



Article Geological Strength Index Relationships with the Q-System and Q-Slope

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Abstract: The Q-system and Q-slope are empirical methods developed for classifying and assessing rock masses for tunneling, underground mining, and rock slope engineering. Both methods have been used extensively to guide appropriate ground support design for underground excavations and stable angles for rock slopes. Using datasets obtained from igneous, sedimentary, and metamorphic rock slopes from various regions worldwide, this research investigates different relationships between the geological strength index (GSI) and the Q-system and Q-slope. It also presents relationships between chart-derived GSI with GSI estimations from RMR89 and Q' during drill core logging or traverse mapping. Statistical analysis was used to assess the reliability of the suggested correlations to determine the validity of the produced equations. The research demonstrated that the proposed equations provide appropriate values for the root mean squared error value (RMSE), the mean absolute percentage error (MAPE), the mean absolute error (MAE), and the coefficient of determination (R-squared). These relationships provide appropriate regression coefficients, and it was identified that correlations were stronger when considering metamorphic rocks rather than other rocks. Moreover, considering all rock types together, achieved correlations are remarkable.

Keywords: rock mass classification; Q-system; Q-slope; geological strength index (GSI)



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1. Introduction

Rock masses can be described as a complex combination of intact rock material separated by geological discontinuities, including joints, bedding planes, veins, shears, and faults. It is practically impossible to identify and characterize every single intact block and discontinuity in a rock mass with respect to the engineering scale of projects (e.g., in tunnels, slopes, and mines).

Rock mass classification systems are a process of grouping or classifying a rock mass based on defined relationships [1] and assigning it a unique description (and number) based on similar geomechanical properties or characteristics so that its behavior may be predicted. Rock mass classifications and design charts are particularly useful for providing:

- Assessment of ground conditions by converting engineering geological descriptions to "numbers" which can be used for engineering purposes;
- Fast prediction of underground excavation and slope performance;
- Guidance on support requirements and stable slope geometry.

The boundaries of the structural zones are typically defined by a significant structural element, such as a fault or a change in the type of rock. Within the same rock type, there may be instances where significant variations in discontinuity spacing or features call for the partitioning of the rock mass into a number of tiny structural sections.

Empirical methods, including rock mass classifications, are most effective when the geometry, geology, hydrogeology, and geomechanical characteristics of the engineering problem (underground excavations, slopes, etc.) under investigation are similar to the

known performance of precedent engineering problems [2]. An excavation will be usable for a certain amount of time without support; after that, major caving and failure may happen [3]. The only basis for empirical design is experience or observation; it is not based on any theory or method of science. Its use in engineering design focuses on comparing the outcomes of prior trials to project future behavior based on the most crucial components of the design.

The design process using rock mass classification (Q-slope for rock slopes) and calculation of the rock mass behavior (using the geological strength index and the Hoek–Brown failure criterion) is shown in Figure 1 [4]. As shown, to design the slope's angle, rock mass classification must be provided by using the Q-slope method, which needs field investigations, and describing block size, roughness, and project factors. In terms of rock mass characterization, the well-known method is the geological strength index introduced by Hoek–Brown. The necessary parameters to analyze the stability of slope in this method are friction, cohesion and uniaxial compressive strength of intact rock.

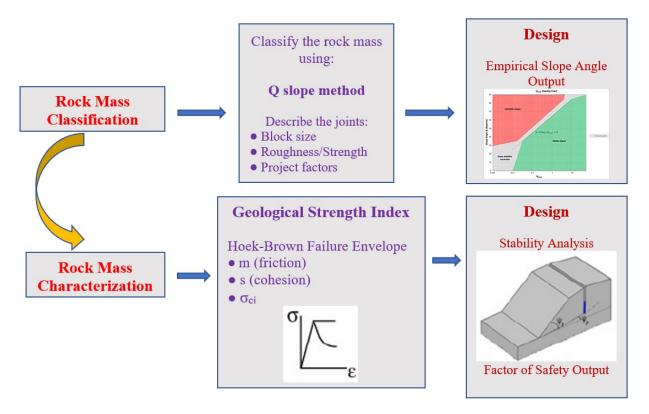


Figure 1. Rock mass characterization vs. Classification for rock slopes [4].

In the engineering design of rock slopes, it is assumed that all four input parameters (GSI, m, s, and σ_{ci}) may be represented by normal distributions. The standard deviations given to these four distributions are based on geotechnical program experience for significant civil and mining projects where sufficient funding is available for high-quality studies [5].

