

Article

Study on Phase Transformation Orientation Relationship of HCP-FCC during Rolling of High Purity Titanium

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Abstract: High purity titanium (Ti) thin strip was prepared by rolling with large deformation and was characterized by the means of Transmission Electron Microscopy (TEM), selected area diffraction (SAED) pattern, high-resolution (HRTEM) analysis, as well as Transmission Kikuchi Diffraction (TKD). It is found that there are face-centered cubic (FCC) Ti laths formed within the matrix of hexagonal close packing (HCP) Ti. This shows that the HCP-FCC phase transition occurred during the rolling, and a specific orientation relationship (OR) between HCP phase and FCC phase obeys $\langle 0001 \rangle_{\alpha}/\langle 001 \rangle_{\text{FCC}}$ and $\{10\overline{10}\}_{\alpha}/\langle 110 \rangle_{\text{FCC}}$. The ORs of HCP-FCC phase transition are deeply studied by TKD pole figure and phase transformation matrix. It is found that the derived results via pole figure and transformation matrix are equivalent, and are consistent with TEM-SAED analysis results, which proves that these two methods can effectively characterize the ORs of HCP-FCC phase transition and predict possible FCC phase variants.

Keywords: high purity titanium; FCC phase; TKD; pole figure; transformation matrix

1. Introduction

Pure titanium (Ti) is a rare metal and widely used in aerospace, automobile, Micro-Electro-Mechanical System (MEMS) and other engineering fields. It is well known that pure Ti has HCP crystal structure and body-centered cubic (BCC) structure at ambient and high temperature conditions, respectively [\[1\]](#page-9-0). Pure Ti is easily oxidized during rolling process at high temperature, while room temperature is required to ensure its purity. However, the stable Ti phase at ambient conditions is HCP phase, which shows a poor ductility. In recent years, some new phase transitions of pure Ti have been discovered, such as an allotropic phase transformation from the HCP $α$ -Ti to the hexagonal $ω$ -Ti during high-pressure torsion (HPT) [\[2\]](#page-9-1) and the HCP-Ti to FCC-Ti transition [\[3\]](#page-9-2). However, the latter is of great interest for the researchers. Hong et al. [\[3\]](#page-9-2) refined pure titanium grains with equal-channel angular pressing (ECAP), and found the transition from HCP-Ti to FCC-Ti. The FCC-Ti is nucleated in the deformation cross-slip zone with the implementation of tensile deformation of pure titanium foil, which belongs to a stress-induced phase transformation. Other authors also have reported the HCP-Ti to FCC-Ti transformation during the deposition of pure Ti thin films [\[4\]](#page-9-3), plastic deformation [\[1](#page-9-0)[,5](#page-9-4)[–9\]](#page-9-5), and heat treatment process [\[1](#page-9-0)[,10](#page-9-6)[–13\]](#page-9-7). The stability of FCC-Ti in pure titanium has been proved by molecular dynamics theory [\[14\]](#page-9-8)

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and first principles calculation [\[15](#page-9-9)[,16\]](#page-9-10). The HCP-Ti to FCC-Ti transition also appears in titanium alloys [\[17](#page-9-11)[,18\]](#page-9-12) and in Nb-Ti-Si based alloys [\[19\]](#page-9-13).

Niu et al. [\[20\]](#page-9-14) found that the deformation mechanism was composed of dislocation slip, twins and HCP→FCC phase transition. The phase transition from HCP to FCC expands the volume of unit cell ~10.5%, and it is expected that the phase transition contributes about 3.6% to the applied strain. Bai et al. [\[21\]](#page-9-15) considered that in the rolling process of high purity titanium, apart from twinning [\[22–](#page-10-0)[24\]](#page-10-1) and dislocation mechanism [\[25\]](#page-10-2), the HCP-FCC phase transition has an important contribution to its elongation process. These show that the HCP-FCC phase transition can occur easily when pure titanium undergoes large plastic deformation at room temperature, which coordinates the deformation.

