



Article

Automatic Classification of Hypertensive Retinopathy by Gray Wolf Optimization Algorithm and Naïve Bayes Classification

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Abstract: Retinal blood vessels are affected by a variety of eye diseases, including hypertensive retinopathy (HR) and diabetic retinopathy (DR). A person with HR needs to be sure to check their eyes regularly, which requires the use of computer vision methods to analyze images of the back of the eye and help ophthalmologists automatically. Automated diagnostic systems are useful for diagnosing different retinal diseases for ophthalmologists and patients who need to establish an automated HR detection and classification system using retinal images. In this work, a sliding band filter was used to improve the back-of-the-eye images and small convex regions to develop an automated system for detecting and classifying HR gravity levels. An image classification with improved wolf optimization along Bayes algorithm was conducted. The current model was tested using the publicly available dataset, and its results were compared to existing models. The results mentioned that the model-improved Naïve Bayes model classified the different HR severity levels on the optimized features and produced a maximum accuracy of 100% while being compared to other classifiers.

Keywords: diabetic retinopathy; nature-inspired optimization; Naïve Bayes; wolf optimization



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1. Introduction

Hypertension is caused primarily by blood pressure and leads to many cardiovascular diseases. It is reported that high blood pressure expenses are expected to cost \$274 billion among the population of the United States in 2030 [1]. Complications caused by high blood pressure put the patient's health and life at serious risk. Hypertensive complications are a significant cause of death, leading to organ injury and other complications [2–5].

While hypertensive retinopathy (HR) can cause a lot of disturbances on the ocular retina, HR does not show any symptoms during the early stages, and more than 90% of HR patients can prevent the disease from being vision threatening with the proper treatment initiated at the right time. The only way to detect this disease is to carry out regular eye examinations using color images of the fundus obtained by the fundus photograph. Computational vision is one of the main tools used in the development of automation in the diagnosis of many diseases. As the computer system ignores all factors unrelated to the diagnosis of the disease, the possibility of error is reduced, and better diagnosis is offered with great accuracy and agility [6]. It is impossible to derive the correct boundaries based on image segmentation traits due to the lack of image detail information.

For fundus image segmentation, threshold segmentation is the best option, as it offers benefits such as easy implementation, less computational complexity, and better performance [7]. Additionally, fundus images can be classified based on threshold values and can be segmented based on a single- or multi-threshold value. Using thresholding, the

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segmentation thresholds are determined by optimizing the criteria, such as the maximum difference between the class variance and the various criteria [3].

When it comes to image segmentation, the thresholding technique shows remarkable performance. When dealing with complex image segmentation issues, the high threshold issue will increase the algorithm's complexity. A multilevel threshold, using Kapur's entropy and the dragonfly optimization algorithm, optimized it to minimize computer complexity [8]. A grey wolf optimizer for multilevel image thresholding was created by adapting Kapur's entropy and Otsu's methods to determine segmentation thresholds [9]. For diagnosing hypertension, ophthalmologists use the ratio of arterial blood vessels of the retina (ARVS) in order to determine the presence of hypertension. Changes in retinal blood vessels may follow retinal disturbances over time, and the abnormal width of the vein leads to a low ratio of the arterial–venous mean diameter (AVR). It has been reported that fundus image segmentation helps in the provision of better treatment [10].

Existing literature has proposed systems for the early detection of HR, and they segmented the vessels using multi-scale filtering [11,12]. Authors estimated the vessel width in the region of interest, and AVR was calculated to detect HR and achieved an accuracy of about 93.1–93.7% [11]. HR detection by segmenting the vessels using moment-based and grey-level features and a support vector machine (SVM) for classification was presented [12]. The segmentation of the blood vessels using top-hat transformation and a double-ring filter produced 75% accuracy [13]. Similarly, another study segmented vessels by extracting intensity- and color-based characteristics to classify vessels as arteries and veins produced a maximum accuracy of 96% [14].

Despite the significant results generated by existing works, the discussed models are complex, in that they are used to segment the grey-scale images instead of the color images with low accuracy. This work presents a wolf optimization algorithm that reduces the computational complexity and improves the segmentation accuracy. We have extracted several prominent features to classify the severity levels of HR using the improved Naïve Bayes classifier. These distinct features are detected based on repeated experiments and are statistically significant in the classification task.

2. Materials and Methods

In this study, we aimed to present a classifier for the classification of HR with improved wolf optimization for the segmentation of the fundus images. The image pre-processing was conducted by applying a sliding band filter for the fundus image enhancement. In the segmentation phase, we applied improved wolf optimization algorithms to the pre-processed image and distinguished the candidate regions.

