

Article **High Mechanical Property and Texture Degree of Hot-Extruded Bi0.905Sb0.095**

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Abstract: Bi_{1−x}Sb_x crystal is one of the best n-type thermoelectric materials below 200 K, but its weak mechanical strength hinders practical applications for deep refrigeration. Herein, we adopted the mechanical enhancement method of hot extrusion to investigate the comprehensive mechanical and thermoelectric properties of $Bi_{0.905}Sb_{0.095}$. It revealed that reducing the grain size of the matrix and increasing the extrusion ratio can improve the gain size uniformity and mechanical properties. Meanwhile, the thermoelectric performance depends on the texture, grain size, and local composition. The extruded sample prepared by ingot with the high extrusion ratio of 9:1 generated uniform small grains, which resulted in the high bending strength of Bi_{1-x}Sb_x~130 Mpa and a high power factor of ~68 µW \cdot cm $^{-1}\cdot$ K $^{-2}$ @173 K, as well as the relatively high figure of merit of 0.25@173K. This work highlights the importance of the uniform distribution of the grain size and the compositions for $Bi_{1-x}Sb_x$, as well as the required universal key parameter for the hot extrusion method.

Keywords: Bi_{1−x}Sb_x; thermoelectric material; hot extrusion; mechanical strength

1. Introduction

Solid-state thermoelectric cooling (TEC) technology, which can directly convert electrical and thermal energy, has the advantages of compact size, no mechanical motion, high reliability, and high precision of temperature control [1-[3\]](#page-8-1). To date, it has become an important heat management thermal profile used for infrared detection, [\[4\]](#page-8-2) bioanalytical devices, [\[5\]](#page-8-3) semiconductor lasers, [\[6\]](#page-8-4) etc. The cooling temperature difference (∆*T*) of the thermoelectric cooling device depends on the figure of merit *zT* (*zT* = $S^2 \sigma T / \kappa$) of thermoelectric materials, where *T* is the absolute temperature, *S* is the Seebeck coefficient, σ is the electrical conductivity, and κ is the thermal conductivity, respectively [\[7\]](#page-8-5). Currently, Bi_2Te_3 is the best-performing thermoelectric material near room temperature. The $Bi₂Te₃$ -based single-stage TEC devices can achieve a ΔT_{max} of about 70 K at room temperature, [\[8\]](#page-8-6) and the four-stage cooling device can achieve a $\Delta T_{\rm max}$ of 133 K at 282 K, [\[9\]](#page-8-7) which almost reaches the cooling limit for $Bi₂Te₃$ -based TEC devices, due to the quick deteriorations of the TE performance in the low-temperature range $[10,11]$ $[10,11]$. Therefore, there is an urgent need for thermoelectric cooling materials with high TE properties near liquid nitrogen temperature.

The layered $Bi_{1-x}Sb_x$ alloy, as one of the earliest n-type thermoelectric materials, has been considered the best thermoelectric material below 150 K [\[11,](#page-8-9)[12\]](#page-8-10). On the one hand, because the electrons and holes along the two directions of [001] and [100] of Bi display strong anisotropic transports, i.e., (*σe*/*σ^h*)// = 9.19 and (*σe*/*σ^h*)[⊥] = 2.12 (// and ⊥ present parallel and perpendicular to the [001] direction) at room temperature, [\[13\]](#page-9-0) it suppresses the common deterioration of different charge carriers for the thermoelectric power in low