There will be a certain orientation relationship (OR) between the new phase and the matrix after phase transformation. Two kinds of ORs between HCP (α) and FCC have been discovered [\[6](#page-9-16)[,9\]](#page-9-5), known as B type: $\langle1\overline{2}10\rangle_\alpha//\langle1\overline{1}0\rangle_{\text{FCC}}$, $\{0001\}_\alpha//\{111\}_{\text{FCC}}$ and P type: $\langle0001\rangle_\alpha/\slash\langle001\rangle_{\text{FCC}}$, $\{10\overline{1}0\}_\alpha/\slash\{110\}_{\text{FCC}}$. Zheng [\[6\]](#page-9-16) and Zu [\[26\]](#page-10-3) found that the P type is accomplished by shuffle and shear shuffle mechanism, while B type depends on the mechanism of Shockley partial dislocation. Ren et al. [\[14\]](#page-9-8) performed the molecular dynamics simulation of uniaxial tension of titanium single crystal nanocolumns along the $\{0001\}_{\alpha}$ plane, which revealed that the phase transition is mainly controlled by the local dislocation slip and stacking fault. In order to study the formation mechanism and characteristics of FCC new phase in matrix, the deep dicussion of OR between two phases is necessary.

Most researchers [\[3](#page-9-2)[,6](#page-9-16)[,20](#page-9-14)[,26\]](#page-10-3) study the phase transition and orientation relationship from HCP-Ti to FCC-Ti via TEM. In this paper, we utilize both TEM and TKD to observe the phase transition ORs. TKD clarified the ORs, which was consistent with that via TEM. Meanwhile, the pole figure and phase transition matrix of the ORs was obtained, based on the results of TEM and TKD analysis. When the phase transition between HCP and FCC obeys the specific OR, the parallel crystal directions and planes of the two phases can be accurately expressed by pole figures and phase transition matrix, and the variants meeting the OR can be predicted.

2. Experimental Material and Procedure

The raw material of high purity Ti (HP-Ti) was supplied by Ningbo Chuangrun New Materials CO., LTD, Ningbo, China. Sheet samples of 11 mm \times 30 mm \times 60 mm size were cut from the raw material, and multi-pass symmetrical rolling was performed to prepare a thin strip with a thickness of 0.86 mm with about 92% total reduction in thickness, as shown in Figure [1.](#page-2-0) Details of the equipment and processing for cold-rolling can be found in the previous literature reports [\[27,](#page-10-4)[28\]](#page-10-5). Talos F200X TEM (Thermo Fisher, Waltham, MA, USA) examinations were used to investigate the FCC-Ti in HCP matrix. A 0.3 mm slice was cut from the sheets by wire cutting, then mechanically polished, and a sample with a diameter of 3 mm and a thickness of 50 μ m was treated by ion milling in order to prepare the sample for TEM analysis.

The FCC-Ti is nanoscale in size and TKD was used to characterize the ORs between HCP-Ti and FCC-Ti. For efficient TKD testing, the cold-rolled strips were annealed at 500 ◦C for 1 h under Argon protection. A Zeiss AURIGA FIB-SEM workstation equipped with TKD capability was carried out to characterize the TEM foils. TKD testing was performed at 30 kV and a step size of 50 nm.

Figure 1. Micro-rolling mill and thin strip samples. (a) Experimental setup; (b) raw material of high with a thickness of 0.86 mm. purity; (**c**) a thin strip with a thickness of 0.86 mm.

