

*Article*



# **The Development of Pneumatic Fatigue Test Rig for Wood-Based Specimens**

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**Abstract:** In product design, the focus is increasingly shifting towards optimizing and increasing the efficiency of the development process. This can be achieved with advanced numerical tools, but these methods require precise knowledge of material properties. One of the desired properties is the dynamic load behavior of the material. The research is directly related with the company that developed the slender wooden beams used in industry to produce windows of larger dimensions (height over 3 m). For the testing of wooden beams, the pneumatic four-point bending fatigue test rig was developed. In this paper, the whole structure of the test rig is described in detail. Based on the performed experiments of dynamic strength, the Woehler curve was determined, which serves as a necessary input for further numerical simulation of the fatigue process of wood-based beams. Knowledge of the response of wood to dynamic loads is very important to predict its life expectancy in various products.

**Keywords:** wood; fatigue; design; test rig; material properties; Woehler curve

## **1. Introduction**

When designing parts and structures, various physical models must be taken into account, which can lead to damage, failure or collapse of a part or an entire structure. The collapse of a part can be caused by a sudden overload (resulting in an impact fracture) or by a regular or continuous change of stress at lower levels under the influence of dynamic stress, which after a certain time leads to fatigue and, consequently, permanent fracture. Repeated loading causes permanent deformation, cracks and fractures even at stresses of lower levels, which would not lead to permanent deformation under static loads. Due to the occurrence of fatigue, the strength of the material under dynamic load is 20 to 60% lower than under static load [\[1\]](#page-15-0). The dynamic strength depends on the type of load and the number of load oscillations. It is determined experimentally by dynamic testing of specimens in special test rigs for fatigue tests. The test specimens are subjected to dynamic loads of a certain intensity until a crack or a fracture occurs. For a given series of test specimens, the mean stress is a constant σ*mean* = const., and the amplitude stress σ*<sup>A</sup>* is gradually reduced with each subsequent test specimen, recording the number of load cycles *N* at which each test specimen was permanently fractured. The test results are shown in σ–*N* (*S*–*N*) diagrams in the form of the number of load cycles *N* until the occurrence of a crack or a fracture in a curve of the dynamic strength of the material (*S*–*N* curve, Woehler curve) (Figure [1\)](#page-1-0). The constant value, to which the curve asymptotically approaches, represents the maximum nominal stress under a periodically changing load that the test piece can withstand for an unlimited number of oscillations without fracture; it is called the permanent dynamic strength of the material.

<span id="page-1-0"></span>

**Figure 1.** Dynamic strength curve for a given σ*mean*. **Figure 1.** Dynamic strength curve for a given σ*mean*.

In recent years, wood has become an increasingly interesting alternative to steel and concrete In recent years, wood has become an increasingly interesting alternative to steel and concrete due to increased environmental awareness and the general trend towards sustainable construction. due to increased environmental awareness and the general trend towards sustainable construction. The construction industry produces about 32% of all waste. In addition to this, more than 50% of non-renewable raw materials are used in the construction industry. All these indicators give wood certain chance and they also increase its applicability for construction purposes (wooden houses, a certain chance and they also increase its applicability for construction purposes (wooden houses, bridges, etc.). bridges, etc.).

Wood is a heterogeneous material with mechanical properties that vary greatly both within a Wood is a heterogeneous material with mechanical properties that vary greatly both within a tree and between trees. Products made from biological materials such as wood often have complex tree and between trees. Products made from biological materials such as wood often have complex mechanical behavior. Although such materials have been used for thousands of years, their mechanical behavior. Although such materials have been used for thousands of years, their mechanical behavior is not yet fully understood. They often vary in their properties from sample to sample and show non-linear mechanical behavior at higher loads. Moisture changes lead to shrinkage or swelling and changed mechanical properties. Wood also shows a dependence on the loading rate, such as creep and [vi](#page-15-1)scoelasticity [2]. However, recently wood has been re-discovered as a building material, which can also be subjected to cyclic (fatigue) loads.

One of the first studies related to the fatigue of wood was carried out b[y](#page-15-2) Wood [3], who One of the first studies related to the fatigue of wood was carried out by Wood [3], who presented the so-called "Madison curve" as the relationship between stress and duration of loading. In recent years, much research has be[en](#page-15-3) carried out to explain the fatigue phenomen[a o](#page-15-4)f wood [4–6]. The general conclusion of these studies is that the fatigue properties of wood are significantly influenced by the amount of water contained in the wood. In addition, the dynamic strength of wood by pulsating loading ( $R = 0$ ) is higher when compared to the completely reversed loading ( $R = -1$ ) at the same peak stress. The dynamic load factor R defines the type of load  $R = F_{min}/F_{max} = \sigma_{min}/\sigma_{max}$  (Figure [1\)](#page-1-0).

