



Article A Combination of Lie Group Machine Learning and Deep Learning for Remote Sensing Scene Classification Using Multi-Layer Heterogeneous Feature Extraction and Fusion

Chengjun Xu^{1,2,*}, Guobin Zhu² and Jingqian Shu¹

- ¹ School of Software, Jiangxi Normal University, Nanchang 330022, China; 005627@jxnu.edu.cn
- ² School of Remote Sensing and Information Engineering, Wuhan University, Wuhan 430072, China; gbzhu@whu.edu.cn
- * Correspondence: 2018102160001@whu.edu.cn

Abstract: Discriminative feature learning is the key to remote sensing scene classification. Previous research has found that most of the existing convolutional neural networks (CNN) focus on the global semantic features and ignore shallower features (low-level and middle-level features). This study proposes a novel Lie Group deep learning model for remote sensing scene classification to solve the above-mentioned challenges. Firstly, we extract shallower and higher-level features from images based on Lie Group machine learning (LGML) and deep learning to improve the feature representation ability of the model. In addition, a parallel dilated convolution, a kernel decomposition, and a Lie Group kernel function are adopted to reduce the model's parameters to prevent model degradation and over-fitting caused by the deepening of the model. Then, the spatial attention mechanism can enhance local semantic features and suppress irrelevant feature information. Finally, feature-level fusion is adopted to reduce redundant features and improve the classification accuracy of the model. Comparative experiments on three public and challenging large-scale remote-sensing datasets show that our model improves the discriminative ability of features and achieves competitive accuracy against other state-of-the-art methods.

Keywords: deep learning; feature representation; Lie Group machine learning; remote sensing scene classification

1. Introduction

Remote sensing images are a valuable data source and the basis for Earth exploration and observation [1]. With the rapid development of remote sensing satellites and technologies, a large number of spectral- and spatial-information-rich Earth observation images can be obtained by airborne or spaceborne sensors, namely, high-resolution remote-sensing images (HRRSI). These HRRSIs can help us better observe and measure the detailed structure of Earth's surface. It is particularly urgent to make full use of the ever-increasing HRRSIs for intelligent Earth observation [2]; therefore, it is extremely important to effectively interpret the large and complex HRRSI.

As one of the most representative research areas in HRRSI interpretation, the scene classification of remote sensing images is also an active research field. Scene classification of remote sensing images aims to classify HRRSI into various semantic categories [1]. In recent years, it has attracted a lot of attention [3], and is widely used in geospatial target detection [4,5], natural hazards detection [6], urban planning [7], and especially remote-sensing image interpretation [1].

Compared to ground-scene target classification, the scene classification of remote sensing images is still a challenging research topic due to the following characteristics:

1. Large variance in object/scene scales: In remote sensing imaging, different sensors in different platforms work at different altitudes. However, different sensors



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). on the same platform work at the same altitude [8]. With the examples illustrated in Figure 1a, the scenes of airplanes, airports, and thermal power stations have huge scale differences at different imaging altitudes and contain a lot of useless background information. Previous research has shown that deeper network models can be used to extract more valuable feature information [9];

- 2. The complex spatial arrangement, object distribution, and the coexistence of multiple ground objects: As the spatial distribution and arrangement of ground objects are complex and diverse, and remote sensing imaging equipment has a wide bird-eye perspective, it is quite common to include multiple ground objects in HRRSIs. HRRSIs are filled with many key objects, which makes it even more difficult to classify scenarios. As shown in Figure 1b, the scenes of freeways contain trees, cars, bridges, etc. The scenes of ground track fields include roads, swimming pools, and trees. Possible solutions include enhanced local semantic representation of scenarios [9] and approaches that are robust to changes in direction are usually appropriate [10];
- 3. High interclass similarity. The existence of the same object between different scenarios or the high semantic overlap between scene categories results in between-class similarity, which can be extremely difficult to distinguish between these scenes. For example, in Figure 1c, sparse residential, medium residential, and dense residential areas all contain the same ground objects, namely, houses and trees. The bridge and overpass scenarios also contain the same ground object, namely, bridges. Recent studies have shown that although deep convolutional features are utilized for semantic feature representation, the fusion of shallower (low-level and middle-level features) can make features more discriminative [11,12].

With the rapid development of deep learning, scholars have proposed many convolutional neural network models (CNN), such as LGRIN [12]. Some improved networks have also achieved state-of-the-art performance [10,12,13]. The success of CNN models demonstrates that high-level features can be used to describe scenes better than low-level and middle-level features [14,15]. Nevertheless, the following problems remain:

- Loss of shallower features (low-level and middle-level features): Commonly used CNN models cannot preserve shallower features during the training process [8]. In addition, when CNN models go deeper, models tend to lose shallower features [16]. However, these shallower features help to enhance the ability of scene representation and improve the accuracy of classification. Some recently proposed approaches for preserving shallower features are not end-to-end [15,17], as it is difficult to adapt to different application scenarios;
- 2. Lack of local semantic features: Since most CNN models utilize the last connection layer as the global feature representation to complete scene classification [18,19], the local regional features of images are ignored. Two remote sensing images with different global structures may belong to the same category because they contain some obvious and same target objects [20]. However, some models only use global semantics to discriminate, which will reduce the accuracy of classification [9];
- 3. Insufficient consideration is given to the correlation between features: Since a certain feature tends to represent the image from one aspect and ignores other feature information, complementary features are usually used to make up for the missing features [21–23]. However, how to select and represent features is still one of the main research topics in the field of machine learning. Serial features and parallel features are two typical methods [24]. However, these methods do not fully consider the correlation between features, leading to feature redundancy, increasing the complexity of calculation, and are not very effective for scene classification.

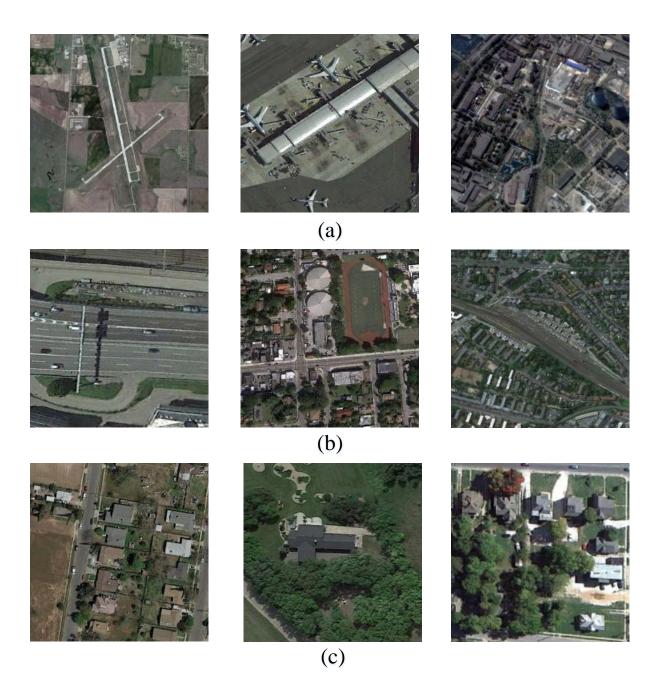


Figure 1. Challenges of HRRSI: (**a**) large variance in object/scene scales; (**b**) complex spatial arrangement, object distribution, and the coexistence of multiple ground objects; (**c**) high interclass similarity. The images are from the NWPU dataset [25].

To address the above problems, in this study, we propose a novel Lie Group deep learning model based on attention mechanisms. The goals include the following.

- 1. Preserve shallower features: Most CNN models cannot preserve shallower features. In addition, the existing methods for preserving shallower features are not flexible end-to-end frameworks [15,17]. Our model involves an end-to-end network to preserve the features of different levels (low-level, middle-level, and high-level) and effectively improve the classification accuracy of the model;
- 2. Enhance local semantic features: Most existing CNN models usually combine local domain filters (average or maximum feature value), which limits the representation of local semantics [25–27]. Our model should have the ability to improve the representation of key features;

3. Enhance feature representation and improve computing performance: Although some methods utilize both local and global features as the final representation [10], they do not consider the interrelation between different features in the HRRSIs. Therefore, our model should consider the relationship between different features and reduce the parameters of the model to improve the computational performance and ensure effective HRRSI feature extraction.

