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Abstract: The installation of high-pressure jet grout piles induces significant lateral soil displacement, which can adversely affect nearby structures, such as diaphragm walls. Based on field tests, this study systematically analyzes the lateral displacement of soil caused by two distinct grouting techniques: the intelligent sensing super jet pile (SJT) technique and the Rodin jet pile (RJP) technique. Experimental results show that the SJT technique induces less disturbance to surrounding soil, with a maximum lateral displacement of approximately 6 mm at the closest inclinometer and an influence range limited to about 4 m. A theoretical model, based on passive pile theory, was developed to predict the lateral deflection of diaphragm walls due to adjacent jet grouting. Using a finite difference algorithm, bending moments on the walls were calculated and compared to measured data, showing a consistent correlation between predictions and observations. These findings are crucial for the design and construction of jet grout piles near sensitive structures, ensuring the safety and reliability of soil improvement practices and underground engineering.

Keywords: jet grout piles; soil improvement; lateral displacement; diaphragm wall; passive pile; deflection differential equation

1. Introduction

As cities expand and infrastructure projects increase in scale, urban underground space is becoming increasingly congested, complicating underground engineering efforts [\[1,](#page-14-0)[2\]](#page-14-1). This congestion leads to more frequent interactions between construction activities, such as adjacent construction and undercrossing projects, which heighten concerns about the safety of underground structures [\[3](#page-14-2)[,4\]](#page-14-3). Engineering activities such as construction loading, pit excavation, and pile driving can negatively impact nearby structures, leading to increased internal forces, deformation, and cracking. These effects compromise structural integrity and may result in catastrophic failures [\[5,](#page-14-4)[6\]](#page-14-5). Notable incidents include the displacement of bridge piers due to subgrade filling of a highway in Lianyungang [\[7\]](#page-14-6), and the collapse of the Nicoll Highway in Singapore during the MRT Circle Line construction in 2004, which claimed four lives [\[8\]](#page-14-7). These cases highlight the need for soil improvement techniques that enhance soil strength and deformation resistance while minimizing adverse impacts on surrounding structures.

High-pressure jet grouting is one of the most widely used and effective soil improvement techniques. This method involves injecting high-pressure cement slurry into the soil to create high-strength grout columns, which enhance load-bearing capacity and soil impermeability [\[9](#page-14-8)[–11\]](#page-15-0). Due to its small construction footprint, low vibration, and minimal noise, jet grouting is ideal for projects subject to strict environmental and deformation controls, making it especially valuable in urban settings. However, jet grouting can also induce considerable ground disturbances, including ground deformation and surface heave, particularly in soft soil regions [\[12,](#page-15-1)[13\]](#page-15-2). Grouting pressures reaching tens of megapascals, combined with the injection of large grout volumes, compress surrounding soil,

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causing ground displacement that may affect nearby underground pipelines, walls, and buildings [\[14,](#page-15-3)[15\]](#page-15-4).

The potential impacts of jet grouting on the surrounding environment, particularly on diaphragm walls, have prompted extensive research [\[16–](#page-15-5)[19\]](#page-15-6). These studies have employed various methods, including field observations, numerical simulations, and semi-theoretical and semi-empirical approaches. Field observation methods allow for the assessment of jet grouting disturbance patterns, enabling the development of empirical prediction formulas [\[20–](#page-15-7)[22\]](#page-15-8). However, these findings are often specific to certain ground conditions, limiting their general applicability across diverse projects. For example, Fontanella et al. [\[21\]](#page-15-9) noted that jet grouting within retaining structures of excavation sites can cause significant outward displacement of diaphragm walls, whereas the excavation process typically induces inward deformation. Wong et al. [\[22\]](#page-15-8) reported that while diaphragm walls are effective in limiting displacements caused by jet grouting, the grouting process can generate bending moments in the walls that exceed 1000 kN·m/m. Numerical simulations allow for comparisons with field monitoring data, yet their practical application in engineering is often hindered by the complexity of input parameters. Feizi et al. [\[23\]](#page-15-10) used numerical modeling to study the effects of grout pressure and flow rate on surrounding ground conditions, while Dong et al. [\[24\]](#page-15-11) analyzed the impact of jet grouting on diaphragm walls, finding that it induces substantial lateral movements and bending moments. Semi-theoretical and semi-empirical methods, such as the cavity expansion theory in an infinite soil mass, have also been applied to characterize the jet grouting process [\[18](#page-15-12)[,25\]](#page-15-13). However, these approaches typically overlook the presence of nearby structures, limiting their predictive accuracy. Despite extensive monitoring and simulation efforts, theoretical research remains limited, especially regarding the detailed mechanisms of soil–structure interaction during grouting. This gap highlights the urgent need for models that can more accurately capture the complex interactions between soil movements caused by grouting and the responses of adjacent structures.

