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In Situ X-ray Measurements to Follow the Crystallization of BaTiO₃ Thin Films during RF-Magnetron Sputter Deposition

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Abstract: Here, we report on adding an important dimension to the fundamental understanding of the evolution of the thin film micro structure evolution. Thin films have gained broad attention in their applications for electro-optical devices, solar-cell technology, as well storage devices. Deep insights into fundamental functionalities can be realized via studying crystallization microstructure and formation processes of polycrystalline or epitaxial thin films. Besides the fundamental aspects, it is industrially important to minimize cost which intrinsically requires lower energy consumption at increasing performance which requires new approaches to thin film growth in general. Here, we present a state of the art sputtering technique that allows for time-resolved in situ studies of such thin film growth with a special focus on the crystallization via small angle scattering and X-ray diffraction. Focusing on the crystallization of the example material of BaTiO₃, we demonstrate how a prototypical thin film forms and how detailed all phases of the structural evolution can be identified. The technique is shaped to enable a versatile approach for understanding and ultimately controlling a broad variety of growth processes, and more over it demonstrate how to in situ investigate the influence of single high temperature sputtering parameters on the film quality. It is shown that the whole evolution from nucleation, diffusion adsorption and grain growth to the crystallization can be observed during all stages of thin film growth as well as quantitatively as qualitatively. This can be used to optimize thin-film quality, efficiency and performance.

Keywords: GISAXS; GIXRPD; XRR; in situ; synchrotron radiation; oxid thin films; BaTiO₃; crystallization; sputter deposition



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1. Introduction

The industrial market for thin films requires the production of more efficient layers with better performance, lower energy consumption, and preferably to lower production cost. With an increasing demand of functional thin films the control and influence of the preparation parameters has to be investigated in situ during the thin film production. A key role in a broad spectrum of applications such as electro-optical devices, solar cell technology or storage devices [1–4] plays the crystallization either for polycrystalline or epitaxial thin films [5,6]. State of the art thin film research has reached a point where only in situ measurements can help optimizing the thin film production, because this way, the influence of the different sputtering parameters can be followed in real time during the deposition process.

To follow the preparation of oxide thin films, we were using the characteristic features of the modern synchrotron radiation source PETRA III [7], a compact and low-weight

sputtering unit [8], and the investigation techniques in situ grazing incidence small angle X-ray scattering (GISAXS) and in situ grazing incidence X-ray powder diffraction (GIXRPD) simultaneously, as well as in situ X-ray reflectivity (XRR) measurements [9,10].

In this work, we follow the crystallization process in situ during the high temperature deposition above the crystallization energy. We deposit BaTiO₃ at 600 °C and followed the film evolution from early formation to polycrystalline thin film of around 40 nm.

2. Materials and Methods

In the present work, BaTiO₃ thin film evolution was studied at P03 at PETRA III [11], two 2D detectors were used simultaneously. One 2D detector (Pilatus 1M, 981 × 1043 pixels, pixel size of 172 μm × 172 μm) was used for GISAXS at a Sample-to-Detector Distance of SDD = 4 m. The X-ray beam had an energy of 13 keV and a beam size of 40 μm (horizontal) × 20 μm (vertical) FWHM, and the angle of incidence (α_i) was set to 0.5°. This angle is above the critical angle of the materials involved. A second single-photon counting pixel detector with 487 × 619 pixel of 172 μm each (Pilatus 300k, Dectris, Baden, Switzerland) was mounted on the detector arm of the diffractometer with SDD = 0.28 m covering the Q-range from 2 Å⁻¹–4.5 Å⁻¹. With this second 2D detector, we were following the evolution by GIXRPD simultaneously to the GISAXS measurement. Both detectors were in air. The measurements were performed with the following parameters. The plasma process and substrate heating was started 10 min. before opening the shutter in front of the sputtering target. The sputtering power on the BaTiO₃ target was 14 W/cm² and the gas mixture was 80% Argon (Ar) and 20% Oxygen (O₂) with a total flow of 1 standard cubic centimetre per minute (SCCM), and a substrate temperature of 600 °C. The distance between the sputtering target and substrate was fixed at a distance of 4 cm. The films were deposited on pre-cleaned SiO₂ wafers with a size of 10 × 10 mm². A more detailed description of the measurement can be found here [8,10]. SiO₂ wafers are not the industrial standard for BaTiO₃ thin film deposition, but we have chosen it to avoid surface related influence on the crystallization process. A more detailed study of the influence of various parameters, such as surface structure and deposition temperature, on the crystallization behavior will be published elsewhere. Figure 1 illustrates the principal scheme of the experiment. The X-rays arrived from the left hand side and hit the wafer inside the sputtering unit under grazing incidence and get detected with the 2D detector behind the chamber.

