

## Article

# Loss Research and Thermal Analysis of BLDC Hollow-Cup Motor Under Reactor Suppression

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**Abstract:** In order to avoid overheating of a BLDC permanent magnet (PM) motor at high speeds, this paper focuses on the loss reduction of a 90 W 47,000 r/min BLDC hollow-cup motor. It is proposed to provide an optimizing method for the series reactors and the parameterization of reactors in the motor system. The finite element method (FEM) is used to calculate and analyze the time harmonic of air-gap magnetic flux density, stator core loss, and rotor eddy current loss in two cases: with a series reactor and without a reactor. By parameterizing the inductance value, the optimal resistance value is determined to minimize motor loss. In addition, an electromagnetic–thermal coupling analysis is conducted, and the results show that the temperature distribution of the stator core, winding, and rotor are improved under reactor suppression. Finally, an experimental platform is built to verify the temperature increase and the efficiency of the motor load operation. A clear reference for the research and optimization analysis of motor loss reduction is provided.

**Keywords:** BLDC hollow-cup motor; time harmonics; reactor; finite element analysis; optimization of losses; temperature field



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## 1. Introduction

BLDC hollow-cup motors are in high demand for unmanned aerial vehicles (UAV), ventilators, and robotic arm applications owing to their high efficiency, low cost, high speed, and other significant characteristics. BLDC hollow-cup motors are different from other types of motors, through which the toothless structure enables the cogging effect of the motor to be suppressed [1]. However, the small armature inductance of BLDC motors cannot effectively suppress current-time harmonics, which leads to increased core loss, reduced efficiency, and higher operating temperatures [2]. In this study, due to the high speed and the current harmonic of the BLDC motor, the significant loss and over-temperature of the BLDC motor is the urgent problem, leading to the irreversible demagnetization of PMs and even to the failure of the motor.

Feng and Yoshida [3,4] proposed the use of special materials, such as amorphous magnetic materials (AMM) and nanocrystalline magnetic materials (NMM), as core elements for high-speed motors to reduce the core losses. A new type of BLDC motor is investigated in Ref. [5]; its stator and rotor are made of soft magnetic composite (SMC) cores, which reduce eddy current losses and increase motor efficiency. The core loss of the segmented stator core is further reduced by applying a corner radius to each tooth root [6]. The literature [7,8] proposes methods to reduce core losses and cogging torque by optimizing the rotor shape of high-speed permanent magnet synchronous motors (PMSMs). The use of molded transposed windings in PMSMs is described in Ref. [9]. This type of winding reduces the copper

loss of the motor, to some extent. Z. Zhang et al. investigated the effects of the winding arrangement and core material on iron loss for high-speed switching motor reluctance [10]. L.Y. and Z. F [11] proposed a split-phase winding method for a HSPMM (high-speed permanent magnet motor) which reduces the rotor eddy current losses. Ref. [12] analyzed the effect of copper shielding on eddy current losses in high-speed PMSMs.

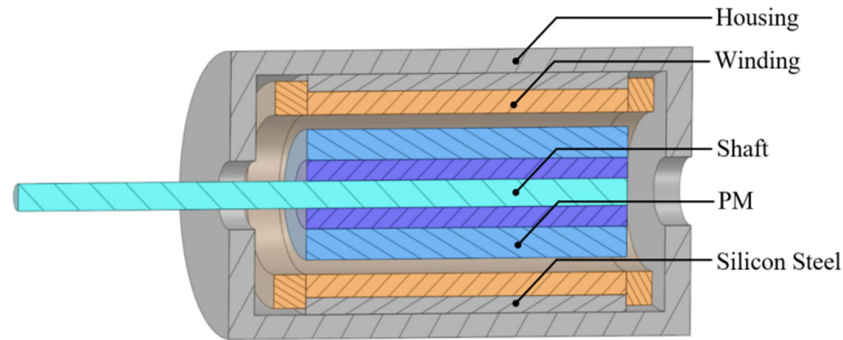
Moreover, the current harmonic magnetic field causes eddy current loss in the rotor, and excessive eddy current losses can lead to an increase in temperature. In the study of the effect of time harmonics on electromagnetic losses, Ref. [13] focused on a surface-mounted high-speed PMSM that uses segmented permanent magnets to reduce eddy current losses in the rotor. Minh and Quoc [14] designed a high-speed PMSM with closed slots that significantly reduced the 11th and 13th harmonics of the air-gap flux density, resulting in a reduction in rotor eddy current losses. Im and Gu [15] proposed an optimized current switching and harmonic elimination scheme based on 7th harmonic current injection for trapezoidal BLDC motors to reduce losses and improve efficiency. Vafaie M. H. et al. proposed the use of Halbach array permanent magnet configurations in brushless DC motors to eliminate reverse electromotive force harmonics and reduce losses [16]. A BLDC motor control scheme is proposed in Ref. [17], where the loss is reduced by current harmony, and its negative effects are minimized. Khazaae et al. analyzed the additional electromagnetic losses in the motor during inverter power supply [18]. The analyzed results show that the current time harmonic and stator slotting are the main reasons for the increase in electromagnetic losses.

In this paper, based on previous research, this study takes a high-speed BLDC motor as the research subject. In order to improve efficiency, it is important to study the loss under reactor suppression by using FEA on the magnetic–thermal coupling. The key innovations in this paper are as follows: by changing the system inductance value and analyzing its effect on motor loss and temperature, a method involving a reactor in series between a BLDC hollow-cup motor and a controller is proposed. Through this method, the core loss and rotor eddy current loss can be effectively suppressed. And finally, the experimental platform using a BLDC motor is built to verify the accuracy of the simulation results by measuring the efficiency and temperature rise of the prototype.

The research content and innovativeness of this paper is presented in Section 1. Section 2 presents the main structure and rated parameters of the motor. The optimization method is proposed in Section 3, which mainly analyzes the characteristics of the motor core loss, voltage, current, rotor loss, etc., based on the reactors with different inductance parameters. Section 4 verifies the effectiveness of the optimization content by performing an electromagnetic field-temperature field coupling on the motor. In Section 5, the performance and temperature increase of the optimized prototype are measured. The measured results are compared with the feasibility and accuracy of the optimization method. Section 6 provides the conclusions of the paper.

## 2. BLDC Hollow-Cup Motor Structure

In this paper, a 90 W 47,000 r/min BLDC hollow-cup motor is presented. The 3D-sectional view of the motor structure is presented in Figure 1. The stator of this motor consists of ring-shaped, toothless silicon steel and a hollow-cup winding. This structure greatly reduces the influence of the cogging effect, reduces the overall size of the motor, and increases the power density. The rotor is made of ring PM, and the PM material is NdFeB. The motor parameters are listed in Table 1.



**Figure 1.** A 3D Model of the BLDC hollow-cup motor.

**Table 1.** Parameters of the motor.

Motor Parameters	Numerical Value
Rated power	90 W
Rated voltage (DCV)	24 V
Rated speed	47,000 r/min
Rated efficiency	85%
Frequency	783 Hz
Number of poles	2
Air-gap length	0.5 mm
Stator inner diameter	20 mm
Stator outer diameter	27 mm
Stator length	50 mm
PM length	50 mm

### 3. Improvement Design Study

#### 3.1. Theoretical Foundation

When a controller is used to power a BLDC hollow-cup motor, a current time harmonic is present in the motor winding, generating an armature magnetomotive force harmonic. The current time harmonic  $I_k$  is shown by Equation (1). The frequency  $f_k$  of the  $k$ th time current harmonic and the amplitude of the  $k$ th armature magnetomotive force harmonic generated by the  $v$ th current time harmonic are shown by Equations (2) and (3) [16], where  $f_1$  is the controller output current in the fundamental frequency, and  $k$  is the order of the current time harmonic [16].

$$I_k = \frac{U_k}{2\pi f_k L_a}, \quad (1)$$

$$f_k = k f_1, \quad (2)$$

$$|F_{(k,v)}| = \frac{3\sqrt{2}}{\pi v p} N k_{wv} I_k, \quad (3)$$

where  $U_k$  is the voltage time harmonic;  $f_k$  is the current time harmonic frequency. The amplitude of the current time harmonic depends mainly on the armature inductance  $L_a$ .  $|F_{(k,v)}|$  is the  $k$ th harmonic amplitude of the armature magnetomotive force generated by the current time harmonic,  $p$  is the number of motor pole pairs,  $k_{wv}$  is the winding factor for the  $v$ th harmonic of the armature's magnetic potential, and  $I_k$  is the RMS value of the  $k$ th current time harmonic.