The lateral displacement imposed on diaphragm walls due to jet grouting can be considered as a "passive pile problem" [\[26–](#page-15-14)[29\]](#page-15-15), where the load on the structure arises from soil movement rather than external forces directly acting on the wall itself. In this context, the diaphragm wall passively resists the soil displacement. Soil movement is the primary driver in passive pile problems, and it can be analyzed using methods like the two-stage analysis approach [\[30–](#page-15-16)[32\]](#page-15-17). This approach evaluates the lateral effects of soil on the structure by first determining the free displacement field of the soil under external loads and then applying this displacement to the passive piles. Considerable research has been conducted on passive pile issues [\[33–](#page-15-18)[36\]](#page-15-19). For instance, Zhang et al. [\[37\]](#page-15-20) derived mathematical expressions for passive pile behavior by establishing control equations for pile–soil interaction, while Hu et al. [\[38\]](#page-15-21) utilized *p*-*δ* and *p*-*y* curves to simulate the pile– soil interaction, presenting an elastoplastic solution. Additionally, Zhao et al. [\[39\]](#page-15-22) used numerical simulations to explore the effects of soil–structure interaction on passive pile behavior under different loading conditions, providing valuable insights into deformation patterns and load distribution.

In summary, the lateral effects of jet grouting on diaphragm walls have become a significant concern that requires careful control. Current studies lack effective methods for evaluating and predicting this impact before design and construction. Additionally, the interactions between jet grout piles, soil, and structures remain insufficiently understood, creating challenges for engineering practice. In the case of the south anchorage of the North Channel Bridge of the Zhangjinggao Yangtze River Bridge, the design involves installing jet grout piles after constructing circular diaphragm walls. This paper investigates the soil displacement induced by jet grouting and proposes a method to assess its impact on diaphragm walls.

2. Background and Nantong (see Figure 1). This project starts from the G40 Shanghai–Shanghai–Shanghai–Shanghai–Shanghai–Shanghai–Shaanxi Express-Shanghai–Shanghai–Shanghai–Shanghai–Shanghai–Shanghai–Shanghai–Shanghai–Shanghai–Shanghai–S

2.1. Project Overview

The Zhangjinggao Yangtze River Bridge, located about 28 km downstream of the Inc Zhangjinggao Tangize Kiver Bridge, ioeated about 20 Km downstream of the south approximation and into the south approximation and α Nantong (see Figure 1). Th[is](#page-2-0) project starts from the G40 Shanghai-Shaanxi Expressway and ends at the S82 Port Expressway, spanning a total length of about 29.8 km. It is divided into three parts: the cross-river bridge and the south and north approach lines; the divided into three parts. The cross-river bridge and the south and north approach lines, the
river-crossing section comprises the north approach bridge, north channel bridge, middle approach bridge, south channel bridge, and south approach bridge; and the south and north channel bridges feature a double-tower, two-span suspension system with spans of 2230 + 717 m and a double-tower, single-span suspension system with a main span $\frac{1}{2200} + 717$ in and a double-lower, single-span suspension system with a main span of 1208 m, respectively. Diaphragm wall foundations are employed for the foundations of the south and north anchorages of the south channel bridge and the south anchorage of the north channel bridge, with soil improvement to enhance the bearing capacity and impermeability of the bearing layer [\[40\]](#page-16-0). For the south and north channel bridge towers, mipermeabinty of the bearing layer profession and north channel bridge towers,
bored pile group foundations are employed, incorporating post-grouting techniques at the pile tips to enhance bearing capacity and reduce settlement. and the S82 Port Expressway, spanning a total length of about 20.8 km. It is is in the spanning a total length of about 29.8 km. It is is in the spanning a total length of about 20.8 km. It is is in the spanning and spann

Figure 1. Location of Zhangjinggao Yangtze River Bridge. **Figure 1.** Location of Zhangjinggao Yangtze River Bridge.

