heating was simulated using mainly professional and sophisticated tools. They are accurate but too time-consuming, especially at the stage of quick preliminary calculations. Secondly, dynamic simulations, especially hourly, can be performed with the simple but well-founded 5R1C model. However, so far, studies on space heating by ventilation with the use of this model have not been presented.

This paper aims to fill this gap by presenting a case study based on simulation and measurements taken in a single room in a building that was thermally refurbished to the low-energy standard.

The next section presents the thermal model of a building zone used for simulations and the experimental setup used during the measurement campaign. Then, statistical indicators used for the evaluation of the model's ability to simulate indoor air temperature are given. In Section 3, detailed results of the measurements and simulations are presented. Finally, concluding remarks are given.

2. Materials and Methods

2.1. The 5R1C Model

The 5R1C thermal network model of a building zone is composed of five thermal conductances and a single capacitor and is presented in Figure 1.

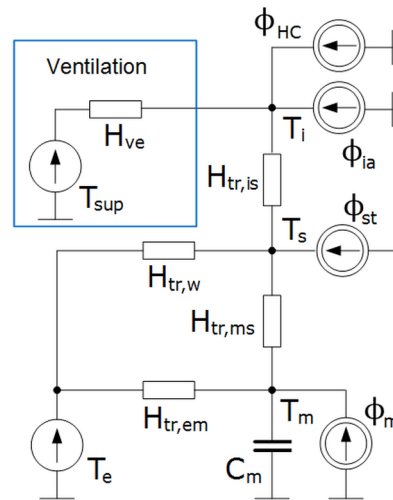


Figure 1. The 5R1C thermal network model of a building zone from EN ISO 13790.

There are distinguished two kinds of building partitions in that circuit. The first group, included in the $H_{tr,w}$ thermal transmission coefficient, consists of thermally “light” building elements (doors, windows, curtain walls, and glazed walls). The second one includes thermally “heavy” elements (walls, ceilings), which are described by the external ($H_{tr,em}$) and the internal ($H_{tr,ms}$) parts connected to the thermal capacity (C_m), representing the thermal mass of the building [65].

The external air temperature is modelled by the T_e source. The T_{sup} source is the supply air temperature, which is connected to the heat transfer by ventilation (H_{ve}). The indoor air temperature is represented by T_i and is connected through the coupling conductance $H_{tr,is}$ with the central node (T_s).

This model is intended for computations in hourly time steps. As a result, the hourly sensible heating or cooling power required to maintain a certain set-point indoor air or indoor operative temperature, ϕ_{HC} , is obtained. This procedure has been presented recently [58,66,67]. Each time step begins with the calculation of heat fluxes due to internal sources (ϕ_{int}) and solar irradiance (ϕ_{sol}), which are divided into three components: ϕ_{ia} , ϕ_{st} , and ϕ_m , connected to the indoor air, central, and thermal mass temperature nodes, respectively. These components are obtained from the following relationships:

$$\phi_{ia} = 0.5\phi_{int}, \quad (1)$$

$$\phi_m = \frac{A_m}{A_t}(0.5\phi_{int} + \phi_{sol}), \quad (2)$$

$$\phi_{st} = \left(1 - \frac{A_m}{A_t} - \frac{H_{tr,w}}{9.1A_t}\right)(0.5\phi_{int} + \phi_{sol}). \quad (3)$$

The solution of the network is based on the Crank–Nicholson scheme. The resulting nodal temperatures T_i and T_s are averages for one hour. The thermal mass temperatures $T_{m,t}$ and $T_{m,t-1}$ are instantaneous values at time t and $t-1$, respectively. $T_{m,t}$ is given by the equation:

$$T_{m,t} = \frac{T_{m,t-1} \left(\frac{C_m}{3600} - \frac{H_{tr,3} + H_{tr,em}}{2} \right) + \phi_{m,tot}}{\frac{C_m}{3600} + \frac{H_{tr,3} + H_{tr,em}}{2}}, \quad (4)$$

where:

$$\phi_{m,tot} = \phi_m + H_{tr,em}T_e + \frac{H_{tr,3}}{H_{tr,2}} \left(\phi_{st} + H_{tr,w}T_e + H_{tr,1} \left(\frac{\phi_{ia} + \phi_{HC}}{H_{ve}} + T_{sup} \right) \right), \quad (5)$$

with:

$$H_{tr,1} = 1/(1/H_{ve} + 1/H_{tr,is}) \quad (6)$$

$$H_{tr,2} = H_{tr,1} + H_{tr,w} \quad (7)$$

and:

$$H_{tr,3} = 1/(1/H_{tr,2} + 1/H_{tr,ms}). \quad (8)$$

When considering a zone that has to be heated only by ventilation air and ventilation airflow is known, then $\varphi_{HC} = 0$ should be assumed.