The main contributions of this paper are as follows:

- A novel efficient HRRSI scene classification model: The Lie Group deep learning (LGDL) model based on an attention mechanism can effectively improve the ability of scene feature representation, the accuracy of scene classification, and can better classify complex scenes. Considering the characteristics of HRRSIs, LGDL utilizes Lie Group machine learning (LGML) to preserve the shallower features (low-level and middle-level features) of HRRSIs, such as scale-invariant feature transform (SIFT) [28] and local binary patterns (LBP) [29]. In addition, deep learning is used to extract highlevel semantic features of HRRSI. Finally, automatic scene learning is implemented based on the fused multi-source heterogeneous features;
- 2. The spatial attention mechanism is used to suppress the weight of irrelevant feature information to improve the ability of local key semantic features. Compared with the maximum pooling and mean operation used in the traditional model, our method improves and enhances the ability of local semantic representation. To deal with HRRSIs in complex scenes, we utilize parallel dilated convolution to enrich scale feature information and utilize kernel decomposition to increase the number of skip connections and reduce the difficulty of training deeper models;
- 3. The Lie Group covariance feature matrix is introduced to represent the extracted shallower features. The feature matrix is a real symmetric matrix, which fully considers the correlation between shallower features and has good computing performance and anti-noise ability. Features of different levels (low-level, middle-level, and high-level) and different spaces are integrated through efficient feature-level fusion. This method fully considers the correlation between features of different layers, avoids feature redundancy and reduces feature dimension, enhances the feature representation ability, and maintains a good computing performance.

The rest of this paper is arranged as follows. Section 2 outlines the existing literature related to scene classification, LGML, and the attention mechanism. Section 3 describes our proposed model in detail. Section 4 evaluates the proposed model against various state-of-the-art models on three public and challenging scene datasets and performs ablation experiments. Finally, conclusions are provided in Section 5.

2. Related Work

In this section, we review some related works of scene classification, LGML, and attention mechanisms.

2.1. Scene Classification Methods

From the perspective of feature extraction and learning, remote sensing scene classification methods are mainly divided into low-level, middle-level, and high-level feature methods. It is worth noting that these three feature methods are not necessarily independent of each other.

2.1.1. Methods Based on Low-Level Features

In the early stage of remote sensing scene classification, scholars extracted a series of low-level features according to the characteristics of remote sensing images, such as SIFT [28], LBP [29], and color histograms (CH) [30]. In fact, the above features are not independent of each other, and the fusion of various features has achieved good results in remote sensing scene classification [31]. However, the above features rely heavily on the prior

knowledge of experts [20]. It is difficult for them to achieve optimum performance in complex scenarios.

2.1.2. Methods Based on Middle-Level Features

To address the shortcomings of the low-level feature method, scholars have proposed a method based on middle-level features, which encoded the above features to obtain higher-order statistical mode, extract more important features in the image, and establish global representation. Typical methods are bag-of-visual-words (BoVW) [32] and probabilistic topic models (PTM) [33] (i.e., probabilistic latent semantic analysis (PLSA) [34] and latent Dirichlet allocation (LDA) [33]). However, this method also has shortcomings: It ignores the correlation between features [35,36], and the feature selection and design also rely on expert domain knowledge, etc.

2.1.3. Methods Based on High-Level Features

In recent years, the deep learning model has profoundly improved the performance of remote sensing scene classification [37–41]. Typical models include CNNs [42], generative adversarial networks (GAN) [43], and autoencoders [44]. Compared with the above two methods, the deep learning model can extract more high-level features and obtain better classification performance [12,45]. This kind of deep learning model usually adopts an autonomous learning feature of a multi-layer network structure and regards the remote sensing scene classification as an end-to-end problem [46].

2.2. Lie Group Machine Learning (LGML)

LGML is a novel branch of the machine learning knowledge system, which has the advantage of a manifold structure and forms a new learning paradigm based on the idea of Lie Groups [47]. Xu et al. [20] proposed a new algorithm based on Lie Group intrinsic mean, deduced the Lie Group kernel function, which can be applied to both matrix and vector data samples, and achieved good results in remote sensing scene datasets. Later, Xu et al. [48] improved the algorithm to further improve the classification accuracy of the model and reduce the number of parameters of the model. Xu et al. [12] proposed a novel scene classification model jointly represented by Lie Group and CNN, which further improved the accuracy of scene classification and the interpretability of the model from the perspective of LGML. Compared with traditional methods, the LGML method does not lose too much image information. Lin et al. [49] utilized the Lie Group Lie Algebra method in the affine transformation process and verified the robustness of the LGML method to direction change. In addition, the LGML method is also used in target recognition detection [50] and pedestrian detection in the video [51], both of which have achieved good results. Tran et al. [52] used automobile point cloud to construct Lie Group samples and used principal geodesic analysis (PGA) [53] to design classifiers, whose classification effect is significantly better than traditional linear methods [54]. Therefore, the LGML method has good advantages in image affine transformation modeling, feature representation, and classification.

2.3. Attention Mechanism

The attention module is designed to focus on the most important part of features. It is inspired by the human perception process [55], and it is an algorithm that simulates human understanding and the perception of images, and can effectively suppress irrelevant feature information. Woo et al. [56] proposed a convolutional block attention module (CBAM), which weighted attention in spatial and channel dimensions, enabling the model to effectively learn key features in the image and improve the performance of most models. Hu et al. [57] fused key points with salient regional features to complete scene classification. Zhang et al. [58] used a significance sampling strategy to extract key features in remote sensing images for classification. However, the above saliency detection method based on texture feature information cannot effectively extract all key feature information. Recently, an adaptive method for extracting key attention features has been

proposed. Mnih et al. [59] combined the recurrent neural network model with the attention mechanism to reduce the feature dimension. Haut et al. [60] used the generated attention masks to multiply the corresponding regions to obtain attention features. Xu et al. [61] proposed an image task model based on "soft" and "hard" attention, which is trained by different propagation algorithms. Hu et al. [62] proposed a squeeze-and-excitation module, which utilizes the global average pooling to abstract the internal features and calculates the weight of each feature through nonlinear activation and linear combination.

3. Method

In this section, the LGDL model is carefully designed to improve the scene classification performance of HRRSI. As shown in Figure 2, the model mainly consists of three branches: LGML branch, deep learning branch, and feature-level fusion branch. For the branch of LGML, the HRRSI extracts shallower features through LGML and implements feature representation through the Lie Group feature covariance matrix. For the branch of deep learning, this branch is divided into three parts: (1) Low flow, (2) Middle flow, and (3) High flow. This branch is used to extract high-level features. Finally, the features extracted from the above two branches are transferred to the feature-level fusion branch, and the improved cross-entropy loss function is used to make the final prediction after the feature-level fusion is completed. By combining the above branches, the feature discrimination of our proposed model is enhanced, the parameters of the model are reduced, and the computational performance of the model is improved. The three branches of our model will be elaborated separately.

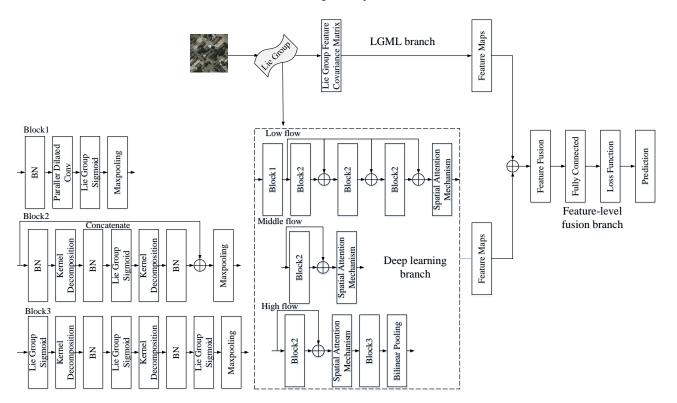


Figure 2. Architecture of our proposed model. The model includes (1) LGML: used to extract shallower features; (2) Deep learning branch: used to extract high-level features; (3) Feature-level fusion branch: used to fuse features.

3.1. LGML Branch

In the task of pattern recognition, it is a key and significant step to extract the discriminative features from data. Remote sensing scene classification is no exception. During the past decade, scholars have been devoted to design discriminative features, as it is critical for remote sensing scene classification, especially for some scenes that do not contain objects, such as forests, beaches, and deserts. For these scenarios, the low-level and middle-level features are more discriminative than the high-level features. Inspired by this, in this section, we extract the low-level and middle-level features of the scene and use the Lie Group feature covariance matrix to represent them.

3.1.1. Sample Mapping

To make full use of the computational advantages and manifold space structure of Lie Groups and Lie Algebras, firstly, we map the data samples to Lie Group manifold space:

$$\mathbf{G}_{ij} = \log(a_{ij}) \tag{1}$$

where a_{ij} represents the *j*th sample of the *i*th class in the dataset, and G_{ij} represents the *j*th sample of the *i*th class in the manifold space of the Lie Group. The following operations are based on the Lie Group data sample G_{ij} [12].