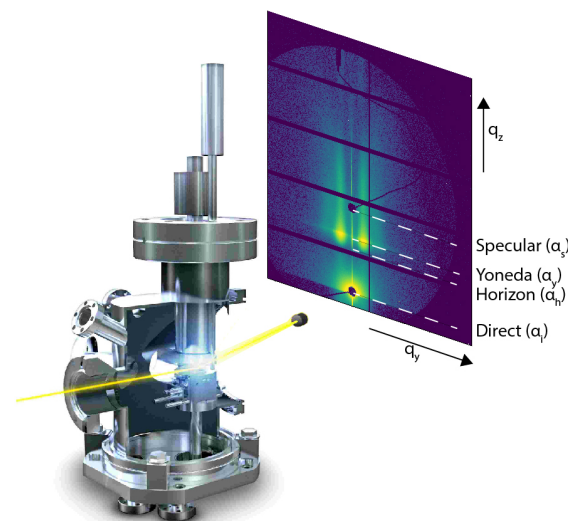


Figure 1. Schematic setup for in situ sputter deposition measurements, with the X-ray beam (yellow), the chamber (silver) including the sample holder in grazing incidence geometry and a 2D detector (blue). Shown is a GISAXS pattern after 40 s of deposition of BaTiO₃ at 600 °C. Denoted is the specular beam $\alpha_s = 2 \times \alpha_i$, the Yoneda peak $\alpha_y = \alpha_c + \alpha_i$ with the α_c the critical angle, sample horizon $\alpha_h = \alpha_i$ and the direct beam α_d . Not shown is the second GIXRPD Detector.

3. Results and Discussion

This in situ experiment recorded the film evolution continuously in reciprocal space, without interrupting the sputtering process. Exemplary patterns for the GISAXS detector can be seen in Figure 1. To analyze these patterns in more detail, horizontal cuts were taken at the level of the Yoneda peak [12]. The Yoneda peak occurs when the exit angle of the scattered beam is close to the critical angle due to signal enhancement from the Vineyard effect [13]. This results in a bright band of intensity at the critical angle (α_c). Below the critical angle the scattering intensity decreases quadratically to zero. With the refraction index $n = 1 - \delta + i\beta$ including the real part δ and the imaginary part $i\beta$, it depends strongly on the wavelength λ and the electron density. Therefore, it is a material dependent effect when the wavelength is constant.

These patterns (seen in Figures 1 and 2a) show a clear evolution perpendicular to the Yoneda peak over the deposition time. This relates to density correlations and arise from a the structure factor with characteristic modulations parallel to the surface. The peaks were fitted with a pseudo-Voigt function (see Figure 2) $pV(x) = \eta G(x) + (1 - \eta)L(x)$, with $G(x)$ the sum of a Gaussian peak and $L(x)$ the Lorentzian peak, as well as the mixing parameter η which describes the fraction of each function.