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TE materials, i.e., the Seebeck coefficient, according to the two-band mode [\[13\]](#page-9-0). Thus, the anisotropic transports of two different carriers result in a high Seebeck coefficient along the [001] direction, which then gives rise to the high-power factor (PF, PF = $S^2\sigma$) of ~77 µW⋅cm⁻¹⋅K⁻² at 300 K and ~200 µW⋅cm⁻¹⋅K⁻² at 100 K, [\[14](#page-9-1)[,15\]](#page-9-2) being much higher than those of Bi_2Te_3 [\[10,](#page-8-8)[16\]](#page-9-3). However, the high thermal conductivity, originating from both high electric and lattice thermal conductivity, brings about the low *zT* value of Bi metal (only 0.18 @ 100 K) [\[14\]](#page-9-1). On the other hand, both bismuth and antimony are semimetals and can form infinite solid solutions due to their similar crystal structures [\[17\]](#page-9-4). When the Sb content is between 7% and 22%, the $Bi_{1-x}Sb_x$ crystals display semiconductor band features, favoring the reduction in thermal conductivity and the improvement of the TE performance [\[18\]](#page-9-5). Therefore, in 1972, Yim and Amith fully investigated the temperaturedependent anisotropic thermoelectric properties of $Bi_{1-x}Sb_x$ single crystals [\[14\]](#page-9-1). When alloying Sb into Bi, particularly for $\text{Bi}_{92}\text{Sb}_{8}$, it can maintain the expected high-power factor and effectively reduce lattice thermal conductivity, producing a high *zT* of about 0.6@100 K along the [001] direction.

Despite $Bi_{1-x}Sb_x$ single crystals exhibiting good thermoelectric properties, their poor mechanical performances have hindered their practical applications. In the past decades, powder metallurgy combined post-deformation [\[19](#page-9-6)[–22\]](#page-9-7) extrusion [\[23–](#page-9-8)[26\]](#page-9-9), and hot-pressing [\[27](#page-9-10)[–29\]](#page-9-11) have been utilized to improve mechanical strength. The reduction in grain size can effectively prevent further extension of the fracture and then improve the mechanical properties. At the same time, it also can scatter more phonons and thus reduce the thermal conductivity. However, polycrystalline samples lost the most important factor of high TE performance achievement for $Bi_{1-x}Sb_x$, namely, out-plane texture. As a result, polycrystalline Bi1−xSb^x deteriorates the electrical properties and the *zT* value. In 2020, a single crystal grown by the Czochralski technique was used for extrusion to maintain the [001] orientation, which has successfully improved the mechanical strength and reduced the thermal conductivity [\[23\]](#page-9-8). When the extrusion ratio is 10, the extruded sample obtained a high bending strength of ~65 MPa at room temperature and a relatively higher peak *zT* of 0.45 around 140 K compared to the powder metallurgy methods. Based on this high TE performance at a low temperature, the lowest cooling temperature of 140 K from 300 K has been achieved by the six-stage TEC device consisting of $n-Bi_{0.91}Sb_{0.09}/p-Bi_2Te_3$ in the ultra-low temperature two-stage module and traditional n/p -Bi₂Te₃ materials for the other four-stage module [\[30\]](#page-9-12).

It is known that the sample undergoes three main processes during the hot extrusion; one is the grain crack owing to the shear stress in the transition region of the die from large to small diameter, another is the grain rearrangement when passing through the transition region, and the last one is the grain growth at hot temperature [\[31](#page-9-13)[–34\]](#page-9-14). Because of the nonuniform distribution of shear stress and temperature distribution along the radial direction, it would produce a nonuniform distribution of the grain size in the sample, which should be eliminated for the precise evaluation of materials' TE performances and the fabrication of reliable TEC devices. Increasing the extrusion ratio (K_e) and extrusion angle is beneficial for improving the quality of the extruded sample [\[32\]](#page-9-15). Therefore, in this work, we systematically investigated the parameters affecting the grain size distribution, mechanical strength, and TE properties by using different matrices and the *K*e. We discovered that reducing the grain size of the matrix and increasing the *K*^e can improve the uniformity of grain size.

