



Article Real-Time, Deep Learning Based Wrong Direction Detection

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Featured Application: The result of this paper is a deep-learning-based application for vehicle moving-violation detection, which achieves effective detection performance under various lighting conditions. The technique can be used as an assistance tool for on-road closed-circuit television cameras.

Abstract: In this paper, we develop a real-time intelligent transportation system (ITS) to detect vehicles traveling the wrong way on the road. The concept of this wrong-way system is to detect such vehicles as soon as they enter an area covered by a single closed-circuit television (CCTV) camera. After detection, the program alerts the monitoring center and triggers a warning signal to the drivers. The developed system is based on video imaging and covers three aspects: detection, tracking, and validation. To locate a car in a video frame, we use a deep learning method known as you only look once version 3 (YOLOv3). Therefore, we use a custom dataset for training to create a deep learning model. After estimating a car's position, we implement linear quadratic estimation (also known as Kalman filtering) to track the detected vehicle during a certain period. Lastly, we apply an "entry-exit" algorithm to identify the car's trajectory, achieving 91.98% accuracy in wrong-way driver detection.

Keywords: convolutional neural networks (CNNs); intelligent transportation system (ITS); you only look once version 3 (YOLOv3); linear quadratic estimation (LQE)

1. Introduction

With the development of the fourth industrial revolution, the role of the intelligent transportation system (ITS) is becoming more and more crucial for ensuring the safety and efficiency of drivers. The purpose of a vision-based ITS is to extract useful and precise traffic data, and to use surveillance technologies as efficiently as possible. According to the National Information Society Agency, there were more than eight million closed-circuit television (CCTV) cameras installed in Korea by the year 2018, which gives the country one of the highest cameras-per-capita rates in the world. CCTV footage certainly cannot be a perfect solution for all traffic violations. However, it is widely and increasingly used by government officials to identify serious violations, along with evidence, testimonies, and documents. Typically, driving the wrong way down a road happens for several reasons: the driver is distracted or confused; the driver did not notice the pavement markings or traffic signs; the driver intentionally breaks the rules; etc. Even though recent pavement delineations and signs are innovative, they might not be enough to alert drivers to wrong-way entry, and car accidents continue to happen. Even though it is almost impossible to control human driving behavior, it is important to classify and understand irregular activity in usual traffic scenarios in order to prevent serious car crashes. So far, the identification task is performed by people who work in monitoring companies. Nevertheless, with the significant increase in camera devices, the need for automated intelligent software is demanded even

more. Wrong-direction detection technologies can be divided into three major categories: sensor-based detection, radar-based detection, and video imaging-based detection. The focus of this research is to automate the recognition of moving violations, thus requiring less human interaction, as well as to identify (using a single video camera) vehicles entering traffic the wrong way onto the highway system (Figure 1).

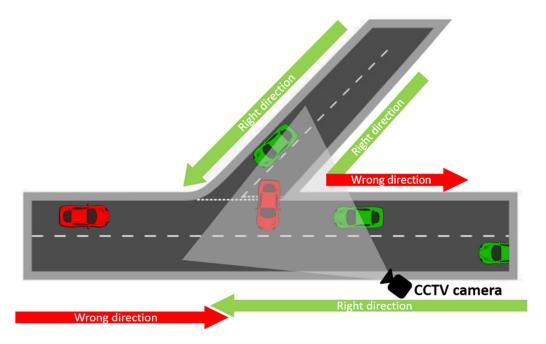


Figure 1. Wrong-direction detection scenario (triangle represents camera's visible region).

While our proposed system relies on video imaging-based detection, it references three different computer vision challenges such as vehicle's localization, tracking, and determining direction. Vision-based learning is one of the cheapest methods and requires lower labor costs by saving people's time, as well as lowering costs by using fewer machines and by eliminating faulty products.

