

## Article

# Intelligent Systems to Optimize and Predict Machining Performance of Inconel 825 Alloy

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**Abstract:** Intelligent models are showing an uprise in industry and academia to optimize the system's outcome and adaptability to predict challenges. In machining, there is difficulty of unpredictability to the part performance especially in super alloys. The aim of this research is to propose an intelligent machining model using contemporary techniques, namely, combinative distance-based assessment (CODAS), artificial neural network (ANN), adaptive neuro-fuzzy inference systems, and particle swarm optimization (ANFIS-PSO) approach for minimizing resultant force, specific cutting energy, and maximizing metal removal rate. Resultant force response has shown to be affected by feed rate and cutting speed with a contribution of 54.72% and 41.67%, respectively. Feed rate and depth of cut were statistically significant on metal removal rate contributing with the same value of 38.88%. Specific cutting energy response resulted to be statistically significant toward feed rate with 43.04% contribution and 47.81% contribution by depth of cut. For the CODAS approach, the optimum parameters are cutting speed of 70 m/min, feed of 0.33 mm/rev, and depth of cut of 0.6 mm for the seventh experiment. The estimated values predicted by the ANN and ANFIS method were close to the measured values compared to the regression model. The ANFIS model performed better than the ANN model for predicting turning of the Inconel 825 alloy. As per quantitative analysis, these two models are reliable and robust, and their potential as better forecasting tools can be used for hard-to-machine materials. For hybrid ANFIS-PSO, the optimum parameters for minimizing resulting force were (82, 0.11, 0.15), for minimizing specific cutting energy (45, 0.44 and 0.6) and maximizing metal removal rate (101, 0.43, 0.54). The hybrid model ANFIS-PSO has proven to be a better approach and has good computational efficiency and a lower discrepancy in assessment.



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**Keywords:** ANN; CODAS; hybrid ANFIS-MOPSO; Inconel 825; turning

## 1. Introduction

In the last two decades, the environmental impact worldwide has led to productivity, reduction of energy consumption, and quality consciousness as the main factors for research in today's manufacturing scenario. The economic, environmental, and legislative drivers have raised awareness of energy consumption and associated environmental impact of manufacturing processes. For sustainability performance, cleaner manufacturing is based on products that conserve natural resources and do not pollute the environment [1]. Considering this, green manufacturing has been proposed and drawn attention from both academia and industry. Appropriate environmental measurements, such as energy consumption, product quality, and production rate, are important for improving manufacturing processes [2]. The prediction of machining parameters has become necessary considering the need to increase production rate, reduce cost of production, and ensure sustainability and product quality. In conventional manufacturing, specific cutting energy can be considered as an adequate parameter to understand the energy consumption and machinability of materials that are primarily responsible for environmental impacts. Understanding machining processes and its complexity provides sufficient knowledge about energy consumption. For sustainable production, there should be a balance between

energy consumption and machining quality [3]. However, with the non-linear nature of the machining process, applying and identifying a suitable and adequate technique is crucial to achieve green and reliable machining performance.

Machinability of super alloys has always been a challenge, as they are suitable for high-temperature applications and are commonly used in critical structures. It has better corrosion resistance in oxidizing environments, and chromium provides oxidizing resistance as well as a stable austenite structure [4]. It is the most suitable material due to its widespread applications in several industries, namely nuclear, aerospace, and chemical industries, to make components such as pressure vessels, propeller shafts, and expansion bellows for deep-sea applications such as marine engine parts and aircraft engine parts industries. However, Inconel alloy 825 has few limitations as it is hard and tough, forms a built-up edge, has work hardening behavior, and possesses lower thermal conductivity and harder continuous chips [5]. This alloy is an expensive material that is difficult to cut due to tool wear. Due to strain hardening, the heat generated in the cutting zone will be higher, increasing thermal stresses and causing faster tool wear. Therefore, 825 alloy is a critical material and still require understanding its behavior and to optimize its processing parameters.

Optimization has become an integral part of each complex machining process, and optimization of cutting factors is logically studied in manufacturing engineering to improve machine performance in terms of cost and accuracy. Many researchers adopted traditional approaches for optimization of machining factors, namely, factorial design, the Taguchi method, and response surface methodology (RSM), to obtain optimal solutions [6–8]. Advanced statistical tools such as grey-based Taguchi analyses was employed for machining AZ91D magnesium alloy to determine the best process parameters [9]. Non-traditional optimization methods are important in various engineering applications. Objective function optimization is used to determine by combining input cutting factors to optimize a single response or multiple responses [6,10]. The literature have proposed various soft computing approaches, namely multi-criteria decision-making techniques (MCDM), namely genetic algorithms, particle swarm optimization (PSO), and technique for order of preference by similarity to ideal solution (TOPSIS), and simulated annealing [11–13]. The combinative distance-based assessment (CODAS) approach developed by Ghorabae was used for the selection of suppliers, cutting fluid and materials, market segmentation, material handling equipment, and airline performance [11,14]. In CODAS, the desirability of alternatives is assessed using two variables. The essential and fundamental metric has to do with how far away alternatives are from the negative-ideal in Euclidean space. This kind of distance necessitates the use of a  $l^2$ -norm indifference space for the criteria. The taxicab distance, which is connected to the  $l^1$ -norm indifference space, serves as the secondary metric. It is obvious that the alternative that is further from the negative-ideal solution is the more desired one. If two options are not comparable using the Euclidean distance, the taxicab distance is used as a backup measurement in this procedure. Two forms of indifference space could be considered in the CODAS process, even though the  $l^2$ -norm indifference space is favored. Ghorabae et al. [11,14] proposed the CODAS approach, which uses primary Euclidean distance and Taxicab distance as the secondary measures for decision-making, and the fuzzy CODAS approach and linguistic variables for the evaluation of market segments. Bolturk et al. [15] proposed a comparative study in the manufacturing industry for the selection of suppliers based on Pythagorean fuzzy-based CODAS and ordinary fuzzy CODAS. Mathew et al. [12] studied CODAS for choosing two material handling equipment according to the weighted aggregated sum product assessment approach. Stojci et al. [13] discussed a review paper based on applications of multiple-criteria decision-making approaches in the field of sustainable engineering using classification into five factors based on transport, energy, supply chains, construction, infrastructure, and logistics. Sofuoglu et al. [16] developed a decision-making approach based on four normalization methods for the selection of cutting fluid and compared it with the Spearman correlation test. In comparison to other MCDM methods such as TOPSIS and evaluation based on distance from average solution (EDAS), CODAS technique of using

two distances provides it with a more desirable feature to reach its conclusion [17]. It has been extensively used in various fields and have proved its feasibility and efficiency [17,18]. The CODAS multi-criteria decision-making method has shown promising potentials for optimally selecting machining parameters in non-conventional manufacturing [18,19].

Data-driven models are more effective due to their computing power, high reliability, and easier data acquisition [20]. Soft computing methods are used for modelling machining processes as they are robust and yield reliable and accurate solutions, becoming an alternative method to conventional statistical methods. To achieve higher machining performance, it will be necessary to adjust the cutting parameters autonomously and adapt to current situations. Machine learning and deep learning play a critical role in the development of intelligent systems for descriptive, diagnostic, and predictive analytics for machine tools and process health monitoring. In example, fuzzy logic systems were used to predict machining settings for metal alloys for different type of machining (turning, drilling and ultrasonic vibration assisted turning) and proved that it is capable of being an accurate prediction method [21,22]. Artificial intelligence (AI) models are robust and reliable systems that are more proficient in reducing time and cost and are suitable for the optimization of complex machining operations [8]. AI models have been used for the estimation of response factors for varied materials and alloys. Muthuram et al. [23] suggested a hybrid predictive model in turning for titanium alloy using artificial neural network (ANN) and genetic algorithms for the prediction of metal removal rate (MRR) and surface roughness. Shivakotia et al. [24] conducted adaptive neuro-fuzzy inference systems (ANFIS) modeling and experimental work in turning for stainless steel 202, based on the Taguchi method for estimating surface integrity and metal removal rate. Sofuoglu et al. [25] developed a suitable cutting depth in turning without chatter vibrations for AISI 1050 steel. Sada et al. [26] suggested a comparative analysis between ANN and ANFIS in turning for AIS steel to estimate tool wear and MRR and indicated that ANN is relatively better as compared to the ANFIS approach, based on prediction errors. Gopal [27] presented the effect of tool geometry in turning using ANN and RSM to predict temperature for aluminum-6061 by an  $Al_2O_3$  coated carbide tool. Chiu et al. [28] studied an intelligent machining system according to the hybrid PSO and an ANFIS predictor using speed, accuracy, and surface smoothness. Literature shows that a limited amount of work was conducted using ANN, hybrid ANFIS-PSO, and optimization of cutting factors by combinative distance-based assessment method for optimization of process parameters for 825 alloy.