Not counting the saturation of the magnetic field, the amplitude of the armature magnetomotive force harmonic is proportional to the amplitude of its corresponding generated magnetic field, expressed as follows:

$$|B_{(k,v)}| \propto |F_{(k,v)}|. \quad (4)$$

According to the law of magnetic induction, the induced electromotive force  $E_{(k,v)}$  generated in the iron core is related to the magnetic field amplitude, the alternating frequency  $f_{(k,v)_r}$ , as shown in Equation (5). According to Ohm’s law, the eddy current  $I_{(k,v)}$  in the core is proportional to its induced electromotive force  $E_{(k,v)}$ . According to Joule’s law, the eddy current loss  $P_{(k,v)}$  generated by  $I_{(k,v)}$  in the core is proportional to the square of the amplitude of  $I_{(k,v)}$  [16]. These relationships are shown as follows:

$$E_{(k,v)} \propto |B_{(k,v)}| \times f_{(k,v)_r} \tag{5}$$

$$I_{(k,v)} \propto E_{(k,v)}, \tag{6}$$

$$P_{(k,v)} \propto I^2_{(k,v)}. \tag{7}$$

Analysis of the above equations shows that the armature inductance  $L_a$  is inversely proportional to the current time harmonic  $I_k$ . The amplitude of the current time harmonic  $I_k$  is proportional to the amplitude of the armature magnetomotive force harmonic  $F_{(k,v)}$ , and the eddy current loss  $P_{(k,v)}$  is proportional to  $|F_{(k,v)}|$  [19].

$$P_{(k,v)} \propto \left( |F_{(k,v)}| \times f_{(k,v)_r} \right)^2. \tag{8}$$

### 3.2. Optimization Method

An analysis of the preceding paragraphs shows that, due to the small armature inductance of a BLDC hollow-cup motor, the current harmonics cannot be effectively suppressed. The current harmonics and armature potential harmonics cause an increase in the electromagnetic loss of the motor. Therefore, the method using a reactor in series between a BLDC hollow-cup motor and a controller is adopted in this chapter. By increasing the inductance of the system, both motor losses and temperature rise are suppressed.

Through FE analysis, the BLDC hollow-cup motor drive circuit is established. In addition, reactors are connected in series in each three-phase circuit to analyze the core loss trend for inductance values in the range of 0  $\mu$ H to 25  $\mu$ H. The BLDC hollow-cup motor drive circuit is presented in Figure 2. The motor speed is 47,000 r/min, the operating frequency is 783 Hz, the power is 90 W, and the DC voltage is 24 V.

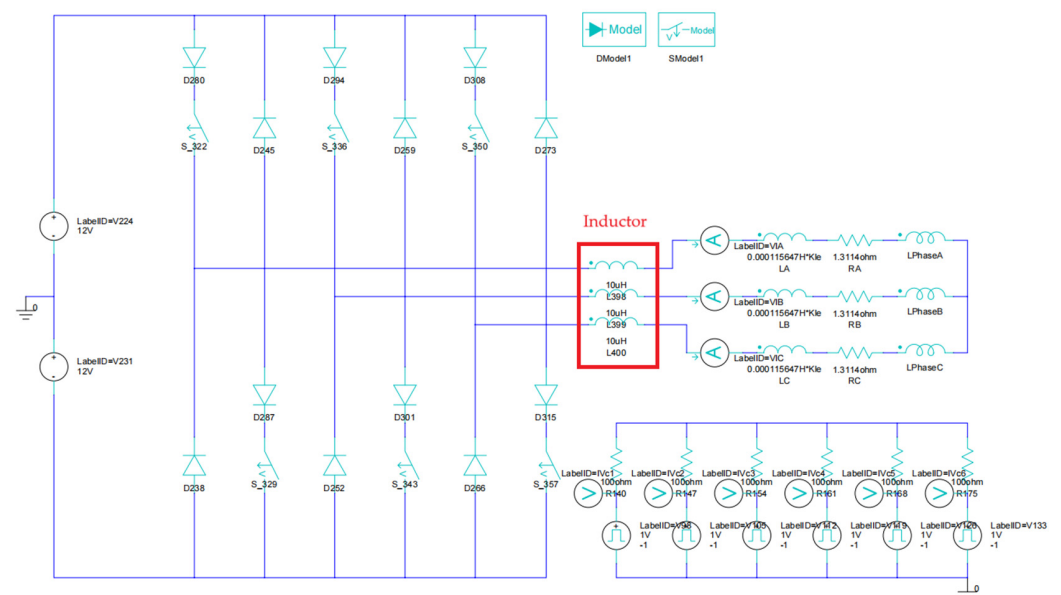


Figure 2. BLDC hollow-cup motor drive circuit.

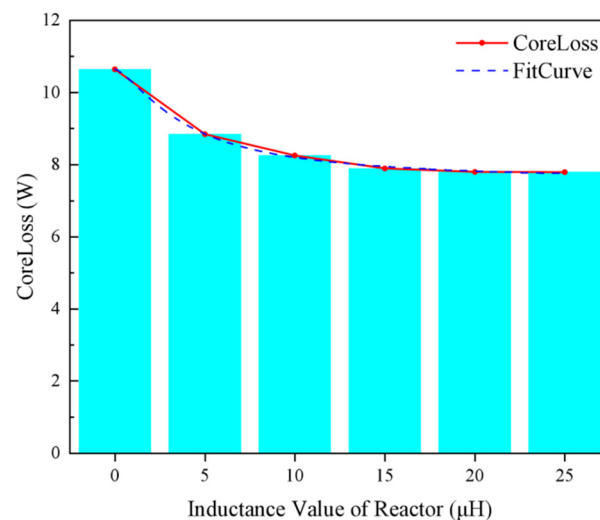
### 3.3. Core Loss Analysis Considering Inductance Value

The armature magneto-kinetic potential is generated by the current harmonics, which in turn generate a magnetically dense harmonic in the core, leading to an increase in core loss. Analyzed through the above equations, the armature magneto-kinetic harmonic amplitude is inversely proportional to the armature inductance  $L_a$  and positively proportional to its resulting flux density amplitude  $B$ . The core loss of the BLDC hollow-cup motor is calculated based on the Bertotti core loss model [20], expressed as follows:

$$P_{Fe} = K_h f B^2 + K_c f^2 B^2 + K_e f^{1.5} B^{1.5}, \quad (9)$$

where  $K_h$  is the hysteresis loss factor,  $K_c$  is the eddy current loss factor,  $K_e$  is the additional loss factor,  $f$  is the magnetic field frequency, and  $B$  is the flux density amplitude.

To analyze the effect of reactor inductance on the core loss, the BLDC hollow-cup motor core loss is calculated for each operating condition by increasing the reactor inductance value by 5  $\mu\text{H}$  in the range of 0  $\mu\text{H}$  to 25  $\mu\text{H}$ . The variation of core loss with the value of the inductance of the reactor is presented in Figure 3.



