



# *Article* **Characteristics of Precipitation of Rare Earth Elements with Various Precipitants**

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**Abstract:** The effective and selective leaching of rare earth elements (REEs) from various sources is frequently possible in practice by adopting a carefully coordinated strategy incorporating a selective precipitation of these elements from undesired ones in solution. In this study, the behavior of chemical precipitation of REEs with commonly used precipitants such as sulfate, carbonate, fluoride, phosphate, and oxalate was examined using thermodynamic principles and calculations. It was found that the pH of the system has a profound effect on determining particular chemical species of precipitants, which are subsequently responsible for the precipitation of REEs. The role of various anions such as Cl<sup>−</sup>, NO<sub>3</sub><sup>−</sup>, and SO<sub>4</sub><sup>2−</sup> derived from the acid used in the leaching process on the precipitation behavior of REEs was examined. These anions form complexes with REEs and display a very positive effect on the precipitation behavior. The nitrate environment exhibits most conducive to precipitation followed by sulfate and then chloride.

**Keywords:** precipitation; leaching; complexation; anion effect; equilibrium calculation; rare earth elements

## **1. Introduction**

Rare earth elements (REEs) are becoming very important in modern society. REEs are essential ingredients in the transition to green technology and there have been numerous recent articles describing their extraction processes from various sources [\[1](#page-11-0)[,2\]](#page-11-1).

Most rare earth bearing minerals are refractory in nature and therefore, a pretreatment or strong acid treatment of ores bearing these minerals is usually necessary [\[3–](#page-11-2)[6\]](#page-11-3) before leaching is affected. Such pretreated ores are then subjected to the leaching process of REEs. The leach liquor is frequently subjected to the removal of impurities such as iron, calcium, uranium, and thorium by going through stage-wise precipitation using various compounds such as hydroxide, carbonate, sulfate, and oxalate [\[7–](#page-11-4)[13\]](#page-11-5). After the removal of these impurities by chemical precipitation, REEs in solution are then subjected to precipitation using various precipitants, which in general takes place at pH above 3−4, since most of these impurities are precipitated at around these pHs. However, during the precipitation of impurities, some REEs are also removed from the solution by coprecipitation or adsorption. Therefore, it is desirable to precipitate REEs before removal of the impurities. It is the hope of this study to identify the precipitants and chemical conditions to achieve this objective.

The chemical complexity of the aqueous medium introduced by various chemical treatment of leach liquor has introduced a complex nature to the system making the analysis of the subsequent chemical precipitation a challenge. In addition to metal ions in the leach liquor extracted from ores, many anions such as  $Cl^-$ , NO<sub>3</sub><sup>-</sup>, and SO<sub>4</sub><sup>2-</sup> mostly derived from acids used in the leaching operation also play an important role in leaching as well as precipitation.

The effect of various anions on the leaching behavior has been discussed in earlier studies [\[14](#page-11-6)[,15\]](#page-12-0). For example, the leaching of Re-phosphate in the presence of sulfuric acid can be simply described by Equation (1). (It is noted that Re is the elemental symbol for rhenium. However, Re(III) refers to only REE(III) in this paper.)

$$
\langle \text{RePO}_4 \rangle + \{H_2 \text{SO}_4\} = \{ \text{Re}^{3+} \} + \{ \text{PO}_4^{3-} \} + \{ \text{SO}_4^{2-} \} + 2 \{ H^+ \}
$$
 (1)

Here the symbols, < > and { } stand for solid and liquid form, respectively. The oxidation state of REEs in solution and solids is assumed to be Re(III) throughout this presentation. It should be noted however, that some REEs can be oxidized to Re(IV) or reduced to Re(II) in aqueous media in very rare cases [\[16\]](#page-12-1). The concentration of the free REEs at equilibrium can be estimated if the concentration of all species involved in Equation (1) is known. However, such calculated values are far from real values since the chemicals produced from the leaching process undergo hydrolysis and complexation [\[14](#page-11-6)[,15\]](#page-12-0). As a result, the correct evaluation of the product concentration requires a very complicated process involving calculations of equilibrium equations simultaneously in some cases.

The chemical precipitation of REEs is similarly complicated. For example, a simple chemical precipitation of a free Re-ion,  $\text{Re}^{3+}$  with phosphate ion,  $\text{PO}_4^{3-}$  can be given by Equation (2).

$$
\{Re^{3+}\} + \{PO_4^{3-}\} = \langle RePO_4 \rangle \tag{2}
$$

It should be noted that REEs precipitate with the phosphate ion as a free Re-ion,  $\text{Re}^{3+}$  at relatively high pHs such as 4 and 6. However, when the pH of the solution changes to a lower value, for example 1 or 2, by adding acids of HCl, HNO<sub>3</sub>, or H<sub>2</sub>SO<sub>4</sub>, the anions such as Cl<sup>−</sup>, NO<sub>3</sub><sup>-</sup>, and SO<sub>4</sub><sup>2-</sup> will form various complexes with REEs [\[3,](#page-11-2)[14,](#page-11-6)[15\]](#page-12-0), and then these complexes are subjected to precipitation. For example, in the presence of sulfate ions, there will be at least  $Re^{3+}$ ,  $Re(SO_4)^+$ ,  $Re(SO_4)_2^-$ , and  $Re_2(SO_4)_3$ , present in solution, and for most of the sulfate concentration,  $Re(SO_4)_2$ <sup>-</sup> is the predominant species when the concentration of sulfate ions is especially more than  $0.1$  M [\[14,](#page-11-6)[15\]](#page-12-0). As a result, in such cases,  $Re(SO_4)_2$ <sup>-</sup> should be used instead of the free ion and the resulting concentration of rare earth elements after precipitation is an order of magnitude different from when the free ion is used.

