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Seismic Fragility of Ordinary Reinforced Concrete Shear Walls with Coupling Beams Designed Using a Performance-Based Procedure

Seong-Ha Jeon¹ and Ji-Hun Park^{2,*}

- ¹ Industry-Academic Cooperation Foundation, Incheon National University, Incheon 22012, Korea; wings616@inu.ac.kr
- ² Division of Architecture and Urban Design, Incheon National University, Incheon 22012, Korea
- * Correspondence: jhpark606@inu.ac.kr; Tel.: +82-32-835-8474

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Abstract: The seismic performance of ordinary reinforced concrete shear walls, that are commonly used in high-rise residential buildings in Korea (h < 60 m), but are prohibited for tall buildings (h \ge 60 m), is evaluated in this research project within the framework of collapse probability. Three bidimensional analytical models comprised of both coupled and uncoupled shear walls exceeding 60 m in height were designed using nonlinear dynamic analysis in accordance with Korean performance-based seismic design guidelines. Seismic design based on nonlinear dynamic analysis was performed using different shear force amplification factors in order to determine an appropriate factor. Then, an incremental dynamic analysis was performed to evaluate collapse fragility in accordance with the (Federal Emergency Management Agency) FEMA P695 procedure. Four engineering demand parameters including inter-story drift, plastic hinge rotation angle, concrete compressive strain and shear force were introduced to investigate the collapse probability of the designed analytical models. For all analytical models, flexural failure was the primary failure mode but shear force amplification factors played an important role in order to meet the requirement on collapse probability. High-rise ordinary reinforced concrete shear walls designed using seven pairs of ground motion components and a shear force amplification factor \geq 1.2 were adequate to satisfy the criteria on collapse probability and the collapse margin ratio prescribed in FEMA P695.

Keywords: ordinary reinforced concrete shear walls; coupling beams; seismic fragility; incremental dynamic analysis; performance-based seismic design

1. Introduction

Performance-based seismic design has been applied to high-rise buildings increasingly in South Korea as well as the USA, owing to progress in nonlinear structural analysis techniques and relevant design guidelines. In Korean Building Code (KBC) 2016, the performance-based seismic design is introduced for the first time and defined as a design method to achieve performance objectives using nonlinear analysis considering inelastic deformation capacity and the over-strength of structures more precisely, and it can be applied to structures in which the design coefficients for elastic design are uncertain or structures required to meet various performance objectives [1]. In South Korea, performance-based seismic design is mostly applied to high-rise apartment buildings in which ordinary reinforced concrete (RC) shear walls are used to resist seismic forces. This is because ordinary RC shear walls are not permitted in the elastic design for buildings that belong to seismic design category D and are taller than 60 m. For such conditions, special RC shear walls are used, but strict confinement details are required in boundary elements with a side effect of higher construction cost and time. The "boundary

element" designate longitudinal end in the cross section of walls where hoop reinforcement is located to confine concrete in high compression. The special RC wall is avoided, particularly in case of thin walls because the spacing of the hoop reinforcement required to be smaller than one third of the wall thickness, and this requirement causes difficulty in the detailing work and concrete placing in an actual construction field. In order to solve this problem, high-rise ordinary RC shear walls are used, using the performance-based seismic design procedure introduced in KBC 2016. The detailed guidelines for the performance-based seismic design are given in "Guidelines for Performance-Based Seismic Design of Residential Buildings" published by the Architectural Institute of Korea (AIK) [2].

Although nonlinear dynamic analysis is used for the detailed verification of seismic performance, it is necessary to verify the structural safety of high-rise ordinary RC shear walls, because such walls are subjected to relatively high axial force ratios, which can lead to brittle failure mode due to the lack of confinement in the boundary elements. In accordance with AIK guidelines, nonlinear response history analyses are conducted using seven pairs of horizontal ground motion components within the framework of performance-based seismic design. However, mean peak response-based design without strength reduction factors for a limited number of ground motion records are questionable in respect to reliability. Representative guidelines on the reliability of seismic design are found in (American Society of Civil Engineers) ASCE 7–16, in which a target reliability for structural stability against earthquakes is proposed as 10% in the case of seismic risk category I and II [3]. FEMA P695 provides a verification methodology for seismic design coefficients in respect to structural stability based on incremental dynamic analysis, by which structures are analyzed repeatedly for earthquakes with increasing intensity measures until structural collapse is identified [4].

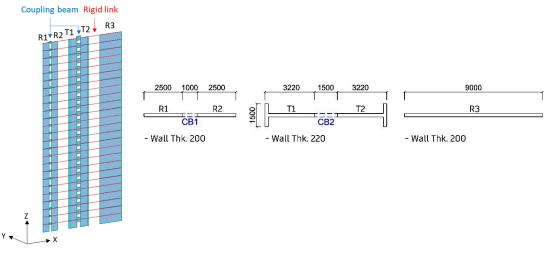
Recently, diverse studies have been conducted to assess the seismic fragility of the RC shear wall. In the study of Chun et al. (2013) [5], seismic fragility analysis was carried out for both ordinary and special RC shear walls, among which some specimens have simplified confinement details for boundary elements. However, their work presents only RC walls with boundary elements in detail. Gogus and Wallace (2015) [6,7] and Rafie Nazari (2017) [8] evaluated the seismic performance of building frame systems, of which the core walls are ordinary or special RC shear walls. Above all, analytical models for buildings in their research have at most 12 and 10 stories, respectively, which are not so high-risen compared to Korean apartment buildings over 60 m designed in a performance-based methodology. Therefore, existing studies on the seismic performance of bearing wall systems consisting of ordinary RC shear walls over 60 m-tall height are insufficient. In addition, existing studies address shear walls designed using the ultimate strength design method based on elastic analysis rather than the performance-based design based on nonlinear analysis.

In this study, the seismic fragility assessment of high-rise ordinary RC shear walls over 60 m designed through performance-based seismic design is conducted to verify whether those structures have adequate collapse margin ratios. The evaluation of the collapse fragility curve and the assessment of collapse prevention performance are conducted in accordance with FEMA P695. The procedure of FEMA P695 is intended to verify the seismic design coefficients, such as response modification factors and over-strength factors and displacement amplification factors. However, the procedure can be applied to any structure that can be grouped as a single category, such as ordinary RC shear walls higher than 60 m designed in accordance with a single design document. Therefore, three analytical models composed of ordinary RC shear walls typical in South Korea but with different heights are designed in accordance with the AIK guidelines using nonlinear response history analysis using seven pairs of horizontal ground motion components. Then, incremental dynamic analysis (IDA) is performed for those structures using 30 ground motion pairs to calculate the collapse fragility curve. Finally, criteria on the conditional collapse probability and the collapse margin ratio (CMR) are evaluated in accordance with FEMA P695.

2. Design of Analytical Models

2.1. Structure

High-rise ordinary shear wall structures were idealized using two-dimensional plane models. A total of three models denoted by Model A, Model B, and Model C are constructed, designed and evaluated. Figure 1a,b show the three-dimensional view and plan of the Model A. The model is composed of five walls, of which R1 and R2 are coupled shear walls with a rectangular cross section, R3 is a single wall with a rectangular cross section, and T1 and T2 are coupled shear walls with a T-shaped cross section as illustrated in Figure 1a,b. CB1 and CB2 represent coupling beams. Those five walls are connected with rigid links (red line), which constrain only the translational degree of freedom in the X-direction. The length of coupling beams CB1 and CB2 in Figure 1b is 1 m and 1.5 m, respectively, reflecting the width of doors and windows. The depth of those coupling beams is set to 0.6 m and 1.2 m, respectively. The width of the coupling beam is the same as the thickness of the adjacent walls. The dimensions of coupling beams are common among the three analytical models. Table 1 represents the characteristics of the three models.



(a) Axonometric view

(b) Plan (unit: mm)

Figure 1. Configuration of Model A.

| Analytical | Component | Lengtl | n (m) | Thickne | ess (m) | Axial Force | Height (m) | T1 (s) |
|------------|-----------|--------|-------|---------|---------|-------------|---------------|--------|
| Model | Wall | Flange | Web | Flange | Web | Ratio | fieight (iii) | |
| | R1 | | 2.5 | | 0.2 | 0.3 | | |
| | R2 | | 2.5 | | 0.2 | 0.3 | | |
| Model A | R3 | | 9 | | 0.2 | 0.15 | 70 | 2.4 |
| | T1 | 1.5 | 3 | 0.22 | 0.22 | 0.15 | | |
| | T2 | 1.5 | 3 | 0.22 | 0.22 | 0.15 | | |
| | R1 | | 2.5 | | 0.2 | 0.3 | | |
| | R2 | | 2.5 | | 0.2 | 0.3 | | |
| Model B | R3 | | 9 | | 0.2 | 0.15 | 81.2 | 3.6 |
| | T1 | 1.5 | 3.5 | 0.25 | 0.25 | 0.15 | | |
| | T2 | 1.5 | 3.5 | 0.25 | 0.25 | 0.15 | | |
| | R1 | | 2.5 | | 0.25 | 0.3 | | |
| | R2 | | 2.5 | | 0.25 | 0.3 | | |
| Model C | R3 | | 9 | | 0.3 | 0.1 | 109.2 | 3.2 |
| | T1 | 2.5 | 4 | 0.35 | 0.35 | 0.1 | | |
| | T2 | 2.5 | 4 | 0.35 | 0.35 | 0.1 | | |

Model B and C have the same configuration as Model A, but the detailed dimensions are slightly different from each other. Height, cross sectional shapes and dimensions for the component walls comprising each model were determined based on typical actual apartment buildings in South Korea and listed with other characteristics in Table 1. The height of Model A, B and C is 70 m (25 floors), 81.2 m (29 floors), and 109.2 m (39 floors), respectively. The height of all of the three models exceeds the upper limit 60 m, below which the ordinary shear walls are acceptable.