**Figure 3.** Variation of core loss with inductance of reactor.

The analysis in Figure 3 shows that the core loss decreases significantly as the inductance value increases. However, as the inductance value of the reactor gradually increases, the decreasing trend of the core loss slows down. By the time the reactor inductance reaches 15  $\mu\text{H}$ , the loss variation is stabilized. The variation of core loss for reactor inductance values of 0  $\mu\text{H}$  and 15  $\mu\text{H}$  is presented in Figure 4.

### 3.4. RMS of Load Line Voltage Analysis Considering Inductance Value

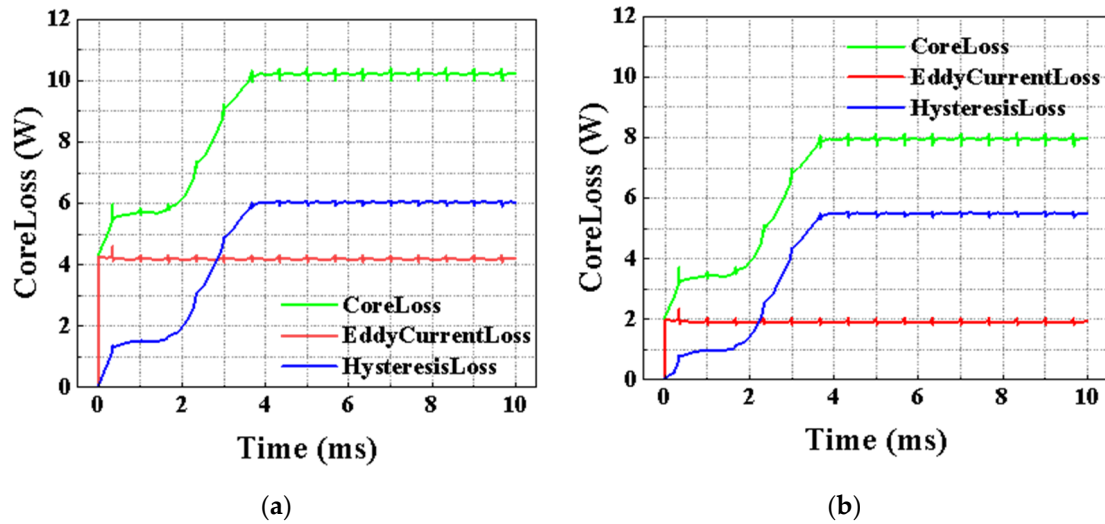
By the time the reactor inductance reaches 15  $\mu\text{H}$ , the loss variation is stabilized. As the inductance of the controller's voltage output continues to increase, the electrical time constant of the entire system will also increase, affecting the system's dynamic performance. The following equations are analyzed. The reactor in series between the BLDC hollow-cup motor and the controller acts as a suppressor of the efficiency of the controller. The differential equation for the voltage at the input of the hollow-cup motor is given in Ref. [20], expressed as follows:

$$U_a = R i_a + (L - M) \frac{d i_a}{d t} + E_a, \quad (10)$$

$$U_b = R i_b + (L - M) \frac{d i_b}{d t} + E_b, \quad (11)$$

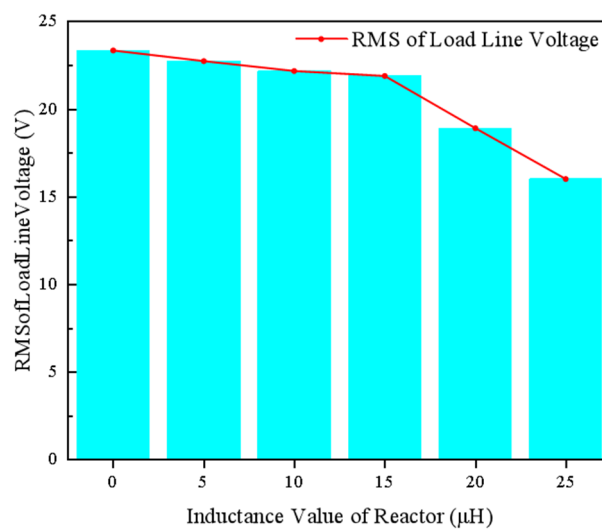
$$U_c = Ri_c + (L - M) \frac{di_c}{dt} + E_c, \tag{12}$$

where  $U_a, U_b,$  and  $U_c$  represent the three-phase voltage,  $E_a, E_b,$  and  $E_c$  represent three opposite electromotive forces,  $i_a, i_b,$  and  $i_c$  represent the three-phase current,  $R$  is the resistance of the three-phase circuit winding,  $L$  is the three-phase circuit inductor, and  $M$  is the mutual inductance in a three-phase circuit.



**Figure 4.** Variation of core loss at different values of inductance: (a) core loss at inductance of 0 μH; (b) core loss at inductance of 15 μH.

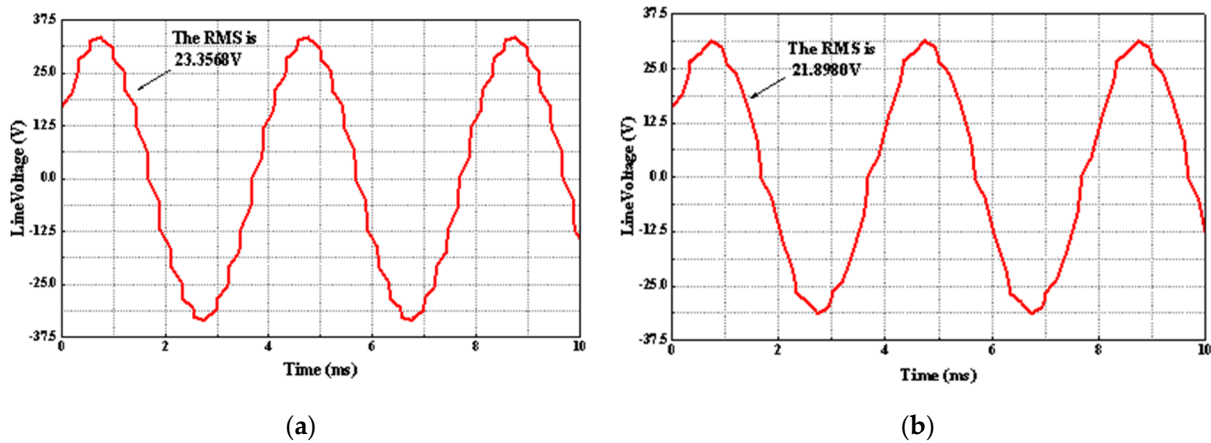
In the following steps, the calculations for the motor load line voltage are performed, the changes in value are analyzed, and the appropriate reactor value is selected. Therefore, loss suppression is achieved, while avoiding the degradation of the dynamic performance of the entire motor system due to excessive inductance values. The trend of the load line voltage RMS is analyzed for each 5 μH increase in reactor inductance in the range of 0 μH to 25 μH. The variation of line voltage RMS with the value of inductance of the reactor is presented in Figure 5.