2. Background

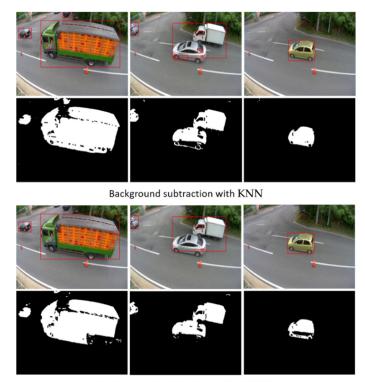
To determine a car's direction, the car itself should be identified, so detection is the first step in our research. Wrong direction estimation is not a contemporary problem, and in this section, we describe and implement different techniques in computer vision to compare different detection and tracking algorithms for vehicles. These techniques include well-known machine learning and deep learning methods.

2.1. Vehicle Detection and Segmentation

2.1.1. Detection Using Background Subtraction

Background subtraction (BS) is a widely used technique for applying a foreground mask for static cameras. Moving objects in the foreground are separated by calculating the foreground mask and subtracting it from the current frame and background model, containing the static part of the scene. Everything moving is considered characteristic of the foreground. BS is performed using two main functions: background initialization and background update. BS algorithms have already been implemented in open-source computer vision libraries such as OpenCV. In OpenCV, two background subtraction methods were implemented: k-nearest neighbor (KNN) algorithm [1] and Gaussian mixture-based background/foreground segmentation algorithm (MOG2) [2,3].

BS showed instability on the false positive detections when it detected several closely located cars as one (Figure 2). The method is very sensitive to changing lighting conditions and, as an example, the results obtained during nighttime could be unacceptably inaccurate.



Background subtraction with MOG2

Figure 2. Comparison between two background subtraction methods. KNN: k-nearest neighbor; MOG2: Gaussian mixture-based background/foreground segmentation.

2.1.2. Optical Flow

One of the machine learning methods for locating a car is an optical flow which is the pattern learning of a moving object. The most widely used optical flow method in computer vision is called the Lucas–Kanade method [4]. The basic idea of optical flow is to assume that the color or intensity of a pixel is constant under displacement from one frame to the next. This optical flow estimation algorithm also assumes that an object's frame-to-frame displacement distance is small and local. In addition, the objective measurement of the local level of reliability of motion information is provided. Shi and Tomasi [5] increased tracking performance by modifying the "good feature" selection criterion of reliability in order to evaluate the texture features of areas, which later led to the creation of the Kanade–Lucas–Tomasi (KLT) tracker [6] (see Figure 3). However, according to Barron et al. [7], optical flow computation techniques are very sensitive to noise and object illumination. Generally, optical flow can be unreliable in cases where the brightness intensity changes, and object occlusions happen. Since our task in focus requires a minimal error rate, usage of optical flow as a detector could be unacceptable due to the changing lighting and weather conditions.

Monteiro et al. [8] described optical flow-based wrong-way driver detection. Their proposed system was separated into three main stages: learning, detection, and validation. For the learning stage, which is the car detection phase, they combined the Lucas–Kanade optical flow method with Gaussian mixture models [9]. They mentioned that their system could detect vehicles moving in the wrong direction from a 320×240 pixel image at 33 frames per second (fps). Accordingly, the experiments conducted on many scenes demonstrated that their proposed system has the following properties: wrong-way vehicle detection, speed, and robustness to illumination and weather conditions. However,

the simulation results and experiments on system accuracy were insufficient to prove the applicability of their method.



Figure 3. Detection with optical flow using the Lucas–Kanade method.