The block diagram of the experimental framework has been visualized in Figure 1. It is decomposed into five stages, including (1) fundus image collection, (2) image preprocessing, (3) image segmentation, (4) feature extraction, and (5) HR severity classification.

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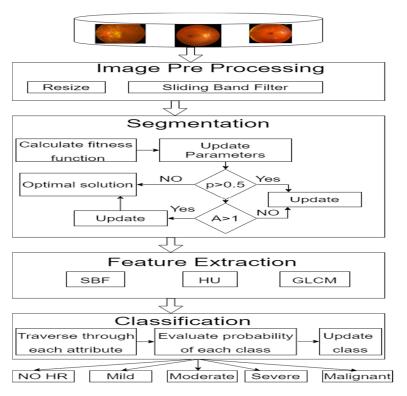


Figure 1. Block diagram of the proposed system.

2.1. Image Collection and Preprocessing

Using the publicly available datasets ODIR [15], DRIVE [16], STARE [17], and VI-CAVR [18], 1200 fundus images were collected. The STARE dataset consists of 400 images, the DRIVE dataset consists of 40 fundal images, the VICAVR dataset consists of 58 fundal images, and the ODIR dataset consists of 6426 fundal images. These images are categorized into six classes by classifiers trained according to international standards for the classification of hypertensive retinopathy. Images of poor quality that do not show clearly visible lesions are considered ungradable. Therefore, the six levels, i.e., normal, mild, moderate, severe, malignant, and ungradable, were included. In the present study, we focused solely on the five-class classification task for HR classification, i.e., we did not use images belonging to the ungradable class. Table 1 shows the breakdown of the collection of data by HR category.

Table 1. Dataset Distribution for this study.

Category	Count		
Normal	200		
Mild	400		
Moderate	200		
Severe	200		
Malignant	200		

We used a sliding band filter to improve the fundus image, a multi-season segmentation for feature extraction, followed by a multi-class Naïve Bayes classifier for image classification. If the retinal lesions could not be completely identified, regardless of the quality of the model, the missing lesion could not be detected at the final detection. Essentially, non-linear gamma transformation was applied to each pixel of the fundus image, with the individual gamma parameter calculated from the pixel and the adjacent pixel. The process was wrapped in a multiscale approach to enhance the differently sized lesions in the fundus image. Sliding band filters (SBF) are found in retinal images. They rely on

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gradient convergence, which identifies lighting changes and, finally, detects low contrast candidates in the noisy retina image. This depends on maximizing the convergence index at every point in the retinal image. An SBF filter eases the detection of the shape and size of the candidates [19].

The mathematical representation of the SBF is:

$$T_{m}(p) = \frac{1}{N} \sum_{t=0}^{N-1} \max_{\substack{B_{min}^{n} < b < B_{max}^{n} \\ b = 0}} \left(\frac{1}{k+1} \sum_{b=(k/2)}^{b+(k/2)} Conv(p, v) \right); \tag{1}$$

$$Conv(t,n) = cos(\theta_t - \alpha(\theta_t,v)) \tag{2}$$

$$\theta_t = \frac{2\pi}{N}(t-1) \tag{3}$$

$$\alpha(\theta_t, v) = \arctan\left(\frac{G_v c}{G_v R}\right) \tag{4}$$

where N represents the support region lines count; B_{min} and B_{max} represent the inner and the outer sliding limits of the band; and $\theta_{p,q}$ represents the angle of the gradient vector. G_vC and G_vR are the column and row gradients at fundus image position; k is the sliding band width; k is the position of the band center in the support region line ranging from B_{min} to B_{max} ; and $cos(\theta_t - \alpha(\theta_t, v))$ is the angle between the gradient vector at (θ_t, v) and the direction of θ_t . The experimental framework was implemented on a 2.2 GHz Intel Core i7 processor with 16 GB RAM using Python 3.7.2.

2.2. Fundus Segmentation

Image segmentation is a critical technique in image processing that splits the given fundus image into specific regions with unique features followed by the extraction of the object of interest. Threshold-based segmentation extracts regions in accordance with pixel intensity values. In [20], the authors' white pixels are substituted for pixels with more significant intensities than a threshold value. The kurtosis-based weighted whale optimization (KMWWOA) selects the optimal n-level cut-off in the retinal image segmentation.

