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Abstract: In the monocular visual-inertia mode of ORB-SLAM3, the insufficient excitation obtained by the inertial measurement unit (IMU) will lead to a long system initialization time. Hence, the trajectory can be easily lost and the map creation will not be completed. To solve this problem, a fast map restoration method is proposed in this paper, which adresses the problem of insufficient excitation of IMU. Firstly, the frames before system initialization are quickly tracked using bag-of-words and maximum likelyhood perspective-n-point (MLPNP). Then, the grayscale histogram is used to accelerate the loop closure detection to reduce the time consumption caused by the map restoration. After experimental verification on public datasets, the proposed algorithm can establish a complete map and ensure real-time performance. Compared with the traditional ORB-SLAM3, the accuracy improved by about 47.51% and time efficiency improved by about 55.96%.

Keywords: visual-inertial SLAM; ORB-SLAM3; initialization; tracking; bag-of-words; MLPNP; loop closure detection; grayscale histogram



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1. Introduction

In the past decade, simultaneous localization and mapping (SLAM) has developed significantly, and the focus of research has gradually shifted from laser SLAM to visual SLAM and visual-inertial SLAM. Through rich visual information, the robot can accurately calculate its own pose in an unknown environment, and construct the map of the environment. Combined with the angular velocity and acceleration information of inertial measurement unit (IMU), we can not only estimate an absolute scale, but also make the SLAM system based on vision more robust.

According to the different ways of back-end optimization, the research on visualinertial SLAM (VINS) can be divided into filtering-based and optimization-based methods. The MSCKF (multi-state constraint kalman filter) proposed by [1] is a visual-inertial odometry (VIO) based on the extended Kalman filter (EKF), but it is not strictly a complete SLAM system because of its lack of loop closure detection and map reuse. OPENVINS proposed by Geneva et al. [2] is a VINS algorithm based on MSCKF, which combines ARUCO (Augmented Reality University of Cordoba) two-dimensional code features and conventional sparse features, and an open source library is provided.

However, since the filtering-based SLAM method has a Markov property, which means it is impossible to establish the relationship between a certain moment and all previous states, the current mainstream SLAM research is mostly based on the framework of nonlinear optimization methods. The LSD-SLAM proposed by Engel et al. [3] is a SLAM system based on the direct method, which can work in a large-scale environment. The SVO [4] is a semi-direct visual odometry, which combines the feature point method with the direct method, and finally calculates the pose based on optimization. With the introduction and application of ORB-SLAM2 [5], the indirect method using an oriented brief (ORB) feature [6] has also achieved good results. ORB-SLAM2 is compatible with monocular, stereo and RGB-D cameras and has real-time performance when working on CPU. In most cases, it is an accurate SLAM system. On the basis of [5], Li et al. [7] proposed

R-ORBSLAM by combining photometric information with ORB features; Yu et al. [8] adds semantic segmentation network SegNet [9] and moving consistency check to improve dynamic performance, and generates dense semantic octo-tree map [10]; Bescos et al. [11] and Zhong et al. [12] also studied to improve the performance of ORB-SLAM2 in a dynamic environment. The former added the function of dynamic target detection and background embedding, while the latter combined with central processing unit (SSD) [13].

With the continuous expansion of the application field of SLAM, the requirements for the robustness and stability of the SLAM system are also increasing. Therefore, the fusion of multi-sensors in the SLAM system has become an inevitable trend, and the joint processing of visual information and IMU data is the most feasible method at present. Leutenegger et al. [14] proposed a tightly coupled stereo VIO algorithm OKVIS (open keyframe-based visual-inertial SLAM). Based on the concept of keyframes, they use sliding windows for batch nonlinear optimization and compute Harris corners as well as BRISK descriptors. However, the algorithm can only output poses with six degrees of freedom. Since there are no loop closing threads, it is not a complete SLAM system. VINS-Mono (visualinertial system) proposed by the Flight Robot Laboratory [15] of Hong Kong University of Science and Technology is a tightly coupled monocular visual-inertial SLAM system, which has a more perfect system framework, including five parts: observation preprocessing, initialization, joint optimization of local visual-inertia, global graph optimization and loop closure detection. VINS-MONO uses the Lucas-Kanade (LK) optical flow method to track inter-frame feature points, and accelerates the tracking process. Not long ago, Rosinol et al. [16] also proposed Kimera, and used technologies such as PGO and loop closure detection, 3D grid reconstruction and semantic labeling. Although it is not stable at present, it shows great potential.

Campos et al. [17] proposed ORB-SLAM3, which is one of the most accurate and robust algorithms at present. ORB-SLAM3 is the first open source algorithm that can support pure visual, visual-inertia and multi-map reuse. It not only supports the pinhole camera model, but also supports the fisheye camera model and custom camera model. It only needs to take the projection, back projection and Jacobian equation as input. ORB-SLAM3 establishes three kinds of data association: short-term, medium-term and long-term data association, which enables the algorithm to adapt to various environments and greatly improves the positioning accuracy through different optimization methods. In the visualinertia mode, ORB-SLAM3 first describes the visual-inertia initialization problem as an optimal estimation problem [18], which enables the inertial measurement unit to initialize in a short time, so that the pose of the lost frame can be calculated temporarily by IMU pre-integration when short-term image tracking is lost. Even in the case of long-term data loss, the current active map is saved by the Atlas multi-map system [19], and then a new map is re-established, initialized and tracked on this new map. Based on ORB-SLAM3, fast corner points are extracted by the adaptive dynamic threshold, and a random sampling consensus (RANSAC) method is used to identify candidate ORB features [20]. Li et al. [21], Hu et al. [22] and Liu et al. [23] improve the performance of dynamic scenes by combining semantic information.

