



Article Optimal Design and Dynamic Characteristic Analysis of Double-Link Trapezoidal Suspension for 3WPYZ High Gap Self-Propelled Sprayer

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Abstract: A fast spraying speed, wide working area, and easy operation are the operational advantages of high-clearance boom sprayers. To address the issue of spray boom mechanical vibration affecting the spraying effect, a double-link trapezoidal boom suspension is designed for the 3WPYZ sprayer. This suspension can achieve passive vibration reduction, active balance, and ground profiling. The kinematic model of the boom suspension is established based on D'Alembert's principle and the principle of multi-body dynamics, and the design factors affecting the stability of the boom are determined. Through orthogonal experimental design and virtual kinematics simulation, the influence of the boom length and orifice diameter of each part on the swing angle and the natural frequency of the boom suspension is investigated. Design-Expert 8.0.6 software is used to analyze and optimize the test results. The optimization results show that, when the connecting boom length L_{AB} is 265 mm, the inner boom suspension boom length L_{AD} is 840 mm, the outer boom suspension boom length L_{BC} is 1250 mm, and the throttle hole diameter d is 4 mm; the maximum swing angle of the boom suspension is reduced by 53.02%. In addition, the natural frequency of the boom is reduced from 1.3143 rad/s to 1.1826 rad/s, and the dynamic characteristic optimization effect is remarkable. The modal analysis results show that the first sixth-order vibration test frequency of the boom sprayer suspension designed in this paper meets the requirements and avoids the influence of external factors. Field tests show that, when the sprayer is excited by the environment at 3.5° to 4° , the boom suspension can reduce the vibration transmitted by the body to a reasonable range. The static analysis shows that the structural design of this study reduces the stress at the connection of the end boom suspension, the maximum displacement, and the maximum stress of the inner boom suspension. The test results of the dynamic characteristics of the implement are basically consistent with the virtual model simulation test results, thus achieving the optimization objectives.

Keywords: high gap sprayer; boom suspension; double-link trapezoidal structure; dynamic characteristics; modal analysis

1. Introduction

A wide range of application, high operation efficiency, and low environmental impact are the characteristics of a high gap self-propelled sprayer, which has become the most widely used model in plant protection spraying machinery [1–5]. Due to the wide working width of the high gap self-propelled sprayer and the complex application environment,



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Copyright: © 2024 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). the sprayer may encounter the influence of unstable factors, such as ground undulations, during the operation of the sprayer, so that the spray rod is subject to the swing transmitted by the body and produces deflection or shaking of different frequencies [6–8]. The boom suspension system is an important part of a high gap self-propelled sprayer, capable of transferring or reducing forces and moments between the sprayer body and the boom [9–11]. In addition, it can reduce the probability of undesirable motion and improve the spray stability of the spray rod during sprayer operation. Based on the above research background, many studies have been carried out on the dynamic characteristics of sprayer suspension in order to achieve a better drug spraying effect [12,13].

Because the sprayer suspension can achieve an excellent vibration damping effect compared with other components when only considering the selection of materials and the design of the structure, many scholars have begun to carry out a series of studies on the structural form and dynamic performance of the sprayer suspension. Through years of research and development, the current structural form of boom suspension is mainly divided into two categories: pendulum-type and double-link trapezoidal structures. O'Sullivan et al. [14] proposed a dynamic model of a double pendulum passive suspension and analyzed its amplitude frequency and phase frequency characteristics. The analysis results show that the double pendulum boom passive suspension can effectively isolate the vibration, which verifies the correctness of the model. Nation et al. [15] established a mathematical analysis model of symmetrical shaft boom passive suspension, and verified the rationality of the model by analyzing the optimal combination of springs and dampers for the passive suspension. Frost [16] improved the design of the two-link trapezoidal boom suspension. His team set one side linkage as an active control hydraulic cylinder, added active suspension to the boom suspension system, and built a dynamic model of the improved boom suspension. Qiu et al. [17,18] designed a motion response method for the front wheel of the sprayer, and the correlation coefficient between the predicted value and the actual value reached 0.9551. Wu et al. [19] analyzed the dynamic characteristics of the boom suspension under different excitations, and the results showed that adding damping to the system could effectively optimize the vibration isolation performance of the boom suspension. Cui et al. [20,21] used the Second Lagrangian Equation to establish a dynamic model of the boom suspension and simulated the dynamic characteristics of the boom suspension.

