



Article A Model Test of the Dynamic Stiffnesses and Bearing Capacities of Different Types of Bridge Foundations

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Abstract: With the rapid development of traffic infrastructures in developing countries, the evaluation demands for the vertical capacities of in-service bridges are increasing. The feasibilities of the transient response method (TRM) and index of dynamic stiffness for evaluating pile foundations are proven. However, their applicability to other types of bridge foundations must be investigated, and the correlation between the dynamic and static stiffnesses is also needed for analysis. In the present study, model tests were performed in a laboratory for various types of bridge foundations. A total of eight foundation models were fabricated for three types of bridge foundations. Both TRM and static loading tests were applied on each model. The influence of the foundation constraint state was tested as well. The results show that there is an obvious correlation between the dynamic and static stiffnesses can reflect the foundation bearing capacity. Accordingly, the TRM can be employed to evaluate different foundation types, including spread, caisson, and pile foundations.

Keywords: bridge foundation evaluation; transient response method (TRM); dynamic stiffness; model test

1. Introduction

With the rapid development of traffic infrastructures in developing countries over the last two decades, the demands for the bridge maintenance, disease diagnosis, and reinforcement are increasing [1,2]. Unlike the bridge superstructures, the pier foundations are buried in the ground, and the disease degree and its location cannot be identified by conventional detection methods. Hence, it is more difficult to quantitatively evaluate the bearing capacities of such foundations [3–6]. In real bridge foundations, it is always a combination of vertical, longitudinal, and lateral forces. The bridge dynamic problem under the action in the horizontal direction has been widely investigated, e.g., under seismic excitation and scour [7–10]. The effect on the lateral state can be directly inspected using diving underwater observation and direct observation during dry periods [11,12]. The dynamic method can also be used to evaluate the later condition of bridge substructures [13,14]. However, as the train loads mainly provide the quasi-static load and parameter excitations in the vertical direction [15-18], when the freight volume or train speed is required to be increased, the associated increase in the axle loads has the potential effect on the vertical bearing capacity of bridge substructures. Thus, the capacities of bridge substructures need to be estimated [19]. To obtain the actual foundation bearing capacity in the vertical direction, the most widely used method is the static loading test (SLT), which is also a typical static method to test the capacities of buildings and bridge foundation piles [20–22]. Wang et al. (2016) [23] discussed different prediction methods for the bearing capacities of piles. Zhang et al. (2016) [24] presented an analytical method to assess the influences of reaction piles on the test pile responses in SLT. Baca et al. (2020) [25] examined a new method of bi-directional



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). SLT in the laboratory using six model piles. In addition to the SLT, dynamic testing can also be employed to estimate the pile capacity. The high-strain dynamic pile testing (HSDPT) method is generally used to evaluate the capacity of a deep foundation [26,27]. However, both SLT and HSDPT are difficult to use on existing bridge foundations that are in service, as permanent displacements can be generated by these methods.

For bridges with potential diseases or for bearing increasing train loads and train speeds, it is considered significant that engineers learn the real foundation capacities to determine whether the foundations need to be strengthened. Then, the transient response method (TRM) and index of dynamic stiffness (K_d) are proven to be feasible. The TRM is also known as the mechanical mobility method. By applying a vertical impact load on the foundation, both the velocity responses and force signals can be analysed in the frequency domain. The mechanical admittance spectrum or mobility can be obtained using the velocity and force spectra [28]. Using the TRM, the dynamic stiffness can be obtained as follows [29–31]:

$$K_{\rm d}(f) = \frac{2\pi f}{|V(f)/F(f)|},$$
(1)

where V(f) is the Fourier spectrum of the velocity response v(t), F(f) is the Fourier spectrum of the force F(t), and the ratio of V(f)/F(f) is the mechanical admittance spectrum or velocity mobility [28]. Figure 1 shows the theoretical velocity mobility of a pile obtained using the TRM. In the low-frequency range, the ideal velocity mobility varies linearly with the frequency; accordingly, the value of K_d in the low-frequency range is a constant.



Figure 1. Theoretical mobility response spectrum tested using the TRM.

