

Review

Radar Technology for River Flow Monitoring: Assessment of the Current Status and Future Challenges

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Abstract: As an emerging non-contact method of flow monitoring, radar technology compensates for the shortcomings of traditional methods in terms of the efficiency, timeliness, and difficulty in monitoring high floods, and can provide accurate measurement results, making it one of the most promising flow monitoring methods in the future. This paper describes in detail the workflow from radar data acquisition to flow calculation; compares and analyzes the current state-of-the-art signal sampling and its limitations, Doppler spectrum estimation, signal processing and flow inversion; points out the challenges that these technologies may face in the future; and provides corresponding solutions in order to improve the real-time and accuracy of hydrometric as well as promote the development of non-contact flow monitoring technology.

Keywords: hydrometric; flow monitoring; non-contact; radar technology

1. Introduction

1.1. Motivation

As the most fundamental hydrological feature of rivers, flow is essential information for the management of water resources, the research of hydrology, as well as the construction of water conservancy projects [1–3]. However, in recent years, the frequent changes in the relation between rain fall and run off along with climatic and environmental parameters have made floods seem to be more abundant and destructive in many regions of the globe [4–6]. As a result, improving the monitoring of river flow in real time and considering the accuracy is not only a key issue concerning various countries in the world, but is also an effective way to prevent the occurrence of floods, thereby reducing the casualties and property losses [7–9].

At present, flow monitoring methods can be roughly divided into two categories: the contact method and the non-contact method. The contact methods include current meters, floats, and Acoustic Doppler Current Profilers (ADCPs), etc. Current meters and floats have emerged as the most used flow velocity measurement methods due to their high applicability. However, they require labor participation, which not only presents safety risks but also poses issues with laborious, low efficiency and measurement difficulties during high floods [10–12]. Compared with the first two methods, although the automation and measurement accuracy of ADCPs have been improved remarkably, they are still expensive and cannot be used in real time monitoring or under the conditions of high turbulence, aviation, and bed movements [13–15]. In addition, the contact methods are particularly susceptible to being damaged by the sand content, aquatic species, and floating objects, which may result in significant measurement errors and high maintenance costs [16–18]. Consequently, it is necessary for us to explore and develop a more economical, safer, and highly efficient non-contact method.

In recent years, the non-contact flow monitoring methods, which mainly include remote sensing, radar, and vision-based methods, have received sufficient attention from



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researchers and made great progress. Remote sensing methods focus on satellite-based platforms to calculate the reach-based river flow rate, which is of great significance in macroscopic water monitoring [19–22]. However, its spatial and temporal resolution make it difficult to satisfy the real-time and continuous requirements for monitoring the velocity and flow rate. As for the vision-based method, it has certain advantages in terms of real-time and continuous measurement. However, its calculation performance of flow velocity is directly determined by the image quality, which is easily influenced and deteriorated by the change of light and meteorological conditions, such as rain, fog, shadows, and nighttime [23–25]. The radar-based measurement method, on the contrary, can detect targets in both day and night, and is not blocked by meteorological conditions such as fog, clouds, and rain, which embodies all-weather and all-day monitoring features [26,27]. Chen et al. [28] and the United States Geological Survey (USGS) [29] compared the applicability of the radar current meter, ADCPs, and rotor current meter for measuring river flow. They all concluded that radar technology was the most appropriate flow measurement method in recent years, which could significantly reduce the measurement time while maintaining high accuracy.

So far, the radar current meter can be divided into two types: the fixed-point radar and the side-scan radar. The fixed-point radar is usually fixed at a certain position of the measured section and can only obtain the flow velocity of a single point or a small area on the river surface, which is widely used in hydrometric and emergency rescue monitoring of small and medium-sized rivers [30–32]. Compared with the fixed-point radar, the side-scan radar is typically set up on the bank, which has a wider monitoring distance, and can monitor the average flow velocity within a segmented range and identify the direction of the signal in space. However, the side-scan radar is still in the research and verification stage, and few applications are promoted [33–35]. The early studies of radar flow monitoring were mostly focused on experiments [36–38]; for example, Teague et al. have successfully verified the possibility of using a radar current meter instead of traditional methods for surface velocity monitoring and flow calculation [39]. Under the urgent requirements of intelligent and automated flow measurement as well as timely and reliable hydrological information, extensive research has been conducted on radar system design [40–44], signal processing [45–49], and flow inversion algorithms [50–55]. However, there are still issues with the existing radar flow measurement technology in some aspects, which limits its future advancement. Therefore, the purpose of this paper is to summarize the current technology of radar flow monitoring, identify its main limitations, describe the challenges that the technology may face in the future, and propose corresponding solutions in order to promote the progress of radar technology in flow monitoring, advance the development of efficient, accurate, and real-time non-contact flow measuring technology, and improve the ability to predict and provide early warnings of flood disasters under extreme conditions.

1.2. Principle of Velocity Estimation

Christian Andreas Doppler, an Austrian scientist, observed in 1842 that the frequency of the echo signal was different from the signal initially released by the source when relative motion occurred between the target and the observer. When the target is close to the source, the wave is compressed, the frequency becomes higher, and the wavelength gets shorter. On the other hand, when the target moves away from the source, the frequency becomes lower, and the wavelength gets longer. The value of the increase or decrease in frequency was called the Doppler frequency shift [56].

Basically, the river surface is illuminated by a radar, and the Doppler frequency shift is determined by receiving and processing the electromagnetic waves backscattered by the rough water surface, as shown in Figure 1. The phenomenon of Bragg scattering, discovered by Crombie in 1955, was frequently cited as the cause of the reflection of electromagnetic waves from river waves, which stated that river waves traveling radially toward or away from the radar would result in the strongest backscatter when their wavelength was exactly half that of the radar, and this resonance was unaffected by wind

speed or water surface conditions [57,58]. However, this theory works only under the specific condition that there must be a highly precise situation-dependent relationship between the electromagnetic wave and a periodic surface structure. After further research, scholars have found that backscattering is a superposition of Bragg scattering and other phenomena, rather than being solely Bragg scattering [59]. Fresnel reflections, multipath, and multibounce scattering were all used to explain non-Bragg backscattering [60,61].

