

## Article

# The New PWV Conversion Models Based on GNSS and Meteorological Elements in the China Region

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**Abstract:** To address the problems of cumbersome processes, large data, and error accumulation in the calculation of conventional GNSS precipitable water volume (PWV), the multi-factor PWV conversion models were established using the multiple linear regression fitting method. This paper analyzed the correlation between PWV and zenith tropospheric delay (ZTD), surface temperature (T), and atmospheric pressure (P) based on the data from 38 GNSS stations in the China region from 2017 to 2018. The research results showed that the mean deviation of the one-factor PWV conversion model based on the GNSS-ZTD was 12.16 mm, and its RMS was 14.30 mm. After adding surface temperature as an independent variable to form the two-factor PWV conversion model, the mean deviation and RMS decreased to 9.07 mm and 11.15 mm. The mean deviation of the two-factor PWV conversion model based on atmospheric pressure and GNSS-ZTD was 0.31 mm, and its RMS was 0.39 mm. The mean deviation of the three-factor PWV conversion model based on surface temperature, atmospheric pressure, and GNSS-ZTD was 0.33 mm, and its RMS was 0.38 mm. The accuracies of the two-factor and three-factor PWV conversion models were similar. The external precision assessment of PWV conversion models was verified by 12 GNSS stations unused for the modelling establishment. The mean deviation and RMS of the two multi-factor PWV conversion models were both less than 0.16 mm and 0.33 mm, which proves their widespread applicability in the China region.

**Keywords:** GNSS; precipitable water vapor; meteorological elements; zenith tropospheric delay; conversion model



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## 1. Introduction

Rainstorms can easily cause stagnant water in cities and trigger flash floods in the mountains and may lead to derivative disasters such as traffic interruption, landslides, river flooding, and farmland inundation [1–3]. Flood disasters not only harm crops and the forestry, fruit, and fishery industries, but also destroy farmhouses and industrial and agricultural facilities, causing human and animal casualties, as well as serious economic losses [4,5]. Almost all the flood disasters in China's history have been caused by heavy rainstorms [6–9].

Atmospheric water vapor is one of the significant driving forces of climate changes and atmospheric circulation [10–12]. The dynamical variation of atmospheric water vapor is a significant factor in forecasting heavy rainstorm disasters [13–15]. However, it is not practical to monitor atmospheric water vapor at a higher spatiotemporal resolution, predominantly due to the higher operational expenses of traditional sensors such as radiosondes, weather radar, and water vapor radiometers [16–18]. Contemporarily, the Global Navigation Satellite Systems (GNSS) have been one of the new technologies to retrieve the atmospheric precipitable water vapor (PWV) due to its lower cost, higher precision, higher spatiotemporal resolution, 24 h availability, and global coverage [17,19,20].

Studies have shown that GNSS-PWV has the potential to predict severe rainstorms [5,21–23] and to study the climate [24–26]. Previous studies [11,22,27–29] have shown that serious rainstorms occur in the descending trends of GNSS-PWV after PWV reaches its initial peak, which can be an obvious sign for rainstorms' forecasting. Lasota et al. [30] used both radio occultation (RO) and ground-based GNSS observations to study the severe hailstorms that occurred in Bulgaria in 2014 and 2019, and the WRF Model and the ERA5 dataset were used to reproduce the temperature profiles for both hailstorms. Guerova et al. [31,32] used statistical regression analysis, real-time GNSS tropospheric products, and instability indices to predict hail and thunderstorms in Bulgaria.

GNSS-PWV can also be used as an important enhancement factor for numerical weather forecasting models [33–36]. Zhao et al. [37] established a precipitation forecast model with the time change trend and predicted the rainfall events in the next 2–6 h, with a correct rate of 80% and a false alarm rate of 60–70%. He et al. [38] analyzed the six typhoon events that occurred in Hong Kong in 2017, and precise point positioning (PPP) was used to analyze the PWV inversion accuracy, which provided a strong reference for the water vapor characteristics of typhoon forecasting. Liu et al. [39] used a variety of meteorological elements (temperature, air pressure, relative humidity), time-related parameters (annual cumulative day, daily cumulative hour, time integral), and PWV to establish a forecasting model by a three-hidden-layer neural network. More than 95% of rainfall events could be predicted, and the false alarm rate was only about 20%, which is nearly 10% lower than the existing short-term rainfall prediction methods, while the false alarm rate was similar. Benevides et al. [40] suggested that the reliability and precision of weather forecasts could be improved after analyzing the 3D distribution variations of PWV. Therefore, the rapid acquisition of GNSS-PWV has important practical significance for improving the efficiency and accuracy of real-time heavy rainstorm forecasting [40–45].

The traditional GNSS-PWV calculation method first calculates the zenith total delay (ZTD), using the GNSS observation based on the double-difference method or PPP technology, and then, the zenith wet delay (ZWD) can be obtained by subtracting the zenith hydrostatic delay (ZHD) from the ZTD. The ZHD is the main delay for the GNSS signals transmitted in the neutral atmosphere, accounting for more than 90% of the ZTD [46,47]. This means that the precision of the ZHD calculated by the Saastamoinen model will indirectly affect the precision of the ZWD. GNSS-PWV can be obtained from the ZWD multiplied by the water vapor conversion factor ( $K$ ) [10]. The weighted mean temperature ( $T_m$ ) is one of the important parameters to calculate  $K$  for the conversion from the ZWD to PWV.

