

Article



# Symmetry Study on Damage Inversion of Wharf Pile Foundation in Three Gorges Reservoir Area Under Ship Impact

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**Abstract:** Periodic change in reservoir water level will have a significant impact on berthing position, and the impact caused by irregular operation during berthing will cause damage to wharf pile foundations. However, most of the existing monitoring methods adopt irregular methods, so it is difficult to accurately identify and analyze the damage causes. Taking a high-piled wharf in the Three Gorges Reservoir area as an example, the uncertainty of reservoir water level change is quantitatively analyzed. By establishing a simplified parametric wharf calculation model, the data set of an inversion model of pile of a high-piled wharf under ship impact is obtained, and the inversion analysis of pile damage of a high-piled wharf under ship pile is carried out based on the artificial neural network model. The results show that the inversion model can accurately and efficiently identify the intensity of ship impact, and a low water level is better than a high water level in the identification of impact position. In this paper, the behavior of wharf structure before and after damage is analyzed symmetrically under the action of damage inducement. In summary, the inversion analysis method can basically meet the requirements of inversion identification of pile foundation damage of a high-pile wharf in a backwater fluctuation area under ship impact.

**Keywords:** ship impact; Three Gorges Reservoir area; uncertain quantification; inversion analysis

## 1. Introduction

As show in the Figure 1, the fluctuation of water level in inland river reservoir ports is closely related to factors such as dispatching and upstream inflow, and the fluctuation of water level is larger than that in a plain port. Taking the Three Gorges Reservoir as an example, the dispatching water level varies by 30 m, and the maximum drop between flood level and low water level can reach more than 35 m. Different from other waters, the research on the symmetry of damage inducement inversion in the Three Gorges reservoir area is mainly aimed at the analysis of the symmetry results of pile foundation in different positions during the response process under the impact of ships.

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Figure 1. Three Gorges Reservoir area.

The berthing position and impact force affected by water flow in the berthing process of operating ships in the port area are closely related to the change in reservoir water level. Huang Qiujie [1] systematically simulated the movement law of water flow and sediment in the reach from Changshou to Luoqi and summarized the variation law of water level in the harbor basin. Zhao Tianhui [2] studied the prediction method of a high-piled wharf under ship impact by using a three-dimensional finite element analysis model. Liu Siqi et al. [3], in combination with time-varying reliability theory, carried out a dynamic analysis on the ship impact force of a high-piled wharf. Liu Xiaoxi et al. [4] applied the limit probability theory to analyze the load effect and carried out the failure probability and reliability index analysis of the horizontal bearing capacity of a high-piled wharf. Wang Jianchao et al. [5] used numerical analysis to analyze and calculate the high-piled wharf structure under ship impact.

In the research of pile foundation damage caused by ship impact, Ye Binbin [6] carried out the experimental study of barge impact on a single pile foundation model, explored the dynamic response and vulnerable area of a single pile foundation structure under impact load, and further studied the dynamic response characteristics of a pile foundation structure under the impact of an inland barge on a high-pile cap group pile foundation system by numerical simulation. Zhu Ruihu et al. [7] conducted a study on the dynamic response of piles with different bent positions through impact load tests and put forward a reinforcement scheme.

There is no relevant report on the inversion of pile foundation damage of a high-piled wharf in a fluctuating backwater area. In this paper, based on the hydrological statistical data of the Three Gorges Reservoir area, the uncertainty of water level variation in the waters where the wharf is located is quantitatively analyzed, and the parametric calculation model of the inland river overhead wharf is established. Based on the artificial neural network model, the inversion calculation of pile foundation damage of the high-piled wharf under the action of a ship pile foundation is carried out. The results show that this method has a good recognition effect on the strength and position of a ship pile foundation, which provides a certain reference for optimizing wharf design.

## 2. Uncertainty and Quantification of Ship Berthing

The uncertainty of ship berthing includes tonnage, size, berthing speed, berthing position, etc. In this paper, we focus on the magnitude and position of the berthing force of a wharf pile foundation.

