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A Sine Cosine Algorithm-Based Fractional MPPT for Thermoelectric Generation System

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Abstract: Thermoelectric generators (TEGs) are equipment for transforming thermal power into electricity via the Seebeck effect. These modules have gained increasing interest in research fields related to sustainable energy. The harvested energy is mostly reliant on the differential temperature between the hot and cold areas of the TEGs. Hence, a reliable maximum power point tracker is necessary to operate TEGs too close to their maximum power point (MPP) under an operational and climate variation. In this paper, an optimized fractional incremental resistance tracker (OF-INRT) is suggested to enhance the output performance of a TEG. The introduced tracker is based on the fractional-order $PI^{\lambda}D^{\mu}$ control concepts. The optimal parameters of the OF-INRT are determined using a population-based sine cosine algorithm (SCA). To confirm the optimality of the introduced SCA, experiments were conducted and the results compared with those of particle swarm optimization (PSO) and whale optimization algorithm (WOA) based techniques. The key goal of the suggested OF-INRT is to overcome the two main issues in conventional trackers, i.e., the slow dynamics of traditional incremental resistance trackers (INRT) and the high steady-state fluctuation around the MPP in the prevalent perturb and observe trackers (POTs). The main findings prove the superiority of the OF-INRT in comparison with the INRT and POT, for both dynamic and steady-state responses.

Keywords: sine cosine algorithm; fractional $PI^{\lambda}D^{\mu}$ control; thermoelectric generator; MPPT



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1. Introduction

In recent decades, thermal energy has become one of the renewable energies abundantly available in several industrial and civil sectors, namely, in powering electronic devices, driving electric vehicles, and in pumping applications [1,2]. Thermoelectric generators (TEGs), used in thermal energy conversion systems, are a type of active equipment that transform thermal power into electricity via the Seebeck effect [3,4]. These thermal devices have received increasing focus due to their capability to directly transform waste heat into electricity. Made up of different thermocouples, joined electrically in series and thermally in parallel, these heat modules are extensively utilized in various areas and domains, thanks to their attractive merits in terms of their power efficiency, the absence of moving parts and pollution, silent operation, free maintenance, and a long service life [1,2,5,6]. These thermal converters have gained increasing interest in the research fields concerned with their modeling, control, and optimization in various real-world applica-

tions. Therefore, characterized, maximum power point tracking (MPPT) approaches are mainly used to maximize the power harvested from TEG converters.

In all renewable energy converters, tracking the maximum power point (MPP) is vital to extracting the most power under varying environmental conditions. Various studies from the literature have reported on the MPPT control design and the implementation of TEG systems. The authors of [7] combined a TEG device with a photovoltaic (PV) module within a hybrid PV–TEG architecture in a pumping application for rural areas. A control approach for a synchronous reluctance motor-based drive train was investigated in the context of a perturb and observe (P&O) MPPT scheme. The motor output energy and pump flow rate of such a hybrid PV–TEG converter are significantly increased in comparison with those adopting only a PV array. The authors of [8] used a hybrid PV–TEG energy source and a dynamic voltage restorer (DVR) for disturbance compensation in a three-phase distribution grid; an intelligent MPPT strategy, based on an advanced variable factor adaptive fuzzy logic controller (VFAFLC), was introduced to obtain the optimal available power from the PV–TEG module. Energy converters, such as the one proposed, efficiently compensate for load disturbances when in the energy conservation mode. The authors of [9] proposed and considered an extremum seeking control (ESC) algorithm-based MPPT approach for a TEG converter. The efficiency of the ESC method has been compared with the P&O method under the same circumstances; the demonstrative results report that the ESC-based MPPT approach captured more energy than the P&O-based one. The authors of [10] present a digital polynomial controller for an automotive TEG system to enhance a vehicle's power supply, in which the maximum power point tracking is achieved with a gradient method and input current control; an adaptive step-size method was proposed to reduce the conversion time of the MPPT algorithm. The authors of [11] proposed a novel MPPT-control approach, based on indirect open-circuit voltage detection and short-circuit current estimation techniques for a TEG system. The authors investigated P&O strategies which best adjusted for the poor performance of transient MPP states during rapid variations of the temperature gradient across the constructor. They introduced a voltage-sensing technique to decrease the number of voltage sensors used to supervise the battery output or load voltages. The authors of [12] proposed an easy and valuable analog MPPT control resolution for a TEG heat converter which sought the peak gain point of the used DC–DC boost converter. The main characteristic of such a control method is that the duty ratio of the input clock pulse moves in the direction of the maximum power point of the TEG by finding the peak point of the voltage conversion gain of the boost converter. An MPPT algorithm, based on open-circuit voltage, is proposed in [13] as the most suitable technique for optimizing the linear electrical properties of TEGs. The study's results, using commercial TEG devices, confirmed that their converter precisely tracked the MPP during thermal transients, with a tracking efficiency of 99.85%.

Recently, an enormous set of MPPT approaches has been introduced in the literature, of which hill climbing (HC) [14], P and O [7,11,15], incremental conductance (INC), and/or incremental resistance (INR) [14,16–18] are the most widely investigated. As is known, the HC-based MPPT approach introduces a disturbance in the duty cycle of the converter [14]. However, the P&O technique introduces a disturbance in the operative voltages of energy converters [14,15]. Thus, in the two discussed MPPT approaches, a tradeoff should be considered in selecting the amount by which to augment the control law, i.e., the PWM duty cycle or reference voltage, is updated; large values decrease the MPP steady-state due to the huge disturbances around it, while lesser values decrease the dynamic action under a rapid variation in the operational conditions or load. The INR- or INC-based MPPT methods leverage the tendency of power to flow in the opposite direction when the voltage at the MPP is zero [16–18]. These MPPT algorithms have been suggested to reinforce the tracking precision and dynamic efficiency of energy converters in the presence of rapidly varying conditions, whereby the steady-state fluctuations, characterizing the HC and P&O methods, are dampened more, or even eliminated, since the derivative of the power of the voltage/current disappears at the MPP. Other techniques such as a short-circuit current

and open-circuit voltage-based MPPT block diagrams have been proposed to obtain the peak power of the renewable energy converters [11,13,19].

From the cited MPPT methods, the INR-based method is the most adopted for TEG systems at present. These MPPT algorithms are extensively employed and perform well due to their easy and low-cost implementation as well as for their high tracking accuracy. Since the conventional algorithm of INR trackers (INRTs) utilizes a settled iteration step size, such an effective control parameter is determined by a tradeoff between the accuracy at a steady-state and tracking speed condition. The design must correctly process the dilemma between tracking dynamics and steady-state oscillations. To overcome this design problem and further improve the steady-state performance of INRTs, many updated methods from the original method have been introduced in the literature. Some improvement strategies propose to consider a variable step size instead of a fixed one, which are called Variable Step-Size Incremental Resistance (VSS-INRT) Tracking strategies [20–24]. The step-size parameter is updated according to the inherent characteristics of the TEG systems. If the operating point is far from the MPP, the VSS-INR tracker increases the step size, enabling a fast-tracking capability. Otherwise, if the operating point is near the MPP, the step size becomes so very small that the steady-state oscillations become well dampened, improving the VSS-INR tracker's efficiency in terms of the steady-state accuracy and tracking response fastness [20,21]. Other enhancement methods use the concepts of MPPT based on the fractional order control and calculus [25–28]. The authors of [25,26] introduced an enhanced Fractional Order Fuzzy Logic Controller (FOFLC)-based MPPT method for TEG and PV-TEG hybrid energy devices to efficiently harvest the maximum power. The fractional-order term used in the INC/INR MPPT algorithms is a supporting fuzzy inference system for the precise tracking of the MPP and to modify the constant output after attaining the MPP. The authors of [27] used a similar fractional fuzzy MPPT approach for a PV system. The fractional-order factor is chosen based on the dynamic range of the fuzzy controller. A large value is first accorded to extend the fuzzy range and minimize the time of checking for the MPP. When reached, the FOFLC algorithm adopts a smaller value of the fractional factor to contract the fuzzy domain and eliminate the oscillations at the MPP. The authors of [28] proposed an interesting INC MPPT technique based on a Fractional-Order Integrator (FOI) for a PV device under climate variations. A Radial Movement Optimization (RMO) algorithm is adopted for attaining the fine gains of the variable step-size FOI-based INC MPPT.