**Figure 5.** Variation of line voltage RMS with inductance of reactor.

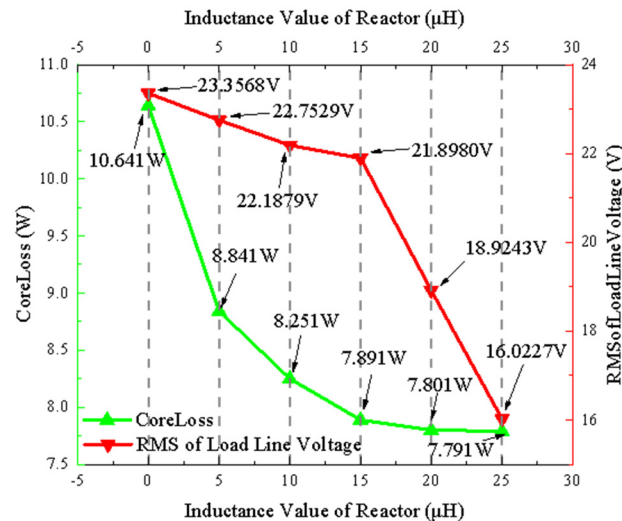
According to the FE calculation, the motor load line voltage tends to decrease with the increase in reactor inductance, and the decreasing trend is more obvious after the

inductance value of 15  $\mu\text{H}$ . The variation of line voltage RMS for the reactor inductance values of 0  $\mu\text{H}$  and 15  $\mu\text{H}$  is presented in Figure 6.



**Figure 6.** Variation of line voltage RMS at different values of inductance: (a) line voltage RMS at value of 0  $\mu\text{H}$ ; (b) line voltage RMS at value of 15  $\mu\text{H}$ .

After comparative analysis, the core loss of the BLDC hollow-cup motor shows a decreasing trend with the increase in the inductance value of the reactor, and this trend tends to stabilize when the inductance value reaches 15  $\mu\text{H}$ . However, the increase in inductance value will have a dampening effect on the motor load line voltage RMS. When the inductance reaches 15  $\mu\text{H}$ , the motor load line voltage RMS decreases more significantly, while the output efficiency of the controller is reduced. In summary, a 15  $\mu\text{H}$  reactor in series between the BLDC hollow-cup motor and the controller improves the efficiency of the motor, without affecting the voltage at the output of the controller. A comparative analysis is shown in Figure 7.



**Figure 7.** Comparative analysis.

Similarly, the calculation results for current and torque also confirm this conclusion. As the effective value of the motor terminal voltage decreases (the inductance value of the reactor in the series motor system increases), to ensure that the output torque of the motor remains unchanged under rated conditions, the input current of the motor will increase accordingly. However, when the inductance value of the reactor exceeds 15  $\mu\text{H}$ , the current increases from 2.5 A to around 3 A, which significantly increases the energy consumption of the motor system. The calculation results for current and torque are shown in Figure 8.

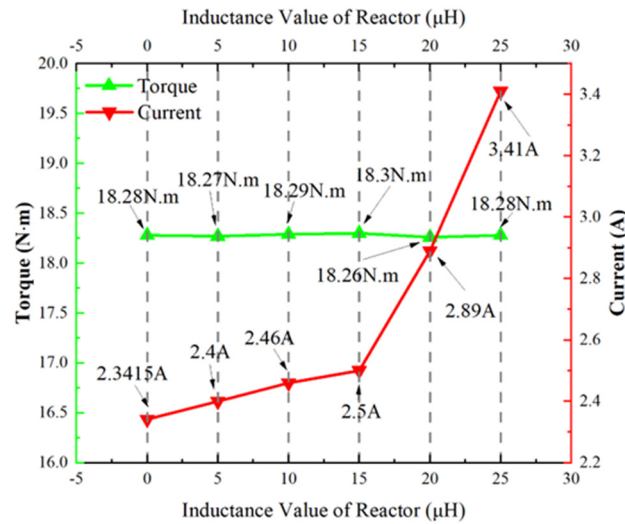


Figure 8. Results for current and torque.

### 3.5. Air-Gap Density Distribution and Current Time-Harmonics Analysis

To analyze the effect of the reactor inductance value on the air-gap flux density and time harmonic, the no-load air-gap flux density and current time-harmonic spectra of the electromagnetic model, before and after the series connection of a 15  $\mu\text{H}$  reactor to motor system, are comparatively analyzed. The radial and tangential air-gap flux density distributions are shown in Figure 9. The radial and tangential air-gap flux density time-harmonic amplitudes are shown in Figure 10.

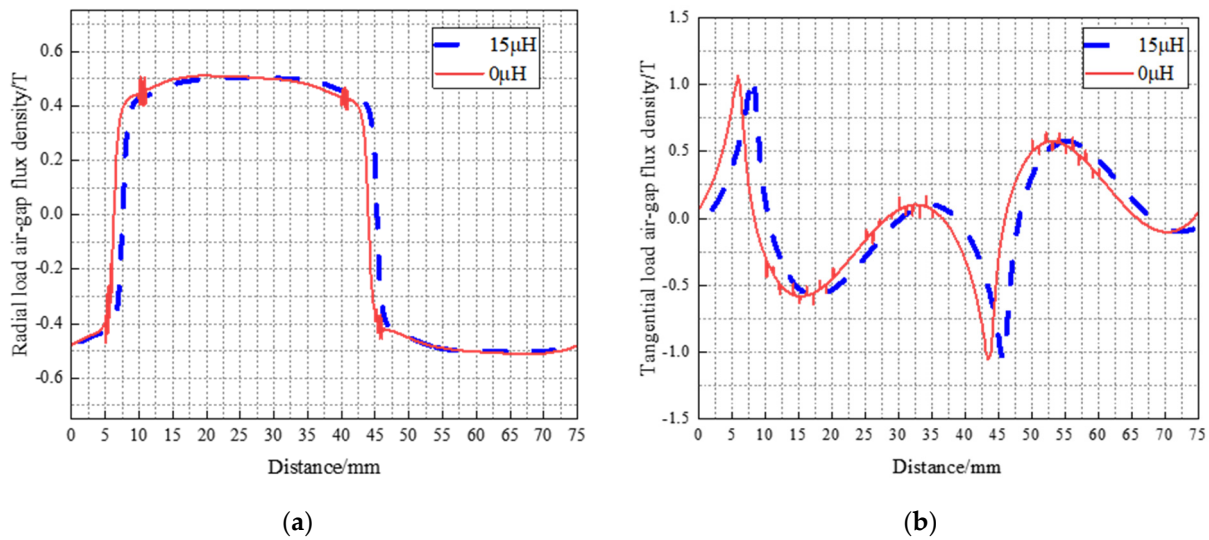


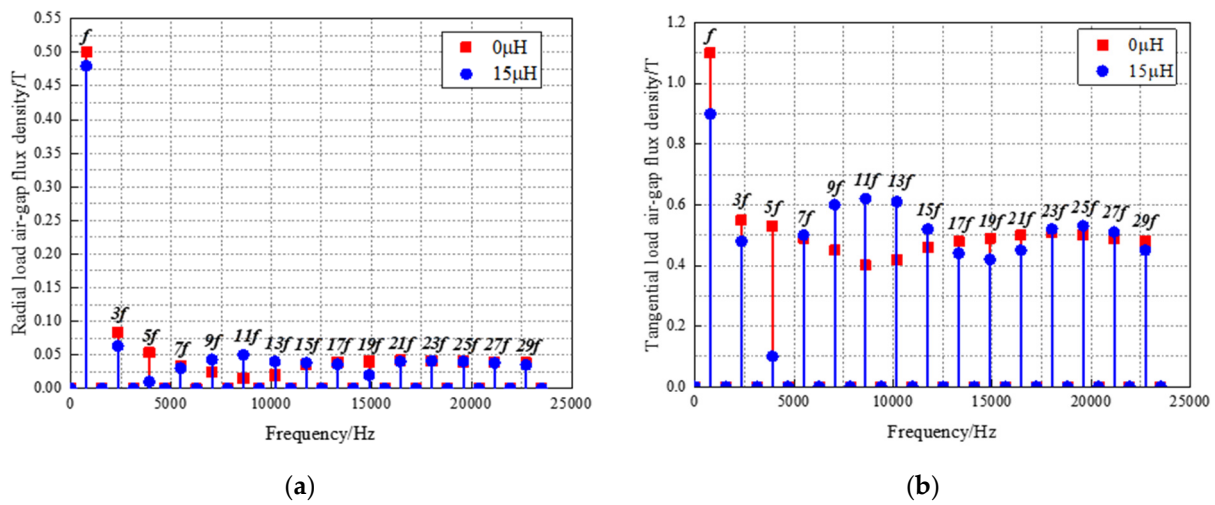
Figure 9. Air-gap flux density before and after series connection of 15  $\mu\text{H}$  reactor: (a) radial air-gap flux density; (b) tangential air-gap flux density.