2.1.3. Convolutional Neural Network (CNN)-Based Detection Methods

Convolutional neural networks (CNNs) are predominantly used as learning structures for image understanding. The benefits of using CNNs are that fewer learning parameters might be used, which greatly improves the learning time and reduces the amount of data required to train the model. A convolution is a weighted sum of the pixel values of an image as the window slides across the whole image. Basically, the convolution process throughout an image with a weight matrix produces another image. The CNN-based approach may be considered one of the best ways to precisely detect a vehicle's position in an image, and so far, it includes sophisticated methods such as the single shot multiBox detector (SSD) [10], the faster regional CNN (faster R-CNN) [11], and you only look once (YOLO) [12]. All these methods have a similar average precision on detections. However, there is a significant difference in the inference time with each method. Although the faster R-CNN (a region proposal network) was the best detection method on Pascal Visual Object Classes (VOC) and Common Objects in Context (COCO) dataset challenges in 2012 and 2015, respectively, we decided to use the YOLOV3 network due to the speed performance.

As Figure 4 shows, all the compared methods have similar mean average precision, but with a huge gap between them for processing times. Since our project is highly reliant on fast processing, we chose to use YOLOv3-416 which took 29 ms to process the COCO dataset.



Figure 4. Performance and inference time of detection methods [13].

2.2. Vehicle Tracking

Car tracking is based on object-tracking techniques and includes three main processes: (1) taking an initial set of detected objects; (2) registering the detected cars and giving them unique identifications (IDs); (3) tracking them as they move around a continuous frame, maintaining the ID assignments, and erasing them once the cars disappear. Moreover, object tracking allows us to count several cars in a frame by counting unique object IDs. Ideally, an object tracking algorithm must satisfy the following conditions:

- require the object detection phase only once;
- be much faster than the actual object detector itself;
- handle a tracked object that "disappears";
- be robust to occlusions;
- pick up objects that are "lost" between frames.

2.2.1. Contour-Based Tracking

The main idea behind contour-based tracking is to define the boundaries of a vehicle. Ambardekar et al. [14] proposed pose detection of a vehicle by using optical flow and camera parameters. According to the authors, part of the system tracks the blobs and tries to correct the errors from the foreground object detection module by estimating the three-dimensional (3D) world coordinates of the points on the vehicles. The system then groups those points together to segment and track the individual vehicles. The authors emphasized that their proposed technique has occlusion detection and multi-vehicle tracking [15].

2.2.2. Kalman Filter for Tracking

Kalman filtering also known as linear quadratic estimation (LQE) is a series of measurements observed over time (in our case, frame by frame). The Kalman filter is a powerful tracking method, for extracting motion from video sequence surfaces over collections of points. It is an optimal estimator that infers the parameters of interest from indirect, inaccurate, and uncertain observations. The Kalman filter consists of two steps: prediction and update. The first step uses previous states to predict the current state. The second step uses the current measurement, such as detection of bounding box location, to correct the state. The Kalman filter has the following important features that tracking can benefit from:

- predict the object's upcoming location;
- correct the prediction based on new measurements;
- reduce noise introduced by inaccurate detection;
- facilitate the process of associating multiple objects with their tracks.

The Kalman filter tracker is fast, which is an advantage over other tracking algorithms. Therefore, we updated the original algorithm and used it in our project as the main tracking method.

Despite quite the variety of methods, we focus on improving the time speed of detection, robustness in different lighting conditions, and accuracy. Therefore, we combined the YOLOv3 method for detection with the Kalman filter for tracking estimation.

3. Proposed System

3.1. Detection and Tracking

We separate our task into three main steps: detection, tracking, and direction checking. YOLOv3 is an object detection method targeted at real-time video processing. The result of the YOLOv3 model extracts a vehicle's bounding box information in order to apply robust tracking algorithms and identify direction.

First, we send a continuous frame to the pre-trained YOLOv3 model that returns us bounding boxes of vehicles. Our algorithm is based on centroid tracking, which is a multi-step process. Centroid tracking assumes that we are passing (x, y)-coordinates in a set of bounding boxes for each detected object in each frame. Once we have the bounding box coordinates, we compute the "centroid" (i.e., the center (x, y)) coordinates of the bounding boxes. Since these are the initial set of bounding boxes presented to our algorithm, we assign them unique IDs. Then, we calculate the cost value between the detected car and its prediction. If there are multiple detections, we need to assign each of them to a tracker. We use intersection over union (IOU) of the tracker bounding box and detection bounding box as a metric. We maximize the sum of the IOU assignment using the Hungarian algorithm [16]. The machine learning package scikit-learn has a build-in utility function that implements the Hungarian algorithm. Then we implement updated Kalman filter equations that are described by Welch and Bishop [17] to predict multiple car objects from a video frame.