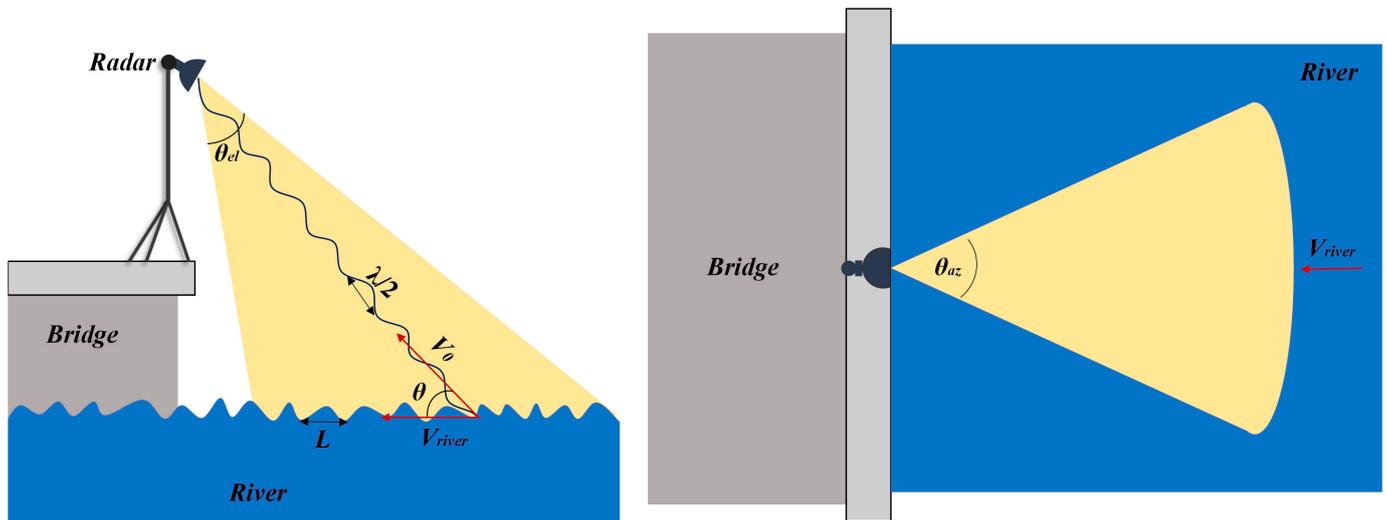


Figure 1. Principle sketch of the measurement setup from side (left) and top view (right), the observation area (marked in yellow) depends on the height of radar and the beam width in elevation θ_{el} and azimuth θ_{az} .

When the radar transmits signals and then successfully receives the targets' echoes from the river surface, the calculation for the surface velocity is as follows: Electromagnetic waves from the source are emitted at a frequency of f_0 , with a speed of u . When the target moving with a velocity of v_0 ($+v_0$ means that target moves away from the source, $-v_0$ is the opposite), the frequency of the electromagnetic wave that it received is f_1 :

$$f_1 = \frac{u \mp v_0}{v_0} f_0 \tag{1}$$

Then, when the electromagnetic wave returns from the target, the frequency f' received by the source is:

$$f' = \frac{v_0}{u \pm v_0} f_1 = \frac{u \mp v_0}{u \pm v_0} f_0 \tag{2}$$

The Doppler frequency f_d is the frequency difference between the transmitted signal and the echo signal, which can be written as:

$$f_d = f_0 - f' \approx \frac{2v_0}{u} f_0 \tag{3}$$

when the angle between the radar and the water surface is θ , the flow velocity of the river is

$$V_{river} = \frac{v_0}{\cos \theta} = \frac{u}{2f_0 \cos \theta} f_d \tag{4}$$

1.3. Outline

This paper describes the method for estimating river flow by using radar technology, outlines the current achievements, and critically assesses the limitations and future challenges.

The principle of radar technology for river flow monitoring is briefly explained, and a short retrospective of the developments of radar applications in hydrometric is reviewed in Section 1. The typical processing steps required from raw radar data acquisition to river flow derivation are described, and their respective challenges are elaborated in Section 2. The state-of-the-art from signal sampling to flow calculation are summarized, and their key limitations are identified in Section 3. In the discussion section, views on the future challenges of radar flow monitoring technology are presented and potential solutions to address these challenges are suggested.

2. The Challenges of Processing River Flow from Raw Radar Data

The overview of the workflow is shown in Figure 2, starting with raw signal data and ending with river flow. The first step is signal sampling, with the aim of converting the beat frequency signal into a processable digital signal, and filtering it to ensure accuracy. The second step is to perform a Doppler spectral analysis of the signal. Different spectrum estimation methods apply differently and may also result in different calculations, so it is particularly important to choose an appropriate method. The third step is signal processing. Usually, the echo signal may contain a variety of noise and clutter, and it is crucial to identify and calculate the flow velocity effectively. The final step is the flow calculation; as the radar obtains the surface velocity of the river, the key to this step is how to calculate the flow rate based on the surface velocity. This section outlines each stage while highlighting the overall difficulties present. The state-of-the-art signal sampling will be followed by more information on the solutions that can be used to address these problems.

2.1. Signal Sampling

Data acquisition starts with digital sampling, which is responsible for providing high-precision data for signal processing and flow calculations. The purpose of digital sampling is to perform digital down conversion and convert the received intermediate-frequency (IF) signal into a digital signal [62]. Usually, the original signal is mixed with various kinds of clutter, so that sampling the signal directly may cause aliasing phenomenon [63]. Therefore, signal sampling is necessary to preserve the quality and integrity of the raw data received.

2.2. Doppler Spectrum Estimation

As shown in Equation (4), the river velocity needs to be calculated using Doppler frequency shift. Frequency estimation techniques, which can be loosely categorized into three categories, are mostly utilized for the frequency extraction of Doppler signals [64,65]. The zero-crossings and the period counting methods fall under the first category, which are usually used for measuring the frequency or the period of a periodic signal. The zero-crossings calculate the frequency of a signal by counting the number of times the signal passes through the zero axis, while the period counting methods directly measure the number of periods of the signal. Both the zero-crossings and the period counting methods belong to the time domain analysis methods, which can intuitively reflect the relationship between wavelength and Doppler effect, because these methods regard the wave length of the echo signal as a stochastic variable with mean, standard deviation, etc. [66,67]. The second category is special analysis methods, which generally comprise wavelet transforms and other analysis methods [68,69]. The third category is the frequency domain analysis methods [70,71], which use spectrum estimation methods to estimate the power spectrum of the signal, including the classical spectrum estimation and the modern spectrum estimation. However, not all of the aforementioned methods are appropriate for calculating river flow velocities. For instance, the zero-crossings and period counting methods have the drawback of being sensitive to noise and signal voltage, which would result in insufficient accuracy and are rarely used in the field of radar flow monitoring [72]. The special analysis methods require a large quantity of data to be processed and take a long time to calculate, which makes them unsuitable for real-time measurement of flow

velocities [73]. The spectrum estimation methods may have problems such as spectrum leakage in some cases [74].