2.2. Geological Conditions

This study focuses on the foundation of the south anchorage of the North Channel Bridge, located on an alluvial island in the river. The strata primarily predominantly of guated only and that sine day, which becaused tayers of siny stated. The apper strata range from loose to slightly dense, the middle strata range from slightly dense to moderately dense, and the lower strata are dense. The Quaternary cover layer is notably thick, with bedrock buried [d](#page-3-1)eeper than 120 m. As shown in Figure 2 and Table 1, the typical geological
Clear to the the total than 120 m. As shown in Figure 2 and Table 1, the typical geological prome materies that the weak overbanden manny comprises sity easy, characterized by
low strength, low friction coefficient, poor plasticity, high compressibility, and a thickness ranging from 43.8 to 50.5 m. The sand layers, starting from level \mathcal{O}_5 and below, are confined aquifers with a high water head, buried 1.6 to 3.25 m below the surface. Quaternary alluvial silt clay, with localized layers of silty sand. The upper strata range profile indicates that the weak overburden mainly comprises silty clay, characterized by

Figure 2. Geological profile of the south anchorage of the North Channel Bridge. **Figure 2.** Geological profile of the south anchorage of the North Channel Bridge.

Layer	γ (kN/m ³)	$w(\%)$	c (kPa)	φ (°)	E_s (MPa)	SPT(N)
(2) Silt sand	19	26	3.1	27.9	10.81	6
\mathcal{Q}_2 Silty Clay	18.4	34	12.2	6.9	4.25	6
$\textcircled{4}_2$ Silty Clay	18.2	33	12	8	3.97	10
5 Silty Clay	18.3	31	14	8.2	4.35	15
7) ₅ Silty Sand	19.7	18	3.3	29	12.36	>50
(7) Medium Sand	19.8	18	$\overline{4}$	28.3	14.01	47
(8) Coarse Sand	20.3	11	3	28.5	13.08	>50

Table 1. Soil profiles at the project site. **Table 1.** Soil profiles at the project site.

2.3. Anchorage Design 2.3. Anchorage Design

in Figure [3,](#page-4-0) the foundation adopts circular diaphragm walls with an outer diameter of 90 m and a thickness of 1.5 m, along with an annular reinforced concrete inner lining support structure. The foundation is 21 m high, with a 0.3 m thick plain concrete pad underneath, and the excavation depth of the pit is 21.3 m. The foundation includes a 7 m thick top slab, a
 $\frac{1}{2}$ at the base, 32 empty chambers of 6 m \times 6 m are set in the front half of the foundation core. Below the foundation is a 27.5 m thick artificially treated ground, located in the dense silty sand layer $\textcircled{7}_5$. Jet grouting was applied to improve an approximately 6000 m² circular area within the diaphragm wall. A total of 2497 jet grout piles were installed, each 2.5 m in diameter with 1.8 m spacing and 0.7 m overlap. Based on the geological conditions and the overall design of the anchorage, as shown 7 m thick bottom slab, and a 7 m high concrete core. For the uniformity of stress distribution

3. Lateral Displacement of Soil Induced by Jet Grouting 3. Lateral Displacement of Soil Induced by Jet Grouting

A field test was conducted to investigate free soil displacement induced by jet grouting. The experiment included two groups, each involving the installation of five jet grout piles labeled sequentially from 1# to 5#, as shown in Figure [4.](#page-5-0) Each pile had a diameter of 2.5 m, with an overlap of 0.5 to 0.7 m between adjacent piles, and extended to depths between between 27 m and 56 m. Different construction techniques were used in the two groups: 27 m and 56 m. Different construction techniques were used in the two groups: Group A employed the Intelligent Sensing Super Jet Pile (SJT) technique, while Group B used the Rodin Jet Pile (RJP) technique. The SJT method is an improved version of the RJP method.
Rodin Jet Pile (RJP) technique. The SJT method is an improved version of the RJP method. By integrating advanced sensors and intelligent algorithms, the SJT technique enables realtime adjustments of construction parameters, supporting quality control and automation

during grouting. Furthermore, its use of a larger pre-drilling hole diameter helps to reduce lateral effects on surrounding soil, making it a more adaptive and controlled approach.

Figure 4. Layout of piles and inclinometers. **Figure 4.** Layout of piles and inclinometers. **Figure 4.** Layout of piles and inclinometers.