Most of the above improvements on the SLAM system require high computational cost to improve the performance of some specific scenes. Excessive computational time cannot meet the real-time requirements of robots in practical applications. At the same time, in the framework of the monocular camera, if the system cannot be well initialized and create an accurate map, it is very detrimental to the expansion of the SLAM system and the tracking of robots in offline state. For the initialization problem of the monocular SLAM system, Martinez et al. [17] calculated the homography matrix and fundamental matrix synchronously, then, selecting the model according to the scores of them will increase the success rate of initialization and achieve the automatic initialization process. In the work of Zhang et al. [24], a fast monocular initialization process. In order to improve the quality and success rate of initialization, Cheng et al. [25] proposed an improved iterative strategy

based on trust region. Yang et al. [26] added the generalized motion feature assumption in the initialization process, and transformed the solution of the rotation and translation matrix of camera motion into the error elimination problem in the initialization process.

However, current monocular initialization methods cannot improve both the accuracy and real-time performance. These methods are all based on SFM, and the initialization process requires the participation of many frames, which is the limitation of the SLAM. In particular, in the initialization of ORB-SLAM3 monocular visual inertial mode, with insufficient IMU excitation will make the initialization process of the system even slower. Due to this limitation, the SLAM system cannot generate a complete map. Therefore, this paper proposes a real-time map restoration method, which avoids the limitation of monocular initialization and generates a complete map with higher accuracy. The improvement of this algorithm is as follows:

- After the scale optimization of ORB-SLAM3, in order to obtain a complete map, all frames before successful initialization are quickly tracked back. In this process, the bag-of-words is used to match the feature points, and the MLPNP [27] is used to estimate the pose.
- In order to offset the extra time consumption caused by reverse tracking, the loop closure detection of each frame is accelerated. The process uses the mean, standard deviation and correlation of grayscale histogram to pre-process and pre-screen the loop candidate frames. It can improve the quality of the loop candidate frames and further reduce the number of invalid calculations in the loop closure verification.

The remainder of this paper is organized as follows. Section 2 discusses in detail the overall framework of the system, the details of reverse tracking and the method of using the grayscale histogram acceleration. The effectiveness of the proposed algorithm is verified on the Euroc dataset, and the comparison of the time efficiency and accuracy with ORB-SLAM3 algorithm is included in Section 3, followed by the conclusion in Section 4.

2. Materials and Methods

Our system pipeline is an extension of ORB-SLAM3. The proposed algorithm improves the tracking thread, local mapping thread, and loop closing thread. We added the map restoration function and introduced the grayscale histogram as a tool to speed up loop closure detection.

2.1. Overview of Real-Time Map Restoration Algorithms

This paper proposes a real-time map restoration algorithm based on ORB-SLAM3. The framework of the system proposed in this paper is shown in Figure 1. In the monocular inertial mode, each image frame will extract ORB feature points and calculate descriptors in the tracking thread. We insert frames that have extracted feature points into a custom stack for reuse. This stack stores all image frames up to the successful initialization of the current active map. In the local mapping thread, when the IMU initialization is successful and the second bundle adjustment (BA) optimization [28] is completed, the frame in the stack is quickly tracked, that is, from the first keyframe of the map to the earlier frame quickly matching and tracking one by one. Moreover, the process is parallel to the tracking thread. The detailed process is demonstrated in Section 2.2. In addition, when the keyframe is inserted from the local mapping thread into the loop closing thread, the grayscale image of the keyframe is adaptively clipped and the grayscale histogram is calculated. After normalization of the grayscale histogram, the standard deviation and mean value are calculated (details refer to Section 2.3). This facilitates the dynamic elimination of common-view frames, detection of candidate frames in loop closing threads, and similarity comparison of grayscale histograms.



Figure 1. System overview. Our system pipeline is an extension of ORB-SLAM3 [17]. Compared with ORB-SLAM3, the main improvements of our system have been marked with "*" in the flowchart. The red part indicates new additions, and the green indicates improvements.