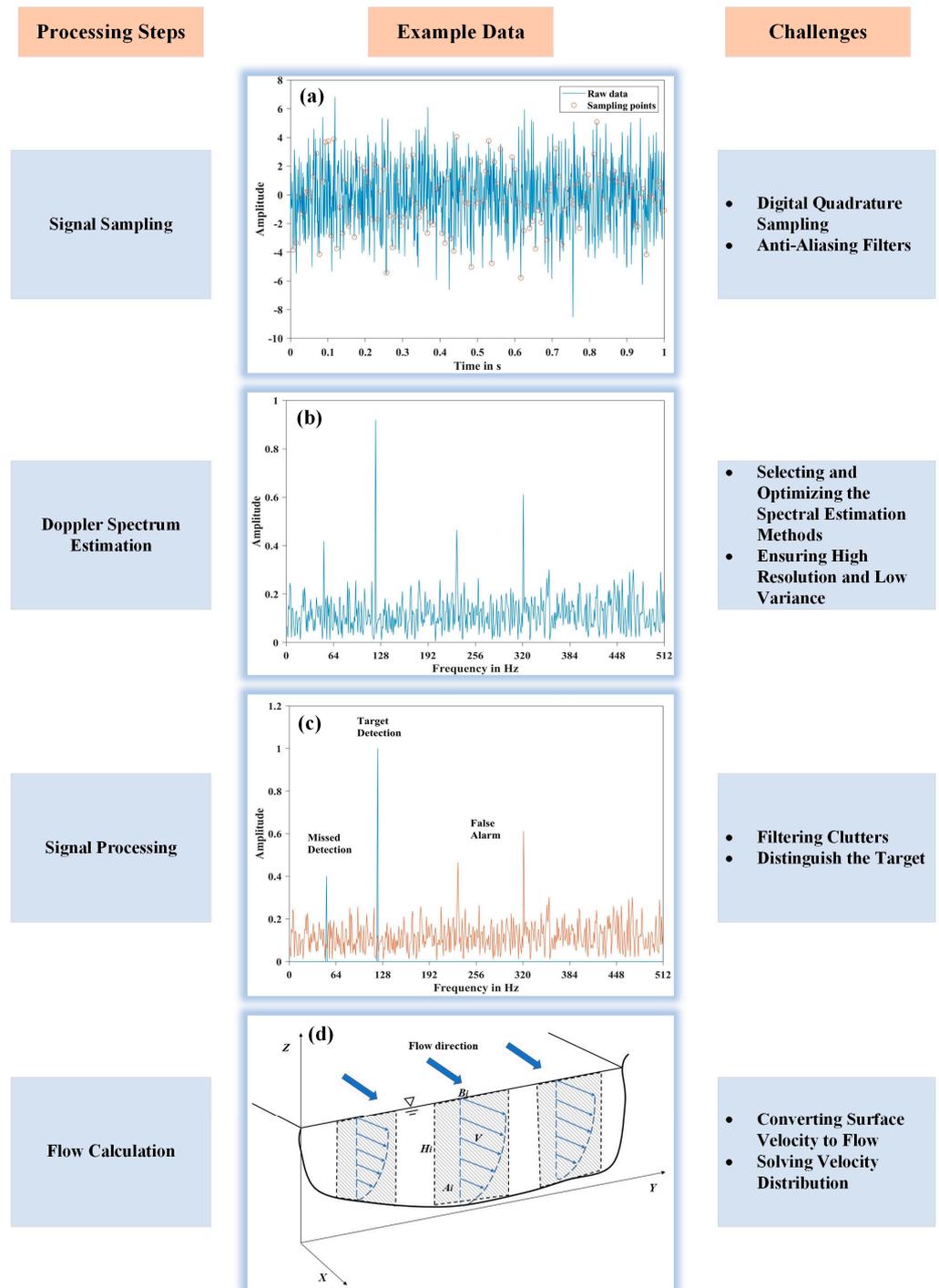


Figure 2. Illustration of a typical workflow, starting from sampling raw signal data to having the river flow. (a) Raw data obtained from radar equipment. (b) Doppler estimation using spectrum methods. (c) Signal processing, including clutter removal and target identification. (d) Converting surface velocity to flow.

2.3. Signal Processing

As seen in Figure 2c, the echo signal received by radar was frequently mixed up with various background clutter within the irradiation range of the antenna beam (such as ground, rain, fog, waves, etc.). False detection and missed detection might occur when

the target signals and clutters were simultaneously received but improperly handled, which would have a significant impact on the accuracy of the results. Therefore, the key challenge lies in identifying the target from the complex clutter background in real time and automatically. Ideally, a fixed threshold (refers to a power threshold above which any return can be considered to probably originate from a target as opposed to one of the spurious sources.) needs to be set if the interference has a constant value. In practice, however, the threshold value must be continuously updated according to the changes in the interference to ensure a constant false alarm probability, which is known as the constant false alarm rate (CFAR) [75,76].

2.4. Flow Calculation

The estimation of river flow is the last step after obtaining the river surface velocity from the signal spectrum. Traditional flow calculation methods usually involve obtaining the depth-averaged velocity or the cross-section average velocity and calculating the flow rate based on the velocity-area method [77]. However, since radar can only measure the flow velocity at a specific place or a small area on the river surface, it is necessary to solve the problem of how to accurately calculate the cross-section flow from the surface velocity [78].

3. State-of-the-Art

3.1. Sampling Methods

Digital sampling is indeed a requirement to ensure data accuracy in radar signal processing. In order to maintain all of the signal's information, especially the amplitude and the phase, the raw data must undergo digital quadrature sampling and quadrature coherent detection after receiving [79]. To achieve the above process, a certain sampling theorem must be followed.

Figure 3 illustrates the streamlined signal sampling procedure in the time domain and in the frequency domain. The continuous signal $x_n(t)$ is multiplied with the impulse function $p(t)$ to obtain the discrete signal $x(nT_s)$, which realizes the conversion from analog to digital. The period of the impulse function in the time domain is T_s , while its period in the frequency domain is f_s . The frequency spectrum of $x(nT_s)$ will likewise exhibit periodicity after being sampled. If f_s is less than twice the maximum frequency f_{\max} of the discrete signal spectrum, then the sampled spectrum appears to exhibit an aliasing phenomenon. The Nyquist theorem states that in order to recover the continuous signal $x_n(t)$ from the discrete signal without distortion, the sampling frequency f_s must be at least twice the maximum frequency f_{\max} of the discrete signal spectrum, $f_s \geq 2f_{\max}$ [80,81].

So far, there are many quadrature coherent detection methods, such as digital product detection [82], Bessel interpolation [83], Hilbert transform [84], and low-pass filtering [85]. The above methods can be broadly classified into two categories: time domain interpolation and frequency domain filtering. Time domain interpolation methods are simple, fast and require low interpolation order, but are difficult to acquire considering the existence of amplitude and phase error between quadrature channels. Frequency domain analysis methods are time consuming and complex to design, but are more resistant to interference and more effective [86]. Considering that the results obtained using the above methods are relatively similar, the more robust low-pass filter is typically employed as the original signal's anti-aliasing filter. For instance, the target signals, as depicted in Figure 2c, are roughly located between 50 and 120 Hz, while false alarms start to arise between 200 and 300 Hz. If the prior knowledge of the target or background clutter is predictable, a 120 Hz low-pass filter could be used simply, as depicted in Figure 4, to efficiently filter out high-frequency congestion.