Rock mass behavior is mainly characterized by strength and deformation modulus of rock mass. In order to provide a good estimation of rock mass behavior, geological strength index plays an important role. Providing accurate values, the error in designing rock slope stability would be minimized and lead to realistic safety factor, as discussed by Ván and Vásárhelyi [6]. They analyzed the sensitivity of GSI-based equations and discovered that relationships are extremely reliant on the input parameters and that changing one parameter by 5% could significantly impact the outcomes. The well-known practical GSI chart provided by Hoek–Brown and non-linear failure criteria can be used for further design as shown in Figure 2.

Generalised HOEX-BROWN CRITERION $\sigma_1^* = \sigma_3^* + \sigma_r \left(m_h^* \frac{\sigma_3^*}{\sigma_c} + s \right)^{\prime \prime \prime}$ $\sigma_1^* = major principal effective stress at failure \sigma_3^* = minor principal effective stress at failure \sigma_6 = uriaxial compressive strength of inteel pieces of rock m_b, s and a are constants which depend on the composition, structure and surface conditions of the rock mass STRUCTURE$		SURFACE CONDITION	VERY GOOD Very rough, unweathered surfaces	GOOD Rough, sightly weathered, iron stained surfaces	FAIR Smooth, moderately weathered or altered surfaces	POOR Sickensided, highly weathered surfaces with compact coachings or fillings containing angular rock fragments	VERY POOR Sickensided, highly weathered surfaces with soft clay coatings or fillings	Rock Mass Characterization	Design Stability Analysis		
	BLOCKY -very well interlocked undisturbed rock mass consisting of cubical blocks formed by three orthogonal discontinuity sets	m,/m, s e_ GSI	0.60 0.190 0.5 75,000 0.2 85	0.40 0.062 0.5 40,000 0.2 75	0.26 0.015 0.5 20,000 0.25 62	0.16 0.003 0.5 9,000 0.25 48	0.08 0.0004 0.5 3,000 0.25 34	9	Factor of Safety Output		
	VERY BLOCKY-interlocked, partially disturbed rock mass with multifaceted angular blocks formad by four or more discontinuity sets	m,/m s E_ GSI	0.40 0.062 0.5 40,000 0.2 75	0.29 0.021 0.5 24,000 0.25 65	0.16 0.003 0.5 9,000 0.25 48	0.11 0.001 0.5 5,000 0.25 38	0.07 0 0.53 2,500 0.3 25		K		
	BLOCKV/SEAMY-folded and faulted with many intersecting discontinuities forming angular blocks	m_/m s a E_ v GSI	0.24 0.012 0.5 18,000 0.25 60	0.17 0.004 0.5 10,000 0.25 50	0.12 0.001 0.5 6,000 0.25 40	0.08 0 0.5 3.000 0.3 30	0.06 0 0.55 2,000 0.3 20		9 20 170m		
	CRUSHED-poorly interlocked, heavity broken rock mass with a mixture of angular and rounded blocks	m,/m s a E ≈ v GSI	0.17 0.004 0.5 10,000 0.25 50	0.12 0.001 0.5 6,000 0.25 40	0.08 0 0.5 3,000 0.3 30	0.06 0 0.55 2.000 0.3 20	0.04 0 0.60 1,000 0.3 10				

Figure 2. Estimation of constants m_b/m_i , s, a, deformation modulus E, and the Poisson's ratio (ν) for the generalized Hoek–Brown failure criterion based upon rock mass structure and discontinuity surface conditions used for the design stage [4].

Furthermore, several researchers established, improved, and updated several rock mass rating methods for tunnel support design. These classification systems also have applications in diverse engineering projects including rock slopes [7–12].

Santos et al. [13] showed using machine learning techniques that it is possible to achieve an accurate RMR classification system using only factors that are directly connected to rock mass quality rather than all RMR variables.

2. Rock Mass Classification System

The most commonly used rock mass classifications include rock mass rating (RMR)₈₉ [1], rock mass quality (Q-system) [14] and geological strength index (GSI) [15]. Since its relatively recent introduction, the Q-slope method for rock slope engineering [16] has also become commonly used for slope stability appraisals. With the use of Q-slope, engineering geologists and rock engineers can evaluate the stability of rock slopes that have been excavated in the field and possibly change the slope angles when the condition of the rock mass becomes clear during construction. The correlation between the geological strength index (GSI) and the rock mass rate was also recently analyzed by Somodi et al. [17].