The no-load air-gap flux density amplitude of the motor is approximately equal after series connection of a reactor of 15  $\mu\text{H}$ . From Figure 9a, it can be observed that the optimized radial air-gap flux density curve is smoother than before optimization. Figure 9b shows that the optimized tangential air-gap flux density is reduced, and the curve is smoother.

From Figure 10a, it can be seen that harmonic of the air-gap flux density is reduced after series connection of a 15  $\mu\text{H}$  reactor; the analysis of the radial air-gap flux density time-harmonic spectrum shows that the main harmonic component is the  $(2n - 1)$ th harmonic. As seen in Figure 10b, the optimization method attenuates the lower harmonics more significantly, the 3rd and 5th harmonics are attenuated more drastically, and the main



harmonic component is the  $(2n - 1)$ th harmonic. From the above analysis, the air-gap flux density amplitude is reduced by series connection of a  $15 \mu\text{H}$  reactor, and the current time harmonic and armature magnetomotive force harmonic are effectively suppressed.



**Figure 10.** Air-gap flux density time-harmonic amplitude before and after series connection of  $15 \mu\text{H}$  reactor: (a) radial air-gap flux density time-harmonic amplitude; (b) tangential air-gap flux density time harmonic amplitude.

### 3.6. Rotor Eddy Current Loss Analysis

The motor rotor eddy current loss is caused by the harmonic magnetic field generated by the current harmonics, while the armature potential harmonics cause an increase in rotor eddy current loss [21]. The previous Equations (1)–(8) are analyzed. It can be noticed that the amplitude of the armature potential harmonic is inversely proportional to the armature inductance and directly proportional to the flux density harmonic amplitude. Faraday’s law of electromagnetic induction is considered, and it is known that the induced electromotive force is generated in an alternating magnetic field, causing eddy currents to form on the surface of the permanent magnet. Equations for induced electromotive force and induced electromotive force magnitude are shown below [21].

$$E_{\text{eddy}} = -\frac{\partial B_m}{\partial t} l_{\text{PM}} w_{\text{PM}}, \tag{13}$$

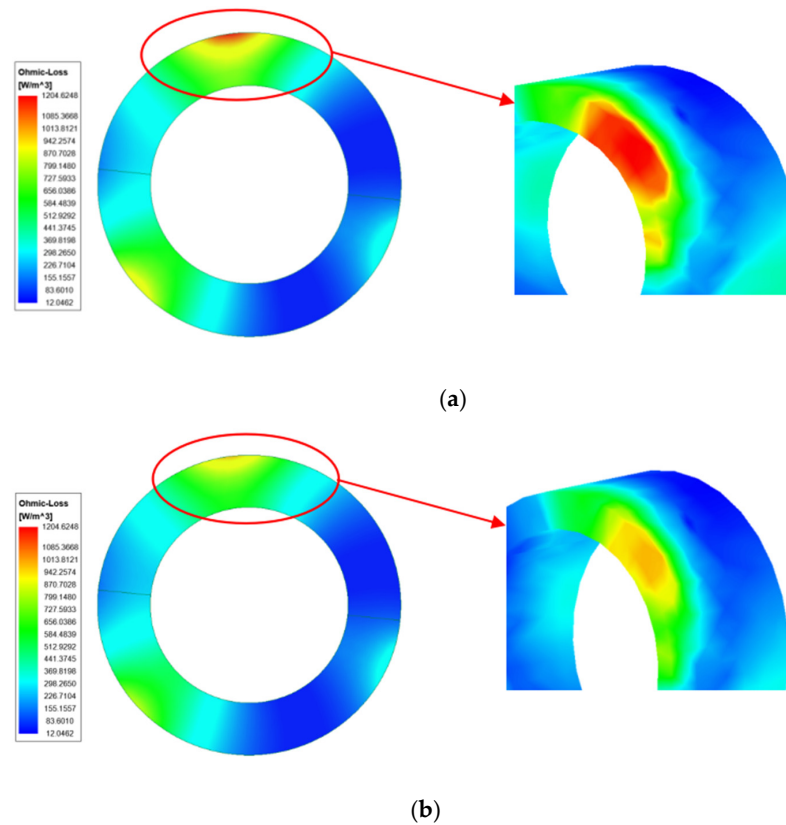
$$E = l_{\text{PM}} w_{\text{PM}} \times \sum n B_n f_n, \tag{14}$$

where  $B_m$  is the harmonic magnetic field,  $l_{\text{PM}}$  is the axial length of PM,  $w_{\text{PM}}$  is the radial length of PM,  $n$  is the number of each harmonic,  $B_n$  is the harmonic magnetic density amplitude, and  $f_n$  is the relative motion frequency. The PM eddy current loss equation is shown below [21].

$$P_{\text{PM}} = \left[ \frac{h_{\text{PM}} w_{\text{PM}}^3 l_{\text{PM}}^3 \sigma}{2(w_{\text{PM}}^2 + l_{\text{PM}}^2)} \sum \left( \frac{|i_s|}{\sqrt{3/2} I_m} \right)^2 n^2 f_n^2 B_n^2 \right] \cdot V_{\text{PM}}, \tag{15}$$

where  $h_{\text{PM}}$  is the radial length of PM,  $i_s$  is the RMS value of the excitation current,  $I_m$  is the motor input current amplitude, and  $V_{\text{PM}}$  is the volume of PM.

To analyze the effect of reactor inductance value on the rotor eddy current loss, the rotor eddy current loss is analyzed using the FEM when the series reactor inductance value is  $0 \mu\text{H}$  and  $15 \mu\text{H}$ . The rotor eddy current loss cloud diagrams for inductance values of  $0 \mu\text{H}$  and  $15 \mu\text{H}$  are shown in Figure 11.



**Figure 11.** Rotor eddy current loss at different values of inductance: (a) rotor eddy current loss at inductance value of 0  $\mu\text{H}$ ; (b) rotor eddy current loss at inductance value of 15  $\mu\text{H}$ .

Analysis of Figure 11 shows that the maximum rotor eddy current loss density is  $1204.62 \text{ W/m}^3$  when the value of reactor inductance is 0  $\mu\text{H}$ , and the maximum rotor eddy current loss density is  $942.26 \text{ W/m}^3$  when the value of reactor inductance is 15  $\mu\text{H}$ . The rotor eddy current loss of the BLDC hollow-cup motor is significantly reduced, by about 22% at the maximum loss density, with the series connection of a 15  $\mu\text{H}$  reactor.

Through the above electromagnetic analysis, it is observed that a reactor with an inductance value of 15  $\mu\text{H}$  in series between the BLDC hollow-cup motor and the controller can effectively suppress the current harmonics and the resulting armature potential harmonics. This leads to a reduction in the core loss and rotor eddy current loss generated during motor operation.

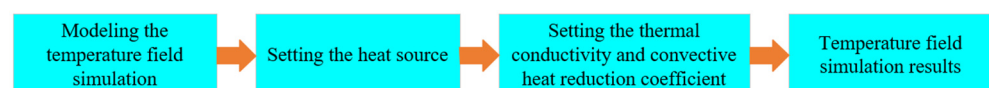
#### 4. Electromagnetic–Temperature Field Coupling Analysis

In this section, the temperature field of a BLDC hollow-cup motor is analyzed for the following two cases:

- (1) The reactor is not connected in series between the motor and the controller.
- (2) The reactor includes the inductance of 15  $\mu\text{H}$  in series between the motor and the controller.