Recently, the TRM and K_d were employed for pile foundation evaluations. Liu and Ma [32] proved that in the pile capacity estimation, a reasonable value of K_d could be employed as an alert value. Ma et al. [33] indicated that K_d could be employed to estimate the pile bearing capacity. Chu et al. [34] investigated the influence of the cap-pile system on K_d . Liu and Ma [35] performed both TRM and SLT on a full-scale pier–cap–pile system and analysed the relationship between the dynamic stiffness and foundation capacity. However, the above studies only analysed the applicability of the TRM to pile foundations; other types of bridge foundations, such as the widely used spread foundation and caisson foundation, were not considered. In addition, most studies have only considered the TRM; a few tests were reported on the use of both TRM and SLT on the same foundation because of low feasibility of the SLT to evaluate in-service pier foundations and the associated high testing cost. If the TRM and K_d are used to evaluate the capacities of different types of bridge foundations, then the relationships between the dynamic stiffnesses and bearing capacities could be further investigated. Therefore, in this study, a model test was performed in the laboratory, where both the TRM and SLT were used to assess three types of bridge foundations: spread, caisson, and grouped pile foundations. The dynamic stiffnesses were analysed when the foundations were first fully buried in the soils and then when the constraint states were changed. Subsequently, the static stiffnesses were calculated using the SLT results. Finally, the relationship between the dynamic and static stiffnesses was analysed.

2. Test Outline

2.1. Foundation Models and Test Method

The model test considered three types of widely used bridge foundations: spread, caisson, and grouped pile foundations. In total, eight test models were prepared by considering different foundation sizes, namely large and small spread foundations (S1 and S2), large and small caisson foundations (C1 and C2), and four grouped pile foundations with different pile lengths and pile numbers (P1–P4), as illustrated in Figures 2 and 3.



Figure 2. Dimensions of the eight fabricated test models (unit: cm). (a) Model S1; (b) model S2; (c) model C1; (d) model C2; (e) model P1; (f) model P2; (g) model P3; (h) model P4.



(a)





(c)

Figure 3. Pictures of the various model foundations: (**a**) grouped pile foundation models; (**b**) spread foundation models; (**c**) caisson foundation model and its sensor locations.

All the models were cast in situ using self-mixed concrete. Each model foundation to be tested was placed within the sand tank individually.

The tests using the TRM were performed using a 2 kg steel bar that impacted the top of the foundation (Figure 4a), and both force signals and velocity responses were recorded. Four velocity sensors were installed along the four edges at the foundation top (Figure 3c), and the average velocities obtained from the four sensors were used to calculate the dynamic stiffness.



Figure 4. Test equipment: (a) impact steel bar; (b) equipment and sensors for the SLT.

The SLTs were performed using the laboratory reaction frame and a 10 t manual jack. The tests followed the slow maintenance loading method [36]. The values of vertical loading and vertical displacement were recorded using pressure and displacement sensors (Figure 4b). Based on the load–settlement curve (P–s curve) of the test, the static stiffness and bearing capacity were obtained.

The dimensions of the sand tank were 2.3 m \times 1.7 m \times 1.5 m (Figure 5). The main soil parameters were tested in detail. The mass density was measured by the cutting ring method. The measured moisture rate is 1.54%, the mass of the cutting ring is 38 g, the total mass of the cutting ring and wet soil is 131.08 g. As the volume of the cutting ring is 60 cm², the natural density and dry density are 1.551 and 1.548 g/cm³, respectively. The void ratio is 0.724.



Figure 5. Cross-sectional views of the sand tank configurations in the laboratory: (**a**) spread foundation; (**b**) caisson foundation; (**c**) grouped pile foundation.

Figure 6 illustrates the grain size diagram. The test sample can be determined as the medium sand. By the direct shear method, the cohesion and the angle of internal friction can be determined as: c = 2.4714 kPa and $\varphi = 12.20^{\circ}$. The sand tank was filled with the sand and the filling sand was levelled every 40 cm height. According to different models, the model was preloaded with 1 ton weight pressure in advance. After the settlement remains stable for 24 h, other tests can be carried out.



Figure 6. Grain size diagram.

3. TRM Test

3.1. Foundation Fully Buried in the Soil

The dynamic stiffness can be calculated as a function of the frequency using Equation (1). The TRM tests were repeated five times for each foundation model, and the average values of

 $K_d(f)$ are illustrated in Figure 7. Owing to the limited impact mass, the $K_d(f)$ values below 10 Hz were small, values between 10 and 50 Hz increased slowly with the frequency, and values increased sharply for frequencies above 50 Hz for most model foundations. Table 1 lists the K_d values of all foundation models for frequencies in the range of 10–50 Hz.



Figure 7. Dynamic stiffnesses of the eight foundation models: (**a**) spread foundations; (**b**) caisson foundations; and (**c**) grouped pile foundations.

