

Article

On the Ionosphere–Atmosphere–Lithosphere Coupling During the 9 November 2022 Italian Earthquake

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Abstract: In the last decades, the scientific community has been focused on searching earthquake signatures in the Earth's atmosphere, ionosphere, and magnetosphere. This work investigates an offshore Mw 5.5 earthquake that struck off the Marche region's coast (Italy) on 9 November 2022, with a focus on the potential coupling between the Earth's lithosphere, atmosphere, and magnetosphere triggered by the seismic event. Analysis of atmospheric temperature data from ERA5 reveals a significant increase in potential energy (Ep) at the earthquake's epicenter, consistent with the generation of Atmospheric Gravity Waves (AGWs). This finding is further corroborated by the MILC analytical model, which accurately simulates the observed Ep trends (within 5%), supporting the theory of Lithosphere–Atmosphere–Ionosphere–Magnetosphere coupling. The study also examines the vertical Total Electron Content (vTEC) and finds notable fluctuations at the epicenter, exhibiting periodicities (7–12 min) characteristic of AGWs and traveling ionospheric disturbances. The correlation between ERA5 observations and MILC model predictions, particularly in temperature deviations and Ep distributions, strengthens the hypothesis that earthquake-generated AGWs impact atmospheric conditions at high altitudes, leading to observable ionospheric perturbations. This research contributes to a deeper understanding of Lithosphere–Atmosphere–Ionosphere–Magnetosphere coupling mechanisms and the potential for developing reliable earthquake prediction tools.

Keywords: earthquake; atmospheric gravity waves; ionospheric irregularities; lithosphere–atmosphere–ionosphere coupling; analytical model; Coulomb software; static displacement; trust fault; co-seismic observations



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1. Introduction

In the recent years, the scientific community's interest in predicting earthquakes (EQs) over the short term has surged. This surge is linked to the identification of certain

atmospheric and ionospheric anomalies that show a statistical relationship with seismic events as a counterpart to anomalies within the Earth's crust. Notably, changes in the density of ionospheric plasma, noted at both the lower and upper levels, hold significant potential [1,2]. As a result, numerous theories have been put forward to elucidate the interactions among the Earth's crust, the atmosphere, and the ionosphere [3–6]. The initial theory posited that radon emissions near the earthquake's epicenter (EE) could disrupt atmospheric conductivity. This disruption might lead to alterations in the atmospheric electric field, which would, in turn, modify the ionospheric plasma density profile [7–9]. The second theory suggested that oscillations near EE could produce atmospheric Acoustic Gravity Waves (AGWs). The latter have the potential to ascend and create disturbances in the ionosphere [10–14]. The last theory proposed that electrostatic effects originating in the Earth's crust could permeate the lower atmosphere, influencing the ionization state of the ionosphere [15,16].

Due to the absence of comprehensive experimental evidence to test these theories, the intricacies of how the Earth's crust, atmosphere, and ionosphere interact are still not fully understood [5,17,18]. However, models that focus on the emission of AGWs seem to hold the most promise for shedding light on this interaction, particularly in relation to seismic activities. The validity of the AGW model is bolstered by various studies that have examined changes in atmospheric pressure, magnetic field, and terrestrial movements before and during earthquakes (e.g., [1,4,6,10,12,19]). For example, the research by Korepanov et al. [20] indicated that AGWs could be a plausible mechanism for the interaction between seismic activity and the ionosphere as suggested by studies of surface atmospheric pressure and magnetic field fluctuations during weather events. In a similar vein, an analysis of the 2004 Niigata-Chuetsu earthquake using wavelet methods revealed increased fluctuations in the 10–100 min range in both surface atmospheric pressure and magnetic field data. These fluctuations fall within the AGW spectrum and were found to have disturbed the lower ionosphere [21].

Moreover, research on earthquakes such as the 2007 Niigata-Chuetsu Oki and 2008 Iwate-Miyagi events has demonstrated that when the lower ionosphere experiences disturbances, there is a noticeable increase in ground movements within the frequency ranges associated with AGWs [22]. Furthermore, detailed examinations of the Earth's crust movements during the 2011 Tohoku earthquake, which utilized Global Positioning System (GPS) data, revealed clear synchronicity with shifts in the very-low-frequency/extreme-low-frequency bands of sub-ionospheric signals and ultra-low-frequency magnetic fields [23–26].

Building upon these prior investigations, Piersanti et al. [6] recently introduced a one-dimensional analytical model of Lithosphere–Atmosphere–Ionosphere–Magnetosphere coupling. This model aims to accurately interpret ground and satellite observations both preceding and following seismic events. Central to the model is the generation of an AGW, which, as it propagates from EE through the atmosphere [14], mechanically interacts with the ionosphere, inducing a localized instability in plasma distribution via a pressure gradient [27]. Such results were confirmed also by numerical simulation using nonlinear shallow water applied to atmospheric disturbances generated by strong seismic events in [28], which found that EQ can transmit waves toward the upper atmosphere in the form of a non-vanishing AGW able to reach the ionosphere, generating changes in the local plasma density.

The present paper aims to provide a new piece of evidence regarding the generation of AGW linked to moderate-to-strong earthquakes. The interest is focused on the 9 November 2022 (hereinafter, EQ2022) earthquake that occurred offshore in the Adriatic Sea (Italy). The seismic characterization will provide the geometric and kinematic parameters of the

fault, sourcing the whole seismic sequence. The simulation of the static displacement field induced by the empirical trust fault, together with its comparison with experimental ground deformation measurements via GNSS, will be used as an initial constraint for the application of the recently developed MILC model [14]. The latter will provide an altitude map of the simulated temperature profiles to be compared with the evidenced ones. To assess the generation of AGW, the potential energy (EP) will be retrieved.

