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Sustainable and Resilient Garment Supply Chain Network Design with Fuzzy Multi-Objectives under Uncertainty

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Abstract: Researchers and practitioners are taking more interest in developing sustainable garment supply chains in recent times. On the other hand, the supply chain manager drops sustainability objectives while coping with unexpected natural and man-made disruption risks. Hence, supply chain managers are now trying to develop sustainable supply chains that are simultaneously resilient enough to cope with disruption risks. Owing to the importance of the considered issue, this study proposed a network optimization model for a sustainable and resilient supply chain network by considering sustainability via embodied carbon footprints and carbon emissions and resilience by considering resilience index. In this paper, initially, a possibilistic fuzzy multi-objective sustainable and resilient supply chain network model is developed for the garment industry considering economic, sustainable, and resilience objectives. Secondly, a possibilistic fuzzy linguistic weight-based interactive solution method is proposed. Finally, a numerical case example is presented to show the applicability of the proposed model and solution methodology.

Keywords: sustainable supply chain; resilient supply chain; disruption risks; possibilistic fuzzy optimization; multi-objective optimization

1. Introduction and Literature Review

The textile and garment supply chain involves several environmental issues, including hazardous pollutants and waste management practices. The garment industry is environmentally unfriendly due to hazardous pollutants such as dyeing chemicals and carbon dioxide emissions during production and transportations. Today, these issues are being addressed by compulsory carbon footprint taxes on textile products, sustainability rules and guidelines, International Organization for Standardization (ISO) certification, and emerging trends for corporate social responsibility [1]. Sustainability is not the only primary focus of supply chain to increase their performance, but the trend shows that sustainability is going to be standard in the near future. On the other hand, uncertain disruption risks associated with supply chains hinder an implementation of the sustainability objective. Many authors have proposed various supply chain risk management strategies to minimize the impact of disruption risks. Among them, resilience is a new approach to design supply chain networks [2]. The most widely used definition of supply chain resilience, proposed by Christopher and Peck [3], is "the ability of a system to withstand and return to its original (or desired) state after being disrupted." Pettit, et al. [4] explained that resilience facilitates a supply chain to return its original performance after disruptions, preparing for unexpected events, and responding to disruptions. Mari, et al. [5] defined supply chain resilience as a method to reduce the severity and likelihood of supply chain disruption risks.

Despite the importance of resilience and sustainable supply chain design, very few studies are available in the literature that jointly discusses resilience and sustainability issues in a supply chain context. According to Rose [6], the extreme disruptions could badly affect the environment, which disrupts the major activities of supply chains. The major barrier in developing the sustainable supply chain network is uncertainty associated with supply chain activities. Therefore, a sustainable supply chain should be resilient and flexible enough to cope with uncertain disruptions [7]. This required to build sustainable supply chains which are simultaneously resilient, agile, and lean to cope with uncertain disruption such as natural or man-made disasters [8]. Recently, Azevedo, et al. [9] discussed the importance of green and resilient supply chain management practices in the automotive supply chain. They showed that the resilient paradigm is considered more important than the green paradigm due to its competitive advantage. The other reason is that green practices are imposed externally and is obligatory. Govindan, et al. [10] discussed the linkage of lean, agile, green and resilient practices. Research showed that lean, agile, green, and resilience practices are important for automotive industry due to their individual competitive advantages. Mari, Lee and Memon [2] proposed network optimization model which simultaneously considered both sustainability and resilience of the supply chain. They developed a multi-objective network optimization model based on goal programming which considers economic, sustainable, and resilience objectives. Disruption of the supply chain network leads to supply uncertainty and is important to sustainable supply chain performance. Firms try to find alternate solutions to cope with disrupted supply and might lose sustainability targets. Therefore, it is important to consider an uncertain environment in the design of sustainable and resilient supply chain networks.

The above discussion shows that sustainability is becoming a primary focus of supply chains and resilience is a necessity to achieve the sustainability targets. Thus, firms should find a better way to manage their resources while coping with unexpected disruption risks. Keeping in view the stated problem, this study proposes an integrated sustainable and resilient supply chain network considering disruption risks. To do so, this article proposes multi-objective sustainable and resilient supply chain optimization model for the garment industry by considering stochastic and recognitive uncertainties. In the garment industry, there are significant opportunities to increase sustainability by making effective production and transportation decisions which are directly related to environmental emissions [1]. Additionally, this study considers an expected disruption cost objective as a resilience metric to estimate location-specific risks. Expected disruption cost is a metric for evaluating the resilience of supply chain and defined as a loss of opportunity cost due to not meeting the demand on time during disruption risks [11]. The likelihood of disruption risks at potential locations of suppliers, manufacturing facilities, and collection center is estimated using the Resilience Index (RI) proposed by FMGlobal [12]. The Resilience Index is a data-driven tool to evaluate the risks inherent in the country based on nine key drivers of supply chain risks (i.e., GDP per capita, Political risks, oil intensity, exposure to natural hazards, quality of risk management, quality of fire management, corruption control, infrastructure, and local supplier quality). RI is bound to scale from 0 to 100 representing the lowest to highest resilience. Furthermore, for the first time, this study considers the reverse supply chain network design in building resilience due to its importance in sustainable supply chain. To the best of authors' knowledge, this research is one of the primary works using possibilistic programming approach for a sustainable and resilient supply chain network design under stochastic and recognitive uncertainties and the literature considering this approach in sustainable supply chain network design is still scarce.

2. Mathematical Model

As discussed earlier, the focus of this research is to design the garment supply chain network based on the triple tradeoffs of economic, sustainable, and resilient objectives. Thus, the problem includes multi-objective optimization model that should give compromise solution based on DMs preferences.

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The problem is structured as a supply chain network (see Figure 1) consisting of a set of suppliers (s), from which various raw materials are purchased by a set of manufacturing facilities (i), where the product is manufactured and distributed to various customer zones (j). Collection centers (k) are required to be opened to collect and process used products. The used products are then sent to either resale markets (l) for selling or donating into poor countries, reclamation mills (m) or flocking industry (n) to recycle the used products that are not reusable.

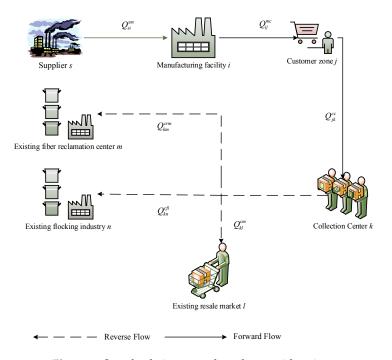


Figure 1. Supply chain network under consideration.

After designing the structure of the supply chain problem, a multi-objective mixed integer linear programming (MOMILP) model is presented. The model consists of three objective functions and constraints related to the garment supply chain network under consideration. The notations and estimations of objective functions and constraints are discussed below.

2.1. Model Notations

Indices	
i	Index of potential location for manufacturing facilities $i = 1, 2,, I$
j	Index of existing customer zones $j = 1, 2,, J$
k	Index of potential locations for collection centers $k = 1, 2,, K$
1	Index of existing markets to sale reusable textile $l = 1, 2,, L$
m	Index of existing fiber reclamation mills $m = 1, 2,, M$
n	Index of existing flocking industry $n = 1, 2,, N$
S	Index of existing suppliers $s = 1, 2,, S$
t	Index of time period $t = 1, 2, \dots, T$
Parameters	
\widetilde{d}_{jt}	Demand for new product at customer zone j in period t (units/period)
	Price of new product in period t (\$/unit/period)
$\widetilde{\psi}_{jt}$	Percentage of products recovered from customer zone j in period t
$egin{array}{l} \widetilde{p}_t \ \widetilde{\psi}_{jt} \ \widetilde{a}_i \ \widetilde{b}_k \end{array}$	Cost of installing manufacturing facility i (\$)
\widetilde{b}_k	Cost of installing collection center k (\$)