Model _	Dynamic Stiffness/(×10 ⁷ N/m)				
	10 Hz	20 Hz	30 Hz	40 Hz	50 Hz
Model S1	2.70	3.58	4.20	5.01	6.29
Model S2	1.73	2.26	2.60	3.03	3.67
Model C1	3.37	4.30	4.97	5.82	7.09
Model C2	2.25	2.79	3.20	3.73	4.53
Model P1	9.62	12.10	13.05	13.65	14.60
Model P2	7.88	9.28	9.88	10.42	11.06
Model P3	3.16	3.90	4.40	5.04	5.96
Model P4	2.38	2.87	3.09	3.27	3.50

Table 1. *K*_d values of all foundation models for frequencies in the range of 10–50 Hz.

For the spread foundation, the K_d of model S1 can be calculated as approximately 1.56–1.71 times that of S2 between 10 and 50 Hz. The ratio of the bottom area of model S1 to that of S2 is 1.78, whereas the ratio of the side areas of these two models is 1.33. For the caisson foundation, the K_d of model C1 can be calculated as approximately 1.5–1.6 times that of C2 between 10 and 50 Hz. The ratio of the bottom area of model C1 to that of C2 is 1.94, whereas the ratio of the side areas of these two models is 1.33. That is, the ratio of the K_d values of the two models is between the values of the ratios of the side areas of the

and bottom areas, which is in good agreement with the actual constraint state and bearing capacity. Figure 8 illustrates the variations in the dynamic stiffnesses of the spread and caisson foundations with the side and bottom areas. The values of K_d increase with both the side and bottom areas, thus indicating that the dynamic stiffness value can reflect the bearing capacity condition.



Figure 8. Dynamic stiffness value variations in the spread and caisson foundations with side and bottom areas.

For the grouped pile foundation, as all the piles were friction piles, their bearing capacities were mainly attributed to the friction areas. Figure 9 illustrates the relationship between the dynamic stiffnesses and total side areas of all the piles. The trends of the curves are similar between 10 and 50 Hz. The dynamic stiffness thus increases with the total side area of the pile and exhibits an exponential growth rather than a linear growth.



Figure 9. Relationships between the dynamic stiffnesses and total side areas of the ground piles.

3.2. Change Foundation Constraint State

The constraint state of the foundation, including the supporting stiffness on the foundation bottom and side friction, is one of the significant factors affecting its bearing capacity. The ability of the dynamic stiffness to reflect the changes in the restraint state is directly related to whether the dynamic stiffness can effectively help evaluate the foundation state. Therefore, in the scale model tests, the following two aspects are mainly analysed: first, the K_d values of foundations that are fully buried in the soil and directly located on the ground are compared; second, the K_d values of foundations with different buried depths are analysed.

Figure 10 illustrates the three types of foundations directly located on the ground and fully buried in the soil. The impact on the foundation surface as well as both force and velocity responses are recorded. Then, the dynamic stiffnesses are obtained using Equation (1). Figure 11 shows a comparison of the $K_d(f)$ values of different foundation models located on the ground and fully buried in the soil. Below 100 Hz, the values of $K_d(f)$ increase logarithmically with frequency f when the foundation models are located on the ground, whereas these increments are exponential with frequency f when the foundation models are fully buried in the soil. As the ground can provide an extremely strong and stiff support to a foundation, in the low-frequency range (<50 Hz), the values of $K_d(f)$ are obviously larger when the foundation models are located on the ground. Therefore, the $K_d(f)$ in the low-frequency range can reflect the vertical support stiffness to some extent.



Figure 10. Foundation models located on the ground and fully buried in the soil: (**a**) spread foundation; (**b**) caisson foundation; (**c**) grouped pile foundation.



Figure 11. Cont.





The above tests are extreme cases when the foundation models are located on the ground. However, it is almost impossible in practical engineering applications to obtain such large values of the vertical support stiffness. Therefore, in the following tests, the soil constraint state of the foundation model is changed, and the law of the dynamic stiffness change is analysed when the contact area between the soil and foundation model decreases. The tests were performed only on models S1, P1, and P3 as typical foundations of each type.

For the spread foundation model S1, changes to the soil constraint states are analysed in three steps, as illustrated in Figure 12. In these three steps, the foundation model was always in the loaded state. Figure 13 shows the $K_d(f)$ value changes with the soil constraint states. With the release of the soil constraint around the foundation, the soil–structure contact area decreases, and the $K_d(f)$ value decreases accordingly.



Figure 12. Cont.



Figure 12. Changes to the soil constraint state on model S1: (**a**) soil constraint released on one side; (**b**) soil constraint released on two sides; and (**c**) soil constraints released on two sides and a corner.



Figure 13. Dynamic stiffness changes with soil constraint states for model S1.