The manuscript is organized as follows: Section 2 is devoted to the characterization of the seismic event along with the simulation of the static displacement field; all the results relative to the recognized anomalies both in the atmosphere and ionosphere are contained in Section 3. A detailed discussion of the achieved results and their potential in the comprehension of the LAIC characteristics is included in Section 4.

2. The 9 November 2022 Italian Earthquake

On 9 November 2022, at 06:07 UT, an earthquake with a local magnitude (ML) of 5.7 and a moment magnitude (M_w) of 5.5 struck approximately 30 km off the coast of the Marche region in the Adriatic Sea (Figure 1a), followed by another ML 5.2 event approximately one minute later. Both events occurred along the Apennine compressional front, at a depth of approximately 5–8 km. The seismic sequence included over 400 aftershocks in the first week, 13 of which had $ML \geq 3.5$ [29]. The area affected by the seismic sequence is characterized by a complex geological structure, influenced by the convergence between the Adriatic and European plates ([30] and references therein). The Apennine Mountain range represents the main tectonic structure, with buried reverse faults extending beneath the Adriatic Sea. Seismic activity in the area has long been debated due to the buried and blind nature of these faults, which makes their identification and the assessment of their activity difficult [30]. However, historical and instrumental seismicity, including the 2012 Mirandola earthquakes (M_w 5.9 and M_w 6.1) and the sequence under study, highlighted the seismogenic character of this buried fault system ([30] and references therein).

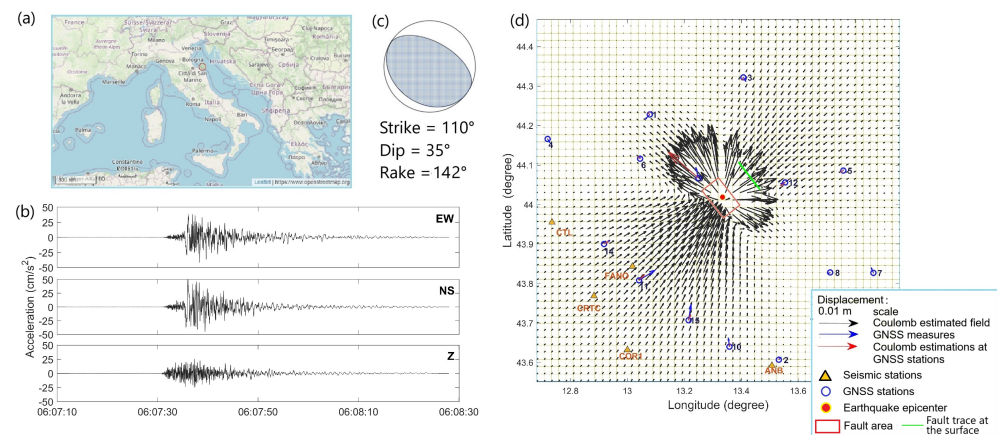


Figure 1. (a) Geographic map of Italy: the red circle indicates the epicenter of EQ2022; (b) Accelerograms acquired at FANO station (43.8434° N and 13.0183° E) along the three directions of motion: east–west (EW), north–south (NS) and vertical (Z) [31]; (c) focal mechanism indicating the nodal planes: strike = 142° , dip = 35° , rake = 110° [32]; (d) static displacement field estimated for the earthquake by using Coulomb software, over a $100 \text{ km} \times 100 \text{ km}$ grid at the sea level. The horizontal displacements measured at the GNSS stations (blue circles) and the modeled ones are represented by blue and black arrows, respectively. The GNSS stations are numbered according to Pezzo et al. [33].

Several studies used a variety of data and methodologies to analyze the seismic sequence, including the location of hypocenters, GNSS investigations [33], and seismological data elaboration [29,30,33]. GNSS measurements have allowed us to identify and model the

fault responsible for the seismic sequence. The results indicate the rupture of a reverse fault approximately 15 km long, dipping about 24° towards south-southwest [33]. Seismic data (see an example in Figure 1b) allowed the estimate of the source mechanism (Figure 1c) for this earthquake based upon the classical approach of [34]. The corresponding empirical fault geometry [31] was retrieved from the focal location leading to about $10 \times 7 \text{ km}^2$ area, dipping 35° towards south-southwest (Figure 1c), which is compatible with that individuated by GNSS measurements.

Pezzo et al. [33] performed the analysis of the magnitude distribution (Gutenberg–Richter law), revealing a relatively high b value (0.94). They interpreted that result as being due to a possible higher proportion of larger-magnitude events in that sequence. However, Spassiani et al. [35] highlighted the need for caution when interpreting this parameter as a precursor because of the high uncertainty in estimating the real-time b value.

Static Displacement Evaluation

The approach of Okada [36] can be adopted when static displacement and strain fields have to be estimated. The main assumptions regard the homogeneity and isotropy of the medium, in which both shear and tensile (both point or finite) faults produce their effects. In the context of a Poissonian half-space, the internal displacement field, caused by a dislocation across a surface, is the linear superposition of displacements due to the strain. Internal deformation field formulas are then derived for shear, tensile, and inflation/deflation sources as a function of the fault length (L), width (W), strike, dip, friction, Young's modulus (E), and Poisson's ratio (σ).

The briefly described Okada's approach [36] has been implemented in the Coulomb software developed in the Matlab environment [37]. The software is used to estimate the static displacement generated by earthquakes as well as strains and stresses induced by fault slip, magmatic intrusion, or dike expansion/contraction. These calculations are performed at a certain depth within an isotropic elastic half-space, including the free surface. In that case, a direct comparison with ground deformation measures by GPS, GNSS, or even tiltmeters [38,39] is possible.