<span id="page-1-0"></span>In addition, the phosphate ion also may not exist depending upon the pH of the system. It should be noted that the values of pKa are 2.0 for  $H_3PO_4/H_2PO_4^-$ , 7.2 for  $H_2PO_4^-/HPO_4^{2-}$ , and 12.0 for  $HPO<sub>4</sub><sup>2</sup>–/PO<sub>4</sub><sup>3–</sup>$  (see Table [1\)](#page-1-0) [\[17\]](#page-12-2). This means that  $H<sub>3</sub>PO<sub>4</sub>$  should be used instead of the phosphate ion in Equation (2) for the system whose pH lies below 2 and likewise,  $H_2PO_4$ <sup>-</sup> for pH between 2 and 7.2 and so on.

Precipitants	pKa		
$H_3PO_4/H_2PO_4^-$	2.1		
$H_2PO_4^-/HPO_4^2^-$	7.2		
$HPO42–/PO43–$	12.0		
$H_2CO_3/HCO_3^-$	6.38		
$HCO3-/CO32-$	10.34		
$HF/F^-$	3.0		
$H_2C_2O_4/HC_2O_4^-$	1.0		
$HC_2O_4^-/C_2O_4^2^-$	4.2		
$HSO_4^-/SO_4^2^-$	2.0		

**Table 1.** The pKa values for various precipitants [\[17\]](#page-12-2).

In this paper, factors such as pH, complexation, and hydration of precipitants affecting the chemical precipitation with various precipitants will be examined and their practical implication in the analysis of such precipitation processes will be discussed. The precipitation behavior of REEs with carbonate, fluoride, phosphate, sulfate, and oxalate was considered in this study, since these precipitants are most widely used in precipitation of REEs in practice.

## **2. Acquisition of Thermodynamic Information**

Table [1](#page-1-0) presents the values of pKa for the precipitants considered in this study. It should be noted that there are some variations in the numerical values of pKa based on various literature sources. For example, the values for oxalic acid given by Pourbaix [\[17\]](#page-12-2) and Dean [\[18\]](#page-12-3) are different from those by HSC [\[19\]](#page-12-4) and Wagman [\[20\]](#page-12-5). However, the effect of such differences on the final outcome of the behavior of chemical precipitation is not very significant.

The thermodynamic data used in this study are listed in Table [2.](#page-2-0) Most data given in the table were taken from the literature information [\[21](#page-12-6)[–26\]](#page-12-7) and those unavailable were estimated using the parallel plot method as described earlier [\[14\]](#page-11-6).

	Carbonate	Phosphate	Sulfate	Fluoride	Oxalate	Oct-Sulfate
La	$-768.5$	$-455.3$	$-892.6$	$-399.8$	$-872.2$	$-1399.9$
Ce	$-761.4$	$-455.2$	$-884.7$	$-396.8$	$-868.3$	$-1340.2$
Pr	$-764.5$	$-451.0$	$-879.4$	$-394.2$	$-860.6$	$-1343.5$
Nd	$-761.6$	$-448.7$	$-877.2$	$-391.5$	$-861.8$	$-1335.0$
<b>Sm</b>	$-759.6$	$-447.6$	$-878.8$	$-392.3$	$-860.1$	$-1330.5$
Eu	$-759.4$	$-446.7$	$-875.3$	$-391.0$	$-859.1$	$-1275.3$
Gd	$-758.6$	$-445.5$	$-874.2$	$-390.5$	$-857.7$	$-1328.1$
Tb	$-757.0$	$-444.7$	$-873.7$	$-388.7$	$-856.9$	$-1313.2$
Dy	$-750.6$	$-442.2$	$-868.9$	$-385.9$	$-856.0$	$-1323.3$
Ho	$-744.2$	$-440.4$	$-861.3$	$-383.0$	$-849.6$	$-1314.3$
Er	$-743.9$	$-439.1$	$-855.9$	$-380.9$	$-842.0$	$-1309.5$
T <sub>m</sub>	$-736.9$	$-438.2$	$-862.9$	$-379.6$	$-846.6$	$-1308.1$
Yb	$-735.5$	$-437.6$	$-861.5$	$-378.4$	$-839.5$	$-1293.4$
Lu	$-734.5$	$-435.7$	$-860.1$	$-376.8$	$-841.3$	$-1319.1$
Y	$-749.9$	$-443.0$	$-866.8$	$-389.4$	$-851.5$	$-1320.6$
<b>Sc</b>	$-714.9$	$-418.2$	$-845.1$	$-361.5$	$-828.4$	$-1300.0$

<span id="page-2-0"></span>**Table 2.** The Gibbs standard free energy formation of various compounds in kCal/mol. Information taken from [\[14,](#page-11-6)[15\]](#page-12-0) with some modifications.