3.1. Monitoring of Lateral Displacement 3.1. Monitoring of Lateral Displacement 3.1. Monitoring of Lateral Displacement

and orientation shown in Figure [4.](#page-5-0) Six inclinemeters, each 56 m long, were positioned 1.5 m from the jet grout piles: three for Group A (labeled A-CX1, A-CX2, A-CX3) and three for Group B (labeled B-CX1, B-CX2, B-CX3). In Figure 4, the [Y](#page-5-0) direction represents radial displacement, the X direction represents tangential displacement, and Y+ indicates displacement along the jetting direction. The inclinometer has an accuracy of $\pm 0.05\%$ of full scale, with a total system accuracy of ± 3 mm over a 30 m range. Inclinometers were used to monitor the lateral soil displacement, with their layout Inclinometers were used to monitor the lateral soil displacement, with their layout

This paper focuses on soil displacement in the Y direction within the depth range of 27 to [5](#page-5-1)6 m. Figure 5 illustrates soil displacement resulting from the SJT technique, where 5#. Figure 6 s[how](#page-6-0)s the corresponding soil displacement induced by the RJP technique, $\frac{1}{2}$ denotes the $\frac{1}{2}$ corresponding for a direct comparison between the two methods. suffixes 1# to 5# denote inclinometer data recorded after the installation of piles 1# to

Figure 5. Y-direction displacement of inclinometers in Group A. **Figure 5.** Y-direction displacement of inclinometers in Group A.

Figure 6. Y-direction displacement of inclinometers in Group B. **Figure 6.** Y-direction displacement of inclinometers in Group B. **Figure 6.** Y-direction displacement of inclinometers in Group B.

3.2. Analysis of Final Lateral Displacement 3.2. Analysis of Final Lateral Displacement 3.2. Analysis of Final Lateral Displacement

After the construction of the jet grout piles, the lateral soil displacement for both Group A and Group B was monitored every 1–2 days until stabilization. Fi[gu](#page-6-1)re 7 compares the final lateral displacement in the Y direction for both groups. The maximum lateral displacements at measurement points CX1, CX2, and CX3 in Group A are approximately 6 mm, 5.5 mm, and 2.0 mm, respectively, whereas for Group B, they are around 8.5 mm, 9 mm, and 9.5 mm. These results indicate that the lateral displacement for Group A (SJT) is slightly lower than that for Group B (RJP). This reduction in or even reversal of displacement in Group A can be attributed to the SJT technique's real-time monitoring and adaptive adjustment of construction parameters, along with a slightly larger pre-drilled hole, which helps to minimize lateral pressure on the surrounding soil.

Figure 7. Comparison of Y-direction displacement between Group A and B.

3.3. Analysis of Grouting Impact Range $\mathbf{F} = \mathbf{F} \mathbf{F} \mathbf{F}$ ment is more proportional in the inclination of the inclining to the pile (CX1), compared to the pile (CX1), c

Figure [8](#page-7-0) reveals that the impact of the two grouting techniques on lateral displacement I igure o revears that the impact of the two grounng techniques on fateral displacement is more pronounced in the inclinometer closer to the pile (CX1), compared to the farther one (CX3). The CX1 hole is positioned 2.75 m away from the 1# pile, while the CX3 hole is 4.3 m away. The maximum lateral displacement at CX1 is 2–3 mm, compared to 1 mm at CX3. This suggests that the influence of grouting decreases as the distance from the pile increases, aligning with findings from other studies $[18,22,23]$ $[18,22,23]$ $[18,22,23]$. The extent and intensity of jet grouting's impact on surrounding soil are influenced by factors such as grouting pressure, with typical influence zones ranging from 1 to 20 m and resulting displacements pressure, with typical influence zones ranging from 1 to 20 m and resulting displacements varying from millimeters to meters. In this study, the lateral effect is effectively localized, varying from millimeters to meters. In this study, the lateral effect is effectively localized, successfully achieving the intended objectives of disturbance control. successfully achieving the intended objectives of disturbance control.

Figure 8. Analysis of grouting impact range for two techniques. (**a**) A-CX1-1# and A-CX3-1#. (**b**) B-**Figure 8.** Analysis of grouting impact range for two techniques. (**a**) A-CX1-1# and A-CX3-1#. CX1-1# and B-CX3-1#. (**b**) B-CX1-1# and B-CX3-1#.