RMR₈₉ and Q are empirical methods that directly guide underground excavation support requirements. Similarly, Q-slope provides direct guidance for long-term stable slope angles. These methods have been used by visually assessing tunnel and slope faces, as well as for the characterization of drill core. The GSI system on the other hand, is an input parameter to the Hoek–Brown failure criterion [18].

Hoek and Brown [19] expanded their intact rock failure criterion for applicability to homogeneous and isotropic rock masses under the assumption that the same type of non-linear envelopes continued to be valid. Rock mass rating, RMR₇₆, and modified rock mass quality, Q', were initially utilized to downgrade intact rock to rock mass strength in the Hoek–Brown failure criterion [20].

2.1. Geological Strength Index (GSI)

Unless a rock mass failure criterion could be connected to a geological description that engineering geologists could make quickly, it would be of no practical use. The geological strength index (GSI) is a system for classifying rocks that was created in the field of rock engineering to address the requirement for accurate estimation of the attributes of rocks for the design of engineering projects [15]. The foundation of the GSI system is an in-depth engineering geology description of the rock mass encountered in engineering projects. Structure and the condition of discontinuities in the rock mass, which can be determined through visual inspection of the rock mass exposed in outcrops, are two essential criteria that determine the value of the GSI [21]. The basic GSI chart's use entails some subjectivity because there are not any quantifiable or more representative metrics, linked interval limits, or ratings for describing the rock structure and surface conditions of the discontinuities. In order to make the method easier to use, particularly for new engineers, numerous publications [18,22,23] presented quantitative GSI charts to quantify the estimation of GSI. In circumstances when there are only one or two sets of discontinuities, the GSI should not be utilized. Instead, it should only be employed when the rock mass is intact or heavily joined. When working with blocky rock masses that have minimum anisotropy, extreme caution should be used. However, it is occasionally reasonable to assign the GSI to the entire rock mass and include the single discontinuity as a layer element in the numerical model for a rock mass that has a single well-defined discontinuity [20]. According to the definition of GSI and subsequent application, it is independent of the water inflow and the in situ stress state. As mentioned, GSI has limits, as do any categorization systems, including the differences in the results of individuals. Others have suggested that the generic GSI may not appropriately reflect the size of the rock mass problem because its parameters, particularly RQD and J_{Cond}, are scale-dependent [24,25].

The two main geological elements behind GSI were the surface conditions of discontinuities and their shear strength, as well as the rock mass structure, which represented the degree of fracture [26]. GSI subsequently replaced RMR in the Hoek–Brown failure criterion. To encourage early adoption, Hoek et al. [15,27] provided the following relationships for estimating GSI, termed GSI_{calc} in this paper from RMR and Q':

$$GSI_{calc} = RMR_{89} - 5 \tag{1}$$

for RMR₈₉ \geq 23

$$GSI_{calc} = 9lnQ' + 44 \tag{2}$$

for $RMR_{89} < 23$

GSI was developed to assess tunnel and slope faces using charts (Figure 3) and cannot be estimated directly from the characterization of the drill core. Equations (1) and (2) also enable the estimation of GSI_{calc} from the drill core.

Hoek et al. [19] suggested quantifying the GSI chart as a function of RQD and the joint condition parameters presented by either [1]: $JCond_{89}$ from RMR₈₉ or Barton et al. [14]; J_r and J_a from Q and Q-slope, on the premise that professionals with less expertise and who are "less at ease with the qualitative descriptions" may utilize this new GSI chart. The suggested equations included [18]:

$$GSI_{2013} = 1.5JCond_{89} + RQD/2$$
 (3)

$$GSI2013 = \frac{52J_r/J_a}{\left(1 + \frac{J_r}{J_a}\right)} + RQD/2$$
(4)

Vásárhelyi et al. [28] and Somodi et al. [29] discovered that visual observation by an expert engineering geologist is the best technique to estimate GSI, compared to the computational and estimation methods examined. Moreover, Deák et al. [30] and Somodi et al. [31] analyzed the relationship between the parameters of the Q-system and the GSI value and the equations are suggested based on the empirical results of different rock engineering projects in Hungary and Australia.

Bertuzzi et al. [32] observed a decent connection between the GSI values derived by the chart (GSI_{chart}) and the GSI quantified (GSI₂₀₁₃) using the Hoek et al. [18] technique (Figure 3). Santa et al. [33] compared the differences between the latest edition of GSI₂₀₁₃ and the prior version (GSI₉₈) in an anisotropic media. They discovered that the 2013 version [18] allocated lower GSI ratings to rock masses with lesser quality and higher values to rock masses with greater quality. Winn et al. [34] revealed that the three alternative techniques proposed by [22,23] for a sedimentary rock mass in a Singapore dive, a variety of outcomes comparable to the field-assessed qualitative GSI, showing their good performance. However, Winn et al. [34] established a new GSI relationship by replacing RQD/2 with RQD/3 in the calculation of GSI₂₀₁₃, which provided substantially higher GSI values that did not correspond to the qualitative field values.