As illustrated in Figure 14, changes in the pile buried depths h = 1.35 m, 1.15 m, 0.95 m, 0.7 m, and 0.05 m for the grouped pile foundation model P1 (H = 1.4 m), and h = 0.7 m, 0.4 m, and 0.1 m for model P3 (H = 1.0 m) were computed.



Figure 14. Changes to the pile buried depths in models P1 and P3.

Figures 15 and 16 illustrate the dynamic stiffness changes with the pile buried depths for models P1 and P3. With the decrease in the pile buried depths, the K_d values decrease. The K_d values exhibit a linear relationship with h, and the correlation coefficients of linear fitting for the 10 Hz frequency are 0.989 and 0.953 for P1 and P3, respectively.



Figure 15. Dynamic stiffness changes for various pile buried depths for model P1: (**a**) $K_d(f)$ function; and (**b**) K_d values at 10, 20, 30, 40, and 50 Hz.



Figure 16. Dynamic stiffness changes for various pile buried depths for model P3: (**a**) $K_d(f)$ function; and (**b**) K_d values at 10, 20, 30, 40, and 50 Hz.

4. SLT Results

The test results in Section 3.2 show that there is an obvious relationship between the dynamic stiffness and foundation constraint state. To quantitatively analyse the relationship between the foundation capacity and dynamic stiffness, SLTs were performed. Figure 17 illustrates the load–settlement curves (P–s curve) for the three types of foundations. For each foundation type, the absolute value of the slope is smaller for foundation models with larger sizes and relatively greater design capacities. That is, under the same vertical load, the foundation models with larger sizes have stronger resistances to vertical settlement or higher static stiffnesses. In addition, the loading values corresponding to the inflection points in the P–s curves of the spread and caisson foundations are higher than those of the grouped pile foundations. This indicates that the spread and caisson foundations have larger allowable bearing capacities, which is consistent with the design size of the model foundation and the actual situation.



Figure 17. SLT *P–s* curves of the (a) spread; (b) caisson; and (c) grouped pile foundations.

During the SLT, the *P*–*s* curve exhibits a linear relationship at the initial loading stage. Figure 18 illustrates the initial loading stages and corresponding linear fitting results of the three types of foundations. The correlation coefficients are greater than 0.99 for the spread and caisson foundations and exceed 0.97 for the grouped pile foundations. Then, the fitting results were used to calculate the static stiffnesses.



Figure 18. Cont.



Figure 18. Linear fittings of the static loading test *P*–*s* curves during the initial loading stage: (a) spread foundation; (b) caisson foundation; and (c) grouped pile foundation.

Figure 19 illustrates the relationship between the dynamic and static stiffnesses of the three types of foundations. For the spread foundations, the static stiffness ratio of models S1 to S2 is 1.51, whereas the average dynamic stiffness ratio of models S1 to S2 is 1.64. For the caisson foundations, the static stiffness ratio of models C1 to C2 is 1.73, whereas the average dynamic stiffness ratio of models C1 to C2 is 1.55. The two groups of ratios are close to each other. For the grouped pile foundations, the average dynamic stiffnesses exhibit a logarithmic growth trend with increase in the static stiffnesses. Generally, the bearing capacities of foundations can be controlled by deformation or strength under different loading conditions. When the capacity is controlled by the vertical deformation, the capacity can be described by the static stiffness value. That is, the dynamic stiffness is a sensitive index that can be used to evaluate the foundation capacity.



Figure 19. Cont.



Figure 19. Relationship between the dynamic and static stiffnesses: (**a**) spread foundation; (**b**) caisson foundation; and (**c**) grouped pile foundation.

5. Conclusions

To evaluate the vertical capacity of bridge substructures using TRM and analyse the correlation between the dynamic and static stiffnesses by experimental method, in the present study a novel model test was performed in the laboratory, where both the TRM and SLT were used to assess three types of bridge foundations: spread, caisson, and grouped pile foundations. The dynamic stiffnesses were analysed when the foundations were first fully buried in the soils and then when the constraint states were changed. Subsequently, the static stiffnesses were calculated using the SLT results. Finally, the relationship between the dynamic and static stiffnesses was analysed. The conclusions can be drawn from the experimental results:

- 1. The index of dynamic stiffness can adequately reflect the foundation bearing capacity. Further, it can recognise changes in the foundation constraint state, such as vertical supporting stiffness on the foundation bottom, side, or bottom contact area, pile length, and pile buried.
- 2. There is an obvious correlation between the dynamic and static stiffnesses.
- 3. The TRM can be employed to evaluate different foundation types, including spread, caisson, and grouped pile foundations.

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