2.2. Map Restoration Based on Reverse Tracking

In the reverse tracking, we first take out a frame F_i in the stack and precise positioning tracking. We quickly match F_i with the first keyframe KF_0 in the current active map using a bag-of-words. In the matching process, only the feature points belonging to the same node are matched, and the number of successful matching points n is obtained. If the number meets the requirements, MLPNP is used to estimate the pose of F_i . MLPNP not only decouples the relationship with the camera model, but also has the advantages of fast speed and high accuracy. Then, the chi-square test is used to eliminate the outliers, and the reprojection error is calculated according to Equation (1),

$$= u - \bar{u}, \tag{1}$$

where *u* is the pose of the feature point of F_i on the pixel plane, \bar{u} is the pose of the map point of KF_0 projected to the F_i pixel plane. Affected by many independent factors, the reprojection error is random. According to the central limit theorem, the reprojection error obeys the Gaussian distribution,

е

$$e \sim N(0, C), \tag{2}$$

where *C* is the covariance,

$$C = (s^{n} \times p)^{2} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix},$$
(3)

where *s* is the scaling factor of the image pyramid, *p* is the standard deviation of the 0th layer. The error term in Equation (1) is weighted by covariance to obtain an error scalar r,

$$r = e^T C^{-1} e, (4)$$

which, according to the monocular projection, is 2 degrees of freedom, and the threshold of chi-square statistics is 5.99 at 0.05 significant level. We believe that the point greater than this threshold is the outlier, and the point less than this threshold is the interior point.

When the number of interior points *m* is sufficient, we update the pose T_{cw} in the world coordinate system of the current frame,

$$T_{cw} = \begin{bmatrix} R_{cw} & t_{cw} \\ 0^T & 1 \end{bmatrix},\tag{5}$$

where R_{cw} and t_{cw} are the rotation and translation matrices from the world coordinate system to the current camera coordinate system, respectively. If the number of interior point *m* obtained in the previous step is small, as shown in Figure 2, the unmatched map points between frame KF_0 and F_i are re-projected to the camera coordinate system of F_i , and the new point pairs are obtained by using a more stringent threshold and smaller window matching. Finally, the pose optimization is carried out again.



Figure 2. Reprojection of mappoints. The red points is the mappoints that has been matched between the two frames, and the black points is the unmatched mappoints. This process is used to generate new matching relations.

After tracking F_i and getting the pose, the fast reference frame tracking begins. After inserting F_i into the keyframe queue, the mappoints are inserted into the point cloud map, and we update this frame as a reference keyframe for the image frame in the stack. The next frame F_{i-1} of pop stack is quickly matched with its reference keyframe through the bagof-words, and then the mappoints of the reference keyframe are projected to F_{i-1} and the pose estimation is carried out according to MLPNP, so as to obtain the pose transformation of the frame in the world coordinate system. The pose transformation T_{cr} of this frame relative to the reference frame is calculated according to Equation (6) and saved to the map file for the generation of map trajectory.

$$T_{cr} = T_{cw} \times T_{wr}$$

$$T_{wr} = T_{rw}^{-1}$$

$$T_{rw} = \begin{bmatrix} R_{rw} & t_{rw} \\ 0^T & 1 \end{bmatrix}$$
(6)

If the number of successful matching points of F_{i-1} is small, the steps similar to the completed precise positioning tracking between F_i and KF_0 are performed. However, in addition to its reference keyframe, the keyframe quickly matched with F_{i-1} also contains a keyframe with high similarity found in the keyframe database. If the calculation condition of pose still does not meet the requirements, the pose of F_{i-1} is directly set as the pose of the previous image frame according to the principle that the pose between two adjacent image frames does not change dramatically. Follow this until the last image frame F_0 in the stack is tracked. After tracking, a complete map trajectory can be obtained, which contains more frame poses, and more mappoints in point cloud map. The generation

of the trajectory does not care about the effect of initialization. Due to the use of all the information of the input sequence, there can also be a good pose within the range of the original unsuccessful initialization, so that the accuracy of the algorithm to estimate the trajectory will also be improved.

The tracking process simplifies the process of using a bag-of-words to search for matching, and adjusts the number of iterations in optimizing pose, which can make this process become extremely lightweight and ensure accuracy. Considering that the pose transformation between image frames is not regular in the initialization process, a constant speed is not used to estimate the pose of the next frame in this tracking process.

2.3. Loop Closure Detection Acceleration Based on Grayscale Histogram

The grayscale histogram of image frame has a small computational cost, but it can well reflect the pixel distribution characteristics of an image. In addition, the grayscale histogram has the advantages of translation, rotation and scaling invariance, which is very suitable for frame measurement in the SLAM system. In this paper, we use the grayscale histogram to accelerate the loop closure detection of each frame, so that the real-time performance of the map restoration algorithm is improved.

In the ORB-SLAM3 system, the local mapping thread will continuously insert keyframes into the keyframe queue of the loop closing thread, and then find out the similar keyframes in the database for the similarity judgment. If the similarity is high, this keyframe will be used as a candidate keyframe. When inserting a keyframe into the keyframe queue of the loop closing detection thread, we calculate the grayscale histogram of the keyframe. In the working process of the SLAM system, there is almost no case that the two frames are exactly the same. Therefore, the grayscale image I_{gray} of the keyframe is adaptively clipped so that the grayscale histogram of the image can retain the main information of the image, and at the same time, the uncertainty caused by the perspective difference is reduced,

$$I'_{gray} = Rect(I_{gray}, \theta_1, \lambda_1, \theta_2, \lambda_2),$$
(7)