The ventilation heat transfer coefficient is computed from the relationship:

$$H_{ve} = \rho_a \cdot c_a \cdot q_{ve}, \quad (9)$$

with the volumetric heat capacity of air is assumed to be constant at $\rho_a c_a = 1200 \text{ J/m}^3\text{K}$ according to EN ISO 13790. However, both ventilation air density and specific heat capacity may vary following outdoor environmental conditions [68,69].

Finally, average hourly values of nodal temperatures are as follows:

$$T_m = (T_{m,t} + T_{m,t+1})/2, \quad (10)$$

$$T_s = \frac{H_{tr,ms}T_m + \phi_{st} + H_{tr,w}T_e + \frac{H_{tr,3}}{H_{tr,2}} \left(H_{tr,1} \left(\frac{\phi_{ia} + \phi_{HC}}{H_{ve}} + T_{sup} \right) \right)}{H_{tr,ms} + H_{tr,w} + H_{tr,1}}, \quad (11)$$

and the internal air temperature:

$$T_i = \frac{H_{tr,ms}T_m + H_{ve}T_{sup} + \phi_{ia} + \phi_{HC}}{H_{tr,is} + H_{ve}}. \quad (12)$$

In addition, based on the circuit diagram from Figure 1 and Equation (9), the ventilation heat flux can be also computed:

$$\phi_{ve} = H_{ve} \cdot (T_{sup} - T_i). \quad (13)$$

2.2. Experimental Setup

Measurements were conducted from 22 December 2021 to 3 January 2022 in a single room in one of the student dormitories in Kraków (south Poland). The whole building was thermally modernised in the year 2017. Its main heating system consists of hydronic radiators connected to the district heating network. That system was sized following the EN 12831 standard and, for the considered room, the design heating load is $\varphi_{HL} = 366 \text{ W}$ at the design outdoor and indoor air temperatures of $-20 \text{ }^\circ\text{C}$ and $20 \text{ }^\circ\text{C}$, respectively. This radiator was turned off during the experiment.

The balanced mechanical ventilation system supplies ventilation air to living spaces. The design ventilation airflow rate of $40 \text{ m}^3/\text{s}$ was assumed for the analysed room. The design supply ventilation air temperature $T_{sup} = 22 \text{ }^\circ\text{C}$ throughout the year. The air handling unit's heating coil is supplied by the central heating system. The heating water with design supply and return temperature of $60 \text{ }^\circ\text{C}$ and $40 \text{ }^\circ\text{C}$, respectively, is supplied from the heat exchanger connected to the district heating network.

The selected room was on a rectangular plane of $4.0 \text{ m} \times 2.7 \text{ m}$ with a height of 2.50 m (Figure 2a). The total internal volume of the room (27 m^3) can be reduced by the enclosed furniture, i.e., by 4.84 m^3 . The locations of the sensors in the room are given in Figure 2b. The external wall with windows was east-oriented, which minimised the impact of solar irradiance.

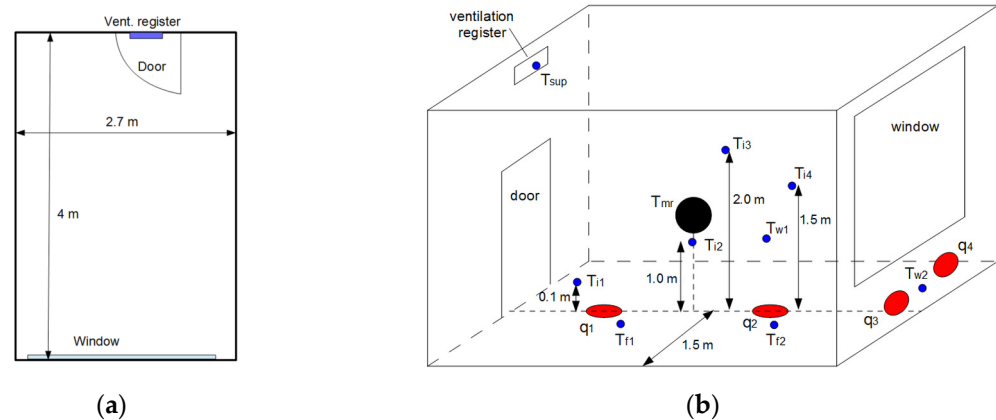


Figure 2. The test room: (a) View of the room selected for experiment; (b) Schematic location of sensors in the room.

In the experiment, four heat flux sensors were used: two on the inside surface of the external wall and two on the floor. Because of low expected values of output signals from these sensors, following manufacturer recommendations, they were connected in series in relevant pairs to logger inputs: $q_1 + q_2$ and $q_3 + q_4$ for the floor and for the external wall, respectively.