2. Materials and Methods

Synthesis: Based on the high TE performance reported in [\[14\]](#page-9-1), $Bi_{0.905}Sb_{0.095}$ was chosen as the research object. The ingot was obtained by melting the raw material (5 N) at the stoichiometric ratio under a vacuum of 1.0 Pa at 1073 K for 3 h and then quenching in water. Interestingly, the ingot shows an obvious cleavage of (001) plane along the axial direction, which would affect the textures of the extruded samples, but not affect the gain size distributions. Two inner diameters (20 mm and 30 mm) of the quartz tubes were

used to load the raw materials to produce the ingot with different diameters for extrusion (marked as Ingot-HE). In addition, some ingot was also ball milled to reduce the grain size to 1–10 μm, which was placed in the center of a larger graphite die with an inner diameter of 30 mm for hot-pressing, performing at a temperature of 473 K under a pressure of 50 MPa for 30 min. The hot-pressed samples with high density (>95% of the theoretical density) were used for extrusion (marked as BM-HE). The extrusion ratio of 4:1 and 9:1 for the ingot and 9:1 for the pressed sample at 473 K and a punch speed of \sim 0.2 mm/min were used for hot extrusion to investigate the main parameters affecting the grain size distribution.
The middle part of the part of the The obtained samples by hot extrusion have high densities (>98%). The middle part of measurement of matrices of matrices in the measurement of matrices of matrices of matrices of matrices of matrices of matrices of matrice the extruded sample was used for the measurement. The schematic diagram of matrices $\frac{1}{2}$ preparation and the hot extrusion, as well as the extruded samples, are shown in Figure [1.](#page-2-0) 1.

Figure 1. Schematic diagram of hot extrusion, matrices preparation, and the hot extrusion. The right **Figure 1.** Schematic diagram of hot extrusion, matrices preparation, and the hot extrusion. The right is the extruded samples. is the extruded samples.

Characterization: The phase composition of the samples was characterized using X-Characterization: The phase composition of the samples was characterized using ray diffraction equipment (D8 Advance, Bruker, Karlsruhe, Germany, Cu *K*α radiation, *λ* X-ray diffraction equipment (D8 Advance, Bruker, Karlsruhe, Germany, Cu *K*α radiation, $\lambda = 0.15406$ nm) in the range of $2\theta = 20°$ –70°. A scanning electron microscope (Thermo Fisher Scientific, Waltham, MA, USA, Apreo 2) was used to observe the microstructure (SEM) and determine the element distribution (EDS). The Seebeck coefficient and electrical conductivity were measured by LSR-1 from LINSEIS, Selb, Germany. The Seebeck coefficient was obtained by linearly fitting the potential difference at different temperature differences, and electrical conductivity was measured by the Vanderbilt method, which differences, and electrical conductivity was measured by the Vanderbilt method, which can accurately measure two-dimensional planar samples of arbitrary shapes. The Hall coefficient of arbitrary shapes. The Hall coefficient (*R_H*) above 300 K was determined using the van der Pauw method with Xiangjin selfmade Hall electrical performance test system (NYMS) in a helium atmosphere. Hall car-self-made Hall electrical performance test system (NYMS) in a helium atmosphere. Hall carrier concentration (n_H) was estimated as $n_H = 1/eR_H$. Thermal diffusion (D) was mea-
samed lands the three initials are the state of OUTIZCCU UEAACZ. Fund fund Converged. The by the transient laser flash method (NETZSCH-LFA467, Frankfurt, Germany). The total total thermal conductivity (κ_{total}) was calculated by the relation of $\kappa_{total} = D\rho C_p$, where \mathcal{L}_{p} is the heat capacity and *p* is the density of samples measured by Archimedes' method. Due to the Debye temperature of $\text{Bi}_{0.9}\text{Sb}_{0.1}$ being 128.5 K [\[35\]](#page-9-16), the *C_p* within 175 K and the Debye temperature of Bi0.9Sb0.1 being 128.5 K [35], the *Cp* within 175 K and 300 K of 300 K of material was calculated by the Dulong–Petit law. The three-point bending strength $\frac{1}{2}$ material was calculated by the Dulong–Petitive material $\frac{1}{2}$ material $\frac{1}{2}$ and $\frac{1}{2}$ the cample was total wing–2 universal toting machine, with a looding speed of of the sample was tested using a universal testing machine, with a loading speed of 0.02 mm/min 0.02 mm/min . sured by the transient laser flash method (NETZSCH-LFA467, Frankfurt, Germany). The *C^p* is the heat capacity and *ρ* is the density of samples measured by Archimedes' method.