It shows that the particle distance initially appears at higher q_y and shifts towards smaller q over deposition time. This shift indicates a coalescence, i.e., mainly a fusion phenomenon of adjacent nuclei or clusters, which leads to an increase of the average center-to-center distance. From the fit, we can take the FWHM, amplitude and position. The latter depicts the center-to-center distance, as mentioned before. The amplitude indicates the amount of scattering sources. The peak width is related to the distribution and displays the disorder of cluster and particle arrangement. Therefore, the FWHM is also a strong indicator which indicates a transition from fast increasing ordering to a slower growth of a two-dimensional (2D) cluster arrangement. This means a conversion from a diffusion-mediated coalescence regime to an adsorption-driven cluster growth regime. This expansion persists until one cluster grows radially into another one by the movement of grain boundaries and not by coalescence anymore (shown in Figure 3a–c). This means the surface is covered and the newly arriving particles contribute only in the vertical growth. This describes the early formation (nucleation, diffusion, adsorption and grain growth) for thin films as known from literature [5,6,10]. The relation $D \approx 2\pi/q$ enables us to track the mean cluster distance during the growth as a quantitative parameter. The peak broadening in Figure 3a at around 120 s corresponds to the growing additional scattering source of crystalline BaTiO_3 particles until the crystalline particles with $\delta = 5.8 \text{ g/cm}^2$ have taken over the whole layer.

From the development of the Yoneda peak itself, we were able to get further information about the growth dynamics. Therefore, we have taken cuts in the q_y -direction at the position of the Yoneda peak (see Figure 3c). The temporal evolution of the intensity at the Yoneda peak corresponds to the surface coverage or particle density at the surface, which leads to a change in the scattering distribution. At the beginning of the deposition, a clear Yoneda peak of SiO_2 can be seen. At a deposition time of 20 s, the Yoneda peak of amorphous BaTiO_3 , with a $\delta = 2.9 \text{ g/cm}^2$, appears and after a deposition time of 60 s, another Yoneda peak appears. This is a relatively broad peak that shows up at $\delta = 5.8 \text{ g/cm}^2$ which correspond to polycrystalline BaTiO_3 . As mentioned above, the Yoneda peak depends on the material—on the electron density, to be precise, which changes when the crystallization launches. This is where it shows an alteration around 30 s after the start of the deposition. It starts with a broadening of the Yoneda wing in q_z , leads to a second line at the density of polycrystalline BaTiO_3 , and ends with a disappearing line at the density of the amorphous clusters. These density findings accord with the literature values for BaTiO_3 [14,15].