Global solar irradiance incident on the external wall was measured by the CMP11 Kipp & Zonen pyranometer. Pt100 and Pt1000 platinum resistance sensors were used for the measurement of indoor air (4 sensors: T_{i1} , T_{i2} , T_{i3} , and T_{i4}), floor surface (2 sensors: T_{f1} and T_{f2}), internal surface of walls (2 sensors: T_{w1} and T_{w2}), ventilation air (T_{sup}), and external air (T_e) temperatures. For air temperature measurements, sensors with low emissivity sheaths were used to minimise the impact of heat transfer by radiation. A globe thermometer with a Pt100 measured the mean radiant temperature at the height of 1.2 m above the floor (Figure 3a). Because of the number of sensors, two data loggers were used: MS6D (Comet) and RSG30 (Endress+Hauser). The measured data were recorded in 10 min intervals. The main parameters of all sensors are listed in Table 1. The ventilation airflow rate was checked several times during the study using a Testo 417 anemometer with an additional air cone (Figure 3b).

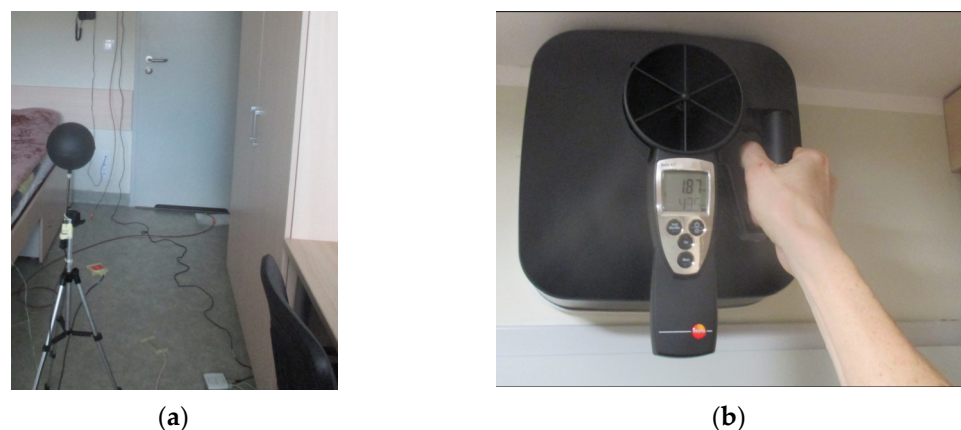


Figure 3. (a) View of the measurement equipment during assembling; (b) Measurement of ventilation airflow rate with Testo 417 anemometer.

Table 1. The main metrological parameters of the measuring sensors used.

Sensor	Measured Variable	Measurement Range	Accuracy
Pt100/Pt1000 platinum resistance sensor	Air and floor temperature	−50 °C ÷ +150 °C	Class A ⁽¹⁾
TP875.1 with the Pt100 sensor	Radiant temperature	−30 °C ÷ +120 °C	±0.2 °C
CMP11 Kipp&Zonen	Global solar irradiance	0 ÷ 4000 W/m ²	Spectrally Flat Class A ⁽²⁾
HFP01 Hukseflux	Heat flux	−2000 ÷ 2000 W/m ²	±3%
Testo 417	Airflow rate	0 ÷ 200 m ³ /h	±0.1 m ³ /h ⁽³⁾

⁽¹⁾ According to EN 60751; ⁽²⁾ According to ISO 9060; ⁽³⁾ Resolution for 0 ÷ 99.9 m³/h range.

Additionally, for sky temperature measurement, the IR thermometer based on an MLX90614 sensor was applied [70]. Numerous studies confirmed its ability for non-contact temperature measurements of temperature in various environmental and building-related applications [71,72]. It has a typical accuracy of ±0.5 °C and a measurement range for object temperature from −70 °C to 380 °C and for sensor temperature from −40 °C to 125 °C.

2.3. Evaluation of the Model

To assess the model's ability to simulate indoor air temperature under the assumed operating conditions of the heating and ventilation system, statistical analysis was performed using several basic indicators such as the mean absolute error (MAE), the root mean square error (RMSE), the mean square error (MSE), and the coefficient of determination (R^2) [73–77].