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Parameters	
	Transportation cost per unit from supplier s to manufacturing facility i in period t
\widetilde{c}_{sit}	(\$/unit/period)
~	Transportation cost per unit from manufacturing facility i to customer zone j in
\widetilde{e}_{ijt}	period t (\$/unit/period)
\widetilde{c}	Transportation cost per unit from customer zone j to collection center k in period t
\widetilde{f}_{jkt}	(\$/unit/period)
~	Transportation cost per unit from collection center k to resale market l in period t
\widetilde{g}_{klt}	(\$/unit/period)
$\widetilde{}$	Transportation cost per unit from collection center k to fiber reclamation mill m in
\widetilde{h}_{kmt}	period t (\$/unit/period)
~	Transportation cost per unit from collection center k to flocking industry n in
\widetilde{o}_{knt}	period t (\$/unit/period)
_ em f	Embodied carbon footprints of material coming from supplier s in period t
ce_{st}^{emf}	(KgCO ₂ /unit/period)
coman	Carbon emission during production of unit product at manufacturing facility i in
ce_{it}^{man}	period t (KgCO ₂ /unit/period)
astsm	Carbon emission for shipping unit product from supplier s to manufacturing
ce_{sit}^{tsm}	facility i in period t (KgCO ₂ /unit/period)
ce_{ijt}^{tmc}	Carbon emission for shipping unit product from manufacturing facility i to
cc _{ijt}	customer zone j in period t (KgCO ₂ /unit/period)
ce ^{tcc} jkt	Carbon emission for shipping unit product from customer zone j to collection
jkt	center k in period t (KgCO ₂ /unit/period)
ce ^{tcm}	Carbon emission for shipping unit product from collection center k to resale
ccklt	market l in period t (KgCO ₂ /unit/period)
ce^{tcr}_{kmt}	Carbon emission for shipping unit product from collection center <i>k</i> to fiber
kmt	reclamation mill m in period t (KgCO ₂ /unit/period)
ce_{knt}^{tcf}	Carbon emission for shipping unit product from collection center <i>k</i> to flocking
knt	industry n in period t (KgCO ₂ /unit/period)
ce_{kt}^{pcc}	Carbon emission during processing unit product at collection center k in period t
Kī	(KgCO ₂ /unit/period)
ce_{mt}^{prm}	Carbon emission during processing unit product at fiber reclamation mill m in
1111	period t (KgCO ₂ /unit/period)
ce_{nt}^{pfi}	Carbon emission during processing unit product at flocking industry n in period t
	(KgCO ₂ /unit/period)
$\widetilde{\pi}_{st}$	Unit purchase cost of material from supplier s in period t (\$\frac{1}{2}\text{unit/period})
\widetilde{eta}_{it}	Manufacturing cost per product at manufacturing facility i in period t
$\widetilde{\chi}_{kt}$	($\$$ /unit/period) Processing cost per product at collection center k in period t ($\$$ /unit/period)
	Processing cost per product at confection center k in period t (ϕ / unit/period)
$\widetilde{\varepsilon}_{mt}$	Processing cost per product at flocking industry n in period t (\$/unit/period)
$\widetilde{\phi}_{nt}$ \widetilde{arphi}_{it}	Capacity of manufacturing facility i in period t (units/period)
$\widetilde{\gamma}_{kt}$	Capacity of collection center k in period t (units/period)
	Capacity of fiber reclamation mill m in period t (units/period)
$\widetilde{\eta}_{mt} \ \widetilde{\lambda}_{nt}$	
$\widetilde{\mathcal{V}}_{st}$	Capacity of flocking industry n in period t (units/period) Capacity of supplier s in period t (units/period)
vst ñsd	Probability of disruption risk at supplier s in period t
Pst ñmd	Probability of disruption risk at suppliers in period t Probability of disruption risk at manufacturing facility i in period t
\widetilde{p}_{st}^{sd} \widetilde{p}_{it}^{md} \widetilde{p}_{kt}^{cd}	Probability of disruption risk at collection center k in period t
Pkt	1 100 ability of distuption fish at conection terries it in period i

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Decision Va	riables
Q_{sit}^{SM}	Transportation quantity from supplier s to manufacturing facility i in period t (units/period)
Q_{ijt}^{MC}	Transportation quantity from manufacturing facility i to customer zone j in period t (units/period)
Q_{jkt}^{cc}	Transportation quantity from customer zone j to collection center k in period t (units/period)
Q_{klt}^{cm}	Transportation quantity from collection center k to resale market l in period t (units/period)
Q_{kmt}^{crm}	Transportation quantity from collection center k to fiber reclamation mill m in period t (units/period)
Q_{knt}^{cfi}	Transportation quantity from collection center k to flocking industry n in period t (units/period)
$x_i = \begin{cases} 1 \\ 0 \\ y_k = \begin{cases} 1 \\ 0 \end{cases}$	If a manufacturing facility i is open 1, otherwise 0
$y_k = \begin{cases} 1 \\ 0 \end{cases}$	If a collection center k is open 1, otherwise 0

2.2. Formulation of Objective Functions

The objective of the proposed sustainable and resilient supply chain model is to minimize the total supply chain cost, minimize carbon emission, and minimize expected disruption cost in all considered periods. First, objective function f_{cost} in Equation (1) minimizes the total cost of supply chain. Second, objective function f_{sus} in Equation (2) minimizes the total carbon emission. Third, objective function f_{edc} in Equation (3) minimizes expected disruption cost. Various estimations related to these objectives are discussed in below section.

Objective 1:

$$Minimize f_{cost}(x) = Total supply chain cost$$
 (1)

Objective 2:

Minimize
$$f_{SUS}(x)$$
 = Total carbon emission (2)

Objective 3:

Minimize
$$f_{edc}(x)$$
 = Expected disruption cost (3)

a. Total supply chain cost (Economic objective)

Various costs associated with the supply chain are calculated in Equation (4). The first two terms represent the installation cost of manufacturing facilities and collection centers, respectively. The remaining terms represent the material purchasing cost, production cost, and processing costs for suppliers, manufacturing facilities, collection centers, fiber reclamation center, and flocking industries along with corresponding transportation costs in all periods, respectively.

Total supply chain cost =
$$\sum_{i} \widetilde{a}_{i} x_{i} + \sum_{k} b_{i} y_{k} + \sum_{s} \sum_{i} \sum_{t} (\widetilde{\pi}_{st} + \widetilde{c}_{sit}) Q_{sit}^{SM} + \sum_{i} \sum_{j} \sum_{t} (\widetilde{\beta}_{it} + \widetilde{e}_{ijt}) Q_{ijt}^{mc} + \sum_{j} \sum_{k} \sum_{t} (\widetilde{\chi}_{kt} + \widetilde{f}_{jkt}) Q_{jkt}^{cc} + \sum_{k} \sum_{l} \sum_{t} \widetilde{g}_{klt} Q_{klt}^{cm} + \sum_{k} \sum_{m} \sum_{t} (\widetilde{\epsilon}_{mt} + \widetilde{h}_{kmt}) Q_{kmt}^{crm} + \sum_{k} \sum_{n} \sum_{t} (\widetilde{\phi}_{nt} + \widetilde{\epsilon}_{knt}) Q_{knt}^{cfi}$$

$$(4)$$

b. Total Carbon emission (Sustainable objective)

Various carbon emissions in the supply chain are computed in Equation (5). The first term estimates embodied carbon footprints and carbon emission during transportation of material coming from various suppliers. It is very important to minimize the embodied carbon footprint of the procured

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material in order to consider every aspect of sustainable supply chain. For instance, if the manufacturer unit available in highly green zone procured raw material with a high carbon embodied footprint, will fail to attain its sustainability objective and may face legal restriction because of being in the green zone. Second term includes carbon emission during production and transportation of product to customer zones. Third term includes carbon emission during processes and collection centers and transportation of used products. Fourth term includes carbon emission during transportation of used products to resale markets. The last two terms include carbon emission during recycling processes and transportation of used products from collection centers to recycling centers.

Total carbon emission =
$$\sum_{s} \sum_{t} \sum_{t} (ce_{st}^{emf} + ce_{sit}^{tsm}) Q_{sit}^{sm} + \sum_{i} \sum_{j} \sum_{t} (ce_{it}^{man} + ce_{ijt}^{tmc}) Q_{ijt}^{mc} + \sum_{j} \sum_{k} \sum_{t} (ce_{jkt}^{tcc} + ce_{kt}^{pcc}) Q_{jkt}^{cc} + \sum_{k} \sum_{l} \sum_{t} ce_{klt}^{tcm} Q_{klt}^{cm} + \sum_{k} \sum_{m} \sum_{t} (ce_{kmt}^{tcf} + ce_{mt}^{prm}) Q_{kmt}^{crm} + \sum_{k} \sum_{n} \sum_{t} (ce_{knt}^{tcf} + ce_{nt}^{pfi}) Q_{knt}^{cfi}$$
(5)

c. Expected disruption cost (Resilience objective)

The goal of this objective is to minimize expected disruption cost due to any disruption risk associated with any member of the supply chain in all periods. In this research, only the forward supply chain is considered to measure the resilience objective since the forward supply chain resiliency is more important and also has an impact on the reverse supply chain. Hence, Equation (6) measures the expected disruption cost due to disruption of the supplier, manufacturing facilities, and collection centers in all periods.