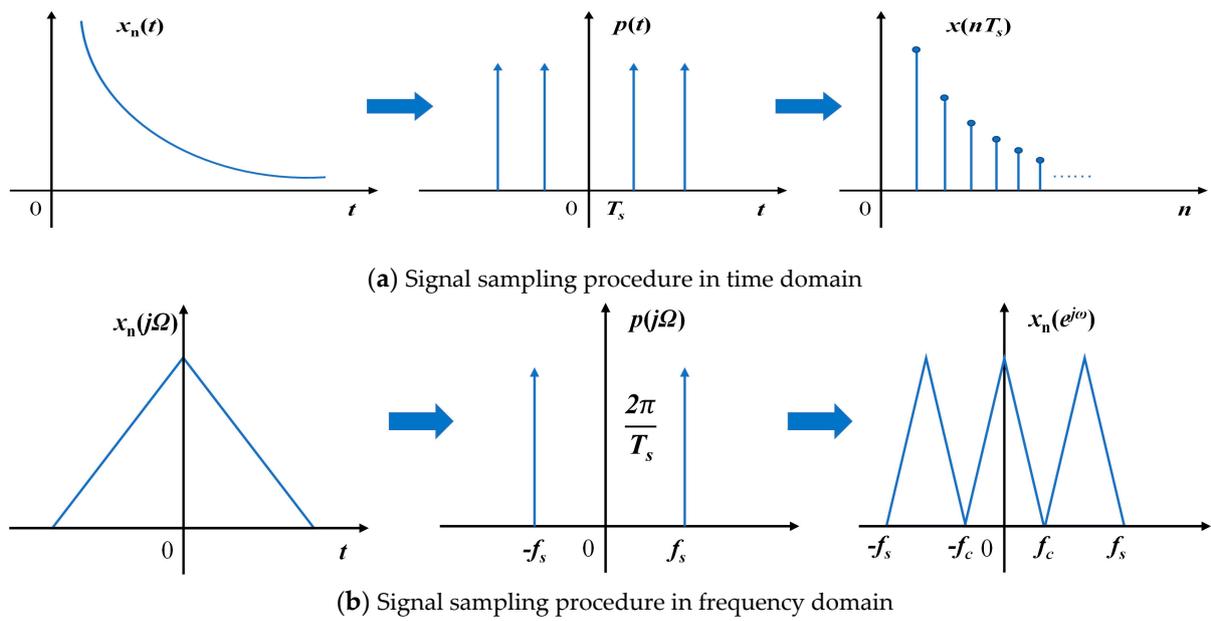


Figure 3. A streamlined signal sampling procedure in the time domain (a) and in the frequency domain (b).

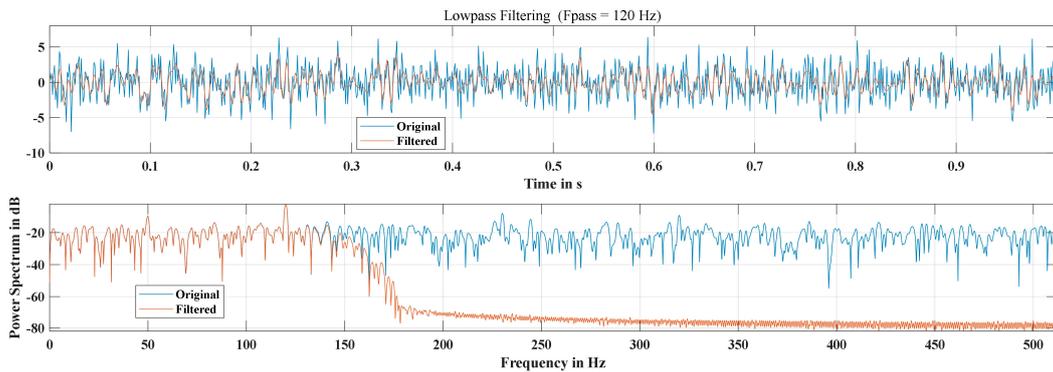


Figure 4. Low-pass filter-based quadrature coherent detection method.

3.2. Spectrum Estimation Methods

Frequency domain analysis, which encompasses both the classical and the modern spectrum estimation, is currently the most common technique for estimating the Doppler spectrum.

3.2.1. Classical Spectrum Estimation

The Fourier transform-based analytical technique known as “the classical spectrum estimation” is frequently used in the design of radar current meters and the signal processing of flow measurement, which includes the periodogram and the correlation function [87,88].

The process of the periodogram is to take N discrete points of the random signal $x(n)$ as a sequence $x_N(n)$, and then perform the Fourier transform on it to obtain $x_N(e^{j\omega})$, after which the square of the amplitude is taken and divided by N to obtain the power spectrum $P(e^{j\omega})$, and the discrete power spectrum $\hat{P}_{PER}(k)$ is obtained by taking ω equally spaced on the unit circle:

$$\hat{P}_{PER}(k) = \frac{1}{N} \left| \sum_{n=0}^{N-1} x(n) e^{-j\frac{2\pi}{N}nk} \right|^2 \tag{5}$$

As can be seen from the equation above, the discrete power spectrum needs to be calculated by n^2 -th multiplication and addition, which is a complex and computationally

intensive process. Considering the portability and cost of a fixed-point radar, the Fast Fourier transform (FFT) is mostly used. Alimenti et al. designed a low-cost radar based on the FFT algorithm, and the results showed that the accuracy of this radar was comparable to that of a high-precision commercial radar flowmeter [89]. The FFT algorithm’s basic idea is to continually split the discrete signal $x_N(n)$ by using the symmetry and periodicity of $e^{-j\frac{2\pi}{N}nk}$. This reduces the computational steps to $(n/2)\log_2 n$ times multiplication and $n\log_2 n$ times addition while maintaining the precision of the results.

The correlation function is to calculate the autocorrelation function $\hat{r}(m)$ of the signal $x(n)$ first, after which the Fourier transform of the autocorrelation function is performed and the power spectrum can be estimated using $\hat{P}_{BT}(\omega)$:

$$\hat{r}(m) = \frac{1}{N} \sum_{n=0}^{N-1} x(n+k)x^*(n), k = 0, 1, 2, 3, \dots, M \tag{6}$$

$$\hat{P}_{BT}(\omega) = \sum_{m=-M}^M \hat{r}(m)e^{-j\omega m}, |M| \leq N - 1 \tag{7}$$

Notably, the periodogram is a specific instance of the correlation function where $M = N - 1$.

3.2.2. Modern Spectrum Estimation

Different from classical spectrum estimation, modern spectrum estimation is model-based, which uses sampled data to build a model that extrapolates the data and thus improves the resolution of the spectral estimate. The modern spectrum estimation mainly includes the parametric model and the non-parametric model. Parametric model methods include the AR (Autoregressive) model, the MA (Moving average) model, and the ARMA (Autoregressive moving average) model [90]. Nonparametric model methods include the minimum variance method [91] and the MUSIC (Multiple Signal Classification) method [92].

The idea of the parametric model is to assume that the signal $x(n)$ is the output of a causal Linear Shift Invariant (LSI) filter with the rational system function defined by $H(z)$. The discrete time series $u(n)$ are the result of applying a linear filtering operation to some unknown time series $x(n)$. Generally, $u(n)$ is assumed to be a white noise sequence with zero mean and variance σ^2 ; the relationship between $x(n)$ and $u(n)$ can be expressed as:

$$x(n) = -\sum_{k=1}^p a_k x(n-k) + \sum_{k=0}^q b_k u(n-k) \tag{8}$$

The $H(z)$ can be represented as:

$$H(z) = \frac{B(z)}{A(z)} = \frac{\sum_{k=0}^q b_k z^{-k}}{\sum_{k=0}^p a_k z^{-k}} \tag{9}$$

The power spectrum of $x(n)$ is as follows:

$$P_x(e^{j\omega}) = \frac{\sigma^2 B(e^{j\omega})B^*(e^{j\omega})}{A(e^{j\omega})A^*(e^{j\omega})} = \sigma^2 \left| \frac{B(e^{j\omega})}{A(e^{j\omega})} \right|^2 \tag{10}$$

By solving σ^2 and a_k, b_k , the power spectrum could be calculated. If the all the coefficients b_k are zero for $k > 0$, the model is referred to as an Autoregressive (AR) model. If all the coefficients a_k , except for $a_0 = 1$, are zero, the model is referred to as a Moving Average (MA) model. If at least one of each of the coefficients a_k and b_k for $k > 0$ are nonzero,

the model is referred to as an Autoregressive Moving-Average (ARMA) model. There are many different algorithms for the above models, such as the Levinson-Durbin, Burg, and Marple algorithms, etc. [93,94]. The AR model represents a regression of the current value that is generated based on the past values, while the MA model generates the current values based on the errors from the past forecasts. The ARMA models cover both aspects of AR and MA, which predicts the future values based on both the previous values and errors, and has better performance than the AR and MA models alone. However, frequency domain analysis methods are mostly used in radar signal processing, and the model-based analysis methods are rarely used [95].