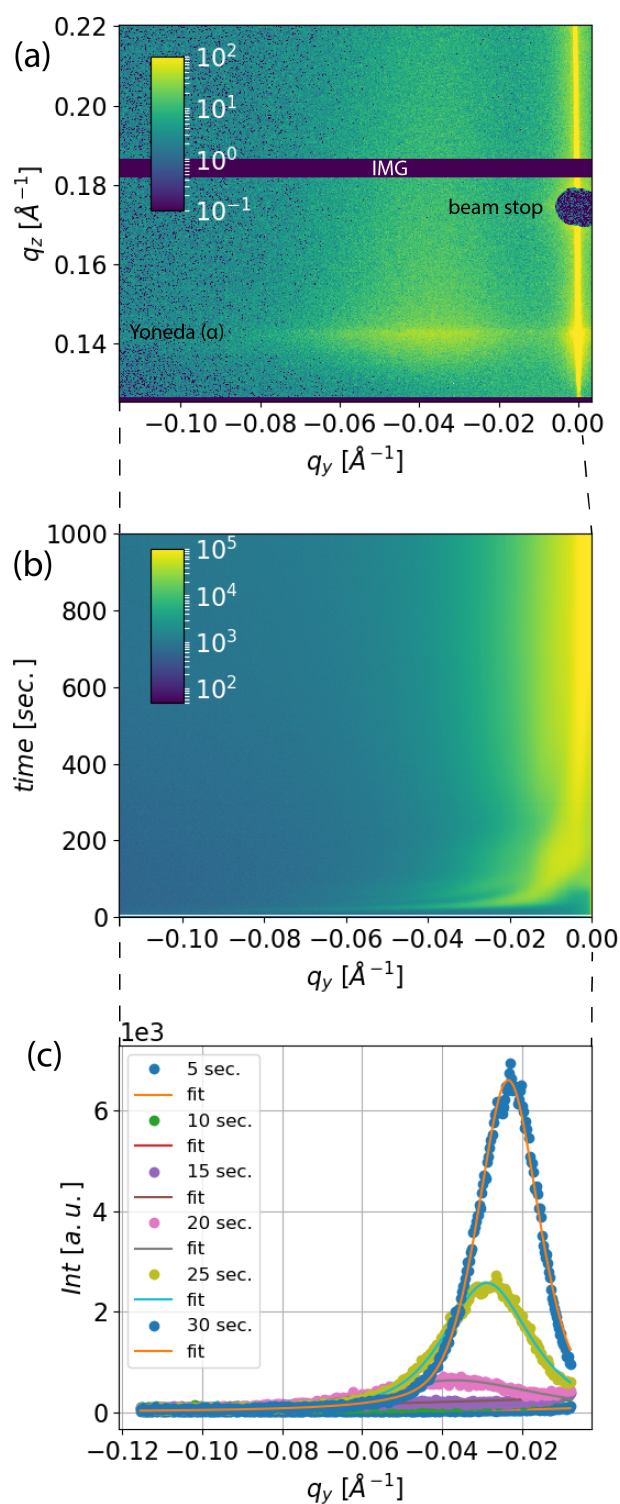


Figure 2. Exemplary region of the GISAXS detector of the two dimensional GISAXS patterns taken at the surface diffraction beam line P03 at PETRA III (a). The bottom line starts at the sample horizon and denoted are the beamstop, the Yoneda level, the inter-module detector gaps (IDG, black stripe). The intensity evolution of the horizontal cuts at the level of the Yoneda peak (b). And the Pseudo-Voigt fits of the Yoneda-cuts during the deposition at 600 °C (c). The data points displaying the background subtracted data and the lines the corresponding fit.

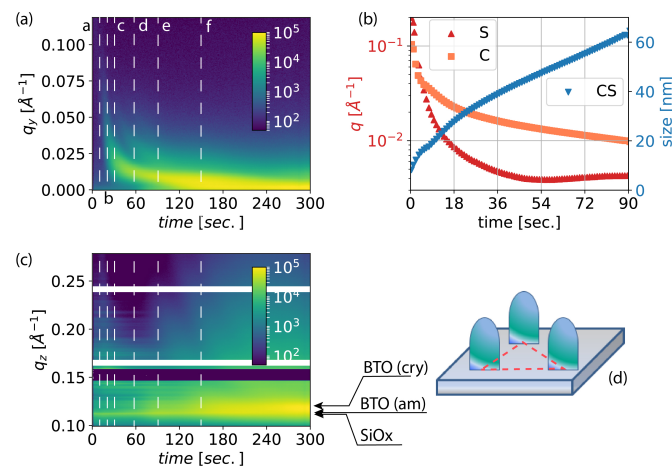


Figure 3. (a) is showing the intensity evolution of at the Yoneda level and (b) the results from the Pseudo-Voigt Fits, given the peak width sigma (S) and the center position (C) as well as the cluster size (CS) for the first 90 s. (c) shows the q_z -cuts at the $q = 0$ position. (d) shows the cluster grow model for the for the first 60 s. Showing 3 nm sized hemispherical shaped particles arranged in a 2D hexagonal lattice.

During this experiment, we collected the wide angle scattering (WAX) with a second detector simultaneously. An exemplary pattern taken after 500 s of deposition is shown in Figure 4, it shows a detector tilt and rotation corrected pattern which was azimuthal resorted using the Python package pyFAI [16]. The software was calibrated by performing a measuring with a NIST standard.