The FCC-Ti is nanoscale in size and TKD was used to characterize the ORS between the ORS between the ORS between $H_{\rm F}$ and $F_{\rm F}$ and $F_{\rm F}$ the cold-rolled strips were annealed strips were annealed at 500 **3. Results and Discussion**

α for α and α *3.1. TEM Observations*

Figure [2](#page-3-0) shows the TEM images of the samples after cold-rolling. Some deformation lath structure with the width ranging from 30 nm to 50 nm was found in Figure [2a](#page-3-0). It divides the subgrain into two parts. The deformation zone almost runs through the whole *3.1. TEM Observations* grain and sub-grain, which plays a significant role for the grain refinement, and is similar to the twinning. Figure [1b](#page-2-0) shows the SAED pattern of deformation lath and its adjacent matrix. The analysis shows that the zone axis of hexagonal phase (α-HCP) is $\overline{[12\overline{1}3]}_{\alpha}$, while the deformation band has FCC crystal structure, and the zone axis is $[112]_{\rm FCC}.$ The lattice parameters of HCP phase are calculated as a = 0.298 nm and c = 0.471 nm and the lattice parameter of FCC phase is a_{FCC} = 0.425 nm. These lattice parameters are consistent with the other studies [3,29]. This shows that the deformat[ion](#page-2-0) laths in Figure 1a are FCC phase structure, instead of deformed twins at this deformation range [\[9,](#page-9-5)[30\]](#page-10-7). In recent years, many researchers have reported that the pure titanium changes from HCP phase to FCC phase under large deformation along with the formation of FCC phase deformation lath [3,7,20,31]. [Th](#page-3-0)e OR of the two phases obtained from Figure 2b is as follow: observed that there is a deformation lath in a sub-grain with a size of about 1 µm, which

$$
\left[\overline{1}2\overline{1}3\right]_{\alpha}//[112]_{\text{FCC}} \quad (10\overline{1}0)_{\alpha}//[220]_{\text{FCC}} \quad (1\overline{2}12)_{\alpha}//[11\overline{1}]_{\text{FCC}} \tag{1}
$$

Figure 2. (a,c,e) TEM pictures and (b,d,f) SAED patterns of the FCC-Ti lath structure and matrix, three determination positions of SAED were remarked by circles in TEM pictures, respectively. positions of SAED were remarked by circles in TEM pictures, respectively.

Figure [2d](#page-3-0) shows the SAED pattern analysis in which the deformation lath is marked by a circle in Figure 1c is also FCC-Ti phase, and its lattice constant is *a* = 0.425 nm. The OR between the two phases in Figure 2c,d is calibrated as follows:

$$
\left[1\overline{2}10\right]_{\alpha}/\left[110\right]_{\text{FCC}} \quad (0002)_{\alpha}/\left(002\right)_{\text{FCC}} \quad (10\overline{1}0)_{\alpha}/\left(2\overline{20}\right)_{\text{FCC}} \tag{2}
$$

Figure [2e](#page-3-0) is another typical TEM picture of the FCC-Ti lath. The lattice parameters of HCP and FCC phases are consistent with the results in Figures 2b and [1d](#page-2-0). The OR between HCP-Ti and FCC-Ti is:

$$
[0001]_{\alpha}//[001]_{\text{FCC}} \quad (10\bar{1}0)_{\alpha}//(220)_{\text{FCC}} \quad (1\bar{2}10)_{\alpha}//(2\bar{2}0)_{\text{FCC}} \tag{3}
$$

The β -Ti alloys mainly exhibit ω phase transformation, which is claimed to be caused of heterogeneous nucleation of the α phase [\[32\]](#page-10-9). Recently, the phase transformation from the HCP α -Ti to the hexagonal ω -Ti was appeared during the high-pressure torsion (HPT) [\[2\]](#page-9-1). In this work, hexagonal ω -Ti phase transition is not found by TEM analysis, which is examined by the difference of SAED patterns between hexagonal ω-Ti and HCP-Ti.

The previous literature reports show that the FCC phase in pure-Ti is Ti-H hydride, not FCC-Ti [\[33](#page-10-10)[–35\]](#page-10-11). In our previous work [\[21\]](#page-9-15), it is found that FCC phase has better plasticity than HCP-Ti, and FCC phase can reverse to HCP phase during deformation. If the FCC phase is Ti-H hydride, its plasticity will be poor. Meanwhile, the transition from FCC Ti-H to HCP phase will not exist during deformation. Therefore, it can be confirmed that the FCC phase in this work is FCC-Ti instead of FCC hydride.