Wood is in fact a natural and anisotropic material with considerable variability in its mechanical properties. In timber construction, wooden parts are usually connected by dowels or screws, which represent stress concentrations due to holes, notches, etc. This notch effect has a negative influence on the fatigue behavior of wooden components, especially in the area of high cycle fatigue [7]. Liu and Ross [8] developed a mathematical model to predict the fatigue str[en](#page-15-6)gth of Douglas-fir beams under sinusoidal loading. They concluded that for a given mean stress the fatigue life decreases with an increase in amplitude stress. Furthermore, for a given stress amplitude, the fatigue life decreases with an increase in the mean stress. The authors also found that the fatigue life is almost independent of the load frequency. Yildirim et al. [9] investigated the fatigue behavior of Scots pine and beech wood using a three-point bending test at different stress levels (from 40 to 80% of the static breaking strength of the material). The authors concluded that the fatigue strength of beech is higher compared to Scots pine. Mejri et al. [10] have analyzed the influence of hygrothermal ageing on the fatigue behavior of wood fibre composites under bending stress. The authors concluded that the damage mechanisms are directly influenced by ageing. When analysing the fatigue behavior of wood components, some authors also considered fracture mechanics and fatigue crack growth theories. The proposed approaches refer Recently, researchers have analyzed various parameters influencing the fatigue behavior of wood.

to Mode-I [\[11](#page-15-9)[–13\]](#page-15-10), Mode-II [\[14](#page-15-11)[–16\]](#page-15-12) or Mixed-Mode-I+II [\[17\]](#page-15-13) fatigue crack growth. The fatigue process is thus present in wood and occurs in many structures, such as furniture [\[18\]](#page-15-14), roof structures, wind turbine blades [\[19\]](#page-15-15), bridges and windows, which are the subject of this research.

The share of wood-based windows (i.e., wooden and aluminium–wooden profiled windows) is the largest (66%) among certified windows for low-energy houses, due to their high energy efficiency and their beneficial life cycle assessment characteristics [\[20\]](#page-15-16). A contemporary architectural design of buildings integrates wooden products in the building envelope as well as in the interior. One of the reasons for this is that it was proven that the use of natural wood in buildings has a positive psychological, emotional and health impacts on the people living in such an environment [\[21\]](#page-15-17). Windows have an important role (solar gains through glazing), effecting the energy efficiency of the building. Consequently, there has been a gradual increase in the proportion of the transparent part of the building envelope, over the last decade. Windows are more and more frequently placed from the bottom to the top of individual storeys, with heights exceeding 3.0 m, or even over several storeys, with heights exceeding 5.0 m. Wooden windows with heights exceeding 3 m, with slim profiles, are desired and the wooden window industry is in search for innovative solutions on how to make such wooden profiles that would limit bending deflections (functionality—ealing of window), performed by cyclic wind loads. Over the last twenty years, many studies have been performed with regard to the flexural rigidity and load-bearing capacity of hybrid beams not only experimentally [\[22–](#page-15-18)[26\]](#page-16-0) but also analytically [\[25](#page-15-19)[,27](#page-16-1)[–31\]](#page-16-2) and numerically [\[32–](#page-16-3)[36\]](#page-16-4). In most of the mentioned studies, much larger cross sections than those used for windows were investigated (e.g., up to 500 mm in height) [\[29,](#page-16-5)[32\]](#page-16-3). Only a few researchers have studied the reinforcing effect on specimens with cross sections smaller than 100 mm  $\times$  100 mm [\[25,](#page-15-19)[31,](#page-16-2)[35\]](#page-16-6), where limited space for reinforcements is available, as in the case discussed in this article.

To improve the performance of window frames of greater heights, an optimized aluminum-reinforced slim wooden beam profile was already developed in coorporation with the selected company that produces wooden windows [\[25\]](#page-15-19). The paper presents the development of a pneumatic four-point bending fatigue test rig used to evaluate the dynamic behavior of such a developed hybrid wooden beam. The design of a fatigue test rig depends, to a large extent, on the test specimens being used. This includes the geometry, the material properties and the experimental procedure, which also defines the required force. All the selected components of the test rig are described in detail. Based on the performed experiments of dynamic strength, the Woehler curve was determined according to the principle proposed by Klemenc and Fajdiga [\[37,](#page-16-7)[38\]](#page-16-8). The scatter of Woehler curves is modelled with a conditional, two parameter Weibull density of probability distribution, in relation to which the shape parameter is determined with a neural network, whereas the scale parameter will follow functional dependency of the durability curve. Determined Woehler curve serves as a necessary input for further numerical simulation of the fatigue process of wood-based beams.