Expected disruption cost =
$$\left(\sum_{s} \sum_{t} \sum_{t} \widetilde{p}_{st}^{sd} Q_{sit}^{sm} + \sum_{i} \sum_{j} \sum_{t} \widetilde{p}_{it}^{md} Q_{ijt}^{mc} + \sum_{j} \sum_{k} \sum_{t} \widetilde{p}_{kt}^{cd} Q_{jkt}^{cc} \right) \widetilde{p}_{t}$$
 (6)

2.3. Formulation of Constraints

Constraints (7)–(11) are capacity restrictions on supplier, manufacturing facilities, collection center, fiber reclamation mill, and flocking industry, respectively, in all periods. In addition, Constraints (8) and (9) ensure that the products are produced and processed only on existing manufacturing facilities and collection centers respectively in all periods.

$$\sum_{s} \sum_{i} Q_{sit}^{sm} \le \widetilde{\nu}_{st}, \ \forall t \tag{7}$$

$$\sum_{i} \sum_{j} Q_{ijt}^{mc} \le x_i \widetilde{\varphi}_{it}, \ \forall t$$
 (8)

$$\sum_{i} \sum_{k} Q_{jkt}^{cc} \le y_k \widetilde{\gamma}_{kt}, \ \forall t$$
 (9)

$$\sum_{k} \sum_{m} Q_{kmt}^{crm} \le \widetilde{\eta}_{mt}, \ \forall t \tag{10}$$

$$\sum_{k} \sum_{n} Q_{knt}^{cfi} \le \widetilde{\lambda}_{nt}, \ \forall t \tag{11}$$

Constraint (12) promises that the amount of products transported from manufacturing facilities to customer zone j should satisfy its demand. Constraint (13) shows that all the used products are collected from customer zones.

$$\sum_{i} \sum_{j} Q_{ijt}^{mc} \ge \widetilde{d}_{jt}, \ \forall t$$
 (12)

$$\sum_{j} \sum_{k} Q_{jkt}^{cc} \ge \widetilde{\psi}_{jt} \widetilde{d}_{jt}, \ \forall t$$
 (13)

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Constraint (14) balances the input and output of the material in a manufacturing facility. The amount of incoming material from suppliers to the manufacturing facility is equal to a number of outgoing products from the manufacturing facility to the customer zone. Similarly, Constraints (15)–(17) balance the input and output of used products in the collection center. The incoming used products from customer zones are either sent to resale markets or separated for fiber reclamation process and flocking process. It is assumed in this study that 50% of collected products are reusable, and the remaining products are then separated for reclamation and flocking processes. According to U.K. industry sources, about 50 percent of collected textile items can be reused and the remaining 50 percent can recycled [13].

$$\sum_{s} \sum_{i} Q_{sit}^{sm} = \sum_{i} \sum_{j} Q_{ijt}^{mc}, \ \forall t$$
 (14)

$$\sum_{i} \sum_{k} Q_{jkt}^{cc} = \sum_{k} \sum_{l} Q_{klt}^{cm} + \sum_{k} \sum_{m} Q_{kmt}^{crm} + \sum_{k} \sum_{n} Q_{knt}^{cfi}, \ \forall t$$
 (15)

$$\sum_{k} \sum_{l} Q_{klt}^{cm} = 0.5 \times \sum_{j} \sum_{k} Q_{jkt}^{cc}, \ \forall t$$
 (16)

$$\sum_{k} \sum_{m} Q_{kmt}^{crm} = \sum_{k} \sum_{n} Q_{knt'}^{cfi} \ \forall t$$
 (17)

Constraints (18) and (19) impose non-negativity and binary restrictions to all the corresponding decision variables, respectively.

$$Q_{sit}^{sm}, Q_{iit}^{mc}, Q_{ikt}^{cc}, Q_{klt}^{cm}, Q_{kmt}^{crm}, Q_{knt}^{cfi} \ge 0, \ \forall \ i, j, k, l, m, n, s, t$$
 (18)

$$x_i, y_k \in \{0, 1\}, \ \forall \ i, k$$
 (19)

3. Proposed Solution Methodology

Several solution methodologies are developed to solve the multi-objective programming models. Fuzzy-based programming techniques are highly used in this area because of their capability in estimation and adjustment of the decision maker's satisfaction level of each objective explicitly [14]. In this study, initially, the methodology proposed by Jiménez, et al. [15] is applied to convert the uncertain model into an equivalent auxiliary crisp model. The proposed uncertain model in previous section assumes possibilistic fuzzy parameters. Then the interactive fuzzy weight, based solution methodology, is developed to solve the proposed sustainable and resilient supply chain model. The steps of the proposed solution methodology are summarized as follows:

Step 1. Convert fuzzy multi-objective model into equivalent auxiliary crisp model

In this stage, the proposed multi-objective model is converted into an equivalent auxiliary crisp model. Jiménez, Arenas, Bilbao and Rodri [15] method used in this study due to: (i) its strong mathematical formation which is based on expected interval and expected value of fuzzy numbers to deal with uncertain parameters; and (ii) its support of any fuzzy membership function such as trapezoidal and triangular with either symmetric or asymmetric forms. Readers can refer Jiménez, Arenas, Bilbao and Rodri [15] for detail information on this method.

Assume that " $\tilde{\vartheta}$ " is a triangular fuzzy number, then the membership function of $\tilde{\vartheta}$ can be defined as in Equation (20), where *pes* is the pessimistic value, *mos* is the most likely value, and *opt* is the optimistic value of triangular fuzzy number.

$$\mu_{\widetilde{\theta}}(x) = \begin{cases} f_{\theta}(x) = \frac{x - \theta^{pes}}{\theta^{mos} - \theta^{pes}} & \text{if } \theta^{pes} \le x \le \theta^{mos} \\ 1 & \text{if } x = \theta^{mos} \\ g_{\theta}(x) = \frac{\theta^{opt} - x}{\theta^{opt} - \theta^{mos}} & \text{if } \theta^{mos} \le x \le \theta^{opt} \\ 0 & \text{if } x \le \theta^{pes} \text{ or } x \ge \theta^{opt} \end{cases}$$
(20)

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According to Jiménez, Arenas, Bilbao and Rodri [15], the expected interval (EI) and expected value (EV) of triangular fuzzy number $\tilde{\theta}$ can be defined as follows.

$$EI(\widetilde{\vartheta}) = [E_1^{\vartheta}, E_2^{\vartheta}] = \left[\int_0^1 f_{\vartheta}^{-1}(x) dx, \int_0^1 g_{\vartheta}^{-1}(x) dx, \right] = \left[\frac{1}{2} (\vartheta^{pes} + \vartheta^{mos}), \frac{1}{2} (\vartheta^{mos} + \vartheta^{opt}) \right]$$
(21)

$$EV(\widetilde{\vartheta}) = \frac{E_1^{\vartheta} + E_1^{\vartheta}}{2} = \frac{\vartheta^{pes} + 2\vartheta^{mos} + \vartheta^{opt}}{4}$$
 (22)

Consequently, using the definition of expected interval and expected value of a fuzzy number, the equivalent auxiliary crisp model of a proposed possibilistic sustainable and resilient supply chain model can be formulated as follows. The uncertain objective functions are converted into crisp forms using expected value definition. In addition, the uncertain constraints will be converted into equivalent crisp forms using expected interval definition. Where, α represents the confidence level. The decision makers can choose level of confidence based on available information and their perception. Additionally, decision makers can vary value of α in order to generate different tradeoff solutions. In this formulation, $\alpha = 0.5$ means that the most likely values of parameters are preferred, whereas $\alpha < 0.5$ means model parameter values are between pessimistic and most likely values. Similarly, $\alpha > 0.5$ means that value of model parameters are between most likely and pessimistic values.