The axial force ratio plays an important role in the flexural and shear capacities of walls. Therefore, axial force ratios and corresponding wall lengths were investigated based on design documents for previously designed apartment buildings. Figure 2 shows that longer walls tend to have lower axial force ratios. Considering this observation, R1 and R2 with relatively shorter length have higher axial force ratio than R3, T1 and T2 in Table 1.

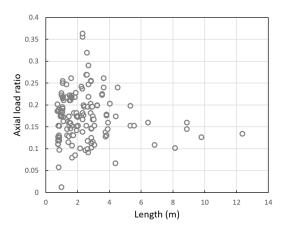


Figure 2. Axial force ratio by wall length.

The purpose of using simplified plane models is to concentrate on the adequacy of ordinary shear walls exceeding the height limit in the design code. However, issues such as irregularity and flexible diaphragms are important in the behavior of actual building structures. Irregular building configuration can cause additional seismic demand to structural systems by torsion in structural systems leading to increased possibility of collapse [9]. In addition, a flexible diaphragm may enhance such an irregularity [10,11]. Therefore, it should be noted that the result of this study can be applied only to buildings with regular configurations and rigid diaphragms, and more sophisticated and realistic models are necessary in further study.

2.2. Ground Motion and Scaling

Seismic hazard was defined based on the maximum considered earthquake (MCE) defined in Korean Design Standard (KDS 41 17 00: 2019) [12]. Effective ground acceleration S, that can be read from peak ground acceleration map, was assumed to be 0.22 g, corresponding to seismic zone I, and the site classification was assumed to be S_4 . As a result, the site belongs to the seismic design category D, for which the building height of ordinary RC shear walls is limited below 60 m. The response spectrum for the MCE is plotted in Figure 3.

Three ground motion suites were selected for the design of three analytical models, respectively. The individual suite is comprised of seven pairs of horizontal components. Ground motion records used in nonlinear dynamic analysis were selected from the NGA-West2 database of PEER [13]. The shear wave velocity corresponding to site class S4 is defined as more than 180 m/s, but the range of shear wave velocity was increased by a small amount to secure a sufficient number of ground motion suites. A method proposed by Han et al. [14] was used for selecting ground motion records fitting the target MCE spectrum in good agreement. The details of ground motion suites adopted for the design of three analytical models are summarized in Table 2.

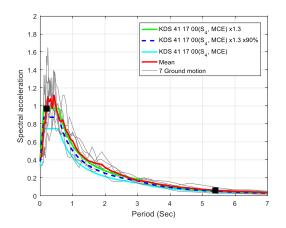


Figure 3. Target response spectra and average response spectra by seven pairs of ground motion scaling (Site class: *S*₄, maximum considered earthquake (MCE), Model B).

| Analytical Model | No. | Earthquake Name | Station Name | Mw | R _{jb} (km) | V _{s,30} (m/s) |
|---------------------|-----|-----------------------|--|------|----------------------|-------------------------|
| | 1 | Imperial Valley-06 | Delta | 6.53 | 22.0 | 242 |
| | 2 | Northridge-01 | Northridge-17645 Saticoy St | 6.69 | 0.0 | 281 |
| | 3 | Superstition Hills-02 | Brawley Airport | 6.54 | 17.0 | 209 |
| Model A | 4 | Northridge-01 | Playa Del Rey-Saran | 6.69 | 24.4 | 346 |
| | 5 | Loma Prieta | Fremont-Emerson Court | 6.93 | 39.7 | 285 |
| | 6 | Kobe Japan | Sakai | 6.90 | 28.1 | 256 |
| | 7 | Northridge-01 | Camarillo | 6.69 | 34.8 | 351 |
| | 1 | Imperial Valley-06 | Delta | 6.53 | 22.0 | 242 |
| | 2 | Northridge-01 | LA-Century City CC North | 6.69 | 15.5 | 278 |
| | 3 | Chuetsu-oki Japan | Niigata Nishi Kaba District | 6.80 | 27.8 | 255 |
| Model B | 4 | Loma Prieta | Dumbarton Bridge West End FF | 6.93 | 35.3 | 238 |
| | 5 | Chuetsu-oki Japan | Kashiwazaki NPP Unit 1: Ground surface | 6.80 | 0.0 | 329 |
| | 6 | Chi-Chi Taiwan-06 | CHY036 | 6.30 | 45.1 | 233 |
| | 7 | Chuetsu-oki Japan | Hinodecho Yoshida Tsubame City | 6.80 | 20.4 | 262 |
| | 1 | Imperial Valley-06 | Delta | 6.53 | 22.0 | 242 |
| | 2 | Northridge-01 | LA-Century City CC North | 6.69 | 15.5 | 278 |
| | 3 | Chi-Chi Taiwan-06 | CHY036 | 6.30 | 45.1 | 233 |
| Model C | 4 | Northridge-01 | Playa Del Rey-Saran | 6.69 | 24.4 | 346 |
| | 5 | Northridge-01 | LA-Pico & Sentous | 6.69 | 27.8 | 305 |
| | 6 | Loma Prieta | APEEL 7-Pulgas | 6.93 | 41.7 | 415 |
| | 7 | Chuetsu-oki Japan | Joetsu Kita | 6.80 | 29.0 | 334 |

Table 2. List of ground motion used in seismic design.

In accordance with KDS 41 17 00, the SRSS spectrum of two horizontal components for each ground motion pair shall be scaled not to fall below 90% of the target spectrum defined as 1.3 times the MCE spectrum. The range of the period for scaling individual response spectrum is defined as 0.2 to 1.5 times the first mode period, T1, in KDS 41 17 00, but the lower bound is modified to be the period where the modal mass participation ratio is over 90% in order to consider the effect of the higher mode sufficiently. Figure 3 shows the target spectrum and 90% thereof and individual scaled spectra for the Model B analysis model.

In this study, a two-dimensional analysis was performed. Only the single horizontal component of ground motion was applied to the in-plane horizontal direction in a single nonlinear dynamic analysis. Each component, comprising a ground motion pair, was applied to the analysis alternately to take into account uncertainty in the azimuth of horizontal ground motion in accordance with KDS 41 17 00. Therefore, a total of 14 nonlinear dynamic analyses were conducted in the in-plane direction for the design of each analytical model.

2.3. Preliminary Elastic Design

The analytical models were designed initially to have a minimum base shear capacity defined as 75% of the base shear determined by an equivalent lateral force procedure to meet the requirement for structures designed with the performance-based seismic design procedure provided by KDS 41 17 00. Response modification factor R = 4.0 for ordinary RC shear walls and importance factor $I_E = 1.2$ for residential buildings with five or more stories were applied to the minimum base shear forces. Material strengths of concrete and reinforcement are summarized in Table 3. Response spectrum analysis was performed for the elastic design. A total of 25, 29 and 39 modes of vibration were included in the analysis of Model A, B and C, respectively, and combined with the complete quadratic combination (CQC) rule. The mass participation factor of the modes included in the analysis was 99.9% for all the three analytical models. For the analysis of the response spectrum, a 5% damping ratio was assumed. The initial design was conducted using MIDAS Gen [15].

| Analytical Model | Floor | f_c (MPa) | f_y (MPa) |
|------------------|-------|-------------|-------------|
| Model A | 11–25 | 21 | 400 |
| 100000171 | 1–10 | 24 | 400 |
| | 16–29 | 21 | |
| Model B | 6–15 | 24 | 400 |
| | 1–5 | 27 | |
| | 26–39 | 21 | |
| | 21-25 | 24 | |
| Model C | 11-20 | 27 | 400 |
| | 6–10 | 30 | |
| | 1–5 | 35 | |

Table 3. Material property of analytical models.

2.4. Inelastic Modeling and Nonlinear Dynamic Analysis

For nonlinear dynamic analysis, shear walls were modeled using fiber elements. Uniaxial inelastic models for concrete and rebar are represented in Figure 4, respectively. The unconfined concrete model proposed by Mander and Priestley was used to represent the nonlinear behavior of the concrete before the maximum compressive stress of concrete [16]. In accordance with the AIK guidelines, the stress drops to the residual stress after reaching the maximum stress at the strain of 0.002. The ultimate strain at the end of stress drop is prescribed as 0.003 in the guidelines. However, the ultimate strain of 0.003 may underestimate the deformation capacity of actual unconfined concrete. Figure 4a represents the nonlinear behavior beyond the maximum compressive stress for concrete models by Saatcioglu, and Mander and Priestley, in which deformation capacities considerably higher than 0.003 are observed [16,17]. Therefore, it is necessary to set an appropriate concrete deformation capacity beyond the maximum compressive stress of concrete.