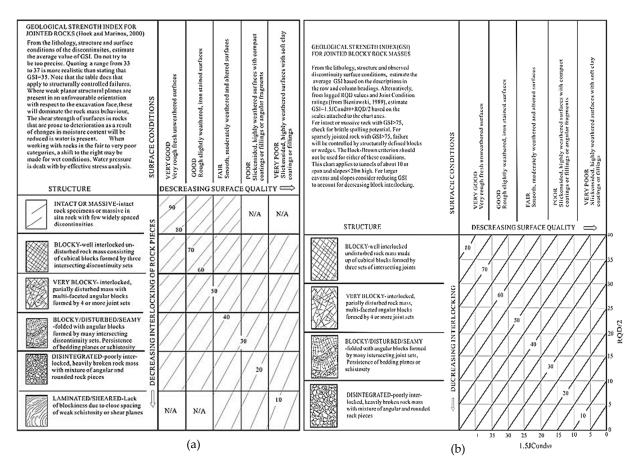


Figure 3. (a) GSI chart for jointed rocks [35]. (b) Quantification of GSI through joint conditions and RQD [18].

Yang and Elmo [36] argue against the quantification paradigm for GSI determination without taking into account the constraints of the idea that GSI quantification approaches may convert subjectivity into objectivity since the parameters under consideration are not quantitative measurements.

2.2. The Q-Slope Method

Barton and Bar [37] are credited with developing the Q-slope, an empirical engineering method for assessing the stability of rock slopes that allows for immediate access to stability with few presumptions. It is descended from the Q-system, which has been used globally for over 40 years to characterize rock exposures, drill core, and tunnels that are under construction [14,38]. Q-slope allows engineering geologists and rock engineers to analyze the stability of excavated rock slopes in the field and make prospective slope angle adjustments as rock mass conditions become obvious during construction [37,39]. The Q_{slope} used Q system components to slope stability assessments are calculated using the expression [16]:

$$Q_{\text{slope}} = \frac{\text{RQD}}{J_{\text{n}}} \times \left(\frac{J_{\text{r}}}{J_{\text{a}}}\right)_{\text{O}} \times \frac{J_{\text{wice}}}{\text{SRF}_{\text{slope}}}$$
(5)

RQD, J_n , J_r , and J_a are the same four parameters used in Q-system. On the other hand, the frictional resistance pair Jr and Ja as necessary, each side of a wedge that may be unstable will receive this treatment. If suitable, simple orientation variables such as $(J_r/J_a)_O$ give an estimate of the reduction in overall whole-wedge frictional resistance. The term J_w , which has now been modified to J_{wice} , refers to a broader range of environmental conditions ideal for rock slopes exposed to the elements for a long time. Extremes of erosive rains and ice wedging, which can occur periodically at opposing extremities of the rock-type and regional spectrum, are examples of these situations. Slope-relevant SRF classifications are also available in slope surface conditions, stress–strength ratios and major discontinuities such as faults, weakness zones or joint swarms [37].

Q' and Q-slope' are estimated using Equations (6) and (7), which merely remove the water, environment, stress, and strength reduction factors from the full Q-system and Q-slope equations:

$$Q' = \left(\frac{RQD}{J_n}\right) \times \left(\frac{J_r}{J_a}\right) \tag{6}$$

$$Q\text{-slope}' = \left(\frac{RQD}{J_n}\right) \times \left(\frac{J_r}{J_a}\right)_A \times \left(\frac{J_r}{J_a}\right)_B \text{ where applicable}$$
(7)

where RQD = rock quality designation (%).

- J_n = joint set number.
- J_r = joint roughness number.
- J_a = joint alteration number.

Q-system and Q-slope ratings for RQD, J_n , J_r , and J_a are described by Barton et al. [14] and Bar and Barton [16]. These parameters are commensurate with the primary factors in GSI: rock mass structure and discontinuity surface conditions.

