



Supplementary: Tables

Table S1. Optimal Results under the Four Cases of Basic Model.

		Four cases			
Optimal		(C,C)	(C,L)	(L,C)	(L,L)
Results					
q_1		$\frac{2(a - \delta\xi - ts)}{9}$	$\frac{10a + 4tus - 14ts + 4\xi - 14\delta\xi}{45}$	$\frac{10a - 14\xi + 4\delta\xi + 4ts - 14tus}{45}$	$\frac{2(a - tus - \xi)}{9}$
π_{M_1}		$\frac{2(a - \delta\xi - st)^2}{27}$	$\frac{2(5a + 2\xi - 7\delta\xi - 7st + 2stu)^2}{675}$	$\frac{2(5a - 7\xi + 2\delta\xi + 2st - 7stu)^2}{675}$	$\frac{2(a - \xi - stu)^2}{27}$
q_2		$\frac{2(a - \delta\xi - ts)}{9}$	$\frac{10a + 4\delta\xi - 14\xi + 4ts - 14tus}{45}$	$\frac{10a + 4\xi - 14\delta\xi - 14ts + 4tus}{45}$	$\frac{2(a - \xi - tus)}{9}$
π_{M_2}		$\frac{2(a - \delta\xi - st)^2}{27}$	$\frac{2(5a - 7\xi + 2\delta\xi - 7stu + 2st)^2}{675}$	$\frac{2(5a + 2\xi - 7\delta\xi - 7st + 2stu)^2}{675}$	$\frac{2(a - \xi - stu)^2}{27}$
p		$\frac{5a + 4(\delta\xi + ts + c)}{9}$	$\frac{5a + 4c + 2(\delta\xi + \xi + ts + tus)}{9}$	$\frac{5a + 4c + 2(\delta\xi + \xi + ts + tus)}{9}$	$\frac{5a + 4(tus + c + \xi)}{9}$
π_{R_1}		$\left(\frac{2a - 2\delta\xi - 2ts}{9}\right)^2$	$\frac{4(5a - 7\delta\xi + 2\xi - 7st + 2stu)^2}{2025}$	$\frac{4(5a + 2\delta\xi - 7\xi - 7stu + 2st)^2}{2025}$	$\frac{4(a - \xi - stu)^2}{81}$
π_{R_2}		$\left(\frac{2a - 2\delta\xi - 2ts}{9}\right)^2$	$\frac{4(5a + 2\delta\xi - 7\xi + 2st - 7stu)^2}{2025}$	$\frac{4(5a - 7\delta\xi + 2\xi - 7st + 2stu)^2}{2025}$	$\frac{4(a - \xi - stu)^2}{81}$

Table S2. Optimal Results under the Four Cases of Imperfect Substitutes.

Optimal results	Four cases			
	(C,C)	(C,L)	(L,C)	(L,L)
q_1	$\frac{2(a-E)}{(b+2)(4-b)}$	$\frac{2(B+(8-b^2)E-2bF)}{(16-b^2)(b^2-4)}$	$\frac{2(B+(8-b^2)F-2bE)}{(16-b^2)(b^2-4)}$	$\frac{2(a-F)}{(b+2)(4-b)}$
π_{M_1}	$\frac{2(a-E)^2(2-b)}{(b+2)(b-4)^2}$	$\frac{2(B+(8-b^2)E-2bF)^2}{(b-4)^2(b+4)^2(4-b^2)}$	$\frac{2(B+(8-b^2)F-2bE)^2}{(b-4)^2(b+4)^2(4-b^2)}$	$\frac{2(a-F)^2(2-b)}{(b+2)(b-4)^2}$
q_2	$\frac{2(a-E)}{(b+2)(4-b)}$	$\frac{2(B+(8-b^2)F-2bE)}{(16-b^2)(b^2-4)}$	$\frac{2(B+(8-b^2)E-2bF)}{(16-b^2)(b^2-4)}$	$\frac{2(a-F)}{(b+2)(4-b)}$
π_{M_2}	$\frac{2(a-E)^2(2-b)}{(b+2)(b-4)^2}$	$\frac{2(B+(8-b^2)F-2bE)^2}{(b-4)^2(b+4)^2(4-b^2)}$	$\frac{2(B+(8-b^2)E-2bF)^2}{(b-4)^2(b+4)^2(4-b^2)}$	$\frac{2(a-F)^2(2-b)}{(b+2)(b-4)^2}$
p_1	$\frac{ab^2-6a-2(b+1)E}{(b+2)(b-4)}$	$\frac{(6-b^2)(2bF-G)-2E(3b^2-8)}{(b-4)(b+4)(b-2)(b+2)}$	$\frac{(6-b^2)(2bE-G)-2F(3b^2-8)}{(b-4)(b+4)(b-2)(b+2)}$	$\frac{ab^2-6a-2F(b+1)}{(b+2)(b-4)}$
p_2	$\frac{ab^2-6a-2(b+1)E}{(b+2)(b-4)}$	$\frac{(6-b^2)(2bE-G)-2F(3b^2-8)}{(b-4)(b+4)(b-2)(b+2)}$	$\frac{(6-b^2)(2bF-G)-2E(3b^2-8)}{(b-4)(b+4)(b-2)(b+2)}$	$\frac{ab^2-6a-2F(b+1)}{(b+2)(b-4)}$
π_{R_1}	$\frac{4(a-E)^2}{(b+2)^2(b-4)^2}$	$\frac{4(B+(8-b^2)E-2bF)^2}{(16-b^2)^2(b^2-4)^2}$	$\frac{4(B+(8-b^2)F-2bE)^2}{(16-b^2)^2(b^2-4)^2}$	$\frac{4(a-F)^2}{(b+2)^2(b-4)^2}$
π_{R_2}	$\frac{4(a-E)^2}{(b+2)^2(b-4)^2}$	$\frac{4(B+(8-b^2)F-2bE)^2}{(16-b^2)^2(b^2-4)^2}$	$\frac{4(B+(8-b^2)E-2bF)^2}{(16-b^2)^2(b^2-4)^2}$	$\frac{4(a-F)^2}{(b+2)^2(b-4)^2}$

Note: $B = ab^2 + 2ab - 8a$, $E = \delta\xi + st$, $F = \xi + st\beta$, $G = ab^2 + 2ab - 8$.