Figure [3](#page-4-0) shows the HRTEM images of the FCC phase lath. It can be seen in Figure [3a](#page-4-0) that the HCP/FCC interface is straight. Filter inverse fast Fourier transform (FFT) image of FCC and HCP phases are illustrated in Figure [3b](#page-4-0),c. The FFT patterns in Figure [3e](#page-4-0),f also proves the existence of two phases, and satisfies the OR in Expression (3). This result is consistent with other studies $[1,3,4,11,12,14,18,31,36,37]$ $[1,3,4,11,12,14,18,31,36,37]$ $[1,3,4,11,12,14,18,31,36,37]$ $[1,3,4,11,12,14,18,31,36,37]$ $[1,3,4,11,12,14,18,31,36,37]$ $[1,3,4,11,12,14,18,31,36,37]$ $[1,3,4,11,12,14,18,31,36,37]$ $[1,3,4,11,12,14,18,31,36,37]$ $[1,3,4,11,12,14,18,31,36,37]$ $[1,3,4,11,12,14,18,31,36,37]$. In Figure [3d](#page-4-0), the inverse FFT analysis of HCP phase near to the FCC phase shows that the HCP matrix phase contains

a quite few edge dislocations, and the extra half planes are parallel to the $\{10\overline{1}0\}$ planes. This means that the mechanism of phase transition from HCP to FCC is related with the dislocation slipping.

Figure 3. HRTEM and FFT of FCC-Ti laths and HCP matrix. (a) HRTEM; (b,c) Filter inverse FFT image; (d) dislocation in HCP-Ti lath; (**e**,**f**) FFT patterns of two phases in (**a**). HCP-Ti lath; (**e**,**f**) FFT patterns of two phases in (**a**).

The microscopic mechanism of the phase transition from HCP to FCC is shown by The microscopic mechanism of the phase transition from HCP to FCC is shown by the schematic diagram in Figure [4.](#page-5-0) The phase transition is caused by the Shockley partial the schematic diagram in Figure 4. The phase transition is caused by the Shockley partial dislocation sliding along the direction $\frac{1}{6}\langle \overline{1}2\overline{1}0\rangle$ on the prism surface $(10\overline{1}0)_{\alpha}$, which is consistent with the results of molecular dynamics theory calculation [\[14\]](#page-9-8), first principles sistent with the results of molecular dynamics theory calculation [14], first principles cal-calculation and TEM analysis [\[3,](#page-9-2)[8,](#page-9-20)[15\]](#page-9-9). Therefore, the transition can improve the plastic defense the position of Γ deformation capability of HP-Ti.

The results of two-phase OR obtained by the SAED patterns analysis are counted in The results of two-phase OR obtained by the SAED patterns analysis are counted in Table [1.](#page-4-1) There are three kinds of relationship formulas with different parallel orientation There is there are three kinds of \mathbf{r} relationship formulas with different parallel orientations and planes in \mathbf{F} is \mathbf{m} and \mathbf{r} . and planes in Figure [2,](#page-3-0) which are named as P_1 , P_2 , and P_3 , respectively.

Type	ORs	Induced From
P_1	$\left[\overline{1}2\overline{1}3\right] _{\alpha}/\left[112\right] _{\text{FCC}}$ $(10\bar{1}0)$ $_{\alpha}$ / $/(2\bar{2}0)$ _{FCC} $(1\overline{2}12)_{\alpha}$ / $/(11\overline{1})_{\text{FCC}}$	Figure 2b
P ₂	$\left[1\overline{2}10\right]_{\alpha}/\left[110\right]_{\text{FCC}}$ (0002) _{α} // (200) _{FCC} $(10\bar{1}0)$ $_{\alpha}$ / / $(2\bar{2}0)$ FCC	Figure 2d
P_3	$[0001]_{\alpha}$ / $[001]_{\text{FCC}}$ $(10\bar{1}0)_{\alpha}$ //(220) _{FCC} $(1\overline{2}10)\frac{1}{\alpha}/(2\overline{2}0)_{\text{FCC}}$	Figure 2f

Table 1. The ORs deduced from the SAED patterns. **Table 1.** The ORs deduced from the SAED patterns.