This paper focuses on using several optimization and prediction artificial intelligence-based meta models investigating three processing parameters (cutting speed, feed rate and depth of cut) to optimize the machining behavior in turning high-strength metal 825 alloy. This is the first paper, to the authors best of knowledge, to consider CODAS optimization model to select the best configuration to machine 825 alloy. In addition, three different prediction models (regression, ANFIS, and ANN) were considered and compared. A hybrid ANFIS-PSO prediction/optimization model was used to train the neural fuzzy network and optimize machinability of Inconel 825. The selected output factors were resultant force, metal removal rate, and specific cutting energy, to understand the impact of cutting parameters.

## 2. Materials and Methods

Experimental procedures and setup were accomplished according to Figure 1. The Kennametal PVD-coated TiAlN coated carbides were selected as CNMG 120408 MS Grade KCU10 with a nose radius of 0.8 mm intended to machine super alloys with DCLNR2525M12 tool holder [29].

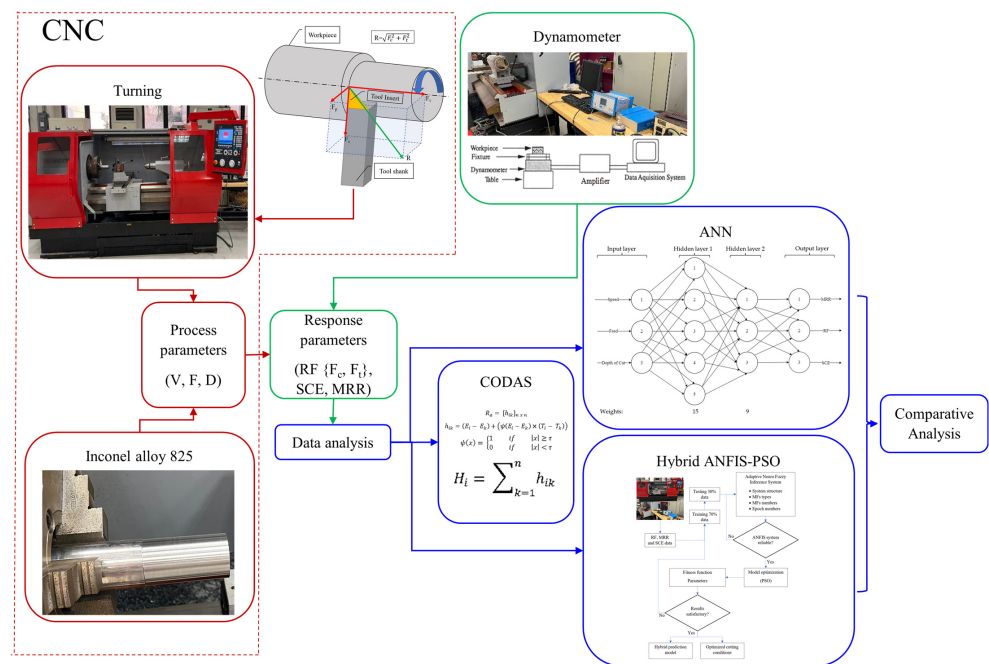


Figure 1. Experiment schematic representation and setup.

The trials were conducted in an orthogonal cutting setting using a CNC lathe EMCO MATE 300 (EMCO, Hampshire, UK) in dry cutting condition. Inconel 825 alloys are chemically composed of ~23% chromium, ~22% iron, 3% molybdenum, ~3% copper, ~1% manganese, ~1.2% titanium, 0.2% aluminum, 0.5% silicon, 0.05% carbon, 0.03% sulfur, and balanced percentage with nickel. The properties of the 825 alloy are represented in Table 1. The dimensions of the considered workpiece were 300 mm in length and 70 mm in diameter. A Kistler tool dynamometer (Kistler Instrument Corp., Amherst, NY, USA) was used to measure the cutting force and the thrust force.

Table 1. Physical, mechanical, and chemical properties for 825 alloys.

Properties	Values
Poisson’s ratio	0.29–0.34
Density (gm/cm <sup>3</sup> )	8.14
Yield strength (MPa)	310
Hardness Brinell (HB)	190–240
Elongation (%)	45
Tensile strength (MPa)	690
Melting point °C	1370–1400

To determine the resultant force, metal removal rate, and specific cutting energy the following equations were considered:

$$\text{Resultant force, } RF = \sqrt{F_c^2 + F_t^2} \text{ (N)} \tag{1}$$

$$\text{Metal removal rate, } MRR = F \times D \times 1000 V \text{ (mm}^3\text{/min)} \tag{2}$$

$$\text{Specific cutting energy, } SCE = F_c / F \times D \text{ (N/mm}^2\text{)} \tag{3}$$

where  $F_c$  is the cutting force,  $F_t$  is the thrust force,  $F$  is the feed rate,  $D$  is the depth of cut, and  $V$  is the cutting speed.

### Design of Experiment

Three machining factors were experimentally considered with four levels for each factor as shown in Table 2 and using an L16 array to represent the design of the experiment study [30,31]. The focus responses in this study were resultant force, specific cutting energy, and metal removal rate. The statistical significance for factors were analyzed using ANOVA and considered a  $p$ -value of less than 0.05 (95% confidence level). The fitted models were determined to describe the experimental data and compute the determination coefficient.

**Table 2.** Levels and control factors.

Factors	Level 1	Level 2	Level 3	Level 4
Cutting speed, $V$ , m/min	45	70	95	120
Feed rate, $F$ , mm/rev	0.11	0.22	0.33	0.44
Depth of cut, $D$ , mm	0.15	0.3	0.45	0.6

## 3. Results and Discussion

### 3.1. Effect of Input Parameters

The experimental results of the L16 array are presented in Table 3. The ANOVA for the resultant force, metal removal, and specific cutting energy are shown in Table 4. The statistical analysis, ANOVA, has shown that the fitted models describe the experimental data and that the determination coefficient is high, which is an indicator of better fit for the observations. Adjusted  $R^2$  of more than 0.75 is a fair value to show the accuracy of measured data [32]. In the ANOVA, it was observed that the  $R^2$  is 0.95, 0.90, and 0.94 for RF, MRR, and SCE, respectively, presenting the fitness of the data fitness and residual's normality. Experiments have shown that the maximum resultant force were resulted at Exp.16 with 401.21 N ( $F_c = 323$  N and  $F_t = 238$  N) while minimum were in Exp.1 of 310.63 N ( $F_c = 258$  N and  $F_t = 173$  N). Further analysis showed that the average resultant force among all experiments was 366.74 N being close to what was resulting in Exp.10 and Exp.13 of 360 N ( $F_c = 300$  N and  $F_t = 199$  N) and 365.8 N ( $F_c = 293$  N and  $F_t = 219$  N), respectively. The highest contributor factor to the resultant force was feed rate of 45.52%, followed by cutting speed of 41.67% and depth of cut of 7.89%, where  $F$  and  $V$  are the significant factors ( $p \leq 0.05$ ). The results agree with the literature showing that the cutting speed and feed rate significantly influence the resultant force [33]. This means that there was an increase in the contact surface of the workpiece on the cutting tool as the depth of cut was at minimum, the cutting speed and feed rate were at the maximum level. Hence, the workpiece would have less force exerted from the tool. Overall, feed rate was observed to highly influence the resultant forces as higher forces were resulted when rate increased. The reason behind this could be the cutting tool contact rate with the workpiece is increasing, wielding higher forces. Regarding MRR, the maximum removal rate was noticed in both Exp. 7 and 8 with 13,860 mm<sup>3</sup>/min and minimum MRR resulted from Exp. 1 of 742.5 mm<sup>3</sup>/min. This is a clear indication from Equation (2), where all factors are proportionally related when increasing leads to a higher MRR. The MRR was most affected equally by feed rate and depth (38.88% contribution) and with only 12.33% contribution from cutting speed. Specific cutting energy has resulted in a maximum value of 15.64 N/mm<sup>2</sup> from Exp.1 and a minimum of 1.20 N/mm<sup>2</sup> from Exp.4. The energy was decreasing the most when increasing the feed rate and depth of cut which clearly is prescribed by the contribution of both factors of 43.04% and 47.81%, respectively. However, there is insignificant contribution from cutting speed (3.44%) to the SCE. Furthermore, the experiment showed that at speeds of 45 and 70 m/min, a feed rate of 0.11 mm/rev and a cut depth of 0.15 mm are above the average and result in higher SCE > 4.75 N/mm<sup>2</sup>. Larger SCE will require longer cutting time and will lead to higher temperature at the cutting zone leading to rapid tool wear and minimum tool life, which has a direct influence on the quality of products. A lower value of cutting energy will indicate a better and smoother machining process.