In this study, the ultimate strain ε_{cu} was determined by comparison of the test and numerical analysis results for an existing specimen tested by Dazio et al. [18]. A total of 1% of the maximum stress is applied to the residual stress of the unconfined concrete model. Using 0.005 for the ultimate strain, it was confirmed that the experimental results and the analytical results were in good agreement for each cycle, and the deformation at the strength drop was simulated well in Figure 5. Therefore, unconfined concrete model with the ultimate strain of 0.005 and residual strength ratio of 0.01 times the maximum stress is adopted for the analytical models in this study. The inelastic material model for reinforcing bars was determined referring to the works of Thomsen and Wallace, Orakcal and Wallace, and Tuna [19–21]. The tensile strength of the rebar was selected to be 1.5 times the yield strength, and the tensile strain at the tensile strength is 0.05. The nonlinear model of reinforcing bars was created symmetrically, but the limit of compressive strain was set to be 0.02 considering buckling as shown in Figure 4b.

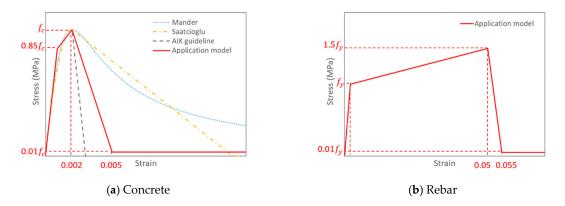


Figure 4. Nonlinear model of concrete and rebar.

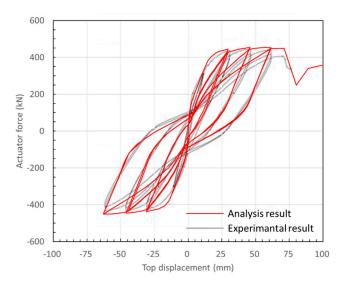


Figure 5. Comparison of experimental result and analysis result [14].

All the shear walls have height-to-length ratios higher than 3.0 and are dominated by flexural behavior [19]. Therefore, the shear of those walls was modeled as linear elastic and regarded as force-controlled behavior. Uncracked stiffness was applied to the shear stiffness of the shear walls in accordance with AIK guidelines [2].

The flexural or shear behavior of coupling beams were modeled with concentrated plastic hinges of which modeling parameters were determined in accordance with the AIK guidelines. The failure mode of coupling beams is classified into flexural or shear one based on the span-to-depth ratio in the AIK guidelines [2]. All the coupled beams included in the analytical models used in this study have the span-to-depth ratio less than 4.0 for which shear failure is dominant. The nonlinear modeling parameters of a coupling beam depend on the normalized shear force determined by Equation (1) and the classification of seismic details between conforming and non-conforming details depending on whether the transverse reinforcement satisfies requirements on the boundary elements of special structural walls prescribed in KDS 14 20 80 or not [22].

$$V/\sqrt{f_{ck}th} \tag{1}$$

where *V* is the shear force demand, f_{ck} is the specified compressive strength of the concrete material, *t* is the thickness of the coupling beam, and *h* is the clear span. Inelastic modeling and nonlinear dynamic analysis was performed using PERFORM 3D V7 [23]. Newmark's method was used for the time history analysis with time step sizes s between 0.005 to 0.02 s according to the ground motion data. For nonlinear analysis, the event-to-event solution strategy adopted in PERFORM-3D was used

to update stiffness and strength of components and to stop analysis when the number of events in a time step exceeds a specified value 1000. Rayleigh damping was used to introduce 2.5% damping ratio in the analytical model.

2.5. Performance Goals and Acceptance Criteria

Collapse prevention against the maximum considered earthquake was adopted as a performance objective for the design of shear walls using nonlinear dynamic analysis. Table 4 summarizes the engineering design parameters and their acceptance criteria used in the design of three models. Details of the acceptance criteria are described as follows.

| En | gineering Demand Parameter | Acceptance Criteria | | |
|---------|--------------------------------------|--|--|--|
| | Inter-story drift ratio | 2.0% | | |
| | Plastic hinge rotation angle | Collapse prevention in ASCE 41-17 | | |
| Co | mpressive extreme-fiber strains | 0.002 | | |
| | AIK guideline [2] | $\gamma Q_u \leq \phi Q_n, \gamma = 1.2, \phi = 1.0$ | | |
| Shoor | Hassan et al., Moehle et al. [24,25] | $\gamma Q_u \le \phi Q_n, \gamma = 1.5, \phi = 1.0$ | | |
| Shear - | TBI v2.03 [26] | $\gamma Q_u \le \phi B Q_n, \gamma = 1.3, \phi = 0.75, B = 0.9(1.5Q_e/Q_n)$ Simplified as follows if flexural rotation is not large $1.12Q_u \le Q_n$ | | |

Table 4. Engineering demand parameters for performance-based seismic design.

Four engineering demand parameters (EDPs) such as inter-story drift ratios, plastic hinge rotation angles, shear forces and compressive extreme-fiber strains were checked with the acceptance criteria for the performance level. TBI v2.03 limits the mean peak inter-story drift ratio for the whole ground motion suites below 3.0% and individual peak inter-story drift ratio for each ground motion suite below 4.5% in order to prevent collapse [26]. However, the upper limit of mean peak inter-story drift ratio is specified as 2.0% for the prevention of collapse in the AIK guidelines, because most shear walls are designed in the type of ordinary shear walls without confinement at boundary regions and 3.0% inter-story drift ratio could overestimate the performance of those shear walls. Therefore, ordinary shear walls in this study were also designed using the 2.0% inter-story drift ratio limit in accordance with the AIK guidelines.

For the plastic hinge rotation angles of shear walls, acceptance criteria prescribed in the AIK guidelines were applied and are essentially equivalent to ASCE 41-17 [27]. To check the plastic hinge rotation angle of shear walls, a yield rotation is necessary to subtract from the peak rotation angle. In this study, the yield rotation angle was calculated using the following Equation (2), where the yield moment strength M_y is estimated using Equation (3) in accordance with the regression analysis of Haselton et al. [28].

$$\theta_y = \left(\frac{M_y}{E_c I}\right) l_p \tag{2}$$

$$M_n/M_y = 1.13$$
 (3)

where M_n and M_y are the nominal and yield flexural moment strengths respectively, E_c is the elastic modulus of concrete, and I is the moment of inertia. l_p is the plastic hinge length of the wall. In this study, l_p was assumed to be a half of the wall length in accordance with ASCE 41-17.

The shear force is a force control action, designed to satisfy the required strength increased with an amplification factor. Table 4 shows the shear design recommendation of the AIK guidelines and other relevant literature, where Q_n and Q_e represent the nominal shear strengths based on the nominal and expected material strengths, respectively. Q_u is the required strength defined by the mean peak response for the whole suite of ground motions. γ and ϕ are the shear force amplification factor and the strength reduction coefficient, respectively. In the AIK guidelines, ϕ and γ are 1.0 and 1.2, respectively [2]. Hassan et al. and Moehle et al. used similar mathematical representation for the acceptance criteria of force-controlled actions, but used 1.5 for γ and adopted expected strength rather than nominal strength [24,25]. In TBI v2.03, the change was made to use $\gamma = 1.3$, but ϕ was applied and a new coefficient *B* was introduced to correct bias in the nominal strength equation. This study applied acceptance criteria of the AIK guidelines but different force amplification factors corresponding to 1.0, 1.2, and 1.5 in order to examine an appropriate level of the factor. Finally, compressive extreme-fiber strains were limited below 0.002 corresponding to the strain at the peak stress in the uniaxial material model for unconfined concrete in order to take into account uncertainty in the descending branch of the model and avoid overestimating the deformation capacity of the ordinary RC shear walls in accordance with the AIK guidelines.

2.6. Analysis and Design Results

In order to confirm whether the analytical model satisfies the target performance, a nonlinear dynamic analysis was performed for the 14 ground motion records described in Section 2.2. The mean peak of inter-story drifts, plastic hinge rotation angles, and compressive extreme-fiber strains were calculated and all component walls were designed to meet acceptance criteria for collapse prevention. The component walls were reinforced with double-layered rebars, and design results are summarized in Table 5. The reinforcement of coupling beams is summarized in Table 6.