where *Rect* denotes that the grayscale image I_{gray} is cut from coordinates (θ_1, λ_1) to coordinates (θ_2, λ_2) ; θ represents the abscissa of the image coordinate system, λ represents the ordinate. Then, the grayscale histogram of the cut I'_{gray} is calculated to obtain *Hist*. A total of 256 grayscale levels are taken from 0 to 255, and the number of pixels corresponding to each grayscale level is calculated, which can represent the frequency of the grayscale level,

$$H(P) = [h(x_0), h(x_1), \dots, h(x_{255})]$$

$$h(x_i) = \frac{S(x_i)}{\sum_i S(x_i)} , \qquad (8)$$

where $S(x_i)$ is the number of pixels in a grayscale level, $\sum_j S(x_j)$ is the total number of pixels. After calculating the grayscale histogram, in order to maintain the relative relationship between the two sets of data and make the data more comparable, the range of *Hist* is normalized by Equation (9),

$$x_{out} = \frac{\beta - \alpha}{\delta - \gamma} (x_{in} - \gamma) + \alpha, \tag{9}$$

where x_{in} and x_{out} are the original values and the normalized values of each grayscale level, respectively. The range of values is mapped from (γ, δ) to (α, β) . For example, Figure 3 shows the process of normalizing histogram (b) of the grayscale image (a) to obtain (c).



Figure 3. Examples of normalization of grayscale histogram. (a) A room image in Euroc dataset.(b) The grayscale histogram of the image. (c) Normalized grayscale histogram.

Then, the normalized grayscale histogram is used to calculate the mean and standard deviation according to Equation (10) as a rough image feature measure.

$$\mu = \frac{1}{M \times N} \sum_{i=1}^{M} \sum_{j=1}^{N} P(i, j)$$

$$SD = \sqrt{\frac{1}{M \times N} \sum_{i=1}^{M} \sum_{j=1}^{N} (P(i, j) - \mu)^2}$$
(10)

where $M \times N$ is the size of the histogram, P(i, j) represents the value of line *i* and column *j* of the histogram.

After obtaining the histogram information of the keyframe, the keyframe is inserted into the loop closure detection queue, and (μ , SD) is used as the coordinate index to add the keyframe to the container that is connected by a mean and standard deviation. This operation makes the keyframes with a similar mean and standard deviation always stored in a certain interval of the container. Filter candidate keyframes first when loop closure detection. According to the container characteristics of the mean-SD structure, the keyframe group similar to the mean and standard deviation of the current keyframe KF_i is taken out, and then all keyframes with common words with KF_i are taken out from the keyframe group through the bag-of-words model and inverted index. This process can help us roughly and quickly exclude some impossible options, saving time for the SLAM system.

The obtained keyframe group is further eliminated according to the common view relationship. If the number of common view keyframes in KF_i is m, the m frames connected to KF_i will be directly eliminated, which is not used to calculate similar scores. Moreover, if the result of insufficient similarity between this keyframe and KF_i is obtained by judging the similarity score; a one-way mark that is not used for detection will be added to this keyframe to illustrate that there is no similarity between this keyframe and KF_i . According to this mark, when traversing the common words of other KF_i and its similar keyframes, those with this mark will skip directly. This also saves a lot of computer resources, with less computational cost to save subsequent invalid duplicate calculations.

Then, a set of keyframes K_M with a high similarity score is obtained by the bag-ofwords matching and calculating the similarity score. According to the characteristics of bag-of-words matching, K_M has high similarity with KF_i in multiple parts, but in many textured similar environments, the overall similarity between K_M and KF_i is still not guaranteed. Thus, before K_M is calculated by Sim3, we calculate the correlation between the grayscale histogram of K_M and KF_i to compare the overall grayscale distribution. Suppose the grayscale histogram of H_1 and H_2 , and the correlation between H_1 and H_2 is $d(H_1, H_2)$, then

$$d(H_1, H_2) = \frac{\sum_I (H_1(I) - \bar{H}_1)(H_2(I) - \bar{H}_2)}{\sqrt{\sum_I (H_1(I) - \bar{H}_1)^2 \sum_I (H_2(I) - \bar{H}_2)^2}},$$
(11)

where,

$$\bar{H}_k = \frac{1}{N} \sum_j H_k(j) \tag{12}$$

If $d(H_1, H_2)$ is closer to 1, it is considered that the correlation between H_1 and H_2 is higher. Although the high correlation between two grayscale images cannot be obtained from the high correlation between grayscale histograms, it can be concluded that there is no similarity between two grayscale images if the correlation between grayscale histograms is insufficient. Combined with the previous bag-of-words model screening, if $d(H_1, H_2)$ is greater than a certain threshold (0.8 in this paper), it can be determined that the similarity between the two frames is high enough. On the contrary, if $d(H_1, H_2)$ is less than the threshold, skip the current keyframe and judge the next keyframe. In the subsequent test, the situation that the candidate frame is abandoned due to poor frame quality will not occur.

If the candidate keyframes K'_M that meets all the above conditions is obtained, a local window W_m is defined. The window contains K'_M and several keyframes with the highest degree of common view. The set of all mappoints in W_m is X_m . Mappoints of X_m and KF_i are matched by a bag-of-words. Then, the Sim3 solver is constructed, and the initial relative pose T_{am} of W_m and KF_i is solved by RANSAC. Through T_{am} , the mappoints in the window and the mappoints in KF_i are projected bidirectionally similar to Figure 2, so as to obtain more matching points. According to Equation (1), a more accurate relative pose is obtained by nonlinear optimization by minimizing the reprojection error. If the number of interior points is greater than a certain threshold, a more stringent search radius and Hamming distance are used to match again. Otherwise this process is repeated to obtain a relative pose with the highest accuracy.

