

Article

Design and Implement a Digital H_∞ Robust Controller for a MW-Class PMSG-Based Grid-Interactive Wind Energy Conversion System

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Abstract: A digital H_∞ controller for a permanent magnet synchronous generator (PMSG) based wind energy conversion system (WECS) is presented. Wind energy is an uncertain fluctuating resource which requires a tight control management. So, it is still an exigent task for the control design engineers. The conventional proportional-integral (PI) control is not ideal during high turbulence wind velocities, and the nonlinear behavior of the power converters. These are raising interest towards the robust control concepts. The robust design is to find a controller, for a given system, such that the closed-loop system becomes robust that assurance high-integrity and fault tolerant control system, robust H_∞ control theory has befallen a standard design method of choice over the past two decades in industrial control applications. The robust H_∞ control theory is also gaining eminence in the WECS. Due to the implementation complexity for the continuous H_∞ controller, and availability of the high speedy micro-controllers, the design of a sample-data or a digital H_∞ controller is very important for the realistic implementation. But there isn't a single research to evaluate the performance of the digital H_∞ controller for the WECS. In this paper, the proposed digital H_∞ controller schemes comprise for the both generator and grid interactive power converters, and the control performances are compared with the conventional PI controller and the fuzzy controller. Simulation results confirm the efficacy of the proposed method

which are ensured the WECS stabilities, mitigate shaft stress, and improving the DC-link voltage and output power qualities.

Keywords: digital H_∞ controller; wind energy conversion system; fuzzy controller; PMSG; high wind turbulence

1. Introduction

Over the period 1990–2010, fossil fuels (e.g., oil, coal, gas) contributed 83% of the growth in energy. Due to the crisis of exhausting fossil fuels and considering the green-house effect, it is predicted that over the next twenty years, fossil fuels contribute 64% of the growth in energy. Renewables (e.g., wind, solar, hydro, wave, biofuels) account for 18% of the growth in energy to 2030. The rate at which renewables penetrate the global energy market is similar to the emergence of nuclear power in the 1970s and 1980s [1]. Among the renewable sources, wind energy is one of the most rapidly growing renewable power source [2]. Wherever the wind speed exceeds approximately 6 m/s there are possibilities for exploiting it economically, depending on the costs of competing power sources [3].

Variable speed wind turbines (VSWTs) can utilize the wind energy proficiently. VSWTs are equipped with the doubly fed induction generators (DFIGs) or the permanent magnet synchronous generators (PMSGs). The popularity of the PMSG based wind energy conversion system (WECS) has been increased because of the simple structure, availability, and efficient power producing capability [4]. However, wind velocity is a highly stochastic component which can diverge very quickly. So, the control of the WECS at different places with different wind velocities is a very challenging task. Various control synthesis methods have been applied in response to the WECS control problems, such as PI control [4–9], LQG control [10,11], or fuzzy control [12,13]. Most of the researches [4–13], provided controllers are designed around an operating point and are valid only for a particular range of operation which are not covered the whole operating region. Most of the cases, wind velocities are chosen within variations ± 1 m/s or ± 2 m/s of the rated wind velocity, or below the rated wind velocity, and simulation results are provided within single range of wind velocities. Therefore, closed-loop stabilities are guaranteed only for the small-range of parameters deviation. Moreover, these control methods are not robust. During the high wind turbulence, PI controller is not ideal. The adaptive controllers such as fuzzy and LQG, the parameters adjustment of these controllers are computationally expensive [3]. Therefore, taking into account of the power producing capacity of the modern WECS (2–5 MW), the high turbulence wind velocities, and the parameter uncertainties, the researchers have prompted to interest in the robust control concepts (e.g., H_2 or H_∞ controllers). In particular, the robust H_∞ controller formulation for the WECS is adopted in [3,14–17], to improve the performance at the high turbulence wind velocities, or parameter uncertainties.

In [3,14,15], the H_∞ control systems design for the DFIGs. The control performance evaluates in a few parameters within the rated wind speed and some short variations of the rated wind speed. There aren't comparisons with other conventional methods. In [16,17], the H_∞ control system design for the

drive-train of the WECS and there are simulation analyses only for the wind speed and rotational speed of the generator. There aren't descriptions about the generated power and other WECS parameters. On the other hand, continuous signals based H_∞ controllers (*i.e.*, continuous H_∞ controllers) are designed in all the previous researches. Usually, a H_∞ control theory is very complex to design for a particular system. So, it is very complicated to implement a continuous H_∞ controller in the real-world systems. The digital H_∞ controller can be implemented for a system through the micro-controller. Also, a computer software can handle some complex parts of the controller. Nowadays micro-controller is inexpensive, under \$5 for many micro-controllers. It can easy to configure and reconfigure through a software. It is highly adaptable, parameters of the program can change with anytime. Digital computers are much less prone to environmental conditions than capacitors, inductors, *etc.* To consider these factors, it is very important to design a digital H_∞ controller based system. But there isn't research on the digital H_∞ controller based WECS.

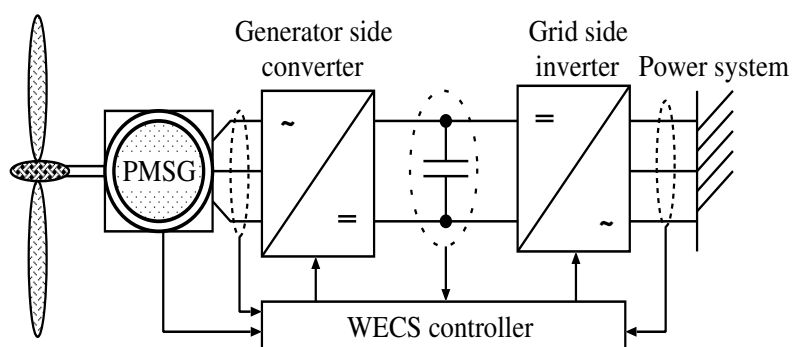
This paper presents a digital H_∞ controller based grid connected WECS. A sub-optimal H_∞ discrete-time loop shaping design procedure (DLSDP) is applied in this paper [18]. Described herein is a comprehensive and systematic way of implementing a new methodology of H_∞ control design algorithm for a 2 MW PMSG based WECS in a power system. The mechanical dynamics are controlled by PI based pitch angle control system while generator-side converter and grid-side inverter are regulated via the digital H_∞ controller. The proposed method is compared with the conventional PI controller method and the fuzzy controller method. Operational stabilities, reduced shaft stress, and improved voltage and power qualities are verified by the MATLAB/SIMULINK® environment with the *Linear Matrix Inequality (LMI)* technique.

2. Wind Energy Conversion System

2.1. Configuration of WECS

Figure 1 shows the interconnection of a PMSG based WECS. Wind energy acquired from the wind turbine is sent to the PMSG. To generate maximum power, rotational speed of the PMSG is controlled by a pulse width modulation (PWM) converter. The output power of the PMSG is supplied to the grid through a generator-side converter and a grid-side inverter.

Figure 1. Wind energy conversion system (WECS) configuration.



2.2. Dynamic Model of WECS

The maximum input power of the WECS can be expressed as

$$P_{wind} = \frac{1}{2} \rho \pi R_o^2 V_w^3 \quad (1)$$

where R_o is the wind turbine blade radius; V_w is the wind speed; and ρ is the air density. The wind turbine input torque T_{wind} can be described as

$$\begin{aligned} T_{wind} &= \frac{\lambda}{\omega_w} P_{wind} \\ &= \frac{1}{2} \rho \pi R_o^3 V_w^2 \end{aligned} \quad (2)$$

where ω_w is the rotational speed of the wind turbine; and λ is the tip speed ratio, can be defined as $\lambda = \frac{R_o \omega_w}{V_w}$.

The wind turbine output power P_w and the wind turbine output torque T_w (*i.e.*, input torque to the PMSG) are defined by the following equations:

$$P_w = \frac{1}{2} C_p(\lambda, \beta) \rho \pi R_o^2 V_w^3 \quad (3)$$

$$T_w = \frac{1}{2} C_p(\lambda, \beta) \rho \pi R_o^3 V_w^2 / \lambda \quad (4)$$

where C_p is the power coefficient; and β is the pitch angle. The power coefficient C_p is defined by the following equation:

$$C_p = 0.22 \left(\frac{116}{\Gamma} - 0.4\beta - 5 \right) \exp^{-\frac{12.5}{\Gamma}} \quad (5)$$

$$\Gamma = \frac{1}{\frac{1}{\lambda + 0.08\beta} - \frac{0.035}{\beta^3 + 1}} \quad (6)$$

From Equations (3) and (5), the WECS output power characteristics are represented in Figure 2, from which it can be seen that, for a particular wind speed, there is a rotational speed ω_{opt} , is known as optimum rotational speed, which generates the maximum power P_{max} . In this way, the maximum power point tracking (MPPT) control to each wind speed can increase the power generation for VSWTs. The value of ω_{opt} is calculated by the differentiating C_p with respect to the ω_w . Therefore, ω_{opt} is approximated as follows [4]:

$$\omega_{opt} = 0.1874 V_w \quad (7)$$

If $\omega_w = \omega_{opt}$, the maximum output power P_{max} of the wind turbine can be obtained. The MPPT control activates when the wind speed V_w is less than the rated wind speed ($V_{w,rated} = 12$ m/s), and above the rated wind speed, the output power of the PMSG is controlled by the pitch angle system. In this paper, the pitch angle is controlled in the region between the cut-in wind speed (5 m/s) and the cut-out wind speed (24 m/s). The pitch angle control system is shown in Figure 3. The pitch angle command β_{CMD} , is determined from the PI controller and the pitch angle selector. The pitch angle β , is constant at 2° when the power error of the PMSG ΔP_g , is zero. If ΔP_g is positive, β will increase to reduce the output power to maintain the rated power of the PMSG P_g , and vice versa. Above the cut-out wind

speed, β is set as 90° for the safety of the WECS. Actually, the pitch angle control system includes a hydraulic servo system that drives the wind turbine blades according to β_{CMD} . The β_{CMD} is limited through a limiter within $2^\circ \sim 90^\circ$ and the maximum rate of change is $\pm 10^\circ/s$.