#### 2.1. Quantification of Ship Tonnage Uncertainty

The probability distribution of deadweight tons of ships is mostly a multimodal distribution [8], and the commonly used multimodal distribution fitting models are the mixed Weibull [9] and the Gaussian mixture model (GMM) [10]. Taking GMM as an example, the single Gaussian probability density function can be expressed as follows [11]:

$$g(x, u, \sigma) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left[-\frac{(x-u)^2}{2\sigma^2}\right]$$
(1)

Taking the monthly statistical data of container transport vessels from January 1 to 31 December 2020 at Chongqing Orchard and Cuntan Container Terminals in the Three Gorges Reservoir area as samples [12], according to the iterative method based on the Gaussian mixture model, the probability density function is fitted, and the results are shown in Table 1.

Statistical Object	Gaussian Component	Weight	Average Value	Standard Deviation
	1	1 0.191 5.98   2 0.233 12.55   2 0.456 1.08	2.55	
Chin tonnogo	2	0.233	12.55	7.25
Ship tormage	3	0.456	1.98	0.89
	4	0.009	50.15	11.21

Table 1. Fitting of probability density function of ship tonnage.

It can be seen from the statistical results that the main types of container ships currently sailing in the Chongqing section of the Three Gorges Reservoir area are 3000 tons and 5000 tons, accounting for 44.28% and 23.09%, respectively, and the proportion of ships above 6000 tons is the smallest, only 6.81%. Considering that the damage cause determined in this study is that the structure bears the load under nonstandard operation conditions such as "barbaric berthing," the calculation benchmark in the calculation of ship berthing load is determined to be 6000 tons.

#### 2.2. Quantification of Ship Impact Position Uncertainty

Taking the water level observation data of Cuntan Hydrological Station in the Yangtze River from 1 January 2016 to 31 December 2020 as a sample, the statistical analysis of reservoir water level changes was carried out [13], and the five-year average water level was fitted by a polynomial to determine the characteristic water level calculated by structural analysis. The results are shown in Figure 2.



Figure 2. Fitting curve of average daily water level from 2016 to 2020.

The deterministic coefficient of fitting is  $R^2=0.8047$ , which shows that the polynomial fitting method can better fit the annual water level changes in the Three Gorges Reservoir area. The water level fitting polynomial can be obtained as follows:

$$y = -8e^{-11}D^4 - 2e^{-6}D^3 + 0.0012D^2 - 0.2081D + 175.3$$
 (2)

According to the analysis results, it is determined that the three representative water levels calculated by structural analysis are 145 m (low), 160 m (medium), and 175 m (high), respectively, which serve as the action points of unfavorable incentives such as ship berthing and bank slope sliding.

## 3. Establishment of Sample Data Set for Damage Inversion

For the neural network model, the input of the model plays a vital role in the prediction results of the model. When the number of input samples is small, it will cause the sample model to be under-fitted. The model can make a good prediction for the given data set, but it is not good for the new data set, which is obviously unfavorable for the identification of damage incentives. In order to get a good prediction result, a large number of data samples need to be collected.

The model is parameterized, and the solid element model is optimized into a beam element model. The finite element program is called by the Python program to carry out parametric calculation and data extraction of the model, and the stress data of pile groups are preprocessed and dimension-reduced.

## 3.1. Establishment of Parametric Model

The parametric model adopts beam theory, and this model adopts the Timoshenko beam theory to model. Assuming that the action of the bank slope is a horizontal thrust, the pile foundation is horizontally loaded under the action of the bank slope, so the elastic foundation beam method can be considered to simulate the pile-soil constraint of the beam element model. The riprap layer and foundation rock are assumed to be elastic bodies, and the pile is regarded as a beam on an elastic foundation. The model is shown in Figure 3.



Figure 3. Parametric dock model.

In order to distinguish different components in the subsequent calculation process, we numbered the load-bearing structure of the wharf: 1-11. The magnitude and longitudinal position of ship impact are applied according to the values determined above, and the specific position is shown in Figure 4.



Figure 4. Distribution of ship impact points.

#### 3.2. Data Collection and Sample Set Construction

The established beam element model db file is set as a callable model, the parameters under ship impact are extracted by random sampling, the parameters are loaded into a solution file (the solution file is an ANSYS command flow file, which contains commands for calling the finite element model, commands for all loads, commands for post-processing to extract stress, and macro files for exporting data), and the MANSYS module is called via subprocess to load the call model.