3. Results and Discussion

Characterization

In order to evaluate the texture degree of the extruded sample which is significant for the high thermoelectrical properties, PXRD patterns were measured and the texture degree was calculated based on the diffraction patterns by the Lotgering method: $F = \frac{P - P_0}{1 - P_0}$ $\frac{1-1}{1-P_0}$ P_{0} *I*0(00*l*) $\frac{I_0(00l)}{\sum I_0(hkl)},\ P\ =\ \frac{I(00l)}{\sum I(hkl)}$ $\frac{I(00I)}{\sum I(hkl)}$, where *I*(*hkl*) and *I*₀(*hkl*) are the peak integral intensities for the measured and randomly oriented samples, respectively [\[36\]](#page-9-17). All PXRD peaks agree with the standard peak of ICSD-192132 [\[37\]](#page-9-18), which can be seen in Figure [2a](#page-3-0), indicating the high purities of all extruded samples. The texture direction of the material is very important in the practical fabrication of the thermoelectric device. Notably, both $Bi_{1-x}Sb_x$ and $Bi₂Te₃$ feature layered structures, resulting in the (001) plane as the main slip plane for both materials. However, for $Bi_{1-x}Sb_x$, there are other main slip systems of (100)[011] and (111)[101], which have been confirmed by the pressure along the direction of $[211]$ [\[20\]](#page-9-19). In contrast, for Bi_2Te_3 , the (015) plane would be another main slip plane due to the weak bonds vertical to (015). It needs to be mentioned that the (001) plane is vertical to the (100) plane, and forms 79.16 \degree with the (111) plane for $Bi_{1-x}Sb_x$. Thus, the grain can slip in the (100) and (111) planes when the pressure or stress deviates from the (001) in-plane direction, giving rise to a weak $F_{(001)}$ value parallel to the pressure direction. However, the (015) and (001) planes of Bi_2Te_3 form an angle of 57.98 $^{\circ}$, which is much closer to the (001) plane than the main slip planes of (100) and (111) for $Bi_{1-x}Sb_x$. As a result, the texture factor of the (001) plane for Bi_2Te_3 is higher parallel to the pressure direction than that vertical to the pressure direction, [\[24\]](#page-9-20) and this phenomenon is contrary to that of $Bi_{1-x}Sb_x$. Despite the different directions of the extruded Bi1−xSb^x and Bi2Te³ samples for the high *F*(001) value, the textures parallel to the pressure for both materials reveal their higher TE performances along this direction due to their different anisotropic transports. Therefore, the extruded $Bi_{1-x} Sb_x$ also favors the practical fabrication of the device. Besides, due to the higher initial texture of the matrix of BM-HE vertical to the pressure direction (ingot show (001) cleavage along the pressure direction), resulting in the higher $F_{(001)}$ vertical to the pressure direction.

Figure 2. Phase analyses of the extruded samples. (a) PXRD patterns, the arrows indicate the X-ray direction. (**b**) EDS mappings of ingot-HE and BM-HE samples. direction. (**b**) EDS mappings of ingot-HE and BM-HE samples.

The EDS mapping results presented in Figure 2b show different ratios of Bi and Sb for the sample prepared by different conditions. In detail, the ingot-HE with $K_e = 4:1$ displays a large deviation from the nominal ratio of the composition. It would be derived from the gravitational field and large difference of the element mass for Sb and Bi, which result in the segregation of the Sb along the axial direction of the ingot and the ingot-HE samples [\[17\]](#page-9-4). In contrast, after remixing the different parts of the ingot, the BM-HE shows a closed atomic ratio of $Bi_{0.905}Sb_{0.095}$, but still with a nonuniformity in the micro range. Notwithstanding, the BM-HE can improve the element distribution in the macro range. The selected part of the ingot-HE with $K_e = 9:1$ shows a close nominal ratio of the composition, which would be beneficial to the high TE performance.