Knowledge of the response of wood to dynamic loads (experimental and numerical) is very important today and will become increasingly important for future applications and the use of wood to predict its life expectancy in various products.

#### **2. Materials and Methods**

Basic guidelines for the design of the test rig construction are the requirements of the selected company producing wooden windows (M SORA d.d., Žiri, Slovenia) for the length of the test beam (1950 mm) and the maximum dynamic load  $P = 35$  kN (dynamic load factor  $R = 0$ ). The selected dimensions and loads are the result of numerical simulations already carried out to optimize the aluminum-reinforced wooden beam profile and the static bending tests (Figure [2b](#page-3-0)) carried out on the optimized beam [\[25](#page-15-19)[,26](#page-16-0)[,36](#page-16-4)[,39\]](#page-16-9). All test specimens were manufactured using the following materials: wood species—Norway spruce, aluminum reinforcements—AW 6060-T66 and two-component polyurethane adhesive—COSMO PU 200.280 (Figure [2a](#page-3-0)). The cross-section of the aluminum-reinforced wooden beam is shown in Figure [2a](#page-3-0).

<span id="page-3-0"></span>

**Figure 2. (a)** Cross section of a specimen with aluminium reinforcement, **(b)** the test equipment for performing the 4-point bending tests [\[25\]](#page-15-19).

The four-point bending tests up to failure were performed using a universal servo-hydraulic The four-point bending tests up to failure were performed using a universal servo-hydraulic testing machine Roell Amsler HA 100 (Zwick GmbH & Co. KG, Ulm, Germany) [\[25\]](#page-15-19), Figure [2b](#page-3-0). The bending load tests were carried out in displacement (i.e., stroke) control mode with an actuator movement speed of 0.1 mm/s until failure. On each specimen, deflections were measured at two points with linear voltage displacement transducers (LVDTs). All physical properties (i.e., displacements,  $\alpha$  and load  $\overline{B}$ ) were measured and recorded with a Dewesoft DEWE 2500 data acqui strains and load P) were measured and recorded with a Dewesoft DEWE 2500 data acquisition system [\[25\]](#page-15-19). performing the 4-point bending tests [25].  $\epsilon$  and load P) were measured and recorded with a Dewesoft DEU  $\epsilon$ acquisition system [25].

# <span id="page-3-2"></span>*2.1. Construction of Test Rig 2.1. Construction of Test Rig 2.1. Construction of Test Rig*

<span id="page-3-1"></span>The basic guideline for the selection and design of the test rig construction was a large and fast The basic guideline for the selection and design of the test rig construction was a large and fast flexibility depending on the shape and size of the test specimen. A composite drawing of the test rig structure is shown in Figure [3.](#page-3-1) structure is shown in Figure 3. flexibility depending on the shape and size of the test specimen. A composite drawing of the test



**Figure 3.** Components of the test rig: 1. Frame, 2. Frame connecting plate, 3. Support, 4. Specimen, 5. Load cell, 6. Pressure element, 7. Pressure element guide, 8. Pneumatic cylinder, 9. Displacement sensor.

The structure consists of extruded aluminum profiles (Figure 4a). The grooves on [th](#page-4-0)e profile allow easy mounting of the components and adjustment to the length of the workpiece. The dimensions of the profile have been chosen according to the permissible beam deformation at the maximum static breaking loads of the reinforced beams obtained from the industrial partner. With the help of the Finite Element Method (FEM), the stress-strain analyses are carried out at critical boundary conditions, i.e., at a cylinder load of 35 kN. The final dimension of the profile is further increased by the test type, as fatigue tests are carried out—which also influences the fatigue of the test rig frame.

<span id="page-4-0"></span>

**Figure 4.** (**a**) Alu profile; (**b**) press element. **Figure 4.** (**a**) Alu profile; (**b**) press element.

The press element consists of two UPN 140 profiles (Figure [4b](#page-4-0)). They are bolted to flat steel plates The press element consists of two UPN 140 profiles (Figure 4b). They are bolted to flat steel plates of  $200 \times 15$  mm. The bolted construction enables the replacement and reworking of components from the assembly and operation of the device; it also enables the replacement of parts due to possible the assembly and operation of the device; it also enables the replacement of parts due to possible damage. The two FTKL 2000 load cells are bolted on the top side. The pneumatic cylinder is screwed damage. The two FTKL 2000 load cells are bolted on the top side. The pneumatic cylinder is screwed on th[e](#page-3-1) bottom side via the interface (Figure 3). Due to the possibility of an asymmetrical breakage and the resulting overload of the load cell and the pneumatic cylinder, the pressure element is connected to the ball linear guideway Hiwin HGW 2[5 H](#page-3-1)A (Figure 3).