Some of the standard Gibbs free energy formation values, such as Y- and Sc-oxalates were not available in the literature and, therefore, were estimated using the parallel method as described by earlier studies [\[14,](#page-11-6)[15\]](#page-12-0). It should be noted that there were typographical errors in the values for Re-octa-hydrated sulfates in earlier publications [\[14,](#page-11-6)[15\]](#page-12-0). It should also be noted that subsequent relevant calculations in the same articles were carried out using correct values, however.

#### **3. Carbonate System**

It is well known that rare earth elements are readily precipitated with carbonate at high pHs. Rare earth elements are readily subjected to precipitation with carbonate [\[27](#page-12-8)[,28\]](#page-12-9) especially at high pHs. Re-carbonates are ideal precipitates, since carbonates are readily available, relatively less expensive than other precipitants, and precipitates can be easily dissolved in a mild acid for further treatments of REEs in subsequent processes of purification. However, it is not easily precipitated in acidic media. As a result, the leach liquor is usually subjected to a neutralization step before the precipitation of REEs with carbonate is affected. During the neutralization process, however, impurities such as  $Fe^{3+}$ ,  $Ca<sup>2+</sup>$  are precipitated first resulting in loss of REEs due to adsorption and coprecipitation of REEs with oxides or sulfates of impurities.

A simple stoichiometric equation describing the precipitation of REEs with carbonate can be written in Equation (3), which is analogous to Equation (2).

$$
2\{\text{Re}^{3+}\} + 3\{\text{CO}_3{}^{2-}\} = \text{Re}_2(\text{CO}_3)_3 \tag{3}
$$

As discussed earlier, the concentration of  $CO<sub>3</sub><sup>2-</sup>$  at pH 1–6 that was considered in this study, which is consistent with the range of pH practiced in industry, is practically zero, since the pK value for  $HCO<sub>3</sub><sup>-</sup>/CO<sub>3</sub><sup>2-</sup>$  is 10.34. The stable species at pH less than 6, is  $H<sub>2</sub>CO<sub>3</sub>$ , which is the dominant species as seen in Table [1](#page-1-0) and, therefore,  $H_2CO_3$  should be used in Equation (3). Furthermore, when pH of the solution is less than 6,  $\text{Re}^{3+}$  is subjected to complexation to become either  $\text{ReCl}^{2+}$ ,  $\text{Re}(\text{NO}_3)^{2+}$ , or  $Re(SO_4)_2$ <sup>-</sup> depending upon the kind of acid used [\[14,](#page-11-6)[15\]](#page-12-0). Therefore, for the working pH range (pH 1–6) in this study, Equations (4)–(6) should be used for chloride, nitrate, and sulfate systems instead of Equation (3).

$$
2 \{ReCl^{2+}\} + 3 \{H_2CO_3\} = \langle Re_2(CO_3)_3 \rangle + 2 \{Cl^-\} + 6 \{H^+\}\
$$
 (4)

$$
2 \{ \text{Re}(\text{NO}_3)^{2+} \} + 3 \{ \text{H}_2 \text{CO}_3 \} = \langle \text{Re}_2(\text{CO}_3)_3 \rangle + 2 \{ \text{NO}_3^- \} + 6 \{ \text{H}^+ \} \tag{5}
$$

$$
2 \{ \text{Re(SO4)}_2 \} + 3 \{ \text{H}_2 \text{CO}_3 \} = \langle \text{Re}_2(\text{CO}_3)_3 \rangle + 4 \{ \text{SO}_4^2 \} + 6 \{ \text{H}^+ \} \tag{6}
$$

In order to illustrate the steps involved in calculating the equilibrium concentration of REEs in solution, let us take Equation (4) as an example. The equilibrium constant for Equation (4),  $K_{eq}$  can be found knowing the Gibbs standard free energy formation of each component involved in the reaction. Such found equilibrium constant is given in Equation (7) below:

$$
K_{eq} = \frac{\{Cl^{-}\}^2 \{H^{+}\}^6}{\{ReCl^{2+}\}^2 \{H_2CO_3\}^3}
$$
\n(7)

Here  ${H^+}$  is known if the pH of the system is known,  ${Cl^-}$  is known since the pH of the system is adjusted by HCl in this reaction, (see Table [3\)](#page-3-0) and  ${H_2CO_3}$  was set as  $10^{-4}$  M. Therefore,  ${[ReCl^{2+}}$  can be determined.