The calculation process of  $K$ ,  $T_m$ , ZHD, ZWD, and PWV is cumbersome. It also involves a large number of meteorological elements such as the surface temperature ( $T$ ) and air pressure ( $P$ ), which easily results in the error accumulation problem. Yi et al. [48] used regression analysis to establish seasonal and annual PWV conversion models and found that the RMS of the PWV conversion models in each season was less than 1.5 mm, while the maximum error did not exceed 3.3 mm. Therefore, PWV can be directly estimated using the seasonal linear regression equation based on the tropospheric delay for short-term weather forecasting if some stations lack meteorological data in a certain period of time. Fan et al. [49] established a PWV direct conversion model based on seven GNSS stations in the Yangtze River Delta region from 2017 to 2018. The results showed that the RMS of the three-factor PWV model based on GNSS-ZTD, temperature, and pressure was 0.47 mm [50]. Huang et al. [51] used the ERA5 reanalysis data from 2012 to 2017 to construct a vertical-correction PWV model in Mainland China considering the time-varying decreasing factor according to the national and geographical division methods. The model had better interpolation accuracy and stability, especially in southern and western China. Compared with the conventional GNSS-PWV method, the abovementioned PWV conversion methods can not only improve the computing efficiency, but also reduce the error accumulation, but most of the above research aimed at a single station or small-scale continuously operating reference station (CORS) networks.

This paper used the data of 38 GNSS stations selected nationwide in 2017 to analyze the changes and their correlation between PWV and GNSS-ZTD, temperature, and pressure and establish several applicable PWV conversion models nationally. The PWV of twelve GNSS stations that did not participate in the modeling was used as the true value to test the external accuracy and reliability of the PWV conversion models.

The outline of this paper is as follows. The data sources of the GNSS products, the relationships and collinearity of PWV, and other meteorological elements are analyzed and shown in the second section. The establishment of the one-factor, two-factor, and three-factor PWV conversion models and their precisions is shown in the third section. The conclusions are given in the fourth section.

## 2. Data Sources and Methods

### 2.1. Data Sources

The research data in this paper came from the Jiangsu Meteorological Bureau and the China Earthquake Administration GNSS data product service platform [52] (<http://www.cgps.ac.cn> (accessed on 15 August 2021)), and the main contents include GNSS-PWV, GNSS-ZTD, and its gradient, surface atmospheric pressure and temperature, etc. The time span was from 1 January 2017 0:00 to 31 December 2018 23:00, and the time resolution was 1 h. The accuracy of GNSS-PWV was within 1 and 3 mm. We selected 50 GNSS stations that evenly cover most of the China region, of which 38 GNSS stations were used for PWV modeling and 12 GNSS stations were used for external conformity testing. Their spatial location distributions are shown in Figure 1. The selection of 38 GNSS stations for modeling and 12 GNSS stations was for the verification according to the three-step topography of high, medium, and low altitudes and five climate zones, and they are evenly distributed in China region. At least one GNSS station was selected for modeling in each province. Their precise locations were shown in Tables 1 and 2.

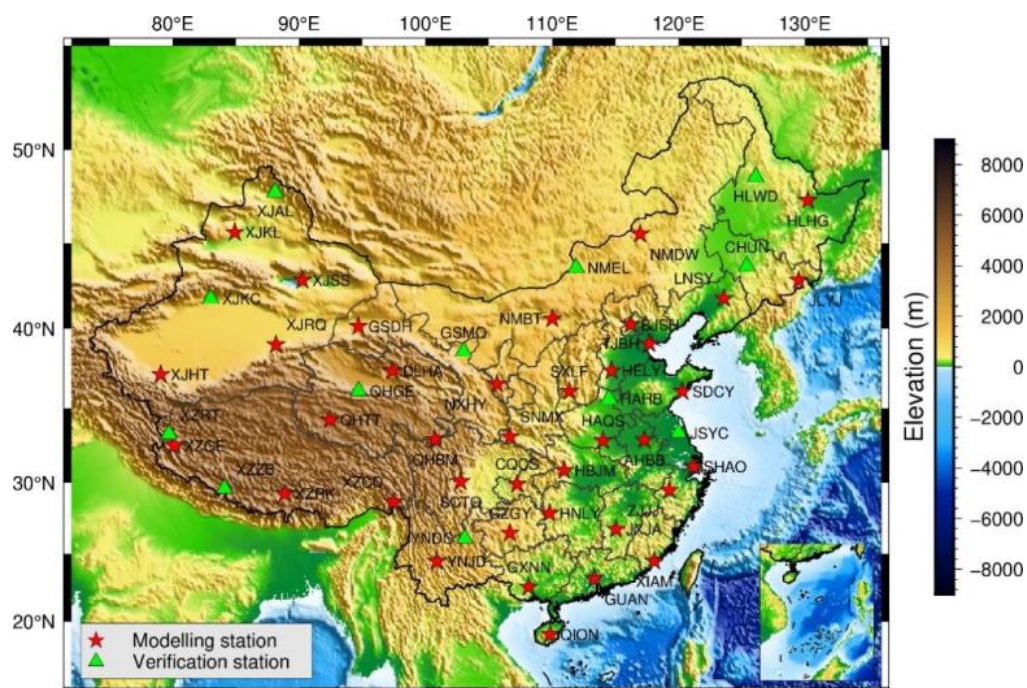


Figure 1. Spatial distribution map of the 50 selected GNSS stations in the China region.