All of the aforementioned spectrum estimation techniques are frequently used to estimate flow velocities, but they are all constrained by determining the direction of arrival and thus cannot fully reconstruct the flow field on the river surface. Due to its multicomponent characteristic, the MUSIC algorithm in the nonparametric model is frequently used to estimate the directional angle of ocean surface currents [34,35,96]. Recently, this method has been gradually applied to rivers [46].

The foundation of the MUSIC algorithm is that there are P -th spatially independent echoes from different orientations θ_i and incidences on the array:

$$S(t) = [s(\theta_1), \dots, s(\theta_p)] \tag{11}$$

Then its output:

$$X(t) = AS(t) + N(t) \tag{12}$$

where $A = [a(\theta_1), \dots, a(\theta_n)]$ is the directional coefficient matrix, $N(t)$ is the noise.

$$a(\theta) = \begin{bmatrix} 1 \\ e^{j\frac{2\pi d \sin \theta}{\lambda}} \\ \dots \\ e^{j\frac{2\pi d_n \sin \theta}{\lambda}} \end{bmatrix} \tag{13}$$

The covariance matrix of the signal is:

$$R_{XX} = E [XX^H] \tag{14}$$

The eigenvalue can be decomposed as:

$$R_{XX} = U \Sigma U^H = U_S \Sigma_S U_S^H + U_N \Sigma_N U_N^H \tag{15}$$

where $\Sigma = \text{diag}(\lambda_1, \dots, \lambda_M)$ is the eigenvalue matrix, U_S is the signal subspace, and U_N is the noise subspace. The spectrum function is denoted as:

$$P(\theta) = \frac{1}{a^H(\theta)U_N U_N^H a(\theta)} \tag{16}$$

Even though the MUSIC algorithm has enhanced the resolution of calculating the direction angle, and opened up the possibility of reconstructing the flow field, the application of this method is still constrained by the fact that the majority of the radar flowmeters used in rivers currently are fixed-point radars, which usually have only one signal channel and can only receive echo from one direction.

3.3. Target Detection Methods

Doppler frequencies are known to be produced by targets with radial movement, and their magnitude varies with the moving velocity. Currently, the differences in velocities are served as the theoretical foundation for separating moving targets from stationary interference clutter. Techniques such as moving target indication (MTI) and moving target detection (MTD) are constantly being used to figure out the target signal and suppress

the clutter. Moreover, CFAR processing is required to maintain the radar target detection system with a certain false alarm probability and detection probability. The main difference between MTI/MTD and CAFR is that the former focuses on clutter suppression while the latter focuses on target detection. Usually, the two algorithms can be used together, for example when dealing with sea clutter problems with severe interference. However, compared with sea clutter, river clutter is relatively simple, so only CFAR is used for velocity detection [97].

3.3.1. MTI and MTD

The purpose of the MTI filter is to minimize clutter interference while maintaining the maximum amount of information in the target signal. In order to increase the ability to detect the target signal while against the background clutter, the output signal-to-clutter ratio (SCR) should be improved as much as possible after the received echo signal passes through the MTI filter [98,99].

Usually, the signal $x(t)$ received by the radar includes the target echo signal $s(t)$ and the noise $n(t)$, and when there is clutter $c(t)$, the echo signal can be expressed as:

$$x(t) = s(t) + n(t) + c(t) \quad (17)$$

The SCR, which is defined as the ratio of signal power to the average power of clutter, is the key factor affecting the signal detection performance, since the average power of clutter P_c is frequently larger than the average power of noise P_s .

$$SCR = \frac{P_s}{P_c} \quad (18)$$

MTI filters can be constructed using both analog and digital methods. Usually, the digital clutter cancellers are the most commonly used, which can be separated into single, double, and multiple types based on the quantity of cancellations [100,101].

The simplest MTI filter is the single delay line canceller, which functions by subtracting two consecutive echo signals. The unit impulse response and its Fourier transform are given when the input is $x(t)$, the system function is $h(t)$, and the output is $y(t)$.

$$h(t) = \delta(t) - \delta(t - T) \xrightarrow{FT} H_1(\omega) = 1 - e^{-j\omega T} \quad (19)$$

The power gain of the single delay line canceller is:

$$|H_1(\omega)|^2 = 4(\sin(\omega T/2))^2 \quad (20)$$

The SCR cannot be improved significantly when the clutter dynamics change due to the single delay line canceller's characteristics. This issue can be resolved by connecting several delay line cancellers in series as shown in Figure 5, which could improve the filtering effect. Its impulse response and power gain are:

$$h(t) = \alpha_0\delta(t) + \alpha_1\delta(t - T) + \alpha_2\delta(t - 2T) \cdots \alpha_n\delta(t - nT) \quad (21)$$

$$|H_n(\omega)|^2 = |H_1(\omega)|^{2n} = 2^{2n}(\sin(\omega T/2))^{2n} \quad (22)$$

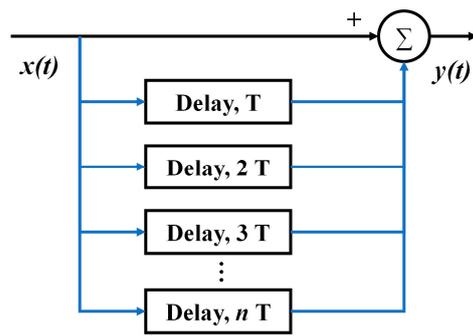


Figure 5. Structure diagram of several delay line cancellers.

The primary idea of MTI is to filter clutter by canceling numerous echoes. However, this method is limited to situations where the clutter never changes or the clutter with fixed features, and has a poor effect on suppressing other types of clutter. Based on the optimal filter theory, MTD was created to address the drawbacks of MTI, and has the advantage of recognizing targets as movable that are not currently moving [102]. In the process of MTD, a narrowband Doppler filter set is cascaded after the MTI in order to cover the entire range of repetition frequencies, which is essentially a coherent integration process for different channels [103,104]. The coherent integration can be expressed as:

$$y(n) = \sum_{i=0}^{N-1} w_i x(n - iT_r) \tag{23}$$

where T_r is the radar repetition period, N is the number of accumulated pulses, and w_i are the weighting coefficients. The weighting coefficients are transformed as follows:

$$w_{ik} = e^{-\frac{j2\pi ik}{N}} \quad (i = 0, 1, 2, \dots, N - 1) \tag{24}$$

where i is the i -th coefficient output and k is the weighted value, corresponding to different Doppler filter responses, the impulse response functions are:

$$h_k(t) = \sum_{i=1}^{N-1} \delta(t - T_r) e^{-\frac{j2\pi ik}{N}} \tag{25}$$

The frequency response functions are:

$$H_k(f) = e^{-j2\pi ft} \sum_{i=0}^{N-1} e^{-j2\pi i(fT_r - \frac{k}{N})} \tag{26}$$

The filter amplitude characteristics can be expressed as:

$$|H_k(f)| = \left| \frac{\sin[\pi N(fT_r - k/N)]}{\sin[\pi(fT_r - k/N)]} \right| \tag{27}$$

So far, a narrowband Doppler filter bank can currently be implemented in two different ways: the time domain method and the frequency domain method [105,106].

