

S1. EEP Model rules and evaluation. The model was trained on 6120 points and tested on 1530 additional points. It consists of 6 rules. The AEP (GSNDVI) served as a dependent variable, while site potential (Sitepot); precipitation (ppt); minimum, maximum and mean temperature (tmin, tmax, tmean) in various seasons served as the explanatory variables.

Cubist [Release 2.07 GPL Edition] Fri May 11 13:18:54 2018

Options:

Application `GSNDVI`
Use 80% of data for training
Maximum of 6 rules
Permit extrapolation of 10%

Target attribute `GSNDVI`

Read 6120 cases (29 attributes) from GSNDVI.data

Model:

Rule 1: [1379 cases, mean 133.5, range 121 to 143, est err 1.5]

```
if
  pptsummersum <= 226
  Sitepot <= 139
then
  GSNDVI = 100.4 + 0.76 Sitepot + 0.0291 pptsummersum + 0.017 pptspringsum
          - 0.23 tmeansummer + 0.041 pptwintersum - 0.61 tminsummeravg
          + 0.17 tmeanwinter + 0.21 tminspringavg + 0.007 pptprevfallsum
          - 0.08 tmeanspring - 0.09 tmaxsummeravg
```

Rule 2: [934 cases, mean 136.6, range 126 to 144, est err 1.4]

```
if
  pptsummersum > 226
  Sitepot <= 139
then
  GSNDVI = -23.6 + 0.92 Sitepot + 0.0622 pptsummersum + 0.053 pptwintersum
          + 0.013 pptspringsum + 0.3 tmaxspringavg - 0.35 tminspringavg
          + 0.16 tmeanwinter
```

Rule 3: [1324 cases, mean 138.4, range 126 to 166, est err 2.0]

```
if
  pptsummersum <= 188
  Sitepot > 139
then
  GSNDVI = 97.1 + 0.95 Sitepot - 0.71 tmeansummer + 0.0265 pptsummersum
          + 0.02 pptspringsum + 0.026 pptprevfallsum - 0.2 tmaxspringavg
          + 0.3 tminspringavg + 0.016 pptwintersum - 0.22 tminsummeravg
```

Rule 4: [612 cases, mean 141.8, range 129 to 161, est err 1.5]

```
if
  tmaxspringavg > 116
  pptwintersum <= 48
  pptsummersum > 188
then
  GSNDVI = 78 + 0.96 Sitepot - 0.96 tmeansummer + 0.126 pptwintersum
           + 0.0348 pptsummersum - 0.73 tmaxspringavg + 0.37 tmeanspring
           + 0.78 tminsummeravg - 0.46 tminspringavg + 0.27 tmaxsummeravg
```

Rule 5: [1117 cases, mean 142.4, range 126 to 163, est err 1.5]

```
if
  pptwintersum > 48
  pptsummersum > 188
then
  GSNDVI = -20.1 + 1.01 Sitepot + 0.0271 pptsummersum + 0.014 pptspringsum
           + 0.4 tminspringavg + 0.26 tmeanwinter - 0.34 tminsummeravg
           - 0.07 tmeansummer - 0.07 tmeanspring
```

Rule 6: [1186 cases, mean 142.6, range 133 to 173, est err 1.6]

```
if
  tmaxspringavg <= 116
  pptwintersum <= 48
  pptsummersum > 188
  Sitepot > 139
then
  GSNDVI = -34.1 + 0.92 Sitepot + 0.0323 pptsummersum + 0.081 pptwintersum
           + 0.33 tminspringavg + 0.09 tmeansummer - 0.11 tmaxspringavg
           + 0.03 tmeanspring
```

Evaluation on training data (6120 cases):

Average error	1.6
Relative error	0.36
Correlation coefficient	0.93

Attribute usage:

Conds Model

100%	100%	pptsummersum
74%	100%	Sitepot
44%	83%	pptwintersum
27%	62%	tmaxspringavg
100%		tminspringavg
86%		tmeansummer
73%		pptspringsum

68%	tminsummeravg
66%	tmeanspring
52%	tmeanwinter
41%	pptprevfallsum
30%	tmaxsummeravg

Evaluation on test data (1530 cases):

Average error	1.5
Relative error	0.36
Correlation coefficient	0.93

S2. Predictive model rules and evaluation. The model was trained on 1280 points and tested on 320 additional points. The model was created with 3-member committee models. The BP (Productivity) served as a dependent variable, while site potential (Site_potential), 3-month SPI (SPI3m), USDM percentile index (USDM), 3-month EDDI, and 3-month ESI in various seasons served as the explanatory variables.