Figure 4. Schematic of HCP \rightarrow FCC phase transient. (a) HCP-Ti phase structure; (b) FCC-Ti phase structure; (**c**) HCP to FCC phase transient by Shockley partial dislocation. structure; (**c**) HCP to FCC phase transient by Shockley partial dislocation.

3.2. Pole Figures 3.2. Pole Figures

It is wen known that the conventional Electron backscattered diffraction (EBSD) can
be used to determine the ORs between the matrix and the second phase with micron or be used to determine the ORs between the matrix and the second phase with micron or even millimeter scale, for example, ferrite precipitates with its neighboring grain holding even millimeter scale, for example, ferrite precipitates with its neighboring grain holding K-S OR via EBSD in medium carbon steel [\[38\]](#page-10-14). TEM results show that the formation of the FCC-Ti has been proposed to preferred the ORs with the HCP-Ti matrix. At the same time, FCC-Ti laths was ranging from 30 nm to 50 nm. TKD has a significantly higher spatial resolution than the conventional EBSD [\[39\]](#page-10-15). TKD was widely applied in crystal ORs determination and phase mapping on a nanoscale in recent years $[40-42]$ $[40-42]$. It is well known that the conventional Electron backscattered diffraction (EBSD) can

Therefore, it is quite feasible for identification of FCC-Ti phase. Figure [5](#page-6-0) illustrates the FCC-Ti grains, characterized by the TKD testing. As shown in Figure [5a](#page-6-0)–c, the FCC-Ti laths were located both within the α grains and at the grain boundaries. The contoured {0001}, $\{10\bar{1}0\}$, $\{1\bar{2}10\}$, $\{1\bar{2}11\}$, $\{1\bar{2}12\}$, $\{20\bar{2}3\}$, $\{10\bar{1}3\}$ poles of the HCP-Ti grain and $\{100\}$, $\{110\}$, $\{3\overline{10}\}$, $\{2\overline{21}\}$, $\{1\overline{11}\}$, $\{112\}$ poles of the FCC-Ti grain from the marked regions $\frac{1}{2}$ in Figure [5c](#page-6-0) are plotted in Figure [5d](#page-6-0). The parallel alignments of low-index directions and planes are marked by the red arrows, which are the same as those listed in Table 1. Pole figures (PFs) in Figure [5d](#page-6-0) obey the P-type OR between HCP-Ti and FCC-Ti phases: (0.0001) , $//(0.01)$ _{ECC}, $\{10\overline{10}\}$ // $\{110\}$ _{ECC}, which was in agreement with SAED results in Table 1 and PFs result [10]. $\langle0001\rangle_{\alpha}/\langle001\rangle_{\text{FCC}}$, $\{10\bar{1}0\}_{\alpha}/\langle110\rangle_{\text{FCC}}$, which was in agreement with SAED results in Table [1](#page-4-1) and PFs result [\[10\]](#page-9-6).

Figure 5. TKD of the HCP-Ti and FCC-Ti phases. (a) Band contrast (BC); (b) inverse pole figure (IPF), (c) Phase mapping, the red part is HCP-Ti phase and the yellow part is the FCC-Ti phase; (d) PFs of the two phases.