# *2.2. Test Rig Actuator System 2.2. Test Rig Actuator System*

It is known from Section 2.1 that the required force is 35 kN, which summarizes the actuator It is known from Section [2.1](#page-3-2) that the required force is 35 kN, which summarizes the actuator selection options. To perform the cyclically pulsating load  $(R = 0)$ , a pneumatic system was used consisting of a compressed air preparation unit, a control unit, a digital air regulator, two valves and consisting of a compressed air preparation unit, a control unit, a digital air regulator, two valves and a cylinder (Figur[e](#page-5-0) 5). In addition to the above elements, there are also switches for pressure overload and air cut-off, as well as a regulator for the supporting pressure required to operate the valves (Figure [5\)](#page-5-0). The entire pneumatic system is designed for working pressures of up to 10 bar.

A two-way pneumatic cylinder with a piston diameter of 250 mm and a stroke of 200 mm was A two-way pneumatic cylinder with a piston diameter of 250 mm and a stroke of 200 mm was used to load the specimens (Figures [3 a](#page-3-1)nd [5\).](#page-5-0) The cylinder can be operated with air in both directions used to load the specimens (Figures 3 and 5). The cylinder can be operated with air in both directions and has built-in pneumatic damping in both end positions of the piston. Inside the piston, there is a and has built-in pneumatic damping in both end positions of the piston. Inside the piston, there is a built-in magnet, through which the movement of the piston can be read with a special position sensor. built-in magnet, through which the movement of the piston can be read with a special position sensor. The cylinder has a declared wide operating pressure range of 1.5 to 10 bar, although in combination The cylinder has a declared wide operating pressure range of 1.5 to 10 bar, although in combination with built-in valves it has been proven to operate at pressures down to 0.5 bar. The speed of the cylinder is declared to be 30 to 5000 mm/s, but this value depends on the air mass flow at a given pressure and the corresponding dimensioning of the supply system. Initially, the cylinder operates in the lower speed range (slow movements). Theoretically, the cylinder is capable of generating a thrust force *F* in the range between 2454 N and 34,361 N, which is directly dependent on the pressure (0.5 to  $\overline{F}$ ) 7 bar) and the piston area (diameter 250 mm). In the opposite case, the traction mode, in which the piston area (diameter 250 mm). In the opposite case, the traction mode, in which the piston returns to the starting point, taking into account the reduction in the piston area by the mounted point piston rod (diameter 50 mm), the traction force is reduced "only" by 4% compared to the thrust force.<br>The thrust conduction is a state of the traction of the traction of the tractional terms of the traction of th To determine the pressure at which the cylinder must be actuated to achieve the target force at which<br>the determine the pressure at which the cylinder must be actuated to achieve the target force at which the loads are applied, the characteristics of this dependence must be measured. For this purpose, the characteristics of this dependence must be measured. For this purpose, the thrust force of the cylinder on the load cell at the set pressure has been measured, thus determining the pressure–force relationship. pressure and the corresponding dimensioning of the supply system. Initially, the cylinder operates in the lower speed range (slow movements). Theoretically, the cylinder is capable of generating a thus.

<span id="page-5-0"></span>

**Figure 5.** Fatigue test rig components: 1. Cut-off switch, 2. Air preparation unit, 3. Regulator for the **Figure 5.** Fatigue test rig components: 1. Cut-off switch, 2. Air preparation unit, 3. Regulator for the support pressure, 4. Digital air regulator, 5. Pressure overload switch, 6. Two valves, 7. Measuring support pressure, 4. Digital air regulator, 5. Pressure overload switch, 6. Two valves, 7. Measuring interface, 8. Load cell amplifier, 9. Programmable logic controller (PLC), 10. Switches (Start-Stop), Power supply, 12. Main power switch (emergency Stop). 11. Power supply, 12. Main power switch (emergency Stop).

Before air is introduced into the pneumatic system, it must be properly filtered and regulated. Before air is introduced into the pneumatic system, it must be properly filtered and regulated. The air for such a system must not contain lubricants, since all pneumatic elements are already The air for such a system must not contain lubricants, since all pneumatic elements are already supplied with the applied lubricants and the additional use of these lubricants could contribute to supplied with the applied lubricants and the additional use of these lubricants could contribute to the acceleration of the wear process or to the improper operation of the elements. Excess moisture the acceleration of the wear process or to the improper operation of the elements. Excess moisture that accumulates in the compressed air supply system must be removed as it causes corrosion of the that accumulates in the compressed air supply system must be removed as it causes corrosion of the pneumatic elements. It is therefore recommended to add a condensation and solid particle collection pneumatic elements. It is therefore recommended to add a condensation and solid particle collection unit for each pneumatic system. Such an element is normally located on the combined unit with the unit for each pneumatic system. Such an element is normally located on the combined unit with the intake air regulator (Figure [6](#page-6-0)). intake air regulator (Figure 6).