Cubist [Release 2.07 GPL Edition] Wed Jul 17 14:48:11 2019

Options:

Application 'Drought_productivity'
Use 80% of data for training
Permit extrapolation of 10%
3-member committee model

Target attribute 'Productivity'

Replacing unknown attribute values:

'ESI_spring' by -0.0013221
'ESI_summer' by -0.0164259

Read 1280 cases (23 attributes) from Drought_productivity.data

Model 1:

Rule 1/1: [194 cases, mean 2068.5039, range 852.496 to 3137.27, est err 135.2723]

if

SPI3m_spring <= 0.1999029
USDM_winter <= 550
USDM_prev_year > 597
EDDI_spring <= 1.59609
Site_potential <= 148

then

Productivity = -10614.0833 USDM_prev_year - 0.053 USDM_winter
+ 0.16 USDM_spring + 0.07 SPI3m_winter + 106 SPI3m_spring
+ 208 EDDI_spring - 12 ESI_spring + 45 Site_potential + 92

Rule 1/2: [143 cases, mean 2097.0156, range 753.131 to 3037.53, est err 133.0036]

if

EDDI_spring > 1.59609
SPI3m_spring <= 0.199029
Site_potential <= 148

then

Productivity = -9205.5039 - 685 EDDI_spring + 90 Site_potential
- 95 EDDI_winter - 0.048 USDM_prev_year + 32 SPI3m_spring
+ 25 SPI3m_winter + 0.07 USDM_winter + 0.04 USDM_spring
+ 9 ESI_winter + 9 ESI_spring

Rule 1/3: [19 cases, mean 2242.9153, range 1171.72 to 3156.42, est err 189.9274]

if

SPI3m_spring > 0.199029
EDDI_spring > 1.3083
Site_potential <= 148
then
Productivity = -7251.5629 - 1341 EDDI_spring + 84 Site_potential
+ 0.05 USDM_winter - 0.012 USDM_prev_year + 10 ESI_spring
+ 9 SPI3m_winter + 8 SPI3m_spring

Rule 1/4: [113 cases, mean 2296.8665, range 1150.59 to 3145.19, est err 130.9743]

if
USDM_winter <= 52
SPI3m_spring > 0.199029
Site_potential <= 148
then
Productivity = -11123.9837 + 95 Site_potential + 115 SPI3m_winter
+ 58 ESI_spring

Rule 1/5: [163 cases, mean 2397.5527, range 1102.54 to 3269.18, est err 149.1111]

if
USDM_winter > 550
SPI3m_spring <= 0.199029
EDDI_spring <= 1.59609
Site_potential <= 148
then
Productivity = -12753.9924 + 101 Site_potential + 1.4 USDM_winter
+ 308 SPI3m_spring + 0.33 USDM_spring + 54 EDDI_winter
+ 24 ESI_winter + 25 SPI3m_winter - 0.018 USDM_prev_year
+ 9 ESI_spring

Rule 1/6: [140 cases, mean 2457.7271, range 1448.69 to 4272.75, est err 117.9184]

if
USDM_prev_year <= 597
SPI3m_spring <= 0.199029
then
Productivity = -9867.5861 + 87 Site_potential + 106 EDDI_winter

Rule 1/7: [531 cases, mean 2486.3311, range 1349.32 to 3534.35, est err 147.6671]

if
USDM_winter > 52
SPI3m_spring > 0.199029
EDDI_spring <= 1.3083
Site_potential <= 148
then
Productivity = -11655.8142 + 99 Site_potential + 0.29 USDM_winter
+ 52 SPI3m_winter + 50 EDDI_spring + 33 EDDI_winter
+ 0.04 USDM_spring + 6 ESI_spring

Rule 1/8: [17 cases, mean 3385.1152, range 2829.53 to 4305.53, est err 229.2913]

```

if
  ESI_spring <= -0.32557
  Site_potential > 148
then
  Productivity = -3768.1619 + 47 Site_potential + 0.56 USDM_winter
    - 0.152 USDM_prev_year + 115 ESI_winter + 92 SPI3m_winter

    + 81 ESI_spring