In the fractional-order MPPT techniques, the error signal that defines the INC/INR of the energy converter is used as an input to the integrator. The gain of such an integrator is the scaling factor to tune the step size of the MPP tracker. The drawback of this VSS MPPT method is the slow dynamic response and poor tracking especially when there are fast changes in the load. To outperform this problem and improve the dynamic response of the INR/INC trackers, an Optimized Fractional INR Tracker (OF-INRT) using a PI^λ instead of a conventional integrator is proposed in this paper. The use of more efficient metaheuristic tools to determine all values of the OF-INRT's design parameters, i.e., proportional gain, integral gain, and fractional order, could improve the effectiveness of the proposed MPPT strategy. Further, in this work, a systematic and straightforward INR-based MPPT methodology using a fractional-order PI^λ controller is proposed and successfully applied to a TEG device. A Sine Cosine Algorithm (SCA), as an efficient and parameter-free metaheuristic, is investigated for the optimal design of the fractional PI^λ -based INRT. The major contributions for this research work are summarized as: (1) An efficient fractional VSS-INR-based MPPT approach for a TEG module is proposed to deal with the steady-state oscillations and lower accuracy of classical MPPT methods for TEG systems such as the PandO and HC techniques. (2) An advanced sine cosine metaheuristic is investigated to deal with the tedious and time-consuming trials-errors based procedures that often lead to local solutions for the problem. (3) ANOVA statistical tests are proposed for a fair comparison of the proposed SCA-INRT with all reported solvers as well as with other similar MPPT techniques, i.e., P&O and conventional INR.

The remainder of the paper is arranged as follows: In Section 2, the mathematical representation of the studied TEG is presented. In Section 3, a brief overview of MPPT approaches for TEGs is described. The conventional perturb and observe, integer control- and fractional-based incremental resistance methods are particularly investigated. In Section 4, the tuning of all effective control parameters of the PI^λ-based OF-INRT is reformulated as a constrained optimization problem. Metaheuristics proposed to solve such a hard optimization problem are described in Section 5. In Section 6, demonstrative results and ANOVA tests are presented and explained for the proposed SCA-INRT's tuning approach. Section 7 states the conclusion and future works.

2. Modeling of the Thermoelectric Generator

The overview of the TEG module is shown in Figure 1a. The fundamental element is a thermocouple that contains p-type and n-type semiconductors [1–6,25,26]. These conductors were electrically interconnected in series using a metal strip. To build a TEG module, several p-type and n-type pellets were interconnected together to increase the required rating of the output power as presented in Figure 1b. They were electrically linked in series to boost the voltage potential, and thermally in parallel to decrease the thermal resistance [26,29–31]. The couples were inserted between two parallel ceramic sheets to form a hot side and a cold side. When there was a temperature variation between the hot part and the cold part, a direct current flowed in the load as presented in Figure 1c.

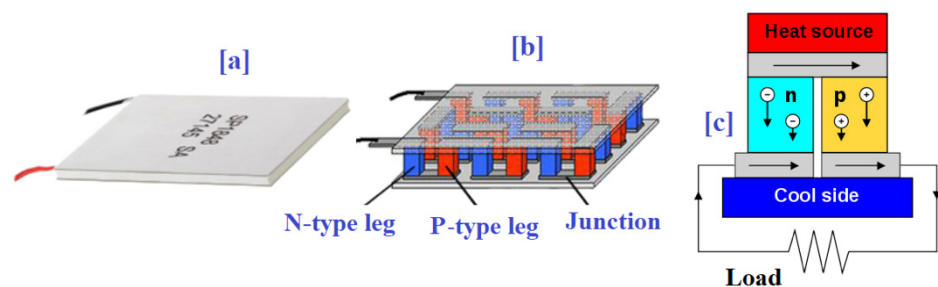


Figure 1. Hardware structure of a TEG module. (a) Overview of the TEG module; (b) P-type and N-type pellets, and (c) TEG circuit.

The core idea of TEG modules is built according to the Seebeck impact [1–4]. The open-circuit voltage of a TEG can be estimated by applying the following formula [7,8,26]:

$$V_{oc} = \alpha(T_h - T_c) = \alpha\Delta T \quad (1)$$

where T_h and T_c are the temperatures at the hot and cold parts of the TEG device, respectively, ΔT indicates the temperature variation between these two sides, and α denotes the Seebeck coefficient.

Considering the steady-state power balance at both parts of the TEG, the absorbed heat generated by the thermal load and the heat passed by the heat sink can be formulated as follows [7,8,26]:

$$Q_h = \alpha IT_h - K_{tc}\Delta T - 0.5I^2R_{teg} \quad (2)$$

$$Q_c = \alpha IT_c - K_{tc}\Delta T + 0.5I^2R_{teg} \quad (3)$$

where K_{tc} indicates the thermal conductivity, R_{teg} is the inner resistance of the TEG, and I is the TEG operating current.

The output power of the TEG can be calculated considering the variation between the heat flows at the hot and cold parts as follows:

$$P_{teg} = Q_h - Q_c = \alpha(T_h - T_c)I - I^2R_{teg} = (\alpha\Delta T - IR_{teg})I = V_{teg}I \quad (4)$$

where $V_{teg} = V_{oc} - IR_{teg}$ denotes the TEG terminal voltage output.

Based on the concept of maximum power transfer [5–8], the most obtainable power of the TEG could be reached when the load resistance was similar to the inner resistance of the TEG.

3. Brief Overviews on MPPT Approaches

Three MPPT techniques were studied in this paper: perturb and observe, the incremental resistance method based on an integer control, and optimized incremental resistance based on a fractional-order PI^λ control. In the following subsections, a brief preview of the major MPPT methods used for TEG systems is provided. The P&O and INR techniques were particularly considered. The synoptic scheme for any MPPT control approach of TEG systems is presented in Figure 2.