The geometrical dimensions of the empirical fault used to estimate the static displacement vectors are listed in Table 1. Moreover, the input conditions to the Coulomb software are reported in the same table along with the seismic moment and net slip. Given the seismic moment $M_0 = 3.75 \cdot 10^{17} \text{ N}\cdot\text{m}$ (<https://esm-db.eu/>, accessed on 12 December 2024), considering the fault's area (A), the Young modulus ($E = 80 \text{ GPa}$), the rigidity ($\mu = E/[2(1 + \sigma)]$), and the Poisson's ratio ($\sigma = 0.25$), the net slip $u = \frac{M_0}{\mu A}$ is estimated to be about 0.17 m.

The simulated displacement field is reported in Figure 1d (black arrows). To validate the modeled field, we compared the values with the GNSS measures, carried out in the area (blue arrows) and reported in the supplementary information of Pezzo et al. [33].

The static displacement calculated in correspondence with the GNSS stations (Figure 1d—red arrows) fits well, in both the direction and order of magnitude, with the observed ones.

Specifically, we performed a χ^2 test, which yields good agreement within $\alpha = 0.05$ with a null hypothesis of Gaussian distribution for the residuals (mean value around 0 mm and standard deviation of 2 mm). Moreover, the direction of the estimated displacement for all the onshore GNSS stations agrees with the observed data within 45° (see Cusano et al. [38]). For the offshore stations, the discrepancy between the modeled and observed directions is significant at about half of the stations. In other words, the onshore locations better constrain the deformation pattern than the offshore ones. Since the offshore GNSS stations are located on industrial platforms, this discrepancy is likely due to the already

observed effects such as operations on the platforms, subsidence acting near the coastlines of the Adriatic Sea, together with some nonlinear local effects, etc. [40,41]. Additionally, we attribute the small observed discrepancies to local effects or lateral heterogeneity in the medium not taken into account in the model. In fact, the Okada analytic model considers a homogeneous and isotropic medium without taking into account the discontinuities due to the contact between two surficial geological units, faults, fractures, etc. [38,42]. Anyway, the obtained displacement pattern is in agreement with the compressional regional regime.

Table 1. Coulomb grid parameters used to estimate static ground displacement.

Fault Vertexes		
Corners	Latitude (°)	Longitude (°)
LL	44.0356	13.2672
UR	44.0013	13.3983
LR	43.9686	13.3428
UL	44.0683	13.3228
SL	44.1091	13.3897
SR	44.0420	13.4653
Coulomb Grid Parameters		
Grid Parameters	Value (km)	
Start—x	43.6	
Start—y	12.7	
Finish—x	44.5	
Finish—y	13.9	
x—increment	2.0	
y—increment	2.0	
Size Parameter	Value	
Plot size	2.0	
Shade/Color increment	1.0	
Exaggeration for disp. and dist.	5,000,000.00	
Cross-section default	Value (km)	
Start—x	43.6	
Start—y	12.7	
Finish—x	44.5	
Finish—y	13.9	
Distant—increment	1.0	
Z—depth	20.0	
Z—increment	1.0	
Map info (°)	Value	
min. lon	12.6826	
max. lon	13.9550	
zero. lon	13.3235	
min. lat	43.5523	
max. lat	44.4705	
zero. lat	44.0130	

3. Co-Seismic Analysis

In the following sections, we perform the coseismic analysis of the atmospheric temperature and ionospheric vTEC to check whether EQ2022 was able to produce perturbations propagating from the lower atmosphere up to the ionosphere.

3.1. Atmospheric Temperature and Acoustic Gravity Waves Evaluation

The atmospheric temperature profiles are obtained from ERA5, which is the fifth generation atmospheric dataset generated by the European Center for Medium-Range Weather Forecasts [43]. This model provides high-resolution global temperature profiles every hour, spanning from near the surface to an altitude of ~ 80 km (0.01 hPa) with 137 different pressure levels. These profiles are derived from various observational sources, including satellites, radiosondes, dropsondes, aircraft, and radars [43]. The dataset features a horizontal resolution of 0.25° in both longitude and latitude.

In this investigation, we use potential energy (E_P) as a crucial measure to assess the activity of AGW. This parameter is directly influenced by the vertical temperature profiles of the atmosphere [44,45], which are extracted from ERA5 for the particular event under consideration. We assess the E_P values using the methodology outlined by Piersanti et al. [6] and Yang et al. [46,47].

E_P [45] is defined as

$$E_P = \frac{1}{2} \left(\frac{g}{N} \right)^2 \overline{\left(\frac{T'}{\bar{T}} \right)^2} \quad (1)$$

where $g = 9.8 \text{ m/s}^2$ is the gravitational acceleration (constant with altitude), N is the Brunt-Väisälä frequency, and T' is the fluctuation with respect to the background temperature \bar{T} . These three variables are functions of altitude z and are derived from the ERA5 profiles. To retrieve \bar{T} , we make a 2 km moving average; T' is obtained by subtracting \bar{T} from the original temperature profile T .

The term $\overline{\left(\frac{T'}{\bar{T}} \right)^2}$, (a variance), is evaluated within a 2 km thick layer, using the following equation:

$$\overline{\left(\frac{T'}{\bar{T}} \right)^2} = \frac{1}{h_{max} - h_{min}} \int_{h_{min}}^{h_{max}} \left(\frac{T'}{\bar{T}} \right)^2 dh \quad (2)$$

where h_{max} and h_{min} represent the top and bottom altitudes of the layer, respectively.