For instance, if there are M intensity levels for each channel in the input-enhanced RGB image, and these levels are in the range of $0, 1, 2, \ldots, M-1$. The probability distribution is represented as

$$P_s^h = \frac{I_s^h}{N} \tag{5}$$

$$\sum_{s=1,h=\{R,G,B\}} P_s^h = 1 \tag{6}$$

where s represents the number of specific intensity level that ranges from 0 to M-1; h represents the image channel; N represents the total number of pixels in the retina image; and I_s^h represents the pixels count for the intensity level s in the channel h. The K_Q^h of each image is represented as

$$K_{Q}^{h} = \sum_{s=1, h=\{R,G,B\}}^{k_{z}^{h}} \left(p_{s} - \left(\frac{sP_{s}^{h}}{Bz_{h}} \right)^{2} \right)^{2}$$
 (7)

The optimal threshold values on the retina image can be evaluated by maximizing the kurtosis between any two classes, and it is represented as

$$T_{c}^{h} = \sum_{z=1, h=\{R,G,B\}} B_{z}^{h} \left(K_{z}^{h} - K_{Q}^{h} \right)$$
 (8)

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where K_z^h and B_z^h represent the kurtosis and the probability of occurrences; and z represents the class from the existing m classes.

The modelling of the occurrence of the probability B_z^h of m classes C_1^h, \ldots, C_m^h

$$B_{z}^{h} = \begin{cases} \sum_{s=1,h=\{R,G,B\}}^{k_{z}^{h}} P_{s}^{h} & z = 1\\ \sum_{s=k_{z}^{h}+1,h=\{R,G,B\}}^{k_{z}^{h}} P_{s}^{h} & 1 < z < m\\ \sum_{s=k_{z}^{h}+1,h=\{R,G,B\}}^{L} P_{s}^{h} & z = m \end{cases}$$

$$(9)$$

The K_z^h of each class is computed as

$$K_{z}^{h} = \begin{cases} \sum_{s=1,h=\{R,G,B\}}^{k_{z}^{h}} \frac{\left(p_{s} - \frac{sP_{s}^{h}}{BZ_{h}}\right)^{4}}{\sum_{s=1,h=\{R,G,B\}}^{k_{z}^{h}} \left(p_{s} - \left(\frac{sP_{s}^{h}}{BZ_{h}}\right)^{2}\right)^{2}}, & z = 1 \end{cases}$$

$$K_{z}^{h} = \begin{cases} \sum_{s=k_{z}^{h}+1,h=\{R,G,B\}}^{k_{z}^{h}} \frac{\left(p_{s} - \frac{sP_{s}^{h}}{BZ_{h}}\right)^{4}}{\sum_{s=1,h=\{R,G,B\}}^{k_{z}^{h}} \left(p_{s} - \left(\frac{sP_{s}^{h}}{BZ_{h}}\right)^{2}\right)^{2}}, & 1 < z < m \end{cases}$$

$$\sum_{s=k_{z}^{h}+1,h=\{R,G,B\}}^{L} \frac{\left(p_{s} - \frac{sP_{s}^{h}}{BZ_{h}}\right)^{4}}{\sum_{s=1,h=\{R,G,B\}}^{k_{z}^{h}} \left(p_{s} - \left(\frac{sP_{s}^{h}}{BZ_{h}}\right)^{2}\right)^{2}}, & z = m \end{cases}$$

$$(10)$$

The search space agents update the positions using the optimum value, and the behavior of the agent is represented as

$$\overrightarrow{Y}(i+1) = \overrightarrow{Y}^*(i) - \overrightarrow{GC}$$
 (11)

$$\vec{C} = |\vec{B}.\overset{\rightarrow}{Y^*}(i) - \vec{Y}(i)| \tag{12}$$

Here, \vec{G} and \vec{B} represent the coefficient vectors, and i represents the current iteration. $\overset{\rightarrow}{Y^*}$ represents the best obtained position vector. $\vec{G}=2\vec{g}\vec{r}-\vec{g}$ and $\vec{C}=2\vec{r}$, where \vec{g} represents the used vector, which decreases the iterations from 2 to 0; and \vec{r} represents a random vector that makes the agent reach the position that ensures that the exploration ranges from 0 to 1.

$$\overrightarrow{Y}(i+1) = \overrightarrow{C'}. e^{f\nu} Cos (2\pi v) + \overrightarrow{Y^*}(i)$$
(13)

Here, $\overset{\frown}{C}$ represents the distance between the whale and the prey; f represents the shape of the spiral; and v represents a random value range from -1 to 1. For updating the whale position, it is mathematically presented as

$$\overset{\rightarrow}{Y^*}(i+1) = \begin{cases}
P\overset{\rightarrow}{Y^*}(i) - \overset{\rightarrow}{GC} & \text{if } p < 0.5 \\
\overset{\rightarrow}{C'} \cdot e^{fv} \cos(2\pi v) + \overset{\rightarrow}{Y^*}(i) & \text{if } p \ge 0.5
\end{cases}$$
(14)

The search agent position is updated similar to as shown below

$$\overrightarrow{C} = |\overrightarrow{B}. \overrightarrow{x_{rand}} - \overrightarrow{Y}|$$
 (15)

$$\overrightarrow{Y}(i+1) = \overrightarrow{x_{rand}} - \overrightarrow{GC}$$
 (16)

where x_{rand}^{\rightarrow} represents the random position vector.