Assuming that x_i is its actual (reference) value of a given physical quantity, x , taken from measurements and \hat{x}_i is its value predicted by the model, \bar{x}_i is the average reference value of x and n is the total number of samples, then it can be written that the aforementioned metrics are given by the following relationships:

$$\text{MAE} = \sum_{i=1}^n \frac{|\hat{x}_i - x_i|}{n}, \quad (14)$$

$$\text{RMSE} = \sqrt{\sum_{i=1}^n \frac{(\hat{x}_i - x_i)^2}{n}}, \quad (15)$$

$$\text{MSE} = \sum_{i=1}^n \frac{(\hat{x}_i - x_i)^2}{n}, \quad (16)$$

$$R^2 = 1 - \frac{\sum_{i=1}^n (x_i - \hat{x}_i)^2}{\sum_{i=1}^n (x_i - \bar{x})^2}. \quad (17)$$

3. Results and Discussion

3.1. Measurements

The measurement campaign was conducted from 22 December 2021 to 3 January 2022 during the Christmas break when there were no occupants in the room. Hence, the troublesome estimation of internal gains was neglected. However, the building's HVAC systems were operating normally due to the presence of international students.

During the studied period, outdoor conditions varied significantly (Figure 4a). The external air temperature ranged from −11.1 °C (at 8:00 on 26 December) to 13.2 °C (at 12:00 on 2 January). The global solar irradiance (Figure 4 b) incident on the external surface of the considered wall ranged from 0 to 223.3 W/m² (at 12:00 on 26 December).

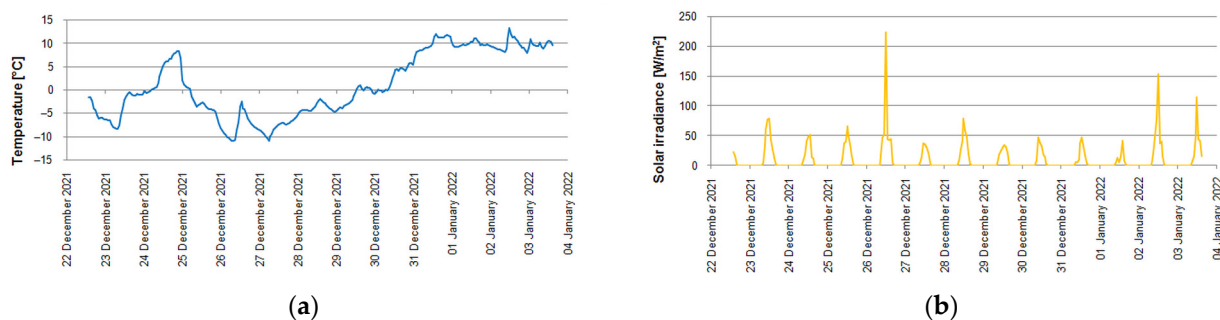


Figure 4. Meteorological conditions during the experiment: (a) External air temperature; (b) Global solar irradiance on the external wall.

Indoor air temperature, measured at four heights along the main door-window axis of the room showed high uniformity (Figure 5a). The highest and the lowest values were noticed for the T_{i3} sensor placed in the centre of the room and for the T_{i4} sensor located about 1.5 m from the window, respectively. T_{i4} ranged from 22.1 °C to 24.5 °C while T_{i3} ranged from 22.4 °C to 24.8 °C. The hourly difference between these two varied from 0.2 °C to 0.5 °C so it is of the same order as temperature measurement uncertainty (about 0.5 °C) and can be treated as negligible. The ventilation air temperature varied more significantly, from 21.3 °C (5:00 on 27 December) to 25.8 °C (11:00 on 24 December). Comparing Figure 4a with Figure 5a it can be noticed that T_{sup} was influenced by outdoor conditions (T_e). However, during the whole analysed period, T_{sup} was within the range between 21 °C and 26 °C acceptable for indoor comfort requirements.

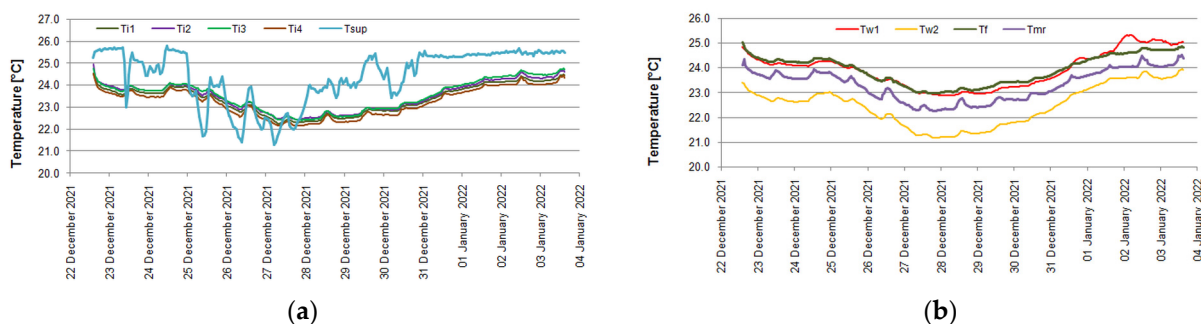


Figure 5. Measurement results: (a) Indoor and supplying air temperature; (b) Mean radiant, floor, and internal wall temperature.