Figure 2. WECS output power characteristics.

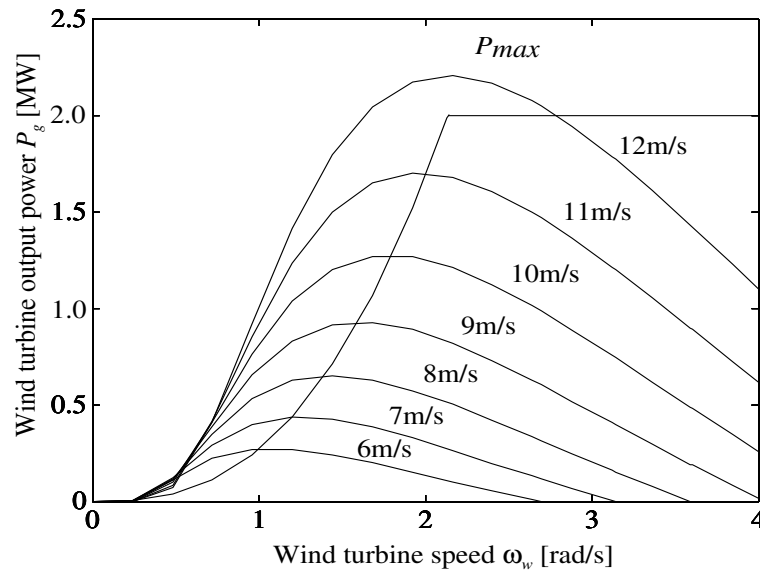
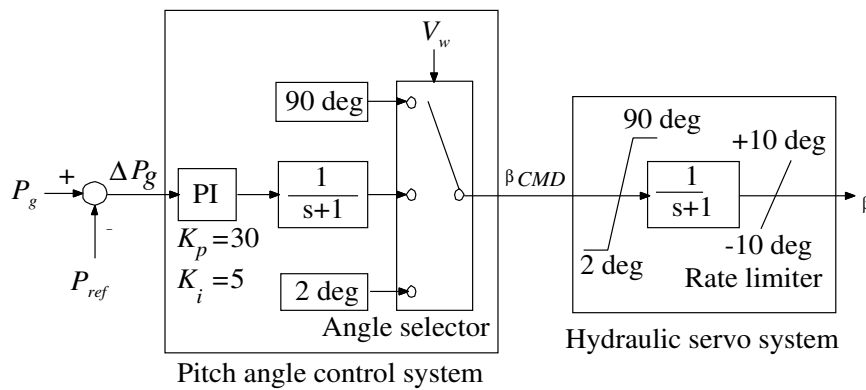


Figure 3. Pitch angle control system.



2.3. Mathematical Model of PMSG

Generally, the mathematical model of a PMSG is same as the permanent magnet synchronous motor (PMSM). The voltage and torque equations of the PMSM in the synchronous reference frame are given by the following equations:

$$v_d = R_a i_d + L_d \frac{di_d}{dt} - \omega_e L_q i_q \tag{8}$$

$$v_q = \omega_e L_d i_d + R_a i_q + L_q \frac{di_q}{dt} + \omega_e K \tag{9}$$

$$T_e = p \{ K i_q + (L_d - L_q) i_d i_q \} \tag{10}$$

where v_d and v_q are the dq -axis voltages; i_d and i_q are the dq -axis currents; R_a is the stator resistance; L_d and L_q are the dq -axis inductances; ω_e is the electrical rotational speed; K is the permanent magnetic

flux; and p is the number of pole pairs. Power generation starts when the electromagnetic torque T_e is negative. In addition, the motion equations of the PMSG and wind turbine are given by the following equations [19,20]:

$$T_e = J_{eq} \frac{d\omega_g}{dt} + D\omega_g + T_{lw} \tag{11}$$

$$T_w = J_w \frac{d\omega_w}{dt} + T_{lw} \tag{12}$$

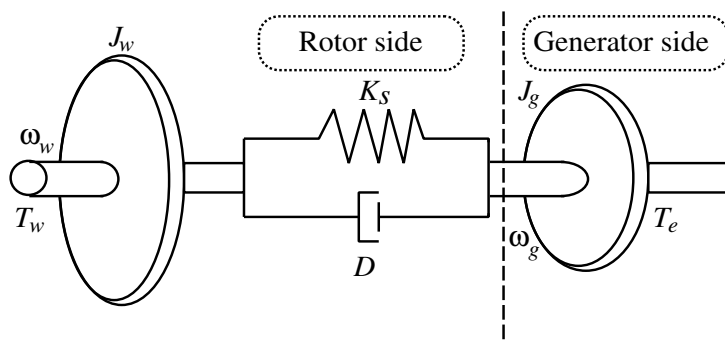
where D is the rotational damping; $J_{eq}(J_{eq} = J_g + J_w)$ is the equivalent inertia; T_{lw} is the load torque; and ω_g is the mechanical rotational speed.

Figure 4 demonstrates a schematic of the WECS mechanics, presented as a shaft coupling the two parts: turbine or rotor side and generator side. Since the PMSG is direct-driven, the gear box does not include here. The spring constant K_s and the corresponding damping coefficient D are related to the rotor side. The three-step model of drive train is shown in Figure 4 which is expressed in state-space format as follows:

$$\begin{bmatrix} \dot{\theta}_s \\ \dot{\omega}_w \\ \dot{\omega}_g \end{bmatrix} = \begin{bmatrix} 0 & 1 & -1 \\ -\frac{K_s}{J_w} & -\frac{D}{J_w} & \frac{D}{J_w} \\ \frac{K_s}{J_g} & \frac{D}{J_g} & -\frac{D}{J_g} \end{bmatrix} \begin{bmatrix} \theta_s \\ \omega_w \\ \omega_g \end{bmatrix} + \begin{bmatrix} 0 & 0 \\ \frac{T_w}{J_w} & 0 \\ 0 & -\frac{T_e}{J_g} \end{bmatrix} \tag{13}$$

where θ_s is the shaft angular twist and it is equivalence to the $\omega_w - \omega_g$.

Figure 4. Two-mass shaft model of WECS.



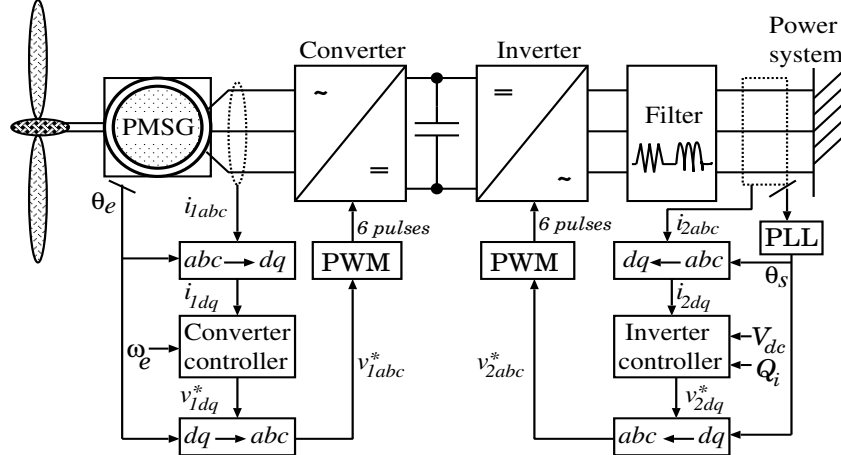
Variable-speed operation of the WECS is increased the fluctuation of output power and somewhat raises the shaft fatigue cycles. Drive train dynamics, system losses, and evading resonant frequencies can be integrated using proper control system implementation, by modifying the reference value for the aerodynamic torque near the resonant rotor speed. The proposed digital H_∞ control method aspires to the lower fluctuations in shaft torsional torque.