| Analytical | Component | Vertical Reinforcement | | | Horizontal Reinforcement | | | |
|------------|-----------|------------------------|---------------|-------|---------------------------|--------------------|---------------------------|--|
| Model | Ŵall | Story | Reinforcement | Story | Design to $1.0V_u$ | Design to $1.2V_u$ | Design to $1.5V_u$ | |
| | | 3~25 | D10@400 | 4~25 | D10@360 | D10@360 | D10@360 | |
| | R1 | 2 | D13@400 | 3 | D10@360 | D10@180 | D10@150 | |
| | | 1 | D13@200 | 1~2 | D10@250 | D10@180 | D10@150 | |
| | | 3~25 | D10@400 | 4~25 | D10@360 | D10@360 | D10@360 | |
| | R2 | 2 | D13@400 | 3 | D10@360 | D10@180 | D10@150 | |
| | | 1 | D13@200 | 1~2 | D10@250 | D10@180 | D10@150 | |
| | T1 | 18~25 | D10@400 | 6~25 | D10@330 | D10@330 | D10@330 | |
| | | 11~17 | D13@400 | 4~5 | D10@330 | D10@330 | D10@200 | |
| | | 8~10 | D13@300 | 3 | D10@330 | D10@200 | D10@140 | |
| Model A | | 3~7 | D13@200 | 1~2 | D10@270 | D10@200 | D10@140 | |
| | | 1~2 | D13@150 | 1~2 | | | | |
| | | 18~25 | D10@400 | 6~25 | D10@330 | D10@330 | D10@330 | |
| | | 11~17 | D13@400 | 4~5 | D10@330 | D10@330 | D10@200 | |
| | T2 | 8~10 | D13@300 | 3 | D10@330 | D10@200 | D10@140 | |
| | | 3~7 | D13@200 | 1~2 | D10@270 | D10@200 | D10@140 | |
| | | 1~2 | D13@150 | 1~2 | D10@270 | D10@200 | D10@140 | |
| | | 15~25 | D10@400 | 6~25 | D10@360 | D10@360 | D10@360 | |
| | Do | 13~23 | D10@400 | 4~5 | D10@360 | D10@360 | D10@210 | |
| | R3 | 1~14 | D13@400 | 2~3 | D10@360 | D10@320 | D10@210 | |
| | | 1~14 | D13@400 | 1 | D10@280 | D10@200 | D10@140 | |

| Table 5. | Reinforcement c | of shear | walls. |
|----------|-----------------|----------|--------|
|----------|-----------------|----------|--------|

| Analytical | Component | Vertica | l Reinforcement | | Horizontal Reinforcement | | | |
|------------|------------|---------|-----------------|-------|---------------------------|--------------------|-----------------------------|--|
| Model | Wall | Story | Reinforcement | Story | Design to $1.0V_u$ | Design to $1.2V_u$ | Design to 1.5V ₁ | |
| | | 16~29 | D10@400 | 4 20 | D10@2(0 | D10@2(0 | D10@2(0 | |
| | D 1 | 6~15 | D10@300 | 4~29 | D10@360 | D10@360 | D10@360 | |
| | R1 | 3~5 | D13@400 | 1.2 | D10@2(0 | D10@ 27 0 | D100100 | |
| | | 1~2 | D13@150 | 1~3 | D10@360 | D10@270 | D10@180 | |
| | | 16~29 | D10@400 | 4 20 | D10@2(0 | D10@2(0 | D10@2(0 | |
| | 7.0 | 6~15 | D10@300 | 4~29 | D10@360 | D10@360 | D10@360 | |
| | R2 | 3~5 | D13@400 | 1.0 | D1002(0 | D100070 | D100100 | |
| | | 1~2 | D13@150 | 1~3 | D10@360 | D10@270 | D10@180 | |
| | | 26~29 | D10@400 | 27~29 | D10@290 | D10@290 | D10@290 | |
| | | 22~25 | D13@300 | 22~26 | D10@290 | D10@290 | D10@200 | |
| | | 16~21 | D13@200 | 13~21 | D10@290 | D10@290 | D10@150 | |
| | T1 | 9~15 | D19@400 | 10~12 | D10@290 | D10@200 | D10@100 | |
| Model B | | 6~8 | D19@300 | 7~9 | D10@240 | D10@160 | D10@100 | |
| | | 2~5 | D19@200 | 4~6 | D10@150 | D10@100 | D10@70 | |
| | | 1 | D19@150 | 1~3 | D10@100 | D10@70 | D10@50 | |
| | | 26~29 | D10@400 | 27~29 | D10@290 | D10@290 | D10@290 | |
| | | 22~25 | D13@300 | 22~26 | D10@290 | D10@290 | D10@200 | |
| | | 16~21 | D13@200 | 13~21 | D10@290 | D10@290 | D10@150 | |
| | T2 | 9~15 | D19@400 | 10~12 | D10@290 | D10@200 | D10@100 | |
| | | 6~8 | D19@300 | 7~9 | D10@240 | D10@160 | D10@100 | |
| | | 2~5 | D19@200 | 4~6 | D10@150 | D10@100 | D10@70 | |
| | | 1 | D19@150 | 1~3 | D10@100 | D10@70 | D10@50 | |
| | | 23~29 | D10@400 - | 9~29 | D10@360 | D10@360 | D10@360 | |
| | | | | 7~8 | D10@360 | D10@360 | D10@280 | |
| | R3 | 1.00 | D100100 | 2~6 | D10@360 | D10@280 | D10@190 | |
| | | 1~22 | D13@400 | 1 | D10@260 | D10@190 | D10@130 | |
| | R1 | 1~39 | D10@400 | 1~39 | D10@290 | D10@290 | D10@290 | |
| | R2 | 1~39 | D10@400 | 1~39 | D10@290 | D10@290 | D10@290 | |
| | | 26~39 | D10@300 | 14~39 | D10@210 | D10@210 | D10@210 | |
| | | 21~25 | D10@200 | 8~13 | D10@210 | D10@210 | D10@160 | |
| | T1 | 6~20 | D10@150 | 6~7 | D10@210 | D10@140 | D10@110 | |
| | | 3~5 | D16@300 | | D100150 | Discritio | D 100 P 0 | |
| Model C | | 1~2 | D13@150 | 1~5 | D10@150 | D10@110 | D10@70 | |
| | | 26~39 | D10@300 | 14 20 | D100010 | D100010 | D100010 | |
| | | 21~25 | D10@200 | 14~39 | D10@210 | D10@210 | D10@210 | |
| | T2 | 6~20 | D10@150 | 8~13 | D10@210 | D10@210 | D10@160 | |
| | | 3~5 | D16@300 | 6~7 | D10@210 | D10@140 | D10@110 | |
| | | 1~2 | D13@150 | 1~5 | D10@150 | D10@110 | D10@70 | |
| | | 6~39 | D10@400 | 2~39 | D10@240 | D10@240 | D10@240 | |
| | R3 | 1~5 | D13@300 | 1 | D10@240 | D10@240 | D10@160 | |

Table 5. Cont.

| Analytical Model | Coupling Beam | Story | Longitudinal | Stirrup | |
|------------------|---------------|-------|--------------|---------|---------|
| Analytical Would | Coupling Deam | Story | Тор | Bottom | Sunup |
| Model A | CB1 | 1~25 | 4-D13 | 4-D13 | D13@160 |
| | CB2 | 1~25 | 4-D13 | 4-D13 | D13@180 |
| Model B | CB1 | 1~29 | 4-D13 | 4-D13 | D13@160 |
| | CB2 | 1~29 | 4-D13 | 4-D13 | D13@180 |
| Model C | CB1 | 1~39 | 4-D13 | 4-D13 | D13@160 |
| | CB2 | 1~39 | 4-D13 | 4-D13 | D13@180 |

Table 6. Reinforcement of coupling beams.

In the nonlinear analysis of final design results, all the individual walls in Model A, B, and C satisfy the acceptance criteria on the inter-story drift ratio, plastic hinge rotation angle, and compressive extreme-fiber strain. Vertical distribution of diverse responses for a wall in Model A is shown in Figure 6a–c. All of the maximum values of peak responses along the entire stories are summarized in Table 7. The maximum of mean peak inter-story drift ratios for Model A, B, and C was 1.27%, 1.25%, and 0.85%, respectively, of which all satisfy the acceptance criteria described above. The demand-capacity ratio (DCR) for plastic hinge rotation angle in Table 7 are expressed in the ratio of the mean peak plastic hinge rotation angle and the acceptance criteria described above and meet the collapse prevention requirements. All the walls in three analysis models satisfy the collapse prevention criteria. It was also found that all compressive extreme-fiber strains are below 0.002.

The plots for 0, 1.2 and 1.5 are shown in Figure 6d. The maximum demand-to-capacity ratios for individual wall elements along the height are summarized in Table 7. The design of shear strength was performed for 1.0, 1.2, and 1.5 times the mean shear force demand in order to investigate the seismic fragility performance with respect to the design shear force level. In Table 7, there are shear walls designed with a DCR much lower than 1.0, which is the result of amplified shear force demands which do not reach the shear strength for the minimum reinforcement ratio defined in the KBC 2016 [1].

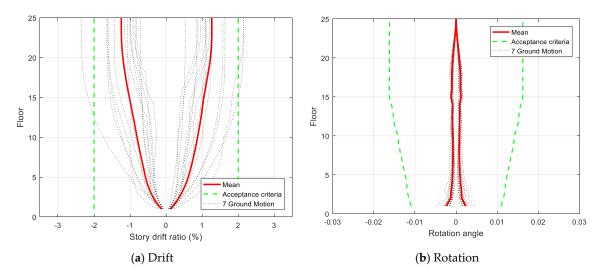


Figure 6. Cont.