**Table 1.** Locations of 38 GNSS stations for PWV modelling in the China region.

Station	Code	Longitude (°)	Latitude (°)	Elevation (m)	Station	Code	Longitude (°)	Latitude (°)	Elevation (m)
Tuotuohe	QHHT	92.44	34.22	4499.10	Karamay	XJKL	84.91	45.61	321.00
Gar	XZGE	80.11	32.52	4427.40	Yanji	JLYJ	129.50	42.88	284.60
Shigatse	XZRK	88.86	29.25	3854.80	Hegang	HLHG	130.24	47.35	210.70
Baima	QHBM	100.74	32.93	3486.70	Qiongzong	QION	109.84	19.03	207.60
Zayu	XZCY	97.47	28.66	3306.80	Zigui	HBZG	110.97	30.84	164.70
Delingha	DLHA	97.38	37.38	2955.80	Beijing	BJSH	116.22	40.25	155.40
Haiyuan	NXHY	105.65	36.55	1822.30	Xiamen	XIAM	118.08	24.45	106.10
Khotan	XJHT	79.05	37.16	1572.70	Nanning	GXNN	108.15	22.57	97.80
Jingdong	YNJD	100.88	24.44	1244.60	Jiande	ZJJJ	119.27	29.48	97.20
Guiyang	GZGY	106.67	26.47	1093.90	Gian	JXJA	115.06	26.75	89.50
Dunhuang	GSDH	94.68	40.14	1080.10	Mayang	HNMY	109.80	27.88	89.00
Baotou	NMBT	110.02	40.60	1053.90	Queshan	HAQS	114.03	32.85	72.10
Ujimqin	NMDW	116.96	45.51	834.20	Shenyang	LNSY	123.58	41.83	69.80
Charkhlik	XJRQ	88.17	39.02	830.70	Qingdao	SDQD	120.30	36.08	58.10
Tianquan	SCTQ	102.76	30.07	773.70	Bengbu	AHBB	117.30	32.90	54.10
Mianxian	SNMX	106.69	33.13	594.00	Guangzhou	GUAN	113.34	23.19	30.90
Linfen	SXLF	111.37	36.08	558.90	Longyao	HELY	114.71	37.40	30.30
Chongqing	CQCS	107.23	29.91	361.40	Shanghai	SHAO	121.20	31.10	22.00
Shanshan	XJSS	90.26	42.89	348.60	Binhai	TJBH	117.69	39.08	1.10

**Table 2.** Locations of 12 selected GNSS stations for verification in the China region.

Station	Code	Longitude (°)	Latitude (°)	Elevation (m)
Zhongba	XZZB	84.10	29.60	4570.05
Ritu	XZRT	79.70	33.30	4256.64
Golmud	QHGE	94.70	36.10	3090.00
Minqin	GSMQ	103.00	38.60	1320.05
Dongchuan	YNDC	103.10	26.10	1297.62
Kuche	XJKC	83.00	41.80	1028.84
Erenhot	NMEL	111.90	43.60	946.18
Altay	XJAL	88.10	47.80	874.87
Wudalianchi	HLWD	126.10	48.60	313.97
Changchun	CHUN	125.40	43.70	268.35
Hebi	HAHB	114.50	35.60	46.55
Yancheng	JSYC	120.02	33.38	12.70

The GNSS product of the China Earthquake Administration uses the Saastamoinen model to calculate the ZHD based on the observed surface meteorological elements at the GNSS stations. Its specific expression is as follows [10].

$$\begin{cases} ZHD = (2.2678 \pm 0.0024) \times \frac{P}{f(\theta, H)} \\ f(\theta, H) = 1 - 0.00266 \times \cos 2\theta + 0.00028H \end{cases} \quad (1)$$

The ZWD can be obtained by subtracting the ZHD from the ZTD.

$$ZWD = ZTD - ZHD \quad (2)$$

According to the empirical equation, PWV can be obtained by multiplying the ZWD by the conversion factor (K):

$$\begin{cases} PWV = K \times ZWD \\ K = \frac{1 \times 10^6}{\rho_w (k_3 / T_m + k_2') R_v} \\ T_m = 70.2 + 0.72T \end{cases} \quad (3)$$

In the formula,  $\rho_w$  is the density of liquid water;  $k_2'$  and  $k_3$  are the constants of atmospheric refraction, and their empirical values are  $22.13 \pm 2.20$  (K/hPa) and



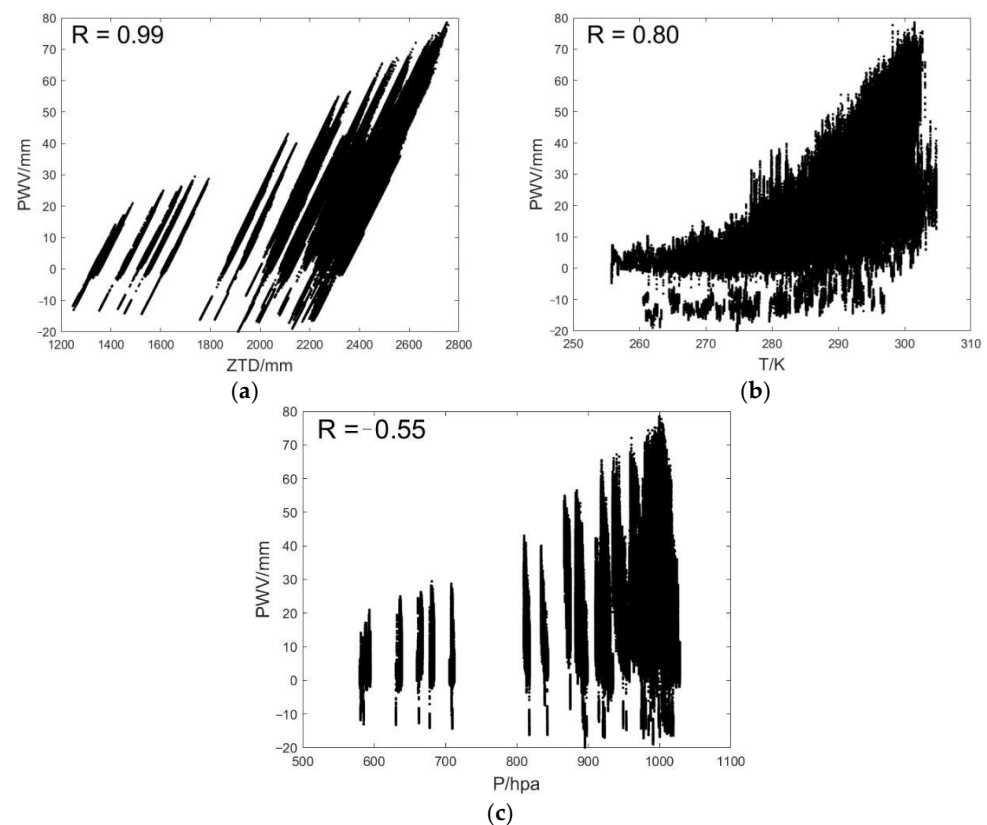
$3.739 \pm 0.012 \times 10^5$  (K/hPa);  $R_v$  is the gas constant of water vapor,  $R_v = 461.495$  ( $\text{J} \cdot \text{kg}^{-1} \cdot \text{K}^{-1}$ );  $T_m$  is the weighted mean temperature. The above GNSS-PWV calculation method is one of the most commonly used and reliable methods in GNSS meteorology [52]. However, this traditional method requires a huge amount of calculation, which may take much time. In this paper, the calculation efficiency could be improved by establishing direct PWV conversion models based on the meteorological elements and GNSS-ZTD.