3.3.2. CFAR

CFAR is an important part of radar signal processing. It distinguishes targets from clutter by setting a certain power threshold, above which is determined as a target. Various sources of interference, including internal device noise, ground features, water waves, rain, and snow, are constantly presented when detecting target signals [107,108]. In an automatic detection system, when the detection threshold was set, the likelihood of false alarms increased as interference intensity rose. Even though there is currently a sufficient

signal-to-clutter ratio, the radar signal processing system is still unable to reach a reliable decision [109]. As a result, a consistent false alarm rate detection is also necessary in order to recover the target signal in a severe interference environment.

CFAR was initially used for processing sea clutter and then for river clutter. In dealing with uniform and smooth clutter, a cell-averaging constant false alarm (CA-CFAR) algorithm was presented by Finn et al., which was based on the assumption that the amplitude of echoes from clutter follows the Rayleigh distribution [110]. This algorithm uses the data from the nearby cells around the detection cell to estimate the power of background clutter and the detection threshold, which has the best detection performance in a uniform environment. However, a target suppression effect refers to the inability to effectively distinguish the target to be measured due to the superposition of multiple signals, which happens when several targets are near together and have the same orientation, or when one target is in the detection cell and others are in the reference cells. To deal with the target suppression effect, and prevent miss detections of the target, Trunk et al. have proposed the Smallest Of (SO)-CFAR algorithm, the threshold value of which is defined by the average minimum value of cells [111]. In addition, the clutter edge effect has been suggested, which occurs at the junction of clutter and can easily lead to missed detections and rapid rise in constant false alarms when the clutter power in adjacent cells differs greatly. Hansen et al. has suggested using the Greatest Of (GO)-CFAR algorithm to reduce false alarms at the clutter edge [112]. The difference between SO-CFAR and GO-CFAR is that instead of the minimum value of the cells now the maximum one is used. In the case of multi-target detection, the Ordered Statistics (OS)-CFAR algorithm was employed to enhance the performance of the CA-CFAR algorithm [111]. Instead of averaging the data in the reference cells to estimate the power, this type of algorithm sorts the data in the reference cells from the smallest to the largest, uses the k -th sorted value as the estimation of the power, and multiplies it by the threshold factor as the detection threshold. Although the OS-CFAR algorithm is processed with only one reference data value, it essentially relies on all sample data within the reference cells, and the value of k directly affects the quality of the detection result. Rohling et al. [113] and Nathanson et al. [114] have studied the length N of the reference window and the value of k of the OS-CFAR algorithm in detail, and the results showed that the clutter edge effect would be enhanced when $k < N/2$. As a result, the value of k is usually taken to be around $3N/4$. Table 1 lists the advantages and disadvantages of the typical algorithms above. However, there is no perfect solution that can fix all problems simultaneously, because the application of the above algorithms is typically constrained, while the background signal clutter is complex and changeable.

Table 1. The advantages and disadvantages of different CFAR algorithms.

Algorithm	Advantages	Disadvantages
CA-CFAR	High detection performance in the case of uniform clutter background.	The detection performance degrades in multiple targets and the clutter edge condition.
SO-CFAR	Good detection performance in the case of multiple targets	The probability of false alarm rises in the clutter edge condition.
GO-CFAR	Robust edge clutter resistance.	Multiple targets increase the likelihood of false alarms and decrease the detection performance.
OS-CFAR	Great detection performance in multiple targets circumstances. Good anti-clutter edge capabilities.	High false alarm loss due to the influence of k -value. Time-consuming process, and high hardware requirements.

3.4. Flow Calculation Methods

Since the radar can only measure the surface velocity, translating the surface velocity into the cross-section flow is of great necessary. The index-velocity method, the probability concept method, and the surface velocity coefficients method are currently the most widely utilized techniques.

3.4.1. Index-Velocity Method

The index velocity method is often used to correct the observations of the flow meters so as to reduce errors from the real average velocity, which is currently one of the most frequently used techniques by many nations and international organizations. The essence of this method is to determine the relationship between the index-velocity and the cross section average velocity, in other words, to utilize the local velocity of the river section to determine the cross section average velocity [115,116]. Three categories of typical index-velocity exist [117]:

1. Single point velocity, which measures the velocity at a single point in a river section.
2. Depth averaged velocity, which takes into account the river's average velocity in a vertical direction.
3. Horizontal average velocity, which utilizes a certain water layer's average velocity.

There are two traditional methods that can be used to determine the cross section average velocity of the river, when the cross section average velocity V_m and the index-velocity V_{index} are obtained:

The first one is the least squares linear regression, which is generally applicable when the changes in water level have little effect on the velocity. Its regression equation is as follows:

$$V_m = aV_{index} + c \quad (28)$$

where a, c are regression coefficients.

The second one is multiple linear regression, which is suitable when the changes in water level have a large impact on the velocity, and its regression equation is as follows:

$$V_m = (a + bH)V_{index} + c \quad (29)$$

where a, b, c are regression coefficients, H is the water level.

3.4.2. Probability Concept Method

In 1988, Chiu et al. [118] introduced the Shannon's entropy theory [119] into the hydraulic calculation and derived the velocity distribution of an open channel, which was known as the probabilistic velocity distribution method. In 1998, this method was used by Chiu and Chen to estimate the river flow rate with the fewest observations in a short time, which solved the problem of monitoring high flows and improved the safety of testing [120]. After that, this method was respectively applied to the tidal and typhoon-affected rivers, and the results demonstrated that it has good applicability for unsteady flow [121].

The fundamental idea of the probability concept method is to convert the traditional y - z coordinate system into a ξ - η iso-velocity coordinate system, as shown in Figure 6. Where ξ is the iso-velocity line, which corresponds to the flow velocity, and the η line is orthogonal to the ξ line. At $y = 0$, the $\xi = \xi_0$, and the maximum flow velocity is reached when $\xi = \xi_{max} = 1$. If $h > 0$, it indicates that the maximum flow velocity occurs below the water surface, if $h < 0$, it is meaningless. The relationship between y and ξ can be expressed as:

$$\xi = \frac{y + \delta_y}{D + \delta_y - h} e^{(1 - \frac{y + \delta_y}{D + \delta_y - h})} \quad (30)$$

where δ_y is related to the cross-sectional geometry of the channel, its relationship with the area A , channel width B , and water depth D is as follows:

$$\frac{A}{BD} = 1 - \frac{\delta_y}{D} \ln\left(\frac{1 + \frac{\delta_y}{D}}{\frac{\delta_y}{D}}\right) \quad (31)$$