The suppression of core losses by the reactor is verified when the motor is operated at 90 W 47,000 r/min.

The temperature field simulation steps are shown in Figure 12.



**Figure 12.** Temperature field simulation steps.

#### 4.1. Setup Heat Source

The electromagnetic losses of the motor are calculated for different values of inductance. Electromagnetic losses for a reactor inductance of 0  $\mu\text{H}$  (without a series reactor) and a reactor inductance of 15  $\mu\text{H}$  are selected as the heat sources for temperature field simulation. Due to the small size of the BLDC hollow-cup motor studied in this paper, the wind friction loss is negligible. The temperature field heat sources are shown in Table 2.

**Table 2.** Temperature field heat source.

Inductance of Reactor/ $\mu\text{H}$	Core Loss /W	Winding Loss /W	Rotor Eddy Current Loss/W
0 (without reactor)	10.64	8.64	1.49
15	8.03	4.99	0.98

#### 4.2. Thermal Conductivity and Convection Heat Dissipation Factor

The material thermal conductivity of each component of the motor used for temperature field calculations is shown in Table 3.

**Table 3.** Thermal conductivity of each component material.

Component (Material)	Density /( $\text{kg}/\text{m}^3$ )	Constant-Pressure Specific Heat Capacity/( $\text{J}/(\text{kg}\cdot\text{K})$ )	Thermal Conductivity /( $\text{W}/(\text{m}\cdot\text{K})$ )
Stator (Silicon Steel)	7650	502	40
Winding (Copper)	8987	381	387.6
Winding (Copper)	8400	504	12

The convection heat dissipation factor for the motor cooling surface is usually related to several physical quantities. To simplify the simulation calculation of the temperature field, the convection heat dissipation factor is calculated with the help of formulas and empirical constants. The convection heat dissipation factor of the inner circle of the stator and the outer circle of the rotor of the motor are affected by the rotor rotation but also by the effect of the stator inner circle surface blocking. The more common method is to use the same heat transfer coefficient for the rotor surface and the stator inner circle surface. The convection heat dissipation factor expressions [19] at the stator end face, at the rotor end face, and at the stator and rotor air gap are shown below.

$$\alpha_s = \frac{1 + 0.04v_\tau}{0.045}, \quad (16)$$

$$\alpha_r = 28 \left( 1 + \sqrt{0.45v_\tau} \right), \quad (17)$$

$$\alpha_\delta = 28 \left( 1 + \sqrt{0.5v_\tau} \right), \quad (18)$$

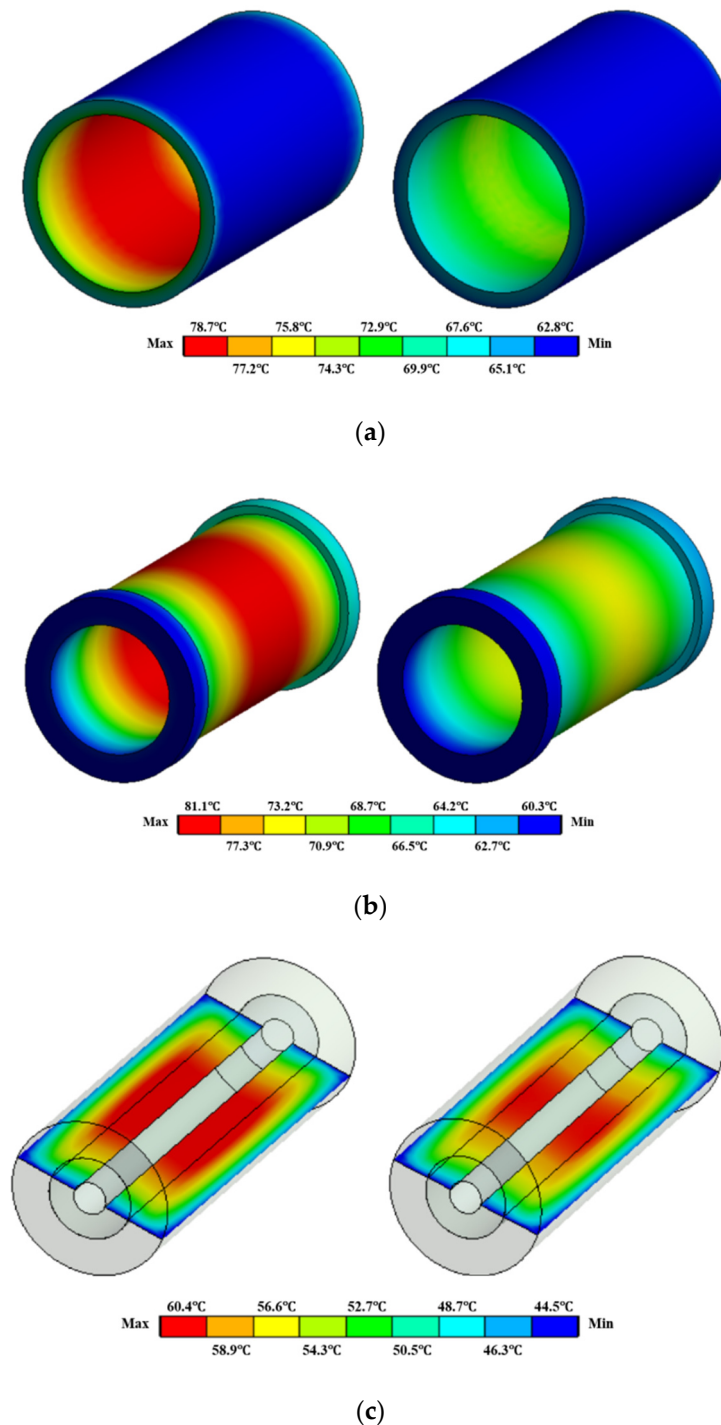
where  $v_\tau$  is the rotor surface circumferential rotation speed, with the unit m/s. The convection heat dissipation factor for each position is calculated from the above equations, as shown in Table 4.

**Table 4.** Convection heat dissipation factor of component.

Component	Convection Heat Dissipation Factor/( $\text{W}/(\text{m}^2\cdot^\circ\text{C})$ )
Stator end face	44.1
Rotor end face	121.2
Rotor surface and stator inner circle	126.2

#### 4.3. Temperature Field Simulation Results

The temperature distribution of each component of the motor is calculated using temperature field simulation, as shown in Figure 13. The temperature of various parts of the motor, before and after the series connection of a 15  $\mu\text{H}$  reactor, is shown in Table 5.



**Figure 13.** Temperature distribution of each component before and after series connection of a reactor with an inductance value of 15  $\mu\text{H}$ : (a) stator (silicon steel) before and after series connection of 15  $\mu\text{H}$  reactor; (b) stator (winding) before and after series connection of 15  $\mu\text{H}$  reactor; (c) rotor before and after series connection of 15  $\mu\text{H}$  reactor.