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To evaluate the optimum thresholds, the equation represents as

$$\eta^{h} = \max_{1 < k_{1}^{h} < \dots ... k_{m-1}^{h} < L} \left(T_{c}^{h} \left(k_{z}^{h} \right) \right) \tag{17}$$

The kurtosis-based, multi-thresholding whale optimization algorithm is presented in Algorithm 1.

Algorithm 1: Kurtosis-based, multi-thresholding whale optimization algorithm.

Input: Enhanced retina Image output: Segmented retina image

- 1. Initialize initial solution xi (i = 1, ..., 250)
- 2. Evaluate the fitness value using equation $\max_{1 < k_1^h < \dots ... k_{m-1}^h < L} (T_c^h \Big(k_z^h\Big)$
- 3. Initialize Y*

while (d < maximum iterations)

for each search agent

update a, A, C, l and p

4. if (p < 0.5); (|A| < 1)

Update the current search agent equation using the equation $\overrightarrow{Y}(\mathbf{i}+1) = \overrightarrow{Y}^*(\mathbf{i}) - \overrightarrow{GC}$ 5. else if (|A| > 1)

select x_{rand} and update the current search agent position using the equation

$$\overrightarrow{Y}(i+1) = \overrightarrow{x_{rand}} - \overrightarrow{GC}$$

6. else if $(p > 0.5)$

update current search position using the equation $\overrightarrow{Y}(i+1) = \overrightarrow{C'}$. $e^{f\nu}$ Cos $(2\pi v) + \overrightarrow{Y^*}(i)$ repeat for all search space agents

- 7. Evaluate the search agent fitness for each and every search agent.
- 8. Segment the retina image with best value which maximizes the kurtosis

2.3. Feature Extraction and Selection

With CAD systems, features are combined to characterize lesions in a similar way to traditional visual diagnosis, with high sensitivities and specificities of features. In computational environments, background image pixels provide sufficient information. Characteristic extraction methods based on color and texture are widely used to evaluate candidates. It is possible to drastically reduce the amount of training data by selecting the most powerful features and incorporating them into the learning algorithm. The types of features were presented, including Hu's [21], the gray level co-occurrence matrix (GLCM), and sliding band features. Hu's seven invariant moments of rotation, similarity, size, and rotation are represented as

$$\mu_{x,y} = \sum_{a,b} (a - a_p)^m (b - b_p)^n \tag{18}$$

where (a_p, b_p) in the object's center.

 $\eta_{xy} = \frac{\mu_{xy}}{\mu_{00}}$ and the evaluated seven moments listed below

(a)
$$\phi_1 = \eta_{2,0} + \eta_{0,2}$$

(b)
$$\phi_2 = (\eta_{2,0} - \eta_{0,2})^2 + 4\eta_{1,1}^1$$

(c)
$$\phi_3 = (\eta_{3,0} - 3\eta_{1,2})^2 + (\eta_{3,0} - 3\eta_{2,1})^2$$

(d) $\phi_4 = (\eta_{3,0} + 3\eta_{1,2})^2 + (\eta_{0,3} + \eta_{2,1})^2$

(d)
$$\phi_4 = (\eta_{3.0} + 3\eta_{1.2})^2 + (\eta_{0.3} + \eta_{2.1})^2$$

(e)
$$\phi_5 = (\eta_{3,0} - \eta_{1,2})(\eta_{3,0} + \eta_{1,2})[(\eta_{3,0} + \eta_{1,2})^2 - 3(\eta_{2,1} + \eta_{0,3})^2] + (3\eta_{2,1} - \eta_{0,3})(\eta_{2,1} + \eta_{0,3})[3(\eta_{3,0} + \eta_{1,2})^2 - (\eta_{2,1} + \eta_{0,3})^2]$$

(f)
$$\phi_6 = (\eta_{2,0} - \eta_{0,2})[(\eta_{3,0} + \eta_{1,2})^2 - (\eta_{2,1} + \eta_{0,3})^2] + 4\eta_{1,1}(\eta)(\eta_{2,1} + \eta_{0,3})$$

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(g)
$$\phi_7 = (3\eta_{2,1} - \eta_{0,3})(\eta_{3,0} + \eta_{1,2})[\left(\eta_{3,0} + \eta_{1,2}\right)^2 - 3\left(\eta_{2,1} + \eta_{0,3}\right)^2] + (\eta_{3,0} - \eta_{1,2})(\eta_{2,1} + \eta_{0,3})[3\left(\eta_{3,0} + \eta_{1,2}\right)^2 - \left(\eta_{2,1} + \eta_{0,3}\right)^2]$$

GLCM highlights the texture information of an image since it computes the texture features by considering the spatial relationship of the pixels. GLCM reduces time consumption. Due to space constraints, we showcased only some of the features in this paper. Table 2 presents the list of its features.