After the T_{am} is calculated, in order to prevent the loop closure failure, it is necessary to check the keyframes like a collection card. This process follows the geometric consistency check in [17] and the loopback continuity check in [5]. Firstly, the geometric consistency check is performed. This process does not depend on time continuity, and K'_M is verified by the degree of common-view between its keyframes and KF_i. If the common-view keyframes of K'_M have enough matching points with KF_i , it is recorded as a successful verification. Traverse these common-view keyframes, and if at least three of them pass the check, exit the check process. Otherwise, the loopback continuity check is performed. The loop closure detection results are verified by projecting X_m to the newly generated keyframes for matching, and the pose of Sim3 is optimized. If the number of matching points meets the requirements, it is recorded as a validation success. If the total number of verification successes (geometric consistency check and loopback continuity check) reaches three times, the detection process will be directly exited, and the final roll angle, pitch angle and yaw angle will be judged. In ORB-SLAM3, the roll angle and pitch angle are required to be less than 0.46°, and the yaw angle is less than 20°, otherwise the loopback result is considered bad. If the above conditions are met, loopback correction will be performed.

3. Simulation Results and Performance Analysis

In order to verify the effectiveness of the proposed algorithm, this paper uses the visual-inertial dataset Euroc [29] collected by a micro aerial vehicle (MAV) for simulation. Euroc contains 11 stereo video sequences, and the dataset environment is divided into indoor rooms and factories. Firstly, according to the different initialization effects caused by different motion characteristics of each sequence, the dataset is divided into two categories, where MH01~MH05 is the sequence with difficulty in initialization, and V101~V203 is the sequence with easy initialization. Since V203 contains motion blur and loop closure, we use it as a sequence to verify time efficiency. The simulation platform is an Intel (R) Core (TM) i7-7700HQ CPU @ 2.80GHz, 24G RAM computer.

3.1. Quantitative Analysis

This paper first provides the number of the pose and trajectory length of the map generated after running on a Euroc dataset before and after the improvement of the ORB-SLAM3 algorithm, and according to Equations (13) and (14), the effect of the number of Pose and trajectory length recovery by the algorithm in this paper compared with ORB-SLAM3.

$$\sigma_{Pose} = \left(\frac{\beta}{\alpha} - 1\right) \times 100\% \tag{13}$$

$$\sigma_{Traj} = (\frac{\gamma}{\mu} - 1) \times 100\% \tag{14}$$

where σ_{Pose} is the effect of the Pose recovery, σ_{Traj} is the effect of trajectory recovery, α and β , μ and γ are the number of the Pose and the total length of map trajectory before and after the algorithm improvement. In order to eliminate interference as much as possible and ensure the rationality of the experimental data, the experimental data are the result of taking the median value after running the Euroc dataset ten times, such as Table 1.

Table 1. Comparison of ORB-SLAM3 and proposed algorithm. It includes the comparison and improvement of the number of the Pose and the trajectory length (unit in meters). The Pose is estimated by the SLAM system according to the video sequence, and its number is the same as the number of the Pose in the trajectory file.

Saguanca	Number o	f Pose	Cains	Traject	Coinc	
Sequence	ORBSLAM3	RBSLAM3 Ours		ORBSLAM3	Ours	- Gallis
MH01	3548	3680	3.72%	78.826	83.253	5.62%
MH02	2207	3037	41.36%	65.517	75.288	14.91%
MH03	2282	2698	18.23%	128.725	141.722	10.11%
MH04	1605	2032	26.60%	91.038	102.449	12.53%
MH05	1789	2262	26.44%	95.522	110.080	15.24%
V101	2800	2894	3.36%	58.413	58.828	0.71%
V102	1592	1705	7.11%	75.478	78.727	4.30%
V103	2000	2139	6.95%	79.127	79.935	1.02%
V201	2183	2275	4.21%	37.368	37.721	0.94%
V202	2269	2346	3.41%	83.744	84.165	0.50%
V203	1810	1917	6.44%	87.076	87.570	0.57%

A more complete map can be generated when there are more Poses or fewer discarded frames. The length difference of map trajectory can also intuitively reflect the effect of mapping and the distance consumed by the algorithm initialization. Due to the recovery tracking and mapping of discarded frames during initialization, this algorithm must have a longer map trajectory than ORB-SLAM3. However, in the initialization, due to different motion modes of different datasets, the effect of map restoration in this paper is different.

The initialization of the visual-inertial SLAM system needs to meet the following conditions at the same time: the perspective changes slowly, the tracking thread works normally, and the IMU excitation is stable and sufficient.

