

Article **Numerical Investigation on the Symmetric Breakup of Bubble within a Heated Microfluidic Y-Junction**

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Abstract: This study numerically investigated the symmetric breakup of bubble within a heated microfluidic Y-junction. The established three-dimensional model was verified with the results in the literature. Two crucial variables, Reynolds number (*Re*) and heat flux (*q*), were considered. Numerical results demonstrated that the bubble breakup was significantly affected by phase change under the heated environment. The "breakup with tunnel" and "breakup with obstruction" modes respectively occurred at the low and high *q*. The breakup rate in pinch-off stage was much larger than that in squeezing stage. As *Re* increased, the bubble broke more rapidly, and the critical neck thickness tended to decrease. The bubble annihilated the vortices existing in the divergence region and made the fluid flow more uniform. The heat transfer was enhanced more drastically as *Re* was decreased or *q* was increased, where the maximum Nusselt number under two-phase case was 6.53 times larger than single-phase case. The present study not only helps understanding of the physical mechanisms of bubble behaviors and heat transfer within microfluidic Y-junction, but also informs design of microfluidic devices.

Keywords: microfluidic Y-junction; bubble breakup; flow characteristics; phase change heat transfer; numerical simulation

1. Introduction

Recently, microfluidic devices have shown potential in cutting-edge areas such as chemical reaction, biomedical engineering, and electronic cooling, among others [\[1,](#page-12-0)[2\]](#page-12-1). Compared with the devices at conventional size, microfluidic devices possess higher heat and mass-transport efficiencies because of their larger surface-to-volume ratio [\[3,](#page-12-2)[4\]](#page-12-3). For electronic cooling at high heat flux, the two-phase flow can utilize the latent heat of vaporization, leading to better heat dissipation performance compared to single-phase flow [\[5](#page-12-4)[,6\]](#page-12-5). At the same time, the complexity significantly increases, and this causes difficulties in predicting heat transfer. Appropriate design for microfluidic devices requires thorough understanding of phase-change phenomena and the mechanisms involved.

As one kind of basic structure for microfluidic devices, the Y-junction has drawn much interest from researchers owing to its applicability to flow control [\[7\]](#page-12-6). By employing the Y-junction under a two-phase flow mode, not only the bubbles or droplets can be formed, but also their sizes can be efficiently controlled [\[8\]](#page-12-7). Recent advancement in highspeed photography techniques has enabled experimental investigation at microscale [\[9\]](#page-12-8). Fei et al. [\[10\]](#page-12-9) experimentally studied the effect of nanoparticles on the breakup of bubble within microfluidic Y-junction, as compared to conventional bubble. They found that the degree of effect caused by nanoparticles varied with breakup stage. Lim et al. [\[11\]](#page-12-10) conducted an experiment on bubble formation using a microfluidic Y-junction. Results indicated that the angle between the gas and liquid channels exerted notable effect on the

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size of formed bubbles. Liu et al. [\[12\]](#page-12-11) concentrated on the unique anti-Y-junctions and experimentally studied the droplet formation characteristics. It was found that both the formation cycle and size varied with branching angle and channel depth. Li et al. [\[13\]](#page-12-12) employed a magnetic field to achieve asymmetric breakup of droplet in symmetric structure, which showed satisfying effects. The mechanism of droplet control under magnetic field was well-revealed.

It should be noted that some flow details still cannot be easily captured through experimental methods. Attributable to the rapid improvements of computing resources and numerical modeling, more and more studies have been performed using simulation. Deka et al. [\[14\]](#page-13-0) numerically studied the droplet under different surface wetting conditions. Three distinct splitting behaviors, including non-splitting, splitting, and oscillating, were seen, and the flow pattern map was provided for reference. Ren et al. [\[15\]](#page-13-1) focused on the bilayer bifurcating microchannel and performed simulations on droplet breakup within it. The unique bubble behaviors and flow characteristics were elucidated. Zheng et al. [\[16\]](#page-13-2) numerically investigated asymmetric droplet breakup behaviors in microchannel based on the VOF method. Slight differences in breakup can be seen with the variation of branching angle. Wang et al. [\[17\]](#page-13-3) developed the numerical model to analyze the liquid–liquid flow within a microfluidic Y-junction. The relation between the velocity ratio and length ratio was revealed by parametric investigations.