The main distinction between Q and Q-slope is that Q uses J_r/J_a from the collection of discontinuities with the least favorable discontinuities. In contrast, J_r/J_a for both sides (A and B) of the wedge can be considered necessary when wedges are encountered while utilizing Q-slope. In order to predict various parameters from others in material sciences and engineering properties of various rock types from their petrographic characteristics in engineering geology and rock mechanics, several researchers have attempted to construct various soft computing models [40–43]. Recent research has examined the relationships between the Q-system, Q-slope, and GSI as well as for other rocks by employing statistical analyses and various soft computing techniques such as root mean squared error value (RMSE), the mean absolute percentage error (MAPE), mean absolute error (MAE), and coefficient of determination (R-squared).

3. Study Area

The current study reviews over 192 case records collected from across 11 countries on five continents to investigate the relationship between the GSI obtained using the popular chart methods in more depth. (GSI_{chart}) and its correlation with Q' and Q-slope'.

The case records were obtained from rock slope faces that were assessed during the Q-slope method development [16] from a range of mining commodities, including gold, copper, iron ore, coal, and diamonds, and civil engineering applications, including roads, highways, and quarries. GSI was estimated for these case studies using GSI chart for jointed rocks (GSI_{chart}). Figure 4 graphically illustrates the results from a selection of case

studies. The case records include over 20 different rock types in vastly different engineering geological, environmental, and climatic settings:

- Igneous rocks include andesite, basalt, diorite, granite, kimberlite, monzodiorite, rhyolite, and tuff.
- Sedimentary rocks include chert, greywacke, limestone, mudstone, siltstone, sandstone, and banded iron formation.
- Metamorphic rocks include marble, metasandstone, phyllite, quartzite, schist, and shale. Figure 5 presents a selection of photographs of rock slopes hosted within vastly

different rock masses and their respective GSI, Q-slope, and Q-slope' ratings for context:

- Case records A and B are both granites. A is massive whilst B is blocky.
- Case records C, D, and E are all siltstones, which are blocky, seamy, and very blocky, respectively. Joint surface quality reduces from very good to good in C and E to fair in F.
- Case record F is a sheared mudstone comprising claystones and siltstones with slickensided, graphitic infilling along bedding planes and bedding shears.
- Case records B and C have the same GSI, but vastly different Q-slope values, due to the orientation of the discontinuities.
- Case records D and E have different GSI and Q-slope' values, but very similar Q-slope values. Both are stable slopes with bench face angles of approximately 65°.

Data analysis was conducted using SPSS23 software to outline the relations between parameters and describe the frequency distribution of GSI values [44]. Three rock types were picked and tested independently, and reliability analyses were also made. Figure 6 indicates the frequency distribution of GSI values, and Table 1 indicates the statistical analysis of the data for all the rocks and each type of rocks separately. According to Table 1, GSI values range between 20 and 90 for all the rock types, indicating that our datasets include very good through very poor rock mass.

Table 1. Statistical analysis of measured GSI values.

	Number of Estimates	Median	Minimum	Maximum
Igneous	26	65	27	89
Sedimentary	139	55	20	85
Metamorphic	27	60	30	90
Total	192	55	20	90

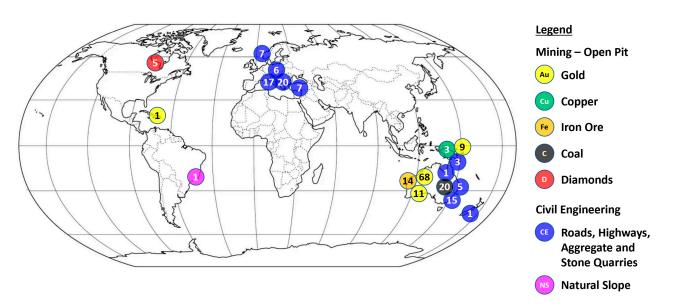


Figure 4. Case records: geographic location and industry and commodity. (The numbers indicate the locations of sampling).

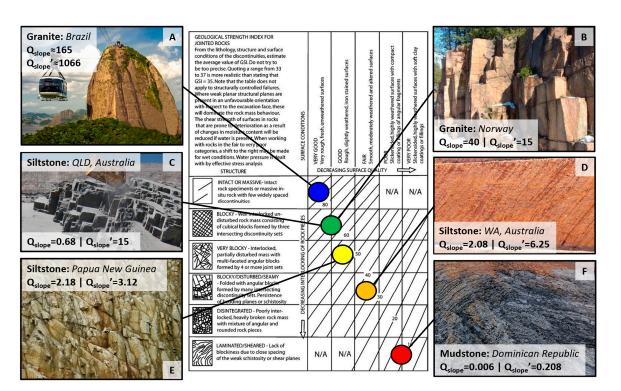


Figure 5. Selection of case studies comparing GSI, Q-slope, and Q-slope'.