It should be noted that Equation (6) is valid above pH 2 but  $\mathrm{SO_4}^{2-}$  should be replaced by  $\mathrm{HSO_4}^-$ when the pH of the system is less than 2 (See Table [3\)](#page-3-0). When Equations (4)–(6) are solved to calculate the equilibrium concentrations of REEs in solution, it was assumed that the final concentrations of Cl−,  $NO<sub>3</sub><sup>-</sup>$ , and  $SO<sub>4</sub><sup>2-</sup>$  are those set by respective acid concentration to adjust the pH of the solution as discussed above. This assumption is reasonable for low pHs but the accurate estimation of the final equilibrium concentrations of REEs at pH 6 should be carried out taking into account all of practical conditions of the system.

It should also be noted that most of precipitants considered here are mostly weak acids and, therefore, they contribute in setting the pH of the solution (see Table [4\)](#page-4-0). This can be a cause of inaccuracy in the final results especially at relatively high pHs, say pH greater than 4. The correction of such effects can be made but no attempt on such corrections was made in this study. This is because the objective of the study is to observe the precipitation behavior at low pHs.

<span id="page-3-0"></span>**Table 3.** Concentrations of various anions used in the study at different pH's [\[17\]](#page-12-2).

	HC <sub>1</sub>	HNO <sub>3</sub>		$H_2SO_4$
pH	$Cl^{-}(M)$	$NO_3^- (M)$	$SO_4^{2-}(M)$	$HSO4- (M)$
6	$1.0 \times 10^{-6}$	$1.0 \times 10^{-6}$	$1.0 \times 10^{-6}$	$9.9 \times 10^{-11}$
5	$1.0 \times 10^{-5}$	$1.0 \times 10^{-5}$	$1.0 \times 10^{-5}$	$9.9 \times 10^{-9}$
4	$1.0 \times 10^{-4}$	$1.0 \times 10^{-4}$	$9.9 \times 10^{-5}$	$9.9 \times 10^{-7}$
3	$1.0 \times 10^{-3}$	$1.0 \times 10^{-3}$	$9.1 \times 10^{-4}$	$9.0 \times 10^{-5}$
2	$1.0 \times 10^{-2}$	$1.0 \times 10^{-2}$	$5.0 \times 10^{-3}$	$5.0 \times 10^{-3}$
1	$1.0 \times 10^{-1}$	$1.0 \times 10^{-1}$	$9.0 \times 10^{-3}$	$9.1 \times 10^{-2}$
$\Omega$	1.0	1.0	$1.0 \times 10^{-2}$	$9.9 \times 10^{-1}$

<span id="page-4-0"></span>

Concentration, M.	$H_3PO_4$ HF		$H_2CO3$	$H_2C_2O_4$
$1.0 \times 10^{-6}$	5.97	6	6.31	h
$1.0 \times 10^{-4}$	4	4.05	5.2	
$1.0 \times 10^{-3}$	3	3.26	4.69	3
$1.0 \times 10^{-2}$	2.3	2.64	4.18	2.09
$1.0 \times 10^{-1}$	1.63	2.1	3.68	1.31

**Table 4.** The pH values of some weak acids for various concentrations.

It is important to note that any calculated value exceeding the highest concentration of REEs in practice should be treated with caution. The highest concentration of REEs possible in the aqueous system is based on the grade of REEs in the ore being leached. Assuming the highest grade of REEs of the ore being treated is 50%, the highest concentration of REEs possible in the aqueous media could be about 1.5 M [\[15\]](#page-12-0). It is safe to assume that when the calculated value is more than 1−2 M, the precipitation is impossible under the conditions considered. On the other hand, when the calculated value is less than the target value, 1 ppm, then the precipitation could be favorable. ny calculated value exceeding the h

Figure [1](#page-4-1) presents the equilibrium concentration of dissolved REEs in solution when REEs are subjected to precipitation with carbonate. In this study, the concentration of the precipitant, was kept constant at  $10^{-4}$  M throughout the paper as stated earlier. The choice of the precipitant concentration being 10<sup>-4</sup> M, which is the final concentration after the precipitation is completed, is arbitrary and deemed reasonable in view of practical application. The horizontal dashed line across the figure represents the concentration of REEs in solution being  $3 \times 10^{-6}$  M, which is about 1 ppm of REEs. This is an arbitrary concentration representing an acceptable target level of precipitation of REEs after subjecting to the carbonate precipitation. ca to presphasion with carbonate. In this study, the concentration of the precipitant, w and surface complexes is significantly better than free REE in free REE is significantly behavior by Eu seems

<span id="page-4-1"></span>

Figure 1. Concentrations of (a)  $\text{Re}^{3+}$ , (b)  $\text{ReCl}_2^+$ , (c)  $\text{Re}(\text{NO}_3)_2^+$ , and (d)  $\text{Re}(\text{SO}_4)_2^-$  in equilibrium with carbonate precipitate with  $\frac{1}{2}$  of total concentration of concentration at  $\frac{1}{2}$ , and 1.  $\frac{1}{2}$ , and 1.  $\frac{1}{2}$ , and 1.  $\frac{1}{2}$ carbonate precipitate with  $10^{-4}$  M of total concentration of carbonate in solution at pH 6, 4, 2, and 1. Cr.concentration: 1 ppm line as a target concentration.