Unlike the adiabatic operation environment, sometimes the phase change phenomenon may be involved under heated operation environment [\[18](#page-13-4)[,19\]](#page-13-5). The phase change could alter the bubble behaviors, which further affects the flow characteristics. Latent heat can be used during the process of phase change, indicating the essential difference in heat transfer mechanism [\[20,](#page-13-6)[21\]](#page-13-7). So far, the two-phase evaporating heat sink has shown promising application in dissipation of high heat flux [\[22](#page-13-8)[,23\]](#page-13-9). Meanwhile, many researchers have conducted fundamental studies to reveal the corresponding heat transfer mechanism. Li et al. [\[24\]](#page-13-10) proposed a new type of microchannel by coupling micro-pinfin arrays. Excellent performance was achieved, with the CHF of 345 $W/cm²$ at the maximum mass flux. The studies from Qiu et al. [\[25\]](#page-13-11), Yuan et al. [\[26\]](#page-13-12), and Yin et al. [\[27\]](#page-13-13) also indicated the merits of configuring micro-pinfin structure for two-phase flow. Apart from the application of pinfin, the open microchannel structure could also produce better heat transfer [\[28,](#page-13-14)[29\]](#page-13-15). Vontas et al. [\[30\]](#page-13-16) numerically evaluated the effect of wettability on boiling heat transfer. The heat transfer mechanism was found to vary with wettability. Generally, the hydrophilic surface could lead to a larger CHF owing to the efficient liquid supply, while the hydrophobic surface could produce a larger heat transfer coefficient due to easier nucleation [\[31\]](#page-13-17). Based on this point, some studies focused on the surface with heterogeneous wettability [\[32,](#page-13-18)[33\]](#page-13-19), which was the combination between the hydrophilic and hydrophobic surfaces. The kind of working fluid also significantly influenced the phase-change process [\[34\]](#page-13-20). Compared with the single kind of working fluid, the mixture working fluid may be beneficial to heat transfer [\[35\]](#page-13-21). It is well-known that instability of heat transfer is harmful in engineering applications [\[36\]](#page-13-22), and many works are devoted to the suppression of instability. Lu et al. [\[37\]](#page-13-23) conducted experiments on flow instability under boiling conditions. Instability was prone to emerge at annular flow mode. A prediction model was developed to predict the instability behavior. By performing detailed analyses, Alugoju et al. [\[38\]](#page-13-24) revealed that the instability can be mitigated by employing the diverging microchannel.

It was found that the previous studies mainly focused on the bubble dynamics in adiabatic microfluidic Y-junction. The evaporation that occurred in the heated microfluidic Y-junction could alter the bubble dynamics and yield new physical phenomena. However, few studies have focused on heated microfluidic Y-junction. In the present work, after the verification of numerical model, the bubble behaviors and flow characteristics were first investigated. Then, the evaporating heat transfer performance was quantitatively studied. The purpose of the present work is to reveal the physical mechanisms of transport phenomena within heated microfluidic Y-junctions, which could help the design of microfluidic devices.

2. Problem Description and Mathematical Model

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The illustration of the bubble motion within a heated microfluidic Y-junction is shown in Figure 1. All the chan[ne](#page-2-0)ls had a width (W) of 100 µm. The microfluidic Y-junction consisted of main channel (MC, with length of 20 *W*) and branching channel (BC, with length of 10 *W* for each one), where the branching angle was 90°. We mainly concentrated on the bubble behaviors and heat transfer within the branching channel, and the different on the bubble behaviors and heat transier whilm the branching channer, and the different
walls of BC should be distinguished. Taking the relative locations into account, the leeward $(BC-L)$, windward $(BC-W)$, and top $(BC-T)$ walls were employed to represent different parts of BC.