1. Prediction phase Notations: *x*—state mean, *P*—state covariance, *F*—state transition matrix, *Q*—process covariance, *B*—control function (matrix), *u*—control input.

$$\overline{x} = Fx + B * u$$
 Predicted (a priori) state estimate; (1)

$$\overline{P} = FPF^T + Q \text{ Predicted (a priori) error covariance.}$$
(2)

2. Update phase Notations: *H*—measurement function (matrix), *z*—measurement, *R*—noise covariance, *y*—residual, *K*—Kalman gain.

$$y = z - H\overline{x}$$
, Innovation or measurement pre – fit residual; (3)

$$S_k = HPH^T + R$$
, Innovation (or pre – fit residual) covariance; (4)

$$K = \overline{P} * H^T * S_k^{-1}, \text{ Optimal Kalman gain;}$$
(5)

$$x = \overline{x} + K * y$$
, Updated (a posteriori) state estimate; (6)

$$P = (I - KH)\overline{P}$$
, Updated (a posteriori) estimate covariance; (7)

$$y = z - H * \hat{x}$$
, Measurement post – fit residual. (8)

The formula for the updated (a posteriori) state estimate works each time for the measurement update pair. The process is repeated with the previous (a posteriori) estimates used to project or predict the new (a priori) estimates. An implementation of the updated Kalman filter algorithm can be found in **Algorithm 1**. Then we used OpenCV drawing libraries to draw tracking lines on each detected car. Figure 5 presents the full pipeline of our proposed method.

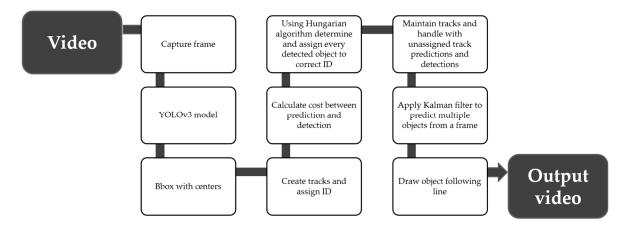


Figure 5. Detecting and tracking pipeline. YOLOv3: you only live once version 3.

Algorithm 1.	Pseudo-code	for Kalman	filter tracker.
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Object tracking function (<i>x</i> , <i>y</i> centroid)
for (iterate \geq number of detected centroids):
if (no track vectors found)
Create tracks
Calculate cost using sum of square distance
Assign detected measurements to predicted classes using Hungarian algorithm
if (tracks with no assignment)
Identify tracks
if (tracks are not detected for long time)
Delete tracks
else
Start new tracks
Update Kalman Filter state, last results and tracks trace

3.2. Direction Estimation

This section describes the method for vehicle trajectory estimation. To check the direction of a tracked vehicle we calculate the difference in the pixels in the F_N -frames range, where N- is the number of frames to track a unique vehicle. First, we calculate the centroid from a detected car's bounding box and set it to be the initial points (X_0 , Y_0) in the frame (F_0). Then, as the car moves, the position of the centroid changes from frame to frame. Thus, we calculate the pixel difference in the range (X_1 , Y_1) to (X_N , Y_N) for each frame, where X_1 , Y_1 indicates the car's centroid position in the frame (F_1), along with X_N and Y_N in frame (F_N). For example, let us assume we use six frames for tracking. The pixel position difference would be $\Delta X = X_5 - X_1$. Basically, we take the second frame as an initial starting point and the sixth frame as the ending point. This is due to the ID assignment step that is done on the first frame as soon as a car is detected. To find the direction, we do simple math: if ΔX is negative and X_5 is smaller than X_1 , the car is moving from right to left; vice versa, then it is moving left to right. **Algorithm 2** describes the pseudo-code to validate the car's direction.