3. Power Converter Control System of WECS

The WECS adopts an AC-DC-AC power converter method with voltage source converters (VSCs). The PMSG is connected to the grid through two PWM VSCs: a generator-side converter and a grid-side inverter. The generator-side converter controls the generator torque of the PMSG, while the grid-side inverter controls the DC-link voltage and the grid voltage, respectively. The power converter control

system is shown in Figure 5. Each of the four quadrant power converters is a standard 3-phase two-level unit, composed of six insulated gate bipolar transistors (IGBTs) and controlled by the triangular-wave (10 kHz) PWM law. Each of the configurations of the control system is described below.

Figure 5. Power converter control system.



3.1. Conventional PI Control System

3.1.1. Generator-Side Converter

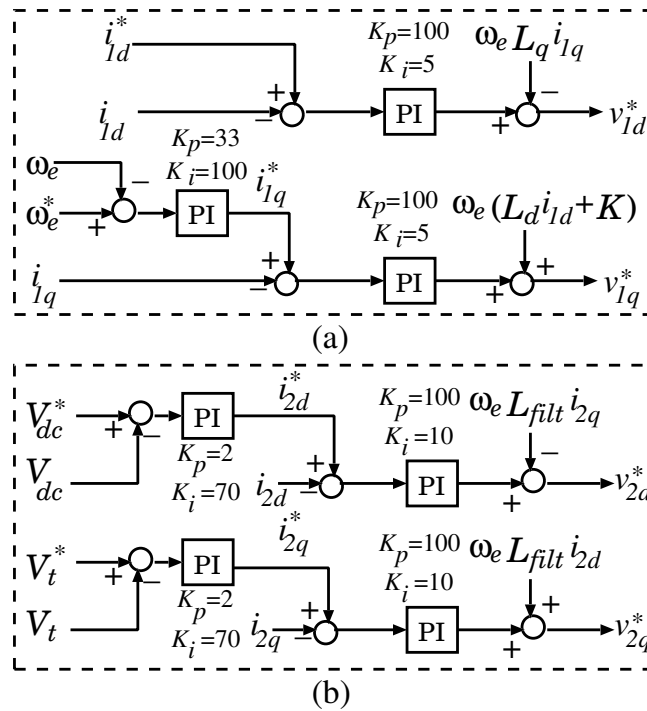
The generator-side converter controls the rotational speed of the PMSG. The vector control scheme is shown in Figure 6a,b. Output of the speed controller is generated the q -axis stator current command i_{1q}^* . The d -axis stator current i_{1d} , is set to zero. The current controller outputs generate the dq -axis voltage commands v_{1d}^* and v_{1q}^* after decoupling. In this figure, ω_e is the PMSG's electrical speed, L_d and L_q are the dq -axis inductances, and K is the permanent magnet flux.

3.1.2. Grid-Side Inverter

The grid-side inverter controls the DC-link voltage V_{dc} and the grid voltage V_t . The DC-link capacitor value is chosen to be 15,000 μF . The control system for the grid-side inverter is shown in Figure 6a. The d -axis current can control the DC-link voltage V_{dc} , and the q -axis current can control the grid voltage V_t . The V_{dc}^* and V_t^* are the DC-link voltage command and the grid voltage command, respectively. The controller outputs are dq -axis voltage commands v_{2d}^* and v_{2q}^* . The angle θ_s is detected by the phase-locked loop (PLL) for the Park transformation.

The PI controllers gains are shown in each figure. Usually PI controller tuning is a difficult problem due to the limitations of PI controller. The PI controller gains are adjusted by the manual methods for loop tuning.

Figure 6. (a) Generator-side converter control system; (b) Grid-side inverter control system.



3.2. Fuzzy Control System

Due to the non-linear behavior of the power system and the linearization problems, the control of the variable speed WECS is difficult by using the conventional PI controller methods. The fuzzy controller is a rule based non-linear control technique. The fuzzy controller presents some advantages as compared with the PI controller. It can obtain variable gains depending on the errors and overcomes the problems which are affected by an uncertain model. The detail analyses of the inverter and converter control systems for the WECS are given in previous section. The fuzzy controller based converter control system and inverter control system are shown in Figure 7a,b respectively. From these figures, the conventional PI controllers are replaced by the fuzzy controllers. Figure 8 shows the detail of the fuzzy based PI control system. It is a multi input–multi output (MIMO) based fuzzy control system. There are two inputs of fuzzy controller such as the system error, e and the change of error ce and two outputs of fuzzy controller that are the proportional gain K_p and the integral gain K_i . Depend on error and the change of error, the fuzzy controller delivers the proportional gain K_p and the integral gain K_i for the PI controller, and generates a reference signal. Figure 9a,b shows the fuzzy input membership functions (*i.e.*, error and change of error), and Figure 9c,d shows the output membership functions (*i.e.*, proportional gain K_p and integral gain K_i) of the fuzzy controller. The fuzzy controller rules are given in Table 1 in which the linguistic variables are represented by negative big (NB); negative medium (NM); negative small (NS); zero (ZO); positive big (PB); positive medium (PM); and Positive small (PS).

Figure 7. (a) Generator-side converter control system; (b) Grid-side inverter control system.

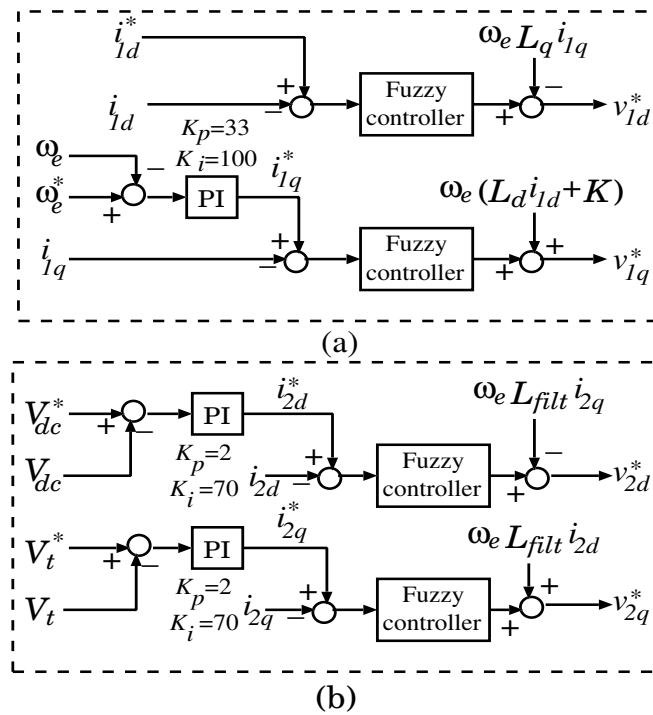


Figure 8. Fuzzy controller based PI control system.

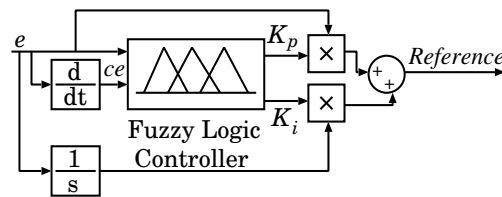


Figure 9. Fuzzy membership functions (a) input members; error e (b) input members; change of error ce (c) output members; proportional gain K_p (d) output members, integral gain K_i .

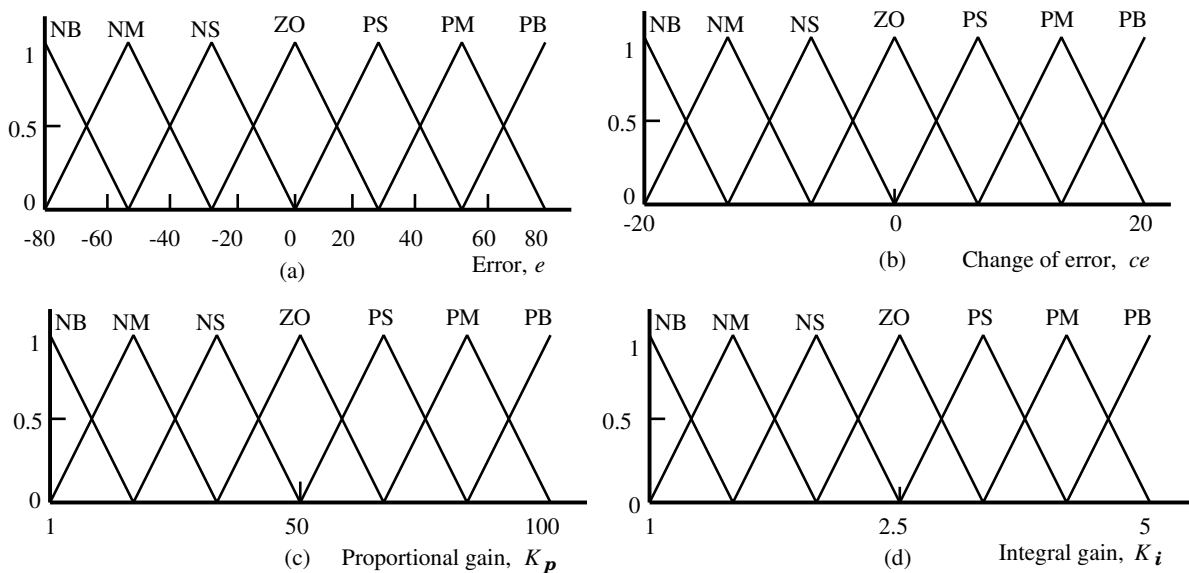


Table 1. Fuzzy membership functions.