**Table 3.** Taguchi orthogonal experimental array.

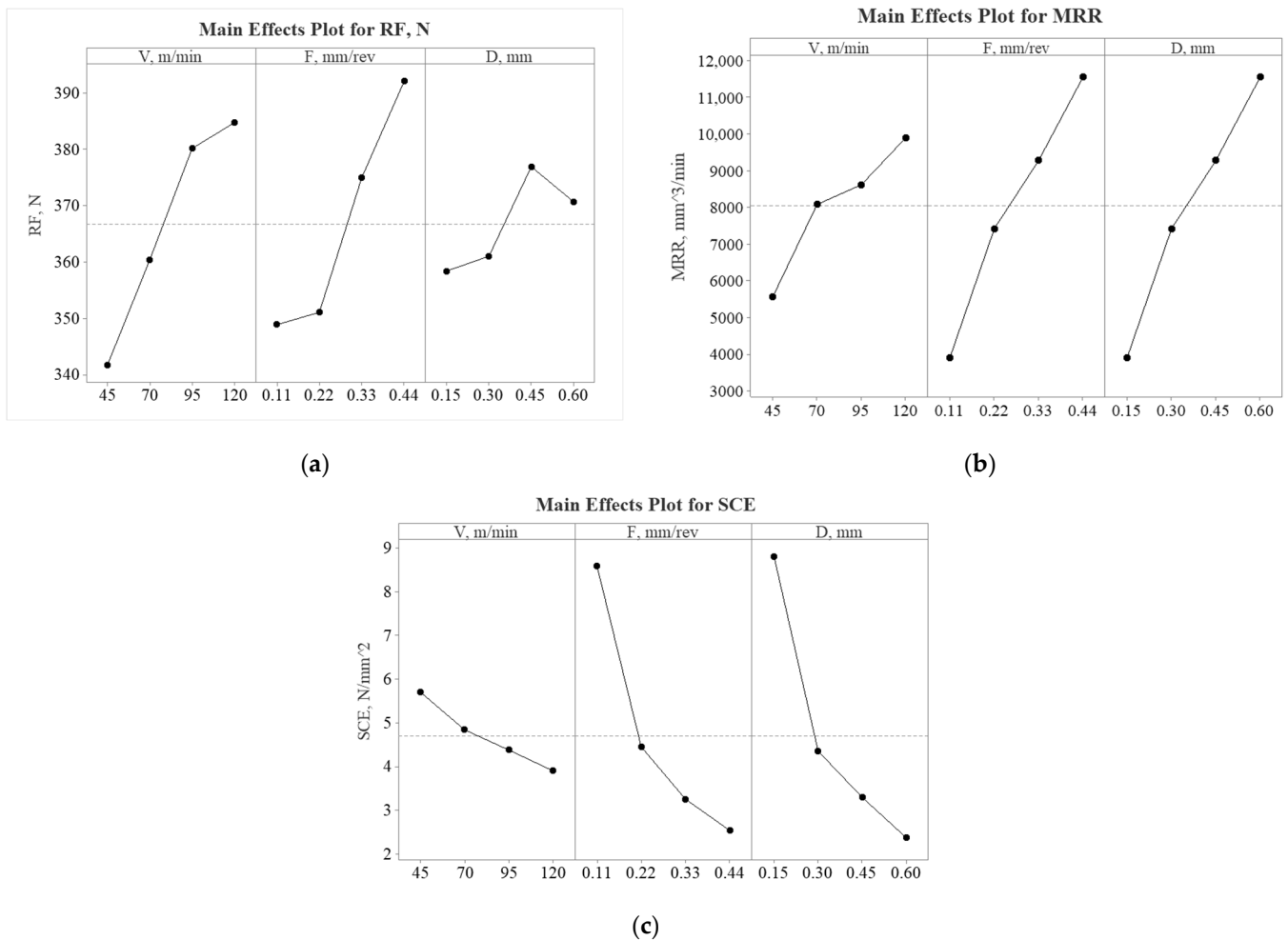
Exp. No.	V m/min	F mm/rev	D mm	F <sub>c</sub> N	F <sub>t</sub> N	Resultant Force N	MRR mm <sup>3</sup> /min	SCE N/mm <sup>2</sup>
1	45	0.11	0.15	258	173	310.63	742.50	15.64
2	45	0.22	0.3	265	184	322.62	2970	4.02
3	45	0.33	0.45	290	200	352.28	6682.50	1.95
4	45	0.44	0.6	317	212	381.36	11,880	1.20
5	70	0.11	0.3	256	215	334.31	2310	7.76
6	70	0.22	0.15	278	198	341.30	2310	8.42
7	70	0.33	0.6	310	212	375.55	13,860	1.57
8	70	0.44	0.45	319	225	390.37	13,860	1.61
9	95	0.11	0.45	323	209	384.72	4702.50	6.53
10	95	0.22	0.6	300	199	360.00	12,540	2.27
11	95	0.33	0.15	311	219	380.37	4702.50	6.28
12	95	0.44	0.3	321	231	395.48	12,540	2.43
13	120	0.11	0.6	293	219	365.80	7920	4.44
14	120	0.22	0.45	305	227	380.21	11,880	3.08
15	120	0.33	0.3	317	230	391.65	11,880	3.20
16	120	0.44	0.15	323	238	401.21	7920	4.89

**Table 4.** ANOVA for response parameters.

Resultant Force ANOVA							
Factors	DF	Seq SS	Adj SS	Adj MS	F-Value	p-Value	Contribution
Cutting speed	3	4676.9	4676.9	1558.95	16.9	0.002	41.66%
Feed rate	3	5108.6	5108.6	1702.87	18.46	0.002	45.52%
Depth of cut	3	885.1	885.1	295.05	3.2	0.105	7.89%
Residual error	6	553.4	553.4	92.23	-	-	4.93%
Total	15	11,224	-	-	-	-	100.00%
Fitness statistics		R <sup>2</sup> = 0.95				Adjusted R <sup>2</sup> = 0.88	
Metal removal rate ANOVA							
Factors	DF	Seq SS	Adj SS	Adj MS	F-Value	p-Value	Contribution
Cutting speed	3	39,625,988	39,625,988	13,208,663	2.49	0.158	12.33%
Feed rate	3	124,894,688	124,894,688	41,631,563	7.85	0.017	38.88%
Depth of cut	3	124,894,688	124,894,688	41,631,563	7.85	0.017	38.88%
Residual error	6	31,839,638	31,839,638	5,306,606	-	-	9.91%
Total	15	321,255,000	-	-	-	-	100.00%
Fitness statistics		R <sup>2</sup> = 0.9				Adjusted R <sup>2</sup> = 0.75	
Specific cutting energy ANOVA							
Factors	DF	Seq SS	Adj SS	Adj MS	F-Value	p-Value	Contribution
Cutting speed	3	17,026,069	17,026,069	5,675,356	1.21	0.384	3.44%
Feed rate	3	2.13 × 10 <sup>8</sup>	2.13 × 10 <sup>8</sup>	70,922,810	15.1	0.003	43.05%
Depth of cut	3	2.36 × 10 <sup>8</sup>	2.36 × 10 <sup>8</sup>	78,785,716	16.77	0.003	47.81%
Residual error	6	28,185,704	28,185,704	4,697,617	-	-	5.70%
Total	15	4.94 × 10 <sup>8</sup>	-	-	-	-	100.00%
Fitness statistics		R <sup>2</sup> = 0.94				Adjusted R <sup>2</sup> = 0.86	