For example, in the MH02 sequence, the initialization of the system can be divided into three stages, namely the vertical reciprocating motion, horizontal reciprocating motion, and horizontal circular motion. Visual-inertial SLAM systems face different challenges at each stage. In the first stage, the local map tracking fails due to the rapid change of perspective, so that the SLAM system cannot create the map. In the second stage, the map cannot be created and the IMU cannot be initialized because the tracking thread is still not working properly. In the third stage, the three conditions for initialization are satisfied, thus completing the computation of the IMU residual, bias and BA optimization of the first part. However, the MAV then landed on the take-off platform, and the lack of excitation of the IMU caused the initialization to fail again. In these three stages, the current ORB-SLAM3 algorithm cannot complete the initialization and loses a lot of initialization information. The initialization cannot be completed until the next time the MAV leaves the platform, however, the map created does not include the map information of the first three stages.

After the recovery tracking of the algorithm in this paper, the Pose recovery of 41.36% can be achieved on the MH02 sequence. Since some frames are stationary, namely, the pose difference is small, the actual trajectory recovery is 14.91%, about 9.771 m. It can be observed from Table 1 that the initialization effect of ORB-SLAM3 is poor in the factory environment; thus, the effect is better after the algorithm is improved in this paper. In the sequence of room environment in V101~V203, ORB-SLAM3 can be initialized quickly, so the effect after recovery and tracking has little improvement, and the recovered trajectory length is only about half a meter away.

Secondly, for example, Table 2, this paper also counts the root mean square error (RMSE) and standard deviation of the ATE to reflect the improvement of robustness and stability of the proposed algorithm compared with the ORB-SLAM3. RMSE can well reflect the global consistency, such as Equations (15) and (16),

$$RMSE(F_{1:n}) := \left(\frac{1}{n} \sum_{i=1}^{n} \|trans(F_i)\|^2\right)^{\frac{1}{2}},$$
(15)

$$F_i := Q_i^{-1} S P_i, \tag{16}$$

where $||trans(F_i)||$ represents the translation part of the ATE, $Q_i \in SE(3)$ is the ground truth, $P_i \in SE(3)$ is the estimated pose, and $S \in SE(3)$ is the transformation matrix from P_i to Q_i . The improvement of the time efficiency of the proposed algorithm is analyzed by calculating the time spent by the SLAM system in the loop closure detection and the mean tracking time of each frame. Table 3 reflects the improvement of each sequence in the Euroc dataset.

Table 2. Comparison of absolute trajectory error (ATE) and time efficiency. The mean time (unit in second) is the time consumed by tracking each frame, and the detection time (unit in millisecond) is the time consumed by each frame in the loop closure detection.

S aguar as	RMSE		Standard Deviation		Mean Time		Detect Time	
Sequence	ORBSLAM3	Ours	ORBSLAM3	Ours	ORBSLAM3	Ours	ORBSLAM3	Ours
MH01	0.042274	0.021442	0.028004	0.008902	0.03448	0.02702	2.00182	0.72322
MH02	0.089979	0.025743	0.035764	0.013315	0.03591	0.02768	1.46197	0.66376
MH03	0.144068	0.035220	0.095012	0.017778	0.03232	0.02814	2.31237	1.09805
MH04	0.140039	0.134385	0.068027	0.060891	0.03118	0.02470	2.58796	1.55749
MH05	0.492024	0.057585	0.300062	0.026758	0.03073	0.02590	2.56432	1.40208
V101	0.058089	0.035530	0.027776	0.012011	0.03059	0.02986	2.24815	0.95563
V102	0.074244	0.017952	0.063103	0.011832	0.02831	0.02615	2.18541	0.85070
V103	0.019957	0.018903	0.008785	0.008886	0.02824	0.02493	2.36221	0.85074
V201	0.048377	0.028486	0.027442	0.014310	0.02632	0.02508	3.27765	1.27054
V202	0.024106	0.015883	0.009851	0.006280	0.02998	0.02612	2.89432	1.11357
V203	0.033258	0.024923	0.017620	0.014805	0.02701	0.02465	2.54009	1.16674

Table 3. Improvement of RMSE, SD, mean tracking time and loop closure detection time.

	MH01	MH02	MH03	MH04	MH05	V101	V102	V103	V201	V202	V203
RMSE	49.28%	85.21%	75.55%	4.04%	88.31%	38.84%	75.82%	5.28%	41.12%	34.11%	25.06%
SD	68.21%	85.93%	81.29%	10.49%	91.08%	56.76%	81.25%	-1.15%	47.85%	36.25%	15.98%
Mean Time	21.64%	22.92%	12.93%	20.78%	15.72%	2.39%	7.63%	11.72%	4.71%	12.88%	8.74%
Detect Time	63.87%	54.61%	52.51%	39.82%	45.32%	57.49%	61.07%	63.99%	61.24%	61.54%	54.07%

After comparing and analyzing the proposed algorithm with ORB-SLAM3 using Euroc dataset, it can be observed that under the same conditions (compared with the complete trajectory of the ground truth), RMSE, standard deviation, mean tracking time and loop

closure detection time of the proposed algorithm are reduced. The RMSE of 11 sequences decreased by 47.51% on average, and the accuracy was improved significantly. Among them, the RMSE on MH01~MH05 sequence is much lower, which is because the number of Pose recovered by the algorithm in this paper on these sequences is up to several hundred, and the final reconstructed map trajectory is long. More information can be provided to the map after trajectory recovery, and keyframes created during tracking can also be involved in global optimization to further improve accuracy. At the same time, because the time efficiency of the SLAM system is improved, there are more sufficient computer resources to complete BA optimization and more stable tracking image frames. The RMSE reduction in V101~V203 is less than in the factory environment. This is because in the sequence of these room scenes, the image frame and IMU data obtained by SLAM system are good and can complete rapid initialization, so the accuracy improvement effect of this algorithm on these sequences is limited. Secondly, the average decline of standard deviation on Euroc dataset is 52.18%, which indicates that the proposed algorithm is more stable than the original algorithm and can run SLAM system consistently.