The second important investigated group of parameters included temperatures of internal surfaces of the floor (T_{f1} and T_{f2}), internal wall (T_{w1}), and external wall (T_{w2}). In addition, the mean radiant temperatures of all internal surfaces facing the tested room measured by the globe thermometer, T_{mr} , were also considered [78–80].

The difference between T_{f1} and T_{f2} was up to 0.2 °C while the difference between the temperature of the internal wall (T_{w1}) and the averaged floor temperature was up to 0.7 °C. In both cases, these discrepancies may be treated as negligible. However, larger differences were noted in the case of the temperature of the internal surface of the external wall (T_{w2}). Due to heat loss to ambient air, it varied from 21.2 °C (22:00 on 27 December) to 23.9 °C (14:00 on 3 January), and in relation to the floor, the temperature was lower by up to 1.8 °C. This was the main reason why the mean radiant temperature (T_{mr}) was higher than T_{w2} and lower than T_f and T_{w1} . Unfortunately, due to the lack of temperatures of other internal surfaces, radiant temperature calculated using relevant view factors could not be obtained for comparison [81].

In the present study, due to the main focus on the ventilation air system and due to the practical problems with accurate measurement of heating power, the convective

hydronic radiator was turned off during the experiment. In the studied object, this can be justified by the relatively small area of the tested room in relation to the entire facility and the good insulation of its envelope, limiting heat loss to the environment. However, in a real building, it is impossible to completely limit the heat exchange with neighbouring rooms as in the adiabatic system. In multi-family buildings, when a radiator in a given flat is lowered or is out of service, this has an impact on the average indoor temperature of the whole building [82]. Therefore, the measurement of the heat flux density flowing through the floor of the room was carried out. This partition was chosen due to the natural tendency of heat to flow upwards as a result of heat gains on the lower storeys and lower thermal resistance for this direction in comparison to other cases [83].

The measured heat flux density varied from 1.0 W/m^2 (12:00 on 3 January) to 2.6 W/m^2 (6:00 on 29 December), which means heat flux from 12.4 W to 30.9 W . These changes were rather connected with ambient conditions than with heat storage in a floor (or, more generally, in the whole building's structure) and its transfer between storeys (Figure 6).

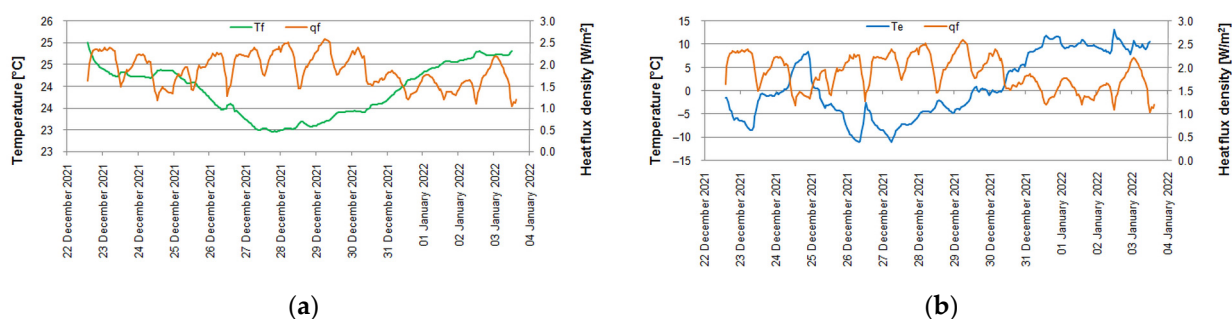


Figure 6. Measurement results: (a) Floor temperature and floor heat flux density; (b) Outdoor air temperature and floor heat flux density.

Finally, from Equation 9, the heat flux due to ventilation can be calculated (Figure 7). As the variation of T_{sup} was below $5 \text{ }^\circ\text{C}$, it was treated as negligible when considering the resulting air density and specific heat capacity of air and constant $\rho_a c_a = 1200 \text{ J/m}^3\text{K}$ was assumed. Then, as the indoor air temperature was rather stable, ϕ_{ve} followed the changes in T_{sup} .