3.1.2. Lie Group Feature Covariance Matrix

According to the above analysis, to enhance the feature representation ability of different scenes, the following features are utilized:

$$F(x,y) = \left[x, y, Y, C_b, C_r, \left|\frac{\partial I(x,y)}{\partial x}\right|, \left|\frac{\partial I(x,y)}{\partial y}\right|, \left|\frac{\partial^2 I(x,y)}{\partial x^2}\right|, \left|\frac{\partial^2 I(x,y)}{\partial y^2}\right|,$$
(2)
$$Gabor(x,y), LBP(x,y), SIFT(x,y), HOG(x,y)\right]^T$$

where (x, y) represents the pixel position; (Y, C_b, C_r) represent the brightness, color difference, and saturation of space, respectively; and $\left|\frac{\partial I(x,y)}{\partial x}\right|$, $\left|\frac{\partial I(x,y)}{\partial y}\right|$, $\left|\frac{\partial^2 I(x,y)}{\partial x^2}\right|$, $\left|\frac{\partial^2 I(x,y)}{\partial y^2}\right|$ represent the first-order gradient and the second-order gradient at the coordinate position (x, y), respectively. The above three features are the most basic feature information of the target object. The same scene contains similar target objects, although these target objects are different in size and shape, their positions in the scene are similar, and the rate of change of pixels is similar. Colors are extremely discriminating features, such as white clouds, blue oceans, and green forests. However, it is not enough to utilize a single color feature. To enhance the robustness and stability of the feature, we choose YCbCr. Experiments have proven that these features have better robustness and stability to scene transformation [12,50,63].

Gabor(x, y) [64,65] represents the grayscale image of the scene, which can simulate the single-cell receptive field of the cerebral cortex to extract significant features. LBP(x, y) [12,65] refers to the binarization operation of the surrounding pixels, which can effectively extract the texture features of ground objects and is invariant to monotonous illumination changes. SIFT(x, y) [28] represents gradient information in the image, which is invariant to brightness, scale, and rotation changes. Histogram of Oriented Gradients (HOG(x, y)) [45,66] represents the statistical feature of the gradient direction histogram of the local area of the image, which has rotation invariance, scale invariance, and sparsity.

The feature covariance matrix of Lie Group is a real symmetric matrix, which represents the variance of features in the diagonal line and the relations between features in the non-diagonal line. In addition, this matrix has a lower dimension, is not affected by the size of HRRSI, has anti-noise ability, and has good computing performance. For other detailed information about this feature matrix, please refer to [12,50].

3.2. Deep Learning Branch

In recent years, remote sensing scene classification methods have sprung up, especially the model based on deep learning [1]. Generally, with the deepening of the network model structure, the model can extract deeper features [1]. However, a very deep model is difficult to train from the very beginning, and the model has the following risks [67]: (1) overfitting, (2) model degradation, and (3) a large number of parameters and high computational

complexity. To address the risks or problems mentioned above, we utilize parallel dilated convolution, kernel decomposition, and pyramid residual connection operations, as shown in Figure 2.

3.2.1. Batch Normalization (BN)

The goal of this layer is to standardize input sample information by reducing internal covariate shift [68]. Previous studies [68] showed that the BN layer inserted before the convolutional layer could accelerate the convergence speed of the model and effectively improve the structural capability of the model. Therefore, in this study, we adopt this approach.

3.2.2. Parallel Dilated Convolution

According to the basis of previous research [12], the existing model adopts depth separable convolutions (DepConv), mainly because the computation of DepConv is eight to nine times less than that of standard convolutions [69], and it contains fewer parameters. However, DepConv does not provide a large enough receptive field for large scenes. Dilated convolution is an effective method to enlarge the receptive field and ensure that large scenes are captured. However, previous studies show that dilated convolution is a time-consuming operation [12,70]. An important goal of our model design is to guarantee good classification accuracy while keeping good computational performance, that is, to expand the receptive field without increasing the computational complexity and the number of parameters of the model.

To address the above problems, three parallel dilated convolution operations with different dilation rates $r \in \{2, 4, 6\}$ are adopted in this study, as shown in Figure 3. To reduce parameters and make the model more slim, shared weights are adopted for parallel dilated convolution. Assume the feature map $fp \in \mathbb{R}^{h \times w \times c}$ and divide it into four parts along the channel fp_{c1} , fp_{c2} , fp_{c3} , $fp_{c4} \in \mathbb{R}^{h \times w \times \frac{c}{4}}$, as shown below:

$$fp_2 = df(con(fp_{c1}, fp_{c2}), sp, 2)$$
(3)

$$fp_4 = df(con(fp_{c2}, fp_{c3}), sp, 4)$$
(4)

$$fp_6 = df(con(fp_{c3}, fp_{c4}), sp, 6)$$
(5)

$$Rt = con(fp, fp_2, fp_4, fp_6) \tag{6}$$

where fp_i represents the dilated convolution using the dilation rate $r \in \{2, 4, 6\}$, sp represents the shared parameters, $df(\cdot)$ represents the dilated convolution function, and Rt represents the result of concatenating the output of the dilation convolution and the original feature maps. Finally, a 1 × 1 depthwise convolution is used to reduce the number of channels:

$$Rt' = DepConv1(Rt) \tag{7}$$

where Rt' represents the final output.

The above operation merges multi-scale features into Rt'. However, in the model, extra features are not always helpful, sometimes increasing the computational complexity of the model and even bringing unexpected consequences. This is another reason why we utilize shared weights. Different dilation rates adopt one filter operation, which is beneficial to the training of the filter and can avoid overfitting to a certain extent. In addition, previous studies have verified that the impact of parallel dilated convolution on time cost is insignificant [70].

As shown in Table 1, the number of parameters of three parallel dilated convolution and ordinary convolution is analyzed. From Table 1, we find that although the kernel size is enlarged, its parameters are much less than those of the other two convolutions. In addition, biases are not used in the module.

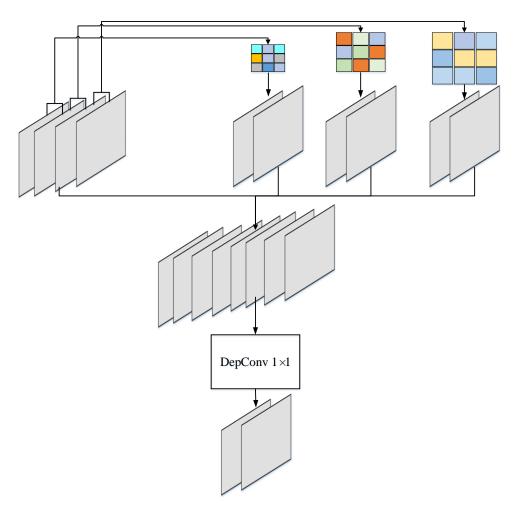


Figure 3. The principle of parallel dilated convolution. The dilation rates are 2, 4, and 6, respectively.

Methods	Kernel Size	Input Channel	Output Channel	Layer	Parameters	Total (M)
Ordinary	3×3	1024	1024	Conv1 Conv2 Conv3	$\begin{array}{c} 1024 \times 1024 \times 3 \times 3 = 9,437,184 \\ 1024 \times 1024 \times 3 \times 3 = 9,437,184 \\ 1024 \times 1024 \times 3 \times 3 = 9,437,184 \end{array}$	23,811,552 ≈ 28.3
Ordinary	5×5	1024	1024	Conv1 Conv2 Conv3	$\begin{array}{l} 1024 \times 1024 \times 5 \times 5 = 26,214,400 \\ 1024 \times 1024 \times 5 \times 5 = 26,214,400 \\ 1024 \times 1024 \times 5 \times 5 = 26,214,400 \end{array}$	78,643,200 ≈ 78.6
Parrallel	5×5	512	512	Conv1 Conv2 Conv3	$512 \times 512 \times 5 \times 5 = 6,553,600$	6,553,600 ≈ 6.55

3.2.3. Lie Group Kernel Function

In the field of machine learning, a large part of training and test data samples are matrix data samples forms other than the common vector data samples forms. In many existing applications, a large number of matrices constitute Lie Groups [47]. Since the dot product operation of vectors satisfies the commutative law, and matrix multiplication does not satisfy the commutative law, therefore, the traditional kernel function based on the vector cannot be applied to the data sample of the Lie Group matrix. According to the basis of pre-

vious studies [20,48], after repeated experimental analysis, the Sigmoid kernel function of Lie Group is adopted in this model:

$$k(x,y) = \frac{1}{1 + e^{c(tr(y^H \cdot x))}}$$
(8)

where *tr* represents the trace calculation of the matrix; for other relevant parameters, please refer to [20,48]. The Lie Group kernel function can satisfy both matrix data samples and vector data samples, which enhances the universality and robustness of the model.