Figure 2 shows the ERA-5 observations for 9 November 2022 at 06:00 UT in a geographical zone close to EE. In particular, Box A in Figure 2 presents the atmospheric temperature T (left panel), T' (middle panel) and E_P (right panel) as a function of the altitude over the earthquake epicenter. It can be easily seen that an AGW develops close to the EQ occurrence. It is confirmed by several fluctuations between 10 km and 40 km. Four wave crests are distinctly observed in T' (central panel) at ~ 15.0 km, ~ 20 km, ~ 29 km, and ~ 35.0 km. This pattern indicates the presence of two sinusoidal periods, with vertical wavelengths of approximately 5 km and 9 km, respectively. E_P (right panel) displays several enhancements coinciding with fluctuations in the temperature deviation. However, only two peaks in the E_P correspond to the smaller wavelength (~ 22 km and ~ 27 km), suggesting the presence of a single AGW with a wavelength of approximately 5 km. The greatest E_P peak at ~ 12 km is representative of the tropopause location [6,47]. Figure 2B illustrates the horizontal distribution of E_P on 8, 9 and 10 November at 06:00 UT, at a constant altitude of 27 km, corresponding to the peak in the potential energy values recorded between the tropopause (~ 12 km) and the stratopause (~ 43 km). On 8 November, the area around the epicenter (left panel) is relatively calm. However, on 9 November, there is a noticeable increase in E_P (central panel) over the epicenter (black circle) compared to the previous day, indicating wave activity around the epicenter coinciding with the earthquake. As can be easily seen, the day after the EQ occurrence (right panel), the EP behavior comes back to a relatively calm situation.

To determine a causal relationship between the earthquake and the observed disturbances in the atmospheric temperature, we compared T' observations with predictions

from the MILC model [6,14]. Using the methodology of Carbone et al. [14], we specifically analyzed the dispersion relation for wave vectors and frequencies of atmospheric pressure perturbations triggered by EQ2022, based on the parameters listed in Table 2. These parameters included Peak Ground Acceleration (PGA), fault length, strong motion duration (Δt), dominant seismogram frequency (ω_s), and phase speed of surface waves (v_s).

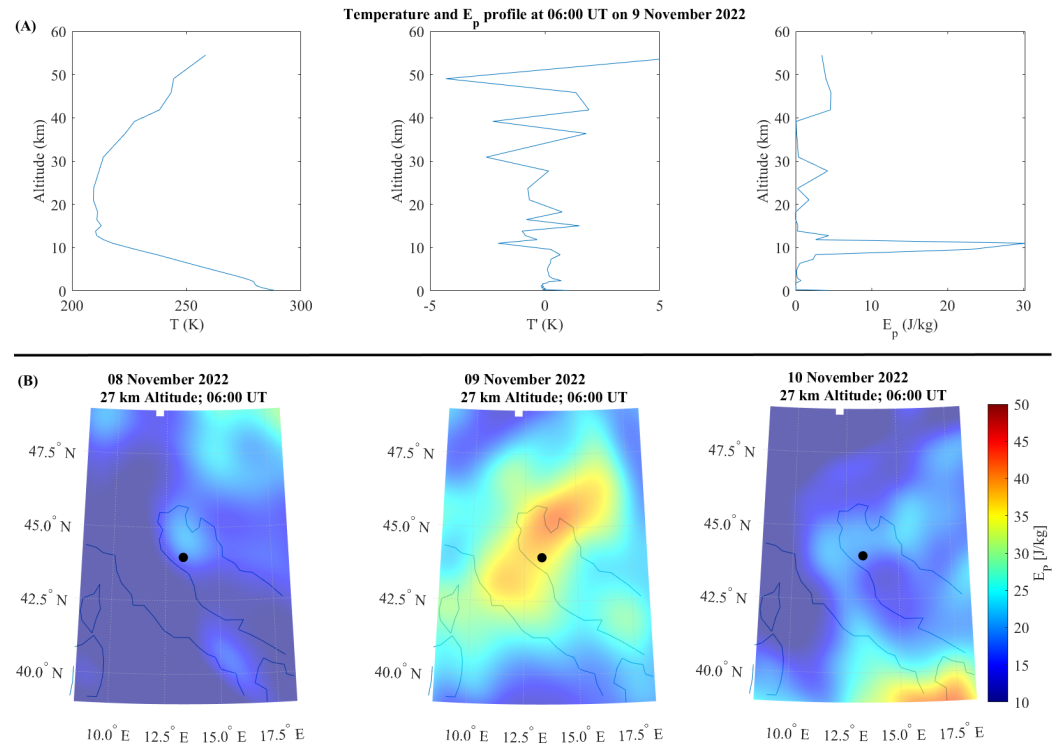


Figure 2. Co-seismic ERA-5 observations. (A) Vertical profiles of temperature (left panel), temperature deviation (middle panel), and potential energy (right panel) on 9 November 2022 at 06:00 UT. (B) Energy potential maps from 8 (left) to 10 (right) November 2022. The date and altitude are indicated in each panel. The earthquake epicenter is marked by a black dot.

Table 2. The EQ2022 characteristics as provided by the USGS website <https://earthquake.usgs.gov/earthquakes/eventpage/us7000infp/executive> (accessed on 12 December 2024). Here, PGA is estimated at the FANO station.