$$\frac{\text{Minimize } f_{cost}(x) =}{\sum_{i} \left(\frac{a_{i}^{pes} + 2a_{i}^{most} + a_{i}^{opt}}{4}\right) x_{i} + \sum_{k} \left(\frac{b_{i}^{pes} + 2b_{i}^{most} + b_{i}^{opt}}{4}\right) y_{k} + \\
\sum_{s} \sum_{i} \sum_{t} \left(\frac{\pi_{st}^{pes} + 2\pi_{st}^{mos} + \pi_{st}^{opt} + c_{sit}^{pes} + 2c_{sit}^{mos} + c_{sit}^{opt}}{4}\right) Q_{sit}^{sm} + \\
\sum_{s} \sum_{i} \sum_{t} \left(\frac{\beta_{it}^{pes} + 2\beta_{itt}^{mos} + \beta_{it}^{opt} + e_{ijt}^{pes} + 2c_{ijt}^{mos} + e_{ijt}^{opt}}{4}\right) Q_{sit}^{sm} + \\
\sum_{i} \sum_{j} \sum_{t} \left(\frac{\lambda_{kt}^{pes} + 2\lambda_{kt}^{mos} + \lambda_{kt}^{opt} + \beta_{jkt}^{pes} + 2\beta_{jkt}^{mos} + \beta_{jkt}^{opt}}{4}\right) Q_{ijt}^{cc} + \\
\sum_{j} \sum_{k} \sum_{t} \left(\frac{\lambda_{kt}^{pes} + 2\lambda_{kt}^{mos} + \lambda_{kt}^{opt} + \beta_{jkt}^{opt} + \beta_{jkt}^{opt}}{4}\right) Q_{kt}^{cm} + \\
\sum_{k} \sum_{l} \sum_{t} \left(\frac{\lambda_{kt}^{pes} + 2\lambda_{kt}^{mos} + \lambda_{kt}^{opt} + \lambda_{kt}^{pes} + \lambda_{kt}^{opt}}{4}\right) Q_{kt}^{cm} + \\
\sum_{k} \sum_{t} \sum_{t} \sum_{t} \left(\frac{\lambda_{kt}^{pes} + 2\lambda_{itt}^{mos} + \lambda_{kt}^{opt} + \lambda_{kt}^{pes} + \lambda_{kt}^{opt}}{4}\right) Q_{ktt}^{crm} + \\
\sum_{k} \sum_{t} \sum_{t} \sum_{t} \left(\frac{\lambda_{kt}^{pes} + 2\lambda_{itt}^{mos} + \lambda_{itt}^{opt} + \lambda_{kt}^{pes} + \lambda_{kt}^{opt}}{4}\right) Q_{ktt}^{cri} + \\
\sum_{t} \sum_{t} \sum_{t} \sum_{t} \left(\frac{\lambda_{it}^{pes} + \lambda_{itt}^{opt} + \lambda_{kt}^{opt} + \lambda_{kt}^{opt} + \lambda_{kt}^{opt}}{4}\right) Q_{ktt}^{cri} + \\
\sum_{t} \sum_{t} \sum_{t} \sum_{t} \left(\frac{\lambda_{it}^{pes} + \lambda_{it}^{opt} + \lambda_{itt}^{opt} + \lambda_{kt}^{opt}}{4}\right) Q_{ktt}^{cri} + \\
\sum_{t} \sum_{t} \sum_{t} \sum_{t} \left(\frac{\lambda_{it}^{opt} + \lambda_{it}^{opt} + \lambda_{itt}^{opt} + \lambda_{itt}^{opt}}{4}\right) Q_{ktt}^{cri} + \\
\sum_{t} \sum_{t} \sum_{t} \left(\frac{\lambda_{it}^{opt} + \lambda_{it}^{opt} + \lambda_{itt}^{opt}}{4}\right) Q_{ktt}^{cri} + \\
\sum_{t} \sum_{t} \sum_{t} \left(\frac{\lambda_{it}^{opt} + \lambda_{it}^{opt} + \lambda_{itt}^{opt}}{4}\right) Q_{ktt}^{cri} + \\
\sum_{t} \sum_{t} \sum_{t} \left(\frac{\lambda_{it}^{opt} + \lambda_{it}^{opt} + \lambda_{itt}^{opt}}{4}\right) Q_{ktt}^{cri} + \\
\sum_{t} \sum_{t} \sum_{t} \left(\frac{\lambda_{it}^{opt} + \lambda_{it}^{opt} + \lambda_{itt}^{opt}}{4}\right) Q_{ktt}^{cri} + \\
\sum_{t} \sum_{t} \sum_{t} \left(\frac{\lambda_{it}^{opt} + \lambda_{it}^{opt} + \lambda_{itt}^{opt}}{4}\right) Q_{ktt}^{cri} + \\
\sum_{t} \sum_{t} \sum_{t} \left(\frac{\lambda_{it}^{opt} + \lambda_{it}^{opt} + \lambda_{it}^{opt}}{4}\right) Q_{ktt}^{cri} + \\
\sum_{t} \sum_{t} \sum_{t} \left(\frac{\lambda_{it}^{opt} + \lambda_{it}^{opt} + \lambda_{it}^{opt}}{4}\right) Q_{ktt}^{cri$$

$$\operatorname{Minimize} f_{sus}(x) = \\
\sum_{s} \sum_{t} \sum_{t} \left(ce_{st}^{emf} + ce_{sit}^{tsm} \right) Q_{sit}^{sm} + \sum_{i} \sum_{j} \sum_{t} \left(ce_{it}^{man} + ce_{ijt}^{tmc} \right) Q_{ijt}^{mc} + \\
\sum_{j} \sum_{k} \sum_{t} \left(ce_{jkt}^{tcc} + ce_{kt}^{pcc} \right) Q_{jkt}^{ccc} + \sum_{k} \sum_{l} \sum_{t} ce_{klt}^{tcm} Q_{klt}^{cm} + \\
\sum_{k} \sum_{m} \sum_{t} \left(ce_{kmt}^{tcf} + ce_{mt}^{prm} \right) Q_{kmt}^{crm} + \sum_{k} \sum_{n} \sum_{t} \left(ce_{knt}^{tcf} + ce_{nt}^{pfi} \right) Q_{knt}^{cfi}$$
(24)

$$Minimize f_{edc}(x) = \begin{pmatrix} \sum_{s} \sum_{i} \sum_{t} \left(\frac{p_{st}^{sd,pes} + 2p_{st}^{sd,mos} + p_{st}^{sd,opt}}{4} \right) Q_{sit}^{sm} + \\ \sum_{i} \sum_{j} \sum_{t} \left(\frac{p_{it}^{md,pes} + 2p_{it}^{md,mos} + p_{it}^{md,opt}}{4} \right) Q_{ijt}^{mc} + \\ \sum_{j} \sum_{k} \sum_{t} \left(\frac{p_{kt}^{cd,pes} + 2p_{kt}^{cd,mos} + p_{kt}^{cd,opt}}{4} \right) Q_{jkt}^{cc} \end{pmatrix} \begin{pmatrix} p_{t}^{pes} + 2p_{t}^{pes} + p_{t}^{opt}}{4} \end{pmatrix} \tag{25}$$

Subject to

$$\sum_{s} \sum_{i} Q_{sit}^{sm} \le \left[\alpha \left(\frac{v_{st}^{pes} + v_{st}^{mos}}{2} \right) + (1 - \alpha) \left(\frac{v_{st}^{mos} + v_{st}^{opt}}{2} \right) \right], \ \forall t$$
 (26)

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$$\sum_{i} \sum_{j} Q_{ijt}^{mc} \le x_{i} \left[\alpha \left(\frac{\varphi_{it}^{pes} + \varphi_{it}^{mos}}{2} \right) + (1 - \alpha) \left(\frac{\varphi_{it}^{mos} + \varphi_{it}^{opt}}{2} \right) \right], \, \forall t$$
 (27)

$$\sum_{j} \sum_{k} Q_{jkt}^{cc} \le y_k \left[\alpha \left(\frac{\gamma_{kt}^{pes} + \gamma_{kt}^{mos}}{2} \right) + (1 - \alpha) \left(\frac{\gamma_{kt}^{mos} + \gamma_{kt}^{opt}}{2} \right) \right], \ \forall t$$
 (28)

$$\sum_{k} \sum_{m} Q_{kmt}^{crm} \le \left[\alpha \left(\frac{\eta_{mt}^{pes} + \eta_{mt}^{mos}}{2} \right) + (1 - \alpha) \left(\frac{\eta_{mt}^{mos} + \eta_{mt}^{opt}}{2} \right) \right], \ \forall t$$
 (29)

$$\sum_{k} \sum_{n} Q_{knt}^{cfi} \le \left[\alpha \left(\frac{\lambda_{nt}^{pes} + \lambda_{nt}^{mos}}{2} \right) + (1 - \alpha) \left(\frac{\lambda_{nt}^{mos} + \lambda_{nt}^{opt}}{2} \right) \right], \ \forall t$$
 (30)

$$\sum_{i} \sum_{j} Q_{ijt}^{mc} \ge \left[\alpha \left(\frac{d_{jt}^{mos} + d_{jt}^{opt}}{2} \right) + (1 - \alpha) \left(\frac{d_{jt}^{pes} + d_{jt}^{mos}}{2} \right) \right], \forall t$$
 (31)