The solution file is loaded and calls the finite element model for calculation, collects data, and exports it. In order to meet the calculation requirements, 10,000 working condition data are randomly selected as samples.

Because the stress data of pile groups have different stress values and too large of a span and the neural network is very sensitive to the data set, the obtained data are normalized, so that all the data fall within the interval of [0,1].

The first two characteristics of each group of samples are taken as the horizontal axis and the vertical axis to draw the scatter diagram, as shown in Figure 5, which shows the original scatter diagram and normalized scatter diagram of pile foundation stress under ship collision.





(b) Normalized scatter plot

Figure 5. Stress scatter diagrams of pile foundation under ship impact.

After the pre-processing of pile group stress data, the data can be directly loaded into the inversion model for training.

However, direct training may result in too long of a training time for the model and flooding of dimensions due to the large sample size of the task, so the principal component analysis method is used to reduce the dimensions of the stress sample data, and the initial principal component number is adjusted according to the recognition effect of the inversion model. The result of dimension reduction is shown in Figure 6.



Figure 6. Scatter diagram of dimension reduction treatment of pile stress under ship impact.

The features obtained after normalization and dimension reduction of stress data are counted as sample features x, the number of rows of x is the number of samples, the number of columns is the number of features, the damage inducement action parameter y corresponding to the counted samples is the target vector, the number of rows of y is the number of samples, the number of columns is 3, y is expressed as [type number, position number, action intensity value], and the one-to-one correspondence between x and y is saved in matrix form [X,y], which is input into the inversion model as a data set for training.

#### 4. Establishment of Damage Inducement Inversion Model

In this paper, the inversion model of wharf damage inducement is built based on the Python language [14]. The main tools used are numpy library and sklearn library. numpy library is a scientific computing library of Python, which provides the function of matrix operation. Sklearn library is a third-party library for Python machine learning, which provides a simple integrated tool for machine learning. Our team has carried out relevant physical model tests and simulated the point where the ship collided. The test results have high reference value for the confirmation of input points in finite element calculation [15–19].

The modeling steps are as follows:

1) Collect stress characteristic data of finite element model pile groups under different working conditions.

2) Fuse and reconstruct the stress sample data; calculate the range, mean, variance, and discrete coefficient of the extracted stress features of each pile; and use the calculated results as a supplement to the sample features to construct a sample data set D, which contains features x and corresponding labels y, where  $X \in \text{Rm} \times n$ ,  $X \in \text{Rm} \times q$ , m is the number of samples, and n is the number of features.

3) Information fusion is carried out on the sample data set by the normalization method, and the first principal components,  $x_PCA \in RM \times a$ , are extracted.

4) The data set is randomly divided into a training set S and a test set T according to a ratio of 3:1 by adopting a set-aside method.

5) Construct the neural network full connection model ANN with three hidden layers. The model optimizer adopts adam algorithm, the activation function adopts {"identity," "logistic," "tanh," "relu"}, the damage function of classification learner in the output layer adopts cross entropy loss, the loss function of regression learner adopts the mean square error function, and the range of penalty factor  $\alpha$  is set (0.0001–10). Set the maximum iteration number and model convergence accuracy, set k-fold cross-validation, split the training set s and load it into the ANN model for self-adaptive training, train the classification problem and regression problem, respectively, and cross-validate the training to obtain the model score to evaluate the performance of the model. The performance metrics mainly adopt precision accuracy and average absolute error MAE, and the low score means the model is unreliable, so the next step of optimization and parameter adjustment is carried out. Parameter optimization is carried out through the Gridsearch toolkit, and the parameters searched include the optimal parameters of the model, such as the number of hidden layers of neural network, the number of hidden layer nodes, and penalty factors.

6) After training and verifying the training set S, load the test set T into the model to further evaluate the generalization ability of the model.

## 5. Inversion Analysis of Damage Inducement

#### 5.1. Artificial Neural Network Model Training

The sample data set is allocated according to the ratio of 75% of the training samples and 25% of the test samples. The location label of ship collision action is loaded into the classification learner for training, and the intensity label of ship collision action is loaded into the regression learner for training.