The pressure in the entire pneumatic system is adjusted with the main regulator. The actual air supply to which the test unit is connected can produce a maximum pressure of 7 bar. An additional regulator is included in the part of the preparation group that only serves to provide the supporting pressure for the valve control (Figure [6\)](#page-6-0). There is also a manual shut-off valve at the inlet before the regulators, which allows the entire system to be disconnected from the air supply and is used for shutdowns or non-operational and maintenance work on the test rig (Figure [6\)](#page-6-0).

<span id="page-6-0"></span>

Figure 6. Preparatory group: 1. Cut-off switch, 2. Main regulator, 3. Additional regulator. shut downtowns group. The car on switch, 2. main regulator, 8. maintena

In order to precisely determine the air pressure and to maintain its value independent of fluctuations in the supply system (taking into account that the supply pressure must not be below the set point), the device is additionally equipped with a Regtronic 300 digital pressure regulator, which precisely monitors the pressure and readjusts it if necessary (Figure 7a). The regulator has a screen on the front panel, which displays the actual pressure, as well as buttons for setting the desired pressure and other pressure control parameters. It is also equipped with an analog input and output, digital communication RS 232 and an alarm output. In order to precisely determine the air pressure and to maintain its value independent of<br>fluctuations in the supply system (taking into account that the supply pressure must not be below the<br>set point), the device is addi the front panel, which displays the actual pressure, as well as buttons for setting the desired pressure

<span id="page-6-1"></span>

**Figure 7.** (**a**) Digital pressure regulator; (**b**) two monostable valves. **Figure 7.** (**a**) Digital pressure regulator; (**b**) two monostable valves.

electromagnet is interrupted, the directional control valve returns to its original state due to the built-in  $\frac{1}{1}$  electronically between two pneumatic channels. The system uses two valves, each of which controls the two valves was performed to achieve a cyclic operation of the cylinder suitable for a fatigue test rig. Built-in pneumatic valves require a back-up pressure to perform valve switching at very low pressures  $\frac{1}{1}$  (practically 0 bar and above). The minimum required value of back-up pressure value for these valves is 2.5 bar.  $\frac{1}{\sqrt{2}}$  bar. or activated state, which is achieved by switching on the electromagnet which presses inside the directional control valve, thus switching between the pneumatic channels. If the power supply to the spring, which acts in the opposite direction than the electromagnet. In this way it is possible to switch the movement of the cylinder in one direction only (Figure [7b](#page-6-1)). Therefore, periodic switching between The built-in electropneumatic 3/2 valves are monostable, i.e., they have only one "energised" is 2.5 bar.

# switch electronically between two pneumatic channels. The system uses two valves, each of which *2.3. Control System of the Test Rig*

The control system of the fatigue test rig ensures the cyclic loading of the test specimen with the possibility to change the test dynamics; it counts the number of loads and stops the test in case of fatigue test rig. Built-in pneumatic values require a back-up pressure to perform values  $\mathbf{r}$ 



<span id="page-7-0"></span>failure of the test specimen (inductive switch). For this purpose, a programmable logic controller (PLC) can be used. The block diagram of the control system of the fatigue test rig is shown in Figure [8.](#page-7-0) 8. 8.



A Start button (upper button) is used to start the experiment and a Stop button (lower button) to stop the experiment (Figure [9\)](#page-7-1). Pressing both buttons simultaneously clears the PLC counter and is used before starting a new experiment. The inductive switch serves as a safety switch and is only triggered when the cylinder piston exceeds a certain stroke (approximately 150 mm). This is set manually by moving the sensor attached to the guides, which the cylinder piston only reaches when the test specimen collapses. Two cylinder control valves are connected to the relay output of the controller. A Mitsubishi Programmable PLC Logic Controller with the designation AL2-14MR-D was used to control the pneumatic system (Figure 9). used to control the pneumatic system (Figure [9\)](#page-7-1). used to control the pneumatic system (Figure 9).

<span id="page-7-1"></span>

**Figure 9.** Mitsubishi Alpha2 PLC. **Figure 9.** Mitsubishi Alpha2 PLC. **Figure 9.** Mitsubishi Alpha2 PLC.

This controller has eight digital inputs and six relay outputs. The controller has an LCD screen (Figure [9\)](#page-7-1) on the front panel where you can display various parameters and data. The PLC has been programmed so that the loading and unloading time can be adjusted with the buttons next to the screen (Figure [9\)](#page-7-1). The main programming of the PLC is done by the PC program Alpha Programming (Figure [10\)](#page-8-0).

<span id="page-8-0"></span>

**Figure 10.** PLC program for cyclic control of a pneumatic cylinder. **Figure 10.** PLC program for cyclic control of a pneumatic cylinder.