$$\sum_{j} \sum_{k} Q_{jkt}^{cc} \ge \left[\alpha \left(\frac{\psi_{jt}^{mos} + \psi_{jt}^{opt}}{2} \right) + (1 - \alpha) \left(\frac{\psi_{jt}^{pes} + \psi_{jt}^{mos}}{2} \right) \right] \times \left[\alpha \left(\frac{d_{jt}^{mos} + d_{jt}^{opt}}{2} \right) + (1 - \alpha) \left(\frac{d_{jt}^{pes} + d_{jt}^{mos}}{2} \right) \right], \ \forall t$$
 (32)

$$\sum_{s} \sum_{i} Q_{sit}^{sm} = \sum_{i} \sum_{j} Q_{ijt}^{mc}, \ \forall t$$
 (33)

$$\sum_{i} \sum_{k} Q_{jkt}^{cc} = \sum_{l} Q_{klt}^{cm} + \sum_{m} Q_{kmt}^{crm} + \sum_{k} \sum_{n} Q_{knt}^{cfi}, \forall t$$
(34)

$$\sum_{k} \sum_{l} Q_{klt}^{cm} = 0.5 \times \sum_{j} \sum_{k} Q_{jkt}^{cc}, \ \forall t$$
 (35)

$$\sum_{k} \sum_{m} Q_{kmt}^{crm} = \sum_{k} \sum_{n} Q_{knt'}^{cfi} \, \forall t$$
 (36)

$$Q_{sit}^{sm}, Q_{iit}^{mc}, Q_{ikt}^{cc}, Q_{klt}^{cm}, Q_{kmt}^{crm}, Q_{knt}^{cfi} \ge 0, \ \forall \ i, j, k, l, m, n, s, t$$
 (37)

$$x_i, y_k \in \{0, 1\}, \ \forall \ i, k$$
 (38)

Step 2. Obtain efficient α -extreme solutions

Usually, two methods are used in practice to find out efficient α -extreme solutions. In the first method, the DMs are encouraged to suggest the bounds on each objective. However, this method is less common because it is difficult for DMs to suggest bounds when the problem is of large scale. The second method that we used in this study is to find an extreme possible solution by solving each objective separately. In this step, the crisp model is solved considering one objective along with constraints in a single run. This results in lower (α -LB) and upper (α -UB) bounds on each objective function.

Step 3. Determine the Fuzzy membership function for each objective

The payoff values (i.e., α -LB and α -UB) are now used to develop the fuzzy membership function for each objective of proposed model. Assuming that membership functions based on preference or satisfaction are linear, the linear membership for fuzzy objectives is given as follows:

$$\mu_{cost}(x) = \begin{cases} 0, & f_{cost} > f_{cost}^{\alpha - UB} \\ \frac{f_{cost}^{\alpha - UB} - f_{cost}}{f_{cost}^{\alpha - UB} - f_{cost}^{\alpha - LB}}, & f_{cost}^{\alpha - LB} < f_{cost} \le f_{cost}^{\alpha - UB} \\ 1, & f_{cost} \le f_{cost}^{\alpha - LB} \end{cases}$$

$$\mu_{sus}(x) = \begin{cases} 0, & f_{sus} > f_{sus}^{\alpha - UB} \\ \frac{f_{sus}^{\alpha - UB} - f_{sus}}{f_{sus}^{\alpha - UB} - f_{sus}^{\alpha - LB}}, & f_{sus}^{\alpha - LB} < f_{sus} \le f_{sus}^{\alpha - UB} \\ 1, & f_{sus} \le f_{sus}^{\alpha - LB} \end{cases}$$

$$\mu_{res}(x) = \begin{cases} 0, & f_{edc} > f_{edc}^{\alpha-UB} \\ \frac{f_{edc}^{\alpha-UB} - f_{edc}}{f_{edc}^{\alpha-UB} - f_{edc}^{\alpha-LB}}, & f_{edc}^{\alpha-LB} < f_{edc} \le f_{edc}^{\alpha-UB} \\ 1, & f_{edc} \le f_{edc}^{\alpha-LB} \end{cases}$$

where μ_{cost} , μ_{sus} , and μ_{res} are satisfaction level of cost, sustainability, and resilience objectives, respectively.

Step 4. Convert multi-objective model into single objective

Various interactive approaches are proposed to solve multi-objective problems. Selection of a suitable solution methodology for a certain multi-objective optimization problem is not easy, as has been made abundantly clear [16]. In this study, the fuzzy linguistic weight-based method is proposed by improving Werner's "fuzzy and" operator method [17]. The proposed method takes advantage of both Werner's and the fuzzy-weighted method. The detail of proposed method is given as follows.

In practice, DMs feel comfortable assigning importance of objectives in linguistic terms. In this proposed method, the fuzzy linguistic variables are suggested to assign the importance of objectives. Table 1 shows the five-scale importance level as triangular fuzzy number adopted from Wang and Lee [18]. Suppose that decision-making panel consists of n DMs, then the importance of objectives can be estimated as follows.

Importance Level	Abbreviation	Fuzzy Number
Very Low	VL	(0,0,0.2)
Low	L	(0.05, 0.2, 0.35)
Medium-Low	ML	(0.2, 0.35, 0.5)
Medium	M	(0.35, 0.5, 0.65)
Medium-High	MH	(0.5, 0.65, 0.8)
High	Н	(0.65, 0.8, 0.95)
Very High	VH	(0.8,1,1)

Table 1. Seven-scale fuzzy linguistic variable for importance level.

- (1) Set the linguistic variables for the importance of objectives.
- (2) Evaluate the importance of objectives based on linguistic variables from Table 1.
- (3) Aggregate each of the fuzzy number using

$$AFN_q = \left(\frac{\omega_1^{pes} + \omega_2^{pes} + \ldots + \omega_n^{pes}}{n}, \frac{\omega_1^{mos} + \omega_2^{mos} + \ldots + \omega_n^{mos}}{n}, \frac{\omega_1^{opt} + \omega_2^{opt} + \ldots + \omega_n^{opt}}{n}\right)$$

where AFN_q is aggregate fuzzy number of q^{th} objective and $(\omega_n^{pes}, \omega_n^{mos}, \omega_n^{opt})$ is n^{th} decision maker perception of importance for q^{th} objective.

(4) Estimate the fuzzy weight of q^{th} objective as shown below.

$$arphi_q = rac{\omega_q^{pes} + 2\omega_q^{mos} + \omega_q^{opt}}{4}$$

where $(\omega_q^{pes}, \omega_q^{mos}, \omega_q^{opt}) = AFN_q$, q = 1, 2, 3 number of objectives.

(5) Calculate the normalized fuzzy weights of objectives by:

$$\omega_q' = \frac{\omega_q}{\sum\limits_{q} \omega_q}$$

(6) Finally, the single objective model using improved Werner's method can be formed as below.

maximize
$$\theta \zeta_0 + (1-\theta) \left(\omega_1' \zeta_1 + \omega_2' \zeta_2 + \omega_3' \zeta_3 \right)$$

subject to $\mu_{cost}(x) \geq \zeta_0 + \zeta_1$
 $\mu_{sus}(x) \geq \zeta_0 + \zeta_2$
 $\mu_{res}(x) \geq \zeta_0 + \zeta_3$
 $\zeta_0, \zeta_1, \zeta_2, \zeta_3 \in [0, 1]$
System constraints (26–38)

where, θ denotes the coefficient of compensation and ζ_1 , ζ_2 , and ζ_3 are the difference between satisfaction level of objectives with their minimum satisfaction level. That is, $\zeta_1 = \mu_{cost} - \zeta_0$, $\zeta_2 = \mu_{sus} - \zeta_0$, and $\zeta_3 = \mu_{res} - \zeta_0$. ω_1' , ω_2' , and ω_3' are the normalized weights for cost, sustainability, and resilience objectives, respectively.

Step 5. Determine the solution method parameters

To solve the mathematical models developed in Step 4, the values of coefficient of compensation (θ) and relative importance of objectives (α_a) are determined.

Step 6. Solve the model

The mathematical models developed in Step 4 are solved using required model and solution methodology parameters. If decision makers are not satisfied with the results, they can provide another solution by modifying the solution method parameters (i.e., θ and $\omega_q^{'}$). If decision makers want to modify value of α , then they must restart the process at Step 2.

4. Numerical Example

In the case when real data are not available, a test problem is developed based on a hypothetical supply chain, where data are conducted based on reasonable assumptions and several public resources. In real life implementation, required data can be obtained from various sources, such as installation and production costs can be obtained from already present manufacturing facilities. Transportation costs between facilities can easily be obtained from available transportation services. In this example, supply chain risk is estimated by using resilience index as discussed above. To solve the proposed model, a garment supply chain is chosen, which consists of five potential suppliers, three manufacturing facilities, four customer zones, three collection centers, two resale markets, two flocking industries, and two reclamation mills, as shown in Figure 2. This numercial example assumes that the supply chain is producing single garment product i.e., jeans.