EQ Characteristics	Value
Length of Fault (km)	10
ω_s (Hz)	0.0422
v_s (m/s)	1614.4
Δt (s)	42.5
PGA	0.35 g

The results are reported in Figure 3. The left panel illustrates that the dispersion relation indicates excitation for wave vectors between 0.8 and 3.5 km, significantly exceeding $k_s = \omega_s/v_s$, and for frequencies ranging from 0.3 to 2.1 Hz, well above ω_s . The red dashed line marks the threshold ($\omega_t = c_0/h$, where h is the temperature scale height and c_0 is the sound speed), determining whether the pressure fluctuations are evanescent or can propagate through the atmosphere up to the ionosphere as a purely vertical AGW (refer to Carbone et al. [14] for more details). The frequency $\omega_t = 0.034$ Hz is calculated using the temperature profile from ERA5, shown in Figure 2 (left upper panel). Since all excited

modes are above (ω_t), the MILC model predicts that a purely vertical AGW will propagate to the ionosphere following the earthquake.

The right panel in Figure 3 presents a direct comparison between the modeled (red line) and observed (blue line) T' profiles. The modeled profile is derived from the estimated pressure fluctuations using the atmospheric gas equation and the three pairs corresponding to the maximum values of η/η_0 in the dispersion relation (left panel), with $T'(0) = 0$ as the boundary condition (refer to Carbone et al. [14] for more details). It is evident that the MILC model accurately reproduces the observed temperature fluctuations, with a root mean square error (RMSE) of 0.75K and a correlation coefficient of 0.79. The statistical significance of the differences between the model and observations is evaluated using the χ^2 test, yielding $\chi^2 = 49.6$. These results suggest that our model can reproduce the observations with over 88% probability, supporting the seismic origin of the AGW measured over the earthquake epicenter.

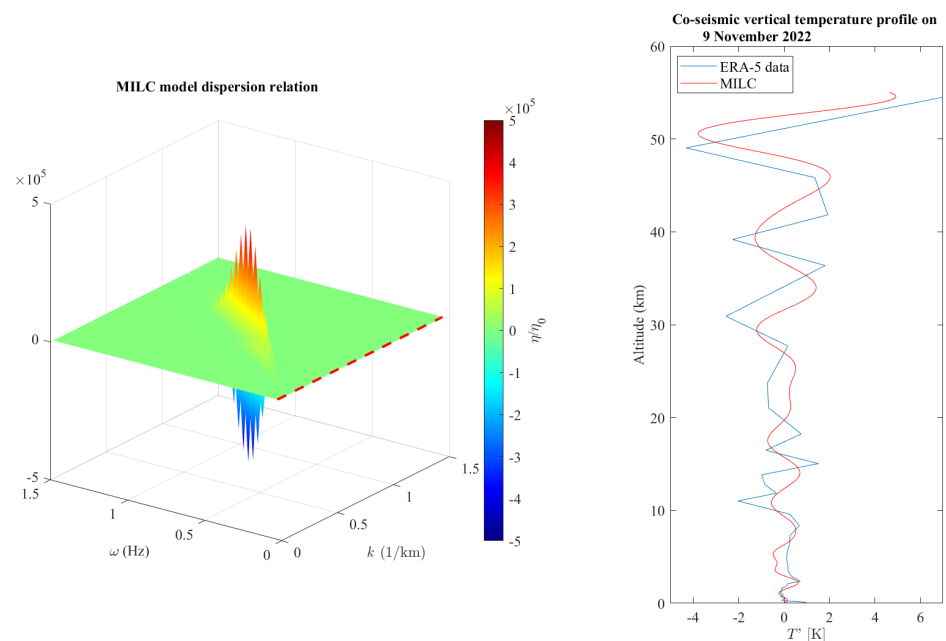


Figure 3. Comparison between the MILC model previsions and the co-seismic ERA5 observations on 9 November 2022. (**Left panel**): dispersion relation of the AGW frequency and wavelength predicted by the MILC model, in which the red dashed line represents the parameter c_0/h . (**Right panel**): comparison between MILC model prevision (red line) and observations (blue line) of the temperature deviation vertical profile. Here, c_0 is the sound speed and h is the temperature scale height

Using the results obtained in Figure 1d and the MILC model, we try to model an E_p map over the EE. To accomplish this task, we run the MILC model for each grid point in Figure 1d ($100 \text{ km} \times 100 \text{ km}$), normalizing the PGA and v_s amplitude with the static displacement field estimated by using Coulomb software. Figure 4 reports the results: the left panel shows the observed E_p (which is a part of Figure 2B, central panel), while the middle panel represents our modeled E_p . It can be easily seen that the MILC model results are strongly consistent with the observations. In fact, as is visible from the right panel in Figure 4, the maximum error made is of the order of 5%. Such a difference may be due to the discrepancies between the observed and modeled deformation pattern as seen in Figure 1d, which can be ascribed to the local effects or to lateral heterogeneity in the medium [38,40,42].

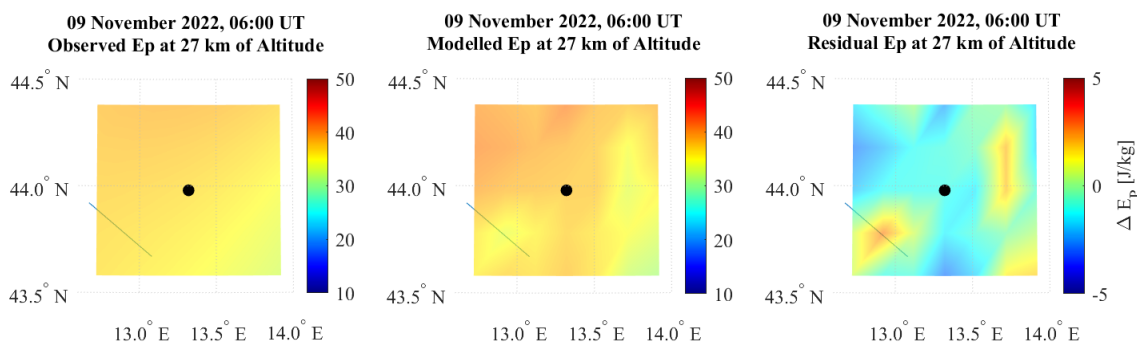


Figure 4. Comparison between the MILC model predictions and the co-seismic ERA5 observations relative to 9 November 2022. (**Left panel**): observed energy potential map. (**Middle panel**): modeled energy potential map. (**Right panel**): difference between observed and modeled energy potential map. The date and altitude are indicated in each panel. The black dot represents the earthquake epicenter.