```

Rule 1/9: [32 cases, mean 3865.9429, range 3226.99 to 4660.15, est err 139.7003]

```

if
  ESI_spring > -0.32557
  Site_potential > 148
then
  Productivity = -4124.1562 + 50 Site_potential + 0.34 USDM_winter
    - 0.007 USDM_prev_year

```

Model 2:

Rule 2/1: [98 cases, mean 2138.9900, range 1448.69 to 2660.75, est err 143.5833]

```

if
  USDM_prev_year <= 811
  SPI3m_spring <= 0.263186
  Site_potential <= 142
then
  Productivity = -7766.5643 - 1.157 USDM_prev_year + 75 Site_potential
    - 75 EDDI_winter

```

Rule 2/2: [165 cases, mean 2150.2087, range 753.131 to 4063.96, est err 192.3959]

```

if
  EDDI_spring > 1.55568
then
  Productivity = -8087.8481 - 0.473 USDM_prev_year + 74 Site_potential
    + 1 USDM_spring + 22 SPI3m_winter - 19 EDDI_spring
    + 15 SPI3m_spring + 8 ESI_spring

```

Rule 2/3: [380 cases, mean 2305.0908, range 852.496 to 4305.53, est err 159.2865]

```

if
  USDM_prev_year > 811
  SPI3m_spring <= 0.263186
  EDDI_spring <= 1.55568
then
  Productivity = -8876.3348 + 80 Site_potential + 180 SPI3m_spring
    + 99 SPI3m_winter + 0.34 USDM_spring
    - 0.097 USDM_prev_year + 45 ESI_spring

```

Rule 2/4: [643 cases, mean 2493.9519, range 1150.59 to 4660.15, est err 166.8486]

```

if

```

SPI3m_spring > 0.263186
then
Productivity = -10346.8617 + 89 Site_potential + 0.43 USDM_spring
+ 67 EDDI_winter + 0.08 USDM_winter
- 0.021 USDM_prev_year + 14 ESI_spring + 12 SPI3m_spring
+ 8 SPI3m_winter

Rule 2/5: [532 cases, mean 2795.2405, range 1670.23 to 4660.15, est err 166.9139]

if
Site_potential > 142
then
Productivity = -7873.809 + 73 Site_potential + 0.61 USDM_winter
+ 140 SPI3m_winter + 112 ESI_spring
- 0.108 USDM_prev_year + 84 SPI3m_spring - 46 EDDI_winter

- 0.18 USDM_spring

Model 3:

Rule 3/1: [119 cases, mean 1936.8162, range 852.496 to 3567.14, est err 135.2686]

if
SPI3m_spring <= -1.18148
EDDI_spring <= 1.64678
then
Productivity = -10905.0495 + 88 Site_potential + 186 EDDI_winter
- 126 ESI_winter - 53 ESI_spring + 0.2 USDM_winter
+ 40 SPI3m_spring + 0.12 USDM_spring
- 0.033 USDM_prev_year + 10 SPI3m_winter

Rule 3/2: [12 cases, mean 2060.9275, range 1171.72 to 3110.11, est err 349.3818]

if
SPI3m_spring > 0.199029
EDDI_spring > 1.49562
then
Productivity = -4434.6249 - 2575 EDDI_spring + 80 Site_potential
+ 0.04 USDM_winter + 6 ESI_spring

Rule 3/3: [387 cases, mean 2120.4473, range 753.131 to 3185.77, est err 136.2435]

if
SPI3m_winter <= -0.26115
Site_potential <= 148
then
Productivity = -10899.6928 + 94 Site_potential - 0.27 USDM_prev_year
+ 0.66 USDM_spring - 98 EDDI_winter

Rule 3/4: [158 cases, mean 2144.1140, range 753.131 to 4063.96, est err 160.3739]

if
EDDI_spring > 1.64678

then

$$\begin{aligned} \text{Productivity} = & -8780.0565 - 1454 \text{ EDDI_spring} + 96 \text{ Site_potential} \\ & - 194 \text{ EDDI_winter} + 0.161 \text{ USDM_prev_year} \\ & + 47 \text{ SPI3m_spring} + 0.12 \text{ USDM_winter} + 26 \text{ SPI3m_winter} \\ & + 13 \text{ ESI_winter} \end{aligned}$$