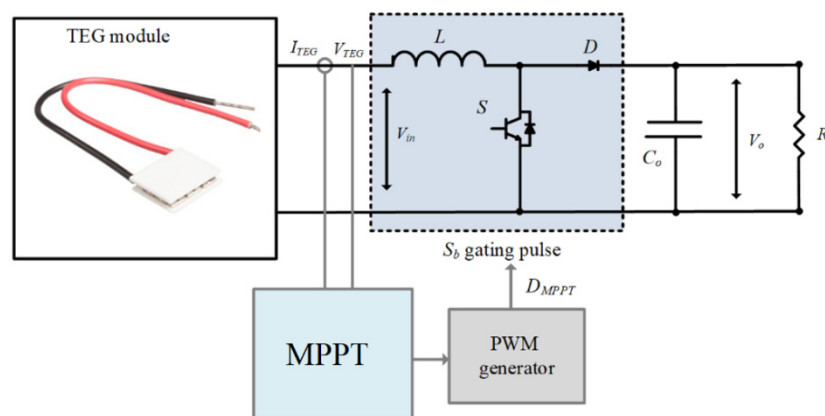


Figure 2. MPPT control scheme of a TEG system.

3.1. Perturb and Observe MPPT Method

In the MPPT formalism, P&O is considered the most frequently adopted method to track the MPP in TEG systems with a more simple structure and less algorithm complexity [7,11,14,15]. As shown in Figure 3, the P&O algorithm periodically introduces a perturbation Δ in the operating current of TEG and contrasts the output power with that of the prior MPPT period [7,11]. A variation in the operating power was noted. As a result, if the operating current of the TEG module changed and the power increased, the P&O MPPT tracker shifted the operative point in that orientation. Otherwise, this operating point was switched in the reversed orientation.

On the other hand, the size of the perturbation Δ is crucial in the design of a conventional P&O tracker. One can observe that the larger the value of perturbation, the faster the P&O tracker's convergence and vice versa. Unfortunately, this perturbation size increase could lead to large fluctuations and oscillations in the output power and drive to a considerable lack of energy. Once the neighborhood of the MPP was reached, the operating point went back and forth around the MPP. Then, the P&O tracker did not precisely attain the MPP, but it fluctuated around that point undefined. To remedy this common problem, several improved P&O-based MPPT methods have been proposed in the literature for several renewable energy converters [32,33].

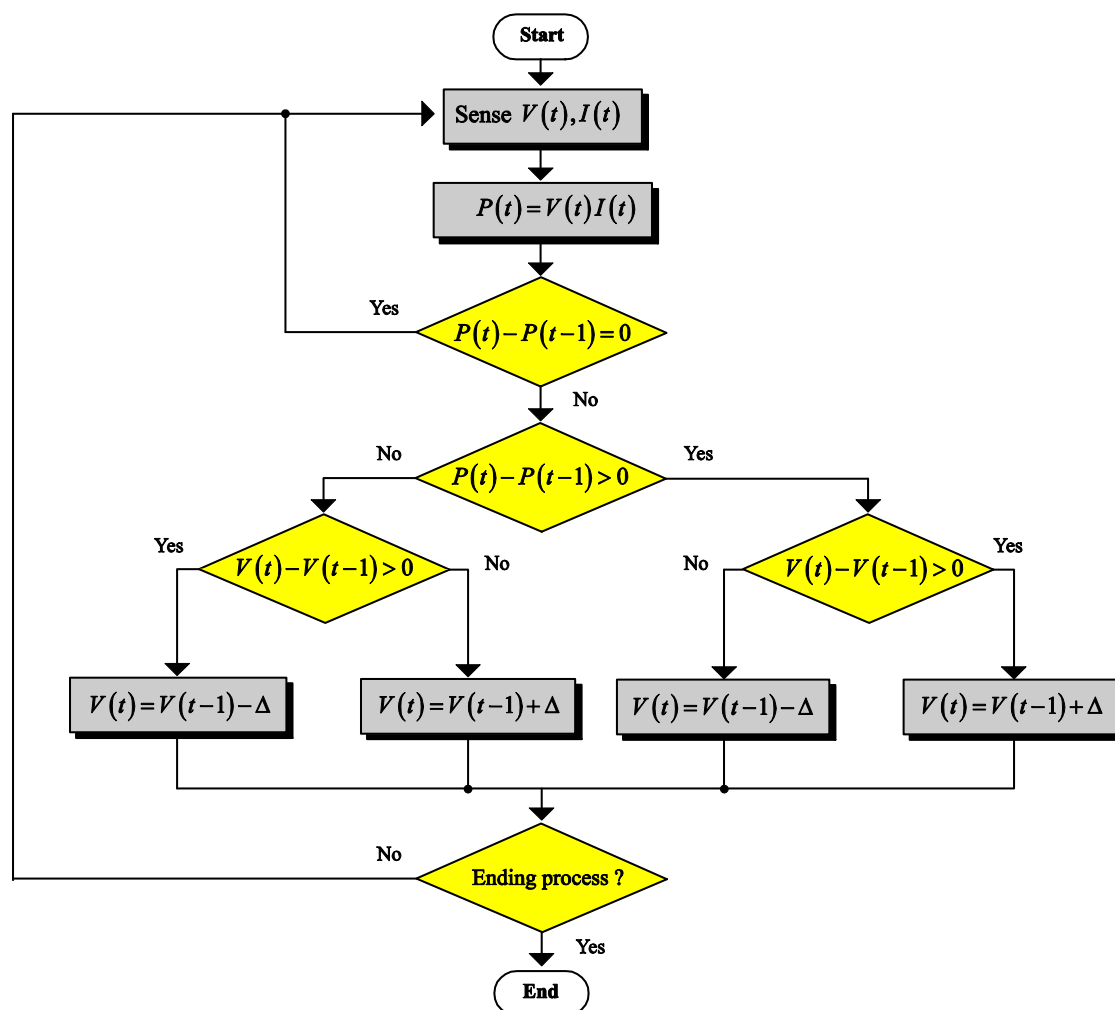


Figure 3. Flowchart of P&O-based MPPT method.

3.2. Incremental Resistance MPPT Technique

Among all the MPPT methods for TEG systems, incremental resistance techniques have been broadly adopted because of the high steady-state tracking precise and oscillations damping/reduction [7,8]. The basic concept of the INR technique is built around the truth that the derivative of the TEG power related to the TEG current (dP/dI) is zero at the MPP [20,25,26]. The slope of the TEG power characteristics is zero at the MPP, positive for values located on the left side of the MPP (amounts of output current smaller than the current at MPP) and negative for amounts located on the right side (values of output current larger than the current at the MPP). Accordingly, the error signal used by the INR-based tracker is formulated as follows:

$$\frac{dP}{dI} = \frac{d(V * I)}{dI} = V + I \frac{dV}{dI} = 0 \Leftrightarrow \frac{dV}{dI} + \frac{V}{I} = \frac{V(t) - V(t-1)}{I(t) - I(t-1)} + \frac{V(t)}{I(t)} = 0 \quad (5)$$

$$e(t) = \frac{V(t) - V(t-1)}{I(t) - I(t-1)} + \frac{V(t)}{I(t)} \quad (6)$$

where V and I are the instantaneous voltage and current of the energy converter, respectively, and t denotes the increment time. The measures voltage and current are used to estimate the instantaneous power.

The maximum power output from a TEG system can be achieved by maintaining the duty cycle D (%) of the DC–DC boost converter, as the power moderator between the TEG module and the load (battery) [25,26]. The modification of such a control parameter

is usually performed by the MPPT tracking algorithms to catch the most power from the TEG. A flowchart for the INR-based tracker of a TEG device is depicted in Figure 4.