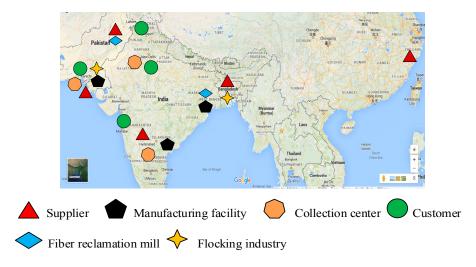


Figure 2. Supply chain network of case example.

The presented supply chain included five suppliers located at Karachi and Faisalabad cities of Pakistan, Hyderabad city of India, Dhaka city of Bangladesh, and Shaoxing city of China. Three potential locations of manufacturing facilities are located in Karachi, Pakistan, Hyderabad, India, and Kolkata, India. Four customer zones are chosen to sell the product located in Karachi, Pakistan, Lahore, Pakistan, Mumbai, India, and Delhi, India. Karachi, Pakistan, Delhi, India, and Hyderabad, India are selected for locations of collection centers. Mali and Libya are selected as resale markets. Potential locations of flocking industries are located at Karachi, Pakistan and Dhaka, Bangladesh, whereas, potential reclamation mills are located at Kolkata, India and Faisalabad, Pakistan. The decisions that have to be made here are following:

- A number of manufacturing facilities required to open and their locations.
- The amount of products produced at each opened facility and which customer zones satisfied from each opened facility.
- Suppliers selected for supplying material to each opened manufacturing facility.
- Quantity of material to be purchased from each selected supplier
- Number and locations of collection centers opened.
- Location of recycling facilities (i.e., flocking industry and reclamation mill) preferred for recycling used products.
- Location of resale market and quantity of products that can be resale to these markets.

4.1. Data population

The collection of data was performed to solve the model and generate useful results. The triangular fuzzy parameters $\tilde{\theta}$ are estimated by initially calculating the most likely θ^{mos} value of parameters. These most likely values of parameters were picked from various sources (such as SeaRates [19] for transportation distances and costs and CargoRouter [20] for CO₂ emissions) some reasonable assumptions were made, and all required calculations were done beforehand. Thereafter, two random numbers (n_1, n_2) are generated between 0.2 and 0.8 using uniform distribution and the pessimistic θ^{pes} and optimistic θ^{opt} values of fuzzy number $\tilde{\theta}$ are estimated as follows.

$$\vartheta^{pes} = (1 - n_2)\vartheta^{mos}$$

$$\vartheta^{opt} = (1 + n_1)\vartheta^{mos}$$

All the required data (the most likely value) are presented in Appendix A with sources (i.e., either official data or hypothetical data).

4.2. Result and Discussion

The crisp sustainable and resilient model is solved using $\alpha = 0.90$ to obtain payoff values. Payoff values (i.e., α -LB and α -UB) of three objectives are shown in Table 2.

Total Supply Chain Expected Disruption Sustainability (KgCO₂) Objective Functions Cost (\$) Cost (\$) Minimize total supply chain cost 1,084,865.00 305,416.60 307,182.30 1,486,758.00 280,782.30 331,000.70 Minimize sustainability 307,944.90 1,296,953.00 287,975.10 Minimize expected disruption cost

Table 2. Payoff values (α -LB and α -UB).

It can be seen from results that all three objectives, i.e., economic, sustainability, and resilience, of supply chain networks are conflicting in nature (see Figures 3–5). If an organization wants to consider the economic perspective, Kolkata is a suitable location for a manufacturing facility. On the

other hand, Karachi is suitable location from sustainability perspective and Hyderabad is suitable location from resilience perspective. Similarly, based on procurement and transportation cost, suitable suppliers are located in Shaoxing, Dhaka, and Hyderabad. Alternatively, suppliers located at Karachi and Dhaka are suitable choices when sustainability objective is given priority over other objectives. Results show that suppliers with higher resilience index or lesser probability of disruptions are given priority when the resilience objective is considered. Similarly, manufacturing facility and collection centers are open in the highest resilience index locations. The resilience objective ensures that the supply chain network should consider disruption risks in advance. This minimizes the risk of dropping supply chain performance during a disruption event. The impact of disruption risks can be minimized by: (1) selecting suppliers based on their adopted resilience level and the probability of disruption risks in suppliers' locations; (2) establishing manufacturing facilities, collection centers, and other service facilities to locations where the probability of disruption risks are low or resilience index score of location is high; (3) transporting minimum quantity of material form higher risk zones and vice versa; and (4) it is also found from this study that it is not a suitable choice to select key suppliers from the same region because this leads to higher supply density, which is vulnerable during high impact and low probability (HILP) risk events.

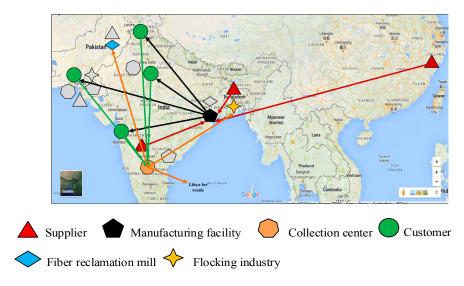


Figure 3. Economical supply chain network.

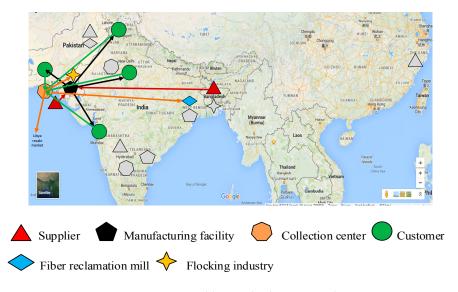


Figure 4. Sustainable supply chain network.

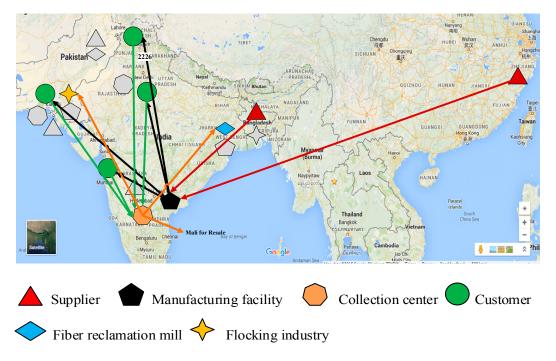


Figure 5. Resilient supply chain network.

The second step of the proposed solution methodology is to develop fuzzy membership function. The fuzzy membership functions for satisfaction level of each objective are given below.

$$\mu_{cost}(x) = \begin{cases} 0, & f_{cost} > 1,486,758.00 \\ \frac{1,486,758.00 - f_{cost}}{1,486,758.00 - 1,084,865.00}, & 1,084,865.00 < f_{cost} \le 1,486,758.00 \\ 1, & f_{cost} \le 1,084,865.00 \end{cases}$$

$$\mu_{sus}(x) = \begin{cases} 0, & f_{sus} > 307,944.90 \\ \frac{307,944.90 - f_{sus}}{307,944.90 - 280,782.30}, & 280,782.30 < f_{sus} \le 307,944.90 \\ 1, & f_{sus} \le 280,782.30 \end{cases}$$

$$\mu_{res}(x) = \begin{cases} 0, & f_{edc} > 331,000.70 \\ \frac{331,000.70 - f_{edc}}{331,000.70 - 287,975.10}, & 287,975.10 < f_{edc} \le 331,000.70 \\ 1, & f_{edc} \le 287,975.10 \end{cases}$$

The proposed model is solved using developed Fuzzy weighted method and results are compared with Werner's method (see Table 3). Results of Werner's method and proposed method show that the proposed method is more flexible as it also considered fuzzy importance level of objectives.

Table 3. Optimal results using Werner and proposed Fuzzy weighted methods.

Method	μ_{cost}	μ_{sus}	μ_{res}	Total Supply Chain Cost (\$)	Sustainability (KgCO ₂)	Resilience (\$)
Werner's Method	0.9918	0.1173	1.0000	1,088,161.00	304,759.50	287,975.10
Proposed Method	0.1018	0.9029	0.7561	1,445,828.00	283,419.90	298,468.50

Note: These optimal results are obtained at $\alpha = 0.9$, $\theta = 0.5$, $\omega_1' = 0.199$, $\omega_2' = 0.411$, and $\omega_3' = 0.390$.