The main effect plots of RF, MRR, and SCE are shown in Figure 2. RF and MRR has shown to be increasing with higher values of cutting speed, feed rate and depth of cut. While SCE is decreased with increasing all process factors of cutting speed, feed rate, and depth of cut. This means that SCE is inversely proportional to RF and MRR. It was noticed

that with a higher depth of cut ( $>0.45$  mm), a critical value was resulted at 0.6 mm which will cause the RF to decrease. This shows that RF, MRR, and SCE are key responses on determining the machinability of 825 super alloys and the possibility of tailoring it. SCE and MRR are one of the most important indicators of machining performance and are adequate parameters to study cutting operation, energy consumption, and understanding the machinability of materials [34]. The ideal balance is to increase the MRR and keep the force at a minimum to avoid unnecessary energy consumption.



**Figure 2.** Input parameters effect on (a) RF, (b) MRR, and (c) SCE.

### 3.2. Combinative Distance-Based Assessment Method

CODAS model considers two types of distances for selective alternatives based on multiple criteria such as Euclidean distance and Taxicab distance. The obtained distances will be in a negative-solution and the ideal scenario is based on which alternative achieves the greater distance. In this paper, the taxicab distance is selected as a secondary measure and the Euclidean distance as a primary measure. To determine the optimal setting to machine the 825 alloy using CODAS, assume that there are  $n$  experiments and  $m$  response. The required steps are considered as follows:

**Step 1:** The design decision-making matrix ( $X$ ), as represented in Table 5, was calculated by the following Equation (4):

$$X = [x_{ij}]_{n \times m} = \begin{bmatrix} x_{11} & x_{12} & \cdots & x_{1m} \\ x_{21} & x_{22} & \cdots & x_{2m} \\ \vdots & \vdots & \vdots & \vdots \\ x_{n1} & x_{n2} & \cdots & x_{nm} \end{bmatrix} \quad (4)$$

where  $x_{ij}$  ( $x_{ij} \geq 0$ ) indicates performance value for  $i$ th alternative on  $j$ th criterion  $i \in (1, 2, \dots, n)$  and  $j \in (1, 2, \dots, m)$ .

**Table 5.** Decision-making matrix Step 1: Final input table.

	Process Parameters			Beneficial	Non Beneficial	
	Speed m/min	Feed mm/rev	Depth mm	Metal Removal Rate mm <sup>3</sup> /min	Resultant Force N	Specific Cutting Energy N/mm <sup>2</sup>
Weights	-	-	-	0.5	0.15	0.35
Min	45	0.11	0.15	477	310.63	112.07
Max	120	0.44	0.6	8910	401.21	1459.39

**Step 2.** Obtain normalized decision matrix using Equation (5).

$$n_{ij} = \begin{cases} \frac{x_{ij}}{\max_i x_{ij}} & \text{if } j \in N_b \\ \frac{\min_i x_{ij}}{x_{ij}} & \text{if } j \in N_c \end{cases} \quad (5)$$

where  $N_b$  and  $N_c$  represent the set of benefit and non-beneficial criteria, respectively. The maximum values are in the beneficial area and the minimum values in the non-beneficial area are converted to 1.

**Step 3.** Calculate the weighted normalized decision matrix considering Equation (6). Using weight criteria, the values of weighted normalized performance will be obtained for estimating negative-ideal solutions and Euclidean distances between alternatives will be obtained.

$$r_{ij} = w_j n_{ij} \quad (6)$$

where  $w_j$  ( $0 < w_j < 1$ ) denotes weight of  $j$ th criteria, and  $\sum w_j = 1$ .

**Step 4.** For the experimental results, the negative ideal solution (point) is calculated by Equations (7) and (8):

$$ns = [ns_j]_{1 \times m} \quad (7)$$

$$ns_j = \min_i r_{ij} \quad (8)$$

**Step 5.** Attaining Taxicab and Euclidean distances for alternatives using negative-ideal solution, Equations (9) and (10) are used.

$$E_i = \sqrt{\sum_{j=1}^m (r_{ij} - ns_j)^2} \quad (9)$$

$$T_i = \sum_{j=1}^m |r_{ij} - ns_j| \quad (10)$$

**Step 6.** Calculate the relative assessment matrix using Equations (11)–(13).

$$R_a = [h_{ik}]_{n \times n} \quad (11)$$



$$h_{ik} = (E_i - E_k) + (\psi(E_i - E_k) \times (T_i - T_k)) \quad (12)$$

$$\psi(x) = \begin{cases} 1 & \text{if } |x| \geq \tau \\ 0 & \text{if } |x| < \tau \end{cases} \quad (13)$$

where  $k \in (1, 2, \dots, n)$ ,  $\psi$  represents threshold function for equality for Euclidean distances for two alternatives and  $\tau$  is threshold factor and is set using a decision-maker.

The suggested value range is 0.01–0.05 difference in Euclidean distances of two alternatives and is less than  $\psi$ . Afterwards, these two alternatives will be compared using a Taxicab distance. In this study, we have selected  $\tau = 0.02$  for prediction [15].

**Step 7.** An assessment score for each alternative is defined using Equation (14).

$$H_i = \sum_{k=1}^n h_{ik} \quad (14)$$

**Step 8.** Rank each alternative based on decreasing assessment value. The best optimal score is with the highest  $H_i$ .

Table 6 presents optimization of Inconel 825 turning responses with CODAS. In this study, the focus was investigating the case of MRR and its relationship with the resulted force to generate less energy during. As the main aim is to achieve better machinability with balancing the consumed energy, MRR was employed with highest impact (50% of weight) in the CODAS optimization approach, following it the SCE with 35% and RF with 15% weight. The CODAS assessment score showed that experiment 7 has the highest rank among all experiments with cutting speed of 70 m/min, feed rate of 0.33 mm/rev, and 0.6 mm depth of cut and would result in the best optimal turning condition of Inconel 825 alloy. The optimum resulted cutting speed of 70 m/min confers with the literature [35]. Kumar et al. [20] reported in special coated tools when machining Inconel 825 alloy, a higher cutting speed of 100 m/min, a lower feed rate of 0.14 mm/rev, and 0.15 mm of depth of cut will result in less tool flank wear and cutting force generation, and better surface roughness and chip formation. Furthermore, Thakur et al. [36] provided sufficient investigation of Inconel 825 in dry turning and the influence of process factors on chip morphology, chip thickness ratio, tool wear, surface, and sub-surface integrity. However, the literature mentioned focuses only on optimizing the machinability of the Inconel 825 alloy to improve tool wear, chip formation, surface roughness, cutting forces, and cutting temperatures regardless of the material and energy consumed [2,31,37–39].

### 3.3. Optimization of Neural Network Parameters

#### 3.3.1. ANN

To model the turning of Inconel 825 alloy, a feed-forward multi-layer perceptron model was considered using Easy NN-Plus V14.0g software (Neural Planner Software Ltd., Stockport, UK). During ANN, several trials were conducted to achieve the predictive model with the least relative error (RE) [40]. The ANN model used a 3-5-3-3 MLP consisting of three layers such as input layer, two hidden layers, weights of each hidden layer, and output as shown in Figure 3. The number of neurons and hidden layers were selected by trial-and-error process. The momentum was set to 0.8, learning rate 0.6, target error 0.01, and calculated up to 100,000 learning cycles. The weights between the layers were automatically set as 15 from the input layer to 1st hidden layer, 15 from 1st to 2nd hidden layer, and 9 from 2nd hidden layer to the output layer. Weights between layers were automatically set by the software [41]. Two out of sixteen experiments (12.5%) were considered to validate the neural network and the remaining percentage (87.5%) trained the network. The network was stopped at 62,801 cycles after achieving within 10% of the validating examples shown in Figure 4.