Algorithm 2. Pseudo-code for the direction check.
if (length of centroids > 0)
for (iterate \geq number of detected centroids):
for (iterate $\geq N$, where N number of tracking frames for unique cars)
take X_1 , Y_1 positions from tracker
take ID for unique car
$\Delta X = X_N - X_1$ if (check ΔX sign and X_1 with X_2)
assign direction

Figure 6 visually explains the changing vehicle's position within N = 6 frames. Green dots show the displacement of the car through each frame. The displayed text "West" in this case shows that the car in the video is moving from right to left.

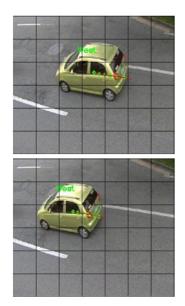


Figure 6. Displacement of a car within N = 6 frames.

3.3. Direction Validation

To determine if the car is going the right way, we created the entry-exit approach. The idea behind it is simple and effective. We create imaginary entry lines on the video frame. If a vehicle crosses the entry lines, the given unique ID of the car is stored in a list, and if it passes through the exit area the ID is removed from the list.

As seen in Figure 7, we crop the video frame to the required region of interest. Traffic must go from the right side to the left (lines 1–4). Green lines represent correct entry and exit directions. Red lines represent directions in which vehicles must not move (lines 5–7). We create three imaginary areas for entering and exiting. Imagine the usual case when the car enters the first area. In such a case, when the car's centroid passes through area A, the ID of the car is stored in list 1 and remains there until the car exists from any exit. If the car enters from area B, the ID is stored in list 2 and the car must exit in area C; otherwise, the car will be detected as the moving the wrong way, and a warning signal will be triggered. If the car enters in area C, this is always the wrong way and the ID of the car is stored in list 3 to check the area from which it exited. Even if a car enters from area C, the alert signal is sent when the car is moving. The algorithm validates according to the vehicle's centroid position.

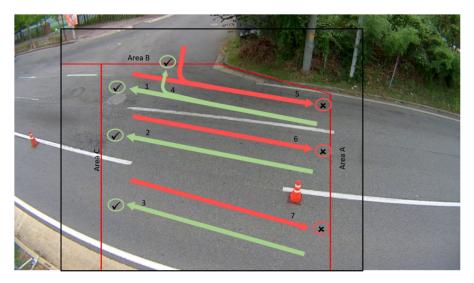


Figure 7. The entry-exit approach (black lines represent the borders of the frame).

4. Experiments and Results

We conducted two types of experiments to check the efficiency of our work. The first consisted of checking the car-detection accuracy under different lighting conditions, and the second consisted of wrong-way driver detection. We were provided access to a real-world camera and created a simulation with a car moving the wrong way.

4.1. Datasets

Data used in our project were taken from a fixed CCTV camera. We create two types of datasets: one is for network training and testing and the other is for wrong direction checking. For the first dataset, we have extracted 12 videos taken at different times of the day. We extract all the frames from every video and randomly split them into training and testing at 70% and 30%, respectively. The second type of dataset is used to check the wrong-direction detection, so it contained only data of a car moving in the wrong way.

4.2. YOLOv3 Model Training

For the detection experiments, we trained the model by annotating real-world data. We had video files from which we extracted frames and created our own CCTV dataset. We annotated extracted images with a specific program [18] and trained our YOLOv3 network using 1750 images on a PC with an NVidia RTX 2080Ti GPU, an Intel Core i5-7600 CPU, and 16 GB RAM. We chose YOLOv3-416, in which images are resized to 416 × 416 pixels, with learning rate $\alpha = 10^{-3}$ batch size = 64 on frozen layers, and batch size = 8 for unfrozen ones, over 100 epochs. We used the Adam optimizer with $\alpha = 10^{-3}$ for frozen layers and $\alpha = 10^{-4}$ after unfreezing the layers. The YOLOv3 network convergence time depends on the quantity of data used in training; so, in our case, it took four to five hours to converge. Since our model is trained with images from the camera used in one fixed position our model applies only to the particular camera.