3.4. Impact of Different Stages

In evaluating the impact of Pile 1# on CX1, monitoring data were assessed across three stages: pre-drilling (S1), grouting (S2), and after final stabilization (S3). As shown in Figure [9,](#page-8-0) the pre-drilling phase had a minimal impact on the adjacent soil, with an
in Figure 9, the pre-drilling phase had a minimal impact on the adjacent soil, with an a verige interar displacement of tess than 1 minimal incogretating phase caused the misst
significant effect due to the increase in pore water pressure, resulting in noticeable outward soil movement, with a peak displacement of approximately 3 mm. The final stabilized displacement fell between the values observed in S1 and S2. As the excess pore water pressure dissipated and the soil consolidated, partial recovery of the displacement was
expansion of the soil consolidated and the soil consolidated in the solid property of the displacement was pre between the values of values markete that while grounng minimy causes significant son
movement, the effect lessens over time as the soil stabilizes and consolidation occurs. sure dissipated and the soil consolidated, partial recovery of the displacement was obaverage lateral displacement of less than 1 mm. The grouting phase caused the most observed. These observations indicate that while grouting initially causes significant soil

Figure 9. Analysis of the impact of two techniques on surrounding soil. (**a**) From A-CX1-1#-S1 to A-**Figure 9.** Analysis of the impact of two techniques on surrounding soil. (**a**) From A-CX1-1#-S1 to CX1-1#-S3. (**b**) From B-CX1-1#-S1 to B-CX1-1#-S3. A-CX1-1#-S3. (**b**) From B-CX1-1#-S1 to B-CX1-1#-S3. **4. Impact on Adjacent Circular Diaphragm Walls**

4. Impact on Adjacent Circular Diaphragm Walls

Piling, loading, and excavation can induce lateral displacement in surrounding soil, which subsequently applies lateral pressure on existing structures. In particular, during jet grouting, soil displacement may impose lateral pressures on adjacent diaphragm walls, due to soil movement rather than direct external forces and can be analyzed using methods
developed for possive piles [20,22,41]. Figure 10 illustrates the approach used in this section developed for passive piles [30,33,41]. Figure 10 illustrates the app[ro](#page-15-18)ach used in this section, where soil displacements recorded by inclinometers during field tests are employed to predict the impact on diaphragm walls in the actual project. posing a passive piles problem [\[26,](#page-15-14)[28\]](#page-15-23). This lateral pressure on diaphragm walls is primarily

Figure 10. Impact of jet grouting on inclinometer and diaphragm wall. **Figure 10.** Impact of jet grouting on inclinometer and diaphragm wall.

4.1. Establishment of Theoretical Model

Based on previous studies and engineering conditions, the basic assumptions for the acting on ulaphiaght walls are as follows. forces acting on diaphragm walls are as follows:

- Fire son is assumed to be an equivalent. 1. The soil is assumed to be an equivalent homogeneous elastic body with a horizontal α horizontal
- 2. The diaphragm walls are modeled as a unit-width plate (or rod) within a homogeneous and isotropic semi-infinite elastic body;

(1)

3. The axial force N in the diaphragm walls is assumed to be constant with depth;

equation for the internal for the internal forces of the internal forces of the wall is generated:

4. The sides of the wall are assumed to be smooth, and the influence of side friction is not considered.

Figure [11](#page-9-0) illustrates the force equilibrium of a micro-segment within the diaphragm Tigue 11 mustates the force equilibrium $\sum F_y = 0$, the following equation can be obtained: $Q + q_{(z)} \cdot dz - (Q + dQ) = 0$; it can be rewritten as in Equation (1). where *z* is the depth, positive downwards; *M*(*z*) is the bending moment, positive clockwise; positive clockwise; *M*(*z*) is the bending moment, positive clockwise; $\frac{1}{2}$

Figure 11. Force equilibrium of a micro-segment within the diaphragm wall. **Figure 11.** Force equilibrium of a micro-segment within the diaphragm wall.