K_p & K_i	e						
	NB	NM	NS	ZO	PS	PM	PB
	NB	NB	NB	NB	NM	NS	ZO
	NM	NB	NB	NM	NM	NS	ZO
	NS	NB	NM	NS	NM	ZO	PS
ce	ZO	NB	NM	NS	ZO	PS	PM
	PS	NM	NS	ZO	PS	PS	PM
	PM	NM	ZO	PS	PM	PM	PB
	PB	ZO	PS	PM	PB	PB	PB

The fuzzy rules and membership functions are determined by the trial-and-error process. Various methods have been proposed for tuning the fuzzy controller, such as self-tuning algorithm based on an experimental planning method, where the scaling factors of optimal parameters can be determined efficiently according to the desired performance indexes, Taguchi tuning method, and tuning the membership functions. However, in this paper, the selection of scaling factors is based on the trial-and-error method.

4. Digital H_∞ Control Scheme for Power Converters

The implementation of digital control systems and real-time systems belong together. In this section, the proposed digital H_∞ robust controller formulation and implementation are described.

4.1. Control Formulation

A generalized digital H_∞ robust control problem is shown in Figure 10a, and the feedback configuration is shown in Figure 10b. A stable and detectable n -order of state-space model for the continuous-time plant, P is described by

$$P : \begin{bmatrix} \dot{x} \\ z \\ y \end{bmatrix} = \begin{bmatrix} A & B_1 & B_2 \\ C_1 & D_{11} & D_{12} \\ C_2 & D_{21} & D_{22} \end{bmatrix} \begin{bmatrix} x \\ w \\ u \end{bmatrix} \tag{14}$$

$$P : \begin{cases} \dot{x} = Ax + B_1w + B_2u \\ z = C_1x + D_{11}w + D_{12}u \\ y = C_2x + D_{21}w + D_{22}u \end{cases} \tag{15}$$

where $x \in \mathbb{R}^n$ is the state vector; $w \in \mathbb{R}^{m_1}$ the exogenous input (external input and disturbance) vector; $u \in \mathbb{R}^{m_2}$ the control input vector; $z \in \mathbb{R}^{p_1}$ the error (output) vector; and $y \in \mathbb{R}^{p_2}$ the measurement vector, with $p_1 \geq m_2$ and $p_2 \leq m_1$. The $K[z]$ is a digital controller to be designed; “ s ” is the sampler with sampling period τ , i.e., y_d is the input of $K[z]$ where $y_d[k] := y(k\tau)$. In a real-time process, the average

processing time per sample is not greater than the sampling period τ . “ H ” denotes the generalized hold with hold function $H(t)$, i.e., u is determined as

$$u(t) = H(t)u_d[k]; (k\tau \leq t < (k + 1)\tau) \tag{16}$$

where u_d is the output of $K[z]$. The control goal is to minimize the induced norm of the input-output operator $\mathcal{T}_{zw}: w \Rightarrow z$. The digital H_∞ control problem is solved by searching a digital controller $K[z]$ and a generalized hold H which internally stabilizes the closed-loop in Figure 10, and the H_∞ norm from w to z is smaller than a specified positive number γ , i.e.,

$$\|\mathcal{T}_{zw}\|_\infty < \gamma \tag{17}$$

The sub-optimal and DLSDP H_∞ controller $K[z]$ can express as

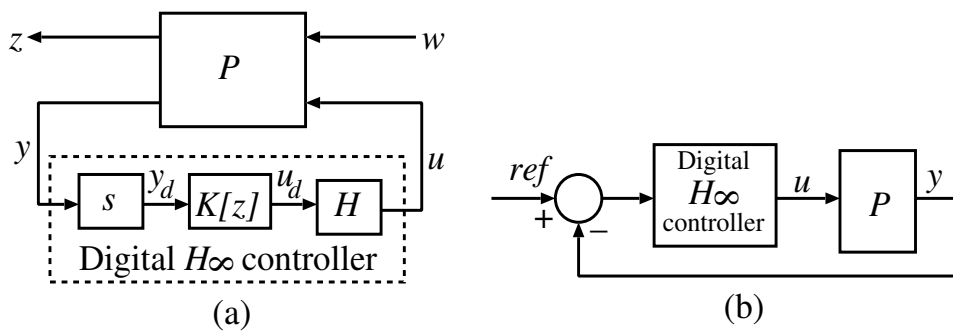
$$K[z] : \begin{bmatrix} x_K[k + 1] \\ u_d[k] \end{bmatrix} = \begin{bmatrix} A_K & B_K \\ C_K & D_K \end{bmatrix} \begin{bmatrix} x_K[k] \\ y_d[k] \end{bmatrix} \tag{18}$$

where

$$\begin{cases} A_K = \hat{A}_K - \hat{B}_K D (I + \hat{D}_K D)^{-1} \hat{C}_K \\ B_K = \hat{B}_K (I + D \hat{D}_K)^{-1} \\ C_K = (I + \hat{D}_K D)^{-1} \hat{C}_K \\ D_K = \hat{D}_K (I + D \hat{D}_K)^{-1}. \end{cases}$$

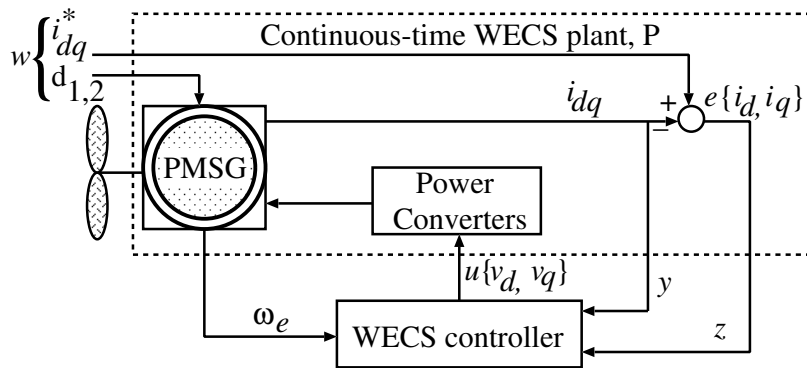
The estimated values \hat{A}_K , \hat{B}_K , \hat{C}_K , and \hat{D}_K can be obtained to solve the *discrete algebraic Riccati equations (DARE)* [19].

Figure 10. Digital H_∞ control problem (a) Generalized closed-loop configuration; (b) Feedback configuration.



The H_∞ control problem is adopted by the WECS which is shown in Figure 11. The signal w is represented the reference inputs and some disturbances. The controller output signal u is a control input in the plant. The output z is the control error, ideally it should be zero. The observed output signal y is available for the plant feedback. The detail electrical systems will discuss in the next sub-section.

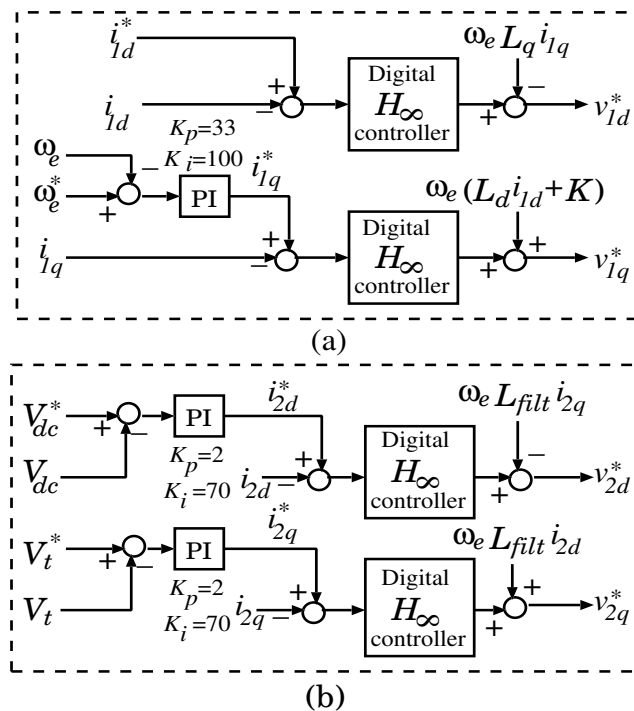
Figure 11. H_∞ control configuration for WECS.



4.2. Digital H_∞ Control Implementation

The generator-side converter and the grid-side inverter are controlled by the digital H_∞ controller which are shown in Figure 12. The configurations of each control system are described in below.

Figure 12. (a) Generator-side converter control method; (b) Grid-side inverter control method.