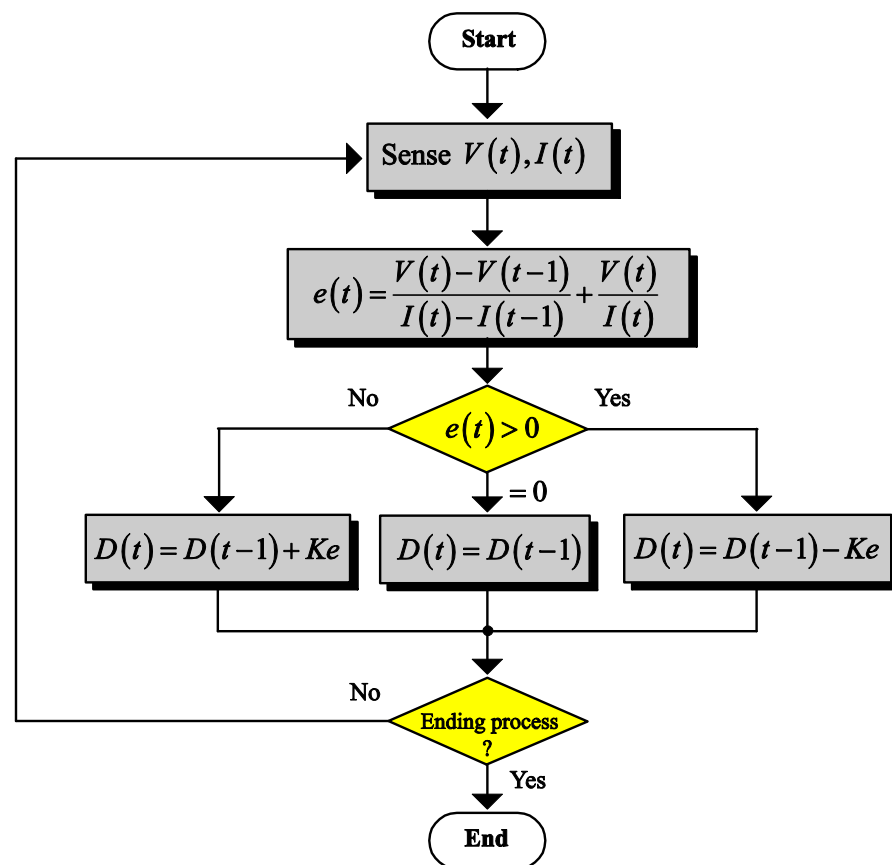


Figure 4. Flowchart of INR-based MPPT technique.

Since the error signal $e(\cdot)$ of Equation (6) was very small around the MPP, the step size of the INR method was updated based on the value of the error signal. To achieve this and to model the INR approach, integer-order control approaches, i.e., mainly such as PID controllers and variants, were widely used in this formalism. To further improve the INR-based MPPT approach in terms of fastness response and steady-state accuracy, the techniques based on VSS-INR trackers have been proposed in the literature. In this case, the step-size parameter was directly proportional to the error signal. Therefore, the step size became small as the error was very small around the MPP. The preciseness of the VSS-INR tracking approach was further improved in the steady-state [20–24]. The VSS-INRT can be presented by a normal discrete integrator with the error signal as the input and a tuned gain.

4. Fractional INRT Design Problem Formulation

4.1. Preliminaries

To improve the dynamic response of the conventional incremental resistance method, a fractional-order $PI^\lambda D^\mu$ -based control was adopted [34–36]. The fractional INRT utilizes a fractional PI^λ controller instead of an integer integrator. The fractional-order control has been investigated previously in different engineering fields and showed remarkable superiority over the conventional PID approaches. Such a control structure contains a non-integer order that has several advantages such as flexibility in design and high robustness. The fractional-order PI^λ transfer function can be defined as [34,35]:

$$C(s) = K_p + K_i s^{-\lambda} \quad (7)$$

where K_p is the proportional gain, K_i is the integral gain of the fractional PI^λ controller, and λ indicates the non-integer order of PI^λ .

4.2. Tuning Problem Formulation

The selection of fine values for the gains of the PI^λ controller of Equation (7) for the OF-INRT of TEGs is often conducted by time-consuming and tedious trial–error-based procedures. This adjusting problem turned into a hard task without a systematic approach and regarding the complexity of the TEG operating conditions. To deal with these difficulties and drawbacks of classical tuning methods, the determination of these effective control parameters through an optimization program remained a promising idea. During the optimization process, the decision variables, i.e., proportional gain $K_p \in \mathbb{R}_+$, integration gain $K_i \in \mathbb{R}_+$, and fractional-order $\lambda \in \mathbb{R}_+$, were used to maximize the harvested energy from the TEG, shown as the objective function of the following formulated optimization problem:

$$\begin{cases} \text{Maximize } f(x) \\ x \in \mathcal{S} \\ \text{Subject to} \\ h_i(x) \leq 0; \forall i = 1, \dots, n_{con-eq} \\ g_j(x) = 0; \forall j = 1, \dots, n_{con-ineq} \end{cases} \quad (8)$$

where $f: \mathbb{R}_+^3 \rightarrow \mathbb{R}$ is the cost function that quantifies the harvest TEG energy,

$\mathcal{S} = \{x = (K_p, K_i, \lambda) \in \mathbb{R}_+^3; x_{\min} \leq x \leq x_{\max}\}$ is the initial search space, which is considered to include targeted design gains, and $h_i: \mathbb{R}_+^3 \rightarrow \mathbb{R}$ and $g_j: \mathbb{R}_+^3 \rightarrow \mathbb{R}$ are the problem's constraints with equality and inequality types, respectively.

Finally, the implemented MATLAB/Simulink model of the optimized fractional-order INRT-based MPPT strategy for the studied TEG device is shown in Figure 5. The population-based SCA metaheuristic, as well as others used as comparison tools, was proposed to solve such a formulated problem. A description of all these reported algorithms is given in the following Section.

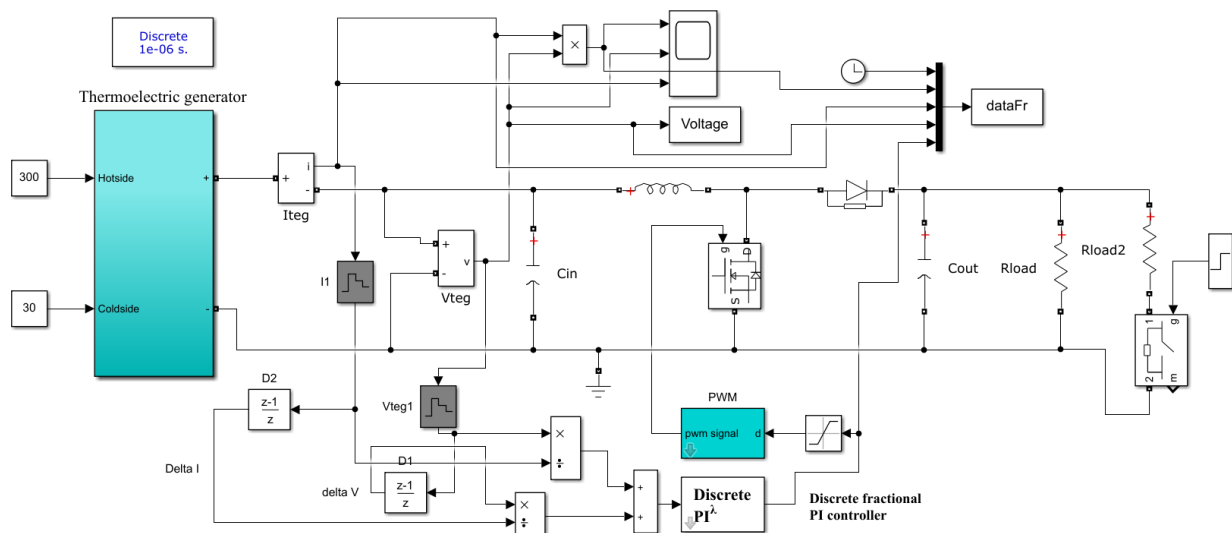


Figure 5. MATLAB/Simulink model of the OF-INRT-based MPPT.