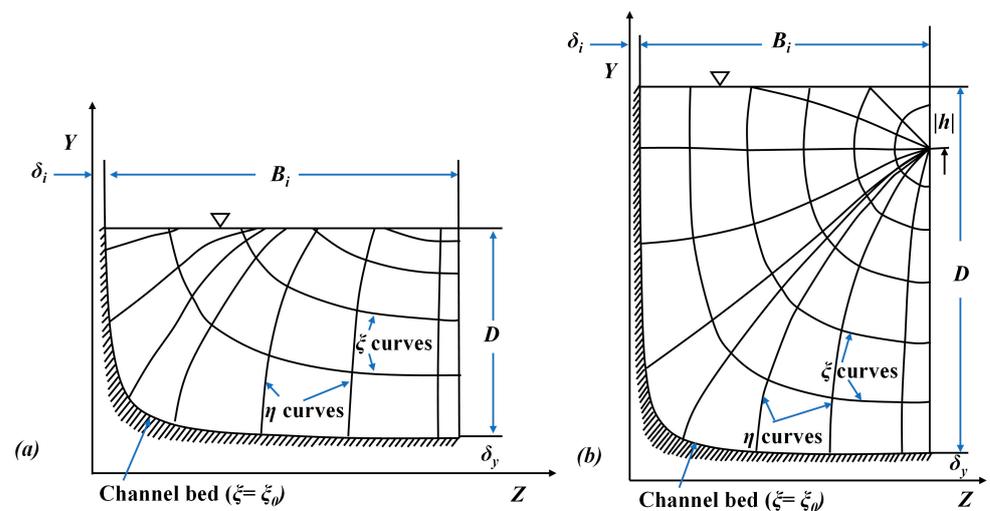


Figure 6. Schematic diagram of the probability concept-based velocity distribution calculation method. (a) Iso-velocity coordinate system for $h < 0$. (b) Iso-velocity coordinate system for $h > 0$.

According to the flow velocity distribution model proposed by Chen, the relationship between the maximum flow velocity and the average flow velocity of the cross section can be deduced as follows:

$$\frac{\xi - \xi_0}{\xi_{\max} - \xi_0} = \int_0^U p(u) du = \frac{e^{M \frac{u}{U_{\max}}} - 1}{e^M - 1} \tag{32}$$

where $p(u)$ is the probability density function, it meets:

$$p(u) = \frac{M}{U_{\max} e^M - 1} e^{M \frac{u}{U_{\max}}} \int_0^{U_{\max}} p(u) du = 1 \int_0^{U_{\max}} u \cdot p(u) du = \bar{U} \tag{33}$$

The relationship between the average flow velocity and the maximum velocity can be determined using the equation below:

$$\frac{\bar{U}}{U_{\max}} = \frac{e^M}{e^M - 1} - \frac{1}{M} = \Phi(M) \tag{34}$$

As a result, the flow rate can then be described as:

$$Q = A\bar{U} = A\Phi U_{\max} \tag{35}$$

3.4.3. Surface Velocity Coefficients Method

As mentioned above, the first step in calculating the flow rate is to obtain the average velocity of the cross section. To achieve this purpose, some researchers have multiplied the surface velocity by the surface velocity coefficient η_s . Then, as illustrated in Figure 2d, the river flow can be computed using the velocity-area method. Commonly used flow distribution models include logarithmic distribution, exponential distribution, parabolic distribution, and elliptical distribution, etc. The most usually used exponential distributions is taken as an example below [122].

Assuming that the flow velocity distribution is exponential, the flow velocity $u(z)$ at any point in the vertical direction can be expressed as:

$$u(z) = u_s \left(\frac{z}{h}\right)^{\frac{1}{m}} \tag{36}$$

where u_s is the surface velocity, h is the depth of water, m is the roughness coefficient of channel.

The mean vertical velocity \bar{v} and surface velocity coefficient η_s are:

$$\bar{v} = u_s \cdot \frac{m}{m+1} \eta_s = \frac{m}{m+1} \quad (37)$$

The relationship between surface velocity coefficient and channel roughness is shown in Table 2

Table 2. The relationship between surface velocity coefficient and channel roughness.

	Pretty Coarse	Coarse	Normal	Smooth
m	1–2	3–4	5–7	8–10
η_s	0.50–0.67	0.75–0.80	0.83–0.88	0.89–0.91

The surface velocity coefficients can be chosen in accordance with Table 2, when the exponential distribution is chosen as the velocity distribution model [123]. The USGS suggests taking η_s in the range of 0.80–0.85 for natural channels. In Japan, $\eta_s = 0.85$ is used as the reference value. In France, Hauet et al. came to the following conclusions after analyzing 3611 stations on 176 channels: (1) The relationship between the surface velocity coefficient and roughness is complex and still unknown. (2) The average value of the surface velocity coefficient for natural rivers (with a sand, cobble, or boulder bed) is 0.80. (3) The average value of the surface velocity coefficient for artificial concrete channels is 0.90 [124].

4. Discussion

4.1. Current and Future Limitations

After assessing the state-of-the-art signal sampling, the following limitations of radar flow monitoring technology can be identified to be most critical:

Limitations of the radar equipment: Since the fixed-point radar can only measure the flow velocity at a specific point or a small range of the river, multiple devices would be required if the river is wide, which would result in high input costs, installation and maintenance challenges, data assimilation calculation complexity, and other issues [125]. Therefore, it is currently only applicable to the hydrological sections that are relatively stable, narrow, and where there are bridges, cableways, or cantilevers that can be used. Secondly, the fixed-point radar has strict requirements on installation position and angle, which increases the uncertainty of measurement and the difficulty of maintenance. The main factors affecting the measurement accuracy are the beam width, azimuth, and elevation angle. As the beam tilt illuminates the water surface, any strong reflection within the elliptical projection formed by the beam width may be identified as the flow velocity, so the larger the beam width, the smaller the elevation angle, and the higher the uncertainty of the measurement. Finally, fixed-point radars usually operate at high frequencies. Considering the cost and portability, the design of this type of radar on the market is relatively simple, and fewer filtering methods are equipped, so the velocity measurement performance will be significantly impacted by heavy rain or other adverse weather conditions. The side-scan radar has a longer measuring distance, can not only monitor the average flow velocity within a segmented range, but also estimate the direction of arrival, which to a certain extent makes up for the shortcomings of the fixed-point radar. However, the current side-scan radars mostly adopt the HF/UHF band to monitor the gravity waves of water flow. Due to the frequency and bandwidth limitations, it has a low Doppler measurement accuracy and is challenging to obtain stable measurements on smooth surfaces or in turbulent flows. Moreover, the band used by this radar might interfere with local communication in some regions [42].

Problems with spectrum estimation methods: The modern spectrum estimation is a non-linear estimation method where the estimation performance is dependent on the parametric model and is weakly applicable. The model used must be appropriate for the signal being

analyzed; otherwise, the spectrum estimate will be incorrect or inaccurate. The classical spectrum estimation based on the Fourier transform is currently the mainstream spectrum estimation method. However, both the periodogram and the correlation function suffer from low resolution and poor variability [126]. The low resolution is due to the fact that the frequency resolution is proportional to the length of the data recorded, and the longer the data, the higher its resolution. However, since the data from radar flowmeters is typically used for short-term or emergency monitoring in some cases, it is impossible to accumulate enough data. The reason for the poor variance performance is that the classical spectrum estimation lacks averaging and limit procedures, which makes it less stable. Improved algorithms for classical spectrum estimation have already emerged, such as the Welch method and the window function method, etc. [127]. The Welch method uses techniques like averaging and smoothing to improve the variance performance of the periodogram, but it lowers the resolution and increases the bias. The window function widens the main lobe of the power spectrum while reducing the resolution simultaneously. Therefore, in practice, a trade-off must be made between variance, bias, and resolution.