3.2. The Vertical Total Electron Content

Following the approach proposed by D’Angelo et al. [27], in order to check for possible ionospheric disturbances related to the earthquake occurrence, we process the GPS data from the RING (Rete Integrata Nazionale GPS, <http://ring.gm.ingv.it/>, accessed on 12 December 2024) network to obtain calibrated vertical Total Electron Content (vTEC) maps over the area struck by the earthquake. Specifically, we process standard daily RINEX files provided by 56 receivers located around the epicenter, whose geographic coordinates are reported in Table 3. By using the technique by Ciruolo et al. [48] and Cesaroni et al. [49], we obtain data that depend neither on the geometry of the GPS constellation nor on the receivers’ network. Furthermore, we use the Fast Iterative Filtering (FIF) technique, recently proposed by Cicone and Zhou [50], to derive the vTEC fluctuations.

Table 3. Geographic location of the GNSS service station receivers used for the vTEC evaluation.

Site Name	Latitude (°)	Longitude (°)
ANCN	43.61	13.53
ARQT	42.75	13.2
ATBU	43.48	12.55
ATCC	43.18	12.64
ATFO	43.37	12.57
ATLO	43.32	12.41
ATMI	43.33	12.27
ATTE	43.2	12.35
BARO	42.25	12.05
BARS	42.34	13.58
BGDR	43.89	11.89
BLGN	44.51	11.35
BRAS	44.12	11.11
BRIS	44.22	11.77
CAFI	43.33	11.97
CAOC	42.29	13.48
CASP	42.79	10.87

Table 3. *Cont.*

Site Name	Latitude (°)	Longitude (°)
CESI	43	12.9
CONI	42.41	13.39
CRMI	43.8	10.98
CSSB	43.21	12.25
CTEL	42.86	13.19
GNAL	42.58	13.52
GRZM	44.26	11.15
GUMA	43.06	13.34
INGP	42.38	13.32
LNSS	42.6	13.04
LPEL	42.05	14.18
MAON	42.43	11.13
MGAB	42.91	12.11
MLAG	43.43	12.78
MODE	44.63	10.95
MOMA	42.8	12.57
MONA	42.9	13.34
MTER	42.51	13.21
MTRZ	44.31	11.42
MTTO	42.46	12.99
MUR1	43.26	12.52
MVAL	43.38	12.41
OSSC	43.52	11.25
PARM	44.76	10.31
PIET	43.45	12.4
PIOB	43.61	12.53
PREC	42.85	13.04
RNSP	43.68	12.27
ROPI	42.33	13.34
RSMN	43.93	12.45
RSTO	42.66	14
SACS	42.85	11.91
SGIP	44.64	11.18
SGRE	42.34	13.5
SIGI	43.34	12.78
USSI	42.97	13.13
VALC	43.28	12.28
VALC	43.28	12.28
VCAH	42.8	11.95

The vTEC behavior in Figure 5 shows vTEC maps every 5 min between 05:56 UT and 06:36 UT on 9 November 2022. Plasma wave activity is distinctly observable here, as evidenced by the regular alternation between negative (blue) and positive (red) vTEC fluctuations over the epicenter (black dot). These fluctuations seem to occur every 5 min starting from the time of the earthquake and persist for approximately 30 min. The characteristic mean period of these fluctuations aligns with the typical properties of Acoustic Gravity Waves/Traveling Ionospheric Disturbances (TIDs) ([51], and reference therein).

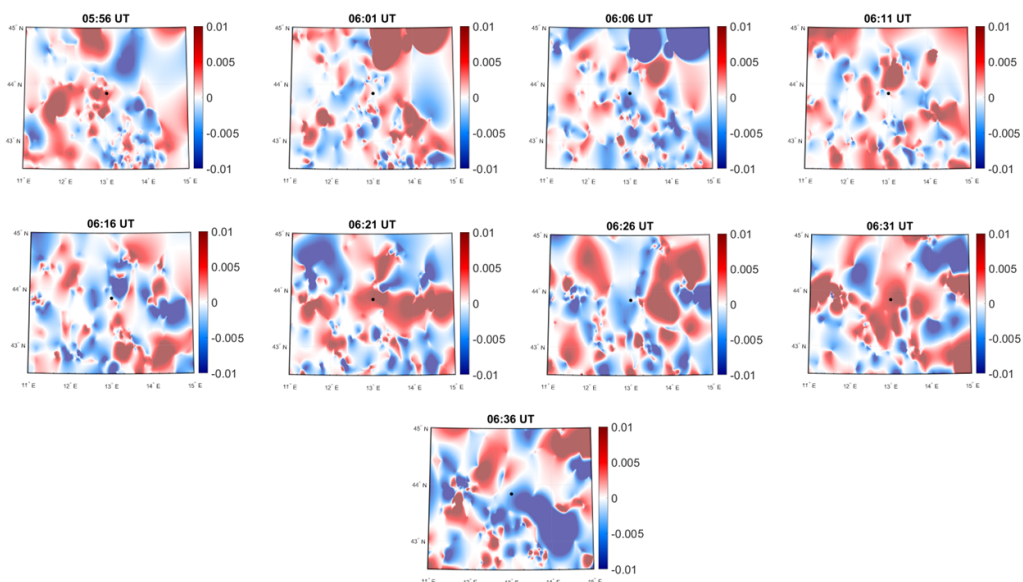


Figure 5. vTEC fluctuations characterized by a period between 5 and 9 min for all the satellites in the field of view of all available GNSS receivers near the EQ epicenter (black dot) recorded every 5 min between 05:56 UT and 06:36 UT on 9 November 2022.