3.2.4. Kernel Decomposition

In the previous research, we found that the ResNet model introduced skip connection, which can reduce the training difficulty of the deeper deep learning model [67]. Later, in the Bi-Real-Net model, Liu et al. [71] enlarged the number of skip connections, and the performance of the model was improved. Inspired by this, in this study, we also adopted the method of adding skip connections to improve the performance of the model. A common method is to decompose the original convolution filter into pointwise convolution and depthwise convolution [72]. However, the feature representation ability of pointwise convolution in this method is limited after binarization, and there are only +1 or -1 states [73]. Therefore, we decompose the 5×5 convolution kernel into 5×1 and 1×5 convolution filters to increase the number of skip connections, as shown in Figure 4. We decomposed a large convolution kernel operation into a horizontal convolution and a vertical convolution kernel in series. To enhance the performance of the model, skip connections were also introduced. In the actual algorithm design, the convolution kernel that cannot be decomposed is approximately decomposed. In the implementation of the algorithm, separable convolution filters are used.

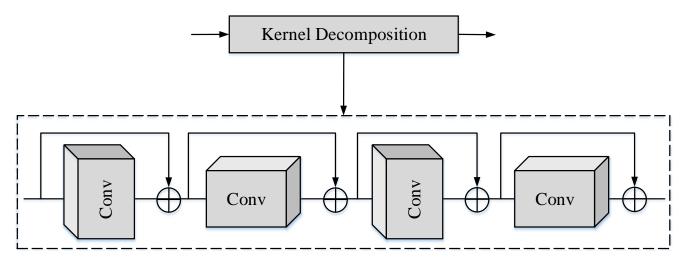


Figure 4. Principle of kernel decomposition.

3.2.5. Residual Connection Operation

To address the problems of model degradation and slow convergence speed, the residual connection operation was adopted in this study [74]. As shown in Figure 2, the concatenate operation is regarded as increasing the depth of the model to a certain extent and enhancing the ability of the model to extract more abstract features, speed up training, and suppress the network degradation. The residual connection operation we utilize is an optimization of the above operation, providing better performance. Since Han et al. [74] demonstrated that a large number of rectified linear units (ReLU) would degrade the performance of the model, unnecessary ReLUs were removed from the residual connection operation. To ensure non-

linearity, we adopt the sigmoid kernel function of the Lie Group, which is more robust and universal. The mathematical meaning of residual unit is as follows:

$$rs_{i+1} = ru(rs_i, w_i) + rs_i \tag{9}$$

where rs_i represents the input of the residual unit, rs_{i+1} represents the output of the residual unit, and ru and ct represent residual operation and concatenate, respectively.

3.2.6. Spatial Attention Mechanism

In the above study, the residual connection operation is used to connect the features from different layers, which may contain some redundant features. To remove redundant features and enhance the ability of the model to extract key features [75], at the same time, to preserve more discriminative features and highlight the local features matching the scene category, in the last residual block of each flow, we add spatial attention mechanisms.

Suppose *FM* represents the feature maps output from maxpooling, FM(i, j) represents the feature vector of a certain pixel (i, j) in *FM*, and the mathematical meaning of attention weight wt_{ij} is as follows:

$$wt_{ii} = softmax(LGSigmoid(tw \cdot FM_{ii}^{T} + b))$$
(10)

where *LGSigmoid* represents Lie Group Sigmoid kernel function, *softmax* represents *softmax* operation, *tw* represents the trainable weight parameter matrix, and *b* represents the bias matrix. Here, to improve the calculation speed, we utilize 1×1 depthwise separable convolution.

After classical mean pooling, the mathematical meaning of the gray value fm' of the corresponding pixel is as follows:

$$fm' = \frac{\sum_{m=0,n=0}^{ws} fm(i+m,j+n)}{ws \times ws}$$
(11)

where fm(x, y) represents the gray value of pixel (i, j) from one of these convolutional features, and *ws* represents the window size of the pooling operation.

After attention pooling, the mathematical meaning of fm' is as follows:

$$fm' = \frac{\sum_{m=0,n=0}^{ws} wt_{i+m,j+n} \cdot fm(i+m,j+n)}{ws \times ws}$$
(12)

After the above operation, the important local features can be weighted and the features can be down-sampled. Figure 5 illustrates the working principle of attention weight in our proposed model:

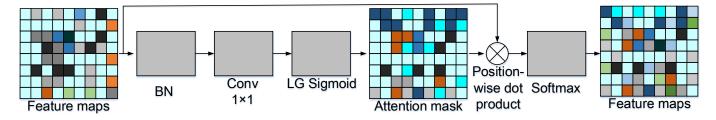


Figure 5. Principle of spatial attention mechanism.

3.2.7. Bilinear Pooling

To enhance the representation of subtle features, we choose bilinear pooling instead of average pooling. Suppose the output of the model is $O \in \mathbb{R}^{nb \times ch}$, Q = O, where *nb* and *ch* represent the number and channels of features, respectively. The mathematical meaning of the bilinear operation is as follows:

$$Rm = O^T Q \tag{13}$$

where Rm represents the result of matrix multiplication for O and T. Following [76], l_2 normalization and the signed square root are applied to the bilinear pooling result Rm. Since its gradients are available, it can be integrated into an end-to-end model.

3.3. Feature-Level Fusion Branch

Previous studies have shown that different features have their meanings and contain different attribute information [12]. Discriminant correlation analysis (DCA) is an optimization method and improvement of canonical correlation analysis [77], which can effectively reduce redundant features and maximize the pairwise correlation of different feature sets, thus obtaining compact but discriminative features. Therefore, DCA was used for feature fusion in this study.

3.3.1. Feature Fusion

Assume a heterogeneous feature set HF_1 , which contains *n* columns and *C* categories, and n_i represents the *i*th category. $hf_{i,j}$ represents the *j*th data sample of the *i*th category, which can be a vector data sample or a matrix data sample. According to previous studies [20,48], firstly, we utilize the Lie Group intrinsic mean to calculate the divergence between each category:

$$S_b = \sum_{i=1}^{C} n_i (\bar{hf}_i - \bar{hf}) (\bar{hf}_i - \bar{hf})^T = Y_x Y_x^T$$
(14)

where hf_i represents the intrinsic mean within the Lie Group of the *i*th category, and hf represents the intrinsic mean within the Lie Group of whole categories.

Then, by calculating the eigenvectors of $Y_x Y_x^T$, the dimensions of HF_1 can be reduced and projected into the reduced space:

$$HF_1' = W_h^T HF_1 \tag{15}$$

where W_b represents a transformation using S_b . In low-dimensional space, different categories can be distinguished. Similarly, given another heterogeneous feature set HF_2 , its projection is obtained by the above steps.

The next step is to make one set of features have nonzero correlation only with the corresponding features in another set. The transformation of HF'_1 and HF'_2 is as follows:

$$\tilde{HF}_1 = W_{b1}^T HF_1' \tag{16}$$

$$\tilde{HF}_2 = W_{b2}^T H F_2' \tag{17}$$

where W_{b1} and W_{b2} represent the transformation obtained by $S'_{hf_1hf_2} = HF'_1HF'^T_2$.

Finally, the transformation is carried out in the following way, and the final feature representation is obtained:

$$Fu_{s_{1,2}} = (\tilde{HF}_1, \tilde{HF}_2)^T \tag{18}$$

Through the above operations, any heterogeneous features can be integrated. In addition, compared with the original heterogeneous features, the dimensionalities of the fused features are greatly reduced.

3.3.2. Loss Function

Due to the high similarity of key features in different HRRSI, the deep learning model may experience overfitting, resulting in the decline in classification accuracy. Possible solutions include the cross-entropy loss functions, thus helping improve the classification accuracy for high similarity scene categories and enhancing the generalization of the model.

According to the previous research, we found that the traditional cross-entropy loss function mainly considers the model to learn from the direction of the largest difference, and does not consider the loss of the wrong category. In practice, the remote sensing dataset contains a large number of similar scene categories. For example, the NWPU-RESISC45 dataset contains 45 categories and 31,500 images, among which only a few data samples can be used for training, and the data samples are uneven. This can easily lead to overfitting and inaccurate prediction of the model, and it is difficult to distinguish similar scene categories. Therefore, the traditional cross-entropy loss function is not enough to address the features of all data samples.