Table 2. GLCM feature lists.

N	Feature	Formula
F1	Angular Second Moment	$\sum_{x}\sum_{y}[p(x,y)]^{2}$
F2	Contrast	$\sum_{q=0}^{M-1}q^2[p_i(q)]$
F3	Correlation	$\frac{\sum_{\mathbf{x}}\sum_{\mathbf{y}}(\mathbf{x},\mathbf{y})p(\mathbf{x},\mathbf{y}) - \mu_{\mathbf{i}}\mu_{\mathbf{j}}}{\sigma_{\mathbf{i}}\sigma_{\mathbf{j}}}$
F4	Inverse difference moment	$\sum_{x} \sum_{y} \frac{1}{1 + (x + y)^2} P(x, y)$
F5	Sum average	$\sum_{\mathbf{x}=2}^{2\mathbf{K}}\mathbf{x}\Big[p_{\mathbf{i}+\mathbf{j}}(\mathbf{x})\Big]$
F6	Sum variance	$\textstyle\sum\limits_{x=2}^{2K} \left(x - \sum\limits_{x=2}^{2K} p_{i+j}(x) \left[p_{i+j}(x)\right]\right)^2 \left[p_{i+j}(x)\right]$
F7	Sum Entropy	$-\sum_{x=2}^{2K}p_{i+j}(x)\Big[p_{i+j}(x)\Big]$
F8	Entropy	$-\sum_{x}\sum_{y}P(x-y)\log[P(x-y)]$
F9	Difference variance	Variance of p _{x+y}
F10	Difference entropy	$-\sum_{x=0}^{K=1}p_{i-j}\log\Bigl[p_{i-j}(x)\Bigr]$
F11	Info. Measure of correlation	$\frac{\text{AIJ} - \text{AIJ}_1}{\text{max}[\text{AI} - \text{AJ}]}$
F12	Max. corel.coefficient	(Square of the eigen value B)1/2; B = $\sum_{k} \frac{P(xk)_{P}(Jk)}{P_{i}(x)P_{j}(k)}$

In addition to detecting all the candidates in a convex shape, SBF features can help differentiate between vessels and arteries. The mean value of the SB filter was output inside the feature ($\mu_{s_{feature}}$) and its neighborhood ($\mu_{s_{neigh}}$). The difference between the mean and the SB filter output inside the feature and its neighbor is

$$\mu_{\text{S}_{\text{feature}}} - \mu_{\text{S}_{\text{neigh}}}.$$
 (19)

Due to the oxidized blood supply, arteries are thinner than veins and have a stronger central reflex. There is less contrast and color variations between veins and arteries. Based on color and statistical features, AVR classifies segmented vessels into arteries and veins. For each segmented vessel, center line pixels were divided into features based on pixel size, vessel profiles, and vessel segments. For AV classification, a total of 59 features were extracted. The characteristic vector containing all the extracted features was created for each central line in the segmented vessels and the surrounding pixels. The feature vector of each pixel was entered into the proposed classifier that identified the vessel and whether it was part of the arterial class or the vein class. This process was repeated for all vessel segments in the fundus images. The classifications of the arterial vessel and the vascular segment of the vein were represented as red and blue, respectively. Feature vectors were created

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by combining textual features, disc margin obscuration features, and vessel features from segmented fundus images. The extracted features and the AVR value detect papilledema.

$$AVR = \frac{\sqrt{0.87a_w^2 + 1.01b_w^2 - 0.22a_wb_w - 10.76}}{\sqrt{0.72a_w^2 + 0.91b_w^2 + 450.05}}$$
(20)

where a_w is the smaller value; and b_w is the larger value.

It was crucial to select the right features for classification in order to achieve successful image recognition. When classifiers were trained with a limited set of learning samples, a peaking phenomenon occurred; thus, feature selection was used. If the number of features increased, the classification rate of the classifiers decreased [22]. An improved ant colony optimization was used to select the features in this study [23].

2.4. Classification Using Improved Naïve Bayes Classifier

Once the affected region was segmented and its features were extracted, a decision support system helped to group by hypertensive retinopathy. In the probabilistic classifier category, the Naïve Bayes (NB) classifiers were independent of features. This has proved effective in many practical applications, including medical diagnosis and system performance management [24,25]. If a data point $\overrightarrow{x} = \{x_1, x_2, \dots, x_m\}$ of m features were given, an improved NB classifier was proposed to predict the class C_q for \overrightarrow{x} based on probability, and its mathematical representation is $P(C_q | \overrightarrow{x}) = P(C_q | x_1, x_2, \dots, x_m)$ for $q = 1, 2 \dots Q$.