Figure 1. Illustration of the bubble motion within a heated microfluidic Y-junction. **Figure 1.** Illustration of the bubble motion within a heated microfluidic Y-junction.

In the present study, the boundary conditions for the inlet and outlet were, respectively,
 the constant heat flux mode, where the heat flux varied from $2000 \,\mathrm{W/m^2}$ to $12,000 \,\mathrm{W/m^2}$. The saturated HFE-7100 liquid entered the microfluidic Y-junction through the inlet, with the Reynolds number (*Re*, *U*·*W*/*v*) varying from 180 to 420. The properties of HFE-7100 are gathered in Table [1](#page-2-1) [\[39\]](#page-13-25). To efficiently facilitate the heat transfer performance, the seed
are properties in Table 1 [39]. To efficiently facilitate the heat transfer performance, the seed placing the seed bubble, the single-phase case was run until the velocity and temperature placing the seed bubble, the single-phase case was run until the velocity and temperature fields became steady. In the simulation, the contact angle for all the walls was set as 0° . velocity inlet and pressure outlet. The boundary condition for the heated walls belonged to bubble strategy was adopted [\[40\]](#page-13-26), where the bubble diameter was fixed at 0.8 *W*. Before

at 0.8 *W*. Before placing the seed bubble, the single-phase case was run until the velocity **Table 1.** Physical properties of HFE-7100 medium [\[39\]](#page-13-25).

Properties	Liquid	Vapor
ρ (kg/m ³)	1425	5.15
μ (Pa·s)	3.56×10^{-4}	1.11×10^{-5}
σ (N/m)	0.0136	0.0136
c_p (kJ/(kg·K))	1.430	0.900
λ (W/(m·K))	0.0618	0.0103
h_{fg} (kJ/kg)	117.8	117.8

2.2. Mathematical Model

The fluid flow within microfluidic Y-junction was assumed to be incompressible and laminar. The VOF method based on the color function *C* was utilized to capture different phases. The vapor and liquid were set as the primary and secondary phases, respectively.

The governing equations were [\[6\]](#page-12-5):

Continuity Equation:

$$
\frac{\partial (C_i \rho_i)}{\partial t} + \nabla \cdot (C_i \rho_i \vec{U}) = S_{m,i} \tag{1}
$$

Momentum Equation:

$$
\frac{\partial(\rho \vec{U})}{\partial t} + \nabla(\rho \vec{U} \cdot \vec{U}) = -\nabla P + \nabla(\mu(\nabla \vec{U} + \nabla \vec{U}^T)) + F_s \tag{2}
$$

Energy Equation:

$$
\frac{\partial(\rho c_p T)}{\partial t} + \nabla(\rho c_p T \vec{U}) = \nabla \cdot (\lambda \nabla T) + S_h \tag{3}
$$

The continuum surface force (CSF) model proposed by Brackbill et al. [\[41\]](#page-13-27) was employed for the treatment of surface tension force *FS*:

$$
F_s = \sigma \kappa \delta_s \vec{n} = -\sigma \nabla \cdot (\frac{\nabla C}{|\nabla C|}) |\nabla C| \tag{4}
$$

It should be mentioned that error in the CSF model may lead to obvious unphysical flow, especially for cases with small capillary number. In simulation, we used the moving reference frame technique to effectively reduce the unphysical flow [\[42\]](#page-13-28).

Herein, the saturated-interface-volume (SIV) phase-change model was employed [\[43\]](#page-13-29). The model validation is showed in Section [3,](#page-3-0) and more details can be found in the literature [\[43,](#page-13-29)[44\]](#page-14-0). By assuming that the interfacial temperature is maintained at saturated state in each iteration, the energy source added on each cell can be acquired by the following Equation (5):

$$
S_{h,la} = \frac{C_l \rho_l c_{pl} (T_{sat} - T) + C_v \rho_v c_{pv} (T_{sat} - T)}{\Delta t}
$$
(5)

The acquisition of energy source did not require nested iterations, significantly reducing the computational cost and eliminating the numerical oscillations. For the implementation of SIV model in FLUENT 17.0 [\[45\]](#page-14-1), the UDFs were in the form of C programming language and the compiling environment was provided by Microsoft Visual Studio 2019. In the transient simulation, the Courant number was maintained at 0.1. The PISO algorithm was utilized to treat the pressure–velocity coupling, which worked well in simulation. The PRESTO and Green–Gauss node-based algorithms were responsible for the discretization of pressure and gradient, respectively. It should also be noted that a total of 2,514,708 cells were used in the simulation domain after performing the mesh independence study.