It is a reasonable assumption that the initial concentration of REEs in the leach liquor would be in the range of 3 × 10<sup>-1</sup> to 3 × 10<sup>-3</sup> M [\[15\]](#page-12-0). It is a usual practice that the initial concentration of the

precipitant is a little more than the stoichiometric amount. It is obvious that carbonate is incapable of precipitating most of REEs, except a few light REEs at pH 6. It is interesting to note that the precipitation of nitrate and sulfate complexes is significantly better than free REE ions. The anomaly behavior by Eu seems to be due to inaccuracy in the standard Gibbs free energy data given in the literature.

## **4. Fluoride System**

It has been well understood that fluoride readily complexes with rare earth elements [\[6,](#page-11-3)[29\]](#page-12-10). The pKa value of HF/F<sup>−</sup> is 3 as seen in Table [1](#page-1-0) and, therefore, the relevant equations governing the precipitation of REEs with fluoride should be formulated in such a way that HF is the precipitant at pH less than 3 and F<sup>-</sup> should be used at higher pHs. For example, the precipitation of ReCl<sub>2</sub><sup>+</sup> with fluoride is described by Equation (8) when the pH of the solution is 6 or 4, while Equation (9) is for pH 2 and 1. Here too, the concentration of the precipitant is assumed to be 10<sup>-4</sup> M. The precipitation of the complexed REEs is remarkable as in the case with the carbonate system. Most of REEs is easily complexed with chloride, nitrate, and sulfate as long as the concentration of these anions is more than 3 and F 0.1 M, below which they remain as  $Re^{3+}$  [\[14,](#page-11-6)[15\]](#page-12-0). ked while enorget, fillule, and burnie as long as the concentration of these antons is file

of the complexed REEs is remarkable as in the case with the case with the case with the case  $\mathbb{R}$ 

$$
\{Re^{3+}\} + 3\{F^-\} = \langle ReF_3 \rangle \tag{8}
$$

$$
{Re3+} + 3 {HF} =  + 3 {H+}9
$$
 (9)

Figure [2a](#page-5-0)–d present the precipitation of  $Re^{3+}$ ,  $ReCl_2^+$ ,  $Re(NO_3)_2^-$ , and  $Re(SO_4)_2^-$  with fluoride, respectively. With regard to Figure [2a](#page-5-0), there appears to be only one line representing pH 6 and 4. This is because when pH is above 3, F<sup>−</sup> is responsible for the precipitation reaction as seen in Equation This is because when  $\beta$  is above  $\beta$ . The respectively for the presiphent reaction as seen in Equation (7), in which the precipitation becomes independent of  $pH$ . As seen in these figures, fluoride is a more powerful precipitant for REEs than carbonate in the pH range considered in this study.  $\eta$  increase  $\eta$  is above 3,  $\eta$  is above 3,  $\eta$  is responsible for the precipitation reaction  $\eta$ 

<span id="page-5-0"></span>

Figure 2. Concentrations of (a)  $\text{Re}^{3+}$ , (b)  $\text{ReCl}_2^+$ , (c)  $\text{Re}(\text{NO}_3)_2^+$ , and (d)  $\text{Re}(\text{SO}_4)_2^-$  in equilibrium fluoride precipitate with 10−4 M of total concentration of fluoride in solution at pH 6, 4, 2, and 1. Cr. and 1 with fluoride precipitate with 10<sup>−4</sup> M of total concentration of fluoride in solution at pH 6, 4, 2, and 1. Cr. Concentration: 1 ppm line as a target concentration.

#### **5. Phosphate System**

When phosphoric acid,  $H_3PO_4$  is placed in water, it dissociates into dihydrogen phosphate, H<sub>2</sub>(PO<sub>4</sub>)<sup>−</sup>, hydrogen phosphate, H(PO<sub>4</sub>)<sup>2−</sup>, or phosphate ion, PO<sub>4</sub><sup>3−</sup> depending upon the pH of the solution. The pKa values of these conjugated species are 2.1 for  $H_3PO_4/H_2PO_4^-$ , 7.2 for  $H_2PO_4^-$ /HPO<sub>4</sub><sup>2-</sup>, and 12.0 for  $\text{HPO}_4^2$ <sup>-</sup>/PO<sub>4</sub><sup>3-</sup> as noted in Table [1.](#page-1-0) Therefore, the relevant equilibrium equations for the precipitation of REEs with phosphate should involve phosphoric acid for pH 1 and 2, and dihydrogen phosphate for pH 4 and 6. These are shown in Equations (10) and (11), respectively, for precipitation of  $ReCl<sub>2</sub><sup>+</sup>.$  $P_{\text{1}}$  for HPO43−2.0 for these are shown in Equations (10) and (11), respectively, for precipitations for the relevant equations for the relevant equations for the relevant equations for the relevant equations for the  $p$ <sup>2</sup>

$$
{\rm \{ReCl_2}^+ \} + {\rm H_2PO_4}^- = {<\rm RePO_4>} + 2{Cl^-} + 2{H^+}
$$
\n(10)

$$
{\rm \{ReCl_2}^+ \} + {\rm \{H_3PO_4\}} = {\rm \langle RePO_4 \rangle + 2{Cl^-} + 3{H^+}\}
$$
 (11)