5. Algorithms for Fractional INRT Design

5.1. Sine Cosine Algorithm

The sine cosine algorithm (SCA) is a random population-based metaheuristic built based on the concepts of trigonometric functions, namely, the sine and cosine functions. Proposed by S. Mirjalili [37], the SCA metaheuristic uses these mathematical functions to

detect the best solution for a given optimization issue [38,39]. Similar to other population-based metaheuristics, the SCA begins with a group of random candidate solutions, and then evaluates them frequently by an objective function and a group of motion standards. In SCA formalism, the position updating equations for both exploration and exploitation phases are given as follows:

$$\mathbf{x}_{k+1}^i = \mathbf{x}_k^i + r_1 \sin(r_2) \left| r_3 \mathbf{p}_k^i - \mathbf{x}_k^i \right|, r_4 < 0.5 \quad (9)$$

$$\mathbf{x}_{k+1}^i = \mathbf{x}_k^i + r_1 \cos(r_2) \left| r_3 \mathbf{p}_k^i - \mathbf{x}_k^i \right|, r_4 \geq 0.5 \quad (10)$$

where $\mathbf{x}_k^i = (x_k^{i,1}, x_k^{i,2}, \dots, x_k^{i,d})$ is the current placement of the i th candidate solution at the actual iteration k and dimension d , $\mathbf{p}_k^i = (p_k^{i,1}, p_k^{i,2}, \dots, p_k^{i,d})$ is the position of the destination point, and r_1, r_2, r_3 , and $r_4 \in \mathcal{U}\{0,1\}$ are random numbers uniformly distributed in the adequate intervals, where $(i, k, d) \in [1, n_p] \times [1, k_{\max}] \times [1, d_{\max}]$.

In the SCA's motion Equations (9) and (10), four main control parameters were introduced [37–39]. The first effective design parameter r_1 dictates the movement direction, i.e., information about the next placement areas. Such an orientation could either be inside the area between the current solution and the aim or out of it. The second design parameter $r_2 \in [0, 2\pi]$ determines how far the solution's motion should be towards or outwards the target. The third coefficient r_3 defines random weights for the destination to randomly assure ($r_3 > 1$) or deemphasize ($r_3 < 1$) the impact of the desalination in determining the distance. The fourth design parameter r_4 equally turns between the sine and cosine parts in the SCA's motion Equations (9) and (10).

Finding the favorable areas of the search space with a non-premature convergence to the global optimum needs a best equilibrium between the exploration and exploitation phases. To optimally balance these two capabilities of the SCA, the range of the sine and cosine in Equations (9) and (10), given by the control parameter r_1 , were adaptively updated as follows:

$$r_1 = \beta - \beta k / k_{\max} \quad (11)$$

where k is the current iteration, k_{\max} is the maximum number of iterations, and β is a constant parameter.

5.2. Particle Swarm Optimization

The particle swarm optimization (PSO) method is a global metaheuristic that uses a population of n_p particles, randomly dispersed within an initially bounded search space, to detect an optimal solution for a given optimization problem [40,41]. Each particle in the swarm was titled with a vector of positions $\mathbf{x}_k^i = (x_k^{i,1}, x_k^{i,2}, \dots, x_k^{i,d})$ and a vector of velocities $\mathbf{v}_k^i = (v_k^{i,1}, v_k^{i,2}, \dots, v_k^{i,d})$.

At the current iteration, the positions and velocities of particles changed depending on the following motion equations [41]:

$$\mathbf{x}_{k+1}^i = \mathbf{x}_k^i + \mathbf{v}_{k+1}^i \quad (12)$$

$$\mathbf{v}_{k+1}^i = w \mathbf{v}_k^i + c_1 r_{1,k}^i (\mathbf{p}_k^i - \mathbf{x}_k^i) + c_2 r_{2,k}^i (\mathbf{p}_k^s - \mathbf{x}_k^i) \quad (13)$$

where w indicates the inertia factor, c_1 and c_2 define the cognitive and the social scaling parameters, $r_{1,k}^i$ and $r_{2,k}^i$ denote two random values uniformly scatted within the domain

$\llbracket 0, 1 \rrbracket$, \mathbf{p}_k^i and \mathbf{p}_k^s are the best placements previously gained by the i th particle and the whole swarm, respectively.

The exploration and exploitation mechanisms of the PSO method can be further reinforced when adopting a linear evolution technique of the inertia factor [40,41]. Such a design parameter of PSO technique was updated over iterations as follows:

$$w_{k+1} = w_{\max} - (w_{\max} - w_{\min})k/k_{\max} \quad (14)$$

where w_{\max} and w_{\min} denote the maximum and minimum values of the time-varying inertia factor typically set to 0.9 and 0.4, respectively.

5.3. Whale Optimization Algorithm

The whale optimization algorithm (WOA) is a population-based metaheuristic proposed by S. Mirjalili and A. Lewis [42]. It is a nature-inspired global algorithm which simulates the hunting behavior of humpback whales in finding and hunting their prey [42,43]. Humpback whales try to hunt and attack herds of small fish or krill that are near to the surface. This is performed by generating specific bubbles in a spiral or nine shaped paths around the prey. The WOA mimicked the bubble-net hunting mechanism to achieve the optimization. The mathematical modeling of each phase in the WOA is detailed in the following parts.

5.3.1. Encircling Prey

Whales can recognize the prey's location in the search space and encircle them. In the WOA formalism, the position of the optimal solution is not known a priori. The algorithm assumes that the current best candidate solution is the target prey or is near to the optimum. After the best search agent is defined, the other agents try to update their positions towards the best one. Such a behavior is modeled at the current iteration by the following motion equations:

$$\begin{cases} \mathbf{x}_{k+1}^i = \mathbf{p}_k^i - \Delta_k^i |2r_k^i \mathbf{p}_k^i - \mathbf{x}_k^i| \\ \Delta_k^i = 2a_k^i r_k^i - a_k^i \end{cases} \quad (15)$$

where \mathbf{x}_k^i denotes the position's vector of humpback whales in the d-dimensional search space, \mathbf{p}_k^i is the position's vector of the best solution obtained so far, r_k^i are random numbers in the interval (0, 1), and a_k^i is a real coefficient linearly decreased vector from 2 to 0 over the course of iterations.