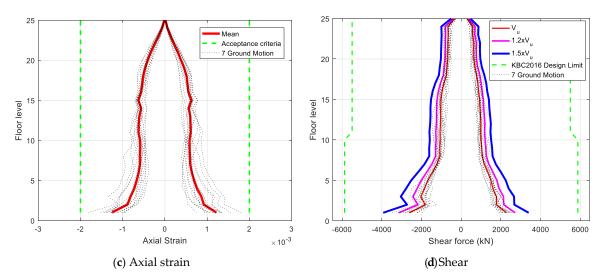


Figure 6. Example of design result for R3 in Model A.

| | | DCR (Demand/Capacity) | | | | | | | |
|---------------------|-------------------|-----------------------|----------|--------|---------------------------|--------------------|---------------------------|--|--|
| Analytical Model | Component Wall | Story Drift | Rotation | Axial | Shear | | | | |
| Widdei | vva11 | Ratio | Angle | Strain | Design to $1.0V_u$ | Design to $1.2V_u$ | Design to $1.5V_u$ | | |
| | R1 | | 0.19 | 0.53 | 0.40 | 0.48 | 0.60 | | |
| | R2 | | 0.40 | 0.77 | 0.72 | 0.86 | 0.99 | | |
| Model A | T1 | 0.70 | 0.26 | 0.75 | 0.64 | 0.77 | 0.97 | | |
| | T2 | | 0.19 | 0.92 | 0.99 | 0.99 | 0.99 | | |
| | R3 | | 0.39 | 0.83 | 0.99 | 0.98 | 0.99 | | |
| | R1 | 0.61 | 0.19 | 0.95 | 0.98 | 0.97 | 0.99 | | |
| | R2 | | 0.12 | 0.30 | 0.25 | 0.30 | 0.38 | | |
| Model B | T1 | | 0.31 | 0.50 | 0.46 | 0.55 | 0.69 | | |
| | T2 | | 0.30 | 0.75 | 0.81 | 0.97 | 0.98 | | |
| | R3 | | 0.17 | 0.82 | 0.99 | 0.98 | 0.98 | | |
| | R1 | | 0.15 | 0.55 | 0.70 | 0.84 | 0.99 | | |
| | R2 | | 0.30 | 0.87 | 0.99 | 0.96 | 0.98 | | |
| Model C | T1 | 0.48 | 0.15 | 0.26 | 0.06 | 0.08 | 0.10 | | |
| | T2 | | 0.18 | 0.44 | 0.17 | 0.20 | 0.25 | | |
| | R3 | | 0.17 | 0.51 | 0.28 | 0.34 | 0.42 | | |

| Table 7. Design results to | or average response of | t seven grounc | l motions. |
|----------------------------|------------------------|----------------|------------|
|----------------------------|------------------------|----------------|------------|

3. Seismic Fragility Assessment Procedure

3.1. FEMA P695 Procedure

A seismic fragility assessment for three analytical model was conducted using the procedure of FEMA P695, one of the methodologies for evaluating the seismic performance coefficients of structural systems that are not prescribed in the standard. The FEMA P695 procedure verifies if seismic-force-resisting systems have an acceptable probability of collapse and a collapse margin ratio (CMR) for the maximum considered earthquake based on the collapse fragility curve obtained by incremental dynamic analysis (IDA).

The spectral shape of ground motion records is an important factor that influences the result of IDA and the corresponding collapse fragility. Baker and Cornell found that the spectral shape for the MCE level ground motion of the western area of United States and the shape design spectrum shape of ASCE 7-05 are different significantly over a certain period of time [29–31]. In addition, the structural analysis for those spectra having such differences showed that there is a considerable difference in collapse prevention performance. Baker and Cornell proposed a conditional spectrum to compensate for that kind of difference. The conditional spectrum has a spectral acceleration corresponding to a specific return period at a control frequency, and spectral accelerations at other periods are determined

by a percentile conditional on the spectral acceleration at the control frequency. The conditional spectrum thus provides statistical information about the variability of the spectrum at periods other than the control frequency. In this study, ground motion suites for the IDA were selected and scaled using the conditional spectrum.

In FEMA P695, when the spectral shape of the general structural design standard is used, the CMR is modified to the adjusted collapse margin ratio (ACMR) using a correction factor called the spectral shape factor (SSF) to take into account difference in the spectral shape mentioned above. However, the conditional spectrum was used directly as the target response spectrum for ground motion suites used in the performance evaluation in this study. Therefore, values of ACMR in this study are the same as those of CMR without modification.

The FEMA P695 criteria for collapse prevention require that the CMR be above a specified allowable value and the collapse probability at the MCE level of spectral acceleration be less than 10%. An example of the seismic fragility curve in the form of a cumulative lognormal distribution function is shown in Figure 7, to illustrate those two collapse prevention criteria. In Figure 7, the CMR is defined as \hat{S}_{CT}/S_{MT} , where S_{MT} is the spectral acceleration corresponding to the fundamental mode period of the analytical model at the MCE level spectrum, and \hat{S}_{CT} is the spectral acceleration with 50% collapse probability in the fragility curve. The collapse probability is evaluated at S_{MT} .

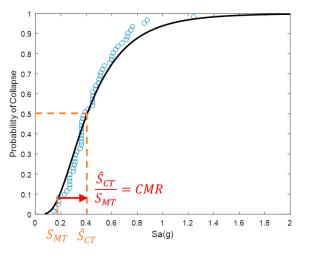


Figure 7. Example of seismic fragility curve.

The spectral acceleration at the first mode period $S_a(T_1)$ was used to represent the intensity measure (IM) of ground motion suites for IDA and the fragility assessment. Higher-mode contribution and period elongation are important factors in the case of high-rise buildings responding to earthquakes inelastically. An intensity measure, such as an average spectral acceleration for multiple periods including an elongated one, may be a better IM that can reduce dispersion and bias in the prediction of collapse [32]. Nevertheless, $S_a(T_1)$ was adopted for the IM in order to achieve consistency in the seismic hazard between design and fragility evaluation as well as to take into account variability in spectral shape by scaling ground motion records to the distribution of conditional spectra anchored to $S_a(T_1)$.

The standard deviation β_{TOT} of the lognormal distribution to account for uncertainty in the fragility curve was determined in accordance with FEMA P695 [4]. β_{TOT} is calculated by Equation (4).

$$\beta_{TOT} = \sqrt{\beta_{RTR}^2 + \beta_{DR}^2 + \beta_{TD}^2 + \beta_{MDR}^2} \tag{4}$$

where β_{RTR} is the record-to-record collapse uncertainty and was calculated based on the dynamic analysis results in this study. β_{DR} is the design requirements-related collapse uncertainty, β_{TD} is the test data-related collapse uncertainty, and β_{MDR} is the modeling-related collapse uncertainty. In FEMA P695, values of 0.1 to 0.5 are assigned to β_{DR} , β_{TD} , and β_{MDR} according to "Superior" to "Poor" grade of quality ratings for each uncertainty source. In this study, 0.2 was used uniformly for the three standard deviation assuming "Good" grade.

3.2. Ground Motion for Incremental Dynamic Analysis

Three ground motion suites were used in the IDA of each analytical model, respectively. All the selected ground motions in each suite have earthquake magnitudes between 6.0 and 7.0 and epicenter distance between 10 and 50 km. The mean shear wave velocities for the upper 30 m of the site profile at the record station is between 150-420 m/s, which are similar to the condition of site class S₄ applied to the design of the analytical models. Ground motions were chosen from the NGA-West2 ground motion database of the PEER, as in the design [13]. The ground motion records comprising a single suite were matched to the probability distribution as well as the median of the conditional spectrum by amplitude scaling in accordance with Baker and Lee's study [33]. The fundamental mode period of each analysis model was chosen for the control period of the conditional spectra. Figure 8 shows the target and matched ground motion spectra for analytical Model B.

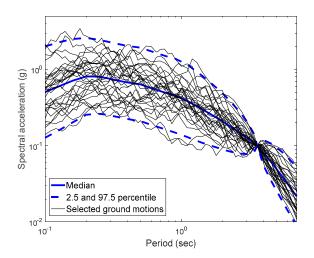


Figure 8. Target conditional spectrum and scaled GMRotD100 spectra for incremental dynamic analysis (Model B).

The individual ground motion suite is comprised of 30 pairs of horizontal components, much more than the seven pairs used for the design phase. Similar to the design of the analytical models, only the single horizontal component of ground motion was applied to the in-plane horizontal direction in a single IDA. Each component comprising a ground motion pair was applied to the IDA alternately, considering the randomness in the azimuth of ground motion. Therefore, total 60 IDA's were conducted in the in-plane direction for a total of 60 ground motion components, respectively.

Regarding the number of ground motion records, 22 pairs of horizontal components are used in FEMA P695 [4]. Baltzopoulos et al. conducted a study on an adequate number of ground motion records necessary to predict the collapse of moment-resisting frames with nonlinear dynamic analysis [34]. According to their research result, 40 to 100 ground motion records are required to achieve a coefficient of variation below 10% with respect to the result using 200 records. The 60 ground motion components used in this study is a reasonable choice considering both computational efforts and accuracy in collapse probability.

It was assumed that the target spectrum was defined in the direction of the maximum spectral acceleration and GMRotD100 spectrum of each ground motion suite is used in amplitude scaling of each suite. The GMRotD100 spectrum is the 100-percentile of the geometric mean dependent on period [35,36]. Figure 9a shows the GMRotD100 spectra of individual ground motion pairs and the target MCE spectrum for the Model B. Figure 9b,c compare the target spectrum and the individual ground motion spectra for each horizontal component, respectively, for the Model B. The median

spectrum and the target MCE spectrum for each direction have considerable difference in the spectral acceleration ordinate, but the difference is only slight at the control period.