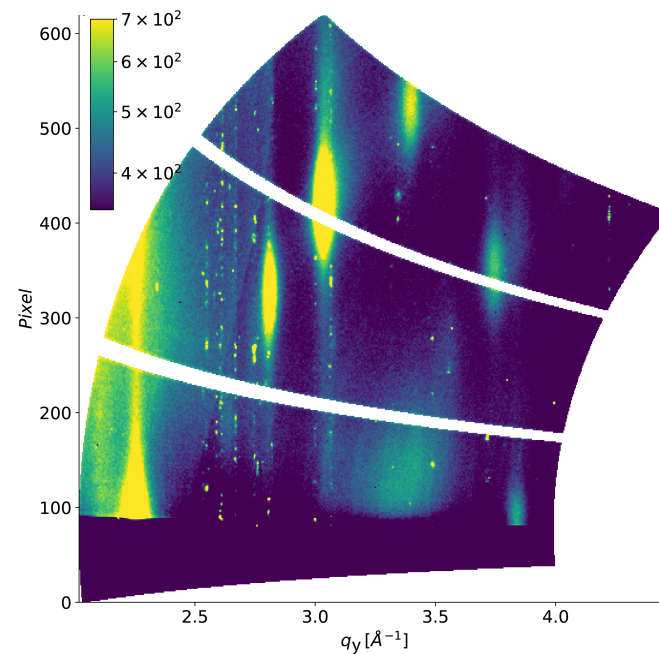


Figure 4. Exemplary two-dimensional GIXRPD false color plot showing a tilt, rotation and azimuthal resorted single patterns of GIXRPD of BaTiO₃ after 1000 s of deposition at 600 °C. White markers show diffraction lines for bulk cubic BaTiO₃ [17]. The offset is an effect of temperature and finite-size effects. The powder diffraction rings show a clear indication for preferred orientation and also double peak structures and peak broadening where the lattice parameter $a = b \neq c$, are indicating tetragonal BaTiO₃ structure. The high-intensity small peaks are background coming from the AlO₂ sample holder and the black part on the bottom is the sample surface. Also shown in the top right corner is the original shape of the 2D detector.

The peak positions for cubic BaTiO₃ are marked and show a good agreement. Small offsets at the higher angle peaks are shown and can be explained as finite-size effect and temperature introduced stress on the wafer and the thin film. The peak broadening of the [200]-peak and the double peak structure at the [211]-peak can be explained with the occurrence of tetragonal BaTiO₃. The preferred orientation arises from particles being oriented on the surface and enhancing the intensities of more defined Bragg reflections, while reducing the intensities of others. [18] The preferred orientation is diminishing with increasing film thickness as shown in Figure 5. This can be explained with the fast increasing film thickness, a layer-plus-island growth and the therefore decreasing influence of the surface and relaxation process due to misfit dislocations [5,6], but still can be seen until the end of deposition. Figure 6 shows the peak evolution by plotting the azimuthal resorted patterns versus time during the deposition at 600 °C and selected GIXRPD pattern after 100, 500 and 1000 s. Figure 7 shows exemplary pseudo-Voigt fits of the peaks. The increasing amplitude corresponds to the quantity of diffraction sources, i.e., crystallites, and the peak width correspond to the nano-crystalline size. The azimuthal integrated patterns versus time can be fitted with a pseudo-Voigt function to extract the peak width and amplitude. Figure 6 shows the results of five second binned fits over time for the [110] and [200] peak, these peak positions are in good agreement with literature [17,19]. The [200] peak occurs after about 200 s of deposition and the [110] peak after about 250 s. This is about 140 s after the appearance of the crystalline Yoneda peak. In the early crystallization stage, the amount of diffraction sources are too small to overcome the background and noise in the GIXRPD detector. With the simultaneous use of two detectors for GISAXS and GIXRPD we have followed the crystallization in detail through the whole evolution of the thin film growth. First, it appears after around 60 s in cuts along q_z at the Yoneda peak (see Figure 3c) as slowly growing peak at the density of crystalline BaTiO₃. After a growing amount of scattering sources through the film thickness it leads to a broadening of the peak along q_y direction (see Figures 2b and 3a) at around 100 s. And finally it appears as a scattering signal in the GIXRPD detector (see Figures 5 and 6) after around 200 s.