## 2.2. Correlation and Collinearity Analysis

Since the ZHD accounts for about 80–90% of the ZTD, the ZWD accounts for a small proportion of the ZTD. The pressure is the main influencing factor of the ZHD. According to Formula (2), the main influencing factor of  $K$  is  $T_m$ , affected by the surface temperature. Therefore, the main influencing factors that may cause GNSS-PWV calculation errors are GNSS-ZTD, surface temperature, and pressure [53]. However, the ZWD accounts for a small proportion of the ZTD, so there may be a limited impact of temperature on the accuracy of PWV. This paper firstly analyzed the correlation level between PWV and GNSS-ZTD, temperature, and pressure, which were selected to establish the PWV conversion models according to the correlation strength.

The Pearson correlation coefficient ( $R$ ) can be used to describe the level of linear correlation between two variables. The larger the absolute value of  $R$ , the stronger the correlation level. This means an extremely strong correlation if the  $R$  is between 0.8 and 1.0. It is a strong correlation if the  $R$  is between 0.6 and 0.8. If the  $R$  is between 0.4 and 0.6, this means a moderate correlation. It is a weak correlation when  $R$  is between 0.2 and 0.4. There is no correlation when  $R$  is between 0.0 and 0.2 [54].

It can be seen from Figure 2 that the correlation coefficient between PWV and GNSS-ZTD is 0.99, which means their correlation is extremely strong, indicating that GNSS-ZTD has the greatest impact on PWV. The correlation coefficient between PWV and temperature is 0.80, showing a strong correlation. The correlation coefficient between PWV and pressure is  $-0.55$ , showing a moderate negative correlation.



**Figure 2.** Correlation analysis between PWV and GNSS-ZTD (a); temperature (b); pressure (c).

In summary, the linear correlation between PWV and GNSS-ZTD is the strongest, and a one-factor PWV conversion model based on GNSS-ZTD can be established. Temperature and pressure also have a greater impact on PWV, and they can be used to establish a three-factor PWV conversion model based on GNSS-ZTD, temperature, and pressure. Considering that pressure and temperature have different influences on PWV, two two-factor PWV conversion models based on GNSS-ZTD and pressure (or temperature) were established, respectively.

Table 3 is a statistics table of the correlations, from which we can see the correlation coefficient between independent variables. If there is a high level of collinearity between two independent variables, the linear regression model based on these variables will be unstable. It is difficult to distinguish the influence of each independent variable on the model results. Therefore, collinearity analysis is necessary for each independent variable.

**Table 3.** The correlation of dependent and independent variables and their collinearity.

Dependent Variable	Independent Variable	Correlation Coefficient (R)	Independent Variable	Independent Variable	Correlation Coefficient (R)	VIF
PWV	ZTD	0.99	ZTD	Pressure	−0.47	1.42
PWV	Pressure	−0.55	Pressure	Temperature	−0.68	1.25
PWV	Temperature	0.80	Temperature	ZTD	0.74	2.70

The variance inflation factor (VIF) was used to analyze the collinearity between independent variables in this paper, its specific expression is as follows.

$$VIF_i = 1 / (1 - R^2) \tag{4}$$

where R is the correlation coefficient between an independent variable and other variables. It is generally believed that there is no multicollinearity when  $0 < VIF < 10$ ; there is stronger multicollinearity when  $10 \leq VIF < 100$ ; there is the strongest multicollinearity when  $VIF \geq 100$ .

It can be seen in Table 3 that the square of the product of the collinearity coefficient of GNSS-ZTD and pressure is 0.30 ( $R_{ZTD-P}^2 = (0.99 \times (-0.55))^2 = 0.30$ ), so  $VIF_{ZTD-P} = 1.42$ . Similarly,  $R_{P-T}^2 = 0.20$ ,  $VIF_{P-T} = 1.25$ ;  $R_{T-ZTD}^2 = 0.63$ , and  $VIF_{T-ZTD} = 2.70$ . It is clear that all the VIF are less than 10, so there is no collinearity between any two independent variables.

### 2.3. Methods

The selected 38 GNSS stations evenly cover the China region, and their GNSS meteorological products in 2017 were used to establish several multiple linear regression models between PWV and other meteorological elements. Taking GNSS-ZTD, pressure, and temperature as the independent variables, PWV as the dependent variable for the multivariate linear model is as follows.

$$\begin{cases} y = \beta_0 + \beta_1 \times x_1 + \dots + \beta_m \times x_m + \varepsilon \\ \varepsilon \sim N(0, \sigma^2) \end{cases} \tag{5}$$

where  $y$  is the dependent variable;  $x_1, x_2, \dots, x_m$  are the independent variables;  $\beta_0$  is the constant term;  $\beta_1, \beta_2, \dots, \beta_m$  are the regression coefficients, these unknown parameters being irrelevant to the independent variables ( $x_1, x_2, \dots, x_m$ );  $\varepsilon$  is an unobservable random variable with zero mean and positive variance ( $\sigma^2 > 0$ ), called the error term. The coefficients ( $\beta_i$ ) of the independent variables can be obtained using the least-squares method.

At the same time, in order to verify the accuracy of the established PWV conversion models, the GNSS-ZTD, temperature, and pressure of each GNSS station in 2018 were substituted into the models to calculate the predicted PWV value, which can be compared with GNSS-PWV (as the true value) to verify the prediction accuracy and reliability of the established PWV conversion models.