Rule 3/5: [211 cases, mean 2380.5793, range 1249.96 to 3269.18, est err 168.2369]

if

$$\begin{aligned} & \text{USDM_winter} > 195 \\ & \text{SPI3m_spring} > -1.18148 \\ & \text{SPI3m_spring} \leq 0.199029 \\ & \text{EDDI_spring} \leq 1.64678 \\ & \text{Site_potential} \leq 148 \end{aligned}$$

then

$$\begin{aligned} \text{Productivity} = & -12950.6832 + 107 \text{ Site_potential} + 352 \text{ SPI3m_spring} \\ & + 1.07 \text{ USDM_winter} - 0.19 \text{ USDM_prev_year} \\ & + 116 \text{ SPI3m_winter} + 0.13 \text{ USDM_spring} \end{aligned}$$

Rule 3/6: [125 cases, mean 2417.6711, range 1029.49 to 4272.75, est err 175.0032]

if

$$\begin{aligned} & \text{USDM_winter} \leq 195 \\ & \text{SPI3m_spring} \leq 0.199029 \\ & \text{EDDI_spring} \leq 1.64678 \end{aligned}$$

then

$$\begin{aligned} \text{Productivity} = & -11455.3714 + 100 \text{ Site_potential} - 0.98 \text{ USDM_winter} \\ & - 156 \text{ EDDI_winter} + 23 \text{ SPI3m_spring} \\ & - 0.019 \text{ USDM_prev_year} + 11 \text{ ESI_spring} + 12 \text{ SPI3m_winter} \end{aligned}$$

Rule 3/7: [87 cases, mean 2512.9185, range 1526.31 to 3269.18, est err 182.9935]

if

$$\begin{aligned} & \text{USDM_prev_year} > 2575 \\ & \text{SPI3m_spring} \leq 0.199029 \\ & \text{EDDI_spring} \leq 1.64678 \\ & \text{Site_potential} \leq 148 \end{aligned}$$

then

$$\begin{aligned} \text{Productivity} = & -14455.6019 + 122 \text{ Site_potential} - 216 \text{ SPI3m_winter} \\ & + 90 \text{ EDDI_winter} + 0.1 \text{ USDM_winter} + 22 \text{ SPI3m_spring} \\ & + 0.07 \text{ USDM_spring} - 0.013 \text{ USDM_prev_year} \end{aligned}$$

Rule 3/8: [461 cases, mean 2518.8743, range 1150.59 to 3534.35, est err 165.2857]

if

$$\begin{aligned} & \text{SPI3m_winter} > -0.26115 \\ & \text{SPI3m_spring} > 0.199029 \\ & \text{EDDI_spring} \leq 1.49562 \\ & \text{Site_potential} \leq 148 \end{aligned}$$

then

$$\begin{aligned} \text{Productivity} = & -12552.8688 + 106 \text{ Site_potential} + 172 \text{ EDDI_spring} \\ & + 0.08 \text{ USDM_prev_year} \end{aligned}$$

Rule 3/9: [28 cases, mean 3602.6821, range 2874.71 to 4272.75, est err 256.8739]

```
if
  USDM_winter <= 565
  Site_potential > 148
then
  Productivity = -366.869 - 0.73 USDM_winter + 27 Site_potential
               - 35 EDDI_winter
```

Rule 3/10: [21 cases, mean 3827.7156, range 2829.53 to 4660.15, est err 317.8513]

```
if
  USDM_winter > 565
  Site_potential > 148
then
  Productivity = -12229.7738 + 14.92 USDM_winter + 710 SPI3m_winter
               + 41 Site_potential - 143 EDDI_winter
```

Evaluation on training data (1280 cases):

Average error	129.8323
Relative error	0.31
Correlation coefficient	0.95

Attribute usage:

Conds Model

72%	61%	SPI3m_spring
64%	100%	Site_potential
58%	35%	EDDI_spring
29%	64%	USDM_winter
19%	82%	USDM_prev_year
18%	76%	SPI3m_winter
1%	66%	ESI_spring
	74%	USDM_spring
	66%	EDDI_winter
	13%	ESI_winter

Evaluation on test data (320 cases):

Average error	143.6743
Relative error	0.32
Correlation coefficient	0.95