3. Verification of the Numerical Model

It was crucial to guarantee the reliability of the numerical model. Herein, two different verification cases were conducted. For the hydrodynamic model verification, the experiment performed by Xu et al. [\[46\]](#page-14-2) was employed. In the experiment setup, the bubble passed through microfluidic Y-junction under the push of liquid. The branching angle was 90° and the channel width was $400 \mu m$. The flow rates for gas and liquid were respectively 2.4 mL/h and 2.2 mL/h. As can be seen in Figure [2a](#page-4-0),b, both the simulated bubble profiles and forward distance showed good agreement with experimental results by Xu et al. [\[46\]](#page-14-2). We also utilized the simulation from Magnini et al. [\[47\]](#page-14-3) to verify the SIV phase change model [\[6\]](#page-12-5). The bubble moved and grew in a heated circular microchannel, with diameter

(*W*) of 500 μm. The heated part of the channel had length of 12 *W* and heat flux of 9 KW/m². The initial bubble length wa[s 3](#page-4-0) W. Figure 2c,d, respectively, show the bubble nose location and the distribution of local heat transfer, which were consistent with the simulation from Magnini et al. [47]. In brief, the established numerical model was capable of simulating the two-phase flow and phase change accurately.

et al. [46]. We also utilize the simulation from Magnini et al. [47] to verify the SIV phase \mathcal{A}

Figure 2. Verifications of hydrodynamic model (a,b) and phase change model (c,d). Xu et al. [\[46\]](#page-14-2); Magnini et al. [47]. Magnini et al. [\[47\]](#page-14-3).

4. Results and Discussion

4.1. Bubble Behaviors and Flow Characteristics

Figure [3](#page-5-0) shows the time-lapse images of the bubble profiles at different *Re* and *q*, where *Re* varies from 180 to 420 and *q* varies from 2000 W/m² to 16,000 W/m² . The bubble was pushed forward by the fluid and symmetrically broke within divergence region, with continuous growth. By changing the heating intensity, two various breakup modes can be seen: (1) "Breakup with tunnel" emerging at low *q* (see Figure [3b](#page-5-0)). Under this mode, the bubble volume was still small when arriving at divergence, and thus the channel cannot be fully blocked. The liquid can easily bypass the bubble and flow to the downstream. It is worth noting that the bubble breakup was closely related to the generated shearing force [\[48\]](#page-14-4); (2) "Breakup with obstruction" emerging at high *q*. Under this mode, the significant bubble growth occurred, and the channel was fully blocked by the bubble. The liquid cannot easily bypass the bubble, and only the accumulated pressure drove the breakup process. The velocity field was significantly affected by the bubble growth

characteristics, and one of the most notable features was the significant acceleration of downstream liquid at smaller *Re* and higher *q*. stream liquid at smaller *Re* and higher *q*. breakup process. The velocity field was significantly affected by the bubble growth characteristics, and one of the most notable features was the significant acceleration of

Figure 3. Time-lapse images of the bubble profiles at different *Re* and *q*. **Figure 3.** Time-lapse images of the bubble profiles at different *Re* and *q*.