4.3. Sensitivity Analysis

The details of the sensitivity analysis of proposed solution method are given in Table 4. The model is solved using the proposed fuzzy linguistic weight method by varying α and θ values. Figures 6–8

show the graphical representations of sensitivity analysis based on different α values, respectively. We assume that DMs reach a final solution at $\alpha=0.9$ and $\theta=0.7$ –0.9 (highlighted row) based on DMs preferences, which results in a supply chain network as shown in Figure 9. The final supply chain required to open a manufacturing facility in Kolkata and procure material from Shaoxing, China, and Dhaka suppliers. The optimal location for the collection center is Karachi where used products can be processed. The reusable products can be sent to Mali, Africa for donations. While the remaining used products will be sent to the flocking industry located at Karachi and reclamation mill located at Kolkata.

α	θ	μ_{cost}	μ_{sus}	μ_{res}	Operational Cost (\$)	Sustainability (KgCO ₂)	Resilience (\$)
	0.0-0.5	0.0868	0.8746	0.7640	1,588,538.00	384,441.10	422,511.00
0.4	0.6 - 0.9	0.8955	0.2389	0.8710	1,244,495.00	408,274.30	416,152.80
	1.00	0.8965	0.2389	0.6891	1,244,040.00	408,272.20	426,960.30
	0.0-0.5	0.09	0.8857	0.7609	1,530,208.00	343,699.70	371,470.40
0.6	0.6 - 0.9	0.8917	0.2292	0.8824	1,197,843.00	365,553.50	365,062.20
	1.00	0.8928	0.2292	0.6982	1,197,395.00	365,551.70	374,779.50
	0.0-0.5	0.1018	0.9029	0.7561	1,445,828.00	283,419.90	298,468.50
0.0	0.60	0.1065	0.8964	0.7561	1,443,965.00	283,595.30	298,468.50
0.9	0.7 - 0.9	0.8860	0.2142	0.9000	1,130,670.00	302,126.20	292,278.00
	1.00	0.8871	0.2143	0.7121	1,336,783.00	301,128.10	311,485.30

Table 4. Sensitivity analysis of proposed solution methodology.

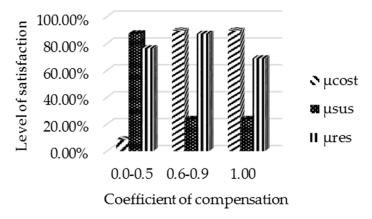


Figure 6. Achievement level of objectives at $\alpha = 0.40$.

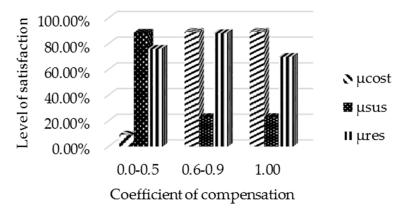


Figure 7. Achievement level of objectives at $\alpha = 0.60$.

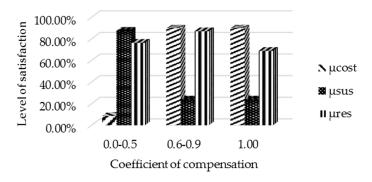


Figure 8. Achievement level of objectives at $\alpha = 0.90$.



Figure 9. Final Supply chain network based on DMs preferences with material flow in two periods.

5. Conclusions

This study focuses on developing sustainable and resilience supply chain network by considering economic, green, and resilience paradigm of supply chain. The research proposed a possibilistic fuzzy multi-objective programming-based approach to handle conflicting objectives, such as supply chain costs, carbon emissions, and resilience. The significant contribution of this research is the inclusion of a resilience factor based on Resilience Index, a data driven tool in the design of the sustainable supply chain network by considering nine major supply chain risks. Furthermore, a fuzzy-weighted Werner's interactive method based solution methodology is proposed to solve a possibilistic fuzzy multi-objective model. Thus, the mathematical model and solution methodology can provide a quality solution to decision makers. It is found from this research that disruption risks create chaotic situations for managers and managing shortages are a priority for them. During these disruption risks, managers try to use alternate sources to minimize shortages and losses, this decision leads to decline in sustainable performance due to possible increment in: (1) embodied carbon footprints; (2) transportation CO₂ emission; and (3) economic losses.

As this is the primary work of developing sustainable and resilient supply chain network design under stochastic and recognitive uncertainties using a possibilistic fuzzy programming approach, many possible future research avenues can be defined in this context. For example, this research utilizes the concept of expected disruption cost to measure resilience in supply chain network; it will be

valuable to consider other measures such as supply chain density and node criticality as the objective function. Furthermore, real-time GIS data can be utilized to calculate the probability disruption risks in various regions. The model can also be extended by incorporating different transportation modes and to consider road restrictions, for example, heavy trucks may not enter some roads.

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Conflicts of Interest: The authors declare no conflict of interest.

Appendix A

The costs of installation for a manufacturing facility and collection centers are estimated as shown in Tables A1 and A2, respectively. The installation costs are hypothetical data based on reasonable assumptions. Depending on the land value, machine installation cost, and labor wages, the cost of installation and production cost differ. Karachi is considered as the most expensive land value while Kolkata as most economical location. Similarly, production cost, material cost from each supplier, processing costs at fiber reclamation mills, flocking industry, and collection centers are set as shown in Tables A3–A6. It is assumed that most likely price of finished product is \$30. Capacities of potential manufacturing facilities are considered higher than total demand of customer zones, which will help to analyze centralized and decentralized network options. However, capacities of the potential supplier are considered less than total demand to analyze multi-sourcing strategies.

Table A1. Installation cost of manufacturing facility (\$).

Facility	Karachi	Hyderabad (India)	Kolkata
Manufacturing facility	900,000	800,000	600,000

Table A2. Installation cost of collection center (\$).

Facility	Karachi	Delhi	Hyderabad (India)
Collection center	300,000	400,000	250,000

Table A3. Production cost of product at potential manufacturing facilities (\$/unit).

Facility	Karachi		Hyderab	oad (India)	Kolkata	
Period	1	2	1	2	1	2
Manufacturing facility	15	15.44	12	12.28	10	9.74

Table A4. Material cost from potential suppliers and their production capacity (\$/unit).

Supplier Location	Kar	achi	ni Faisalabad		Hyderabad (India)		Dhaka		Shaoxing	
Period	1	2	1	2	1	2	1	2	1	2
Purchase cost	4.0	4.10	3.50	3.57	4.50	4.62	4.10	4.20	3.60	3.70

Table A5. Processing cost of product at potential recycling centers (\$/unit).

Facility Location	Kar	achi	Faisa	labad	Kol	kata	Dh	aka
Period	1	2	1	2	1	2	1	2
Reclamation mill		_	4.0	4.11	3.50	3.60	_	_
Flocking industry	3.50 3.58		_		_		2.50	2.56

Table A6. Processing cost of product at potential collection centers (\$/unit).

Location	Kaı	Karachi		Delhi	Hyderabad (India)		
Period	1	2	1	2	1	2	
Processing cost	4.0	4.12	5.50	5.63	4.50	4.60	

The probability of disruption risks at potential locations of suppliers, manufacturing facilities, and collection center are estimated using Resilience Index (RI) proposed by [12]. Resilience index and the normalized probability of disruption risk of potential locations are shown in Table A7. Higher resilience index score means a lesser probability of disruption risks and vice versa.

Table A7. RI and normalized probability of disruption risk of potential locations.

Region	Pal	cistan		Bangl	adesh	China			
Potential location	Karachi	Faisalabad	Hyderabad (India)	New Delhi Kolkata		Dhaka		Shaoxing	
Period	1	2	1	2		1	2	1	2
Resilience Index (0-100)	22.2	11.6	27.1	1	19.2		21.1	45.3	32.2
Relative Probability of disruption risks	0.2815	0.2798	0.2637	0.2558		0.2569	0.2498	0.1979	0.2146

Transportation costs between potential locations of suppliers, manufacturing facilities, customer zone, collection centers, flocking industry, fiber reclamation mills, and resale markets are shown in Tables A8 and A9 for period 1 and period 2, respectively. Transportation costs between potential locations are estimated based on the single product (Jeans Trouser). It is estimated that 8800 units of product can be loaded per TEU. The unit transportation costs are estimated using Google map for the shortest distance between locations, also using available transportation routes search (available from SeaRates [19]) and by gathering quotation from transportation companies. The truck-water freights are considered for cross-border shipping, commonly called Fishy-back transportation method.

Table A8. Unit transportation cost between potential locations in period 1 (\$/unit).