4.3. Detection Testing

To test detection performance, we created another dataset from unseen videos. Next, we manually calculated the number of cars appearing in those videos. Then, we randomly selected videos taken at different time intervals. We chose various time intervals including morning, afternoon, dusk, and evening times. For evaluating detection precision, we decided to calculate the mean average precision (mAP or μ) with IOU threshold $\mu \geq 0.75$, where the mAP with threshold is found by,

$$\mu = \frac{\text{bounding box area of detected car}}{\text{bounding box area from manual annotation}} \ge 0.75$$
(9)

We manually counted the number of cars that appeared within the mentioned intervals and annotated them to determine the cars' positions in a frame. We counted only unique cars. The car was considered as correctly detected one only when the IOU rate was above 0.75. As seen in Table 1, the detection method identified cars with average mAP of 90.80% for both daytime and nighttime. The reason for the slight change in mAP is the different lighting conditions. Since our application is supposed to be used in real-world scenarios, we tested it for precision and speed. Therefore, along with precision, we also checked the processing time of our algorithm, which was similar to that of Redmon and Farhadi [16]. Despite having only one class to detect, we achieved a higher mAP score than the authors of the original YOLOv3 (see Figure 4).

Time Interval 10:23-10:25 13:49-13:52 15:50-15:54 18:05-18:07 21:10-21:13 Results 250 Num. of cars 30 44 85 50 41 227 Detected cars 27 41 80 44 35 mAP > 0.75 (%) 90.00 93.18 94.12 88.00 85.36 90.80 APT (ms) 25 26 28 29 27

mAP: mean average precision; APT: average processing time (ms: milliseconds).

To justify the efficiency of our work, we provided a qualitative experiment. Testing wrong-way detection is based more from the structure of the related facts than from the testing of the existing assumption. Therefore, we tested our implemented "entry-exit" algorithm for wrong-direction detection on two types of data: real data and simulated data. Due to the difficulty in getting actual wrong way driving events, we simulated them by intentionally driving a car the wrong way. For the first simulation case, we checked daytime wrong-direction detection. As illustrated in Figure 7, a car going the wrong way enters from area C and is tracked until it reaches area A, which in this case is where it exits. As soon as it reaches area C, image and information about the car were sent to the monitoring center using the File Transfer Protocol (FTP) and Transmission Control Protocol (TCP). The program detects moving vehicles from an 807×646 video frame at 30 fps.

Due to safety reasons, Korean road traffic authority (KoROAD) did not allow us to simulate driving during nighttime. Therefore, for the second and third simulation cases we inverted daytime and nighttime videos as shown in Figure 8 to check true-positive results. Results obtained from the first simulation case can be seen in Table 2 where 'positive direction' is the number of cars moving in the correct direction, and 'negative direction' is the number of wrong-way driving cases. For case 1 we considered the case when the car was driven wrong-way in the daytime, where N is the total number of unique cars. For case 2 we considered a horizontally flipped video from case 1 and finally for the third case we took a flipped nighttime video to check the accuracy during nighttime. The reason we flipped the video frame is that Monteiro et al. [8] used the image flipping method to check the accuracy of their system. From Table 2 we can measure the performance of our wrong-direction detection system (Table 3). Visual results are presented in Figure 8.

Case 1: N = 114	Predicted Positive Direction	Predicted Negative Direction
Positive direction	110	0
Negative direction	0	4
Case 2: N = 114		
Positive direction	0	0
Negative direction	12	102
Case 3: N = 36		
Positive direction	0	0
Negative direction	5	31

Table 2. Confusion matrix for three simulation cases (quantity of cars).

Table 3. Performance measurement in (%).