5.3.2. Bubble-Net Hunting

This phase presents the exploitation mechanism of WOA. It can be divided into two parts: the shrinking encircling of the prey, and the spiral upward encirclement and suppression [42,43]. The shrinking behavior is performed by reducing the value of a_k^i in Equation (15). The spiral updating position mimics the behavior of a humpback whale around its prey in a spiral movement according to the following equation:

$$\mathbf{x}_{k+1}^i = \begin{cases} \mathbf{p}_k^i - \Delta_k^i |2r_k^i \mathbf{p}_k^i - \mathbf{x}_k^i|, \rho < 0.5 \\ \delta_k^i e^{bl} \cos(2\pi l) + \mathbf{p}_k^i, \rho \geq 0.5 \end{cases} \quad (16)$$

where $\delta_k^i = |\mathbf{p}_k^i - \mathbf{x}_k^i|$ denotes the distance of the i th humpback whale to the prey, i.e., the best solution found so far, b is a constant to define the form of the logarithmic spiral, l and ρ are random numbers uniformly distributed in the ranges $(-1, 1)$ and $(0, 1)$, respectively.

5.3.3. Search for Prey

The humpback whales explore randomly for their prey in accordance with the position of each other. Dissimilar to the exploitation technique, the updated position of a search

agent was performed based on a randomly chosen search candidate rather than the best search one captured yet. This exploration technique is modeled as:

$$\begin{cases} x_{k+1}^i = x_k^{rand} - \Delta_k^i |2r_k^i x_k^{rand} - x_k^i| \\ \Delta_k^i = 2a_k^i r_k^i - a_k^i \end{cases} \quad (17)$$

where x_k^{rand} is a random position vector, i.e., a random whale, selected from the current population of size n_p .

6. Results and Discussion

Firstly, for examining and analyzing the output characteristics of the studied TEG device with varying temperature differences, a MATLAB code was designated. In the current study, a TEG (12611-6.0) module was considered. Table 1 presents the operational characteristics and specifications of the studied TEG.

Table 1. Specifications of the TEG (12611-6.0).

Characteristics	Specification
Hot side temperature	300 °C
Cold side temperature	30 °C
Open-circuit voltage	8.4 V
Matched load resistance	1.2 Ω
Matched load voltage	4.2 V
Matched load current	3.4 A
Matched load power	14.6 W

Figure 6 illustrates the TEG's power versus its operating current under a variation of the hot side temperature. In this design, the cold side temperature was fixed at 30 °C. Based on these demonstrative results, one can observe that there was a good agreement between the simulated data (blue line) and the manufacturing data (yellow points).

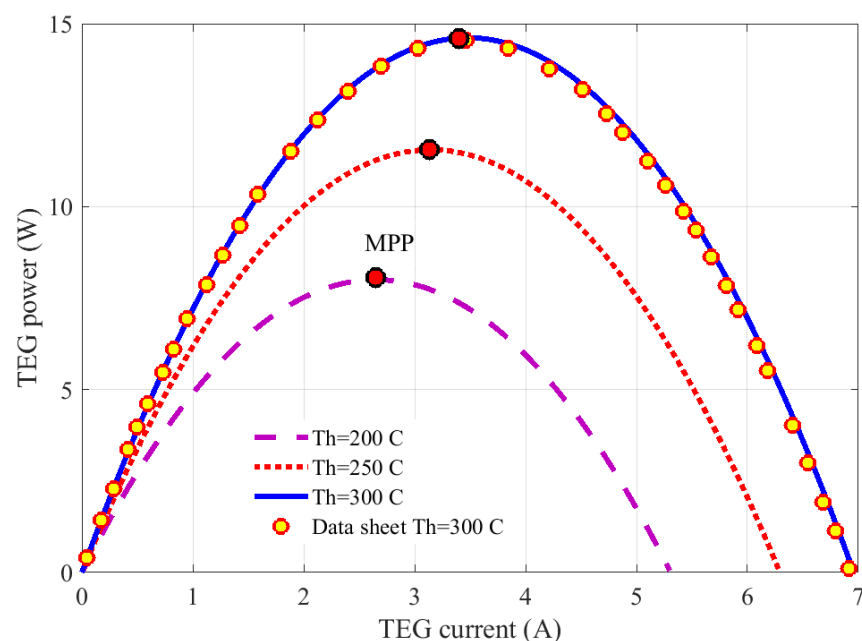


Figure 6. TEG power against current.

Three optimizers were stratified to evaluate the optimal gains of the introduced PI^λ -based OF-INRT. These population-based metaheuristics were SCA, PSO, and WOA. In this

design, the proportional gain K_p , integration gain K_i , and fractional order coefficient λ of the PI^λ controller were treated as the decision variables of the formulated optimization problem. The objective function to be maximized one was the amount of the harvested energy of the TEG. For a fair comparison, the population size and the maximum number of iterations for all reported optimizers were set to 10 and 25, respectively. To validate the reliability of the reported algorithms, every optimizer was executed independently 30 times. The best parameters of the OF-INRT found for the design problem (8) applying SCA, PSO, and WOA are presented in Tables 2 and 3. The statistical assessment of the considered optimizers is also demonstrated, i.e., results of Table 2.

Table 2. Optimal gains of the OF-INRT and statistical evaluations (30 runs).

	PSO	WOA	SCA
K_p^*	0.03346	0.0332	0.03765
K_i^*	06.6776	5.47598	8.43451
λ^*	0.98458	00.9425	1.01008
Best	01.3757	1.36972	1.34877
Worst	0.57694	0.70707	1.26059
Average	1.10599	1.16222	1.32868
Median	1.32888	00.2287	0.01591
Variance	0.10465	1.31844	1.33071
STD	0.32349	00.0523	0.00025
Efficiency (%)	80.3339	84.4638	96.5610

Table 3. Details of 30 runs using the considered optimizers.

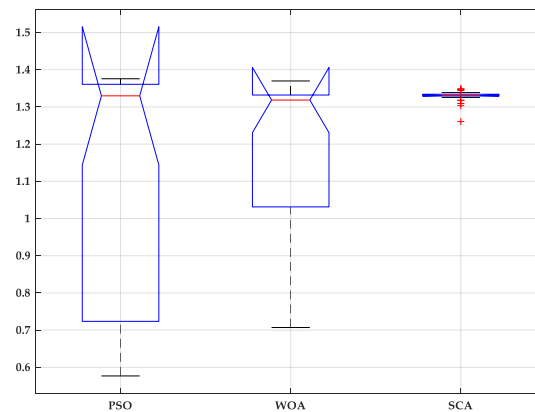
Run	PSO	WOA	SCA	Run	PSO	WOA	SCA
1	0.7275	1.04516	1.34397	16	1.36184	0.71506	1.32962
2	1.32642	1.36731	1.30919	17	0.60096	1.31844	1.33071
3	1.36623	1.33082	1.32548	18	1.34176	1.35291	1.33043
4	1.32796	1.21181	1.32965	19	0.68507	1.32879	1.32971
5	1.36341	1.36972	1.30332	20	1.37222	0.70707	1.33192
6	0.78113	1.33076	1.26059	21	1.31299	1.03375	1.31771
7	1.3757	1.34959	1.33083	22	0.70488	1.33196	1.33343
8	1.33915	0.83358	1.33339	23	1.37224	1.03113	1.34716
9	1.36749	1.30094	1.34877	24	1.34435	1.03126	1.33854
10	1.33397	1.36757	1.32855	25	0.68323	1.32933	1.33411
11	0.71208	1.03375	1.31771	26	1.35098	0.71506	1.32962
12	1.32979	1.33196	1.33343	27	0.61278	1.31844	1.33071
13	0.57694	1.03113	1.34716	28	1.36042	1.35291	1.33043
14	1.33174	1.03126	1.33854	29	0.73653	1.32879	1.32971
15	0.79199	1.32933	1.33411	30	1.28803	0.70707	1.33192

Referring to Table 2, the average cost function values varied between 1.10599 W and 1.32868 W. The maximum value was achieved by the proposed SCA. The standard deviation (STD) values changed between 0.32349 and 0.00025. The minimum STD' value was also achieved by the SCA technique. Concerning the efficiency, the maximum efficiency of 96.56% was achieved by the SCA metaheuristic, whereas the lowest efficiency of 80.33% was attained by the PSO one.