According to the TKD results in Figure 5[, t](#page-6-0)he composite PFs representation of HCPTi and FCC-Ti are satisfying the P-type OR is illustrated in Figure 6. Due t[o s](#page-6-1)ymmetry, only a quarter of the whole PF is shown, which is consistent with other study [9]. FCC-Ti phase may have several variants due to its high symmetry, for example, P_1 $(\overline{1213}]_{\alpha}/[\overline{112}]_{\text{FCC}})$ and P'_1 $(\overline{1213}]_{\alpha}/[\overline{112}]_{\text{FCC}})$ in Figure 6a, P_2 $((\overline{1010})_{\alpha}/(\overline{20})_{\text{FCC}})$ and P'_2 ((10 $\overline{10}$)_{α}//(110)_{FCC}) in [Fig](#page-6-1)ure 6b are all equivalent. It can be concluded from the PF that P_1 , P_2 , and P_3 , the ORs induced from the SAED patterns in Figure 2 are equivalent, but the zone axis is different from each other during TEM analysis. Therefore, the PF is an important method to study the OR and variations of phase transition in HCP and FCC phases. the red part is HCP-Ti phase and the yellow part is the FCC-Ti phase; (**d**) PFs of the two phases.

Figure 6. Composite PFs representation of HCP and FCC satisfying the ORs. (a) Parallel crystal phase, (**b**) parallel plane indexes. orientation indexes of two phase, (**b**) parallel plane indexes.

3.3. Matrix of Orientation Relationships 3.3. Matrix of Orientation Relationships 3.3. Matrix of Orientation Relationships

ORs mean that the second phase (S) and matrix (M) obey the conditions of parallel crystal orientation [uvw] and parallel crystal plane [hkl]. The transformation between crystal orientation and crystal plane, and the relationship between real space and reciprocal space of crystal can be characterized by the transformation matrix [\[29](#page-10-6)[,43](#page-10-18)]. For the sake of simplicity, uppercase (HKL) and lowercase (hkl) represent the crystal plane index of **M** and **S**, respectively, and uppercase [UVW] and lowercase [uvw] represent the crystal orientation index of matrix and second phase, respectively.

It is known that the transformation matrix [**B**] of the parallel crystal orientation index of **M** and **S** is [\[44\]](#page-10-19):

$$
[\mathbf{B}] = \left(\begin{array}{ccc} H_1 & K_1 & L_1 \\ H_2 & K_2 & L_2 \\ H_3 & K_3 & L_3 \end{array}\right)^{-1} \left(\begin{array}{ccc} d_1/D_1 & 0 & 0 \\ 0 & d_2/D_2 & 0 \\ 0 & 0 & d_3/D_3 \end{array}\right) \left(\begin{array}{ccc} h_1 & k_1 & l_1 \\ h_2 & k_2 & l_2 \\ h_3 & k_3 & l_3 \end{array}\right) \tag{4}
$$

In which, $(H_iK_iL_i)$ and $(h_i k_i l_i)$ $(i = 1,2,3)$ represent three groups of parallel crystal planes of **M** and **S**, respectively, d_i is the interplanar spacing of the **S** phase $(h_1k_1l_1)$ crystal planes, D_i is the plane spacing of **M** phase $(H_iK_iL_i)$ crystal planes.

The parallel crystal plane index [UVW] and [uvw] of **M** and **S** satisfying the special ORs is converted as follows: $\sqrt{ }$

 $\overline{}$

$$
\begin{bmatrix} U \\ V \\ W \end{bmatrix} = [\mathbf{B}] \begin{bmatrix} u \\ v \\ w \end{bmatrix}
$$
 (5)

It can be deduced that the transformation matrix of the parallel crystal plane indices of M and S phases is $[R] = [B]^T$, and the transformation relationship between matrix and the parallel crystal plane of the second phase (HKL) and (hkl) is as follows [\[44\]](#page-10-19):

$$
\begin{bmatrix} \mathbf{h} \\ \mathbf{k} \\ 1 \end{bmatrix} = [\mathbf{R}] \begin{bmatrix} \mathbf{H} \\ \mathbf{K} \\ \mathbf{L} \end{bmatrix} = [\mathbf{B}]^{\mathrm{T}} \begin{bmatrix} \mathbf{H} \\ \mathbf{K} \\ \mathbf{L} \end{bmatrix}
$$
 (6)

Formulas (5) and (6) show that if the M phase crystal plane (HKL) and crystal orientation [UVW] are known, the **S** phase crystal plane (hkl) and crystal orientation [uvw] can be obtained and vice versa.