The grain size distribution was characterized by the SEM measurement, which can be seen in Figure [3.](#page-4-0) The Ingot-HE with $K_e = 4.1$ shows significantly different grain sizes around the edge ($\text{25 }\mu\text{m}$) and the middle ($\text{57 }\mu\text{m}$) of the sample. When K_e increased to 9:1, the difference in grain sizes reduced and the majority of grains were within the range of $10-40 \mu m$ for the edge and $4-20 \mu m$ for the middle according to the statistics of the grain size. The average grain sizes were estimated to be \sim 8.2 μ m and \sim 6.5 μ m for the edge and middle parts, respectively, by the method of total area dividing the number of grains. It is reasonable that increasing *K*^e is to increase the deformation extent, which could induce more proportion of the sample to experience the first two main processes, i.e., crack and rearrangement. Besides, increasing the extrusion ratio and extrusion angle also improves the uniform distribution of stress, and then improves the uniformity of grain size. Furthermore, the BM-HE sample with $K_e = 9:1$ shows an almost uniform distribution of the grain size between 2 and 15 μ m for the whole sample, and the relevant average grain size is \sim 2.8 μ m and 2.7 μ m for the edge and middle parts. Therefore, reducing the grain size of the matrix and increasing the K_e can improve the uniformity, which is consistent with the finite element simulation [\[32\]](#page-9-15).

Figure 3. Grain size distributions of the extruded samples. SEM images of the fracture surface for **Figure 3.** Grain size distributions of the extruded samples. SEM images of the fracture surface for Ingot-HE with (a) $K_e = 4:1$, (b) $K_e = 9:1$, (c) BM-HE with $K_e = 9:1$ around the edge and the middle of the samples. the samples.

Mechanical performance is an important factor for the practical applications of TE Mechanical performance is an important factor for the practical applications of TE materials, particular for $Bi_{1-x}Sb_x$. The bending strengths of the extruded samples in this work and the measured data in the literature for comparison are shown in Figure 4a. It work and the measured data in the literature for comparison are shown in Figure [4a](#page-5-0). It can be seen that the bending strength increases as the grain size reduces and the value increases from 40 Mpa for the ingot to ~130 Mpa and 140 Mpa for the Ingot-HE and BM-HE with

Figure 4. Bending strength and anisotropic transports. (a) The bending strength of ingot and extruded $Bi_{0.905}Sb_{0.095}$ samples in comparison with the $Bi_{0.905}Sb_{0.095}$ single crystal and extrusion $Bi_{0.9}Sb_{0.1}$ sample [\[23\]](#page-9-8). The temperature dependence of anisotropic electrical and thermal conductivity of BM-HE with $K_e = 9.1$. (b) Electrical conductivity, (c) thermal conductivity, (d) the ratio of the electrical and thermal conductivity. and thermal conductivity.

Due to the high texture of the BM-HE sample. However, despite the BM-HE sample with small grain sizes, the electrical and thermal conductivity at low temperatures .
show strong anisotropic transports, as shown in Figure [4b](#page-5-0)–d. The anisotropic degrees of transport weaken when the temperature increases. This phenomenon originates from the involvement of two transport features of the polycrystal and the single crystal. In detail, as the temperature increases, the electrical and the thermal conductivity of $Bi_{1-x}Sb_x$ polycryst[al](#page-9-9) significantly increases [26,37], but the electrical conductivity of the single crystal has a contrary trend while the thermal conductivity of the single crystal only increases slightly [14]. Therefore, the electrical and thermal conductivities of polycrystalline and crystalline Bi_{1−x}Sb_x around room temperature are closer compared to those at low temperatures. In addition, the parallel to the pressure direction achieves higher *σ/κ* than that of vertical to the pressure; therefore, the TE properties of other samples were only measured along this direction. $\overline{}$