After applying the Bayes theorem, the mathematical representation of the above equation is:

$$P(C_{q}|\overrightarrow{x}) = \frac{p(\overrightarrow{x}|C_{q})p(C_{q})}{p(\overrightarrow{x})}$$
(21)

$$=\frac{P(x_1,x_2,\ldots,x_m\big|C_q)p\big(C_q\big)}{P(x_1,x_2,\ldots,x_m)}$$

The mathematical representation of the decomposition of the term $P\left(x_1, x_2, \ldots, x_m \middle| C_q\right)$

$$P(x_1, x_2, ..., x_m | C_q) = P(x_1 | x_2, ..., x_m, C_q) P(x_2 | x_3, ..., x_m, C_q) P(x_{n-1} | x_n, C_q) P(x_n | C_q)$$
(22)

Considering the Naïve Bayes' conditional independence, and the features in \overrightarrow{x} are independent to each other. The mathematical representation of the decomposition is:

$$P(x_1, x_2, \dots, x_m \big| C_q) = P\left(x_s \big| C_q \right) = > P(x_1, x_2, \dots, x_m \big| C_q) = \prod_{s=1}^m p(x_s | D_s); \tag{23}$$

thus,

$$P(C_q|x_1, x_2, ..., x_m) \alpha P(C_q, x_1, x_2, ..., x_m)$$

$$\alpha P(C_q) P(x_1, x_2, \dots, x_m | C_q)$$

$$\alpha \, P \big(C_q \big) \, P(x_1 \big| C_q) \ P(x_1 \big| C_q) \; , \ldots \ldots , \; P(x_m \big| C_q)$$

$$\alpha P(C_q) \prod\nolimits_{s=1}^m p(x_s|D_s) \tag{24}$$

where α dentoes proportionality. The distribution over the class C_q is represented as

$$P(C_{q}|x_{1},x_{2},...,x_{m}) = \frac{1}{N} P(C_{q}) \prod_{s=1}^{m} p(x_{s}|D_{s})$$
(25)

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 $P(\overrightarrow{x}) = P(C_q)P(\overrightarrow{x}|C_q)$ represents the scaling factor, depending on x_1, x_2, \dots, x_m .

The data point $\overrightarrow{x} = \{x_1, x_2, \dots, x_m\}$ of m features were assigned to the best relevant class by evaluating $P(C_q) = \prod_{s=1}^m p(x_s|D_s)$ for $q=1,2,\dots,Q$, class C_q was assigned to \overrightarrow{x} for the maximum value, and it was mathematically represented as

$$\hat{C} = argmax_{q \in \{1Q\}} R(x_s) P(C_q) \prod_{s=1}^{m} p(x_s | D_s)$$
 (26)

$$\text{here} R(x_s) = \frac{1}{M} \sum\nolimits_{k=1}^{M} \frac{\left(x_k - \frac{1}{N} \sum\nolimits_{k=1}^{M} x_k\right)^4}{\left(\frac{1}{M'} \sum\nolimits_{k=1}^{M} x_k\right)^4}$$

3. Results

The experiments were undertaken to assess the performance of the proposed segmentation model for vessel segmentation. The proposed model was implemented with different threshold levels, 2–5. In Table 3, we tabulated the results of different thresholds their corresponding accuracies and noted that a higher threshold value led to more accurate results.

Table 3. Accuracies and processing times of the proposed model for different segmentation results.

Threshold	Accuracy	Processing Time (ms)		
2	98.67	0.2474		
3	98.85	0.2479		
4	99.04	0.2482		
5	99.36	0.2485		

The evaluation function was implemented in the proposed against different threshold levels between 2 and 5. Table 4 compares the proposed values with various optimization algorithms at various threshold levels. It was evident that the proposed model provided more precise and robust segmentation and less computation time with an increase in the number of thresholds.

Table 4. Comparison of average accuracy for different segmentation models at different threshold levels.

Threshold Level	old Level PSO		KMWWOA	
2	96.34	97.25	98.67	
3	96.79	97.37	98.85	
4	97.35	98.33	99.04	
5	97.47	98.62	99.36	

Table 5 presents population stability of 50–100 iterations, and the peak PSO model reached stability [26]. In addition, the maximum level of exploration prevented the model from dropping into local minima and allowed it to be more effective [27]. Compared to the advanced model, it required fewer iterations to reach the best value. It was easy to identify which algorithm converged quickly based on the number of iterations. For iteration 50 and population size 100, the state-of-the-art model achieved stability faster than the state-of-the-art model with the same threshold value.