On the other hand, an analysis of the variance test (ANOVA, [44,45]) was conducted to verify the consistency of the SCA in determining the parameters of OF-INRT. ANOVA test results are presented in Table 4, and the distribution of the observations through the number of runs is presented in Figure 7. From these results, the p -value was much higher than the F value, which confirmed the difference between the provided performances. As illustrated in Figure 7, the SCA could provide the best results in terms of the mean fitness. Moreover, it had the lowest variation range where the fitness function varied from 1.26059 to 1.34877. Accordingly, the results demonstrated the SCA's robustness and consistency.

Table 4. ANOVA test results.

Source	SS	df	MS	F	<i>p</i> -Value > F
Columns	0.78479	2	0.3924	7.65	0.001
Error	4.36282	84	0.05194		
Total	5.14761	86			

**Figure 7.** ANOVA test results.

After identifying the best gains of the proposed PI^λ -based OF-INRT, the tracking performance of the SCA-based MPPT, i.e., SCA-MPPT, was examined and assessed by numerical MATLAB simulations under a changing temperature and load demand. The idea of changing the operating conditions was to investigate the tracking ability of the SCA-MPPT tracker. The scheme diagram of the system is presented in Figure 5. It includes one TEG module, DC–DC converter operating in a continuous conducted current mode with a switching frequency of 30 kHz, an input inductance of 1 mH, and an output capacitor of 47 μ F. The load value was 10 Ω . At a time of 0.6 s, an extra resistance of 10 Ω was added in parallel to the load. The cold side temperature of the TEG raised from 30 $^\circ$ C to 50 $^\circ$ C at a time of 0.3 s, whereas the hot side temperature was reduced from 300 $^\circ$ C to 250 $^\circ$ C at a time of 0.3 s and then returned to 300 $^\circ$ C at a time of 0.9 s.

To confirm the superiority of the optimized fractional SCA-MPPT controller, the tracking ability was compared with the classical INR and P&O techniques as shown in Figures 8–11. For the conventional INR approach, the gain of the discrete integrator was assumed to be 0.8. However, for the SCA-MPPT, the fractional PI^λ controller's parameters were 0.03765, 8.43451, and 1.01008 for the proportional gain, integral gain, and fractional-order coefficient, respectively, as summarized in Table 2. Figure 8 presents the TEG power for the three reported MPPT strategies with changing operating conditions, load, and temperature variations. Based on these conducted results, it can be noted that the SCA-MPPT reached the MPP of 14.6 W faster compared to the traditional INR and P&O MPPT techniques. The classical INR MPPT still needed more time to catch up to the MPP due to the slow dynamic response of the INR tracker. The fluctuations around the MPP were removed thanks to the SCA-based PI^λ compared with the basic P&O approach. At the time of 0.3 s, the temperature difference was reduced from 270 $^\circ$ C to 200 $^\circ$ C. Therefore, the maximum output power was reduced from 14.6 W to 9.4 W. At the time of 0.6 s, the load demand decreased from 10 Ω to 5 Ω . The SCA-MPPT rapidly came back to the MPP, whereas the P&O and INR required extra time to modify the duty cycle value to attain the MPP as presented in Figure 11. In addition, at the time of 0.9 s, the difference temperature increased from 200 to 250 $^\circ$ C. Hence, the output power increased from 9.4 W to 12.11 W. The tracking performance of the SCA-MPPT was better than those of the INR and P&O techniques. The detailed variations of the TEG current, TEG voltage, and PWM duty cycle are presented in Figures 9–11, respectively.

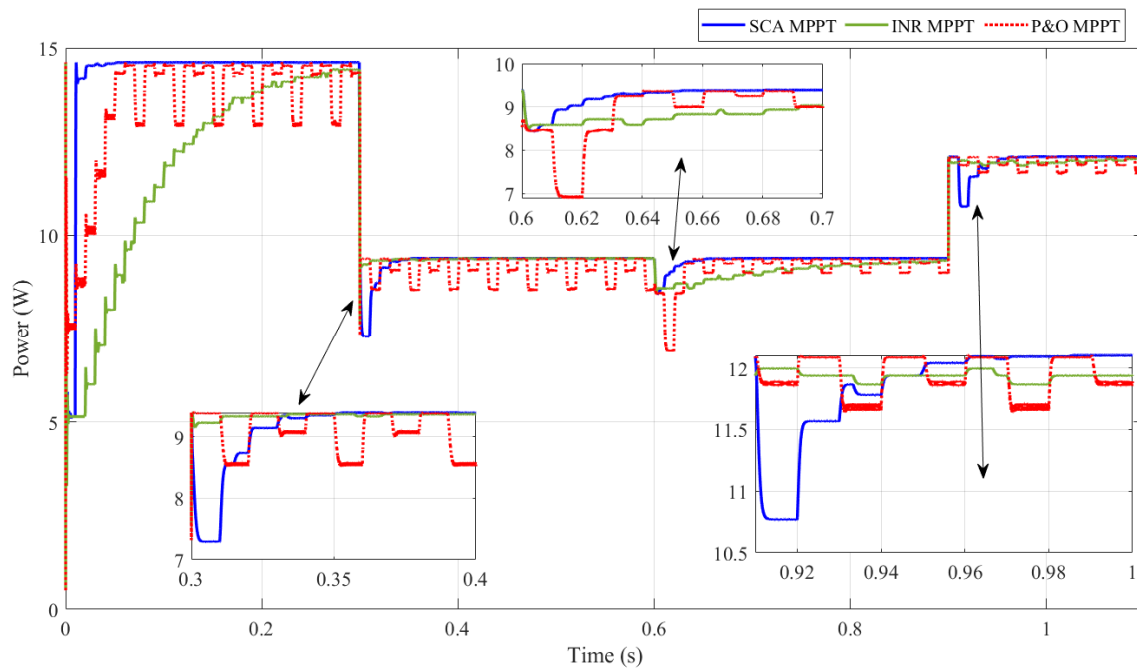


Figure 8. Detailed system performance with different MPPTs under load and temperature variation: TEG power.