4.2.1. Generator-Side Converter

The proposed digital H_∞ robust controller converter control system is depicted in Figure 12a. To design a H_∞ controller, at first to develop a state-space expression for the generator-side converter. From the Equations (8) and (9), the following equations can be rewritten as:

$$\frac{d}{dt}i_{1d} = \frac{1}{L_d}\{-R_a i_{1d} + \omega_e L_q i_{1q} + v_{1d}\} \tag{19}$$

$$\frac{d}{dt}i_{1q} = \frac{1}{L_q}\{-R_a i_{1q} - \omega_e(L_d i_{1d} + K) + v_{1q}\} \tag{20}$$

From the Equations (19) and (20), the plant state-space expression in (15) can be derived by

$$\begin{aligned} \begin{bmatrix} \dot{i}_{1d} \\ \dot{i}_{1q} \end{bmatrix} &= \begin{bmatrix} -(R_a/L_d) & 0 \\ 0 & -(R_a/L_q) \end{bmatrix} \begin{bmatrix} i_{1d} \\ i_{1q} \end{bmatrix} \\ &+ \begin{bmatrix} 0 & 0 & (1/L_d) & 0 \\ 0 & 0 & 0 & -(1/L_q) \end{bmatrix} \begin{bmatrix} i_{1d}^* \\ i_{1q}^* \\ d_1 \\ d_2 \end{bmatrix} \\ &+ \begin{bmatrix} (1/L_d) & 0 \\ 0 & (1/L_q) \end{bmatrix} \begin{bmatrix} v_{1d} \\ v_{1q} \end{bmatrix} \end{aligned} \tag{21}$$

The tracking error z is given as:

$$\begin{aligned} z &= \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} i_{1d} \\ i_{1q} \end{bmatrix} + \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{1d}^* \\ i_{1q}^* \\ d_1 \\ d_2 \end{bmatrix} \\ &+ \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} v_{1d} \\ v_{1q} \end{bmatrix} \end{aligned} \tag{22}$$

The measured output y can be written as:

$$\begin{aligned} y &= \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} i_{1d} \\ i_{1q} \end{bmatrix} + \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{1d}^* \\ i_{1q}^* \\ d_1 \\ d_2 \end{bmatrix} \\ &+ \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} v_{1d} \\ v_{1q} \end{bmatrix} \end{aligned} \tag{23}$$

From the above Equations (21)–(23), state variables x , external inputs and disturbances w , and control inputs u are as:

$$x = \begin{bmatrix} i_{1d} \\ i_{1q} \end{bmatrix}, w = \begin{bmatrix} i_{1d}^* \\ i_{1q}^* \\ d_1 \\ d_2 \end{bmatrix}, u = \begin{bmatrix} v_{1d} \\ v_{1q} \end{bmatrix} \tag{24}$$

The decoupling components consider as the disturbances to enhance stabilities of the system, as follows

$$\begin{cases} d_1 = \omega_e L_q i_{1q} \\ d_2 = \omega_e (L_d i_{1d} + K) \end{cases}$$

The measured outputs are

$$y = [i_{1d} \ i_{1q}]^T \tag{25}$$

while tracking errors are

$$z = [e_{1id} \ e_{1iq}]^T \tag{26}$$

defined as $e_{1id} = i_{1d}^* - i_{1d}$ and $e_{1iq} = i_{1q}^* - i_{1q}$.

4.2.2. Grid-Side Inverter

Figure 12b shows the proposed digital H_∞ controllers based grid-side inverter control system. The controllers control the DC-bus voltage and the grid-voltage. To develop a state-space expression for the grid-side inverter, the following voltage equations with the RL -filter are considered [5].

$$\frac{di_{2d}}{dt} = \frac{1}{L_{filt}} \{v_{2d} - R_{filt} i_{2d} + \omega_e L_{filt} i_{2q}\} \tag{27}$$

$$\frac{di_{2q}}{dt} = \frac{1}{L_{filt}} \{v_{2q} - R_{filt} i_{2q} - \omega_e L_{filt} i_{2d}\} \tag{28}$$

where R_{filt} is the filter resistance and L_{filt} is the filter inductance. From the above Equations (27) and (28), state-space expression in Equation (15) for the grid-side inverter can be written as:

$$\begin{aligned} \begin{bmatrix} \dot{i}_{2d} \\ \dot{i}_{2q} \end{bmatrix} &= \begin{bmatrix} -(R_{filt}/L_{filt}) & 0 \\ 0 & -(R_{filt}/L_{filt}) \end{bmatrix} \begin{bmatrix} i_{2d} \\ i_{2q} \end{bmatrix} \\ &+ \begin{bmatrix} 0 & 0 & (1/L_{filt}) & 0 \\ 0 & 0 & 0 & -(1/L_{filt}) \end{bmatrix} \begin{bmatrix} i_{2d}^* \\ i_{2q}^* \\ d_3 \\ d_4 \end{bmatrix} \\ &+ \begin{bmatrix} (1/L_{filt}) & 0 \\ 0 & (1/L_{filt}) \end{bmatrix} \begin{bmatrix} v_{2d} \\ v_{2q} \end{bmatrix} \end{aligned} \tag{29}$$

The tracking error z can be defined as:

$$\begin{aligned} z &= \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} i_{2d} \\ i_{2q} \end{bmatrix} + \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{2d}^* \\ i_{2q}^* \\ d_3 \\ d_4 \end{bmatrix} \\ &+ \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} v_{2d} \\ v_{2q} \end{bmatrix} \end{aligned} \tag{30}$$

The measured output y is defined as:

$$y = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} i_{2d} \\ i_{2q} \end{bmatrix} + \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{2d}^* \\ i_{2q}^* \\ d_3 \\ d_4 \end{bmatrix} + \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} v_{2d} \\ v_{2q} \end{bmatrix} \tag{31}$$

From the above Equations (29)–(31), state variables x , the external inputs and disturbances w , and control inputs u are as:

$$x = \begin{bmatrix} i_{2d} \\ i_{2q} \end{bmatrix}, w = \begin{bmatrix} i_{2d}^* \\ i_{2q}^* \\ d_3 \\ d_4 \end{bmatrix}, u = \begin{bmatrix} v_{2d} \\ v_{2q} \end{bmatrix} \tag{32}$$

The measured outputs are

$$y = [i_{2d} \ i_{2q}]^T \tag{33}$$

The decoupling components are considered as disturbances

$$\begin{cases} d_3 = \omega_e L_{filt} i_{2q} \\ d_4 = \omega_e L_{filt} i_{2d} \end{cases}$$

while tracking errors are

$$z = [e_{2id} \ e_{2iq}]^T \tag{34}$$

can be defined as $e_{2id} = i_{2d}^* - i_{2id}$ and $e_{2iq} = i_{2iq}^* - i_{2iq}$.

The H_∞ controller $K[z]$ supplies the control signal u to the converters to ensure closed-loop stability of the WECS plant P by incorporating feedback. By utilizing a norm reduction method, the H_∞ control design problem searches the gain matrix $K[z]$ such that the H_∞ -norm conforms to Equation (16) for the closed-loop operator, from the external input variables and disturbances w to the output z . Hence, the H_∞ problem is to find the stabilizing controller $K[z]$ that minimizes Equation (16) and internally stabilizes the closed-loop system subject to the structural constraints dictated by the control law specifications [15].

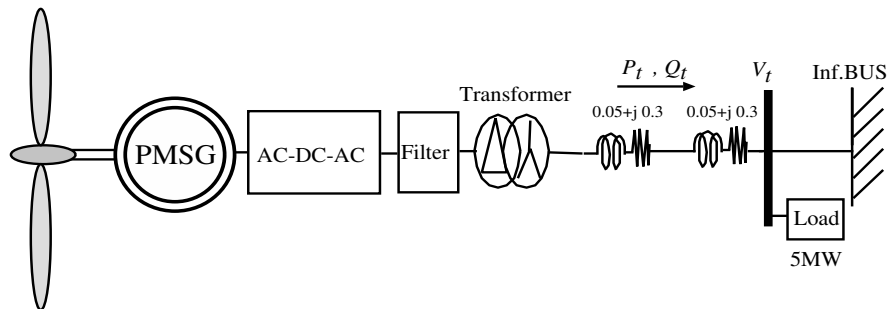
Numerical analyses of the above values of the proposed digital H_∞ controller are verified by the *Robust Control Toolbox* of the MATLAB®/SIMULINK.

5. Simulation Results

The overall power system for the numerical simulation is shown in Figure 13. In this figure, the grid-side inverter is connected to an infinite bus and a local load through a RL -filter, transformer and transmission line. The parameters of the wind turbine, PMSG and power converters are given in APPENDIX. To evaluate effectiveness of the proposed method, WECS operations are verified under two

different types of the wind velocities which are confirmed the robust stabilities. The simulation results are compared among the conventional method (*i.e.*, PI controller method), the fuzzy controller method, and the proposed method (*i.e.*, digital H_∞ controller method).

Figure 13. Power system model.