Table S3. Optimal Results under the Four Cases of Price Game.

Optimal results	Four cases			
	(C,C)	(C,L)	(L,C)	(L,L)
p_1	$\frac{D(2a + \delta\xi + st) + 2a}{(2-d)N}$	$\frac{R_1^1 st + R_1^2 \xi + aR_1^3}{MN(2-d)(d+2)}$	$\frac{R_2^1 st + R_2^2 \xi + R_2^3 a}{MN(2-d)(2+d)}$	$\frac{D(\xi + \beta st) + 2a(3-d^2)}{(2-d)N}$
π_{M_1}	$\frac{D(d+2)(a+(\delta\xi+st)(d-1))^2}{(2-d)N^2}$	$\frac{D(B_1^1 st + B_1^2 \xi + B_1^3 a)^2}{M^2 N^2 (2-d)(d+2)}$	$\frac{R_2^1 st + R_2^2 \xi + R_2^3 a}{MN(2-d)(2+d)}$	$\frac{D((\xi+st)(d-1)+a)^2 (d+2)}{(2-d)N^2}$
p_2	$\frac{D(2a + \delta\xi + st) + 2a}{(2-d)N}$	$\frac{R_2^1 st + R_2^2 \xi + R_2^3 a}{MN(2-d)(2+d)}$	$\frac{R_1^1 st + R_1^2 \xi + aR_1^3}{MN(2-d)(2+d)}$	$\frac{D(\xi + \beta st) + 2a(3-d^2)}{(2-d)N}$
π_{M_2}	$\frac{D(d+2)(a+(\delta\xi+st)(d-1))^2}{(2-d)N^2}$	$\frac{(B_2^1 st + B_2^2 \xi + aB_2^3)^2 D}{M^2 N^2 (2-d)(d+2)}$	$\frac{D(B_1^1 st + B_1^2 \xi + B_1^3 a)^2}{M^2 N^2 (2-d)(d+2)}$	$\frac{D((\xi+st)(d-1)+a)^2 (d+2)}{(2-d)N^2}$
π_{R_1}	$\frac{D^2((d-1)(\delta\xi+st)+a)^2}{(2-d)^2 N^2}$	$\frac{D^2((\beta st+\xi)(d-1)+a)^2}{(d-2)^2 N^2}$	$\frac{D^2((\beta st+\xi)(d-1)+a)^2}{(2-d)^2 M^2}$	$\frac{D^2(a+(d-1)(\xi+\beta st))^2}{(2-d)^2 N^2}$
π_{R_2}	$\frac{D^2((st+\delta\xi)(d-1)+a)^2}{(2-d)^2 N^2}$	$\frac{D^2((\beta st+\xi)(d-1)+a)^2}{(2-d)^2 M^2}$	$\frac{D^2((\beta st+\xi)(d-1)+a)^2}{(2-d)^2 N^2}$	$\frac{D^2(a+(d-1)(\xi+\beta st))^2}{(2-d)^2 N^2}$

Note: $M = 4 - 2d^2 + d$, $N = 4 - 2d^2 - d$, $D = 2 - d^2$, $H_1^1 = d\beta(2-d^2) + (2d^4 - 8d^2 + 8)$, $H_1^2 = (2d^4 - 8d^2 + 8)\delta + d(2-d^2)$,

$$H_1^3 = (4d+3)(2-d^2) + 2(1+d), \quad H_2^1 = 2d - d^3 - 8d^2\beta + 2d^4\beta + 8\beta, \quad H_2^2 = 2d\delta - d^3\delta + 2d^4 - 8d^2 + 8, \quad H_2^3 = 8 - 2d^3 - 3d^2 + 6d,$$

$$R_1^1 = 2d^5\beta - 10d^3\beta + 12d\beta + 3d^4 - 14d^2 + 16, \quad R_1^2 = (2d^5 - 10d^3 + 12d) + (3\delta d^4 - 14\delta d^2 + 16\delta),$$

$$R_1^3 = (d^4 - 6d^2 + 9)4d - 6d^2 + 16 + 2(3d^4 - 14d^2 + 16), \quad R_2^1 = 2d(d^4 - 5d^2 + 6) + (3d^4 - 14d^2 + 16)\beta,$$

$$R_2^2 = (3d^4 - 14d^2 + 16) + (d^4 - 5d^2 + 6)2d\delta, \quad R_2^3 = 4d^5 - 24d^3 + 36d + 6d^4 - 34d^2 + 48, \quad B_1^1 = (2d^4 - 9d^2 + 8) + d\beta(d^2 - 2),$$

$$B_1^2 = 2d^4\delta - 9d^2\delta + 8\delta + d^3 - 2d, \quad B_1^3 = 2d^3 + 3d^2 - 6d - 8, \quad B_2^1 = 2d^4\beta - 9d^2\beta + 8\beta + d^3 - 2d, \quad B_2^2 = 2d^4 - 9d^2 + 8 + d^2d\delta - 2d\delta,$$

$$B_2^3 = 2d^3 + 3d^2 - 6d - 8.$$