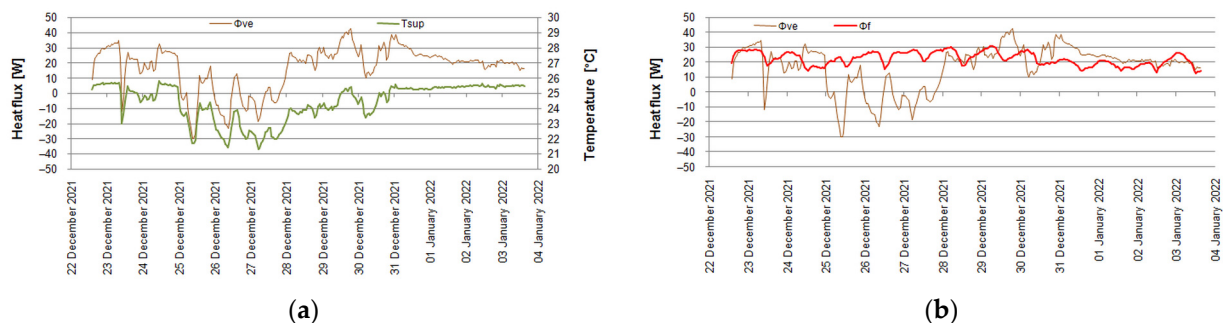


Figure 7. Measurement results: (a) Calculated ventilation heat flux and supplying air temperature; (b) Calculated ventilation heat flux and measured floor heat flux.

Ventilation heat flux ranged from -30 W (10:00 on 25 December) to 42.7 W (19:00 on 29 December) and, except for the period between 25 and 28 December, was of the same order as heat flux through the floor (ϕ_f).

There are no installed thermostats in the building and the indoor air temperature in the analysed room was the result of current thermal conditions. In case of unfavourable indoor conditions, occupants may use window opening or roller blinds to prevent overheating or set the thermostatic valve on the radiator.

3.2. Simulations

Values of thermal conductances and single capacitance (Table 2) in the network model of the room were calculated following the procedures given in EN ISO 13790.

Table 2. Thermal network model elements of the building.

Element	Value	Unit
$H_{tr,w}$	2.61	W/K
$H_{tr,is}$	193.48	W/K
$H_{tr,ms}$	264.32	W/K
$H_{tr,em}$	0.84	W/K
H_{ve}	16.67	W/K
C_m	2.63	MJ/K

The physical properties of materials were obtained from the manufacturers and from PN-EN EN ISO 10456 [84]. Thermal resistances were calculated using the procedure of ISO 6946 [83]. Thermal bridges were neglected. Thermal capacitances were calculated using the detailed method of ISO 13786 [85] for a calculation period of 24 h.

Due to the relatively low variation of the supply air temperature (below 5 °C—see Figure 5a), the volumetric heat capacity of air was assumed to be constant at $\rho_a c_a = 1200 \text{ J/m}^3\text{K}$ according to EN ISO 13790, as in other studies [65,86,87].

Solar absorptance of the external wall: $\alpha_{sol} = 0.9$. The total solar energy transmittance of glazing $g_{gl} = 0.54$ was taken from the technical data of the manufacturer.

Simulations were performed in two cases. They differed by only one element, namely heat flux by the floor. In the first case, it was omitted, but in the second one, it was taken into account as internal heat gain, φ_{int} .

Figure 8 presents a comparison of measured and calculated internal air temperature. In the first case, the hourly difference between them varied from 1.1 °C (15:00 on 3 January) to 3.4 °C (22:00 on 27 December). In the second case, this discrepancy was lower and ranged from 0.1 °C (12:00 on 3 January) to 2.3 °C (22:00 on 27 December). Better quality in the second case can be also shown by the aforementioned statistical measures (Table 3).

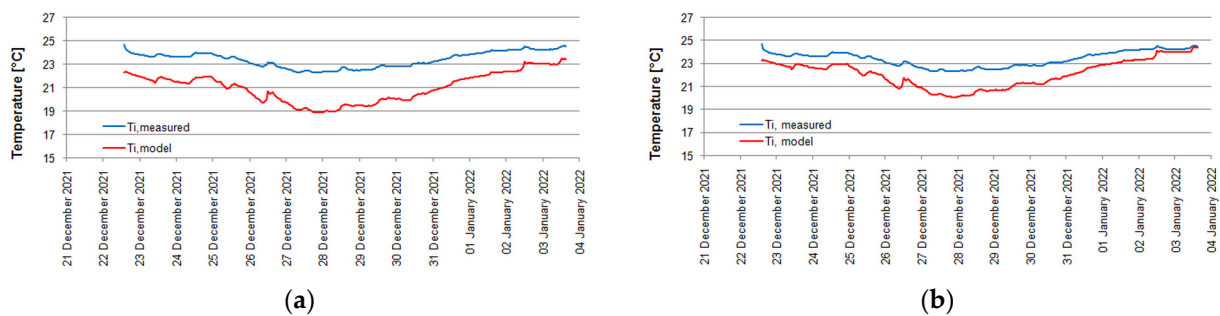


Figure 8. Measured and simulated indoor air temperature: (a) Case 1; (b) Case 2.

Table 3. Statistical indicators for indoor air simulation obtained for both cases.