Although a certain vibration reduction effect can be achieved through the above research methods, when the wide sprayer above 20 m is working in the field at a high speed, the spray bar suspension will still be affected by the body swing and terrain changes, producing undesirable movements which will cause unnecessary effects on the spraying effect. This is due to the slow speed of the field pesticide application and the potholes on the driving road, which puts forward high requirements for the stability and smoothness of the spray rod of the whole vehicle, especially the sprayer with a spray rod length of more than 20 m [22]. In addition to testing the dynamic characteristics of the sprayer, it is also necessary to test and explore the damage of the suspension structure caused by long-term use in the harsh environment of farmland, so it is necessary to carry out load analysis on the bearing capacity of the suspension [18].

It can be seen that, under the premise of comprehensively considering the structural layout of the sprayer, it is necessary to optimize the design of a double-link trapezoidal boom suspension that can achieve passive vibration damping, active balance, and ground profiling in order to reduce the probability of undesired motion and improve the stability of spraying. In this study, the kinematic model of the boom suspension is established by analyzing the existing problems in the high-clearance boom sprayer, and the inadequacy of the existing optimization design schemes, using the D'Alembert principle and the multibody dynamics principle. The rationality of the simulation optimization is verified by combining dynamic characteristics and static simulation with experimental verification.

2. Materials and Methods

2.1. Design Requirements and Working Principle

The suspension isolates vibrations and the boom suspension should be able to achieve the function of active balance and ground profiling through its own structural characteristics and external damping, so as to ensure the stability of spraying operations. In order to meet the spraying requirements of different crops in different periods, the height of the boom suspension needs to be adjusted in a large range to achieve the best spray height. In order to meet the needs of frame stiffness and strength during operation, and ensure that each component does not suffer fatigue failure, the natural frequency of the suspension should be dispersed and not coincide with the external excitation frequency to avoid resonance. If the above conditions are met, the sprayer suspension designed in this paper can meet the requirements of plant protection spraying operation.

The operating principle of the boom suspension to isolate vibrations, active balancing, and ground profiling is shown in Figure 1.

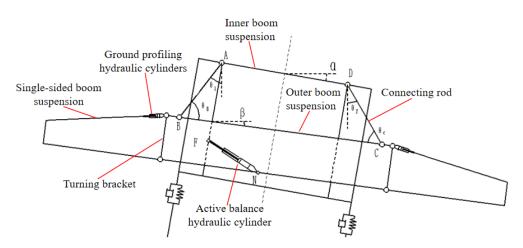


Figure 1. Schematic diagram of the working principle of the boom suspension.

(1) The ability of the suspension to isolate vibrations:

The inner boom suspension transmits vibrations to the outer boom suspension and the single-side boom suspension, when the sprayer operation is affected by environmental factors and produces undesirable motion. This process causes the outer boom suspension to produce an unfavorable relative displacement with the inner boom suspension. The active balance hydraulic cylinder designed in this paper hinders the vibration that the inner boom suspension transmits by the damping that the damping aperture produces through the damping hole, and achieves the effect of isolating the vibration.

(2) The ability of the suspension to active balancing and ground profiling:

When the spray bar suspension is used as an active suspension, it controls the expansion and contraction of the active balancing hydraulic cylinder and simultaneously controls the movement of the outer boom suspension. The outer boom suspension realizes the active balance of the boom suspension by driving the single-side boom suspension to move.

(3) The ability of the suspension folds and deploys:

The lifting hydraulic cylinder controls the expansion and contraction of the piston rod to achieve the purpose of adjusting the suspension height of the overall boom. By lifting hydraulic cylinder, ground profiling hydraulic cylinder and folding hydraulic cylinder work together to realize folding and unfolding integral boom suspension. 2.2.1. Mathematical Model of the Boom Suspension

Based on D'Alembert's principle and the principle of multi-body kinematics, the mathematical model of the boom suspension is constructed, and the following reasonable assumptions are made:

- (1) In this modeling, the boom suspension is treated as a rigid beam on the vertical plane, without considering the elastic deformation.
- (2) It is assumed that the integral boom suspension is well lubricated throughout, and the effect of frictional damping is not considered.
- (3) The mass of the individual connecting members is not considered.
- (4) Assuming that the ground inclination change is equal to the body inclination change, the vibration damping effect of the sprayer chassis suspension and tires is ignored.