Figure [5a](#page-6-0) displays the comparison of the temperature-dependent electrical conductivity for the three samples in this work: the single crystal vertical and parallel to the [001] direction, crystal-HE, as well as the polycrystal combined hot deformation (HD) $[22,23,26]$ $[22,23,26]$ $[22,23,26]$. The electrical conductivity for Ingot-HE and BM-HE is located between those of single crystal and polycrystal. All samples have similar carrier concentrations around 7.0 \times 10^{18} cm $^{-3}$ Interestingly, the temperature-dependent trend of electrical conductivity transformed from a single crystal to a polycrystal for the Ingot-HE as the K_e increases mainly due to the reduction of the grain size. However, the BM-HE sample with smaller grains almost has the same σ as the Ingot-HE with the same K_e . This is because of the different element ratios of the compositions and the element ratio-dependent anisotropy of electrical conductivity, as and compositions and the clement ratio dependent anisotropy of electrical conductivity, as
well as their different texture degrees. In detail, on the one hand, the electrical conductivity reduces as Sb content increases for the increase of the band gap and the defect scattering. On the other hand, when the ratio of Sb is smaller than 7.5%, the *σ* vertical to the [001] direction is higher than that parallel to [001], but when the ratio is larger than 7.5%, the anisotropy changes, and the *σ* vertical to [001] is smaller than that parallel to [001] [\[14\]](#page-9-1). Therefore, the Sb and Bi elements distribution and their ratio as well as the texture degree are significant for the electrical transport. tures as *ob* content increases for the increase of the *band gap* and the defect station

Figure 5. The temperature dependence of thermoelectric properties of the extruded samples. (**a**) **Figure 5.** The temperature dependence of thermoelectric properties of the extruded samples. (**a**) Elec-Electrical conductivity, (**b**) Seebeck coefficient, (**c**) power factor, (**d**) thermal conductivity, (**e**) effectrical conductivity, (b) Seebeck coefficient, (c) power factor, (d) thermal conductivity, (e) effective thermal conductivity (data of commercial Bi_2Te_3 provided for comparison [\[16\]](#page-9-3)), (**f**) figure of merit. The reported results of the Bi $_{0.92}$ Sb $_{0.08}$ single crystal [\[14\]](#page-9-1) and Bi $_{0.82}$ Sb $_{0.18}$ hot-deformation sample, [\[22\]](#page-9-7) extruded ${\rm Bi}_{0.91}{\rm Sb}_{0.09}$ (single crystal as the matrix) [\[23\]](#page-9-8), and ${\rm Bi}_{0.85}{\rm Sb}_{0.15}$ (polycrystal as the matrix) [\[26\]](#page-9-9) are provided for comparison.

All samples show negative Seebeck coefficients, which are consistent with the n-type TE materials transport. According to the literature [\[14\]](#page-9-1), by increasing the Sb ratio in the range of 0–12% for the single crystal, the Seebeck coefficient increases below 173 K but decreases above 225 K. And the temperature-dependent trend of the Seebeck coefficient also turns from increase to decrease as the ratio further increases. In comparison, the Seebeck coefficients for polycrystals reduce as the temperature increases above 145 K. Therefore, the absolute value and the temperature-dependent trend of the Seebeck coefficient for $Bi_{1-x}Sb_x$ are related to the composition and the morphology, increasing the complexity of analyzing the underlying mechanism. In this work, all Seebeck coefficients decrease as the temperature increases due to the narrow measured temperature range. The temperaturedependent Seebeck coefficients (Figure [5b](#page-6-0)) display a similar trend of *σ* for different *K*e, namely, increasing the *K*^e value promotes the transformation of *S* from single crystal to polycrystal for the Ingot-HE samples. Thus, the *S* of Ingot-HE with $K_e = 9:1$ is higher than that with $K_e = 4:1$. However, BM-HE with the smallest grains shows the smallest *S* value, deviating from the transform trends from single crystals to polycrystals of $Bi_{1-x}Sb_{x}$, which would be derived from the high texture degree.

The PFs of the Ingot-HE samples in this work are closed and located between those of single crystal and polycrystal. They have much higher peak values ~70 μ W·cm⁻¹·K⁻² @173 K than that of the deformed polycrystal as shown in Figure [5c](#page-6-0). However, due to the low Seebeck coefficient, BM-HE displays the lowest PF within the temperature range of 173–300 K, which is even smaller than that of the deformed polycrystal.