Taking the moment at the center of the wall section yields the following equation, $M + Q \cdot dz - (M + dM) + N \cdot (-\varphi_z) dz + q_{(z)} \frac{(dz)^2}{2} = 0$. Neglecting the second-order highstiff the and anticipreducing \tilde{f} represented by \tilde{f} order terms and differentiating yields

$$
\frac{d^2M_{(z)}}{dz^2} = \frac{dQ}{dz} - N\frac{d\varphi_{(z)}}{dz}
$$
 (2)

condition, the lateral earth pressure *q*(*z*) per unit width on the wall, caused by the con-Combining Equation (1) and $\frac{dy}{dz} = \tan \varphi_{(z)} \approx \varphi_{(z)}$, $\frac{d^2y}{dz^2} = \frac{d\varphi_{(z)}}{dz} = \frac{M_{(z)}}{E_P I_P}$ $\frac{M(z)}{E_p I_p}$, the differential equilibrium equation for the internal forces of the wall is generated:

$$
E_p I_p \frac{d^4 y}{dz^4} + N \frac{d^2 y}{dz^2} = q_{(z)}
$$
\n(3)

where *z* is the depth, positive downwards; *M*(*z*) is the bending moment, positive clockwise; *Q*(*z*) is the shear force, positive in the direction of the *y*-axis; *N* is the axial force in the wall, positive in compression; *q*(*z*) is the lateral earth pressure, positive in the direction of the *y*-axis; $\varphi_{(z)}$ is the rotation angle, where a clockwise rotation of the wall results in *dz* being positive and *dy* being negative; *E^p* is the elastic modulus of the diaphragm walls material, and I_p is the moment of inertia of the wall section.

4.2. Horizontal Subgrade Reaction Modulus on the Wall

During the jet grouting, the free displacement field of soil is denoted as *δ*. Due to the stiffness of the wall, the combined displacement of the wall and soil is represented by *y*, where $0 < y < \delta$. The difference between these two is termed constrained displacement.

According to the Winkler hypothesis and based on the wall-soil deformation coordination condition, the lateral earth pressure $q_{(z)}$ per unit width on the wall, caused by the constraint, is deconstraint, is **matured using the** *m***-method, expressed as** $\boldsymbol{\kappa}$ + , where $\boldsymbol{\kappa}$

dz dz

$$
q_{(z)} = k_h(\delta - y) \tag{4}
$$

Thus, the equilibrium differential Equation (3) can be written as

$$
E_p I_p \frac{d^4 y}{dz^4} + N \frac{d^2 y}{dz^2} = k_h(\delta - y) \tag{5}
$$

where δ is the free soil displacement adjacent to the jet grouting piles; the vertical axial force N is considered as 0; and k_h is the horizontal subgrade reaction modulus of the foundation soil, which can be determined using the *m*-method, expressed as $k_h = mz$, where *m* is the proportional coefficient of the subgrade reaction modulus and can be selected according to relevant standard [\[42\]](#page-16-2).

4.3. Numerical Solution of Equilibrium Differential Equation

From Equation (5), it is evident that deriving an analytical expression for the pile displacement *y* is quite challenging. This issue can be overcome by discretizing the equation using numerical methods. By performing numerical calculations, a series of discrete values for the pile displacement *y* can be obtained, which can then be used to determine other
your waters were as the intermal fourth of the nile Judgets derivatives foils. If for your website displacement parameters such as the internal forces of the pile. In this study, the finite difference method is parameters start as the internal refers of the pitch in this state_f, the limite americine method is
employed to discretize the differential equation, and the corresponding results are obtained using MATLABR2024a.

As shown in Figure [12,](#page-10-0) the diaphragm walls are equally divided into *n* sections along 1 1 its depth, with each section having a length of *h*. From the top to the bottom of the pile are y_0 , y_1 , y_2 , y_n , for a total of n points. For the n-th node, the second and fourth derivatives of y_i are expressed as follows: derivatives of y_i are expressed as follows: $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\ddot{\hspace{1ex}}$

$$
\begin{cases}\n\varphi_{(z)} = \frac{y_{i+1} - y_{i-1}}{2h} \\
M_{(z)} = EI \frac{y_{i+1} - 2y_i + y_{i-1}}{h^2} \\
Q_{(z)} = EI \frac{y_{i+2} - 2y_{i+1} + 2y_{i-1} + y_{i-2}}{h^2}\n\end{cases}
$$
\n(6)

Figure 12. Micro-segment of the diaphragm walls. **Figure 12.** Micro-segment of the diaphragm walls.

Substituting Equation (6) into Equation (5) yields the discrete form of the equilibrium equation at *yⁱ* :

$$
y_{i+2} + (a-4)y_{i+1} + (6+b-2a)y_i + (a-4)y_{i-1} + y_{i-2} = c\sigma
$$
 (7)

This can be briefly written as $A \times y = c\sigma$, where $a = \frac{Nh^2}{E_pI_p}$, $b = \frac{k_h\overline{B}h^4}{E_pI_p} = k_hc$, $c = \frac{\overline{B}h^4}{E_pI_p}$. $\sigma_{vz} = k_h \delta$, and \overline{B} is the equivalent width of the pile.