4. Discussion and Conclusions

This work investigates an offshore Mw 5.5 earthquake that occurred off the Marche region's coast on 9 November 2022, focusing on identifying potential co-seismic signals in the atmosphere and ionosphere.

The observations outlined earlier indicate that an AGW was introduced into the atmosphere coinciding with EQ2022. As illustrated in the upper panels of Figure 2, an AGW with a wavelength of approximately 5 km propagated through the atmosphere. Additional evidence of wave activity concurrent with the earthquake is provided in the lower panels of Figure 2. These panels show a notable increase in E_p over the EE (central panel), in contrast to the relatively calm conditions observed on 8 November and 10 November (left and right panels) in the same region and at the same altitude.

Being that the establishing of a causal link between an AGW and an earthquake is very complex, we applied the MILC analytical model to the atmospheric temperature profile observations. The model results were able to reproduce the atmospheric temperature variation profile with an accuracy of 88% (as concluded by the χ^2 test). In addition, running the MILC model on an estimated displacement field grid induced by the specific seismic fault (Figure 1), we made a direct comparison between the geographical distribution of the map observed and modeled on 9 November 2022 E_p . The results (see Figure 4, right panel) show that the MILC model was able to reproduce the E_p observations with an error of about 5%, reinforcing the hypothesis that the AGWs generated by the earthquake influenced atmospheric conditions at high altitudes. It is well known that many other factors, such as meteorological activity in the troposphere, auroral activity, the passage

across the solar terminator, solar eclipses, and eruptions (refer to Šindelářová et al. [52] and related references), can also generate AGWs. So, we checked both the atmospheric weather and interplanetary space conditions. Figure 6 shows the SW parameters (Boxes A and B) and the Sym-H index (Box C). The red dashed lines represent the time of the EQ occurrence. Interplanetary magnetic field (IMF) observations are obtained from the DSCOVR satellite (Box A), while solar wind (SW) parameters are obtained from the WIND satellite (Box B). Both spacecraft are located at the first Lagrangian point (~ 200 Earth Radii). We use two different satellites because DSCOVR plasma observations are not available for the period under analysis. Unfortunately, almost the same situation happens for the WIND data. Data are freely available on the NASA website (accessed on 12 December 2024). (<https://cdaweb.gsfc.nasa.gov/>, accessed on 12 December 2024). It can be easily seen that no SW particular structure (like interplanetary shock, coronal mass ejection, corotating interaction region, high speed stream, etc.) is present ~ 45 min before the EQ occurrence. This time is the typical delay time for a SW structure when traveling from the satellite position down to the Earth's magnetopause. In addition, the Sym-H value is stable around -40 nT representing almost quiet conditions.

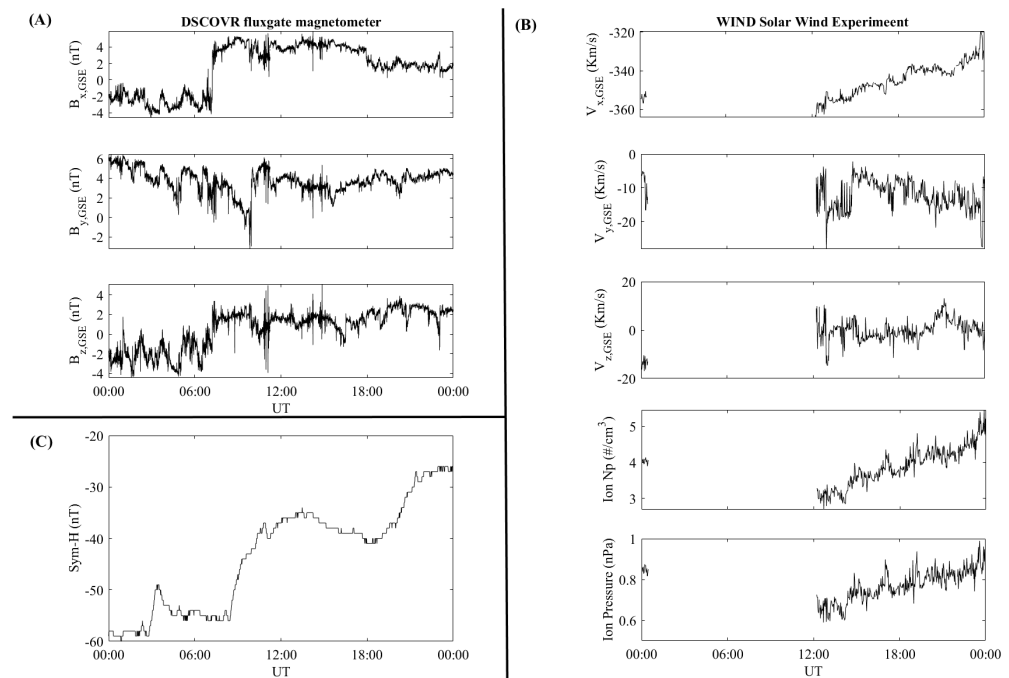


Figure 6. Solar wind parameters and the Sym-H index (<https://cdaweb.gsfc.nasa.gov/> (accessed on 17 December 2024)) for 9 November 2022. Box (A) shows the Interplanetary magnetic field components. Box (B) shows the solar wind parameters, namely (from the top) the three components of the solar wind speed, solar wind plasma density, and solar wind dynamic pressure. Box (C) shows the Sym-H index. Red dashed lines represent the time of the EQ occurrence.