As long as the matrix [**B**] is obtained, the crystal plane index or orientation index of **M** and **S** phases with specific ORs can be obtained. According to the ORs obtained by SEAD in Figure [1,](#page-2-0) three groups of parallel crystal planes $(H_1K_1L_1)/((h_1k_1L_1), (H_2K_2L_2)/((h_2k_2L_2),$ $(H_3K_3L_3)//(h_3k_3l_3)$ of α -HCP and the second FCC phase are, respectively, taken as $(10\bar{1}0)_{\alpha}/(220)_{\text{FCC}}$, $(1\bar{2}10)_{\alpha}/(2\bar{2}0)_{\text{FCC}}$, $(0002)_{\alpha}/(002)_{\text{FCC}}$.

The lattice parameters of HCP phase a_α = 0.298 nm, c = 0.471 nm; The lattice parameter of FCC phase is $a_{FCC} = 0.425$ nm. The above parameters are substituted into formula (4) to obtain matrix [**B**] and transpose matrix $[\textbf{B}]^{\mathrm{T}}$.

$$
\begin{bmatrix} \mathbf{B} \end{bmatrix} = \begin{bmatrix} 1.208305 & 1.208305 & 0 \\ -0.442270 & 1.650576 & 0 \\ 0 & 0 & 0.940299 \end{bmatrix}
$$
(7)

$$
\begin{bmatrix} \mathbf{R} \end{bmatrix} = \begin{bmatrix} 1.208305 & -0.442270 & 0 \\ 1.208305 & 1.650576 & 0 \\ 0 & 0 & 0.940299 \end{bmatrix}
$$
 (8)

Tables [2](#page-8-0) and [3](#page-8-1) show the possible parallel relationship between crystal plane and orientation predicted by [**B**] and [**R**] transformation matrix. Only some low orientation indexes and plane indexes are listed in the Tables [2](#page-8-0) and [3,](#page-8-1) which correspond to the points in the pole maps in Figure [5.](#page-6-0) It should be pointed out that the ORs obtained by transformation matrix is different from the result of edge-to-edge matching model prediction [\[45\]](#page-10-20). This model has been used to predict the OR between HCP Mg alloys and the FCC-precipitates via diffusion-controlled phase transformations.

$(HKIL)_{HCP}$	$(HKL)_{HCP}$	$(hkl)_{FC}$ via Matrix Calculation	$(hkl)_{ECC}$ via TKD
(0001)	(001)	[0 0 0.95]	(001)
(1210)	(120)	$[2.10 \, \overline{2.10} \, 0]$	(110)
$(1\overline{2}11)$	$1\overline{2}1$	$[2.09 \overline{2.09} 0.94]$	$(2\overline{2}1)$
$(1\overline{2}12)$	$1\overline{2}2)$	$[2.09 \overline{2.09} 1.88]$	(111)
(1010)	100)	[1.21 1.21 0]	(110)
$(20\bar{2}3)$	(203)	[2.42 2.42 2.85]	(111)
(1013)	$[103]$	[1.21 1.21 2.82]	(112)
$(20\overline{2}1)$	[201]	[2.42 2.42 0.94]	(221)
(2201)	(221)	$[3.30 - 0.88 0.94]$	(311)
$(3\overline{21}0)$	(320)	[4.51 0.32 0]	(100)
1100)	(110)	$[1.65 - 0.44 0]$	$(3\bar{1}0)$

Table 2. Parallel crystal orientation indexes predicted by transformation matrix and PFs.

Table 3. Parallel crystal plane indexes predicted by transformation matrix and PFs.