The controller has been programmed so that when all operating conditions are met, the system switches between the valves according to a predetermined dynamic. The dynamic is defined by the test piece were test piece were were were the values of the test piece were defined by the test piece were defined by the test "flicker" function, where both the duration of the on and off time can be set. These values are general but can also be set individually if required. During the test, the recording of the load cycles was carried out with a counter. In certain test cases, the number of load cycles can be much higher than the upper limit of the counter ( $2^{15} = 32,768$ ). A solution was therefore found by using two counters, with the limit of the first counter set at 10,000 units and an additional counter that only counts tens of thousands. This means that the system can currently run up to a good 327 million cycles before stopping, as long as it does not meet any of the test stop conditions. The controller screen displays information about the duration of each experiment, the number of cycles completed and the valve opening times. Due to the dimensioning of the system, the fatigue frequency for the current setup is limited to a maximum of 0.063 Hz and corresponds to a 16 s cycle interval—an eight second load period is followed by an eight-second relaxation period.

#### *2.4. Testing Rig Measuring System*

During the test the number of load cycles, the load force and the bending of the test piece were measured. Figure [11](#page-9-0) shows a block diagram of an existing measurement system.

For recording the measured values of the sensors, the measuring interface of the company, National Instruments, with the marking NI USB 6009 (Figure [11\)](#page-9-0) was used, and in the software package, LabView, a special software interface (Figure [12\)](#page-9-1) was developed, which allows one to display and record the measurements in the desired binary file (TDMS) and to stop the measurements if the test specimen collapses. Due to the complexity and the large amount of data, the analysis of the measurement results is performed separately.

<span id="page-9-0"></span>

Figure 11. Block diagram of the measuring system of the testing rig.

<span id="page-9-1"></span>

**Figure 12.** Software interface. **Figure 12.** Software interface.

## 2.4.1. Measurement of Input Force

2.4.1. Measurement of Input Force<br>The fatigue test on a specimen works based on the principle of four-point bending, whereby force is applied to the specimen by a compression element via two rollers with a diameter of 30 mm at a is applied to the specimen by a compression element via two rollers with a diameter of 30 mm at a<br>distance of 600 mm from each other (Figure 13). The specimen is supported at the ends by two fixed cylindrical elements with identical dimensions at a distance of 1850 mm.

<span id="page-9-2"></span>

**Figure 13.** Four-point bending test and its main components. **Figure 13.** Four-point bending test and its main components.

To facilitate design and operation, the system is arranged upside down, i.e., the pressure element presses upwards on the test specimen and the side supports are at the top (Figure 13). Such an arrangement does not make operation significantly more difficult, but one must be aware that the pressure force is not equal to the product of the pressure in the cylinder and piston area, as friction losses due to the use of guides, and of course the weight of the pressure element itself, must be taken into account. Therefore, in such a system, it makes sense to measure the force directly below the pressure rollers (Figures 13 and [14\)](#page-10-0). For this purpose, two measuring cells (type FTKL) with a maximum individual load capacity of 2000 kg and shear operation (Figure 14) are used.

<span id="page-10-0"></span>

Figure 14. (a) Pressure element with load cells; (b) the side profile of the load cell during fatigue of a wood specimen. wood specimen.

<span id="page-10-1"></span>The load cells were connected to a measurement amplifier BA 662/660 (A.S.T.—Angewandte The load cells were connected to a measurement amplifier BA 662/660 (A.S.T.—Angewandte System Technik GmbH, Dresden, Germany), which ensures sufficient amplification and filtering of System Technik GmbH, Dresden, Germany), which ensures sufficient amplification and filtering of the load cell measurement signal (Fi[gure](#page-10-1) 15).



**Figure 15.** AST signal amplifier for load cells. **Figure 15.** AST signal amplifier for load cells.

The calibration of the built-in load cells was performed by placing known masses of weights on The calibration of the built-in load cells was performed by placing known masses of weights on the load cells and reading the values of the output voltages from the amplifier. Due to the limited set the load cells and reading the values of the output voltages from the amplifier. Due to the limited set of weights  $(2 \times 1 \text{ kg}, 2 \times 2 \text{ kg}$  and  $2 \times 10 \text{ kg}$ ) the measurements were only carried out in the lower force range. For load cell 1 connected to amplifier 660, the dependence between the voltage *U* in millivolts and the force *F* in Newton (Figure [16\)](#page-11-0) was determined according to the following Equation (1):

<span id="page-11-0"></span>

$$
F = 2.1572U + 5.4858 \tag{1}
$$

**Figure 16.** Voltage—force ratio graph for load cell 1 (660). **Figure 16.** Voltage—force ratio graph for load cell 1 (660).