According to Equation (7), $n - 3$ equations can be generated, while there are $n + 1$ unknowns. Therefore, additional boundary conditions are required. Generally, the top and bottom of the pile satisfy certain constraint conditions, which can be classified as free end, hinged end, and fixed end. In this study, the top and bottom of the diaphragm wall are assumed to be fixed, meaning both displacement and rotation are constrained to zero. This assumption is based on the presence of concrete pavement at the top and a dense soil layer at the bottom, which provide effective restraint to minimize movement at both ends.

$$
\begin{cases}\n y_0 = 0 \\
 y_n = 0 \\
 y'_1 \approx \frac{y_1 - y_0}{h} = 0 \\
 y'_n \approx \frac{y_n - y_{n-1}}{h} = 0\n\end{cases}
$$
\n(8)

Two virtual points are introduced at both the top and bottom of the pile, with their corresponding *y* denoted as *y*−2, *y*−1, *yn*+1, and *yn*+2. There is a total of *n* + 5 unknowns *y*. Equation (7) provides $n + 1$ equilibrium equations. Combined with the boundary conditions determined by Equation (8), there are $n + 5$ equations in total, matching the number of unknowns. The matrix form of coefficient *A* is as follows:

$$
\begin{bmatrix}\n0 & 1 & 0 & -1 & 0 \\
0 & 0 & 1 & 0 & 0 \\
1 & a_0 & b_0 & a_0 & 1 \\
& & \ddots & \ddots & \ddots & \ddots & \ddots \\
& & & & 1 & a_0 & a_0 & 1 \\
& & & & & 1 & a_0 & a_0 & 1 \\
& & & & & & 1 & a_0 & a_0 & 1 \\
& & & & & & 0 & 0 & 1 & 0 & 1 \\
& & & & & & & 0 & 1 & 0 & -1 & 0\n\end{bmatrix}
$$
\n(9)

where $a_0 = a - 4$, and $b_0 = 6 + b - 2a$.

By solving the equations, the lateral displacement y_i at each node can be obtained, and subsequently, the corresponding rotation angle, bending moment, and shear force can be derived. The calculation formulas are as follows:

$$
\begin{cases}\n\varphi_{(z)} = \frac{y_{i+1} - y_{i-1}}{2h} \\
M_{(z)} = EI \frac{y_{i+1} - 2y_i + y_{i-1}}{h^2} \\
Q_{(z)} = EI \frac{y_{i+2} - 2y_{i+1} + 2y_{i-1} + y_{i-2}}{h^2}\n\end{cases}
$$
\n(10)

4.4. Analysis of Calculation Results

Based on the results of the field experiments described in Section [3,](#page-4-1) the design plan employs the SJT technique to reinforce the soil from 22 to 50 m below the pit bottom. Using the theoretical derivation presented in this section, along with the free soil displacement data obtained from A-CX-1-5#, the lateral deflection and bending moment of the circular diaphragm wall induced by jet grouting were predicted (Figure [9\)](#page-8-0). In the calculations, the diaphragm wall extends from a depth of 0.5 to 55.5 m, with a thickness of 1.5 m. According to the geotechnical investigation (Figure [2\)](#page-3-0) and the recommended *m* value for different soil in relevant standards [\[42\]](#page-16-2), the *m* values are assigned as follows: 3000 kN/m⁴ for 0–15 m, 5000 kN/m⁴ for 15–24 m, 10,000 kN/m⁴ for 24–47 m, 20,000 kN/m⁴ for 47–62 m, and 25,000 kN/m⁴ for 61–70 m. As shown in Figure [13,](#page-12-0) due to the disturbance caused by jet grouting, significant deflection occurs in the diaphragm wall between depths of 22 m and grouting, significant deflection occurs in the diaphragm wall between depths of 22 m and 50 m, with the predicted maximum lateral displacement reaching approximately 5 mm at a 50 m, with the predicted maximum lateral displacement reaching approximately 5 mm at depth of around 25 m. The predicted bending moment of the diaphragm wall ranges from $-1000 \text{ kN} \cdot \text{m/m}$ to 850 kN \cdot m/m.

Figure 13. The predicted lateral effects of jet grouting include free soil displacement, deflection, and **Figure 13.** The predicted lateral effects of jet grouting include free soil displacement, deflection, and bending moment of diaphragm wall. bending moment of diaphragm wall.