In addition, this algorithm can also significantly improve the time efficiency. In the Euroc dataset, tracking the time efficiency increased by 12.91% on average, and the detection time efficiency increased by 55.96% on average. Similarly, the time efficiency is significantly improved in the sequences with difficulty in initialization, which is due to the computational lightweight of the map restoration algorithm in this paper. Of course, the improvement is not high in the easy initialization sequence. It is worth noting that V103, V202 and V203 sequences are easy to initialize, but there are loop closures in their sequences. After the loop closure, the number of common-view keyframes will increase significantly, so that more frames can be eliminated, and the detection time and tracking time can be significantly reduced.

Therefore, compared with ORB-SLAM3, the proposed algorithm can first generate a complete map, and then significantly improve the accuracy and time efficiency of the difficult initialization sequence. According to the characteristics of the algorithm, in the environment that initialization is easier to fail and the number of loop closure is more, or when the system runs longer, the accuracy and time efficiency of the system are improved more obviously.

3.2. Qualitative Analysis

In order to evaluate the performance impact of the proposed algorithm on the SLAM system more intuitively, two representative sequences (MH02 and V203) are selected and qualitatively analyzed. This is where the MH02 is the sequence with difficulty in initialization, and V203 is the sequence with easy initialization. First, the differences between the estimated trajectories before and after the algorithm improvement and the groundtruth trajectories are compared. Then, the difference of RMSE of ATE between the two algorithms is compared.

As shown in Figures 4 and 5, the trajectories on the MH02 sequence and the V203 sequence are compared, respectively. The blue line is the trajectory generated by the algorithm in this paper, the brown line is the trajectory generated by ORB-SLAM3, and the gray dotted line represents the ground truth trajectory. The red rectangle in the figure marks the position where ORB-SLAM3 initialization is completed.

It is obvious that ORB-SLAM3 loses a large part of the initial map information when faced with challenging sequences (MH02). In this case, the map recovered by the proposed algorithm has higher value. On the other hand, in the easily initialized sequence (V203), the maps we can recover are limited because ORB-SLAM3 is able to complete the initialization at an earlier position.



Figure 4. Trajectory comparison in the MH02 sequence.



Figure 5. Trajectory comparison in the V203 sequence.

As shown in Figure 6, the ATE of the proposed algorithm (yellow) is smaller than that of ORB-SLAM3 (blue) in both difficult and easy initialization sequences, and is more obvious in difficult initialization sequences. Due to the slow initialization of ORB-SLAM3 in the MH02 sequence, there is no data at the beginning. In addition, some outliers will be generated in our restored map. This is because there are many static scenes at the beginning of the sequence, and it is unstable to process this information through vision. However, the effectiveness of the map will not be affected by these few outliers. We further analyze the ATE of the two, as shown in Figure 7. The blue part of the box plot is ORB-SLAM3, and the brown part is the algorithm in this paper. It can be clearly observed that the data obtained by the proposed algorithm are more concentrated, and they are all concentrated in areas with small ATE. The above is the qualitative analysis of the proposed algorithm. Next, V203 is taken as an example to analyze the improvement of the time efficiency of the loop closure detection part by the proposed algorithm.



Figure 6. Comparison of ATE (raw date). (**a**) and (**b**) are the ATE comparison between the proposed algorithm and ORB-SLAM3 in MH02 sequence and V203 sequence respectively. The yellow line represents the result of the proposed algorithm, and the blue line represents the result of ORB-SLAM3.



Figure 7. Comparison of ATE (box plot). (**a**,**b**) are the comparison of ATE between the proposed algorithm and ORB-SLAM3 in MH02 sequence and V203 sequence, respectively, by box plot. The results of ORB-SLAM3 are shown in blue and ours are shown in brown.

V203 is a fast moving sequence with motion blur. In this sequence, a large number of repeated scenes begin to appear in the middle and late stages. The SLAM system should complete loop closure detection and loop correction during this period. However, not all frames can be used as the reference frames of the loop, because most frames are blurred or the rpy direction angle changes too much. Although these frames can extract feature points and match them, they will eventually be abandoned. Therefore, there are many times of invalid calculations in V203 due to the above reasons, in which each calculation takes tens of milliseconds, which seriously wastes computer resources. However, the grayscale histogram is very sensitive to the changes of pitch angle, roll angle and yaw angle. If one of the changes is too large, the grayscale distribution of image frames will change greatly. According to this feature, the proposed algorithm eliminates these image frames which may cause invalid calculation in advance, thus improving the quality of input frames.