**Table 5.** The temperature of each component.

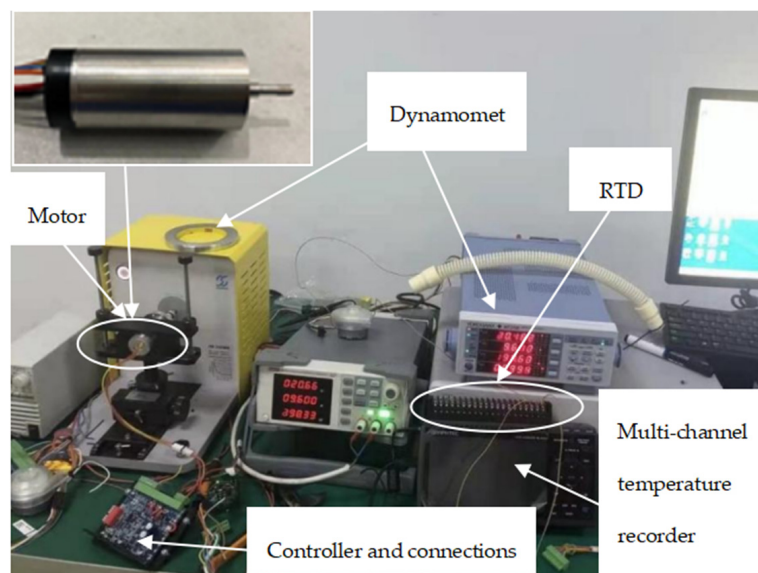
Component (Material)	$T_{\max}/^{\circ}\text{C}$ (Reactor Inductance = 0)	$T_{\max}/^{\circ}\text{C}$ (Reactor Inductance = 15 $\mu\text{H}$ )	Temperature Difference/ $^{\circ}\text{C}$
Stator (Silicon Steel)	78.7	72.9	−5.8
Winding (Copper)	81.1	73.2	−7.9
Rotor	60.4	54.3	−6.1

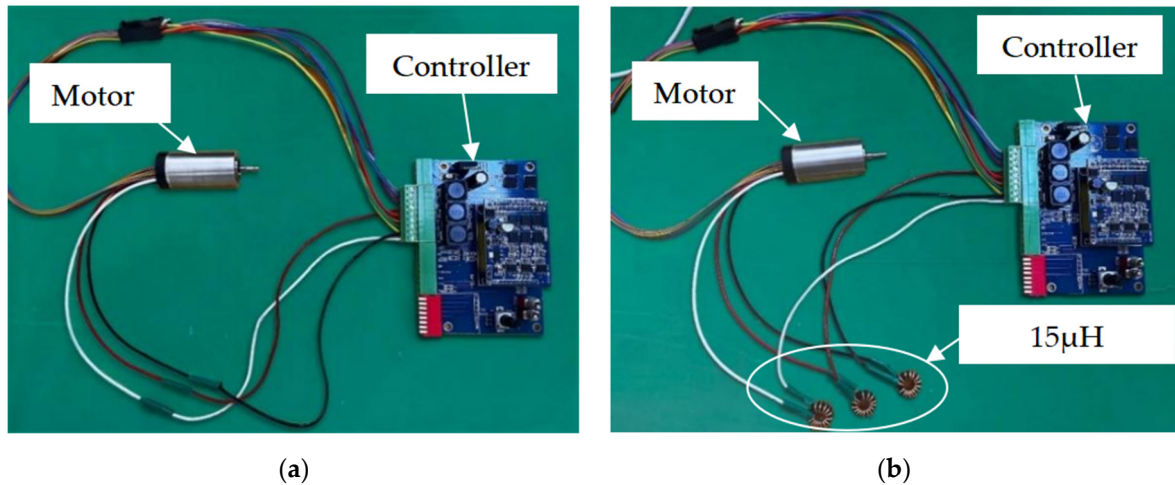
In summary, the maximum temperatures of the stator silicon steel, stator winding, and rotor decreased by 5.8 °C, 7.9 °C, and 6.1 °C, respectively, when the motor was operated with a 15  $\mu\text{H}$  reactor in series with the controller. From the temperature field simulation results, it is shown that when the 15  $\mu\text{H}$  reactor is connected in series between the motor and the controller, temperature increase is effectively reduced.

## 5. Experiments and Comparative Analysis

To verify the suppression effect of the reactor on the electromagnetic losses of the BLDC hollow-cup motor, based on the theoretical analysis and FE calculation in the previous section, an experimental platform is built to test the efficiency and temperature rise of the motor at the rated load.

Load experiments are carried out in two cases, without a reactor in series between the motor and the controller and with a reactor of 15  $\mu\text{H}$  in series, to verify the correctness and accuracy of the FE. The experimental platform with the BLDC hollow-cup motor is shown in Figure 14. The equipment includes a BLDC hollow-cup motor, reactors, a controller, a WT310 dynamometer, a PT100 sensor, and a QG6003S power supply. A comparison of the setup before and after adding the series reactor to the motor system is shown in Figure 15.

**Figure 14.** The experimental platform.



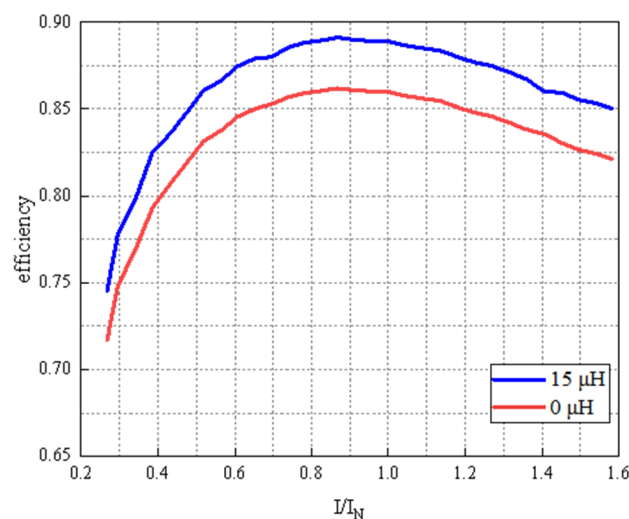
**Figure 15.** Comparison of the setup before and after adding a series reactor to the motor system: (a) before adding the system series reactor; (b) after adding the system series reactor.

5.1. Efficiency Test Experiment

In this section, the motor efficiency is measured and calculated for the motor with no series reactor between the motor and the controller and with a 15 µH reactor in series. The results are compared and analyzed to verify the reasonableness of the optimization method.

Measurements of electromagnetic torque ( $T$ ), input voltage ( $U$ ), and input current ( $I$ ) at different rotational speeds ( $n$ ) are recorded, and the efficiencies are calculated using a WT310 dynamometer. Efficiency calculations are carried out based on the MTPA (maximum torque per ampere) control method to measure the motor’s [22] success in achieving maximum torque output with minimum stator current for a given load condition. See Tables A1 and A2 of results. The efficiency is calculated using Equation (19), and the comparison of efficiency is shown in Figure 16.

$$\eta = \frac{P_2}{P_1} = \left( \frac{T \times n}{9.55} \right) / (U \times I). \tag{19}$$



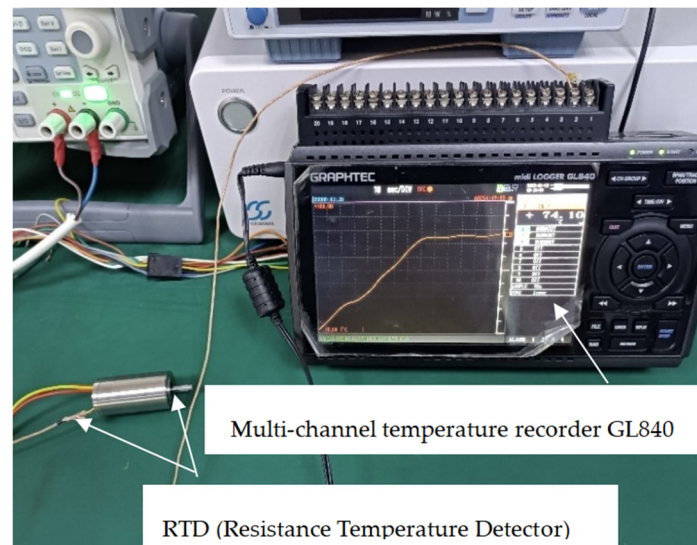
**Figure 16.** Comparison of efficiency.