For further analysis, possible solutions include the use of a regularization strategy, that is, label smoothing; the use of hyperparameter ζ to achieve a better trade-off between positive samples and negative samples; and the use of soft-one hot to add noise and constrain the output loss function. The cross-entropy loss relationship between the corrected real label y_{LSc} and the corresponding probability p_c is as follows:

$$y_{LS_c} = y_c(1-\zeta) + \zeta u(c) = \begin{cases} 1-\zeta + \frac{\zeta}{C}, & \text{if } c = hf \\ \frac{\zeta}{C}, & \text{if } c \neq hf \end{cases}$$
(19)

where *C* represents the total number of categories, *c* represents the index of a specific category, and u(c) follows the uniform distribution of *C* categories. A new loss function can be obtained:

$$Loss_n = -\sum_{c=1}^{C} y_{LS_c} logp_c = \begin{cases} (1-\zeta) \cdot Loss, & \text{if } c = hf\\ \zeta \cdot Loss, & \text{if } c \neq hf \end{cases} = -(1-\zeta+\frac{\zeta}{C}) logy_{hf} - \frac{\zeta}{C} \sum_{c \neq hf} logp_c$$
(20)

where:

$$Loss = -\sum_{c=1}^{C} y_c log p_c \tag{21}$$

where y_c represents the actual category, and p_c represents the corresponding probability. $y_c = 1$ indicates the correctly classified category, and $y_c = 0$ indicates other categories. The specific expression is as follows:

$$y_c = \begin{cases} 1, & \text{if } c = hf \\ 0, & \text{if } c \neq hf \end{cases}$$
(22)

This function can satisfy the evaluation of the loss of the correct category and reduce the difference between the wrong category. In particular, it can effectively improve the difference between different scenes in remote sensing datasets and enhance the generalization of the model.

4. Experimental Results

In this section, we conduct a comprehensive experiment and analysis to evaluate the feasibility and robustness of our proposed method. Firstly, three challenging datasets used in the experiment are outlined. Secondly, the relevant settings of the experiment are described. Finally, we compared and analyzed our method with some of the state-of-the-art methods and performed ablation experiments on the modules in the model.

4.1. Experimental Datasets

In this section, we chose UC Merced [78], AID [79], and NWPU-RESISC45 [25], three public and challenging datasets. The UC Merced dataset [78] contains 21 land-use scenes with a total of 2100 images. The AID dataset [79] contains 30 scene types, each with 200 to 400 images. The NWPU-RESISC45 dataset [25], published by Northwestern Polytechnical University, contains 45 scene classes with a total of 31,500 images. The above dataset has the following characteristics: (1) They are the most influential of the remote sensing datasets, which have been widely used in the classification and retrieval of remote sensing image scenes; (2) the diversity of images, taking into account the different times, seasons, and imaging conditions of the scene; (3) the image contains variations in spatial resolution, viewpoint, occlusion, and background, which increase the challenge of classification; (4) the

scale of the remote sensing scene dataset is significantly expanded, with large intraclass differences and high interclass similarity. To prevent overfitting, data augmentations were used to supplement the number of datasets during the experiment, including horizontal and vertical flipping and rotation at different angles.

4.2. Experiment Setup

The model is implemented based on the deep learning platform of Tensorflow [80]. The model was optimized by stochastic gradient descent (SGD) algorithm. The experimental environment settings are shown in Table 2. After the initial setting is completed, the initial learning rate is reduced by 105 times while observing the validation loss decreasing slowly.

To fairly compare with other experimental models, we stipulate that the ratio of the training set and test set should be the same as that of most previous models [25]. The evaluation indicators include the overall accuracy (OA), the Kappa coefficient (KC), and the confusion matrix. To obtain reliable experimental results, we randomly divided three datasets according to the ratio of training and test sets, repeated the experiment 10 times, and calculated the standard deviation and average value to obtain the final experimental results.

Table 2. Experimental environment parameters.

Item	Content
Processor	Inter Core i7-4700 CPU with 2.70 GHz $\times 12$
Memory	32 GB
Operating system	CentOS 7.8 64 bit
Hard disk	1T
GPU	Nvidia Titan-X ×2
Python	3.7.2
PyTorch	1.4.0
ĊUDA	10.0
Learning rate	10^{-3}
Momentum	0.9
Weight decay	$5 imes 10^{-4}$
Batch	16
Saturation	1.5
Subdivisions	64

4.3. Experimental Results

Previous studies have shown [25,79] that the model based on CNN far surpassed the method based on shallower features. Therefore, in this experiment, we did not choose to compare with the traditional method based on handcrafted features.

The experimental results are shown in Table 3, as follows:

The experimental results on the UCM dataset are listed below:

- When the training ratio is 50%, the accuracy of our proposed model achieves 98.67%, surpassing all the previous models. The experimental results indicate that the classification accuracy can be improved effectively by adding shallower features (low-level and middle-level features), parallel dilated convolution, Lie Group kernel function, kernel decomposition, and skip connection. Shallower features and multidilation pooling modules are used in LGRIN [12], but the classification accuracy of our model is 0.06% higher than that of LGRIN [12]. Our model is 0.19% higher than CSCD [8], 0.1% higher than SEMDPMNet [81], and 5.91% higher than Xception [82]. When the training ratio is 80%, our proposed model is 3.45% high than MobileNet V2 [81] and 0.02% higher than SCC-CNN [37].
- In addition, we also analyzed the Kappa coefficient corresponding to the above models. When the training ratio is 50%, the Kappa coefficient of our model is 98.31%, which is 4.04% higher than that of APDC-NET [16] and 2.74% higher than that of LCPB [83]. When the training ratio is 80%, the Kappa coefficient of our model is 99.76%, which is

0.01% higher than that of LCNN-GWHA [38] and 0.26% higher than that of LCNN-CMGF [40]. The above experimental results verify the superiority of our model.

3. As shown in Figure 6, our proposed model fully recognized most of the scene categories, and the recognition rate of the medium residential and dense residential scene is lower than that of other scenes. Therefore, we believe that there is a large confusion between them, mainly because their distribution is quite similar, and the difference between the extracted shallower features and the high-level features is small.

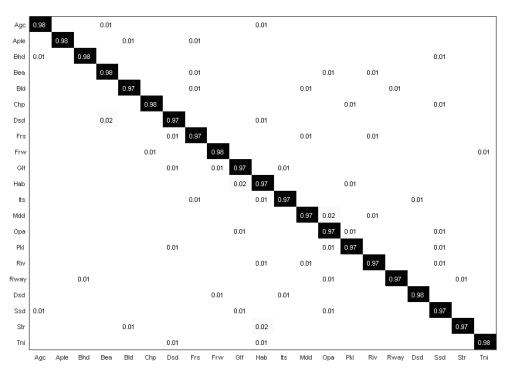


Figure 6. Confusion matrix of our proposed method with the UC Merced dataset.

Table 3. In the experimental results under three different datasets of UC Merced (UCM), AID, and NWPU-RESISC45 (NWPU), we utilized 24 models to compare the overall accuracy (OA%) and Kappa coefficient (KC) with our proposed model.

Madala	UCM	(50%)	UCM	(80%)	AID (20%)	AID ((50%)	NWPU	(10%)	NWPU	(20%)
Models	OA	KC										
	(%)	(%)	(%)	(%)	(%)	(%)	(%)	(%)	(%)	(%)	(%)	(%)
CSCD [8]	$\begin{array}{c} 98.48 \pm \\ 0.21 \end{array}$	98.28	$\begin{array}{c} 99.52 \pm \\ 0.13 \end{array}$	99.39	$\begin{array}{r}94.29\pm\\0.35\end{array}$	93.39	$\begin{array}{c} 96.70 \pm \\ 0.14 \end{array}$	96.21	$\begin{array}{c}91.64\pm\\0.16\end{array}$	91.43	$\begin{array}{c}93.59\pm\\0.21\end{array}$	93.27
APDC- Net [16]	$\begin{array}{c}95.01\pm\\0.43\end{array}$	94.27	$\begin{array}{c}97.05\pm\\0.43\end{array}$	96.33	$\begin{array}{c} 88.56 \pm \\ 0.29 \end{array}$	87.37	$\begin{array}{c}92.15\pm\\0.29\end{array}$	91.53	$\begin{array}{c} 85.94 \pm \\ 0.22 \end{array}$	84.36	$\begin{array}{c} 87.84 \pm \\ 0.26 \end{array}$	86.67
CNN + GCN [84]	-	-	-	-	$\begin{array}{c}94.93\pm\\0.31\end{array}$	92.75	$\begin{array}{c} 96.89 \pm \\ 0.31 \end{array}$	95.27	$\begin{array}{c} 90.75 \pm \\ 0.21 \end{array}$	89.62	$\begin{array}{c}92.87\pm\\0.13\end{array}$	91.63
LCPB [83]	$\begin{array}{c} 96.66 \pm \\ 1.36 \end{array}$	95.57	$\begin{array}{c} 98.32 \pm \\ 1.03 \end{array}$	97.75	$\begin{array}{c} 87.68 \pm \\ 0.25 \end{array}$	86.77	$\begin{array}{c}91.33\pm\\0.36\end{array}$	90.65	-	-	-	-
LCPP [83]	$\begin{array}{r}97.54\pm\\1.02\end{array}$	97.32	$\begin{array}{r}98.78\pm\\1.12\end{array}$	97.73	$\begin{array}{c} 90.96 \pm \\ 0.33 \end{array}$	89.78	$\begin{array}{r}93.12\pm\\0.28\end{array}$	92.66	-	-	-	-
LG - Sigmoid	$\begin{array}{c} 98.32 \pm \\ 0.13 \end{array}$	96.56	$\begin{array}{r} 98.92 \pm \\ 0.35 \end{array}$	97.63	$\begin{array}{c}93.25\pm\\0.35\end{array}$	91.62	$\begin{array}{c}95.87\pm\\0.16\end{array}$	94.57	$\begin{array}{c} 90.19 \pm \\ 0.11 \end{array}$	89.62	$\begin{array}{c} 93.21 \pm \\ 0.12 \end{array}$	92.96
[20] LG - RBF [48]	$\begin{array}{c} 98.37 \pm \\ 0.15 \end{array}$	97.66	$\begin{array}{c} 98.95 \pm \\ 0.16 \end{array}$	97.49	$\begin{array}{c}94.17\pm\\0.25\end{array}$	93.43	$\begin{array}{c} 96.19 \pm \\ 0.28 \end{array}$	94.33	90.23 ± 0.13	89.17	$\begin{array}{c} 93.25 \pm \\ 0.12 \end{array}$	93.02