Table 6. CODAS optimization of Inconel 825 alloy turning.

Exp. (i   j)	Weight Criteria			0.15	0.5	0.35	$E_i$	$T_i$	Assessment Score	
	Normalization			Weight Normalization					$H_i$	Rank
	RF N	MRR mm <sup>3</sup> /min	SCE N/mm <sup>2</sup>	RF N	MRR mm <sup>3</sup> /min	SCE N/mm <sup>2</sup>				
1	1.000	0.054	0.077	0.150	0.027	0.027	0.034	0.034	-4.122	16
2	0.963	0.214	0.299	0.144	0.107	0.104	0.115	0.186	-2.838	13
3	0.882	0.482	0.615	0.132	0.241	0.215	0.286	0.419	-0.124	8
4	0.815	0.857	1.000	0.122	0.429	0.350	0.516	0.731	3.568	3
5	0.929	0.167	0.155	0.139	0.083	0.054	0.067	0.107	-3.602	14
6	0.910	0.167	0.143	0.137	0.083	0.050	0.064	0.100	-3.642	14
7	<b>0.827</b>	<b>1.000</b>	<b>0.764</b>	<b>0.124</b>	<b>0.500</b>	<b>0.268</b>	<b>0.531</b>	<b>0.722</b>	<b>3.813</b>	<b>1</b>
8	0.796	1.000	0.745	0.119	0.500	0.261	0.528	0.710	3.764	2
9	0.807	0.339	0.184	0.121	0.170	0.064	0.148	0.185	-2.320	12
10	0.863	0.905	0.529	0.129	0.452	0.185	0.454	0.597	2.575	4
11	0.817	0.339	0.191	0.122	0.170	0.067	0.148	0.189	-2.309	11
12	0.785	0.905	0.494	0.118	0.452	0.173	0.450	0.573	2.506	5
13	0.849	0.571	0.270	0.127	0.286	0.095	0.268	0.338	-0.410	9
14	0.817	0.857	0.390	0.123	0.429	0.136	0.416	0.518	1.968	6
15	0.793	0.857	0.375	0.119	0.429	0.131	0.415	0.509	1.946	7
16	0.774	0.571	0.245	0.116	0.286	0.086	0.266	0.318	-0.446	10
<b>Negative ideal solution</b>				0.116	0.027	0.027	-	-	-	-

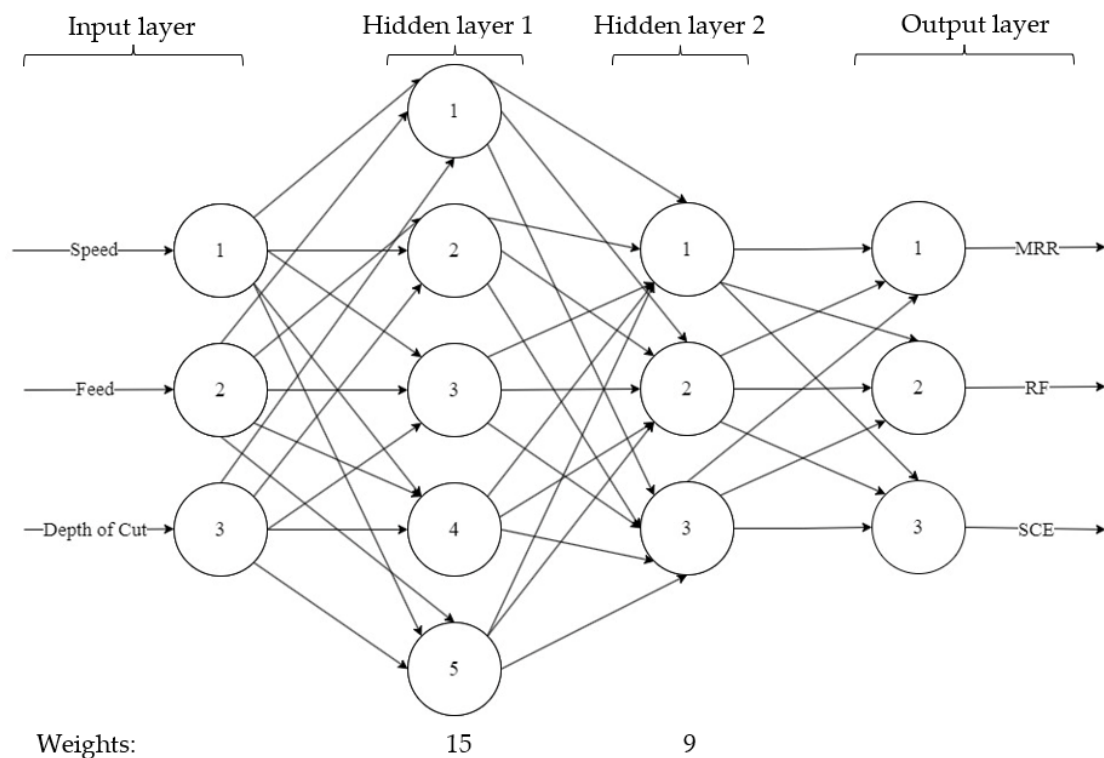


Figure 3. Artificial neural network multi-layer perceptron model.

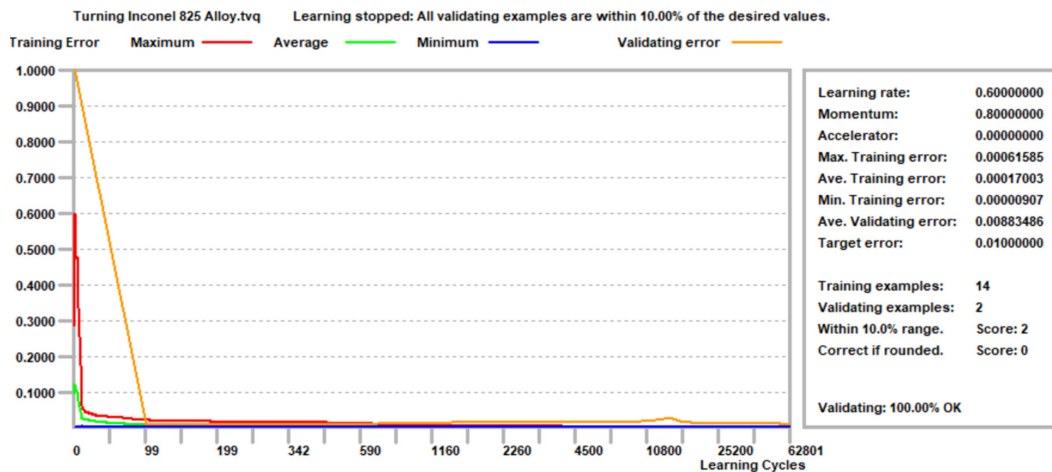


Figure 4. Neural network training and validating graph.

### 3.3.2. Adaptive Neuro-Fuzzy Inference System

The capability to develop applications of intelligent system applications is an effective approach to the estimation of prediction models for solving linear and non-linear processes. The first order Sugeno fuzzy model, identical to ANFIS, combines the least squares and back propagation gradient descent approaches. It consists of six layers as inputs, namely fuzzification, fuzzy rule, normalization, defuzzification, and summation. Figure 5 represents an output and two membership functions (MF) for each input. This network has one output,  $y$ , and two inputs,  $x_1$  and  $x_2$ . First-order polynomials are taken as output and two fuzzy sets as input. The considered four rules are as follows:

- **Rule 1:** IF  $x_1$  is A1 AND  $x_2$  is B1 THEN  $y = f_1 = k_{10} + k_{11}x_1 + k_{12}x_2$
- **Rule 2:** IF  $x_1$  is A2 AND  $x_2$  is B2 THEN  $y = f_2 = k_{20} + k_{21}x_1 + k_{22}x_2$
- **Rule 3:** IF  $x_1$  is A2 AND  $x_2$  is B1 THEN  $y = f_3 = k_{30} + k_{31}x_1 + k_{32}x_2$
- **Rule 4:** IF  $x_1$  is A1 AND  $x_2$  is B2 THEN  $y = f_4 = k_{40} + k_{41}x_1 + k_{42}x_2$