Figure 8 shows the comparison of the time-consumed for loop detection in each frame of the V203 sequence, where blue is the proposed algorithm and red is ORB-SLAM3. It is obvious that the time-consuming of the proposed algorithm is generally significantly lower than that of ORB-SLAM3. When a large number of similar frames appear in the medium term, many calculations over 10 ms are performed in ORB-SLAM3. However, the proposed algorithm completes the loop correction process only after two such calculations.

It is worth noting that on the same sequence, the loop completion time of the proposed algorithm is slightly earlier than that of ORB-SLAM3. This is because when ORB-SLAM3 calculates and optimizes the pose, it takes too much time, resulting in missing the most

suitable loop candidate frame, and only finding the appropriate loop candidate frame after the calculation is completed.



Figure 8. Computation time used to loop closure detection for each frame in V203.

Around 230 of the sequence, the loop closure detection process is mainly concentrated here. For example, loop closures can be detected by the bag-of-words model in both Figure 9a,b, but only the keyframe pair in Figure 9a can finally pass the loop closure check. In Figure 9b, the computer reappears at the same angle, so some descriptors are successfully matched. By matching using the bag-of-words model, we think that the camera came to the same location. However, in this keyframe pair, the computer is at different distances in the image, and the roll angle of the camera changes significantly. In the loop closure check, because the scale of the feature points has a large difference or the angle of the rpy direction changes too much, we think that the loop closure at this time has a great risk, and thus reject the loop closure. However, this situation can be effectively avoided by improved methods. For example, the grayscale histogram similarity of the keyframe pair in Figure 9a is 0.9782, and in Figure 9b is 0.6659. Therefore, the loop closure in Figure 9b will be eliminated early.



Figure 9. Pairs of keyframes detected by loop closures in V203 sequences and their grayscale histograms. (a) Good loopback situation. The loopback detection thread can usually complete the loopback here. (b) Bad loopback situation. The loopback detection thread is prone to loopback rejections here.

More importantly, when we combine Figures 6b, 8 and 9, we can understand why there are some larger ATEs at certain time spots. We found that in the V203 sequence, its

ATE was larger during the period when loop closures were easily identified. This is because different threads need to coordinate the allocation of computer resources when the SLAM system processes tasks. Moreover, when ORB-SLAM3's loop closing thread requests more time to process the loopback, the work of tracking the thread becomes more challenging. As a result, the accuracy of the Poses we obtain will decrease. Of course, not all larger ATEs are only affected by time efficiency. As shown in Figures 9b and 10, motion blur and large scale changes will affect our accuracy. In general, both motion blur and scale differences will affect the quality of the feature points extracted by the SLAM system. When we use these feature points to track and estimate pose, there will be fluctuations in accuracy.



Figure 10. Motion blur in V203 sequences. The image in the red rectangle is the blurred image.

4. Conclusions

This paper proposes a real-time map restoration algorithm based on ORB-SLAM3. This method reversely tracks all frames before successful initialization, and accelerates the loop closure detection. We can generate a complete map in real time regardless of the initialization effect of the system. After comparing the RMSE of ATE, the accuracy was increased by 47.51% on average. Compared with standard deviation, the stability is increased by 52.18% on average. After comparing the time consumption, the time efficiency in the loop closure detection stage increases by 55.96% on average, and the average tracking time of the system decreases by 13% on average. Experiments show that the proposed algorithm can achieve map restoration while ensuring real-time performance. The complete map generated by this algorithm is significant for off-line robot tracking.

The map restoration method proposed in this paper is mainly for the scenes with difficult initialization, and the effect is not obvious in simple scenes. In addition, the proposed algorithm is based on the assumption of low dynamic environment and does not eliminate dynamic objects, so the accuracy in an high dynamic environment will decrease. In the future, dynamic detection function should be added so that robots can adapt to more complex environments.

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Abbreviations

The following abbreviations are used in this manuscript:

SLAM	Simultaneous Localization and Mapping
IMU	Inertial Measurement Unit
MSCKF	Multi-State Constraint Kalman Filter
MLPNP	Maximum Likelihood Solution to The Perspective-N-Point
VIO	Visual Inertial Odometry
OPENVINS	Open Visual-Inertial SLAM
VINS	Visual-Inertial SLAM
EKF	Extended Kalman filter
ARUCO	Augmented Reality University of Cordoba
LSD-SLAM	Large-Scale Direct SLAM
SVO	Semidirect Visual Odometry
ORB	ORiented Brief
LK	Lucas–Kanade
RGB-D	RGB-Depth
CPU	Central Processing Unit
SSD	Single Shot Multibox Detector
OKVINS	Open Keyframe-Based Visual-Inertial SLAM
BRISK	Binary Robust Invariant Scalable Keypoints
PGO	Pose Graph Optimizer
SFM	Structure From Motion
RANSAC	Random Sampling Consensus
Sim3	Similar Transformation Using 3 Pairs of Points
MAV	Micro Aerial Vehicle
BA	Bundle Adjustment
ATE	Absolute Trajectory Error
RMSE	Root Mean Square Error
SD	Standard Deviation

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