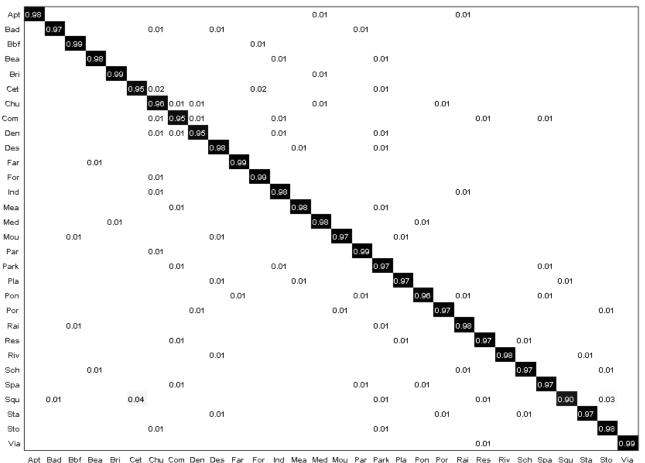
	UCM	(50%)	UCM	(80%)	AID (20%)	AID ((50%)	NWPU	(10%)	NWPU	(20%)
Models	OA (%)	KC (%)	OA (%)	KC (%)	OA (%)	KC (%)	OA (%)	KC (%)	OA (%)	KC(%)	OA (%)	KC (%)
LGRIN [12]	$\begin{array}{c} 98.61 \pm \\ 0.22 \end{array}$	97.65	$\begin{array}{r} 98.97 \pm \\ 0.31 \end{array}$	97.89	$\begin{array}{r}94.74\pm\\0.23\end{array}$	93.56	$\begin{array}{r}97.65\pm\\0.25\end{array}$	96.31	$\begin{array}{r}91.91\pm\\0.15\end{array}$	91.53	$\begin{array}{r}94.43\pm\\0.16\end{array}$	93.28
VGG19 [85]	-	-	-	-	$\begin{array}{r} 87.73 \pm \\ 0.25 \end{array}$	86.65	$\begin{array}{c}91.71\pm\\0.42\end{array}$	90.06	$\begin{array}{c} 81.34 \pm \\ 0.32 \end{array}$	80.22	$\begin{array}{r} 83.57 \pm \\ 0.37 \end{array}$	82.17
Caffe - Net [79]	$\begin{array}{c} 93.98 \pm \\ 0.67 \end{array}$	92.86	$\begin{array}{c}95.02\pm\\0.81\end{array}$	94.33	$\begin{array}{c} 86.86 \pm \\ 0.47 \end{array}$	85.23	$\begin{array}{c} 89.53 \pm \\ 0.31 \end{array}$	88.36	-	-	-	-
GoogLe - Net [79]	92.70±	91.37	$\begin{array}{c}94.31\pm\\0.89\end{array}$	92.26	$\begin{array}{c} 83.44 \pm \\ 0.40 \end{array}$	82.17	$\begin{array}{c} 86.39 \pm \\ 0.55 \end{array}$	85.27	$\begin{array}{c} 82.46 \pm \\ 0.12 \end{array}$	81.37	$\begin{array}{c} 85.36 \pm \\ 0.17 \end{array}$	83.36
Mobile- Net V2 [81]	$\begin{array}{c} 92.17 \pm \\ 0.13 \end{array}$	91.06	$\begin{array}{c} 96.33 \pm \\ 0.15 \end{array}$	94.91	$\begin{array}{c} 93.26 \pm \\ 0.25 \end{array}$	92.19	$\begin{array}{c} 96.95 \pm \\ 0.26 \end{array}$	95.37	$\begin{array}{c} 89.83 \pm \\ 0.16 \end{array}$	87.65	$\begin{array}{c} 92.16 \pm \\ 0.15 \end{array}$	91.07
VGG- VD-16 [79]	$\begin{array}{c}94.14\pm\\0.69\end{array}$	93.52	$\begin{array}{c}95.21\pm\\1.20\end{array}$	94.75	$\begin{array}{c} 86.59 \pm \\ 0.29 \end{array}$	85.37	$\begin{array}{c} 89.64 \pm \\ 0.36 \end{array}$	88.45	-	-	-	-
ResNet50 [85]) _	-	-	-	$\begin{array}{c} 92.39 \pm \\ 0.15 \end{array}$	91.51	$\begin{array}{c}94.69\pm\\0.19\end{array}$	93.47	$\begin{array}{c} 86.23 \pm \\ 0.41 \end{array}$	85.32	$\begin{array}{c} 88.93 \pm \\ 0.12 \end{array}$	87.61
SE - MD PMNet [81]	$\begin{array}{c} 98.57 \pm \\ 0.11 \end{array}$	97.36	$\begin{array}{c} 98.95 \pm \\ 0.12 \end{array}$	97.74	$\begin{array}{c}94.68\pm\\0.17\end{array}$	93.22	97.14 ± 0.15	95.87	$\begin{array}{c} 91.80 \pm \\ 0.07 \end{array}$	90.79	$\begin{array}{c}94.11\pm\\0.03\end{array}$	92.96
Contour- let - CNN [86	-	-	$\begin{array}{c} 98.97 \pm \\ 0.21 \end{array}$	97.81	-	-	$\begin{array}{c} 97.36 \pm \\ 0.45 \end{array}$	96.19	$\begin{array}{c} 85.93 \pm \\ 0.51 \end{array}$	84.36	$\begin{array}{c} 89.57 \pm \\ 0.45 \end{array}$	88.35
Inceptior V3 [85]	1- <u>-</u>	-	-	-	$\begin{array}{c}93.27\pm\\0.17\end{array}$	92.11	$\begin{array}{c}95.07\pm\\0.22\end{array}$	93.91	$\begin{array}{c} 85.46 \pm \\ 0.33 \end{array}$	84.62	$\begin{array}{c} 87.75 \pm \\ 0.43 \end{array}$	86.46
Xcep - tion [82]	$\begin{array}{c}92.76\pm\\0.31\end{array}$	91.41	$\begin{array}{c}94.40\pm\\0.15\end{array}$	92.77	$\begin{array}{c} 86.12 \pm \\ 0.28 \end{array}$	85.73	$\begin{array}{c} 90.14 \pm \\ 0.52 \end{array}$	89.07	$\begin{array}{c} 81.64 \pm \\ 0.32 \end{array}$	80.52	$\begin{array}{r} 84.79 \pm \\ 0.26 \end{array}$	83.56
Efficient Net [87]	-	-	$\begin{array}{c}94.37\pm\\0.14\end{array}$	93.27	$\begin{array}{c} 86.56 \pm \\ 0.17 \end{array}$	85.32	$\begin{array}{r} 88.35 \pm \\ 0.16 \end{array}$	87.21	$\begin{array}{r} 78.57 \pm \\ 0.15 \end{array}$	77.26	$\begin{array}{c} 81.83 \pm \\ 0.15 \end{array}$	79.53
SCC- CNN [37	-	-	$\begin{array}{r} 99.76 \pm \\ 0.05 \end{array}$	99.51	$\begin{array}{r}93.15\pm\\0.25\end{array}$	92.06	$\begin{array}{r}97.31 \pm \\0.10\end{array}$	96.03	$\begin{array}{r}92.02\pm\\0.50\end{array}$	90.57	$\begin{array}{r}94.39\pm\\0.16\end{array}$	93.13
LCNN- GWHA [38]	-	-	$\begin{array}{c} 99.76 \pm \\ 0.25 \end{array}$	99.75	$\begin{array}{c}93.85\pm\\0.16\end{array}$	93.63	$\begin{array}{c} 97.64 \pm \\ 0.28 \end{array}$	97.55	$\begin{array}{c} 92.24 \pm \\ 0.12 \end{array}$	92.04	$\begin{array}{c}94.26\pm\\0.25\end{array}$	94.13
RS- DARTS	-	-	-	-	$\begin{array}{c} 88.34 \pm \\ 0.25 \end{array}$	87.26	$\begin{array}{c}91.25\pm\\0.23\end{array}$	90.37	$\begin{array}{c} 85.73 \pm \\ 0.26 \end{array}$	84.26	$\begin{array}{c} 89.15 \pm \\ 0.36 \end{array}$	88.06
[39] LCNN- CMGF [40]	-	-	$\begin{array}{c} 99.52 \pm \\ 0.34 \end{array}$	99.50	$\begin{array}{c} 93.63 \pm \\ 0.10 \end{array}$	93.51	$\begin{array}{c}97.54\pm\\0.25\end{array}$	97.45	$\begin{array}{c}92.53\pm\\0.56\end{array}$	92.17	$\begin{array}{c}94.18\pm\\0.35\end{array}$	94.04
DF- CNN [41	-	-	$\begin{array}{c} 99.62 \pm \\ 0.13 \end{array}$	99.53	$\begin{array}{c}94.63\pm\\0.15\end{array}$	94.46	$\begin{array}{c} 96.43 \pm \\ 0.26 \end{array}$	95.83	$\begin{array}{c} 89.88 \pm \\ 0.37 \end{array}$	88.62	$\begin{array}{c}94.44\pm\\0.35\end{array}$	94.23
Proposed	$98.67 \pm$	98.31	$\begin{array}{c} 99.78\pm\\0.16\end{array}$	99.76	$\begin{array}{c}94.79\pm\\0.28\end{array}$	94.57	$\begin{array}{r}97.72\pm\\0.25\end{array}$	97.61	$\begin{array}{c}92.62\pm\\0.15\end{array}$	92.25	$\begin{array}{c}94.49\pm\\0.36\end{array}$	94.31