5.1. Low Turbulence Wind Velocity

Figure 14 shows the simulation results at the low turbulence wind speed. The wind speed is shown in Figure 14a. The rated wind speed is 12 m/s (dashed line) and wind speed is varied from 9 m/s to 15 m/s. The pitch angle (Figure 14b) activates with respect to the wind speed to control the rated power of the PMSG (2 MW). At simulation time (25–30 s), wind speed is high and the pitch angle is also high in this period. The output power of the PMSG is shown in Figure 14c. From this figure, the proposed method and the fuzzy controller method can generate more stable output power as compared with the conventional PI controller method. At simulation time (25–30 s), output power of the conventional method becomes unstable due to the high fluctuation of wind speed. In Figure 14d, the torque difference (*i.e.*, difference between input torque and output torque of the PMSG) is reduced by the proposed method as compared with the fuzzy controller method and conventional method. Therefore, the proposed method can reduce the shaft stress of the WECS. From Figure 14e,f, the high frequency components of the DC-link voltage and current are reduced by the proposed method. So, it can reduce the size and stress of the DC-link capacitor. The proposed method can inject an efficient output power to the power grid as compared with the conventional method and the fuzzy controller method which is confirmed in Figure 14g. But the fuzzy controller method can deliver an almost similar power as the proposed method and shows a good performance as compared with the conventional method. From this figure, power loss of the proposed method is lower than that of the conventional method because the proposed method can improve qualities of the torque difference, DC-link current and voltage.

Figure 14. Simulation Results (Low turbulence wind speed). (a) Wind speed; (b) Pitch angle; (c) Output power of PMSG; (d) Torque difference; (e) DC-link voltage; (f) DC-link current; (g) Output power of grid-side inverter.

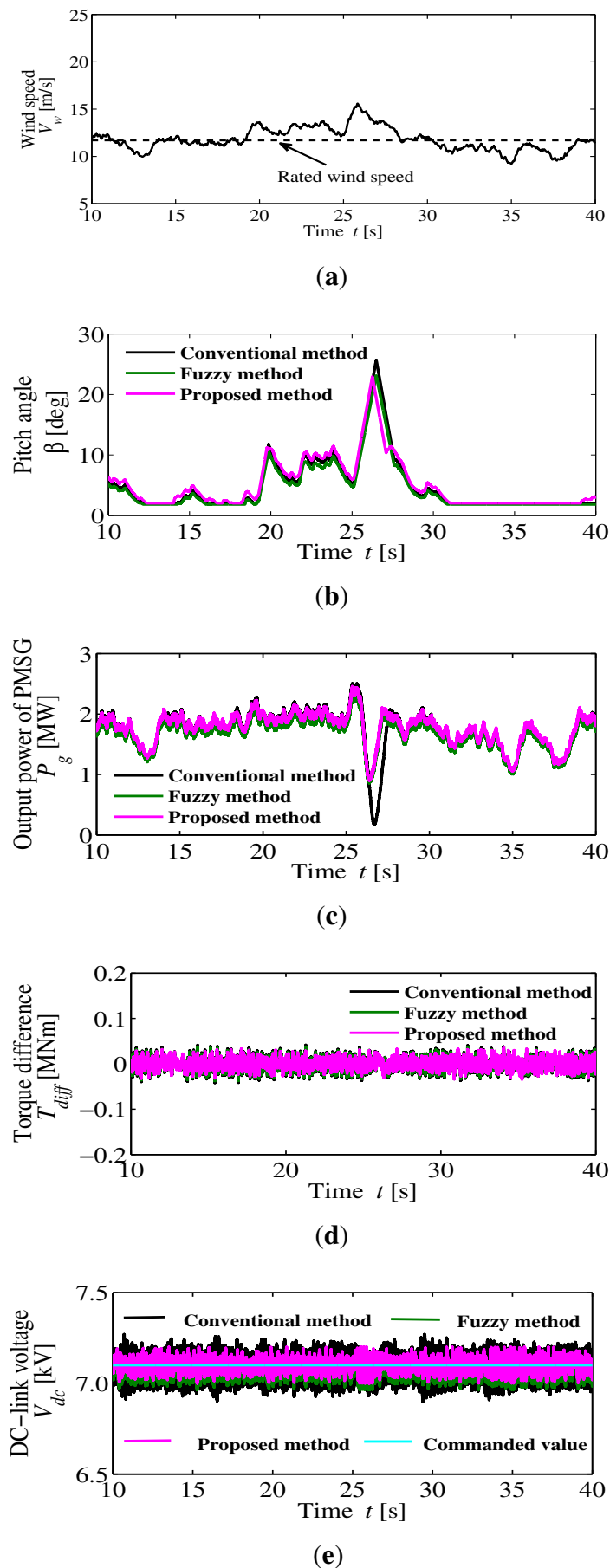
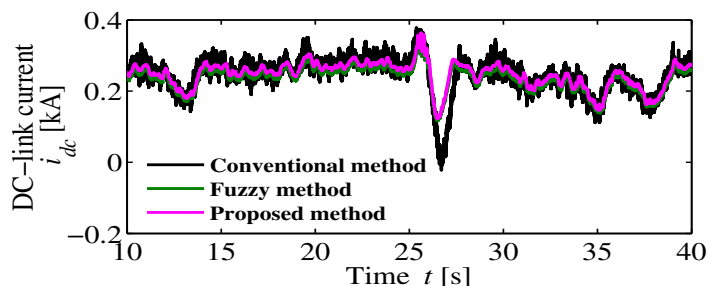
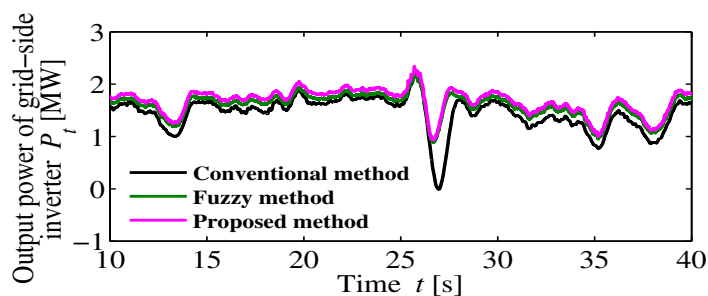


Figure 14. Cont.



(f)



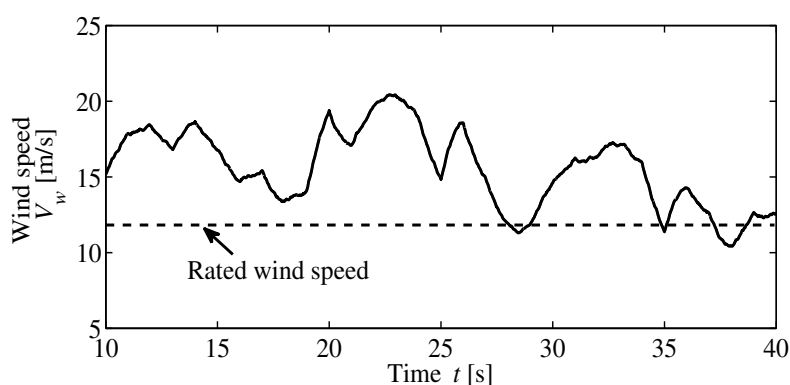
(g)

5.2. High Turbulence Wind Velocity

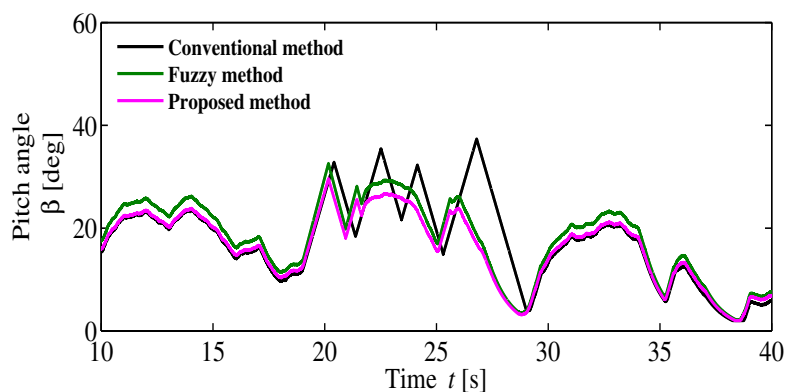
Figure 15 shows the simulation results for another pattern of the wind velocity. It considers as the high turbulence wind speed. The wind speed is received by the WECS which is shown in Figure 15a. It is higher than the rated wind speed. The pitch angle is shown in Figure 15b. Figure 15c,d reflects the final outcomes (*i.e.*, v_{1q}^* and v_{1d}^*) of three different methods. In Figure 15c, the q -axis commanded voltage is fluctuated widely by the conventional method and the fuzzy controller method (especially at simulation time 20–30 s) as compared with the proposed method. From Figure 15d, the d -axis commanded voltage is controlled precisely by the proposed method. Usually, the PI controller gains (proportional and integral) adjustment depend on the wind speed. For different set of wind speeds, the PI controller gains are different and required additional adjustments. If the PI controller gains regulate for the low turbulence wind velocities, these may not perfect for the high turbulence wind velocities or vice versa. On the other hand, the fuzzy controller method can show the similar behavior as the proposed in low turbulence wind speed (in Figure 14) but in high turbulence wind velocity the proposed method shows a superior performance as compared with the fuzzy controller method. The tuning of fuzzy controllers (gains and rules) is perfect in the low turbulence wind speed but in high turbulence wind speed, the fuzzy controller requires additional tuning to improve the performance. But in both cases, the fuzzy controller method can improve the performance as compared with the conventional PI controller method. In case of the proposed control method, it can apply at different wind speeds without additional adjustments. Figure 15e shows a comparison of the generated power of the PMSG. From this figure, generated power of the conventional method becomes unstable due to the high turbulence wind velocity. The proposed method can generate stable output power as compared with the conventional method. The fuzzy controller method can generate a stable power as compared with the conventional method but the

output power is more fluctuate than the proposed method. In Figure 15f, the torque difference of the PMSG can be reduced significantly by the proposed method as compared with the conventional method and the fuzzy controller method. The torque difference is much higher than the previous case as shown in Figure 14d. As a result, the proposed method can prevent the shaft stress and the damage of the WECS. High frequency components of the DC-link voltage and current are decreased extensively by the proposed method (Figure 15g,h). So, it can reduce size and stress of the DC-link capacitor. As a consequent, it can increase the life time of the capacitor. The output power of the grid-side inverter is depicted in Figure 15i. From this figure, the proposed method ensures the system power stability and delivers an efficient output power to the power grid. The proposed shows the better performance as compared with another two methods. The fuzzy controller method can generate more stable power as compared with the conventional PI controller method but worse than the proposed method.