The sketch of bubble profiles and the time variation of bubble neck thickness are shown in Figure [4.](#page-6-0) The dimensionless time was defined as *U*in·*t*/*W*. During the breakup process, the bubble neck thickness monotonically declined, where the declining rate experienced large variations. For the earlier squeezing stage, the declining rate of neck was relatively small and uniform. It was found that this stage took up the majority of breakup process. As the time elapsed, the bubble broke more rapidly, indicating the appearance of pinch-off stage. The breakup was governed by surface tension and could not halt in this stage [\[10\]](#page-12-9). In other words, if the upstream liquid supply was removed, the bubble could still break into two daughter bubbles. The duration time of the pinch-off stage was much shorter than that of the squeezing stage. As a special case, in the case of $q = 2000 \text{ W/m}^2$ (with *Re* = 300), the bubble cannot touch the windward wall in the initial stage, which attenuates the breakup rate. This stage was named as 'pre-breakup' stage. Along with the increase in *Re*, the breakup rate increased, and the critical neck thickness for the breakup stage transition tended to decrease. Generally, the effect of *q* on the breakup rate was weak.

stage transition tended to decrease. Generally, the effect of *q* on the breakup rate was

Figure 4. Sketch of bubble profiles (a) and the time variation of bubble neck thickness (b).

Figure 5 shows the time variation of dimensionless bubble volume (V/V_0) . The bubble volume increased due to evaporation, with increasing growth rate. In the later stage, the volume increased due to evaporation, with increasing growth rate. In the later stage, the bubble evaporation area increased. The evaporation strengthened because of the low flow velocity and accumulation of sensible heat for branching channel. The fluctuations of bubble volume emerged at larger *Re*. The terminal bubble volume was decreased by 6.2% as Re varied from 180 to 420. The terminal bubble volume at $q = 16,000$ W/m² was 7.42 times larger than that at $q = 2000 \text{ W/m}^2$.

Figure 5. Time variation of dimensionless bubble volume at different *Re* (**a**) and *q* (**b**).

To further reveal the mechanism of flow characteristics, the streamline profile and To further reveal the mechanism of flow characteristics, the streamline profile and detailed velocity field for both single-phase and two-phase cases are shown in Figure [6](#page-7-0). detailed velocity field for both single-phase and two-phase cases are shown in Figure 6. Under the single-phase case, the streamline was relatively circuitous and the symmetrical Under the single-phase case, the streamline was relatively circuitous and the symmetrical vortices occurred in proximity to leeward wall. As can be concluded from the cross-sections **Figure 5.** Time variation of dimensionless bubble volume at different Re (**a**) and q (**b**).
To further reveal the mechanism of flow characteristics, the streamline profile and
detailed velocity field for both single-p

of the branching channel, the flow velocity in the windward wall side was much larger than that in the leeward wall side. Unlike the single-phase case, the streamline became relatively smooth, and the vortices disappeared when the bubble traveled at divergence. Moreover, the distribution of velocity for the cross-sections of branching channel tended to be more uniform.

Under the single-phase case, the streamline was relatively circuitous and the symmetrical

Figure 6. Figure 6. Streamline profile and detailed velocity field for both single-phase and two-phase cases. Streamline profile and detailed velocity field for both single-phase and two-phase cases.

4.2. Two-Phase Heat Transfer Performance

4.2.1. Transient Heat Transfer

Before moving to discussion of local distribution of heat transfer, detailed time-lapse images of the temperature field are shown in Figure [7](#page-8-0) first. Under the single-phase case, the region near the leeward wall had higher temperature, indicating more sensible heat storage. The temperature of the heated region increased with decreasing *Re* and increasing *q*. The temperature of bubble interface was kept at saturated state. When the bubble got in contact with the superheated liquid, the phase change was activated, which absorbed the sensible heat and cooled the wall. The bigger the bubble size, the more notable a removal of sensible heat was achieved.

Figure [8](#page-9-0) shows the time variation of the local Nusselt number (*Nu*). The bubble profiles are also provided (see Figure $8a-c$ $8a-c$). The heat transfer of different walls was represented by the local *Nu* in the center line. The definition of *Nu* was:

$$
Nu = \frac{q}{T_w - T_{sat}} \cdot \frac{W}{\lambda_l} \tag{6}
$$

where λ_l represented the coefficient of heat conductivity for liquid. Under the single-phase case, the *Nu* of BC-W wall was the largest, which was found to drastically decrease along the downstream direction. The *Nu* of BC-L wall was always the smallest, which was relatively smooth. Interestingly, the *Nu* of BC-T wall increased first and then decreased.