Applicability of target detection algorithms: Conventional target detection techniques usually have a fixed center of the filter bank, while the Doppler frequency of a moving target might be located anywhere between two adjacent filters, which may result in signal loss and even lead to filtering failure. In addition, these techniques generally perform well only in specific clutter environments, but the detection performance cannot be guaranteed due to the complexity of the clutter environment in practice, which makes it difficult to maintain a certain false alarm rate and an accurate target detection probability.

Accuracy of flow inversion algorithms: Methods for calculating river flows by obtaining surface velocities inevitably have some limitations. For instance, the empirical index-velocity method depends on the utilization of long-term measured velocity and flow rate to determine the relationship between the average velocity and the index velocity, which is challenging to use in areas where data are not available. In addition, this method also has limited ability to predict the flow rate over the long term because it merely performs a simple regression of surface velocity and index velocity without accounting for the characteristics of the cross-section. The probability concept method points out that there is a linear relationship between the maximum surface velocity and the average velocity, so when this method is used for flow calculation, the location of the maximum surface velocity is generally needed to be measured in advance. Another disadvantage of this method is the poor resilience of long-term observations, since the movement of the flow field is intricate and the velocity at each location cannot be constant. The surface velocity coefficients method is typically used for wide and shallow rivers, which generally assumes that all unit sections follow the same velocity distribution model while ignoring the interactions between waters, and its accuracy needs to be improved.

4.2. Future Potentials

In recent years, different radar technologies, such as phased array, multiple input multiple output, over-the-horizon, quantum detection, terahertz, and others, have been developed significantly in various fields [128]. These developments have guided the theory and practice of expanding radar techniques applied to hydrometric. For instance, radar integrated with phased array and over-the-horizon techniques can accomplish measurements of velocity, flow direction, and flow rate in extra-wide rivers or lakes, which used to be conducted via manual methods. Additionally, the hydrometric can be expanded to monitor the physical and chemical properties using non-contact measurement techniques such as terahertz, quantum detection, and other new technologies.

In addition, radar technology for river flow monitoring is a non-contact method. The use of radar eliminates the need for workers and equipment to come into contact with the water, which improves the safety of the operators, particularly during times of extreme floods and emergencies. Moreover, it has no impact on ship navigation, and is suitable for seasonal rivers or low water level areas without being damaged by sand content or

floating objects. Therefore, radar is a necessary and crucial piece of hydrological monitoring equipment for the future, whether it is for emergency monitoring of floods brought on by severe weather or dealing with extreme water flow conditions such as high velocity, high water level, and high sand content.

Furthermore, radar has made significant advancements in the temporal and spatial density of data acquisition compared to traditional methods. Traditional methods are labor-intensive, yield few results, and are expensive due to the manual labor involved. Radar can obtain surface velocity data from multiple sections in a short time, without on-call personnel and independent of weather, which significantly lessens the workload of hydrometric and shifts the focus from labor-intensive testing to data analysis and processing. As a result of these modifications, we are now able to automate and intelligently perform hydrometric while also obtaining large amounts of data with high temporal and spatial resolution as the target dynamics change. We are also no longer restricted to flow monitoring and can use big data analysis techniques and multi-dimensional data for real-time forecasting and even achieve early warning of extreme natural disasters, which is a big trend for the future.

4.3. Future Challenges

The following scientific issues must be resolved in order to advance the state-of-the-art signal sampling and make the announced potential applications feasible in the future:

Multi-point and high-precision flow monitoring radar: The fixed-point radar can only monitor a single point or a small area, while the side-scan radar can monitor a large area, but the accuracy needs to be improved. As a result, both fixed-point and side-scan radars are lacking in monitoring range or accuracy at present. It is required to build a radar system that balances the detection distance and resolution accuracy to realize simultaneous multi-point measurements of velocity. Typically, the higher the radar frequency, the better is its measurement performance. Therefore, the millimeter-wave radar can be introduced into the flow measurement system to improve the flow measurement accuracy. In addition, multi-channel frequency modulated continuous wave radar can be used to innovatively achieve distance and velocity estimation at multiple points on the river surface from both range and Doppler dimensions, so as to improve system robustness and meet various application scenarios and accuracy requirements.

Adaptive filtering algorithms: The monitoring of flow velocity is highly dependent on the filtering methods when there is clutter interference. However, at the present, different filtering algorithms only work when there is prior knowledge of the clutter. In order to obtain highly accurate monitoring results, a model of the target clutter background must be created first or simply fit an existing model, such as the Rayleigh, the Log-Normal, or the Weibull distribution [129]. Once the clutter model has been determined, the number of interference targets and the clutter edge of the clutter background can then be determined. After that, the filtering algorithm can be adaptively selected based on the clutter model to achieve better detection results.

High-precision analysis of Doppler spectrum: The components of the radar echo signal are complex, and the Doppler spectrum is greatly broadened due to the antenna beam width, the distributed multiple scattering points, and environmental conditions. The exploitation of the micro-Doppler information is insufficient because current signal processing is only able to be operated in the one-dimensional frequency domain and relies mostly on a relatively rough Doppler spectrum analysis of the strong scattering points. As a result, in the future, it may be possible to develop micro-Doppler models using time-frequency analysis of the Doppler spectrum at various time and frequency scales to produce more precise flow velocity results.

Flow inversion algorithm considering hydrodynamic processes: The traditional surface velocity to flow algorithms are mostly empirical or semi-empirical models, which do not consider the influence of water movement on the flow field, and therefore have poor applicability for calculating different river flows. In order to ensure the accuracy and

universality of the model, the relationship between the surface flow field and cross-section flow velocity distribution should be considered from the perspective of hydrodynamics.

Integration with other monitoring technologies: Due to the complexity of information acquisition, the amount of data collected by a single sensor is relatively sparse, and complex algorithms are usually required to obtain the necessary information, which increases the difficulty of calculating velocity. Limited by the construction of the sensor, the detectable range, detectable objects, and the type of data obtained are different, which can lead to false or missed detections and cannot achieve all-weather, high-precision monitoring of the target. Therefore, in order to obtain more complete and accurate comprehensive information, traditional monitoring methods or other non-contact methods (such as satellite, vision, etc.) can be considered in combination with radar technology to extend the measurement range and enhance the adaptability and robustness of the system.

5. Conclusions

Radar-based flow monitoring techniques have advanced significantly since they were first used in hydrometrics. The derived flow results are now comparable to those of traditional methods owing to the developments in signal sampling, Doppler spectrum estimation, signal processing, and flow inversion techniques. The advantages of non-contact methods and the dramatic advances in the temporal and spatial density of the acquired data show the potential of radar technology. The application prospects for this technology are fairly extensive due to the ongoing advancements in radar technologies and the rising demand for dynamic, accurate, and intelligent hydrological information.

To fully utilize this technology, though, a number of challenges must be overcome. The monitoring distance and accuracy of the radar equipment currently used still need to be improved, and the filtering algorithms, Doppler spectrum analysis techniques, and flow inversion techniques still have their limitations. However, with an increase in active studies and a focus on non-contact monitoring techniques in several nations over the past few years, radar-based flow monitoring techniques have acquired progressively momentum, and the research on radar flow monitoring is becoming an established field in hydrometrics. It is hoped that the assessment of the current state-of-the-art signal sampling and the general comments on its limitations and challenges will be helpful in directing future study in this fascinating and developing field.

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