The calibration was carried out in the same way for load cell 2 on amplifier 662, Equation (2):

$$
F = 2.1537U - 0.3045 \tag{2}
$$

2.4.2. Bending Measurement of Specimen The measured dependency (voltage–force) was extrapolated to the entire measuring range of the forces.

#### 2.4.2. Bending Measurement of Specimen

In addition to force measurements, the bending of the sample under the load was also measured in a four-point bending test. The measuring system is designed in such a way that the position of the piston can be monitored without contact. The sensor is attached to the cylinder housing and follows the movement of the magnet, which is mounted inside the cylinder on the piston itself, without contact (Figure [17\)](#page-12-0). The measuring system operates on the phenomenon of magnetostriction, in which the dimensions of the crystal lattice of ferromagnetic materials (iron, nickel and cobalt) change under the influence of a changing external magnetic field [\[40\]](#page-16-10). In principle, the phenomenon of magnetostriction is present in all ferromagnets, but it is practically measurable and only useful in some cases if the deformations are large enough (in the order of  $\mu$ m/m). The non-contact nature of the measuring system ensures a long life without maintenance.

<span id="page-12-0"></span>

Figure 17. (a) Non-contact displacement sensor, (b) and in the mounted state next to the cylinder.

# <span id="page-12-2"></span>*2.5. Fatigue Life Data Analysis 2.5. Fatigue Life Data Analysis*

For a profiled bending beam made of spruce wood only a few fatigue tests have been carried For a profiled bending beam made of spruce wood only a few fatigue tests have been carried out so far. To shorten the test time, the fatigue tests were terminated after  $500,\!000$  load cycles. The test data are shown in Figure 18 in Se[cti](#page-12-1)on 3 together with a modelled Woehler curve. The Woehler curve was determined according to the principle proposed by Klemenc and Fajdiga [\[37\]](#page-16-7) and improved by Klemenc [\[38\]](#page-16-8). Within this approach, the Woehler curve is modelled using the conditional Weibull probability density function  $g(N|F)$ , whose scale parameter  $\eta$  depends on the load force F by an inverse power-law:

$$
g(N|F) = \frac{\beta}{\eta(F)} \left(\frac{N}{\eta(F)}\right)^{\beta-1} \exp\left[-\left(\frac{N}{\eta(F)}\right)^{\beta}\right]; \ \beta, \eta(F) > 0 \tag{3}
$$

$$
\eta(F) = 10^{A+B \cdot \log(F)}\tag{4}
$$

ߟሺܨሻ = 10ା∙୪୭ሺிሻ (4) The three parameters, i.e., a Weibull shape parameter β, an intercept *A* and a slope *B* in a log*N*-log*F* diagram determine the Woehler curve model. In this way, it is possible to model both a trend and a scatter of the Woehler curve. The three unknown parameters  $\beta$ ,  $A$  and  $B$  are estimated on the basis of the experimental fatigue-life data set  $\{(F_i, N_i, \delta_i); i = 1, ..., n\}\$ using the following maximum likelihood  $\text{cost function } L:$   $\begin{array}{c} \n\frac{1}{n} \n\end{array}$ cost function *L*:

$$
L(A, B, \beta) = \sum_{i=1}^{n} (\delta_i \cdot \ln[g(N_i|F_i)] + (1 - \delta_i) \cdot \ln[1 - G(N_i|F_i)])
$$
\n(5)

 $\delta_i$  is an indicator of a fatigue failure ( $\delta_i = 1$ ) or a run-out experiment ( $\delta_i = 0$ ).  $G(N_i|F_i)$  is a cumulative ำงา probability function of the probability density function from the following Equation (3):

$$
G(N_i|F_i) = \int_{N=0}^{N_i} g(N|F_i) \cdot dN = 1 - \exp\left[-\left(\frac{N_i}{\eta(F_i)}\right)^{\beta}\right]
$$
(6)

The maximisation of the objective function *L* in Equation (5) against the parameters β, *A* and *B* was performed with a real-valued genetic algorithm, as explained in [\[38\]](#page-16-8). Ten runs of the genetic algorithm from different random initial values were repeated.

### <span id="page-12-1"></span>**3. Results and Discussion**

After several months of operation of the test rig, it can be determined that the system works reliably and robustly. However, there are some limitations due to the small number of functions offered

by the PLC and therefore it might be useful to combine the control and data acquisition in a more advanced system that reacts dynamically and adapts itself during the test. There are solutions on the market that allow not only the control of the test rig but also the recording of all relevant test parameters (forces, deflection); test parameters are recorded either locally on flash media (SD card) or saved at a network location [\[40\]](#page-16-10). However, such systems do not offer solutions for the processing and analysis of the measurement data and this still has to be carried out separately, which is an additional disadvantage besides the very high purchase price. At the same time, it would make sense to use the already existing outputs (analog and digital) on the measurement interface NI USB 6009 and thus change the amplitude and frequency of the load in the fatigue process. In a more complex implementation of PLC with the measuring system on the test rig, the frequency and time of the valve opening could also be actively changed (e.g., FM—frequency modulation) and the load intensity could be controlled by adjusting the pressure on the pressure regulator (e.g., AM—amplitude modulation).