According to the monitoring scheme for the south anchorage of the North Channel According to the monitoring scheme for the south anchorage of the North Channel Bridge, 64 steel stress monitoring sensors were installed on the diaphragm walls. The arrangement of these monitoring points is depicted in Figure 14. [Usi](#page-12-1)ng the tensile and compressive stress of the steel bars, along with the height of the concrete compression zone, the bending moment of the diaphragm wall at different heights can be estimated. the bending moment of the diaphragm wall at different heights can be estimated.

Figure 14. Layout of steel stress monitoring points on the diaphragm walls (cm). **Figure 14.** Layout of steel stress monitoring points on the diaphragm walls (cm).

Figure 15 illustrates the bending moment at measuring point QGJ-3 on the diaphragm wall. The black lines represent th[e p](#page-12-0)redicted bending moments from Figure 13, while the other polylines represent the bending moments calculated from monitoring data at discrepancy the measured values of the measur different times. The results show a consistent trend between the predicted and measured which the results show a consistent tonia servicent the prediction distribution.

values, though the measured values are systematically higher. This discrepancy can be attributed to two main factors. First, the predictive model was based on displacement data from only five jet grout piles, whereas the actual project involved 2497 piles, leading to a cumulative lateral effect. Second, the inclinometers in the field test were positioned 1.5 m from the piles, whereas in the actual project, the piles were installed only 0.5 to 1.0 m from from the phes, whereas in the actual project, the phes were instance only 0.5 to 1.6 in nom the diaphragm wall. This reduced distance intensified the observed disturbance, resulting in higher bending moments in the monitoring data.

Figure 15. Bending moment in the diaphragm walls (kN·m/m). **Figure 15.** Bending moment in the diaphragm walls (kN·m/m).

5. Conclusions

This study provides valuable insights into the effects of high-pressure jet grout piles on surrounding soil and circular diaphragm walls, offering essential guidance for the design and construction of soil improvement projects. The main conclusions are as follows:

- 1. The influence patterns of jet grouting on surrounding soil were investigated, focusing on final lateral deformation, impact range, and different stages (pre-drilling, grouting, and stabilization). These findings enhance the understanding of lateral effects caused by jet grouting and provide essential data to support accurate assessments of ground deformation risks during the construction.
- 2. A comparative analysis shows that the Intelligent Sensing Super Jet Pile (SJT) technique causes less disturbance to surrounding soil than the Rodin Jet Pile (RJP) technique. The experimental results indicate that the SJT technique induces a maximum lateral displacement of approximately 6 mm at the closest inclinometer, with an influence range limited to around 4 m. The advantage of the SJT technique lies in its real-time monitoring and adaptive adjustment system, along with a larger pre-drilled hole, which effectively reduces lateral pressure on surrounding soil. For urban areas with strict deformation control requirements, the SJT technique is recommended, along with additional monitoring of soil and structural deformation.
- 3. This study presents a predictive method for assessing the impact of jet grouting on adjacent diaphragm walls, based on passive pile theory. Using soil displacement

data from field tests and the theoretical assumptions established in this research, the approach reliably predicts deformation and bending moments on nearby diaphragm walls. It provides a valuable reference for optimizing construction designs in similar projects.

4. For the circular diaphragm walls of the south anchorage of the North Channel Bridge, the SJT technique was employed for soil improvement. The predicted bending moments based on field test exhibited a consistent correlation with the measured data. However, the measured bending moments were generally higher than predicted, likely due to two main factors: the cumulative lateral effect from the significantly larger number of jet grout piles in the actual project, and the closer proximity of these piles to the diaphragm wall, which intensified the disturbance and resulted in higher bending moments.

Building on the findings of this study, future research could greatly benefit from advanced numerical simulation techniques to further clarify the impacts of jet grouting. Specifically, FEM models, potentially combined with PFC or DEM, could offer a highly detailed representation of the jet grouting process. Such simulations would enable the comprehensive analysis of the complex interactions between jet grout piles, surrounding soil, and adjacent structures, providing deeper insights into the lateral effects of jet grouting. Additionally, future studies could also explore different construction techniques and parameters to better understand their effects on soil and structural responses. This research would offer practical guidance for optimizing construction processes and finetuning jet grouting parameters to improve safety and efficiency in complex urban and geological environments.

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