To confirm and refine these findings, we used the software BornAgain (BA) [20] to simulate and fit the evolution of the thin film. For the early formation, we get the best results for small sized hemispherical shaped particle ($\delta = 2.9 \text{ g/cm}^2$) with a small distribution on the height of 3 nm and the radius of 3 nm for the beginning and growing over time. In the early stage, there is only a cumulative disorder of inter-particle distances along the X-ray footprint. This corresponds to the early stage of nucleation, diffusion and adsorption (see Figure 7a–c). Over time, the mean particle diameter rises, forming small clusters growing in diameter and shrinking in distance. At this stage, the best model assumes uniform hemispherical clusters of radius R arranged in a 2D hexagonal lattice with the correlation distance D between the lattice points. Assuming that all BaTiO₃ deposited on this triangular area is separated into three individual uniform clusters (see Figure 3d), this leads to the equation:

$$R = \sqrt{\frac{2\pi}{f_A} \frac{t}{3^{\frac{1}{4}}}}$$

With R the micro-domain size, f_A the form factor ratio $\frac{A_{circle}}{A_{hexagon}}$, with $A_{circle} = 3\pi R^2$ and $A_{hexagon} = \frac{3\sqrt{3}}{2} t^2$, where t is the side length of the hexagon, with the local maximum for close packing at $t = 2r$. This maximum emphasizes the fully covered surface as mentioned before (see Figure 3a).

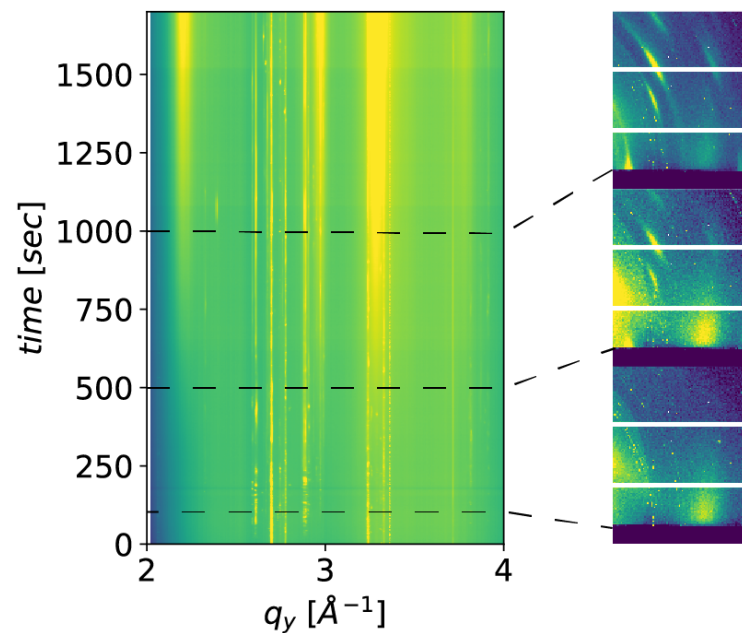


Figure 5. GIXRPD false color plot showing a tilt and rotation corrected and azimuthal resorted integration versus time in one-second steps on the left hand side. The selected Q-range from 2 \AA^{-1} – 4 \AA^{-1} . On the right hand side exemplary original GIXRPD pattern collected after 100, 500 and 1000 s. The high intensity small peaks are background coming from the AlO_2 sample holder. The early stage of deposition shows a more diffuse scattering at around 2 \AA^{-1} and 3.5 \AA^{-1} . This turns into a preferred orientation for the early crystallization which later evolves into a more evenly distributed poly-crystalline ring structure.