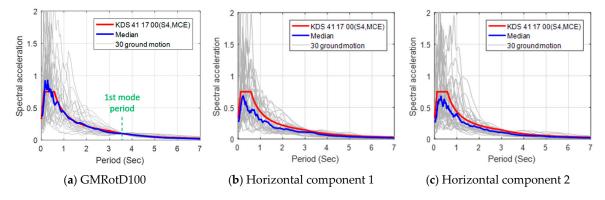


Figure 9. Target and scaled response spectra for Model B.

The ground motion suites for the design of the analytical models were scaled so that the mean SRSS spectrum is fit to 1.3 times the MCE spectrum, while those for IDA was scaled so that individual GMRotD100 spectrum has the same Sa(T1) as that of the MCE spectrum itself. The mean SRSS spectra of the ground motion suites for design and IDA is plotted, respectively, and compared to 1.3 times the MCE spectrum in Figure 10. The mean SRSS spectrum of the ground motion suite for IDA is lower than that for design at most periods longer than 0.2 s. For consistency between the design and performance evaluation, S_{MT} , the spectral acceleration at T_1 for MCE spectrum itself, is modified into S'_{MT} using a scale factor defined by the ratio of spectral accelerations at T_1 on the mean SRSS spectra for design and IDA. The scale factor for each analytical model and corresponding S'_{MT} are summarized in Table 8. In the following, the collapse probability and collapse margin of wall group models are calculated for S'_{MT} rather than S_{MT} .

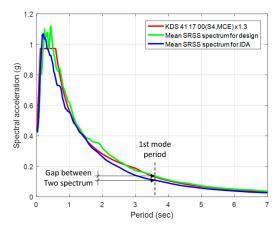


Figure 10. Mean SRSS Spectra of ground motion suites used for seismic design and performance evaluation.

Table 8. Spectral accelerations at the fundamental period for MCE.

| Analytical | Acceleration at T_1 on the | e Mean SRSS Spectrum | Scale Factor (a)/(b) | S _{MT} | S'_{MT} |
|------------|------------------------------|-----------------------|----------------------|-----------------|-----------|
| Model | For Seismic Design (a) | Reference for IDA (b) | | - 1/11 | - MI |
| Model A | 0.2336 | 0.1979 | 1.18 | 0.18 | 0.21 |
| Model B | 0.1338 | 0.1071 | 1.25 | 0.10 | 0.12 |
| Model C | 0.1645 | 0.1350 | 1.22 | 0.12 | 0.15 |

Four EDPs are considered in order to determine the collapse of the structure. Those EDPs include the rapid increase of inter-story drift, exceedance of the acceptable plastic hinge rotation angle, concrete compression failure at the boundary of wall section, and the shear failure, and are described as follows. Table 9 summarizes the acceptance criteria for the four EDPs and details are given in the following sections.

| Engineering Demand Parameter | Acceptance Criteria | | | | |
|-----------------------------------|--|--|--|--|--|
| Inter-story drift ratio | 20% of initial slope | | | | |
| Plastic rotation angle | Collapse prevention in ASCE 41-17 | | | | |
| Compressive extreme-fiber strains | 0.005 | | | | |
| Shear | $\begin{array}{l} 1.5V_n > V_u \text{ if } \theta/\theta_y < 2 \\ 0.7V_n > V_u \text{ if } \theta/\theta_y > 8 \\ 1.5V_n \text{ and } 0.7V_n \text{ are interpolated linearly when } \theta/\theta_y \text{ is between 2 and 8} \end{array}$ | | | | |

Table 9. Engineering demand parameters for seismic fragility assessment.

3.3.1. Inter-Story Drift

The first EDP is the maximum of the peak inter-story drift for entire stories. Figure 11a shows IDA curves with the horizontal axis of the inter-story drift and the vertical axis of the first mode spectral acceleration. The collapse of structures is a kind of instability and is identified by the rapid increase of the inter-story drift on the IDA curve. In other words, this is the case when the increase in spectral acceleration is small but the inter-story drift ratio is significantly increased. The collapse in this study is defined as the point on the IDA curve where the slope of the curve decrease to the 20% of the initial slope according to the recommendation by Vamvatsikos and Cornell [37]. However, when such a point did not occur, the point where the maximum inter-story drift ratio reaches 10%, which is judged to be a sufficient measure of instability, and was defined as the collapse point. The collapse points are marked with circles in Figure 11a.

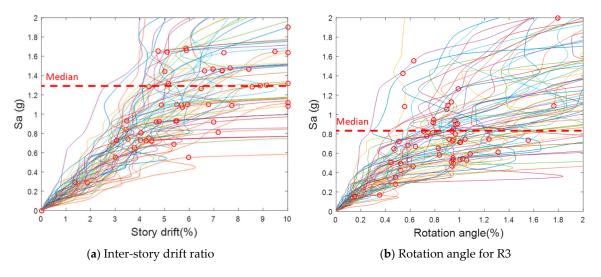
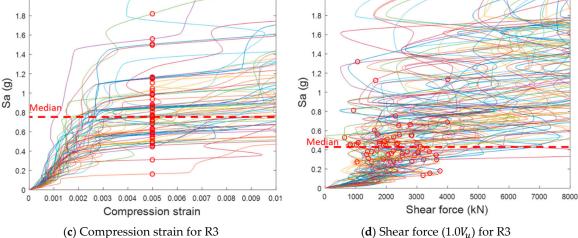


Figure 11. Cont.

2





2

Figure 11. Incremental dynamic analysis (IDA) results by failure mode (Model A).

3.3.2. Plastic Hinge Rotation Angle

The second EDP is the plastic hinge rotation angle of the wall element. The exceedance of acceptance criteria by at least one shear wall element was deemed collapse. The acceptance criteria for collapse prevention defined in ASCE 41-17 was adopted. The allowable plastic rotation angle is dependent on the extent of confinement at the boundary of the wall section and was determined for each analysis case, considering the axial force ratio and shear force demand determined from the dynamic response analysis results. IDA curves with respect to the plastic hinge rotation angle are plotted in Figure 11b for the component wall R3 in Model A. The circles represent a point where the EDP reaches the acceptance criteria. Plastic hinge rotation angles at the circles are different because they are dependent on the shear force demand for the wall.

3.3.3. Compression Strain

Thirdly, concrete compression failure at the boundary of the wall section can cause instability of the structure. The instability of the wall structure due to concrete compressive failure is assumed to occur when the compressive strain of concrete reaches a value where the stress drops to zero, passing through the peak stress at 25% of the wall length from the compressive extreme of the wall section as shown in Figure 12, according to the study of Gogus and Wallace and the NIST 10-917-8 report [6,7,38]. This is based on experiences showing that the instability of wall structures occurs in pushover analysis when concrete stress at such a place drops to zero. In this study, pushover analysis for the three analytical models was conducted to examine the adequacy of the acceptance criteria for the compressive strain at the specified location. The concrete model used in this study reaches residual strength (1% of the maximum strength) at the strain of 0.005, as mentioned in the preceding section. The results of the pushover analysis are shown in Figure 13, in which the roof drifts where the compressive strain reaches 0.005 at the point of 25% wall length, away from the compressive extreme of the section are also represented. As a result of the analysis, it is observed that a sharp drop of strength and the concrete compression failure at the specified location occur simultaneously. Therefore, the concrete compression failure criteria can predict collapse appropriately and included in collapse probability calculation. IDA curves with respect to the compression strain are plotted in Figure 11c for the component wall R3 in Model A. The circles represent a point where the compression strain reaches the acceptance criteria for the compression strain.

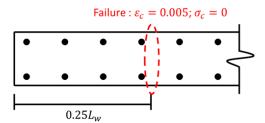


Figure 12. Concrete crushing in unconfined wall.

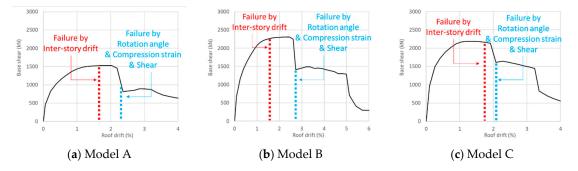


Figure 13. Result of pushover analysis and location of failure.

3.3.4. Shear Strength

In literature, decrease in shear strength with respect to flexural ductility was considered in the seismic evaluation based on existing experimental data [20,39,40]. This reduction of shear strength is caused by increasing damage due to flexural deformation. In this study, the envelope of the shear strength with respect to the flexural ductility suggested in the study by Gogus was adopted to examine whether the failure of shear components that are modeled elastically occurs or not after each nonlinear dynamic analysis. An example of shear failure envelope and the history of shear force with respect to flexural ductility is illustrated in Figure 14. In the illustrated model, 1.5 times the nominal strength is permitted when the flexural ductility is 2 or less, but only 0.7 times the nominal strength is permitted when the flexural ductility reaches 8 or more. When the flexural ductility value is between 2 and 8, linear interpolation is used. IDA curves with respect to the shear force are plotted in Figure 11d for the component wall R3 in Model A. The circles represent a point where the shear force reaches the acceptance criteria. Shear forces at those circles are different because they are dependent on the flexural ductility of the wall.

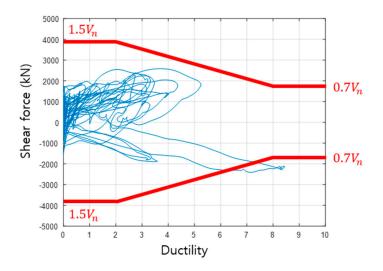


Figure 14. Example of shear failure (Model A, R3).