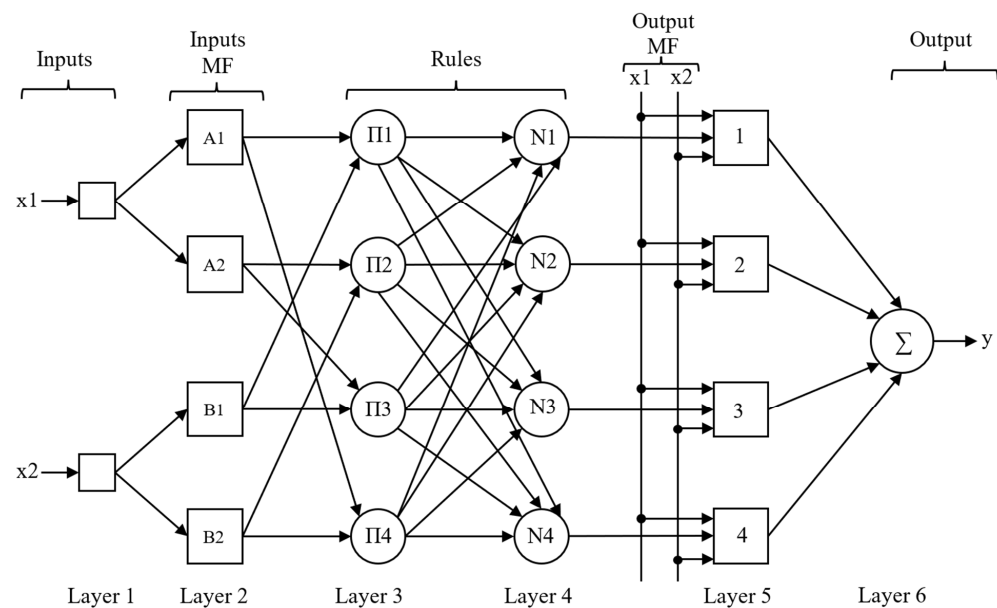


Figure 5. ANFIS model.

As shown in Table 7, **Layer 1** interprets A1, A2, B1, and B2 as membership functions. **Layer 2** has a bell-shaped structure and fuzzification neurons. Within **Layer 3**, each neuron is represented by a single sugeno-type fuzzy rule. The rule neurons obtain input from indi-

vidual fuzzification neurons and determine the firing strength of the rule. Moreover, it will indicate output of rule 1 represents firing strength. **Layer 4** is considered the normalization layer, the firing strength is the ratio of sum of the firing strengths for all rules, and the firing strength is the output of neuron  $i$ . Defuzzification **Layer 5** is a defuzzification layer where each neuron will be connected to an individual normalization neuron and determine a weighted consequent value. A single summation neuron of **Layer 6** will calculate the sum of responses for all defuzzification neurons and the actual output of ANFIS.

**Table 7.** Fuzzy inference system layering equations.

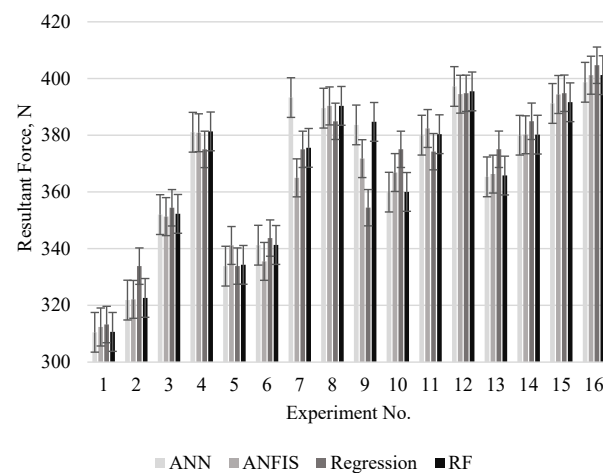
Layer Number	Equation	Layer Number	Equation
1	$y_i^{(1)} = x_i^{(1)}$	4	$y_i^{(4)} = \frac{\mu_i}{\sum_{i=1}^n \mu_i} = \bar{\mu}, (i = 1, n)$
2	$y_i^{(2)} = \frac{1}{1 + \left(\frac{x_i^{(2)} - a_i}{c_i}\right)^{2b_i}}$	5	$y_i^{(5)} = x_i^{(5)} [k_i + k_1x_1 + k_2x_2] = \bar{\mu} [k_{i0} + k_{i1}x_1 + k_{i2}x_2]$
3	$y_i^{(3)} = \prod_i = \mu_{A_j}(x) \times \mu_{B_j}(y) = \mu_i$	6	$y = \sum_{i=1}^n \bar{\mu} [k_i + k_1x_1 + k_2x_2]$
Membership function equations		Triangular = $\max\left(\min\left(\frac{x-a}{b-a}, \frac{c-x}{c-b}\right), 0\right)$	
		Trapezoidal = $\max\left(\min\left(\frac{x-a}{b-a}, 1, \frac{d-x}{d-c}\right), 0\right)$	
		Gaussian = $e^{-\frac{(x-c)^2}{2\sigma^2}}$	
		Bell-shaped = $\frac{1}{1 + \left \frac{x-c}{a}\right ^{2b}}$	
		Sigmodal = $\frac{1}{1 + e^{-a_k(x-c_k)}}$	

It should be noted that  $k_{i0}$ ,  $k_{i1}$ , and  $k_{i2}$  are result factors set (consequent parameters) for  $i$  rule and  $a_i$ ,  $b_i$ , and  $c_i$  are premise parameters,  $\mu_i$  is firing strength for rule 1 and  $n$  is the total rule neurons and  $a$ ,  $a_k$ ,  $b$ ,  $c$ ,  $c_k$ ,  $d$ , and  $\sigma$  are membership function parameter sets. For the ANFIS model, Matlab software 2022a (The MathWorks, Inc., Natick, MA, USA) was used. Evaluation criteria are based on measured data such as test data (12.5%) and training data (87.5%). Different fuzzy membership function numbers (2 2 2 and 3 3 3) and forms (triangular, trapezoidal, gaussian, bell-shaped and sigmodal) were considered and compared to minimize the model RMSE error. The fuzzy inference factors have a constant output function and 50 epochs. For the resultant force, the selected membership function factor was Gaussian with 2 2 2 resulting of an average of 1.40% RMSE and  $R^2$  of 0.96. In terms of metal removal rate, a triangular membership function form with numbers of 2 2 2 shows an RMSE of 0.0003% and  $R^2$  of 0.99. Whilst the specific cutting energy output, a trapezoidal MF type and numbers of 3 3 3 was chosen that resulted with 1.40% RMSE and 0.99  $R^2$ . In other studies, Gaussian MF have shown to be a suitable type to predict MRR and surface roughness [42]. However, MF type itself is not an important factor to shape the model performance. The most important in fuzzy logic is to break the 0–1 modeling [43]. In this study, simple shapes such as triangular and trapezoidal MF type was seen to satisfy the 0 and 1 model for MRR and SCE, respectively. Whilst resultant force showed to be modeled best when using Gaussian MF, it is known for its smoothness and concise notation [43].