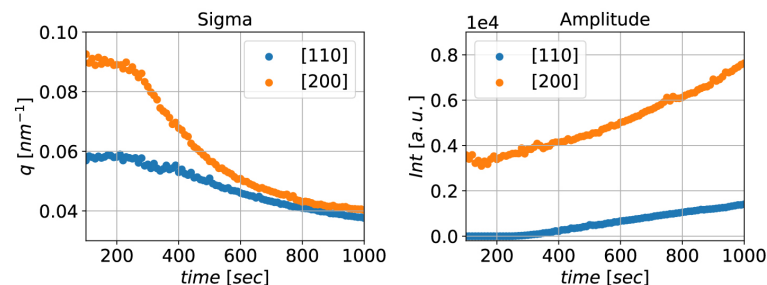
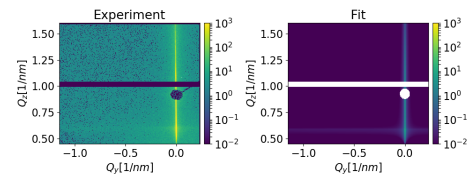


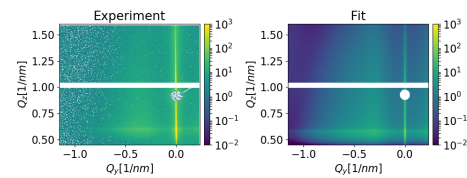
Figure 6. Exemplary fits of the [110] and [200] BaTiO_3 peaks versus time. Showing the evolution of the peak width and amplitude of the peaks during the deposition at $600 \text{ }^\circ\text{C}$. The GIXRPD patterns were binned for five seconds due to the background and noise. The [200] BaTiO_3 peak at 3.1 \AA^{-1} occurs after about 200 s and the [110] BaTiO_3 peak at 2.2 \AA^{-1} occurs after about 250 s of deposition. The [200] BaTiO_3 peak shows some peak broadening in the early stage indicating the existence of tetragonal BaTiO_3 and with time developing a homogeneous average poly-crystallization size showing by the width comparison to the [110] BaTiO_3 peak. The increasing amplitude corresponds to the quantity of diffraction sources, i.e., crystals. The different intensity in the beginning corresponds to the increasing background.

Since we were depositing on a substrate temperature higher than the known crystallization energy for BaTiO_3 [1,2], a re-crystallization was expected to happen, and was shown in the cuts along the q_y direction at about 60 s. Following our evolution modeling, we have assumed a covered surface of hemispherical clusters ($\delta = 2.9 \text{ g/cm}^2$) with embedded particles ($\delta = 5.8 \text{ g/cm}^2$). For these particles with the density of crystalline BaTiO_3 , the best fitting shape are cylinders with a radius of 2 nm and a height of 3 nm which grow over time (see Figure 7d). The fitting model with the highest agreement show these cylinders growing near the interface of the substrate to the thin film. After about

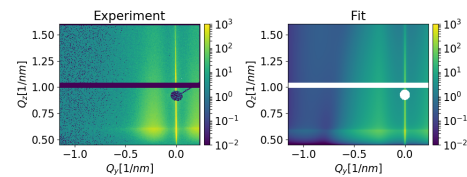
100 s of deposition, the best fitting model is a 10 nm thick amorphous thin film with a high surface roughness and growing hemispherical poly-crystalline clusters (see Figure 7f). After the crystallization of the whole thin film the arriving amorphous particle coming from the sputtering target will quickly crystallize. The high surface roughness stays until the end of the deposition which is also confirmed by the missing interference pattern in the q_z -cuts at the $q = 0$ position shown in Figure 3c, which is in strong agreement with the literature [10]. A schematic of the thin film evolution during the deposition is shown in Figure 8.



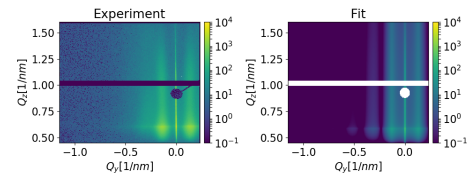
(a) after 10 seconds of deposition.