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Table 5. Comparison of the performance of the proposed with the state-of-the-art models with effect
of iterations and population size.

PSO			Proposed			
Population Size	Iterations	Avg Threshold Value	Population Size	Iterations	Best Threshold Value	
	1	31		1	24	
	25	28		25	21	
	50	27		50	20	
50	75	32	50	75	26	
	100	35		100	25	
	150	27		150	25	
	200	25		200	25	
	1	21		1	18	
	25	25		25	21	
	50	26		50	25	
100	<i>7</i> 5	21	100	<i>7</i> 5	25	
	100	22		100	25	
	150	25		150	25	
	200	25		200	25	
	200					

The parameter values chosen for the number of iterations and population size were based on the findings of many search agents. Maximum iterations could approximate the global optimum better for faster convergence, and any other value would weaken it. From Figure 2, it is evident that we were achieving more accurate results by raising the threshold value.

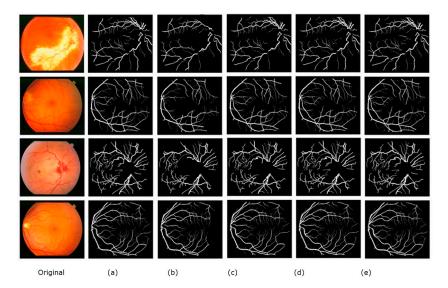


Figure 2. Segmentation results with threshold levels from STARE dataset: (a) ground truth, (b) threshold 2 segmented image, (c) threshold 3 segmented image, (d) threshold 4 segmented image, and (e) threshold 5 segmented image.

Table 6 tabulated the performance of the proposed improved WOA compared to the state-of-the-art models. Compared with other alternative models, it produced accurate, detailed segmentation results with tiny vessels, making it a perfect choice for automatic CAD systems that rely on vessel segmentation results to estimate their estimates.

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Model	Accuracy	Sensitivity	Specificity	
GrasshopperOA [28]	95.24	82.64	97.42	
AntCO [29]	94.63	79.46	97.21	
Rider OA [30]	96.72	89.46	97.46	
GreyWOA [31]	97.36	91.63	98.42	
Proposed	99.36	93.56	99.85	

Table 6. Comparison of segmentation results with the state-of-the-art models.

Figure 3 shows the vessel segmentation and detection by the proposed model with the STARE and DRIVE datasets. We used an improved Naïve Bayes classifier for HR classification. To figure out the Bayes classifier's performance, precision, recall, and F1 score, parameters were used. During the test time, we obtained a predictive posterior distribution. By avoiding multiple training sessions, this method required less resources and improved the accuracy of the classification and detection of hypertensive retinopathy. Multi-class classifications require predicting the likelihood of several mutually exclusive classes. Based on the clinical criteria applied, these classes represented pathology 4 or 5 [25,32].

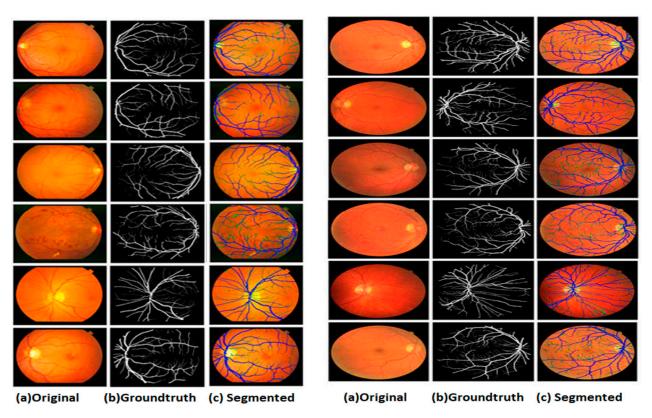


Figure 3. Vessel Segmentation using Improved WOA for STARE (left) and DRIVE (right) datasets.

A severity classification confusion matrix is shown in Figure 4, along with samples that were correctly and incorrectly classified. Almost all sample classes (i.e., no HR, mild, moderate, severe, and proliferative) were correctly classified. Once these statistical values of the classifier were calculated, they were compared against the state-of-the-art models for robustness and efficiency findings. Table 7 tabulates the comparison of the proposed with the state-of-the-art model's performance measures for multi-class classification in terms of accuracy, precision, recall, and F1 score.