Based on the above assumptions, the force analysis of the boom suspension is shown in Figure 2.

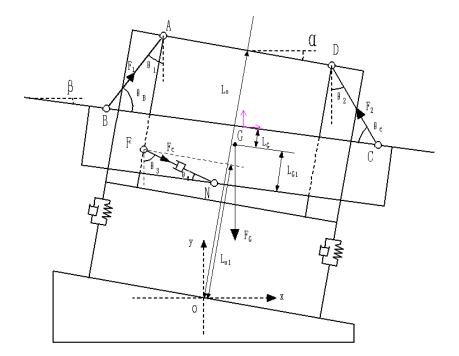


Figure 2. Force analysis diagram of boom suspension.

As shown in Figure 2, the hinge points on the inner and outer boom suspension are A, B, C, D four points, and the outer boom suspension is connected to the inner boom suspension by connecting rods AB and CD. The center of gravity of the outer boom suspension and the boom suspension on both sides is G, and the equivalent damping composed of the hydraulic cylinder and the throttle hole is hinged between the inner and outer boom suspension, and the handover points are F and N. To simplify the mathematical model, it is assumed that the sprayer fuselage rotates around a fixed axis parallel to the direction of the locomotive and through point O. The mathematical model is as follows:

$$\begin{cases} x = -\frac{L_{AD}}{2}\cos\alpha + L_{0}\sin\alpha - L_{AB}\sin\theta_{1} + \frac{L_{BC}}{2}\cos\beta - L_{G}\sin\beta \\ x = \frac{L_{AD}}{2}\cos\alpha + L_{0}\sin\alpha - L_{CD}\sin\theta_{2} - \frac{L_{BC}}{2}\cos\beta - L_{G}\sin\beta \end{cases}$$
(1)

$$\begin{cases} y = L_0 \cos \alpha + \frac{L_{AD}}{2} \sin \alpha - L_{AB} \cos \theta_1 - \frac{L_{BC}}{2} \sin \beta - L_G \cos \beta \\ y = L_0 \cos \alpha - \frac{L_{AD}}{2} \sin \alpha - L_{CD} \cos \theta_1 + \frac{L_{BC}}{2} \sin \beta - L_G \cos \beta \end{cases}$$
(2)

where L_{AD} is the length of suspension rod AD (m); L_{AB} is the length of suspension rod AB (m); L_{BC} is the length of suspension rod BC (m); L_{CD} is the length of suspension rod CD

(m); L_O is the length of the suspension to the center of gravity; α is the angle of inclination of the body (rad); β is the angle of inclination of the boom (rad); and L_G is the length of the rod BC to the center of gravity.

The initial values of the angle θ_1 , θ_2 between the connecting rod AB, CD, and the vertical direction is

$$\overline{\theta} = \sin^{-1} \left(\frac{L_{BC} - L_{AD}}{L_{AB} + L_{CD}} \right) \tag{3}$$

Due to the α , the β change values are small; then, there are the following:

$$\begin{cases} \sin \alpha = \alpha, \ \sin \beta = \beta\\ \cos \alpha = 1 - \frac{\alpha^2}{2}, \ \cos \beta = 1 - \frac{\beta^2}{2}\\ \sin \theta_1 = \sin \overline{\theta} + \Delta \theta_1 cos \overline{\theta}\\ \cos \theta_1 = \cos \overline{\theta} - \Delta \theta_1 \sin \overline{\theta}\\ \sin \theta_2 = \sin \overline{\theta} + \Delta \theta_2 \cos \overline{\theta}\\ \cos \theta_2 = \cos \overline{\theta} - \Delta \theta_2 \sin \overline{\theta} \end{cases}$$
(4)