Considering the vast territory, undulating terrain, and complex meteorological conditions in the China region, this paper selected 12 GNSS stations unused for modeling to further verify the accuracy of the external coincidence prediction accuracy and reliability of the established PWV conversion models.

### 3. Results and Discussions

#### 3.1. PWV Conversion Models

##### (1) Three-factor model

Taking GNSS-ZTD, temperature, and pressure as the independent variables and GNSS-PWV as the dependent variable, a three-factor linear regression model can be established as follows.

$$PWV = \beta_0 + \beta_1 \times ZTD + \beta_2 \times T + \beta_3 \times P \quad (6)$$

The GNSS-ZTD, temperature, pressure, and GNSS-PWV of the 38 GNSS stations in 2017 were all taken into the above formula, and the model coefficients can be estimated by the least-squares method. Finally, the three-factor PWV conversion model was obtained as follows.

$$PWV = 0.1631 \times ZTD - 0.3710 \times T + 0.0159 \times P - 5.3494 \quad (7)$$

##### (2) Two-factor model

In the same way, the GNSS-PWV, GNSS-ZTD, and temperature of the 38 GNSS stations in 2017 were all put into Formula (5), and the two-factor PWV conversion model based on GNSS-ZTD and temperature can be obtained as follows.

$$PWV = 0.015 \times ZTD + 1.049 \times T - 313.0672 \quad (8)$$

If the GNSS-PWV, GNSS-ZTD, and pressure of the 38 GNSS stations in 2017 are all put into Formula (5), the two-factor PWV conversion model based on GNSS-ZTD and pressure can be obtained as follows.

$$PWV = 0.1641 \times ZTD - 0.3731 \times P - 1.1352 \quad (9)$$

##### (3) One-factor model

In the same way, the GNSS-PWV and GNSS-ZTD of the 38 GNSS stations in 2017 were all taken into Formula (5), and the one-factor PWV conversion model based on GNSS-ZTD can be obtained as follows.

$$PWV = 0.0341 \times ZTD - 54.3775 \quad (10)$$

#### 3.2. Internal Coincidence Accuracy

Due to space limitations, Figure 3a lists the time series of the predicted PWV of some GNSS stations during 2017–2018, in which GNSS-PWV can be used as the true value to compare with the PWV predicted by different PWV conversion models. It can be seen from Figure 3 that the one-factor PWV model based on the ZTD showed a small change, and its deviations from the GNSS-PWV series were the largest. The change trends of other PWV sequences were basically the same. Among them, the two-factor PWV based on the ZTD and pressure and the three-factor PWV based on the ZTD, pressure, and temperature were the closest to GNSS-PWV, showing obvious rising and falling trends and seasonal changes in a year. They are in line with the climatic characteristics of a hot and humid summer and a dry winter in China.

Figure 3b describes the deviations of each PWV conversion model from GNSS-PWV during 2017–2018. It can be seen from the figure that the deviations of the one-factor predicted PWV based on the ZTD were basically within 40 mm; the deviations of the two-factor predicted PWV based on the ZTD and temperature were mostly within 30 mm; the deviations of the two-factor predicted PWV based on the ZTD and pressure were basically

within 1.0 mm. The deviations of the three-factor predicted PWV based on the ZTD, pressure, and temperature were within 1.0 mm as well. However, the three-factor PWV conversion model showed the highest accuracy among them. Moreover, the deviations of the two-factor and three-factor predicted PWV during 2018 were basically the same as those during 2017.