Figure [3](#page-6-0) illustrates the precipitation of  $\text{Re}^{3+}$ ,  $\text{ReCl}_2{}^+$ ,  $\text{Re}(\text{NO}_3)_2{}^-$  and  $\text{Re}(\text{SO}_4)_2{}^-$  with phosphate. Unlike the carbonate but similar to fluoride systems, the phosphate system shows a powerful  $\,$ precipitation behavior even for free REEs. REEs are readily precipitated for all forms of rare earth element ions in solution except Re-chloride complexes. Here again, the unusual behavior shown by europium is most likely due to erratic thermodynamic data given in the literature. It should be noted that industrially important REE-bearing minerals are monazite and xenotime, both of which are phosphate compounds. Chemical interaction between REEs and phosphate has been investigated in numerous studies [30,31].

<span id="page-6-0"></span>

**Figure 3.** Concentrations of (a)  $Re^{3+}$ , (b)  $ReCl_2^+$ , (c)  $Re(NO_3)_2^+$ , and (d)  $Re(SO_4)_2^-$  in equilibrium with phosphate precipitate with 10<sup>−4</sup> M of total concentration of phosphate in solution at pH 6, 4, 2, and 1. Cr. Concentration: 1 ppm line as a target concentration. Cr. Concentration: 1 ppm line as a target concentration.

#### **6. Sulfate System** *Minerals* **2020**, *10*, 178 8 of 14

## $6.1. \text{ Sulfate } (SO_4{}^{2-})$

The precipitation of REEs with sulfate is given in Figure [4.](#page-7-0) In Figure [4a](#page-7-0), the concentration of free *6.1. Sulfate (SO42−)*   $REEs$  in solution in equilibrium with  $Re$ -sulfate precipitates is shown. In the construction of this figure,  $\,$ Equations (12) and (13) were used. Equation (12) was used for pH 6 and 4, while Equation (13) was used for pH 2 and 1. As mentioned earlier, the concentration of precipitants was kept constant at 10<sup>-4</sup> M. At pH 6, the concentration of sulfate ion is 10<sup>-4</sup> M plus 10<sup>-6</sup> M, in which the first was added by the rule and the latter was from sulfuric acid to adjust the pH. In addition, at pH 4, on the other hand, the concentration of sulfate ion is  $2 \times 10^{-4}$  M, because of the added sulfate plus sulfate provided by sulfuric acid to adjust the pH of the solution. The same is also applicable for Figure [4d](#page-7-0), in which case, Equations (14) and (15) were used instead of Equations (12) and (13).

(14) and (15) and (16) were used instead of Equations (12) and (16).<br>It is noted that the precipitation is better at low pHs, namely pH 2 and 1, compared to those at pH 6 and 4. The reason for this is because there is more sulfate present at low pHs due to the supply of 6 and 4. The reason for this is because there is more sulfate present at low pHs due to the supply of sulfate via sulfuric acid to adjust the pH of the solution. sulfate via sulfuric acid to adjust the pH of the solution. It is noted that the precipitation is better at low pHs, namely pH 2 and 1, compared to those at  $p\to\infty$ 

$$
2\{\text{Re}^{3+}\} + 3\{\text{SO}_4{}^{2-}\} = \langle \text{Re}_2(\text{SO}_4)_3 \rangle \tag{12}
$$

$$
2 \{ \text{Re}(\text{SO}_4)_2 \} = \langle \text{Re}_2(\text{SO}_4)_3 \rangle + \{ \text{SO}_4^2 \} \tag{13}
$$

$$
2 \{ \text{Re(SO4)}_2 \} = \langle \text{Re}_2(\text{SO}_4)_3 \rangle + \{ \text{SO}_4^2 \} \tag{14}
$$

$$
2\left\{Re(SO_4)_2^-\right\} + \left\{H^+\right\} = \langle Re_2(SO_4)_3 \rangle + \left\{HSO_4^-\right\} \tag{15}
$$

<span id="page-7-0"></span>

Figure 4. Concentrations of (a)  $\text{Re}^{3+}$ , (b)  $\text{ReCl}_2^+$ , (c)  $\text{Re}(\text{NO}_3)_2^+$ , and (d)  $\text{Re}(\text{SO}_4)_2^-$  in equilibrium with sulfate precipitate with 10<sup>−4</sup> M of total concentration of sulfate in solution at pH 6, 4, 2, and 1. **Cr. Concentration:** 1 ppm line as a target concentration. Additional sulfate is provided by sulfuric acid in (**a**) and (**d**).

(**c**)(**d**)

For the precipitation of  $\text{Re}(\text{SO}_4)_2$ <sup>-</sup> using sulfate, the precipitation calculations were done using Equations (14) and (15). The precipitation of Re(SO<sub>4</sub>)<sub>2</sub><sup>-</sup> with sulfate is unusual in that the species does not need any precipitant but it has to release one sulfate or bisulfate to form the precipitate <Re $_2({\rm SO}_4)_3$ > as seen in Equations (14) and (15). Such precipitation can be referred to as a decomposition precipitation.