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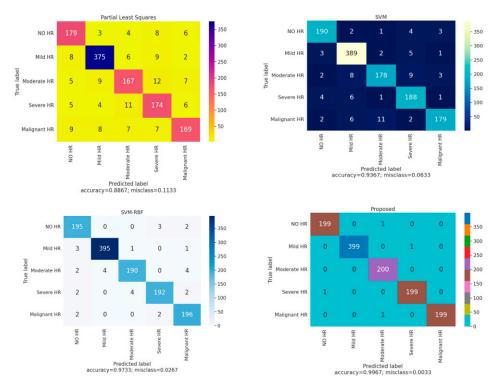


Figure 4. Confusion matrix for multi class classification.

Table 7. Performance measure for multi class classification.

Project	Classifier	Accuracy	Precision	Recall (%)	F-Score (%)	AUC	Class
	Partial Least	96	87	89	88	0.97	No HR
		96	94	94	94	0.97	Mild
Agurto et al. [33]		95	86	83	84	0.95	Moderate
· ·	Squares	95	83	87	85	0.95	Severe
		96	89	84	87	0.96	Malignant
		98	94	95	95	0.97	No HR
		97	95	97	96	0.97	Mild
Irshad S et al. [34]	SVM	97	92	89	90	0.98	Moderate
		97	90	94	92	0.98	Severe
		97	96	89	92	0.97	Malignant
	SVM-RBF	99	99	97	96	0.98	No HR
		99	99	99	99	0.98	Mild
Akbar et al. [35]		99	97	95	96	0.98	Moderate
		99	97	96	97	0.98	Severe
		99	96	98	97	0.99	Malignant
	Improved Naïve Bayes	100	99	99	99	0.99	No HR
		100	100	100	100	0.99	Mild
Proposed		100	99	100	99	0.99	Moderate
-		100	99	99	99	0.99	Severe
		100	100	99	100	0.99	Malignant

4. Discussion

Many people around the world suffer from HR disease, which is caused by high blood pressure in the retinal blood vessels. However, HR patients are not aware of the disease, and its severity can be detected by a patient's eye ophthalmologic examination. Blindness or vision loss often results from HR diagnosed at the last stage. This mainly focuses on HR detection using a nature-inspired optimization algorithm. Hypertensive retinopathy vessels are segmented more accurately by whale optimization. HR diagnosis requires

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a deep analysis of the retinal vasculature. A feature map that represents the maximum features of retinal blood vessels is designed in this study to detect retinal blood vessels in unconstrained scenarios.

We proposed an automated CAD system to detect and classify hypertensive retinopathy. Starting with the contrast enhancement, performed using sliding band filtering, the resulting output can be seen. In addition to enhancing and highlighting the legion region, these preprocessing steps make it difficult to classify the region. We used the KMWWOA algorithm to segment the vessels, which improved the segmentation by targeting small vessels. As it was applied to different datasets with different conditions, it proved robust to changes in the input fundus images. No matter if the entry image was normal or abnormal with exudates or microaneurysms, the accuracy was preserved.

The number of iterations has an essential impact on the multi-thresholding model's performance. We tested the effect of iterations number on the best threshold level value and convergence using both the proposed model as well as the state-of-the-art models, such as PSO and WOA. The algorithm had a high level of exploration, which, in turn, allowed one to search all over the search space. This prevented it from falling into local minima. From the results, the proposed solution achieved the highest value with fewer iterations than the PSO. In PSO, there was a better level of exploitation that may have fell within local minima, and the proposed option would present a greater variety of exploration and exploitation speeds. Depending on the number of iterations, when the number increased, the thresholding level became better. This was until it reached an extent to which increasing the number of iterations had not affected the most effective threshold level. From the number of iterations, it could be determined that the suggested algorithm converged faster. Both the proposed algorithm and the PSO almost reached the same highest intensity threshold level of 25. The proposed method achieved faster convergence than PSO with the same threshold level value.

This study used various features, and the developed model produced 96.7% accuracy, a specificity of 0.935, and a sensitivity of 0.998 during feature extraction. Comparing the performance of the developed model with the state-of-the-art models on the DRIVE, STARE, and VICAVR datasets, it saved computational time and achieved accurate, detailed segmentation results with tiny vessels. Consequently, this model was suitable for classifying HR severity levels based on vessel segmentation and estimations. It exceeded most state-of-the-art models in terms of overall accuracy, and the proposed classifier needed to produce more misclassifications.

5. Conclusions

A novel vessel segmentation model for a kurtosis-based, multi-threshold WOA in fundus images was presented in this study. Using KMWWOA, optimum n-level thresholds were automatically selected for retinal image segmentation. According to the results, they were identical to the ground truth, which was an indication of high accuracy compared to state-of-the-art models. In this study, we detected and classified the five stages (i.e., no HR, mild, moderate, severe and malignant) of HR based on the improved segmentation technique. The performance metrics were approximately reached 100% with the proposed classifier.

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