Cases	Accuracy	Precision	Recall	F1 Score
Case 1: Daytime	100.00	100.00	100.00	100.00
Case 2: Daytime (flipped)	89.83	100.00	89.00	94.44
Case 3: Nighttime (flipped)	86.11	100.00	86.00	92.53

Another evaluation we conducted determined false-positive results. The system was tested for 24 h to identify the number of false-positives. Our program counted 5552 cars passing by the camera within 24 h, identifying only one false-positive that occurred owing to the car's illumination at night (Table 4). Visual results on determining false-positive cases can be seen on Figure 9.

Table 4. Confusion matrix for real-world cases.

N = 5552	Predicted 'NO'	Predicted 'YES'
Actual 'NO'	5551	1
Actual 'YES'	0	0

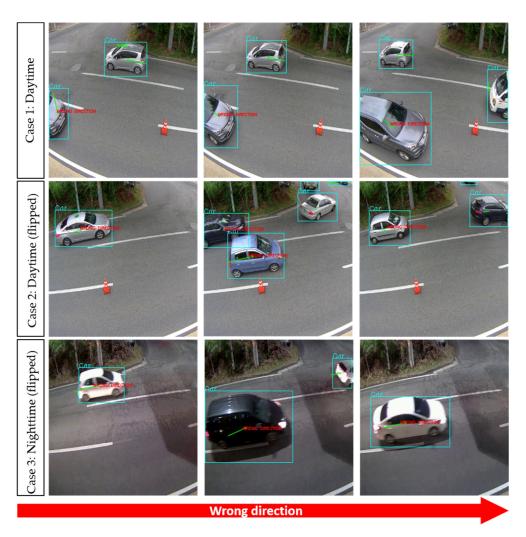


Figure 8. Wrong-direction detection for the three simulation cases.

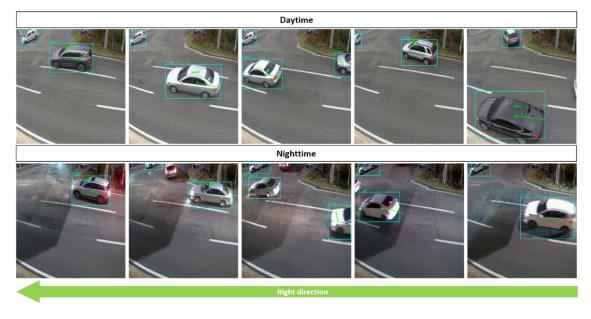


Figure 9. Real-time detection example during both daytime and nighttime.

5. Conclusions and Future Work

We propose a combined state-of-the-art YOLOv3 method with an updated linear quadratic equation to detect and track vehicles. To identify vehicles traveling in the wrong direction, we contributed a unique "entry-exit" method; and for simulation, in the three cases, we achieved an averaged accuracy of 91.98% in wrong-direction detection results. This system, as shown by the results obtained from simulations, presents excellent performance under various lighting conditions, so we can implement the program with real-world cameras. The current system works at 30 fps and was implemented on one of the roads in South Korea as a part of ITS solutions. Despite the good performance, our next milestone is adding new detection features to our network. As we experimented, we found many cases where pedestrians crossed the road in a prohibited area, so the next step in our research is to add violation detection of jaywalking.

Author Contributions: S.U. contributed towards the detection and tracking code. S.U. also worked on background system checks by implementing other researchers' works. S.U. worked on improvement parts as well as analysis of a system and performed experiments. S.B. provided the experiments by recording and making the result tables and made visualizations and figures for the paper. S.B. also worked on frame extractions and annotations. K.J.W. provided all the data we used in this research and found a place where we could test our system in real-time. K.J.W. was the motivator and provided guidance about the "entry-exit" approach for direction validations and gave practical advice throughout the whole research process. All authors have read and agreed to the published version of the manuscript.

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Conflicts of Interest: The authors declare they have no conflicts of interest.

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