Concerning atmospheric weather conditions, the observations are reported in Figure 7.

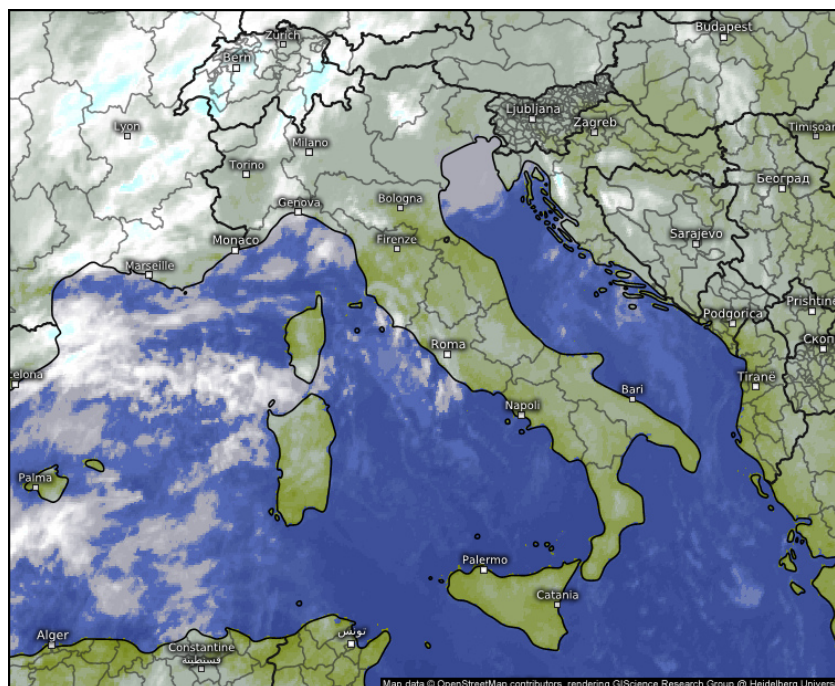
It can be easily seen the total absence of any weather system affecting the Marche region at the time of the EQ occurrence. Hence, we are confident that the AGW observed at 06:00 UT is likely linked to the seismic event.

Additionally, the analysis of the vTEC reveals significant fluctuations at the EE with a peculiar period consistent with TIDs driven by AGW [51], suggesting the coupling between the lithosphere and ionosphere, as well.

In conclusion, the findings confirm the presence of a coupling among the lithosphere, atmosphere, and ionosphere at the time of the earthquake. Specifically, the co-seismic analysis

reveals that disturbances initiated by the earthquake propagated from the lower atmosphere into the ionosphere, giving strong support to the AGW driving mechanism theory.

Further research could consolidate these results and develop a short-term earthquake prediction system based on the Lithosphere–Atmosphere–Ionosphere coupling. It is important to analyze a greater number of seismic events to verify the robustness of the MILC model, identify any recurring pattern, and integrate different data sources, such as satellite magnetic field and temperature data, to obtain a more complete view of the phenomenon. This study opens new perspectives for understanding the coupling mechanisms between the different layers of the Earth and for developing more reliable earthquake prediction tools.



Satellite nature

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Italy

meteologix.com

satellite data: EUMETSAT

Figure 7. Weather report maps over Italy (<https://meteologix.com/it/satellite/italy/satellite-nature-15min-en/20221109-0500z.html>) (accessed on 1 January 2024) for the 9 November 2022 at 06:00 UT.

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Data Availability Statement: Seismic signals and the parameters of the 2009 Italian earthquake are provided by EMS (<https://esm-db.eu>, accessed on 12 December 2024) and by USGS (<https://earthquake.usgs.gov/earthquakes/eventpage/us7000infp/executive>, accessed on 12 December 2024). The Coulumb software for the static displacement is available online: <https://pubs.usgs.gov/of/2011/1060/>, accessed on 12 December 2024; ERA-5 data can be retrieved from <https://www.ecmwf.int/en/forecasts/datasets/reanalysis-datasets/era5>, accessed on 12 December 2024;

The Global GNSS Network (GGN) data can be retrieved from <https://www.unavco.org/>, accessed on 12 December 2024. Weather report maps can be found at (<https://meteologix.com/it/satellite/italy/satellite-nature-15min-en/20221109-0500z.html> (accessed on 17 December 2024)). Solar wind data, interplanetary field data and Sym-H index data can be freely downloaded at NASA cdaweb site (<https://cdaweb.gsfc.nasa.gov/> (accessed on 17 December 2024)).

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Abbreviations

The following abbreviations are used in this manuscript:

AGW	Acoustic Gravity Wave
EE	Earthquake epicenter
EQ	Earthquake
TID	Traveling Ionospheric Disturbance
FIF	Fast iterative Filtering
GNSS	Global Navigation Satellite System
MILC	Magnetospheric–Ionospheric–Lithospheric Coupling
TEC	Total Electron Content
vTEC	Vertical TEC

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