The grid search method is used to search for the optimal parameters, and the above key parameters are searched. The classification learner uses the precision index, and the regression learner uses the R2 index. The neural network model is verified by cross-validation. According to the set maximum iteration times and convergence error, each neural network model reaches the automatic stop of the convergence error model, and it is considered that the internal weight of the neural network model is optimal at this time. The optimized parameters of the neural network inversion model of ship impact obtained by grid search are shown in Table 2:

Demonster	Parameter				
Farameter	<b>Classification Learner</b>	<b>Regression Learner</b>			
Optimizer	Adam	Adam			
Hidden layer	2	2			
Number of hidden layer nodes	[50,30]	[100,50]			
Activate function	Relu	Identity			
Convergence error	0.001	0.001			
Penalty factor	0.01	0.2			
Maximum number of iterations	500	500			

Table 2. Optimal parameters of artificial neural network model.

#### 5.2. Damage Inversion Analysis Results

1) Ship impact location identification

Location recognition is a classification problem, and the classification learner uses cross entropy loss as the model loss index. It can be seen from Figure 7 that when the neural network model is iterated 160 times, the model converges.



Figure 7. Loss curve of classification learner.

In order to test the generalization ability of the model at each action position of injury inducement, the trained model is verified on the training set and the test set at different positions, and the specific indexes are shown in Table 3.

The accuracy in the table represents the correctness of the action position recognition result, and the closer it is to 1, the better it represents the result. F1 is based on the harmonic average of sample recall rate and precision rate, and the closer to 1, the better the result. Hamming loss is the distance between the predicted value and the true value of the sample, and the closer it is to 0, the smaller the result error.

	Training Data Set					Test Data Set			
Location	Sample Number	Precision	F1	Hamming	Sample Number	Precision	F1	Hamming	
1	FOC	0.05	0.040	0.040	1(0	0.800	0.000	0.1	
1	526	0.95	0.949	0.049	169	0.899	0.888	0.1	
2	493	0.937	0.933	0.063	166	0.903	0.901	0.096	
3	497	0.974	0.998	0.026	163	0.975	0.975	0.024	
4	534	0.949	0.95	0.051	159	0.905	0.91	0.0943	
5	473	0.858	0.832	0.141	165	0.8	0.815	0.211	
6	513	0.988	0.987	0.012	160	0.969	0.952	0.0312	
7	499	0.952	0.949	0.048	177	0.949	0.948	0.0508	
8	480	0.885	0.882	0.114	158	0.829	0.831	0.17	
9	487	0.944	0.94	0.055	176	0.937	0.925	0.0625	
10	478	0.971	0.969	0.029	166	0.957	0.955	0.032	
11	522	0.998	0.989	0.001	167	0.998	0.986	0.001	
12	530	0.999	0.989	0.01	179	0.969	0.971	0.0287	
13	507	0.999	0.995	0.011	179	0.98	0.985	0.015	
14	466	0.989	0.985	0	157	0.971	0.979	0.0215	
15	495	0.99	0.995	0.02	159	0.982	0.985	0.0122	
total	7500	0.942	0.942	0.057	2500	0.943	0.941	0.0576	

Table 3. Identification results of ship impact position.

It can be seen from Table 3 that the position recognition accuracy of the training set is mostly above 0.94, and the recognition accuracy of the test samples is also above 0.9, which indicates that the neural network model has strong generalization ability for ship collision and can correctly identify the position of ship collision inducement.

2) Identification of ship impact strength

The identification of ship impact strength is a regression problem, and the regression learner uses variance as the model loss index. As can be seen from Figure 8, when the neural network model is iterated 500 times, the loss error reaches about 0.001, at which time the model can be basically judged to converge.



Figure 8. Loss curve of regression learner.

The results of the training set and the test set of ship impact damage inducement are counted by position, and the performance index Table 4 of the model is obtained.