Table 3. Cont.

The experimental results on the AID dataset are presented below:

 The AID dataset is different from UCM dataset. The AID dataset is multi-sourced: It is collected from different regions of the world with different spatial resolutions and times. In addition, these images are captured by different sensors, which makes scene classification more difficult. When the training ratio is 20%, the accuracy of our proposed model achieves 94.79%, 7.11% higher than LCPB [83], 3.83% higher than LCPP [83], and 0.16% higher than DF-CNN [41]. When the training ratio is 50%, the accuracy of our proposed model achieves 97.72%, 0.41% higher than SCC-CNN [37], 0.08% higher than LCNN-GWHA [38], and 3.03% higher than ResNet50 [85].

- 2. When the training ratio is 20%, the Kappa coefficient our proposed achieves 94.57%, which is 9.2% and 0.11% higher than VGG-VD-16 [79] and DF-CNN [41], respectively, and 9.34% higher than CaffeNet [79]. When the training ratio is 50%, the Kappa coefficient our proposed achieves 97.61%, which is 0.16% higher than LCNN-CMGF [40], 0.06% higher than LCNN-GWHA [38], and 1.58% higher than SCC-CNN [37].
- 3. As for the confusion matrix shown in Figure 7, our model can achieve 96% in most scenes, and 100% in some scenes, such as in parks and forests. However, the classification accuracy of some scenes is low. After further analysis, we found that their structure and composition are highly similar, such as the shallower features of ponds and buildings, so the classification accuracy is low.



Apt Bad Bbf Bea Bri Cet Chu Com Den Des Far For Ind Mea Med Mou Par Park Pla Pon Por Rai Res Riv Sch Spa Squ Sta Sto

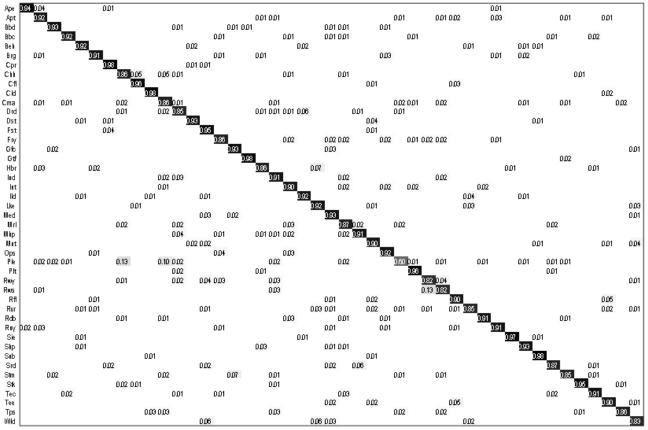
Figure 7. Confusion matrix of our proposed method with the AID dataset.

The experimental results on the NWPU dataset are listed below:

- 1. The NWPU dataset is large in terms of the total number of categories of images and scenes. In addition, the dataset has large intraclass differences and high interclass similarity, and it contains variations in spatial resolution, viewpoint, illumination, occlusion, and background, which represents a more challenging scene classification task than the UCM and AID datasets. When the training ratio is 10%, the accuracy of our proposed model achieves 92.62%, which is 0.09% higher than that of LCNN-CMGF [38], 0.71% higher than that of LGRIN [12], and 0.38% higher than that of LCNN-GWHA [38]. When the training ratio is 20%, the accuracy of our proposed model achieves 94.49%, which is 0.9% higher than that of CSCD [8], 0.06% higher than that of LGRIN [12], and 0.38% higher than that of SE-MDPMNET [81].
- 2. When the training ratio is 10%, the Kappa coefficient of our proposed model achieves 92.25%, which is 0.21% and 0.08% higher than LCNN-GWHA [38] and LCNN-CMGF [40], respectively. When the training rate is 20%, the accuracy of our proposed model achieves

94.31%, which is 0.08% higher than DF-CNN [41], 0.27% higher than LCNN-CMGF [40], and 1.03% higher than LGRIN [12].

3. Confusion matrix as shown in Figure 8: Similar to the AID dataset, the classification accuracy of our proposed model can achieve 92% in most scenarios. Due to the large scale of NWPU datasets, large intraclass differences, and high interclass similarity, none of the categories are completely correctly classified. Because churches and palaces have similar physical structures and other characteristics, these two kinds of scenes are easy to be confused.



Ape Apt 8bd 8bc 8ei 8rg Cpr Cii Cfi CkiCma Drd Dst Fst Fry Gfc Gtf Hbr Ind Int Ild Lke Med Mri Mip Mint Ops Pie Pit Rwy Rws Rfi Rur Rdb Rny Sie Sip Sub Srd Sim Sik Tec Tee Tps Wild

Figure 8. Confusion matrix of our proposed method with the NWPU-RESISC45 dataset.

5. Discussion

The above results can be explained from the following aspects:

- 1. The existing CNNs model tends to retain the high-level features while ignoring the shallower features in the image, resulting in the classification accuracy of the scene being relatively low. However, the model of our proposed efficiently integrates different features of multiple levels, especially the shallower features, providing more features required by the model and effectively improves the classification accuracy of the scene;
- 2. Our proposed model adopts a spatial attention mechanism, kernel decomposition, and the method of increasing the number of skip connections. It can effectively extract more important weight feature information in the image and preserve the feature information of different levels, making the extracted feature more discriminative to the scene;
- 3. Generally, deeper and wider models can extract more global features, but it is easy to increase the complexity and number of parameters of the model, and it is also easy to extract features through pure linear stacked convolution modules, thus affecting the classification accuracy. In our model, skip connections, parallel dilated

convolution, and expanded kernel size was used to expand the receptive field and extract more global features, which effectively reduced the number of parameters and complexity of the model and improved the classification accuracy;

4. The pyramid residual connection is adopted in our proposed model, which can not only reduce the complexity of the model but also reuse parameters and features, reduce the parameters of the model, enhance the feature learning ability of the model, and establish connections with shallower features. In other words, the pyramid residual connection further reduces the computational complexity and the number of model parameters and ensures the ability of the model to extract deeper features.

5.1. Evaluation of Size of Models

In this experiment, we select 10 classical models to compare the size of the model, namely, CaffeNet [79], GoogLeNet [79], MobileNet V2 [81], SE-MDPMNet [81], ResNet50 [85], VGG-VD-16 [79], Inception V3 [85], LCNN-GWHA [38], SCC-CNN [8] and LGRIN [12], where GMACs represent the complexity of computation. From Table 4, we found that compared with SE-MDPMNet [81], our model has advantages in terms of parameter number and GMACs. In addition, compared with lightweight models, GoogLeNet [79] and MobileNet [81], our model achieves a better trade-off between OA, model parameters, and GMACs. Since parallel dilated convolution is adopted in our model, compared with LCNN-GWHA [38], our model reduces the number of parameters and further improves the computational performance of the model. Our model has much fewer parameters, but the classification accuracy is still better than other CNN models. In addition, the time complexity of the model is $O(nlog_2n)$ in the best case and $O(n^2)$ in the worst case.