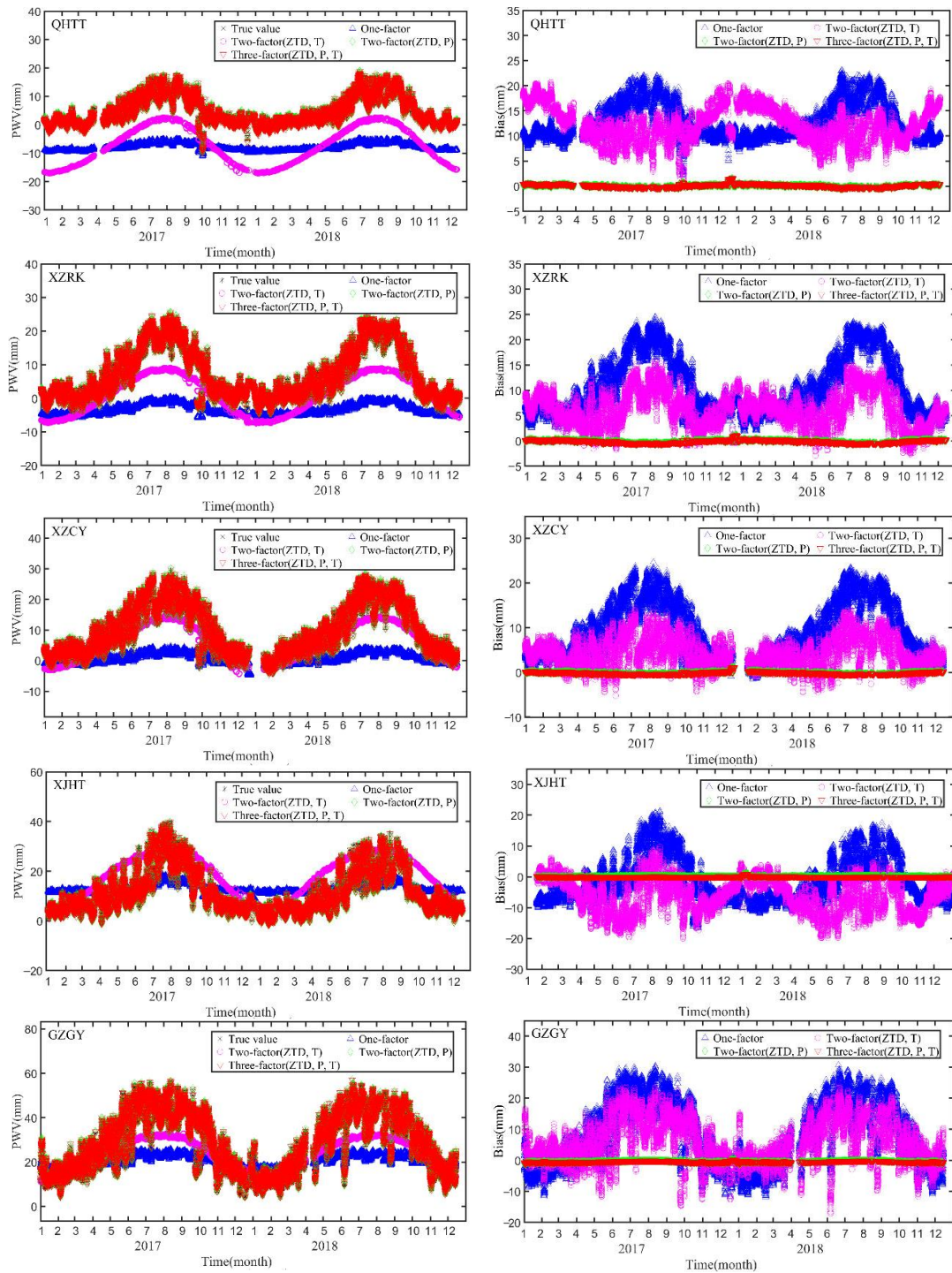


Figure 3. Cont.



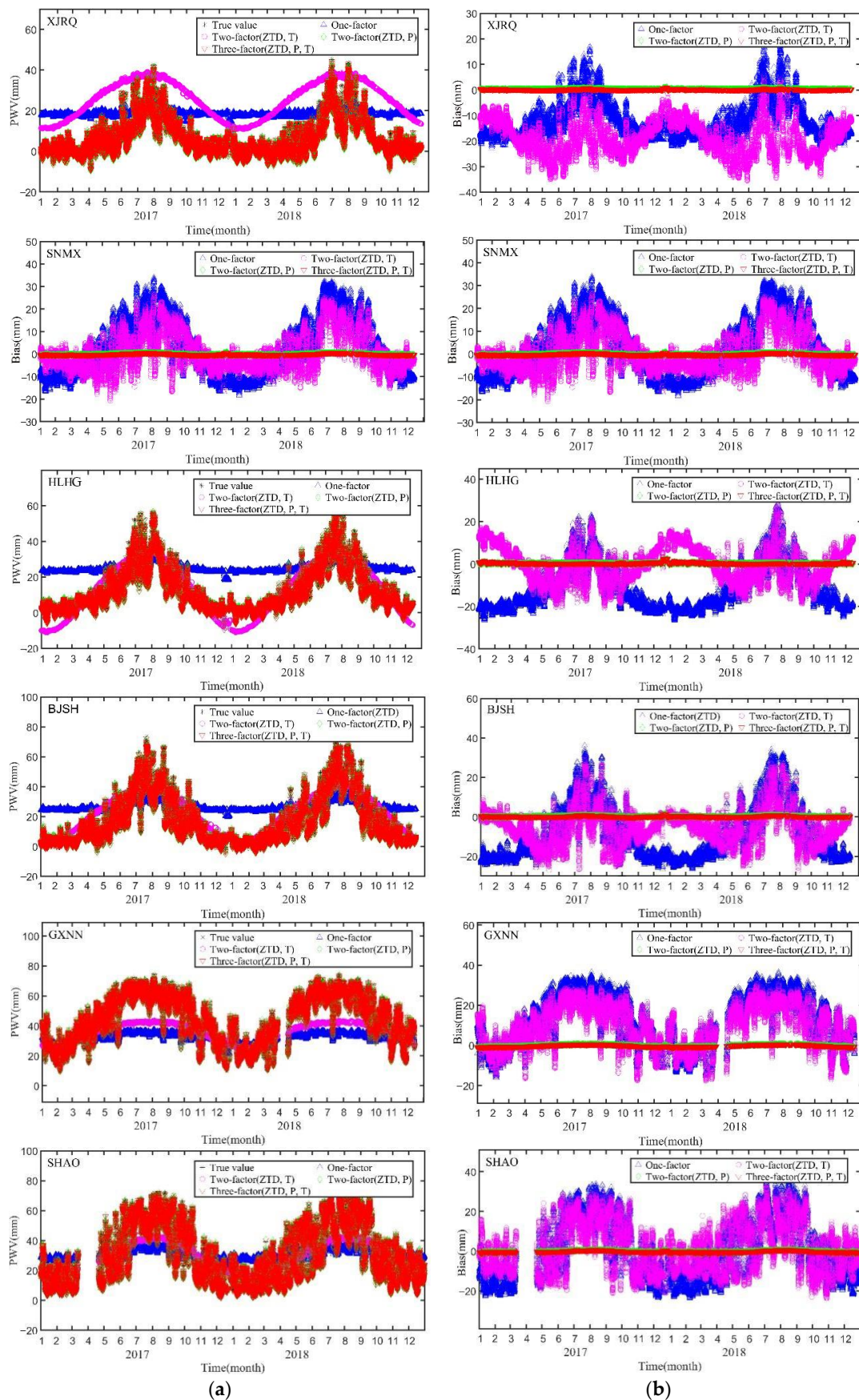


Figure 3. Variation trends (a) and their deviations (b) of the predicted PWV during 2017–2018.

For some high-altitude (>3000 m) GNSS stations, the one-factor predicted PWV based on the ZTD was negative, which is obviously inconsistent with common sense (PWV should always be positive). Therefore, the one-factor PWV model cannot be used in a high-altitude region. The two-factor predicted PWV based on the ZTD and temperature also had a large deviation at high-altitude stations, the maximum PWV being close to 25 mm, and the predicted PWV in some periods was also negative, indicating the weak correlation between the PWV and temperature in high-altitude areas. It is clear that the one-factor and two-factor PWV models based on the ZTD and temperature are not suitable for high altitudes (>3000 m).