The thermal conductivity was measured in the temperature range of 173–300 K as shown in Figure [5d](#page-6-0). Notably, the Ingot-HE with $K_e = 4:1$ displays the highest thermal conductivity in the whole temperature range, and the value is also higher than those of single crystal in-plane and out-plane. The increase in *K*^e produces smaller grains which results in the reduced thermal conductivity for the Ingot-HE for the increased grain boundary scattering for phonons. The thermal conductivities of the Ingot-HE and BM-HE with K_e = 9:1 are located between the values of single crystal in-plane and out-plane $[14]$ but are significantly higher than those of deformed polycrystal [\[22\]](#page-9-7) and crystal-HE [\[23\]](#page-9-8). Notably, this deviation from the data in the literature would be derived from the different measurement methods and equipment. In this work, we adopted the transient laser flash method, which possesses a high precision, while indirect calculation from the *zT* based on the Harman method for the crystal-HE and the absolute method for the single crystal and deformed polycrystal were used in the literature. Therefore, the thermal conductivity for the $Bi_{1-x}Sb_x$ prepared by different methods under the same condition is crucial for a precise comparison.

The high thermal conductivity and high-power factor of the extruded samples in this work favor the achievement of effective thermal conductivity (*κ*eff), which can be applied in heat dissipation. It is another main functional application of TEC devices [\[1\]](#page-8-0). It is calculated by $\kappa_{\rm eff}=\kappa+\frac{PF\cdot T_{\rm H}^2}{2\Delta T}$, where $T_{\rm H}$ is the hot-side temperature of TEC and ΔT is the temperature difference between the two sides [\[38\]](#page-9-21). When the temperature difference is 1 K, κ_{eff} at different hot end temperatures is shown in Figure [5e](#page-6-0), from which we can find the extruded $Bi_{1-x}Sb_x$ with higher κ_{eff} (62–210 W·m⁻¹·K⁻¹) in low−temperature and comparable value with that of the high-cost commercial $Bi₂Te₃$ when $T_H > 290$ K for the Ingot-HE with K_e = 9:1. Therefore, the low-cost extruded $Bi_{1-x}Sb_x$ is also suitable for application in heat dissipation.

The temperature-dependent *zT* values of all samples between 173 K and 300 K are shown in Figure [5f](#page-6-0). Although, the PFs of the hot-extruded samples in this work are significantly higher than those of polycrystalline $Bi_{1-x}Sb_x$ alloys prepared by extrusion [\[26\]](#page-9-9), hot-deformation [\[22\]](#page-9-7), and hot-pressing [\[39](#page-10-0)[,40\]](#page-10-1). The high thermal conductivity measured by the transient laser flash method counteracts the high electrical properties, resulting in that their *zT* values only lie between 0.15 and 0.33, which are much lower than those of the single crystals, and even lower than those of polycrystalline samples. Therefore, the evaluation of the advantage for TE performance by the extrusion method still depends

on the thermal conductivity measured at the same condition for the samples prepared by different methods.

4. Conclusions

In summary, we investigated the grain size distribution and the mechanical strength and thermoelectric properties of hot-extruded nominal $Bi_{0.905}Sb_{0.095}$ by using different matrices of Ingot and ball milling combined with hot pressing as well as the extrusion ratio, discovering the inherent law of the extrusion method that reducing the grain size of the matrix and increasing the extrusion ratio can improve the gain size uniformity and mechanical properties. While, the thermoelectric performance depends on the texture degree, grain size, and local composition. As a result, the extruded sample prepared by Ingot with a high extrusion ratio achieves uniform small grains, producing a high bending strength of ~130 Mpa and a high-power factor of 68 µW·cm⁻¹·K⁻²@173 K, respectively, which is beneficial to the practical application of heat dissipation. Furthermore, the advantage of the extrusion method for the TE performance of $Bi_{1-x}Sb_x$ still requires further evaluation under the same measurement conditions compared to the samples prepared by different methods. Additionally, how to balance the grain size, texture degree, and TE performance is still a scientific issue for the low-temperature $Bi_{1-x}sb_x$ thermoelectric material.

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Data Availability Statement: The original contributions presented in the study are included in the article, further inquiries can be directed to the corresponding authors.

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