$(uvw)_{ECC}$	$(UVW)_{HCP}$ by Matrix Calculation	$(UVtW)_{HCP}$	$(UVtW)_{HCP}$ via TKD
$[1\overline{1}0]$	$\left[0 - 2.10\,0\right]$	$[0.70 \overline{1.40} \ 0.70 \ 0]$	$[1\overline{2}10]$
$\left[\overline{3}32\right]$	[0 6.29 1.90]	[2.10 4.20 2.10 1.9]	$[1\overline{2}11]$
$[1\overline{1}1]$	$\overline{0}$ $\overline{-2.10}$ 0.95	$[0.70 \overline{1.40} \ 0.70 \ 0.95]$	$\sqrt{2423}$
$[2\overline{2}3]$	$[0\ \overline{4.20}\ \overline{2.85}]$	$[1.40 \ \overline{2.80} \ 1.40 \ \overline{2.85}]$	$\left[1\overline{2}1\overline{2}\right]$
$\overline{1}12$	[0 2.10 1.90]	$\sqrt{0.70}$ 1.40 $\sqrt{0.70}$ 1.9	$\overline{1}2\overline{1}3$
$[110]$	[2.42 1.21 0]	$[1.21 \ 0 \ \overline{1.21} \ 0]$	$[1010]$
$[3\overline{1}3]$	$[2.42 \overline{2.98} \overline{2.85}]$	$[2.61 \overline{2.79} 0.18 2.85]$	$[1\overline{1}01]$
$[111]$	[2.42 1.21 0.95]	$[1.21 \ 0 \ \overline{1.21} \ 0.95]$	$[1011]$
$[112]$	[2.42 1.21 1.9]	$[1.21 \ 0 \ \overline{1.21} \ 1.90]$	$[20\overline{2}3]$
$[113]$	[2.42 1.21 2.84]	$[1.21 \ 0 \ \overline{1.21} \ 2.85]$	$[10\overline{1}2]$
$[1\overline{2}0]$	$\left[\overline{1.21} \,\overline{3.75} \,0 \right]$	$[0.44 \overline{2.10} 1.65 0]$	$[1\bar{5}40]$
[001]	$[0\;0\;0.95]$	[0 0 0 0.95]	[0001]

Even though [**B**] and [**R**] transformation matrix is obtained by P3 OR, the calculation results in Tables [2](#page-8-0) and [3](#page-8-1) are consistent with P1 and P2 ORs. These results are also consistent with the P-type OR reported in literatures. The P-type OR has the same mechanism of phase transition as the Shockley partial dislocation sliding along the direction $\frac{1}{6}\langle\overline{1}2\overline{1}0\rangle$ on the prism surface $(10\overline{1}0)_{\alpha}$ shown in Figures [3](#page-4-0) and [4.](#page-5-0)

Therefore, when the phase transition between HCP and FCC satisfies the specific crystallographic OR, the parallel crystal orientation and crystal plane indexes of the two phases can be accurately expressed by PFs and transformation matrix, and the second phase variants satisfying the OR can be predicted.

4. Conclusions

(1) A large number of FCC-Ti laths are found in the rolling structure of high purity titanium, and the OR between HCP and FCC phases is P type: $\langle 0001 \rangle_{\alpha} / / \langle 001 \rangle_{\text{FCC}}$ $\{10\overline{1}0\}_{\alpha}/\{110\}_{\text{FCC}}$. The width of FCC-Ti laths is from 30 nm to 50 nm.

(2) According to the OR, the deformation mechanism of the phase transformation process is mainly realized by dislocation slip mechanism, and the phase transformation is caused by the Shockley partial dislocation sliding along the direction $\frac{1}{6}\langle\overline{1}2\overline{1}0\rangle$ on the prism surface $\left\{10\overline{1}0\right\}_{\alpha}$.

(3) Phase mapping and PF functions of TKD were quite feasible for the OR identification of a nanoscale FCC-Ti phase. When the phase transition between HCP and FCC obeys the specific crystallographic OR, the parallel crystal directions and planes of the two phases can be accurately expressed by pole figures and phase transition matrix, and the variants meeting the OR can be predicted.

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