Figure 15. Simulation Results (high turbulence wind speed). (a) Wind speed; (b) Pitch angle; (c) q -axis voltage command; (d) d -axis voltage command; (e) Output power of PMSG; (f) Torque difference; (g) DC-link voltage; (h) DC-link current; (i) Output power of grid-side inverter.

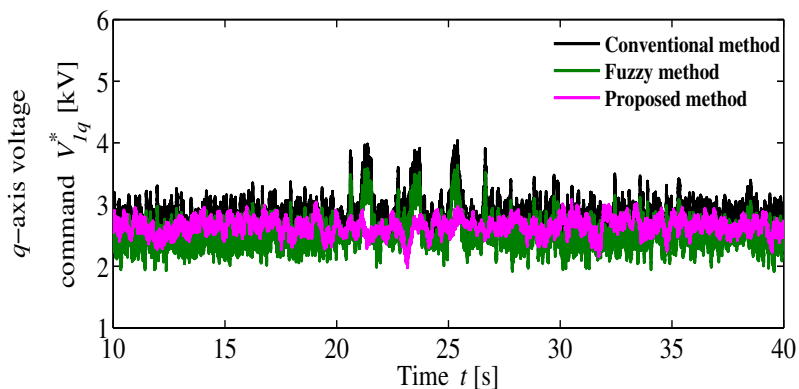


(a)

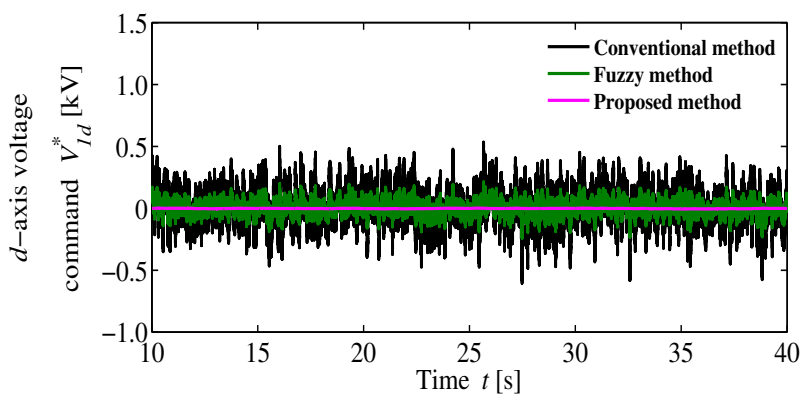


(b)

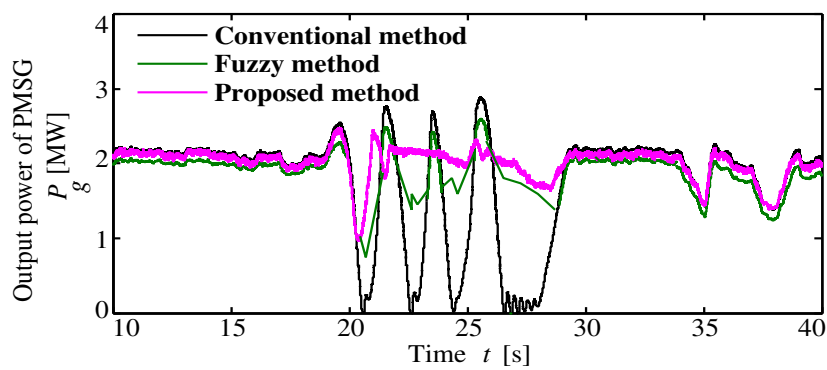
Figure 15. Cont.



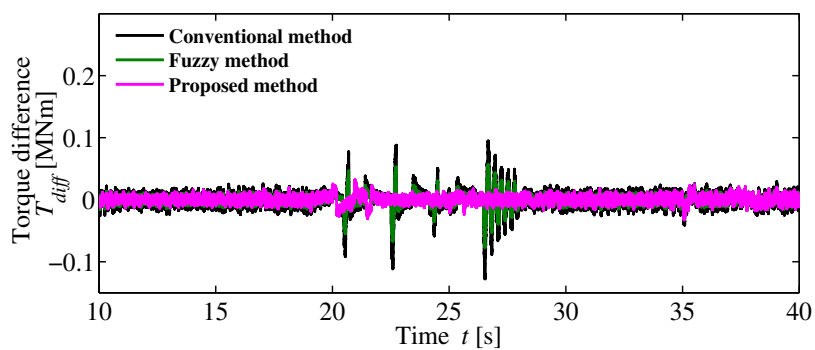
(c)



(d)

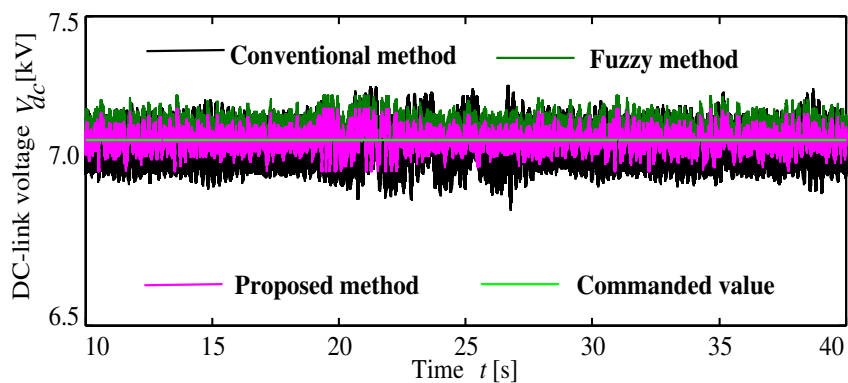


(e)

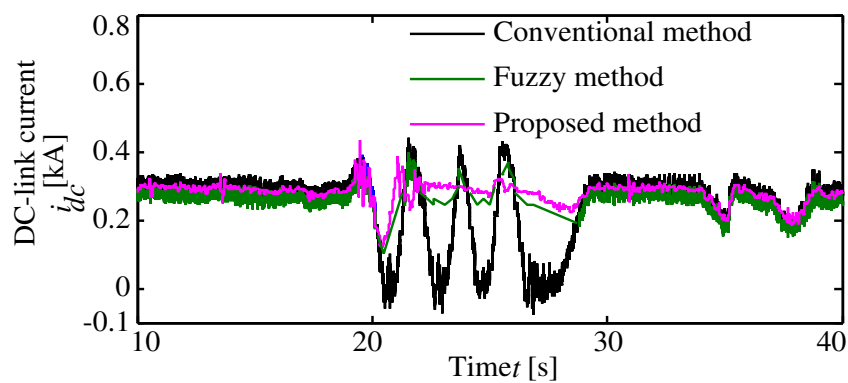


(f)

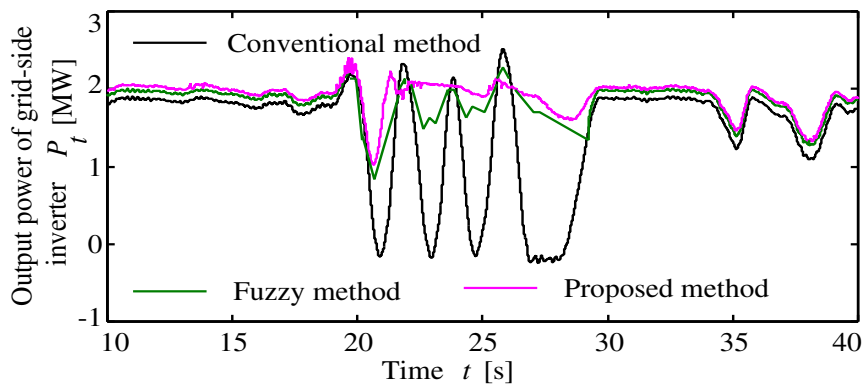
Figure 15. Cont.