It should be noted that in practice, REEs are usually precipitated with double salt sulfate [\[5](#page-11-7)[,32\]](#page-12-13), since the precipitation is more effective with double sodium sulfate. However, in this study, precipitation of REEs with only sulfate was carried out. Although double salt sulfate precipitation is more powerful than  $REES$ simple sulfate precipitation, the precipitation behavior of the two systems is expected to be very similar.  $\frac{1}{2}$  is more than  $\frac{1}{2}$  more effective with double solid sulfate. Precipitation is more power.

## 6.2. Octa-Hydrated Sulfate (SO<sub>4</sub>·8H<sub>2</sub>O)

The chemical precipitation of REEs with sulfate to form octa-hydrated sulfate is very similar to the precipitation behavior of sulfate. The relevant equations used in this analysis are given in<br>Exections (16) (10) Equations (16)–(19).  $p_{\text{max}}$  (10) (12).

$$
2 \{Re^{3+}\} + 3 \{SO_4{}^{2-}\} + 8 \{H_2O\} = \langle Re_2(SO_4)_3 \cdot 8H_2O \rangle \tag{16}
$$

$$
2 \{Re^{3+}\} + 3 \{HSO_4^-\} + 8 \{H_2O\} = \langle Re_2(SO_4)_3 \cdot 8H_2O \rangle + 3 \{H^+\}\
$$
 (17)

$$
2\left\{Re(SO_4)_2\right\} + 8\left\{H_2O\right\} = \langle Re_2(SO_4)_3 \cdot 8H_2O \rangle + \left\{SO_4^{2-}\right\} \tag{18}
$$

$$
2 \{ \text{Re}(SO_4)_2 \} + \{ H^+ \} + 8 \{ H_2 O \} = \langle \text{Re}_2(SO_4)_3 \cdot 8H_2 O \rangle + \{ \text{HSO}_4 \} \tag{19}
$$

As in the case with the sulfate system, the appearance of sulfate or bisulfate is based on the pH of the  $s$ olution. In other words, when the pH of the system is greater than 2, sulfate is the predominant species and at low pHs, bisulfate should be used as shown in Table [3.](#page-3-0) It was expected that the octa-hydrated system is favored in the chemical precipitation compared to simple sulfate precipitation [\[14,](#page-11-6)[15\]](#page-12-0). However, the results shown in Figure [4;](#page-7-0) Figure 5 sh[ow](#page-8-0) that the two systems behave very similarly.

<span id="page-8-0"></span>

**Figure 5.** Concentrations of (a)  $Re^{3+}$ , (b)  $ReCl_2^+$ , (c)  $Re(NO_3)_2^+$ , and (d)  $Re(SO_4)_2^-$  in equilibrium with octa-hydrated sulfate precipitate with 10−<sup>4</sup> M of total concentration of sulfate in solution at pH 6, 4, 2, and 1. Cr. Concentration: 1 ppm line as a target concentration. Additional sulfate is provided by sulfuric acid in (**a**) and (**d**).

#### **7. Oxalic Acid** sulfuric acid in (**a**) and (**d**).

Oxalic acid is the most commonly used precipitant for REEs from solution and the majority of **7. Oxalic Acid**  investigators have used this precipitant to separate REEs in the solution from other dissolved ions. This is because oxalic acid has in general a very favorable affinity with REEs in general [4[,6,](#page-11-3)[9](#page-11-9)[,13\]](#page-11-5). As seen in Table [1,](#page-1-0) the pKa values are 1 and 4.2 for  $H_2C_2O_4/HC_2O_4^-$  and  $HC_2O_4^-/C_2O_4^2^-$ , respectively. As a result, the relevant equations to be used to solve the equilibrium concentrations of REEs in solution after precipitation are Equations (20) and (21) for pH 6 and 4, and Equation (22) for pH 2 and 1, respectively. practice precise precisely and  $(21)$  for pH 6 and 4, and Equation  $(22)$  for pH 2 and 1, respect

$$
2\left\{Re(SO_4)_2\right\} + 3\left\{C_2O_4^{2-}\right\} = \langle Re_2(C_2O_4)_3 \rangle + 4\left\{(SO_4)^{2-}\right\} \tag{20}
$$

$$
2 \{ \text{Re}(SO_4)_2 \} + 3 \{ \text{HC}_2O_4 \} = \langle \text{Re}_2(C_2O_4)_3 \rangle + 4 \{ (\text{SO}_4)^2 \} + 3 \{ \text{H}^+ \} \tag{21}
$$

$$
2\left\{Re(SO_4)_2\right\} + 3\left(HC_2O_4\right) + \left\{H^+\right\} = \left\{Re_2(C_2O_4)_3\right\} + 4\left\{(HSO_4)^-\right\} \tag{22}
$$