Figure 7. Time-lapse images of the temperature field at different *Re* and *q*. **Figure 7.** Time-lapse images of the temperature field at different *Re* and *q*.

Figure 8 shows the time variation of the local number and the stage problem of the bubble pro-
two-phase case. For the bubble nose at 1 *W* (see Figure [8d](#page-9-0)–f), because the bubble did not fully touch the branching channel, the thin-film evaporation was relatively weak. Only the small part of corner produced very outstanding heat transfer performance. It should be *w sat l* transfer enhancement at *q* = 8000 W/m² became notable, while it was still inconspicuous at transfer enhancemen
nose located at 3 W (see *The TCC T T C Solid flow.* As the bubble nose located at 3 *W* (see Figure [8g](#page-9-0)–i), the heat transfer enhancement at $q = 8000 \text{ W/m}^2$ became notable, while it was still inconspicuous was caused by the thinner liquid film thickness emerging at lower flow velocity. When the bubble nose located at downstream 7 *W* (see Figure 8j–l), both the affecting region and intensity of heat transfer enhancement drastically increased. At *q* = 2000 W/m², the *Nu* in time region for BC-E want was far larger final that for BC-T and BC-T walls. The americine in *Nu* in film region for different walls became tiny at $q = 8000 \text{ W/m}^2$. There were some differences between the heat transfer under single-phase case and noted that the local fluid flow was affected by the bubble, which may hinder the local heat transfer. Some local regions with negative heat transfer enhancement emerged due to the for the case of $q = 2000 \text{ W/m}^2$. The *Nu* at *Re* = 180 was larger than that at *Re* = 300, which film region for BC-L wall was far larger than that for BC-W and BC-T walls. The difference

Figure 8. Time variation of the local Nusselt number. (a-c) show the bubble profiles. (d-f), (g-i), and $(i-1)$ respectively correspond to the instants of bubble nose locating at 1 W, 3 W, and 7 W.

4.2.2. Time Variation of Heat Transfer under single-phase and $\frac{1}{2}$

Figure [9](#page-10-0) shows the time variation of the Nusselt number under different *Re* and *q*. Under single-phase case, the averaged heat transfer of BC-W wall was better than other walls. The *Nu* increased with *Re* owing to the improvement of convection heat transfer intensity. Under two-phase case, the *Nu* of MC wall rose first and then reduced. The *Nu* of BC walls always rose, where the small fluctuations were caused by breakup behaviors. Unlike the single-phase cases, the two-phase heat transfer at larger *Re* was poor. This was i), the heat transfer enhancement at *q* = 8000 W/m2 became notable, while it was still because that the liquid film became thicker at larger *Re*, which hindered the evaporating because that the liquid film became thicker at larger *Re*, which hindered the evaporating heat transfer. Overall, the *Nu* increased with the increase in *q*. One result of interest was heat transfer. Overall, the *Nu* increased with the increase in *q*. One result of interest was that the maximum value of *Nu* for BC-L and BC-T walls did not occur at the highest *q*. The that the maximum value of *Nu* for BC-L and BC-T walls did not occur at the highest *q*. The bubble experienced very rapid expansion at the highest *q*, which facilitated the velocity of bubble experienced very rapid expansion at the highest *q*, which facilitated the velocity of the downstream part of the bubble. The local liquid film increased correspondingly, hence the downstream part of the bubble. The local liquid film increased correspondingly, hence suppressing the heat transfer. At $q = 2000 \text{ W/m}^2$ and 4000 W/m^2 , it was seen that the slight negative enhancement of heat transfer existed in the BC-T wall. negative enhancement of heat transfer existed in the BC-T wall.

of BC walls always rose, where the small fluctuations were caused by breakup behaviors.

Figure 9. Time variation of the averaged Nusselt number for different walls. (a-d), (e-h) respectively show the effects of *Re* and *q* on the averaged Nusselt number. show the effects of *Re* and *q* on the averaged Nusselt number.