3.4. Processing the Result of IDA

The peak value of an EDP was calculated, and the corresponding acceptance criterion was checked for each story and component wall. The most critical story or component wall determined whether the failure occurred or not by the EDP. The collapse of a whole analytical model was determined by the EDP that exceeded the acceptance criteria at the lowest IM in the IDA for a single ground motion record. By fitting the IM–collapse probability relation, the seismic fragility curve for each analytical model was calculated. In a similar way, the seismic fragility curve can be calculated for each component wall.

4. Seismic Fragility Assessment Results

The result of seismic fragility assessment based on IDA is summarized for each component wall of three analytical models in Figure 15, and Tables 10 and 11. All the shear wall groups were designed to satisfy shear force demand with an amplification factor 1.2 to the mean peak shear force in accordance with the AIK guidelines. The seismic fragility curves in Figure 15 were constructed based on the failure mode that occurred at the lowest intensity measure among four failure modes investigated in the IDA. That is, if one of the four EDPs does not satisfy its acceptance criteria earlier than others, the corresponding intensity measure was used for the calculation of fragility curves.

FEMA P695 requires the collapse probability of individual building model to be limited below 20%, and the average collapse probability for the performance group comprised of different structural models with the same structural system to be limited below 10%. All the three analytical models have a collapse probability less than 20% in Table 10 if the maximum collapse probability among the component walls is defined as the collapse probability of the analytical model. Additionally, the average collapse probability among the three analytical models is 8.1%, which is below the 10% limit. As a result, all of the three analytical models satisfy the requirement for collapse prevention as prescribed in FEMA P695.

| Analytical Model | Component Wall | Length (m) | Axial Force Ratio (%) | MCE Collapse Probability (%) | Pass/Fail | |
|---------------------|-------------------|------------|--------------------------|---------------------------------|-----------|--|
| | R1 | 2.5 | 30 | 9.8 | - | |
| | R2 | 2.5 | 30 | 9.9 | Pass | |
| Model A | T1 | 3 | 15 | 3.7 | - | |
| | T2 | 3 | 15 | 5.5 | - | |
| | R3 | 9 | 15 | 7.3 | - | |
| | R1 | 2.5 | 30 | 4.4 | - | |
| | R2 | 2.5 | 30 | 5.6 | Pass | |
| Model B | T1 | 3.5 | 15 | 0.9 | - | |
| | T2 | 3.5 | 15 | 1.0 | - | |
| | R3 | 9 | 15 | 5.5 | - | |
| | R1 | 2.5 | 30 | 8.8 | Pass | |
| | R2 | 2.5 | 30 | 7.4 | - | |
| Model C | T1 | 4 | 10 | 2.4 | - | |
| | T2 | 4 | 10 | 3.5 | - | |
| | R3 | 9 | 10 | 5.3 | - | |
| | Performance gi | 8.1 | Pass | | | |

Table 10. Summary of collapse probability for analytical models designed for the shear force amplification factor = 1.2.

| Analytical Model | Component Wall | Length (m) | Axial Load Ratio | $S_{MT}^{'}$ | \hat{S}_{CT} | ACMR (1) | Acceptance ACMR _{20%} (2) | (1)/(2) | Pass/Fail | Representative ACMR (3) | Acceptance ACMR _{10%} (4) | (3)/(4) | Pass/Fail |
|--|-------------------|---------------|---------------------|--------------|----------------|-------------|---------------------------------------|---------|-----------|----------------------------|---------------------------------------|---------|-----------|
| | R1 | 2.5 | 0.3 | 0.21 | 0.42 | 2.02 | 1.59 | 1.27 | Pass | 2.03 | 2.09 | 0.97 | - |
| | R2 | 2.5 | 0.3 | 0.21 | 0.42 | 2.03 | 1.62 | 1.26 | | | | | |
| Model A | T1 | 9 | 0.15 | 0.21 | 0.52 | 2.53 | 1.56 | 1.62 | | | | | |
| | T2 | 3 | 0.15 | 0.21 | 0.48 | 2.43 | 1.62 | 1.50 | | | | | |
| | R3 | 3 | 0.15 | 0.21 | 0.41 | 2.25 | 1.62 | 1.39 | | | | | |
| | R1 | 2.5 | 0.3 | 0.12 | 0.29 | 2.42 | 1.56 | 1.55 | Pass | | | 0.97 | - |
| | R2 | 2.5 | 0.3 | 0.12 | 0.28 | 2.36 | 1.59 | 1.48 | | 2.36 2.02 | | | |
| Model B | T1 | 9 | 0.15 | 0.12 | 0.38 | 3.53 | 1.59 | 2.22 | | | 2.02 | | |
| | T2 | 3.5 | 0.15 | 0.12 | 0.35 | 3.53 | 1.59 | 2.22 | | | | | |
| | R3 | 3.5 | 0.15 | 0.12 | 0.24 | 2.42 | 1.59 | 1.52 | | | | | |
| | R1 | 2.5 | 0.3 | 0.15 | 0.35 | 2.28 | 1.69 | 1.35 | | | | | |
| | R2 | 2.5 | 0.3 | 0.15 | 0.33 | 2.19 | 1.59 | 1.37 | | | | | |
| Model C | T1 | 9 | 0.1 | 0.15 | 0.50 | 3.30 | 1.66 | 1.99 | Pass | 2.28 | 2.23 | 1.02 | - |
| R2 2.5 0.3 0.12 0.28 2.36 1.59 1.48 Model B T1 9 0.15 0.12 0.38 3.53 1.59 2.22 Pass 2.36 T2 3.5 0.15 0.12 0.35 3.53 1.59 2.22 Pass 2.35 R3 3.5 0.15 0.12 0.35 3.53 1.59 2.22 Pass 2.35 R3 3.5 0.15 0.12 0.24 2.42 1.59 1.52 Model C R1 2.5 0.3 0.15 0.33 2.19 1.59 1.37 Model C T1 9 0.1 0.15 0.50 3.30 1.66 1.99 Pass 2.2 Model C T1 9 0.1 0.15 0.45 3.13 1.73 1.81 R3 4 0.1 0.15 0.35 2.33 1.56 1.49 | | | | | | | | | | | | | |
| | R3 | 4 | 0.1 | 0.15 | 0.35 | 2.33 | 1.56 | 1.49 | | | | | |
| Performance group $A + B + C$ (Average) | | | | | | | | | | | 1.05 | Pass | |

Table 11. Summary of collapse performance evaluation for analytical models designed for the shear force amplification factor = 1.2.

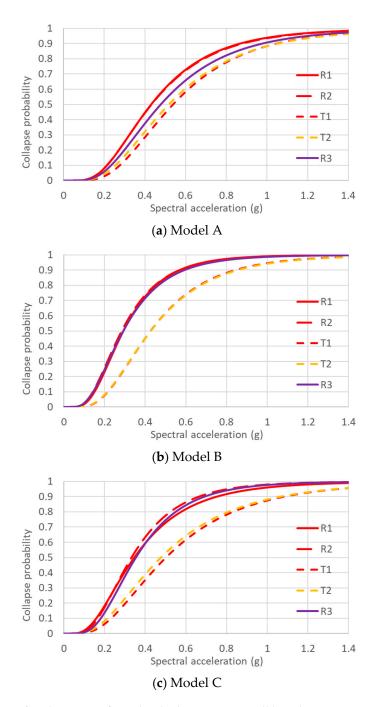


Figure 15. Seismic fragility curves for individual component wall based on governing failure modes.

The wall with the highest collapse probability in each wall group model has 2.5 m length and 30% axial force ratio from the observation of Model A, B, and C. In other words, it was found that the component walls with a high risk of collapse are short walls with large axial forces. This is supposed to be the result of the predominant effect of the compression failure at the wall boundary region, rather than shear failure.

ACMR is examined for individual models as well as the performance group comprised of all the three models in comparison with the FEMA P695 criteria $ACMR_{10\%}$ and $ACMR_{20\%}$, respectively. In Table 11, it is observed that the lowest ratio of ACMR over $ACMR_{20\%}$ in each wall group model is obtained for the wall with the highest collapse probability, e.g., R2 in Model A. It is observed that the ACMR_{20%} criteria corresponding to the 20% collapse probability are met for all of the three wall group models. When three wall group models are grouped as a single performance group, the acceptance

criteria ACMR_{10%} corresponding to the 10% collapse probability should be met for the average ACMR. After identifying the ACMR of the most vulnerable wall in each wall group model as a representative ACMR, three ACMRs are averaged and compared with the ACMR_{10%} acceptance criteria. As shown in the last row of Table 11, the performance group satisfies the ACMR_{10%} acceptance criteria.