The measured values of motor efficiency are analyzed, and under two conditions with the same input power, the motor efficiency with the 15 µH reactor in series has a significant upward trend compared to that without the reactor in series. When the input current is

the rated current of the motor, the efficiency of the motor with the 15  $\mu\text{H}$  reactor in series is about 3.77% higher than the efficiency of the motor without the reactor in series. This measurement shows that the motor losses are significantly reduced when the 15  $\mu\text{H}$  reactor is connected in series, which is consistent with the FE simulation results.

### 5.2. Temperature Rise Experiment

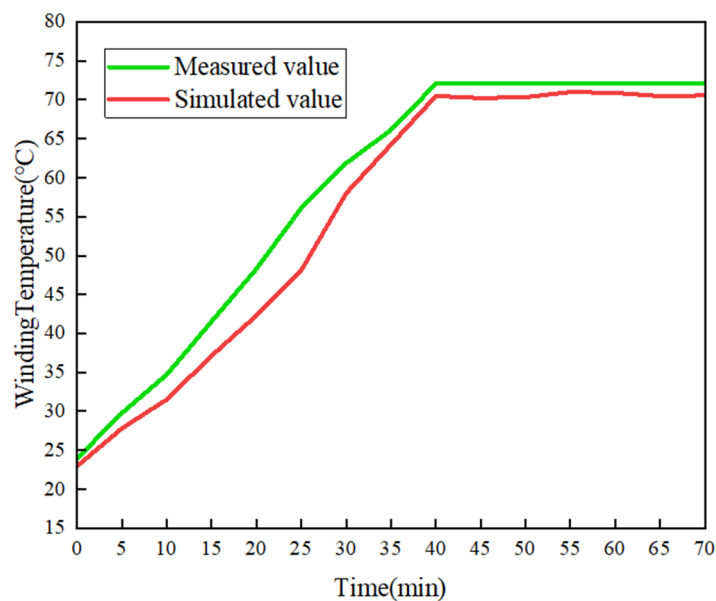
After completing the actual measurement of the efficiency of the BLDC hollow-cup motor, the temperature rise of the winding at 15  $\mu\text{H}$  in series is measured. The measured results are compared with the simulated results. The wiring of the PT100 and the motor are shown in Figure 17.



**Figure 17.** Wiring of PT100 and motor.

The comparison between the measured and simulated results of the winding temperature rise of the BLDC hollow-cup motor with the 15  $\mu\text{H}$  reactor in series is shown in Figure 18. When the motor runs to a stable state, the winding is measured to be 74.9  $^{\circ}\text{C}$ , while the FE temperature rise calculation of the motor winding is 73.2  $^{\circ}\text{C}$ , which is a difference of 2.3%. This result shows that the difference between the simulated and measured results is within acceptable limits. It can be determined that the winding temperature is reduced by approximately 11% when the 15  $\mu\text{H}$  reactor is connected in series. The above experimental results verify that the temperature rise suppression effect of series reactors on a BLDC hollow-cup motor is in accordance with the results of the previous theoretical analysis.

The reason for the deviation in the finite element calculation results from the measured results is that the temperature and humidity in the laboratory where the measurements are made are not constant. However, the initial temperature is kept constant at 25  $^{\circ}\text{C}$  in the finite element calculation, which will change the heat transfer conditions of the motor. Moreover, the mesh density during finite element calculation is not well homogenized in the complex region of the model. The above conditions cause the deviation in the theoretical compared to the measured temperature rise.



**Figure 18.** Comparison between measured and simulated results.

## 6. Conclusions

In this paper, electromagnetic loss optimization and temperature field coupling analysis are carried out for a 90 W 47,000 r/min BLDC hollow-cup motor applied in a UAV drive system. This paper focuses on the influence of different values of series reactors on motor losses and line voltage. Furthermore, the magnetic–thermal coupling simulation is adopted to compare the performance of the improved design with the original design. Finally, the simulation results are verified by the experiments of the prototype. The following conclusions were drawn.

With the increase in inductance in the BLDC hollow-cup motor system, the iron core loss is effectively reduced. However, if the inductance value exceeds a certain limit (15  $\mu\text{H}$ , in this article), the RMS of the motor load line voltage can be suppressed, and the output efficiency of the motor controller can also be correspondingly suppressed.

This paper adopts an optimization method to determine which reactors will minimize the motor loss. By parameterizing the inductance value, the reactors can be investigated according to their impact on motor core losses, rotor eddy current losses, and controller efficiency. A clear reference for the research and optimization analysis of motor loss reduction is provided.

Using FEA and experimental verification, it is concluded that a reactor with an inductance value of 15  $\mu\text{H}$  can increase motor efficiency by 3.77% and reduce temperature rise by 9.7%, without affecting the output voltage of the controller.

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**Conflicts of Interest:** The authors declare no conflicts of interest.

## Appendix A

**Table A1.** Calculated motor efficiency (no reactor is connected).

$I_1/I_n$	DC Current $I_1/A$	DC Voltage $U_1/V$	Input $P_1/W$	Speed $n/r/min$	Torque $T/N\cdot m$	Output $P_2/W$	Effi. $\eta/\%$
0.30	1.8	23.673	30.89	50,489	0.004012	21.69	74.69
0.39	1.59	23.567	40.12	49,833	0.006389	29.89	79.66
0.52	2.18	23.712	53.41	49,003	0.007689	43.57	83.14
0.61	2.549	23.489	62.33	48,713	0.010059	51.84	84.67
0.70	3.106	23.901	71.89	48,398	0.013008	59.19	85.13
0.85	3.698	23.478	89.71	47,280	0.014999	76.67	86.33
0.91	3.745	23.633	93.67	47,113	0.015976	79.46	85.79
1.00	4.283	23.678	103.45	46,398	0.018630	88.15	85.67
1.09	4.396	23.789	111.03	46,289	0.021113	94.37	85.43
1.22	5.199	23.569	124.84	45,031	0.021986	105.89	84.8
1.31	5.713	23.496	132.78	44,811	0.024663	111.46	83.09
1.41	5.998	23.465	143.59	44,702	0.026789	119.03	82.99
1.50	6.66	23.39	151.72	43,695	0.027133	124.82	82.17
1.58	6.91	23.296	160.13	43,338	0.029386	131.74	81.99

**Table A2.** Calculated motor efficiency (15  $\mu$ H reactor is connected).

$I_1/I_n$	DC Current $I_1/A$	DC Voltage $U_1/V$	Input $P_1/W$	Speed $n/r/min$	Torque $T/N\cdot m$	Output $P_2/W$	Effi. $\eta/\%$
0.30	1.27	22.866	30.30	50,407	0.004463	23.56	77.75
0.39	1.66	22.823	39.48	49,907	0.006232	32.57	82.50
0.52	2.23	22.759	52.99	49,161	0.008859	45.61	86.07
0.61	2.61	22.717	61.88	48,696	0.010614	54.13	87.47
0.70	3.00	22.673	70.93	48,228	0.012359	62.42	88.00
0.85	3.735	22.59	88.09	47,300	0.015849	78.51	89.12
0.91	3.93	22.568	92.55	47,088	0.016701	82.35	88.98
1.00	4.30	22.527	101.12	46,594	0.018424	89.89	88.90
1.09	4.68	22.483	109.96	46,124	0.02015	97.33	88.51
1.22	5.26	22.418	123.14	45,381	0.022727	108.01	87.71
1.31	5.64	22.375	131.83	44,924	0.024424	114.90	87.16
1.41	6.06	22.327	141.33	44,419	0.026124	121.52	85.98
1.50	6.43	22.284	149.70	43,959	0.027821	128.07	85.55
1.58	6.80	22.240	158.06	43,504	0.029504	134.41	85.04

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