4.2.3. Heat Transfer Enhancement

The time-averaging treatment for the heat transfer enhancement $(Nu_{\text{tp}}/Nu_{\text{sp}})$ was conducted to directly show the evaporating heat transfer characteristics. The definition of time-averaged Nusselt number for the main channel was:

$$
\overline{Nu}_{MC} = \int_{t_1}^{t_2} \frac{Nu_{MC}dt}{t_2 - t_1}
$$
 (7)

where t_1 and t_2 respectively indicated the instants that the bubble nose just touching the heated main channel and touching the heated branching channel. The definition of the time-averaged Nusselt number for the branching channel was:

$$
\overline{Nu}_{BC} = \int_{t_2}^{t_3} \frac{Nu_{BC}dt}{t_3 - t_2}
$$
 (8)

where t_3 indicated the instant that the bubble nose just left the heated part. The heat transfer enhancement for the overall microchannel was acquired by averaging the treatment for the heat transfer enhancement of different walls.

The time-averaged heat transfer enhancement for the microfluidic Y-junction versus *Re* and *q* is shown in Figure [10.](#page-11-0) Generally, the BC-L wall achieved the best enhancement of heat transfer, where the maximum *Nu* under two-phase case was 6.53 times larger than that under single-phase case. The phase change intensity for the main channel was weak, leading to poor heat transfer enhancement (less than 1.3) compared to branching channel. As *Re* increased from 180 to 420, the liquid film became thicker, which hindered the phase-change intensity. The falling rate of heat transfer enhancement for the overall Y-junction was 70.4%. The increase in *q* led to more intense evaporation, strengthening the heat transfer. The increasing rate of heat transfer enhancement for the overall Y-junction was 90.36% as q changed from 2000 W/m² to 16,000 W/m². Interestingly, the heat transfer of BC-L wall showed a declining trend as *q* exceeded 8000 W/m². This was because the bubble breakup mode had converted to "breakup with obstruction". The contact degree between the bubble and BC-L wall during breakup process was weakened under this mode.

Figure 10. Time-averaged heat transfer enhancement for the microfluidic Y-junction versus Re (a) and *q* (**b**). and *q* (**b**).

5. Conclusions 5. Conclusions

In the present study, the high-fidelity simulation on the symmetric breakup of bubble In the present study, the high-fidelity simulation on the symmetric breakup of bubble within a heated microfluidic Y-junction (90°) was performed with variations of Reynolds number (*Re*) and heat flux (*q*). Two aspects were mainly studied, namely the bubble breakup behaviors and two-phase evaporating heat transfer. The main conclusions and underlying mechanisms were as follows:

1. Bubble breakup behaviors were significantly affected by evaporation. The "breakup with tunnel" and "breakup with obstruction" modes respectively occurred at low with tunnel" and "breakup with obstruction" modes respectively occurred at low and high *q*. The bubble successively experienced long-period squeezing stage and short-period pinch-off stage during the breakup process, where the breakup rate under pin-off stage was much larger. Along with increase in *Re*, the bubble broke more rapidly, and the critical neck thickness tended to decrease. The influence of heat flux on the breakup was weak. The downstream fluid accelerated more obviously at smaller *Re* and higher *q*. The bubble annihilated the vortices existing within the divergence region and made the fluid flow more uniform.

2. The evaporating heat transfer was affected by bubble behaviors. Compared to the single-phase case, the heat transfer was drastically improved due to the evaporation under two-phase case. The most significant enhancement occurred at the leeward wall. The increase in *Re* promoted single-phase convective heat transfer while hindering the two-phase heat transfer. Slight negative enhancement of heat transfer existed at lower *q*. In addition, the phenomenon of heat transfer deterioration was observed at higher *q.* Generally, the heat transfer was enhanced as *q* was increased.

The present study not only helps understanding the physical mechanisms of bubble behaviors and heat transfer within microfluidic Y-junctions, but also informs the design of microfluidic devices.

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