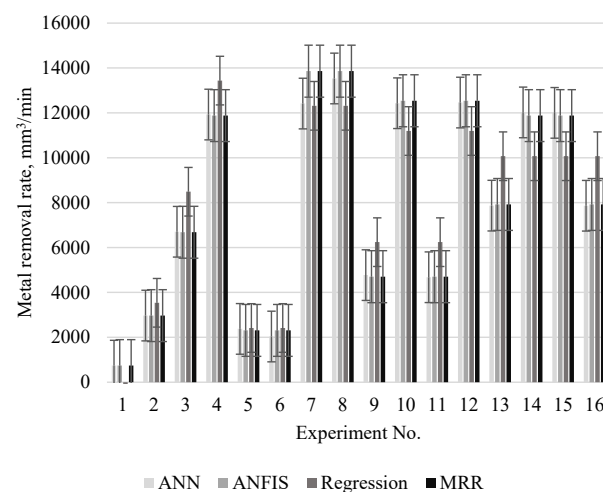
### 3.3.3. Model Efficiency and Performance Criteria

To confirm model efficiency and validity of the model, regression models were developed for all three outputs using Minitab 17.0 software (Minitab LLC., State College, PA USA). Multilinear regression analysis was considered including machining parameters (cutting speed, feed rate and depth of cut) for each response (resultant force, metal removal rate and specific cutting energy) [44]. All regression models were run using confidence interval of 95% with two-sided type, adjusted (Type III) for sum of squares and no transformation of Box-Cox transformation. The ANN, ANFIS, and regression models are presented

in Figure 6. In all cases, ANFIS and ANN presented better prediction modeling than regression. Based on different statistical error measurements, the predicted values obtained by ANN and ANFIS for are within an acceptable range of measured values for all given responses. Based on relative error, the predicted values obtained by the ANFIS method were closer to the measured values when comparing to the ANN model in cases of MRR and SCE. However, when predicting the resultant forces, ANN presented a lower RE of 0.16% against the ANFIS model 0.91%. In terms of MRR, the accuracy of the ANFIS model showed 0.0003% RE and ANN resulted in 2.21% RE. Prediction of specific cutting energy was accurately predicted by 1.18% and 8.47% RE for ANFIS and ANN models, respectively. Meanwhile, for ANN analysis, the corresponding values of the resultant force for MAE are 0.16%, RMSE 0.24%, MAPE is 0.16%, and the coefficient of correlation is 0.99. In MRR case, MAE is 2.21%, RMSE is 4.74%, and MAPE is 2.21%, and the coefficient of correlation is 0.99. The SCE ANN prediction model presented an MAE of 4.22%, RMSE of 5.17%, and MAPE of 8.47% and the coefficient of correlation is 0.99. On the other hand, in the ANFIS model, the corresponding values for the MAE of the resulting force are 0.90%, RMSE 1.40%, MAPE 0.91%, and the correlation coefficient is 0.98. In SCE, ANFIS prediction error resulted in MAE of 0.47%, 1.40% RMSE, 1.66% MAPE, and coefficient of correlation of 0.99. Whereas for metal removal rate, 0.0003% MAE, RMSE, MAPE, and coefficient of correlation of 1 were seen.

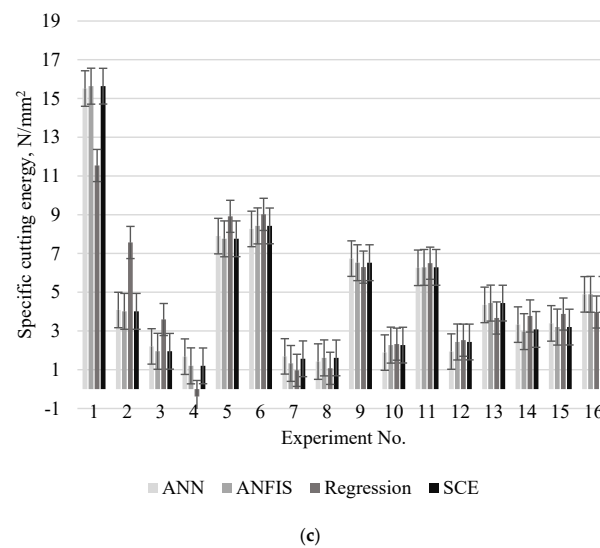


(a)



(b)

Figure 6. Cont.



**Figure 6.** Model efficiency of the ANFIS model for (a) RF, (b) MRR and (c) SCE.

The validation experiments and their prediction value for all models with errors are shown in Table 8. The ANN showed to have a better prediction model for only the SCE response while ANFIS is better for others. In the validation examples of the two experiments, overall ANFIS presented a better prediction model. However, in SCE validating examples, ANN model had lower errors. Based on statistical measurements, the ANFIS model is better than the ANN model for predicting the resultant force and the metal removal rate. Whilst ANN model is a better predictive procedure to forecast specific cutting energy of Inconel 825 alloy in turning operation. Nevertheless, according to the quantitative analysis, the developed six forecasting models are reliable and robust, and their potential for better forecasting tools can be used for hard-to-machine materials.

**Table 8.** Experimental and predicted error values of ANN, ANFIS, and regression models for all response.

Exp. No.	Resultant Force, N			Metal Removal Rate, mm <sup>3</sup> /min			Specific Cutting Energy, N/mm <sup>2</sup>		
	Real	ANN	ANFIS	Real	ANN	ANFIS	Real	ANN	ANFIS
7	376	393	365	13,860	12,418	13,859	1.566	1.689	1.326
14	380	380	380	11,880	12,023	11,879	3.081	3.328	2.968
Avg. RE%		2.32	1.49		5.81	0.0003		7.97	9.46
RMSE%		3.16	2.09		8.38	0.0003		7.80	8.70
MAE%		2.26	1.50		6.49	0.0003		7.40	8.19
MAPE%		2.33	1.49		5.81	0.0003		7.97	9.46

### 3.4. Particle Swarm Optimization of ANFIS Method

Kennedy and Eberhart introduced PSO in 1995 as one of the well-known nature-inspired optimization techniques. The first step in the PSO algorithm is to create a random population. The best values for each set of choice variables should be given for each component of nature. Each element in the solution space corresponds to a vector. In addition to the location vector, the algorithm also includes a velocity vector that forces the population to move around in the search space. The two vectors that make up velocity are pbest and gbest. The best position a particle has ever achieved is pbest, while the best position a particle in its immediate global vicinity has ever reached is gbest. Each particle in this method offers a solution after each iteration. PSO cooperates for both local and global best particles. The efficiency of PSO will be determined by the right formulation of

the fitness function. The mathematical description of PSO is described by the following equations:

$$\begin{cases} V_i(t+1) = wV_i(t) + C1(P_i(t) - x_i(t)) + C2(g(t) - x_i(t)) \\ x_i(t+1) = x_i(t) + V_i(t+1) \end{cases} \quad (15)$$

$$V_{ij}(t+1) = wV_{ij}(t) + r_1C_1(P_{ij}(t) - x_{ij}(t)) + r_2C_2(g_j(t) - x_{ij}(t)) \quad (16)$$

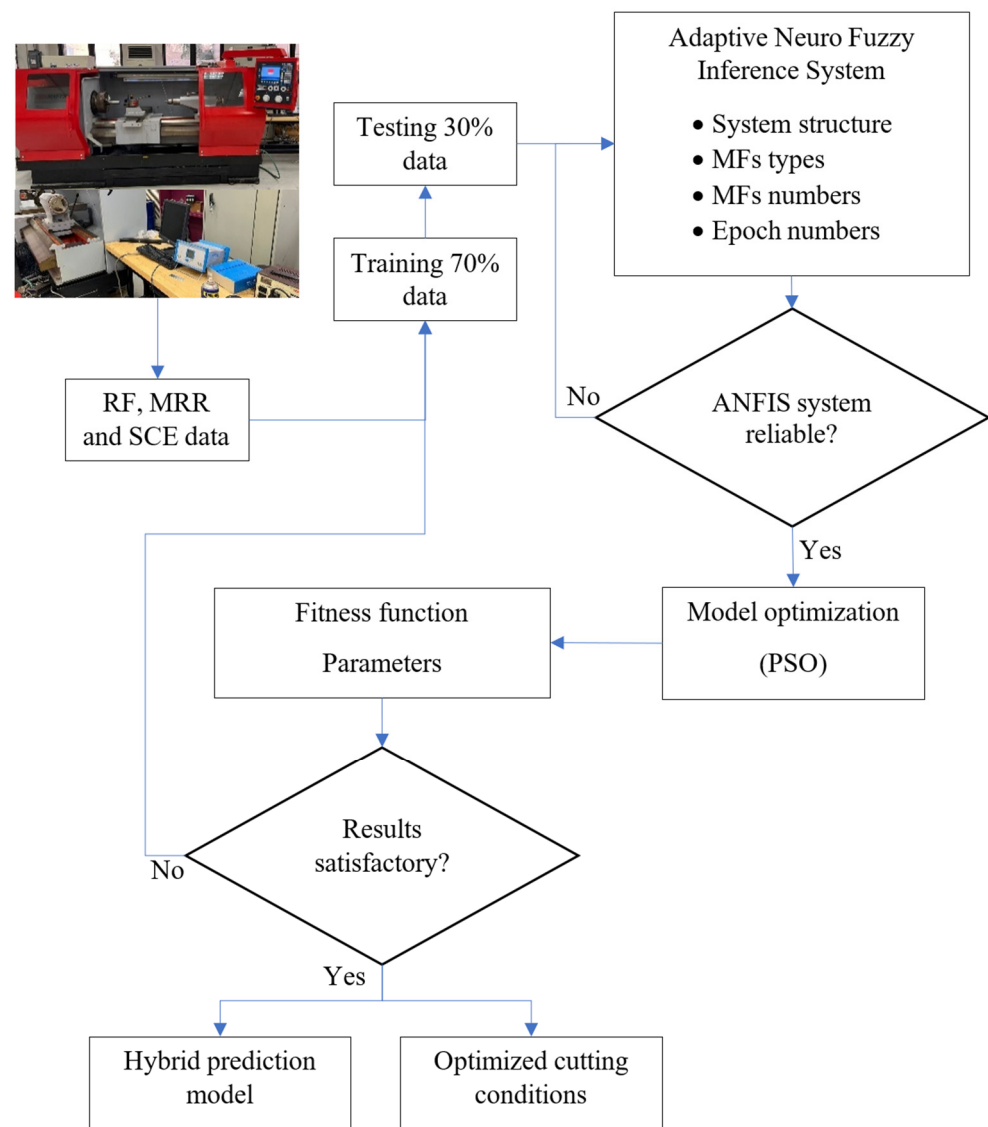
$$x_{ij}(t+1) = x_{ij}(t) + V_{ij}(t+1) \quad (17)$$