Despite the known purpose of the test rig, the design of the test rig took into account the customer's wish to be able to perform other tests on the test rig in the future, both dynamic (tension, compression) and static, which meet the test requirements of ISO 13061-4: 2014 [\[41\]](#page-16-11) and ISO 13061-3: 2014 [\[42\]](#page-16-12) for determining the modulus of elasticity and bending strength. For this purpose, it would be necessary to introduce a new regime, in addition to the existing cyclic operation, in which the piston movements are precisely controlled. According to the standard ISO 13061-4: 2014 [\[41\]](#page-16-11), the test specimen must fail within a time frame between 0.5 and 5 min at constant velocity of the pressure element. With existing components, a closed velocity control loop could be realized. An existing (already used) contactless magnetic position measuring system would be used to measure the velocity. The control algorithm would be implemented in a LabView application using the existing measurement interface NI USB 6009. The constant velocity of the cylinder piston or pressure element would be provided by the existing pressure regulator, with the pressure being adjustable via the analog voltage input.

<span id="page-13-0"></span>A cost analysis of the test rig components was also performed. Table [1](#page-13-0) shows the total costs for the main components of the test facility. The cost analysis shows that the test rig is much more cost-effective for the customer and the intended use compared to commercial test equipment.

<b>Item</b>	Cost (EUR)
Frame	1300
Pneumatics	2200
Guide	400
Controller	150
Load cells	400
Consumables	500
Total	4950

**Table 1.** Approximate component costs.

A total of ten fatigue-life tests were performed at three load levels of force *F*: 8700 N, 8000 N and 7300 N (see Figure [18\)](#page-14-0). Nine tests resulted in fatigue failures and the terminal value of 500,000 load cycles was reached in one test at the lowest load level.

The ten experimental data points from Figure [18](#page-14-0) were used to estimate the parameters β, *A* and *B* of the modelled Woehler curve according to the procedure in Section [2.5.](#page-12-2) In each of the repetitions of the genetic algorithm, a convergence to the final value of the parameters β, *A* and *B* was achieved between 10,000 and 100,000 iterations. The highest value of the objective function *L* was 103.5697. The corresponding values of the parameters in Equations (3) and (4) are:  $\beta = 0.5378$ ,  $A = 112.1910$  and *B* = −27.5385. The relatively low value of the shape parameter  $\beta$  indicates a high scattering of the test results, which is confirmed by an outlier at the loading level of *F* = 7300 N, which is far to the left of the Woehler curve for 10% probability of failure. On the other hand, the slope parameter *B* for spruce beams is two to three times lower compared to the typical slopes of the Woehler curves for structural

steels and aluminium alloys. This means that spruce wood is less sensitive to the fatigue phenomenon than the typical structural metals. A total of ten fatigue-life tests were performed at three load levels of force *F*: 8700 N, 8000 N and 300 notes and annunual anotes. This include that sprace wood is icss schstave to the taugue phenomenon

<span id="page-14-0"></span>

**Figure 18.** Experimental data and the modelled Woehler curves for different probabilities of failure. **Figure 18.** Experimental data and the modelled Woehler curves for different probabilities of failure.

#### The ten experimental data points from Figure 18 were used to estimate the parameters *β*, *A* and **4. Conclusions**

The test rig was developed in cooperation with a company that manufactures large wooden windows (height over 3 m to 6 m). The dimensions of the aluminum-reinforced wooden beam were decisive for the design of the test rig and its components. The components of the test rig are presented, and their characteristics and tasks are explained. The test rig has been working robustly and reliably for a long time. The cost analysis of the test rig components shows that, for the specific company producing wooden windows, the construction of a dedicated test facility with the possibility to adapt it to the company's test requirements is much cheaper than commercial test facilities. With the presented in-house developed test rig, it is possible to perform fatigue life tests on bending beams. Despite the significant scattering of the fatigue test data, they allow an estimation of the Woehler curve and its scattering. The first experimental results show that spruce wood is less sensitive to the fatigue **4. Conclusions**  FEM analyses of material fatigue, which allows the prediction of the duration of the product (such as a hybrid wooden beam). That manufactures large wooden with a company that manufactures large wooden beam  $\mathbf{r}$ phenomenon than typical metals. The results in the form of *S*–*N* curves serve as input parameters in

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