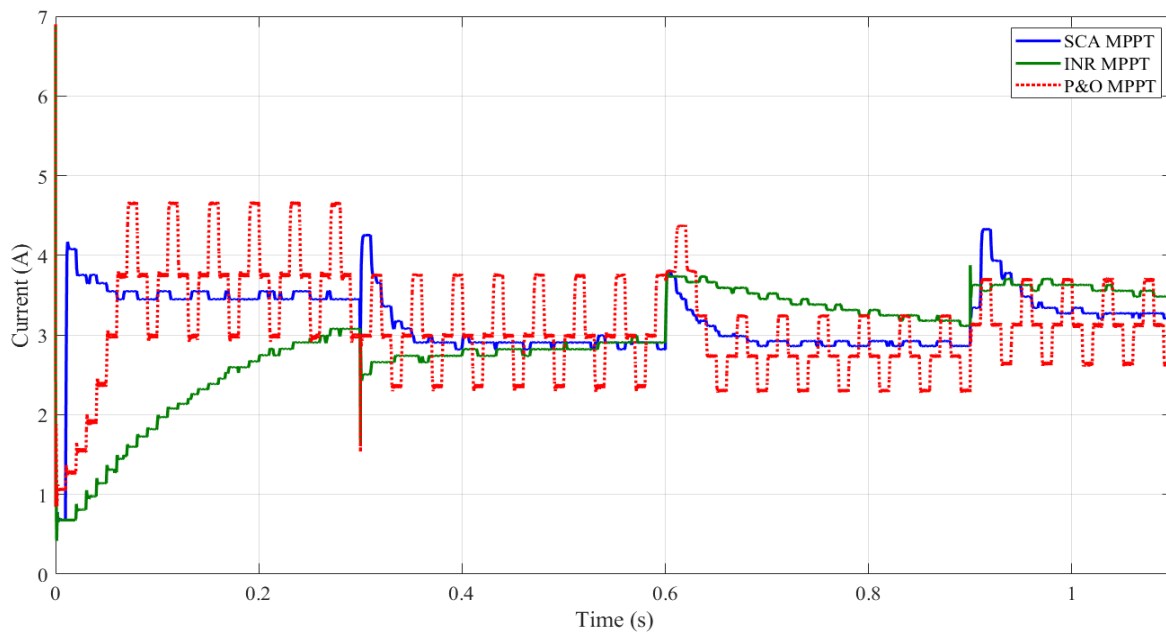


Figure 9. Detailed system performance with different MPPTs under load and temperature variation: TEG current.

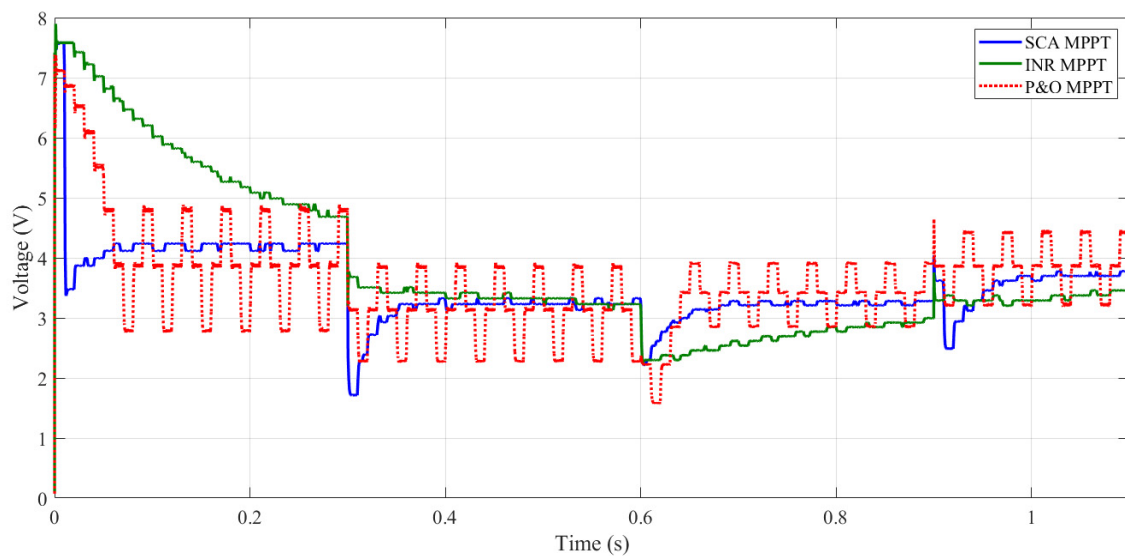


Figure 10. Detailed system performance with different MPPTs under load and temperature variation: TEG voltage.

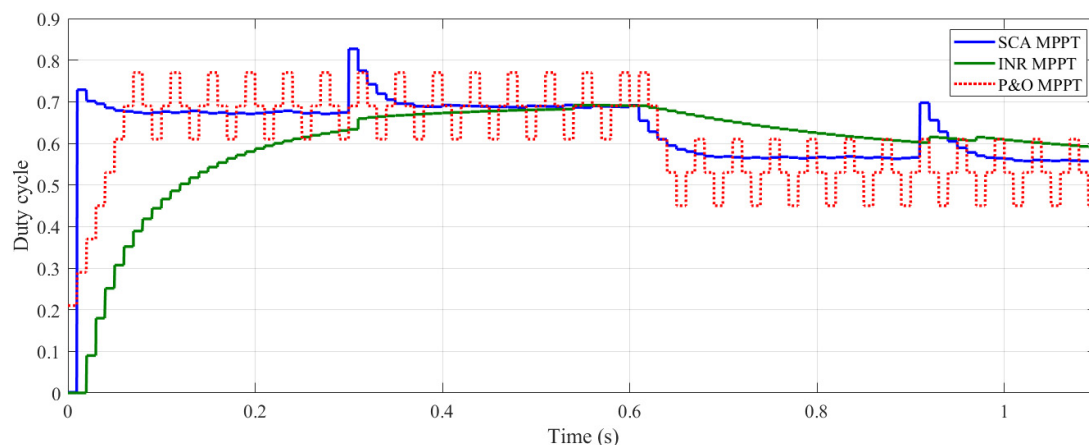


Figure 11. Detailed system performance with different MPPTs under load and temperature variation: PWM duty cycle.

7. Conclusions

To improve the dynamic response of the conventional incremental resistance (INR) MPPT approach and remove the steady-state variations of the P&O MPPT technique, in this paper, an Optimized Fractional INR Tracker (OF-INRT) was proposed based on an SCA-tuned PI^λ controller to rise the energy harvested from the thermoelectric generator (TEG). First, the best effective gains of the proposed OF-INRT were identified using a stochastic and parameter-free SCA. To demonstrate the superiority of the SCA optimizer, demonstrative results were carried out and compared with those obtained by the particle swarm optimization (PSO) and whale optimization algorithm (WOA)-based techniques. The results confirmed the superiority of the proposed SCA in terms of the fastness of the non-premature convergence and solution optimality. The average cost function values varied between 1.10599 W and 1.32868 W. The maximum value was achieved by the SCA tool. The STD values changed between 0.32349 and 0.00025. The minimum STD was also achieved by the SCA optimizer. Concerning the efficiency, the maximum efficiency of 96.56% has been achieved by SCA, whereas the lowest efficiency of 80.33% was attained by PSO. In sum, the optimized fractional MPPT method succeeded to increase the dynamic response and eliminate the steady-state oscillations compared with the incremental resistance (INR) and perturb and observe (P&O) MPPT methods, respectively.

A future works process should mainly include the real-world implementation and prototyping of the introduced SCA-MPPT strategy for the studied TEG using a dSPACE board associated with the MATLAB/Simulink software toolkit. The formulation of the fractional-order INRT design problem in an online optimization framework was also investigated.

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