(g)



(h)



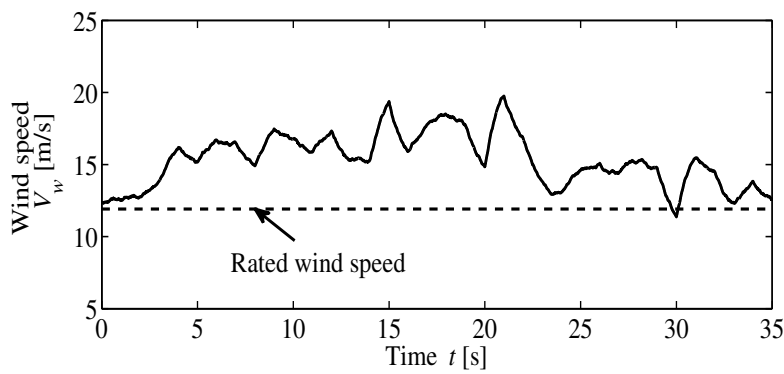
(i)

5.3. Robustness of the Proposed H_∞ Controller

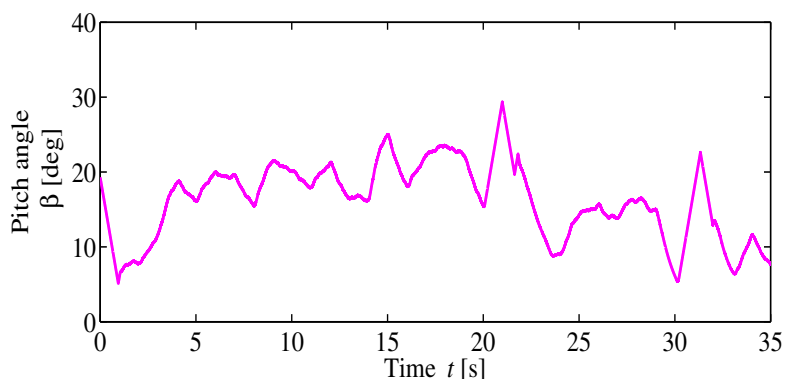
The external inputs (current references) and disturbances (decoupling components), w are may vary during the applications. To prove the robustness of the proposed H_∞ controller, these inputs are measured under 10% error of estimation. The simulation results are shown in Figure 16. Figure 16a shows the wind speed. It is also a high turbulence wind speed. The pitch angle of the WECS is shown in Figure 16b. The output power of the PMSG, DC-link voltage and DC-link current are shown in Figure 16c–e respectively. All simulation results show a good behavior. The output power of the grid-side inverter is shown in Figure 16f which also shows good behavior. On the other hand, simulation

results show from the time 0s which includes the transient region of the wind turbine generation system. From the simulation results, the controller performances at transient regions are perfect.

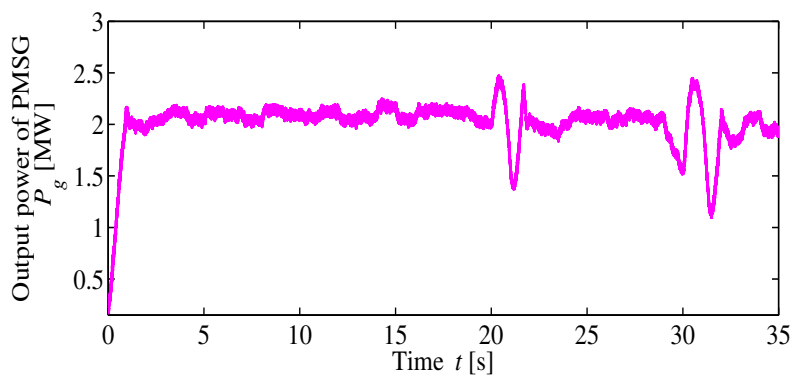
Figure 16. Simulation Results (Robustness of the proposed system). (a) Wind speed; (b) Pitch angle; (c) Output power of PMSG; (d) DC-link voltage; (e) DC-link current; (f) Output power of grid-side inverter.



(a)

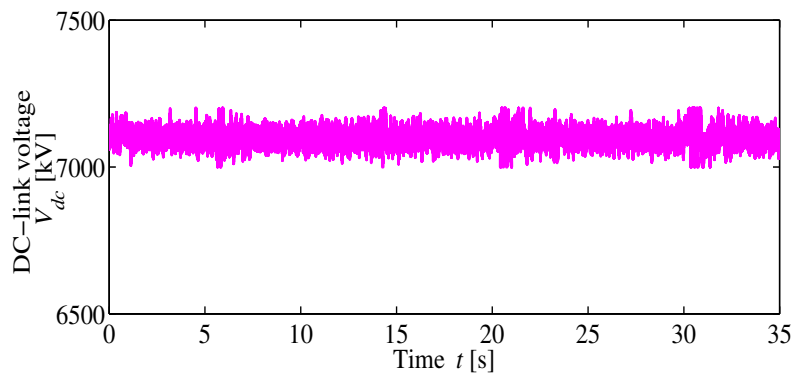


(b)

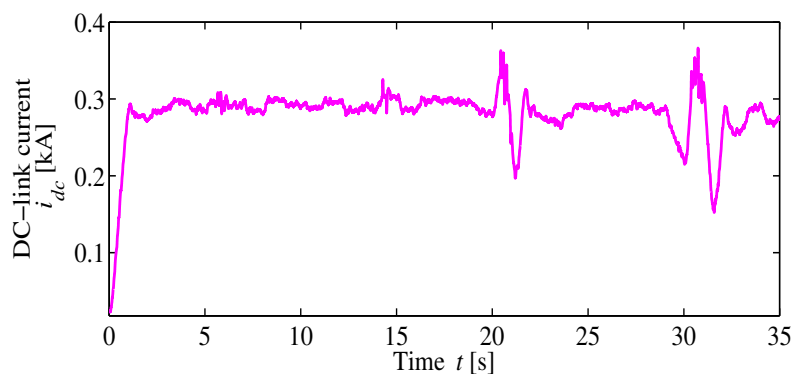


(c)

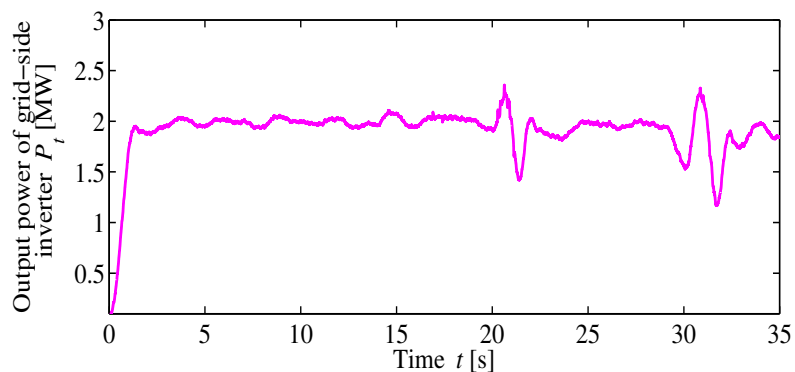
Figure 16. Cont.



(d)



(e)



(f)

From the above three different analyses, it is confirmed that when the wind speed becomes much higher than the rated speed, the conventional PI controller cannot control the large current and voltage accurately. The fuzzy controller requires additional adjustment for different levels of wind speeds. But the fuzzy controller method can improve performances as compared with the conventional PI controller method. The proposed digital H_∞ robust controller can control the WECS perfectly any types of wind speeds.

6. Conclusions

Due to the uncertainties of the wind speed and increasing the rated power of the WECS, it is complicated to control the all operating regions through a conventional PI controller. In this paper, a new type of robust control methodology has been presented. Most of the wind energy researches have been proposed within a low turbulence wind velocities. So, it does not ensure the robust stabilities of the WECS. This paper shows the two different wind speeds and parameters error to establish the robust control abilities of the proposed method. From the simulation results, the proposed method can reduce the shaft stress, and the high frequency components of the DC-link voltage and current significantly as compared with the conventional PI controller method and the fuzzy controller method. Moreover, it can ensure the system stabilities during the high turbulence wind velocities. So, the proposed method can apply to any environment (low or high turbulence wind speeds) with a large capacity WECS. Also, the proposed digital H_∞ controller can reduce the implementation complexities for a real system.

Appendix

Simulation parameters of the WECS utilized in the analysis are as follows [4]:

(a) **Wind turbine:** blade radius $R_o = 39$ m, inertia $J_{eq} = 10,000$ kg·m², air density $\rho = 1.205$ kg/m³, rated wind speed $V_{w,rated} = 12$ m/s, cut-in speed $V_{w,cut-in} = 5$ m/s, and cut-out speed $V_{w,cut-out} = 24$ m/s.

(b) **Parameters of generator:** rated power $P_{g,rated} = 2$ MW, number of poles pair $p = 11$, stator resistance $R_a = 50$ $\mu\Omega$, d -axis inductance $L_d = 0.0055$ H, q -axis inductance $L_q = 0.00375$ H, field flux $K = 135.25$ V·s/rad, rotational damping $D = 0$.

(c) **Parameters of power converter:** PWM carrier frequency $f_p = 10$ kHz, rated DC-link voltage $V_{dc,rated} = 7.1$ kV, DC-link capacitor $C = 15,000$ μ F.

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