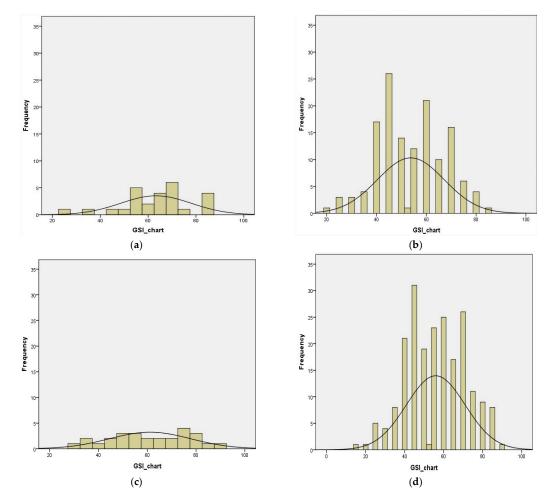


Figure 6. Histogram of measured GSI for (a) igneous rocks, (b) sedimentary rocks, (c) metamorphic rocks, and (d) all the rock types.

4.1. Correlation between GSI and Q'

The Q' values were calculated by using Equation (6) and correlated to the GSI_{chart} . These results are summarized in Figure 7. Figure 7a shows the correlation for three types of rocks (igneous, sedimentary, and metamorphic) separately, and Figure 7b shows the correlation for all rocks together. The more reliable correlation relates to metamorphic rocks ($R^2 = 79\%$). Also, for all cases, the best fitting is in logarithmic. These relationships have similarities with Equation (2).

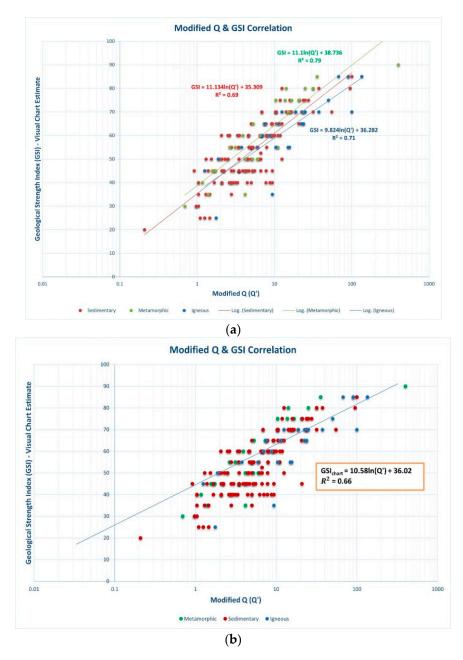
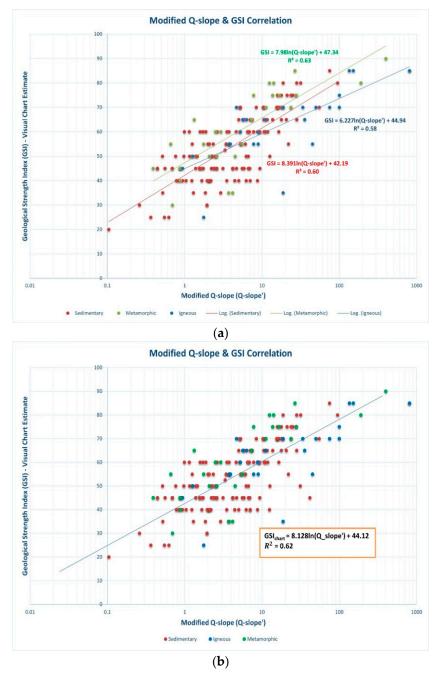


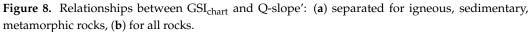
Figure 7. Relationships between GSI_{chart} and Q': (**a**) separated for igneous, sedimentary, metamorphic rocks, (**b**) for all rocks.

4.2. Correlation between GSI and Q-Slope'

In addition, using Equation (7), the Q-slope' values were calculated and correlated to the GSI_{chart}. Figure 8 summarizes these findings. Figure 8a shows the correlation for three different types of rocks (igneous, sedimentary, metamorphic), while Figure 8b shows the

correlation for all rocks combined. The more reliable correlation is with metamorphic rocks ($R^2 = 63\%$). Also, in all cases, the best fitting is logarithmic. These relationships also have similarities with Equation (2).