Location	Training Data Set			Test Data Set				
	Sample Number	R2	MSE	MAE	Sample Number	R2	MSE	MAE
1	526	0.997	33.476	4.601	169	0.997	37.917	5.016
2	493	0.996	46.082	5.394	166	0.996	43.113	5.132
3	497	0.997	40.894	5.006	163	0.997	39.684	5.019
4	534	0.997	41.190	5.240	159	0.996	43.729	5.351
5	473	0.996	51.385	5.789	165	0.995	66.184	6.395
6	513	0.997	39.907	4.901	160	0.997	38.344	4.964
7	499	0.997	40.407	5.077	177	0.996	56.719	5.907
8	480	0.996	47.118	5.448	158	0.996	44.238	5.165
9	487	0.996	53.087	5.900	176	0.996	49.533	5.739
10	478	0.994	71.079	6.999	166	0.994	76.648	7.475
11	522	0.997	35.147	4.738	167	0.998	34.737	4.732
12	530	0.997	43.386	5.276	179	0.996	54.646	6.054
13	507	0.997	39.084	5.051	179	0.996	46.148	5.428
14	466	0.997	38.028	4.971	157	0.997	39.069	5.063
15	495	0.997	39.171	5.022	159	0.997	43.802	5.331
total	7500	0.992	43.963	5.294	2500	0.996	47.781	5.527

Table 4. Identification results of ship impact strength.

R2 in Table 4 represents the fitting degree of the model to strength identification, and the closer it is to 1, the better it represents the model. MSE is the mean square error, which represents the expectation of the square error between the predicted value and the true value of intensity identification. The closer it is to 0, the higher the accuracy is. MAE is the mean absolute error, which reflects the actual situation of intensity prediction error.

The minimum value of the goodness-of-fit index R2 of training set and test set is 0.989, the mean square deviation is 30–70 kN, and the average absolute error is 3–7 kN, which is relatively small compared with the value of ship impact force. For comparison, the absolute error curve and relative error curve of test set are drawn, and 20 predicted samples are randomly selected for comparison with the set value, as shown in Figure 9.



(c) Comparison of predicted values of 20 random samples

10

Number of samples

12 14

Figure 9. Comparative analysis of settlement results.

It can be seen from Figure 9 that some samples in the test set have large errors, reaching about 20 kN, most of which are within 10 kN, and the average relative error is about 3%. The performance of the model is relatively excellent and can meet the demand of inversion analysis of the inducement of ship impact damage.

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#### 6. Conclusions

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Based on the wharf pile foundation in the high fill area of the Three Gorges Reservoir area, this paper carries out the back analysis of the damage inducement under the action of ship pile foundation, establishes the relevant data analysis model, and obtains a structural analysis conclusion suitable for similar engineering environments:

1) Based on the statistical data of ships operating in the Three Gorges Reservoir area and water level, through the quantitative analysis of uncertainty, using probability density function and polynomial fitting method, the analysis parameters of ship impact damage incentives in the fluctuating backwater area in the Three Gorges Reservoir area are obtained, which are 6000 tons in size and 145 m, 160 m, and 175 m in position.

2) The optimal parameters of the neural network model are searched by a grid search, the scores of the evaluation indexes of the model are cross-verified, and the inducement of ship collision damage is analyzed. After analysis, the location recognition accuracy of ship collision is 0.94, and the average absolute error of size recognition is 5.5 kN. The inversion model has a very good generalization ability for ship collision injury inducement samples.

3) The finite element simplified analysis model is established, and the MANSYS module is called by Python's subprocess module for analysis, which proves the feasibility of batch calculation of pile foundation stress in the complex structure of the overhead vertical high-pile wharf. By comparing the stress characteristics with the solid element model, the calculation results of the simplified analysis model are verified to be correct, so that the sample space for inversion analysis can be obtained by using the simplified model calculation results.

4) After analysis, compared with the strength and position of the ship's pile foundation, the pile foundation of the inland river overhead high-pile wharf is more sensitive to the strength and the position of the pile foundation at low water level. Therefore, in the process of wharf pile foundation design and health inspection, attention should be paid to the structural state under the conditions of large tonnage and low water level.

In recent years, the Laboratory of Complex Systems and Computational Intelligence of Taiyuan University of Science and Technology [20–29] has done a lot of research on data storage and modeling methods and has obtained a series of research results, among which the new modeling technology mentioned provides reference data for better solving the problem of damage inducement inversion model in this paper. In the follow-up research, we will further optimize the modeling method and deepen the related research of this paper.

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