The concentrations of (a)  $Re^{3+}$ , (b)  $ReCl_2^+$ , (c)  $Re(NO_3)_2^+$ , and (d)  $Re(SO_4)_2^-$  in equilibrium with oxalate precipitate with 10<sup>-4</sup> M of total concentration of oxalate in solution at pH 6, 4, 2, and 1 is plotted in Figure [6.](#page-9-0) in Figure 6.  $\overline{\mathbf{C}}$ 

<span id="page-9-0"></span>

Figure 6. Concentrations of (a)  $\text{Re}^{3+}$ , (b)  $\text{ReCl}_2^+$ , (c)  $\text{Re}(\text{NO}_3)_2^+$ , and (d)  $\text{Re}(\text{SO}_4)_2^-$  in equilibrium with oxalate precipitate with 10<sup>−4</sup> M of total concentration of oxalate in solution at pH 6, 4, 2, and 1. Cr. Concentration: 1 ppm line as a target concentration.

As seen in this figure, oxalic acid is proven to be the most effective precipitant for REEs in solution. The degree of precipitation is very favorable for all pH ranges.

## **8. Comparison Among Precipitants**

As expected, all of the precipitants considered in this study have shown good precipitation characteristics. In general, the most effective precipitant is oxalate, which has shown an outstanding precipitation behavior for REEs even at low pHs. On the other hand, most of precipitants are not effective unless the pH of the system is relatively high. As s[een](#page-10-0) in Figure 7, the precipitation of free Re-ions,  $\text{Re}^{3+}$  is relatively poor even at pH 6 with the exception of oxalate and phosphate. When the pH of the system is low, such as pH 1 (Figure [7b](#page-10-0)), even oxalate loses its effectiveness. As seen in Figure [7,](#page-10-0) it is in general that the order of precipitation power follows: oxalate > phosphate > fluoride > sulfate > carbonate.

<span id="page-10-0"></span>

Figure 7. Concentration of  $\text{Re}^{3+}$  in equilibrium with various precipitants at  $10^{-4}$  M and at (a) pH 4 and (**b**) pH 1. (**b**) pH 1.

However, when REEs complex with the anions such as Cl<sup>−</sup>, NO<sub>3</sub><sup>−</sup>, and SO<sub>4</sub><sup>2−</sup> or HSO<sub>4</sub><sup>−</sup>, which almost always exist, especially at low pHs, since acids frequently used in dissolving Re-bearing almost always exist, especially at low pHs, since acids frequently used in dissolving Re-bearing minerals in the leaching operation are either HCl, HNO<sub>3</sub>, or H<sub>2</sub>SO<sub>4</sub>. As discussed in the earlier studies [\[8](#page-11-10)[,9\]](#page-11-9), when such acids are present in the aqueous system, REEs immediately form complexes with these anions. In the presence of chloride,  $ReCl_2^+$  is the most dominating species,  $Re(NO_3)_2^+$  for the nitrate system and  $\text{Re(SO4)}_2$ <sup>−</sup> is for the sulfate system. As a result, the calculations involved to find equilibrium concentrations of REEs should be carried out using these chemical moieties in place of the equilibrium concentrations of REEs should be carried out using these chemical moieties in place of Re<sup>3+</sup>. Consequently, the precipitation behavior of REEs will also change and therefore, Figure [8](#page-10-1) will be be the relevant figure in place of Figure 7 for the nitric system as an example. the relevant figure in place of Figure [7](#page-10-0) for the nitric system as an example.

It is very notable in the case of the nitrate system, the precipitation power of carbonate has It is very notable in the case of the nitrate system, the precipitation power of carbonate has overtaken over the characteristic and sulfate and sulfate. Similar plots were made for the characteristic system as well as the characteristic system as well as the characteristic system as the characteristic system as well as the c that of fluoride and sulfate. Similar plots were made for the chloride system as well as the sulfate system  $\frac{1}{2}$ and the results were quite similar but the intensity of precipitation was not as strong as the nitric system.<br>

<span id="page-10-1"></span>

Figure 8. Concentration of  $\text{ReCl}_2{}^+$  in equilibrium with various precipitants at  $10^{-4}$  M and at (a) pH 4 and (**b**) pH 1. and (**b**) pH 1.

### **9. Conclusions**

The chemical precipitation of REEs with precipitants including carbonate, fluoride, phosphate, sulfate, and oxalate was studied over a wide range of pH such as 1, 2, 4, and 6. The concentration of precipitants was fixed at  $10^{-4}$  M chosen as the standard concentration for comparison. Such precipitation occurs in practice after primary leaching as a part of the purification process.

With all of the five precipitants studied, Ligjt REEs tend to precipitate much easier than Heavy REEs. The effect of anions associated with acids used in the leaching process was found to have had a significant impact on the overall precipitation process. In general, the complexed REEs with these anions tend to provide a conducive environment in precipitation resulting in an order of magnitude difference in the precipitation extent. The nitrate system was found to be most effective followed by sulfate and chloride systems. The pH of the system has another significant factor in determining the precipitation in that the difference in pKa values of the precipitants introduces precipitant moiety of the precipitants, which has a pronounced effect on the overall precipitation.

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