4.3. Correlation between GSI_{chart} and GSI₂₀₁₃

Furthermore, Equation (3) was used to produce the GSI_{2013} values, which were then compared with GSI_{chart} . Figure 9 summarizes the findings. Figure 9a depicts the correlation for three different types of rocks (igneous, sedimentary, metamorphic), while Figure 9b depicts the correlation for all rocks. Metamorphic rocks have a more reliable correlation ($R^2 = 88\%$). In addition, the optimal fitting is linear in all circumstances.

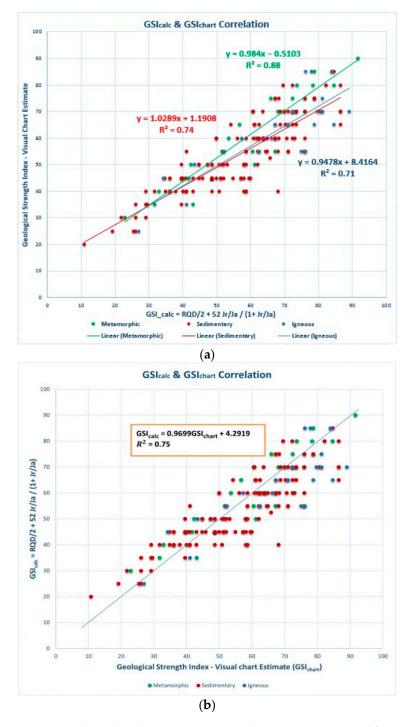


Figure 9. Relationships between GSI_{chart} and GSI₂₀₁₃: (**a**) separated for igneous, sedimentary, metamorphic rocks, (**b**) for all rocks.

5. Key Findings

Several different relationships between GSI (GSI_{chart}) and Q' and Q-slope' have been identified using over 200 new case records. The relationship between the GSI value and the Q value is:

$$GSI = A \ln(Q) + B, \tag{8}$$

where A and B are material constants, depending on the rock type [30].

• For Q': A and B values range from 9.82 to 11.13 and from 35.31 to 38.74, respectively.

• For Q-slope': A and B values range from 6.23 to 8.39 and from 42.19 to 47.34, respectively.

All derived relationships are summarized in Table 2.

Table 2. Empirical equations derived in this study.

Types of Correlation	Equation	R ²
GSI _{chart} & Q' for Metamorphic rocks	GSI = 11.10ln(Q') + 38.74	0.79
GSI _{chart} & Q' for Sedimentary rocks	GSI = 11.13ln(Q') + 35.31	0.69
GSI _{chart} & Q' for Igneous rocks	GSI = 9.82ln(Q') + 36.28	0.71
GSI _{chart} & Q' for all rocks	GSI = 10.58ln(Q') + 36.02	0.66
GSI _{chart} & Q-slope' for Metamorphic rocks	GSI = 7.98ln(Q-slope') + 47.34	0.63
GSI _{chart} & Q-slope' for Sedimentary rocks	GSI = 8.39ln(Q-slope') + 42.19	0.60
GSI _{chart} & Q-slope' for Igneous rocks	GSI = 6.23ln(Q-slope') + 44.94	0.58
GSI _{chart} & Q-slope' for all rocks	GSI = 8.13ln(Q-slope') + 44.12	0.62
GSI _{chart} & GSI ₂₀₁₃ for Metamorphic rocks	$GSI_{2013} = 0.98(GSI_{chart}) - 0.51$	0.88
GSI _{chart} & GSI ₂₀₁₃ for Sedimentary rocks	$GSI_{2013} = 1.03(GSI_{chart}) + 1.19$	0.74
GSI _{chart} & GSI ₂₀₁₃ for Igneous rocks	$GSI_{2013} = 0.95(GSI_{chart}) + 8.41$	0.71
GSI _{chart} & GSI ₂₀₁₃ for all rocks	$GSI_{2013} = 0.97(GSI_{chart}) + 4.29$	0.75

6. Quantitative Relationships and Errors

Four common statistical metrics, including determination coefficient (\mathbb{R}^2), root mean square error ($\mathbb{R}MSE$), mean absolute error ($\mathbb{M}AE$), and mean absolute percent error ($\mathbb{M}APE$), were used to assess the statistical efficiency of the GSI_{chart} prediction in the training and testing sets [45]. Equations (9)–(11) specify the following performance measures:

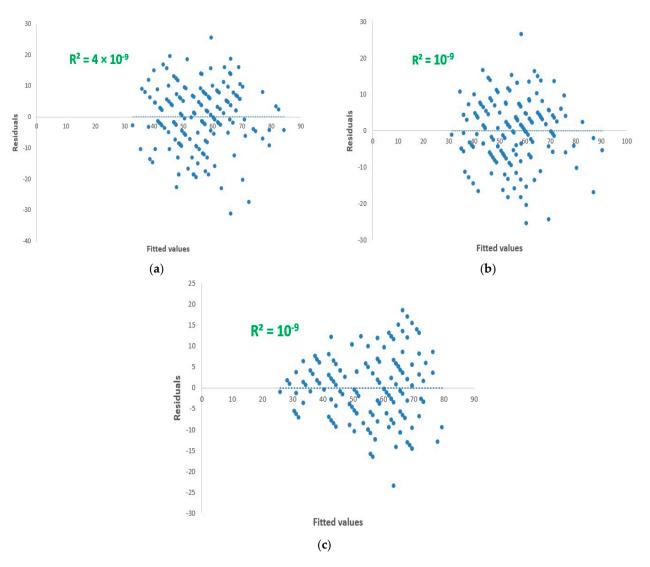
$$RMSE = \sqrt{\frac{\sum_{i=1}^{n} (pi - qi)^2}{n}}$$
(9)

$$MAPE = \frac{1}{n} \sum_{i=1}^{n} \left| \frac{qi - pi}{qi} \right| \times 100$$
(10)

$$MAE = \frac{\sum_{i=1}^{n} |pi - qi|}{n}$$
(11)

Here, p_i and q_i stand in for the i_{th} predicted and expected results, respectively, and n denotes the total number of experiments. Since significant errors are dealt with far more successfully than smaller ones, RMSE is a widely used metric. When the RMSE approaches 0, it means that the prediction error was minimal. However, it does not always guarantee top performance. Additionally, MAE was calculated and is incredibly helpful when data are smooth and continuous [46].

Plotting the residuals vs. the fitted values of the dependent variable allows one to assess the error of the proposed model. The residuals are the discrepancies between the experimental outcomes and the values that the suggested model predicted. The values that



have been fitted are those that the proposed model anticipated. Figure 10 illustrates the residuals' balanced and symmetrical dispersion about the horizontal axis.

Figure 10. Distribution of the residuals against fitted values: (**a**) between GSI_{chart} and Q-slope', (**b**) GSI_{chart} and Q', (**c**) GSI_{chart} and GSI_{calc}.

Additionally, the residuals' outermost points resemble a circular in shape. The residuals' independent nature and random distribution around the centerline are confirmed by this distribution [47,48]. To make sure of this, the determination coefficient, R-squared, is computed. It turns out to be very nearly equivalent to zero. In other words, the residuals are not dependent on one another. The proposed model's goodness of fit is therefore excellent.

The calculations: These new statistical indicators that provide quantitative connections between GSI_{chart} and Q' and Q-slope', as well as GSI_{2013} , are given in Table 3.

Table 3. Statistical indicators for Q-slope' vs. GSI_{chart}, Q' vs. GSI_{chart}, and GSI_{calc} vs. GSI_{chart} models.

Statistical Metrics	Q-Slope' ve	5. GSI _{chart}	Q' vs. G	SSI _{chart}	GSI _{calc} vs. GSI _{chart}	
	Training	Testing	Training	Testing	Training	Testing
RMSE	9.93	10.8	8.5	9.56	7.47	7.85
MAPE	0.16	0.18	0.13	0.16	0.11	0.11
MAE	7.87	8.5	6.69	7.8	5.95	5.9

7. Conclusions

The relationships between the geological strength index (GSI) and the Q-system and Q-slope are explored in this paper. Quantitative correlation analyses have been carried out systematically using study data from various igneous, metamorphic, and sedimentary rocks.

Validated results show that the proposed simplified quantitative correlations accurately reflect the observed relationship between the mentioned parameters.

The statistical measures employed to assess the effectiveness of the model were mean absolute error (MAE), mean absolute percentage error (MAPE), and root means square error (RMSE). These indicators have various relationships: the logarithmic equations provide good forecasting results between GSI_{chart} and Q' and Q-slope', while the linear equations between GSI_{chart} and GSI_{2013} fall in the "stronger prediction" category.

These correlations can be used to assess the surrounding rock mass of various rock types in various places. While these and other connections are likely relevant elsewhere in similar ground conditions, readers are strongly recommended to validate them at their local site before using them. Thus, it is strongly encouraged that engineering geologists and geotechnical engineers have to develop a site-specific correlations chart at various locations.

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