Models	OA (%)	Parameters (M)	GMACs (G)
ResNet50 [85]	94.69	25.61	1.8555
CaffeNet [79]	89.53	60.97	3.6532
MobileNet V2 [81]	95.96	3.50	0.3451
GoogLeNet [79]	86.39	7.00	0.7500
SE-MDPMNet [81]	97.14	5.17	0.9843
VGG-VD-16 [79]	89.64	138.36	7.7500
Inception V3 [85]	95.07	45.37	2.4356
LGRIN [12]	97.65	4.63	0.4933
LCNN-GWHA [38]	97.64	0.3	0.0467
SCC-CNN [8]	97.31	0.49	0.0592
Proposed	97.72	0.28	0.0421

Table 4. Taking AID (50%) as an example, the size of the model is evaluated.

5.2. Comparison of Prediction Time

As shown in Table 5, the prediction time of a single HRRSI from each of the three datasets is compared. The prediction time of our model is significantly reduced compared with other models. The experimental results in Table 5 show that the reduction in the parameters in the model is beneficial to improving the prediction time of the model. There is little difference in the number of parameters between our proposed model and LCNN-GWHA [38], but our prediction speed is 0.015S (on average) faster than LCNN-GWHA [38], which shows that the kernel size and receptive field are increased in parallel dilated convolution, and the computational performance of the model is not reduced.

Models	UCM (80%)	AID (50%)	NWPU (20%)
MobileNet V2 [81]	0.076	0.089	0.095
GoogLeNet [79]	0.157	0.193	0.255
SE-MDPMNet [81]	0.512	0.737	0.973
VGG-VD-16 [79]	1.206	1.682	2.151
Inception V3 [85]	0.091	0.126	0.143
LGRIN [12]	0.082	0.095	0.137
LCNN-GWHA [38]	0.075	0.087	0.125
Proposed	0.070	0.081	0.091

Table 5. Prediction times (S) of different models with three datesets.

5.3. Ablation Experiment

Taking the AID (50%) dataset as an example, we conducted a series of experiments to analyze the effect of each module in the model. To ensure a fair comparison, all evaluated are set with the same parameters.

5.3.1. Effects of LGML in the Model

To clarify the effect of LGML in the model, two different structures are designed based on dense connected convolutional neural network (DCCNN) and LGML. DCCNN is a model used to retain shallower features [88]. The experimental results are shown in Table 6: It has been shown that the model based on LGML has good performance. The relative improvements of each metric approximates 4% to 5%. The characterization method of the Lie Group feature matrix in LGML adopts a real symmetric matrix. Compared with the DCCNN model, it has fewer parameters, good computational performance, and an anti-noise ability. In addition, it can better express features and their correlation between features, and improve the comprehensibility of the model from the perspective of LGML.

Table 6. Influence of LGML.

Modulars	OA (%) ↑	KC (50%) ↑	Parameters (M) \downarrow
DCCNN [88]	92.56	92.35	5.26
LGML	97.72	97.61	0.28

5.3.2. Effect of Spatial Attention Mechanism

To confirm the effect of spatial attention mechanism on the model, we compared our classification results with the model without spatial attention mechanism, and the results are shown in Table 7. Our proposed model achieves the highest classification accuracy, and the spatial attention mechanism improves the classification accuracy of the model by 3.36%. These experimental results indicate that the spatial attention mechanism in the model is beneficial to scene classification.

Table 7. Influence of spatial attention mechanism.

Modulars	OA (%) ↑
Without spatial attention	94.36
Ours	97.72

5.3.3. Influence of Different Distance Space Calculation Methods on Model Scene Classification

Since most of the existing CNN models utilize Euclidean space distance for calculation, in practical application scenarios, Euclidean space distance is mainly applicable to vector space data samples, and there are limitations for non-Euclidean space samples. As shown in Figure 9, Figure 9a is the distance calculated by using Lie Group manifold distance, and Figure 9b is the distance directly calculated by using Euclidean space distance. Obviously, the manifold space distance can better reflect the real distance between data samples. As shown in Table 8, the experimental results obtained by calculating Euclidean space distance and manifold space distance are adopted, respectively. The experimental results show that the manifold space distance can achieve higher classification accuracy.

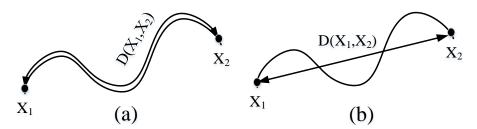


Figure 9. Difference of Manifold distance and Euclidean distance: (a) represents the distance between the samples X_1 and X_2 on the manifold space of the Lie Group, and the distance is on the manifold space; (b) is the distance obtained by directly using Euclidean distance to calculate samples X_1 and X_2 .

Table 8. Influence of different distance space calculation methods.

Methods	OA (%) ↑
Euclidean space distance	91.37
Ours	97.72

5.3.4. Contribution of Pyramid Residual Connection and Bilinear Pooling to the Model

To verify the effects of pyramid residual connection and bilinear pooling, we compare our classification results (i.e., using pyramid residual connection and bilinear pooling, PRC + BIP) with the following three situations, that is, using the residual connection and global average pooling (RC + GAP), residual connection and bilinear pooling (RC + BIP), pyramid residual connection and global average pooling (PRC + GAP). All experimental results are listed in Table 9 and can also be found follows:

- 1. In all experiments, the proposed model achieves the highest classification accuracy, while RC + GAP achieves the lowest classification accuracy;
- Compared with PRU + GAP, our classification accuracy is improved by 4.31%, indicating that the model based on bilinear pooling has better classification performance. We can consider that this method can provide many subtle and discriminative features for the model;
- 3. The experimental results indicate that both the pyramid residual connection and bilinear pooling are beneficial to scene classification. In addition, as shown in Figure 1, the pyramid connecting is also beneficial to the convergence of the model and improves the fitting effect of the model.

Table 9. Influence of pyramid residual connection and bilinear pooling to the model.

Methods	OA (%) ↑
RC + GAP	91.26
RC + BIP	92.43
PRC + GAP	93.41
PRC + BIP	97.72

5.3.5. Influence of Cross-Entropy Loss Function on Model Scene Classification

To verify that the traditional cross-entropy loss function (CEL) and cross-entropy loss function based on label smoothing (CELLS) influence scene classification, we compare our classification results with the model using the traditional cross-entropy loss function. The experimental results are shown in Table 10. The classification accuracy of CELLS is 2.34% higher than that of the CEL model, which shows that CELLS is more suitable for scene

classification. Label smoothing corrects the loss function and improves the generalization ability of the model.

Table 10. Influence of cross-entropy loss function on model scene classification.

Functions	OA (%) ↑
CEL	95.38
CELLS	97.72

6. Conclusions

Intraclass diversity and interclass similarities are existing in HRRSIs, which have complex spatial distributions and geometric structures. The traditional CNN model based on linear superposition cannot extract key and discriminative features. Therefore, this study proposes a novel Lie Group deep learning model to address the above problems. Firstly, by combining LGML and deep learning, our proposed model jointly learns shallower features (low-level and middle-level features) and high-level features (semantic features). In this model, the parallel dilated convolution, Lie Group kernel function, kernel decomposition, and pyramid residual connection are adopted to expand the receptive field, reduce the number of parameters and calculation, prevent model degradation and overfitting, and effectively extract the key and discriminative features at different levels. Secondly, the spatial attention mechanism in the model can effectively suppress irrelevant feature information and enhance local semantic features. Finally, the feature-level fusion method is adopted to avoid feature redundancy and reduce the dimension of feature, enhance the capability of feature representation and maintain good computing performance. In addition, to reduce the influence of high similarity categories on scene classification, the model adopts the cross-entropy loss function based on label smoothing. The proposed model is performed on three public and challenging large-scale datasets, and the experimental results verify that our method has better performance than other methods.

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Abbreviations

AID	Aerial Image Dataset
BoVW	Bag-of-Visual-Words
CBAM	Convolutional Block Attention Module
CH	Color Histogram
CNN	Convolutinal Neural Network
DCA	Discriminant Correlation Analysis
DCCNN	Dense Connected Convolutional Neural Network
DepConv	Depth separable Convolutions
F1	F1 score
GAN	Generative Adversarial Network
HRRSI	High-resolution Remote Sensing Images
KC	Kappa Coefficient
LBP	Local Binary Pattern
LDA	Latent Dirichlet Allocation
LGDL	Lie Group Deep Learning
LGML	Lie Group Machine Learning
LGRIN	Lie Group Regional Influence Network
OA	Overall Accuracy
PGA	Principal Geodesic Analysis
PLSA	Probabilistic Latent Semantic Analysis
PTM	Probabilistic Topic Models
ReLU	Rectified Linear Units
SGD	Stochastic Gradient Descent
SIFT	Scale-invariant Feature Transform

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