Element	Case 1	Case 2
MAE	2.37	1.28
RMSE	2.45	1.38
MSE	5.98	1.91
R^2	0.71	0.77

It also should be mentioned that comparing Figure 8 with Figure 4a, it can be noticed that during the second part of the measurement period, when the outdoor temperature was positive, the difference between simulated and measured indoor air temperature was

lower than it was during the remaining time. This may indicate that during the warmer period, the differences between indoor temperatures between neighbouring rooms, which were not measured in this study, were less significant.

Measurement results presented in Figure 6 show that heat flux density through the floor was very small and the inclusion of this quantity into the thermal balance of the room significantly improved the quality of simulation results (Table 3). When multiplying this heat flux by 1.8, i.e., by adding heat flux from 22.3 W to 55.6 W to the base case, the following values of the aforementioned metrics were obtained: MAE = 0.50 °C, RMSE = 0.62 °C, MSE = 0.39 °C², and R² = 0.808. An additional heat gain of 50 W, which is lower than in the case of moderate activity of a single person [88], could be sufficient to obtain very good quality modelling results. From this, two conclusions can be drawn. Firstly, internal temperatures in neighbouring rooms should be measured to determine the possibility of heat flow between them, because it may be a significant problem in energy-efficient buildings [89]. Secondly, an additional heater with controlled and measured heating power can be installed in the considered room to easily control thermal stability between rooms.

However, to obtain a more detailed view of the results there should be also made a comparison with other works with thermal measurements and simulations in buildings.

Bagheri et al. [90] simulated a simple single-zone building in thermally heavy and light versions using the TRNSYS program. Outputs from these simulations were used as datasets for the parameter identification in MATLAB of the 4R3C model of a building. In [91], authors used thermal network models of various complexities, namely: 2R1C, 3R1C, 4R3C, 5R3C, 5R4C, and 4R2C for the simulation of two residential test houses. The models were identified in a MATLAB environment using datasets generated by the detailed simulation TRNSYS program. Then, model outputs were compared with TRNSYS results and performed measurements.

Boodi et al. [92] used a parameter identification of a 3R2C model for the simulation of a single room in an educational building. The 3R2C network was used for each external wall, floor, and roof, resulting in the 22R9C model of the studied zone. It was then validated against measurements, but no quantitative indicators were used for this purpose.

In [93], the author used the 5R1C model of EN ISO 13790 to model natural stack ventilation in a residential building. Then, a comparison with the annual hourly simulation in EnergyPlus was made for hourly ventilation flow. In [43], the model was expanded for the simulation of indoor air temperature in a test cell with a double skin façade. The authors also presented a review of various experimental studies of real buildings and test cells in free-running conditions showing that the mean and maximum typical errors of internal air temperature were from 0.3 °C to 2.9 °C and from 1.8 °C to 21.9 °C, respectively.

In [94], this model was modified to the 4R1C version to better describe varying ventilation flow. Simulations in EnergyPlus for 10 different locations were performed for comparison.

Wang et al. [95] used the 3R2C model to simulate the thermal behaviour of a single-family one-story test home. Measurements were used for the identification of the model parameters and then also for 24 h indoor temperature prediction.

Danza et al. [96] used the 3R2C network for each element of a building's envelope. The model was validated against measurements in a test cell showing an average underestimation of an internal air temperature of −0.08 K.

Vivian et al. [97] presented an evaluation of the 5R1C and 7R2C models to compute the thermal needs of buildings in relation to TRNSYS simulations. Detailed analysis of errors for heating needs and peak load estimation was presented but no further considerations on internal air temperature were given.

Barone et al. [98] developed in MATLAB a simulation tool DETECt based on the thermal resistance-capacitance network approach. They performed an extensive validation procedure using BESTEST tests and measurements taken in a test room located in an educational building. The Mean Absolute Error for indoor air temperature from February to October was 0.39 °C.

Numerous studies devoted to the application of resistance-capacitance models for the thermal modelling of buildings focused only on thermal load analyses, not providing any data on indoor air prediction accuracy [60,66,99]. Only several considered the indoor air temperature (Table 4).

Table 4. Simulations of buildings with the use of thermal network models with error analyses of indoor air temperature.

Reference	Object	Model	Simulation	Measurement	MAE	RMSE	MSE	R ²
[91]	9 zones	2R1C	TRNSYS	N	n.a.	6.55 °C	42.51 °C ²	n.a.
[91]	9 zones	3R1C	TRNSYS	N	n.a.	8.49 °C	17.71 °C ²	n.a.
[91]	9 zones	4R3C	TRNSYS	N	n.a.	1.06 °C	0.76 °C ²	n.a.
[91]	9 zones	5R3C	TRNSYS	N	n.a.	5.02 °C	3.37 °C ²	n.a.
[91]	9 zones	5R4C	TRNSYS	N	n.a.	0.70 °C	0.81 °C ²	n.a.
[91]	9 zones	4R2C	TRNSYS	N	n.a.	3.08 °C	6.72 °C ²	n.a.
[43]	1 zone	5R1C	-	Y	0.95–1.13 °C	n.a.	n.a.	n.a.
[94]	1 zone	4R1C	EnergyPlus	N	0.30–0.48 °C	0.61–0.93 °C	0.37–0.86 °C ²	0.84–0.93
[95]	1 zone	3R2C	-	Y	0.34–0.5 °C	0.42–0.65 °C	n.a.	n.a.