Table 4 summarizes the mean deviations and RMS of the predicted PWV of the four conversion models for the 38 GNSS stations during 2017–2018. It can be seen from the table that the RMS of the one-factor PWV conversion model based on the ZTD was 12.16 mm and 14.30 mm. After adding temperature as a new independent variable, the mean deviation of the two-factor PWV conversion model reduced to 9.07 mm, its RMS reduced to 11.15 mm, and the accuracy slightly improved. While adding pressure as a new independent variable, the mean deviation of the two-factor PWV conversion model based on GNSS-ZTD and pressure was 0.31 mm, and its RMS was 0.39 mm. While adding pressure and temperature as two independent variables, the mean deviation of the three-factor PWV conversion model was 0.33 mm, and its RMS was 0.38 mm.

**Table 4.** Precision statistics of the one-, two-, and three-factor PWV conversion models (mm).

Models	RMS			Bias		
	2017	2018	Mean	2017	2018	Mean
One-factor (ZTD)	14.39	14.21	14.30	12.19	12.13	12.16
Two-factor (ZTD, T)	11.30	10.99	11.15	9.17	8.97	9.07
Two-factor (ZTD, P)	0.40	0.38	0.39	0.32	0.31	0.31
Three-factor (ZTD, P, T)	0.39	0.37	0.38	0.31	0.30	0.33

From Formulas (1–3) in Section 2.1, it can be seen that the ZHD accounted for about 80–90% of the ZTD, mainly calculated by the pressure; adding pressure into the two-factor PWV model can improve its accuracy. The conversion factor (K) is mainly calculated by the surface temperature and  $T_m$ , where  $T_m$  is also mainly calculated from the air temperature. The ZWD accounts for a small proportion of the ZTD, so the accuracy improvement by adding the temperature is limited. Therefore, the accuracy of two-factor PWV model based on the ZTD and pressure was significantly improved compared to that of the two-factor PWV model with temperature added.

It can be seen that atmospheric pressure is a key meteorological element that greatly improved the accuracy of the PWV conversion models. The RMS of the two-factor and three-factor PWV conversion models by adding pressure were lower than 0.40 mm, and their accuracies were sufficient to meet most atmospheric requirements.

### 3.3. External Coincidence Accuracy

It is known from Section 3.2 that the accuracies of the two-factor and the three-factor PWV conversion model by adding pressure were relatively high. Therefore, 12 stations that did not participate in the modeling and that are distributed at different altitudes were selected to verify the accuracy of the above two PWV conversion models in this section.

Figure 4a–l lists the deviations of the predicted PWV for the 12 GNSS stations during 2017–2018. Overall, the predicted PWV deviations of the two models were larger in summer and smaller in winter. Most of the predicted PWV deviations were between −0.5 and 1.0 mm.

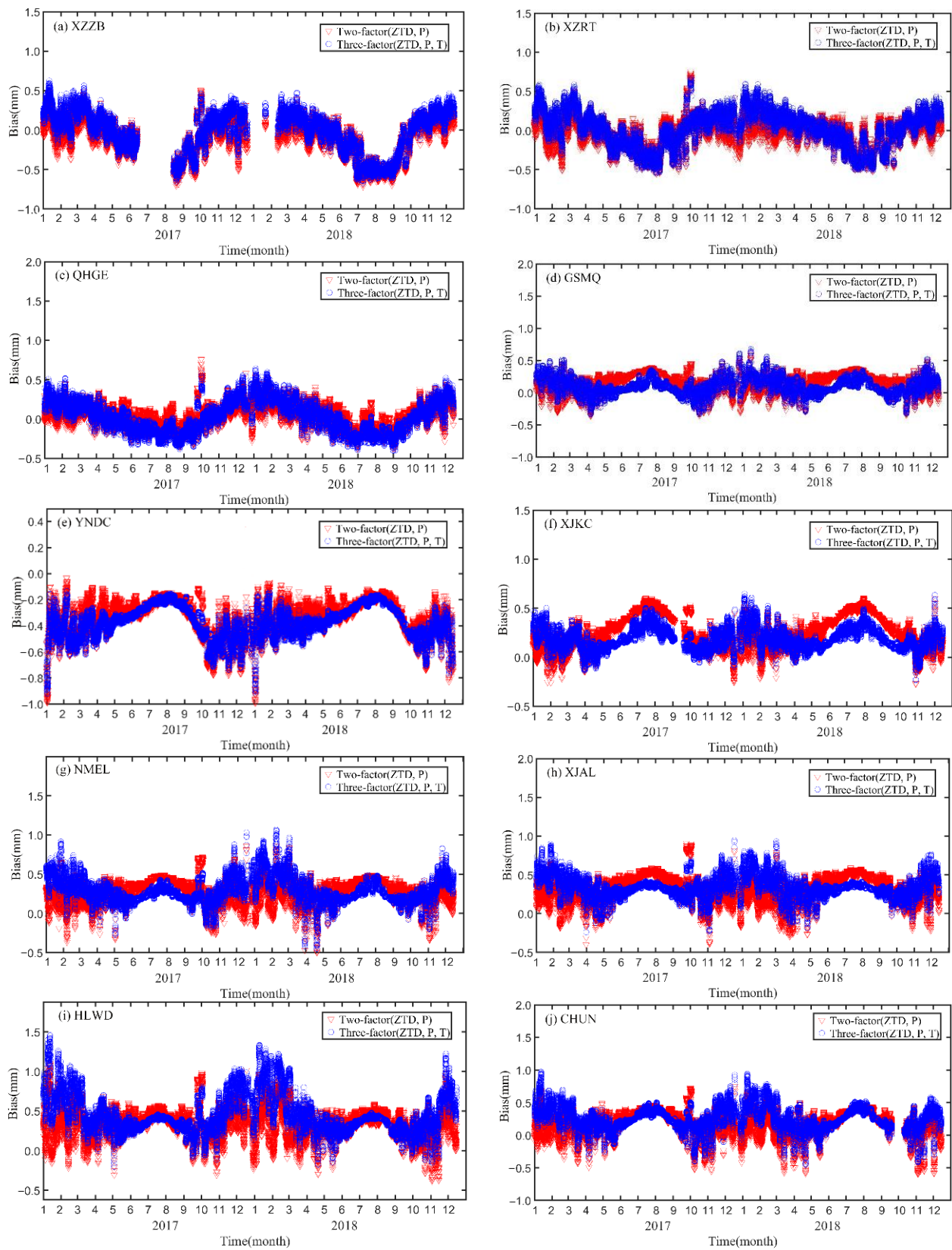
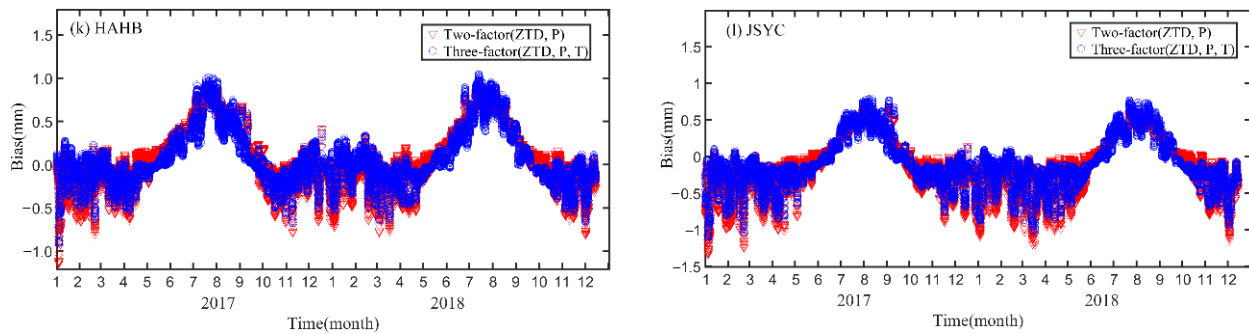