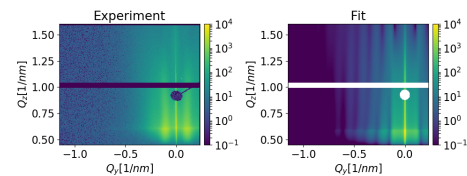
(b) after 20 seconds of deposition.



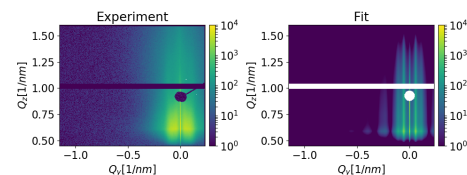
(c) after 30 seconds of deposition.



(d) after 60 seconds of deposition.



(e) after 90 seconds of deposition.



(f) after 150 seconds of deposition.

Figure 7. GISAXS patterns and fit of BaTiO₃ after the deposition time marked in Figure 3 (a = 10, b = 20, c = 30, d = 60, e = 90, f = 150 s). Showing the early formation (nucleation, diffusion, adsorption) in a, b, c to the start of the crystallization in d and e to the stage of the domination of the poly-crystalline BaTiO₃ in f as also marked in Figure 3.

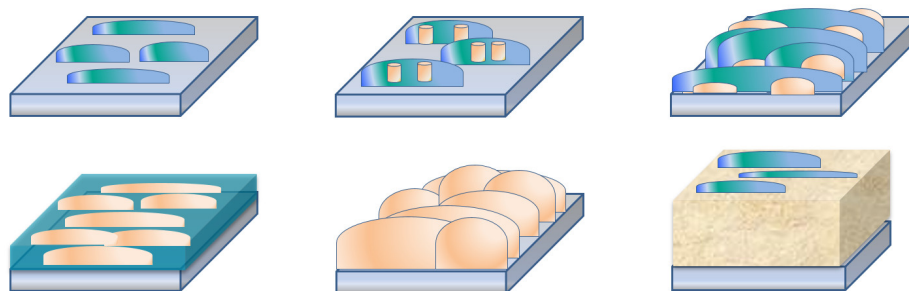


Figure 8. Schematic of the BaTiO₃ thin film evolution over time above the crystallization temperature. Showing, as described in detail in the text, the early formation (nucleation, diffusion, adsorption and grain growth) towards the crystallization inside the amorphous clusters, towards the growing ploy-crystalline cluster grow, up to the ploy-crystalline final thin film grow with on coming amorphous BaTiO₃.

4. Summary and Outlook

By means of various X-ray diffraction and scattering experiments, we have shown that the characterization of the film formation and film growth, and especially to follow the crystallization, is feasible in real time, thus adding the important dimension to the fundamental understanding of the evolution of the film micro structure. Furthermore, these techniques were used to study the crystallization dependence of the deposition process and the growth on SiO₂ substrate material. It is observed that the whole evolution from nucleation, diffusion adsorption and grain growth to the crystallization can be observed during all stages of thin film growth as well as quantitatively as qualitatively using the prototypical showcase of BaTiO₃. Investigations of various parameters of the deposition process and their influence on the crystallization such as surface structure and deposition temperature was also performed and will be published elsewhere. A logical next step would be a in situ study of the deposition and crystallization using the thin film pair distribution function analysis (tfPDF) [21].

Author Contributions: P.W. has conceived the experiment. The experiment was performed by P.W., M.I., J.R., W.O., C.B.Z. and U.K. The data was analyzed by P.W. The original draft was written by P.W. with dedicated contributions by M.I. and U.K. All authors have read and agreed to the published version of the manuscript.

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Data Availability Statement: Raw data were generated at PETRA III at DESY, Hamburg, large scale facility. Derived data supporting the findings of this study are available from the corresponding author upon reasonable request.

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Conflicts of Interest: The authors declare no conflict of interest. The funders had no role in the design of the study; in the collection, analyses, or interpretation of data; in the writing of the manuscript, or in the decision to publish the results.

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