The presented review reveals that there is no study focusing on the simulation of a single, selected room or zone in a more complex, multifamily, building. For this purpose, more detailed simulation tools are used such as EnergyPlus, TRNSYS, ESP-r, or others. Only Shen et al. [58] proposed a modification of a generic 5R1C scheme with zone thermal coupling. They performed an extensive validation of the model against detailed EnergyPlus simulations. The presented values of errors for heating and cooling loads predictions confirmed the good accuracy of the proposed solution. However, the authors did not show such an analysis with regard to internal air temperature. In addition, as the temperature of neighbouring zone is required, this model could not be used in the present study.

An interesting addition to the presented research is the study by Zhang et al. [100] in which authors compared CFD simulation with measurements performed in a test chamber to assess the effect of selected parameters on indoor air quality, indoor comfort, and energy efficiency of stratum ventilation used for space heating. The authors suggested setting maximum ventilation flow and modulation of supply air temperature following the outdoor weather condition.

4. Conclusions

This paper presents the application of a simple thermal network model of a building zone to simulate indoor air temperature in a single room of a multi-storey building with a mechanical ventilation system with heat recovery. Ventilation air was supposed to be the only heat source and its ability to maintain the required indoor air temperature was checked in simulations and then compared with measurements. The performed measurements showed the practical applicability of the analysed ventilation system to provide space heating while maintaining indoor air temperature within the required range under studied outdoor conditions.

For simulations, the simple but well-known 5R1C thermal network model of a building zone from EN ISO 13790 was used. Comparison with measurements showed the Mean Absolute Error (MAE) and Root Mean Square Error (RMSE) of the calculated indoor air temperature to be 2.37 °C and 2.45 °C, respectively.

As these values were not satisfying, further analysis was performed. When including heat gains from the bottom storey, a significant improvement in the quality of prediction was obtained with MAE = 1.28 °C and RMSE = 1.38 °C. Further introduction of artificial heat flux with a value of 80% resulted in MAE = 0.50 °C and RMSE = 0.62 °C. Hence, in future measurements, it can be checked whether the quality of the model will be better during normal use of the room when internal gains for occupants can be added.

It also would be advisable to measure the temperature of internal surfaces facing the considered room in terms of indoor comfort and the impact of solar irradiance. The indoor temperature in surrounding rooms should also be known to determine the possibility of heat transfer direction between them and the analysed space. The simulation model can be also extended to include additional couplings with neighbouring zones.

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Symbols

A_f	total conditioned (heated and/or cooled) floor area, m ²
A_m	effective thermal mass area, m ²
C_m	thermal capacity of the building, J/K
$H_{tr,em}$	external part of the $H_{tr,op}$ thermal transmission coefficient, W/K
$H_{tr,is}$	coupling conductance, W/K
$H_{tr,ms}$	internal part of the $H_{tr,op}$ thermal transmission coefficient, W/K
$H_{tr,op}$	thermal transmission coefficient for thermally heavy envelope elements, W/K
$H_{tr,w}$	thermal transmission coefficient for thermally light envelope elements, W/K
H_{ve}	thermal transmission coefficient by ventilation air, W/K
T_e	external (outdoor) air temperature, °C
$T_{e,mn,an}$	mean annual temperature of outdoor air, °C
$T_{e,max,m}$	maximum mean monthly temperature of outdoor air, °C
T_i	internal (indoor) air temperature, °C
$T_{i,C,set}$	set-point indoor air temperature for cooling, °C
$T_{i,H,set}$	set-point indoor air temperature for heating, °C
T_m	average air temperature in the duct, °C
T_s	central node temperature, °C
T_{sup}	supply air temperature, °C
c_a	specific heat capacity of air, J/(kg·K)
ρ_a	air density, kg/m ³
φ_{ia}	heat flow rate to internal air node, W
φ_{int}	heat flow rate due to internal heat sources, W
φ_m	heat flow rate to mass node, W
φ_{sol}	heat flow rate due to solar heat sources, W
φ_{st}	heat flow rate to central node, W
φ_{ve}	heat flow rate by ventilation, W
φ_{HC}	heating or cooling power supplied to or extracted from the indoor air node, W

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