Table 12 summarizes performance evaluation results for the performance group designed using different shear force amplification factors 1.0, 1.2 and 1.5 to the design shear force considering record-to-record variability. The same procedure and criteria as used in Tables 10 and 11 are used in the performance evaluation. It is observed that the collapse performance criteria of FEMA P695 were satisfied when the amplification factors 1.2 and 1.5 were used. However, the collapse performance criteria was not satisfied when the amplification factor 1.0 was used. In addition, amplification factor 1.5 improved the collapse probability at MCE and ACMR only minorly compared to amplification factor 1.2. Therefore, 1.2 can be a marginal value for the amplification factor of shear force.

| Evaluation Category | Performance Evaluation of MCE Collapse Probability | | | | |
|---|--|---------------------------|---------------------------|--|--|
| Evaluation Category | Design to $1.0V_u$ | Design to $1.2V_u$ | Design to $1.5V_u$ | | |
| MCE collapse probability (%) | 10.6 | 8.1 | 7.9 | | |
| Performance evaluation of MCE collapse probability (Less than 10%) | Fail | Pass | Pass | | |
| ACMR/ACMR10% | 0.97 | 1.05 | 1.06 | | |
| Performance evaluation of ACMR (ACMR ratio is 1 or higher) | Fail | Pass | Pass | | |

Table 12. Evaluation results for each design shear.

Figure 16 shows relationship between the axial force ratio and the collapse probability of individual component walls shown in Table 10. Component walls having an axial force ratio of 10% have collapse probabilities from 2.4 to 5.3% while component walls having an axial force ratio of 30% have a collapse probability from 4.4 to 9.9%. Therefore, the collapse probability of shear walls tend to increase as the axial force ratio of those walls increases. This result is consistent with the fact that the deformation capacity of shear walls usually decreases with higher axial force ratio.

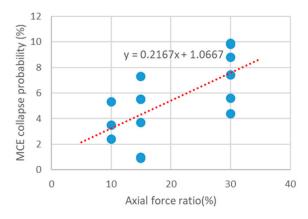


Figure 16. MCE collapse probability by axial force ratio.

In Figure 17, collapse fragility curves for individual walls comprising Model A are shown as an example. Those fragility curves were calculated for each EDP, respectively. Table 13 presents failure probabilities at the MCE for each EDP obtained from the collapse fragility curve plotted in Figure 17. The failure probability for each EDP was calculated for individual walls to determine which EDP is dominant. The EDP with the highest collapse probability among the five individual walls comprising a wall group model was chosen as the primary failure mode of the wall group model and is shown in Table 13.

| Analytical Model | Component Wall | Collapse Probability by MCE (%) | | | | | | – Primary Failure Mode | | | |
|---------------------|-------------------|---------------------------------|----------|-------------|--------|--------------------|--------------------|-------------------------------------|---------------------------|--------------------|--------------------|
| | | D :4 | Rotation | Compressive | Shear | | | i iiiiary railure Mode | | | |
| | | vvall | Drift | Angle | Strain | Design to $1.0V_u$ | Design to $1.2V_u$ | Design to $1.5V_u$ | Design to $1.0V_u$ | Design to $1.2V_u$ | Design to $1.5V_u$ |
| | R1 | 0.2 | 8.1 | 6.1 | 6.1 | 2.2 | 1.3 | Shear Rotation a | | e Rotation angle | |
| | R2 | 0.2 | 8.0 | 6.1 | 7.2 | 3.6 | 1.4 | | Rotation angle | | |
| Model A | T1 | 0.2 | 3.8 | 0.2 | 2.3 | 1.0 | 0.6 | | | | |
| | T2 | 0.2 | 5.1 | 0.1 | 2.9 | 0.7 | 0.1 | | | | |
| | R3 | 0.2 | 1.4 | 0.2 | 11.2 | 6.9 | 4.2 | | | | |
| | R1 | 0.1 | 4.2 | 2.1 | 0.9 | 0.9 | 0.7 | Shear | Rotation angle | Rotation angle | |
| | R2 | 0.1 | 4.3 | 2.2 | 2.5 | 1.4 | 0.9 | | | | |
| Model B | T1 | 0.1 | 0.3 | 0.4 | 1.6 | 0.7 | 0.4 | | | | |
| | T2 | 0.1 | 0.3 | 0.8 | 1.8 | 0.4 | 0.2 | | | | |
| | R3 | 0.1 | 1.8 | 0.3 | 11.4 | 4.9 | 2.0 | | | | |
| Model C | R1 | 1.9 | 2.2 | 6.6 | 5.3 | 5.3 | 5.3 | | | | |
| | R2 | 1.9 | 2.2 | 4.3 | 5.5 | 5.5 | 5.5 | Compressivestrain Compressivestrain | | | |
| | T1 | 1.9 | 0.6 | 1.0 | 2.0 | 1.5 | 1.6 | | Compressivestrain | | |
| | T2 | 1.9 | 0.5 | 0.9 | 2.7 | 2.3 | 2.2 | | | | |
| | R3 | 1.9 | 1.0 | 0.5 | 4.2 | 4.2 | 2.5 | | | | |

Table 13. Primary failure mode by analysis model.

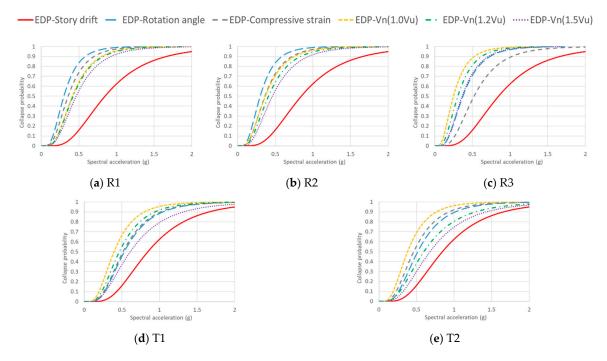


Figure 17. Seismic fragility curve for individual engineering demand parameters (EDPs) and acceptance criteria (Model A).

For individual component walls of Model A, the plastic hinge rotation angle has the highest collapse probability in most walls, but the highest collapse probability (11.2%) observed in the longest wall (R3) corresponds to the shear failure for amplification factor 1.0. As a result, the primary EDP changes from shear failure to plastic hinge rotation angle failure as the amplification factor to shear increases from 1.0 to 1.2 and 1.5, which reduces the potential of shear failure in the walls. Model B has a tendency similar to Model A, but shear failure is the primary failure mode of T1 and T2 as well as R3, and the transition from shear failure to plastic hinge rotation angle failure occurs at the amplification factor 1.2. In the case of the Model C, unlike the other two models, the wall with the highest collapse probability was R1, of which the failure mode is the compressive axial strain failure without change, in spite of the increasing amplification factor to shear force. This is due to the high axial force ratio of R1 caused by the small cross-section area and the characteristics of high-rise buildings. On the whole, the amplification factor to shear force 1.2 is enough to prevent shear failure from being the primary failure mode of the analytical model.

5. Conclusions

In this study, the seismic performance of the ordinary RC shear wall system, which is widely adopted for high-rise residential apartment buildings in South Korea, was assessed and an adequate amplification factor to wall shear forces was investigated. Three analytical models composed of five ordinary RC shear walls taller than 60 m were designed for seismic design category D using a performance-based procedure to circumvent limitations on the seismic force-resisting system in KBC 2016. Seismic performance evaluation was performed in accordance with the procedure and criteria of FEMA P695 based on incremental dynamic analysis. A total of four engineering parameters were taken into account, including inter-story drift, plastic hinge rotation angle, concrete compressive strain at the boundary of wall section, and shear force. Based on the result of seismic fragility assessment for the three analytical models, the ordinary RC shear walls designed with a shear force amplification factor higher than or equal to 1.2 can meet the performance criteria on collapse probability and the collapse margin ratio. Implications obtained for limited conditions of this study are summarized as follows.

- 1. The shear force of individual walls at each story is the primary engineering demand parameter contributing to the collapse probability most significantly when the shear force amplification factor 1.0 is applied to the design of individual walls. However, the collapse of analytical models designed with a shear force amplification factor higher than or equal to 1.2 is governed by flexural failure, determined by plastic hinge rotation angle. Therefore, the amplification factor 1.2 is recommended for the design shear force in the performance-based procedure to prevent brittle failure and the collapse of ordinary RC shear wall systems with regular configuration and rigid diaphragms. However, a 1.5 or higher amplification factor may be required for buildings with irregular configuration or flexible diaphragms due to contribution from higher modes.
- 2. Component walls with relatively high stiffness tend to fail in shear, given the collapse probability of individual component walls. Therefore, it is recommended that an amplified design shear force at the initial elastic design stage is used, considering the amplification expected in the nonlinear dynamic analysis in order to reduce the number of iterative nonlinear analyses. However, the amplification factor may be reduced for component walls with relatively low stiffness in which shear failure is anticipated to be insignificant.
- 3. Taller ordinary RC shear walls tend to be less sensitive to the shear force amplification factor than lower walls. In this case, increasing the shear force amplification factor has little impact on performance improvement. Therefore, the shear force amplification factor can be determined considering the primary failure mode.
- 4. In case of thin walls comprising the majority-part of residential buildings in Korea, it is very difficult to install hoops required for special RC shear walls, because the spacing is smaller than one third of the wall thickness. For buildings higher than 60 m and located at the area of seismic category D, the ordinary RC shear wall system with simple reinforcement details can be adopted as an alternative to the special RC shear wall and designed using a performance-based procedure with appropriate acceptance criteria satisfying required collapse margin as shown in this study.
- 5. The result of this study is limited to ordinary shear wall structures with regular configurations and rigid diaphragms, since there is a limited number of two-dimensional analytical models. This study can be utilized as a basis for further study, considering the effects of irregular configuration and flexible diaphragms that are present in actual building structures.

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