Figure 4. Cont.





**Figure 4.** The deviations of the predicted PWV of 12 GNSS verification stations (a–l) during 2017–2018.

It can be seen from Table 5 that the mean RMS of the two-factor PWV of the 12 GNSS stations during 2017–2018 was 0.31 mm, and the mean deviation was 0.16 mm. The mean RMS of the three-factor PWV was 0.33 mm, and the mean deviation was 0.16 mm. Therefore, the key meteorological elements affecting PWV were the ZTD and pressure. The two-factor and three-factor PWV conversion models based on GNSS-ZTD and pressure can obtain the predicted PWV with an accuracy better than 0.5 mm in this paper. However, the three-factor model will need one more meteorological parameter, which increases the difficulty of obtaining the temperature. In this case, the two-factor model is generally better and more practical than the three-factor PWV model.

**Table 5.** The external precision of predicted PWV of verification stations during 2017–2018 (mm).

Stations	Elevation (m)	Two-Factor (ZTD, P)		Three-Factor (ZTD, P, T)	
		RMS	Bias	RMS	Bias
XZZB	4570.05	0.26	0.19	0.28	0.22
XZRT	4256.64	0.20	0.15	0.24	0.18
QHGE	3090.00	0.19	0.13	0.23	0.18
GSMQ	1320.05	0.23	0.12	0.19	0.11
YNDC	1297.62	0.36	0.11	0.39	0.10
XJKC	1028.84	0.31	0.14	0.24	0.10
NMEL	946.18	0.35	0.14	0.39	0.15
XJAL	874.87	0.39	0.14	0.41	0.12
HLWD	313.97	0.44	0.16	0.56	0.21
CHUN	268.35	0.29	0.16	0.36	0.16
HAHB	46.55	0.36	0.28	0.33	0.25
JSYC	12.70	0.38	0.11	0.35	0.09
Mean		0.31	0.15	0.33	0.15

#### 4. Conclusions

Based on the data of 38 GNSS stations in China from 2017 to 2018, this paper used multiple linear regression fitting and established one-factor, two-factor, and three-factor PWV conversion models suitable for the China region based on GNSS-ZTD, temperature, and pressure. Compared with the conventional GNSS-PWV acquisition method, the PWV conversion models not only improved the computing efficiency, but also reduced the error accumulation. The main research conclusions are as follows:

- (1) There are extremely strong and moderate linear correlations between GNSS-PWV and GNSS-ZTD, temperature, and pressure. The correlation coefficient between PWV and GNSS-ZTD is 0.99; the correlation coefficient between PWV and temperature is 0.80; the correlation coefficient between PWV and pressure is  $-0.55$ . There is no collinearity between any two independent variables.
- (2) The mean deviation of the one-factor predicted PWV based on GNSS-ZTD is 12.16 mm, and its RMS is 14.30 mm. The mean deviation of the two-factor predicted PWV after



adding temperature reduced to 9.07 mm, and its RMS reduced to 11.15 mm. The mean deviation of the two-factor predicted PWV based on ZTD and pressure is 0.31 mm, and its RMS is 0.39 mm. The mean deviation of the three-factor predicted PWV based on GNSS-ZTD, pressure, and temperature is 0.33 mm, and its RMS is 0.38 mm.

- (3) In terms of external coincidence accuracy, the RMS of the two-factor and three-factor predicted PWV based on the ZTD and pressure is better than 0.33 mm, and the mean deviation is better than 0.16 mm. Obviously, these two new PWV conversion models are good enough to be widely used in the China region.

Moreover, the latitude and elevation both affect the accuracy of the ZHD and ZWD. Due to the smaller number of stations at high latitudes and elevations, these two factors were not considered in this paper. The latitude and elevation may improve the fitting effect and accuracy if they are added into the PWV conversion model in high-altitude areas.

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