where  $V_i$  is the velocity of each particle  $i$  in function of time,  $x_i$  is the particle position that belongs to particle population  $\in X$ ,  $w$  is the inertia weight,  $P_i(t)$  is the best experience of particle  $i$ ,  $g(t)$  is the common experience among the members of swarm,  $r_1$  and  $r_2$  are random numbers in the range of 0 to 1,  $C_1$  and  $C_2$  are acceleration coefficients and named personal learning coefficient and global learning coefficient, respectively.

The output and input parameters will be correctly mapped by the fitness function. As a fitness function, the predicted model for the output is employed. The ANFIS-PSO framework is presented in Figure 7. In comparison to the hybrid method, the traditional mathematical/statistical model may not be successful in mapping complicated manufacturing processes. The input data and measured data are considered when choosing the training parameters for ANFIS to increase the predictive model's accuracy. ANFIS is evaluated considering 135 different models of different membership types (Triangular, Trapezoidal, Gaussian, Bell-shaped, Sigmoidal) and numbers (2, 2, 2 to 4, 4, 4) during testing 30% of the experimental data that is correlated with RMSE to determine the lowest testing error for selecting effective learning factors. Furthermore, PSO factors are configured for the execution of optimization iterations as shown in Table 9 that comprises of fitness function and constraints of output responses based on the ANFIS model [45,46]. Every particle in the swarm acts as a solution and communicates with other particles to improve their quality. In the optimization process, swarm initialization will be proceeded by evaluation and density assessment solutions. The pbest method compares each particle's present position to its previous pbest position. In contrast, the gbest approach uses undominated solutions that were modified in the prior phase. In this study, the developed ANFIS-PSO Matlab code [47] was modified according to this study requirements and is used to minimize the resultant force and specific cutting energy whilst maximize the metal removal rate for improved machinability of Inconel 825 alloy.

**Table 9.** Parameters of PSO.

No.	Parameters	Value
1	Population size	100
2	Epoch	50
2	Inertia weight	1
3	Inertia weight damping ratio	0.99
4	No. of iterations	1000
5	Number of variables	3
6	Personal learning coefficient (C1)	1
7	Global learning coefficient (C2)	2
8	Lower range	45 m/min, 0.11 mm/rev, 0.15 mm
9	Upper range	120 m/min, 0.44 mm/rev, 0.6 mm



**Figure 7.** ANFIS-PSO framework.

Evaluation of the ANFIS model of the testing data resulted in the least RMSE of 7.84% resulted for the RF response using the triangular membership type with 3 2 2 membership numbers. For SCE, the bell-shaped membership type and 3 4 2 numbers resulted in the least RMSE error of 7.03%. Lastly, MRR ANFIS-PSO model, triangular membership type with 2 2 2 numbers showed the minimal RMSE error of 0.77%. The optimum levels proposed for hybrid ANFIS-PSO for the factors considered and their predicted values are shown in Table 10. Optimization of the parameters for the resultant force (82, 0.11, 0.15) and the predicted value is 242 N. The PSO entails that a slight increase in speed with the least value feed and depth of cut would result in the minimum resultant force. While in the case of MRR (101, 0.43, 0.54), the predicted value is 24,145 mm<sup>3</sup>/min. The MRR optimum configuration presents a meaningful outcome as both the feed rate and the depth of cut are the main contributors, as shown in the ANOVA analysis in Table 4. In case of SCE, the optimum parameters are (45, 0.44, and 0.6) with a prediction of 1.20 N/mm<sup>2</sup> with 0% relative error. These optimal levels of SCE are consistent with the statistical method considered for ANOVA. The PSO predicted that reducing cutting speed along with maximizing feed rate and depth of cut would result in the lowest specific cutting energy [48]. This shows that the hybrid model of ANFIS-PSO is a viable approach to predict and optimize the machining of Inconel 825 alloy concurring with other studies [40].



**Table 10.** Optimum parameters by ANFIS-PSO.

Response	Speed m/min	Feed mm/rev	Depth mm	Predicted	Actual	% RE
Resultant force	82	0.11	0.15	242		N/A
MRR	101	0.43	0.54	24,145		N/A
SCE	45	0.44	0.6	1.20	1.20	0

#### 4. Conclusions

For this research work, the effects of input factors on resultant force, specific cutting energy, and metal removal rate based on the L16 array are investigated. The scope of this study is to optimize the machining parameters for the Inconel 825 alloy and create a reliable and robust prediction model. The machine parameters were optimized using statistical analysis, CODAS, and ANFIS-PSO approaches. The prediction model was created using the ANN, ANFIS, and hybrid ANFIS-PSO approach. These meta-heuristic algorithms are computational intelligence methods commonly used for the optimization and prediction of machining parameters. This research paper presented and contributed several contributions to knowledge and is summarized as follows:

- As shown in Figure 2, optimized parameters can be used for machining the 825-super alloy by increasing the cutting speed to 120 m/min, feed rate to 0.44 mm/rev, and depth of cut to 0.4 mm which consequently will increase the metal removal rate, reduce energy consumption, and satisfy the requirements of green manufacturing.
- Given in Table 6, the optimized parameters resulted by the CODAS to improve Inconel 825 machinability (i.e., increase MRR and decrease SCE) were to set the cutting speed to 70 m/min, feed rate to 0.33 mm/rev, and depth of cut to 0.6 mm.
- In Table 10, the ANFIS-PSO model shows that minimizing RF optimum parameters were 82 m/min cutting speed, 0.11 mm/rev feed rate, and 0.15 m depth of cut. To maximize MRR, ANFIS-PSO resulted the factors to be set at 101 m/min cutting speed, 0.43 mm/rev feed rate, and 0.54 mm depth of cut. Lastly, to minimize SCE, the optimum levels were 45 m/min cutting speed, 0.44 mm/rev, and 0.6 mm depth of cut.
- Considering statistical errors and based on the provided data in Figure 6, the hybrid model ANFIS-PSO has proved to be a better method based on comparison to other predictive models on the time factor, the lower discrepancy in assessment, and having good computational efficiency.
- According to results and the literature, data-driven models have shown high potential in predicting and measuring machining parameters more accurately compared to analytical and statistical methods. The developed hybrid ANFIS-PSO method can be implemented for different super alloy in complex machining processes, including grinding, milling, and non-traditional machining processes. Further analysis of work-piece surface roughness, chip formation, and cutting temperature must be considered to increase the intelligence of the proposed prediction model.

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