Potential Location	Karachi	Faisalabad	Lahore	Hyderabad (India)	Kolkata	New Delhi	Mumbai	Dhaka	Shaoxing	Mali	Sabha
Karachi	_	0.1679	0.1808	0.2752	0.3511	0.2551	0.0891	0.1311	0.1608	0.2322	0.3043
Faisalabad	0.1679	_	0.0463	0.2807	0.2811	0.1030	0.2352	0.2704	0.2985	_	_
Lahore	0.1808	0.0463	_	0.1985	0.2543	0.0891	0.2241	0.2833	0.3115	_	_
Hyderabad (India)	0.2752	0.2807	0.1985	_	0.1985	0.2062	0.1072	0.1546	0.3039	0.3878	0.3868
Kolkata	0.3511	0.2811	0.2543	0.1985	_	0.1972	0.2585	0.0948	0.2129	_	_
New Delhi	0.2551	0.1030	0.0891	0.2062	0.1972	_	0.1886	0.2073	0.3567	0.4475	0.5221
Mumbai	0.0891	0.2352	0.2241	0.1072	0.2585	0.1886	_	0.0952	0.2133	_	_
Dhaka	0.1311	0.2704	0.2833	0.1546	0.0948	0.2073	0.0952	_	0.1425	_	_
Shaoxing	0.1608	0.2985	0.3115	0.3039	0.2129	0.3567	0.2133	0.1425	_	_	_

Table A9. Unit transportation cost between potential locations in period 2 (\$/unit).

Potential Location	Karachi	Faisalabad	Lahore	Hyderabad (India)	Kolkata	New Delhi	Mumbai	Dhaka	Shaoxing	Mali	Sabha
Karachi	_	0.1714	0.1767	0.2675	0.3613	0.2486	0.0872	0.1349	0.1569	0.2275	0.2982
Faisalabad	0.1714	_	0.0453	0.2728	0.2893	0.1004	0.2302	0.2783	0.2913	_	_
Lahore	0.1767	0.0453	_	0.1929	0.2617	0.0868	0.2194	0.2916	0.3040	_	_
Hyderabad (India)	0.2675	0.2728	0.1929	_	0.2043	0.2009	0.1049	0.1591	0.2966	0.3769	0.3759
Kolkata	0.3613	0.2893	0.2617	0.2043	_	0.1922	0.2530	0.0976	0.2078	_	_
New Delhi	0.2486	0.1004	0.0868	0.2009	0.1922	_	0.1846	0.2133	0.3481	0.4361	0.5088
Mumbai	0.0872	0.2302	0.2194	0.1049	0.2530	0.1846	_	0.0980	0.2082	_	_
Dhaka	0.1349	0.2783	0.2916	0.1591	0.0976	0.2133	0.0980	_	0.1391	_	_
Shaoxing	0.1569	0.2913	0.3040	0.2966	0.2078	0.3481	0.2082	0.1391	_	_	_

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To estimate the environment impact from supply chain operations, CO₂ emission during production, recycling, and transportation of product are estimated. It is estimated that a pair of Jeans produces 33.4 kg of CO₂ during its life cycle, out of which 40% accounts only for production and packaging process, 9% of raw material production, and 3% in recycling or landfill [21]. In this case, CO₂ emissions during production at different locations are set as shown in Table A10. The CO₂ emission per capita is used as a basis to differentiate the total emission at different locations. CO₂ emission per capita is collected from World Bank data [22].

 CO_2 emission during transportation is estimated from CO_2 emission index using cargo router calculator (CargoRouter [20]). CO_2 emission index defined as the amount of CO_2 released per unit of gaseous, liquid and solid fuels used [23], it is estimated in grams of CO_2 released. Tables A11–A13 represent the embodied carbon footprints, CO_2 emission during processing at collection centers, and CO_2 emission during the recycling process. Table A14 shows the CO_2 emission during transportation between potential locations based on distance traveled and mode of transportation used.

Table A10. CO₂ emission during production (kgCO₂/unit).

Facility	Kar	achi	Hyderab	ad (India)	Kolkata		
Period	1	2	1	2	1	2	
Emission during production	12.66	12.92	13.65	14.05	13.96	13.55	

Table A11. Embodied carbon footprints of material coming from supplier (kgCO₂/unit).

Supplier Location	Karachi		Faisalabad		Hyderaba	Dh	aka	Shaoxing		
Period	1	2	1	2	1	2	1	2	1	2
carbon footprints	3.0	2.94	3.30	3.37	3.50	3.00	2.80	2.74	3.80	3.70

Table A12. CO₂ emission during processing at collection centers (kgCO₂/unit).

Location	Karachi		New	Delhi	Hyderabad (India)		
Period	1	2	1	2	1	2	
CO ₂ emission	0.90	0.82	1.0	0.97	1.30	1.27	

Table A13. CO₂ emission during recycling process (kgCO₂/unit).

Location	Karachi		Faisalabad		Kolkata		Dhaka	
Period	1	2	1	2	1	2	1	2
Reclamation mill	_	_	1.0	1.02	1.30	1.27	_	_
Flocking industry	0.90	0.82	-	_	-	_	1.0	1.02

Table A14. Carbon emission between potential locations in period 1 and period 2 (kgCO₂/unit).

Potential Location	Karachi	Faisalabad	Lahore	Hyderabad (India)	Kolkata	New Delhi	Mumbai	Dhaka	Shaoxing
Karachi	_	21.0×10^{-5}	23.1×10^{-5}	33.0×10^{-5}	49.1×10^{-5}	24.4×10^{-5}	2.7×10^{-5}	10.1×10^{-5}	29.5×10^{-5}
Faisalabad	21.0×10^{-5}	_	2.7×10^{-5}	37.3×10^{-5}	40.6×10^{-5}	11.3×10^{-5}	31.2×10^{-5}	30.6×10^{-5}	49.7×10^{-5}
Lahore	23.1×10^{-5}	2.7×10^{-5}	_	36.7×10^{-5}	38.5×10^{-5}	9.5×10^{-5}	31.7×10^{-5}	32.6×10^{-5}	51.8×10^{-5}
Hyderabad (India)	33.0×10^{-5}	37.3×10^{-5}	36.7×10^{-5}	_	26.7×10^{-5}	28.4×10^{-5}	14.0×10^{-5}	17.4×10^{-5}	29.8×10^{-5}
Kolkata	49.1×10^{-5}	40.6×10^{-5}	26.7×10^{-5}	26.7×10^{-5}	_	29.4×10^{-5}	37.5×10^{-5}	5.5×10^{-5}	22.3×10^{-5}
New Delhi	24.4×10^{-5}	11.3×10^{-5}	9.5×10^{-5}	28.4×10^{-5}	29.4×10^{-5}	_	26.3×10^{-5}	32.1×10^{-5}	49.3×10^{-5}
Mumbai	2.7×10^{-5}	31.2×10^{-5}	11.3×10^{-5}	14.0×10^{-5}	37.5×10^{-5}	26.3×10^{-5}	_	$8.4 imes 10^{-5}$	27.8×10^{-5}
Dhaka	10.1×10^{-5}	30.6×10^{-5}	32.6×10^{-5}	17.4×10^{-5}	5.5×10^{-5}	32.1×10^{-5}	$8.4 imes 10^{-5}$	_	23.0×10^{-5}
Shaoxing	29.5×10^{-5}	49.7×10^{-5}	51.8×10^{-5}	29.8×10^{-5}	22.3×10^{-5}	49.3×10^{-5}	27.8×10^{-5}	23.0×10^{-5}	_

Finally, the importance of objectives based on decision makers' preferences is given in Table A15. The demand of new products at different customer zones and percentage of used products recovered from these customer zones are assumed as shown in Table A16. Reusable products are assumed to be donated to NGOs in Sabha, Libya and Mali, Africa markets.

Table A15. Importance of objectives based on decision makers preferences.

Objective Functions	D	ecision Mak	er Preferenc	es	Fuzzy Calculations				
Objective Functions	DM1	DM2	DM3	DM4	AFN	FW	NFW		
Cost	ML	L	MH	L	(0.200,0.350,0.500)	0.350	0.199		
Sustainability	MH	H	MH	H	(0.575, 0.725, 0.875)	0.725	0.411		
Resilience	Н	M	MH	Н	(0.538, 0.688, 0.838)	0.688	0.390		

Note: AFN = Aggregate fuzzy number, NFN = Normalized fuzzy number, NFW = Normalized fuzzy weight.

Table A16. Demand of products at customer zones and percentage of used products recovered.

Location	Karachi		Lahore		New	Delhi	Hyderabad (India)	
Period	1	2	1	2	1	2	1	2
Demands (units)	4000	4105	3000	3086	2500	2425	2000	2056
Percent of recovered used products	57%	59%	51%	52%	55%	57%	52%	53%

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