With the simultaneous (1)–(4) derivation, and ignoring the second-order small quantity, the center of gravity *G* coordinates are obtained:

$$\dot{x} = \left(L_0 + \frac{\cos\overline{\theta}}{2\sin\overline{\theta}}L_{AD}\right)\dot{\alpha} - \left(\frac{\cos\overline{\theta}}{2\sin\overline{\theta}}L_{BC} + L_G\right)\dot{\beta}$$
(5)

$$\ddot{x} = \left(L_0 + \frac{\cos\overline{\theta}}{2\sin\overline{\theta}}L_{AD}\right)\ddot{\alpha} - \left(\frac{\cos\overline{\theta}}{2\sin\overline{\theta}}L_{BC} + L_G\right)\ddot{\beta}$$
(6)

 $\dot{y} = 0 \tag{7}$

$$=0$$
 (8)

According to the coordinates (x_F , y_F) and (x_N , y_N) of the connection points F and N of the equivalent damper [20], the damping force of the equivalent damper can be obtained as follows:

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$$F_{c} = \frac{8L_{FN}^{2}A^{3}\rho}{C_{d}^{2}\pi^{2}d^{4}}$$
(9)

where L_{FN} is the speed of change in damping (m·s⁻¹); *A* is the effective working area of hydraulic cylinders (m²); ρ is the oil density (kg·m⁻³); C_d is the flow coefficient; and *d* is the throttle diameter (m).

$$\begin{cases}
M_B \ddot{x} = F_1 \sin \theta_1 - F_2 \sin \theta_2 + F_C \sin \theta_3 \\
M_B \ddot{y} = F_1 \cos \theta_1 - F_2 \cos \theta_2 - F_C \sin \theta_3 - M_B g \\
I_B \ddot{\beta} = F_1 \left(L_G \cos \theta_B + \frac{L_{BC}}{2} \sin \theta_B \right) - F_2 \left(L_G \cos \theta_c + \frac{L_{BC}}{2} \sin \theta_c \right) \\
-F_C L_{G1} \cos \theta_N
\end{cases}$$
(10)

According to the planar D'Alembert's principle, the following is obtained:

where F_1 is the force experienced by the connecting rod AB (N); F_2 is the force experienced by the connecting rod CD (N); M_B is the sum of the masses of the outer boom suspension and the boom suspension on both sides (kg); and θ_B , θ_C is the angle between the connecting rod AB, CD, and the outer boom suspension (rad).

$$\begin{cases} \theta_B = \frac{\pi}{2} - \theta_1 + \beta \\ \theta_C = \frac{\pi}{2} - \theta_2 + \beta \end{cases}$$
(11)

By combining Equations (3)–(11), the following mathematical formulas are obtained:

$$\begin{cases} F_1 = \frac{M_B g \sin \theta_2 + \cos \theta_2 M_B \ddot{x} - F_C(\sin \theta_3 \cos \theta_2 - \cos \theta_3 \sin \theta_2)}{\cos \theta_1 \sin \theta_2 + \sin \theta_1 \cos \theta_2} \\ F_2 = \frac{M_B g \sin \theta_1 - \cos \theta_1 M_B \ddot{x} + F_C(\sin \theta_1 \cos \theta_3 + \cos \theta_1 \sin \theta_3)}{\cos \theta_2 \sin \theta_1 + \sin \theta_2 \cos \theta_1} \end{cases}$$
(12)

From the above analysis, it can be seen that the quality of the boom suspension is only related to the mechanism design and suspension material, so M_B is a constant parameter and is not considered as a relevant variable. And the influence of θ_1 on F_c is very small, so θ_1 is set as a fixed value, and its influence on the inclination angle of the boom suspension is not considered. Therefore, there are four main influencing factors affecting the inclination angle of the boom suspension, namely, the length of the rod member L_{AD} of the inner boom suspension, the length of the rod on the outer boom suspension L_{BC} , the length of the connecting rod L_{AB} , and the diameter of the throttle diameter d.

$$f = \begin{bmatrix} L_{AD} & L_{BC} & L_{AB} & d \end{bmatrix}^{\mathrm{T}}$$
(13)

Influencing factor *f* can be expressed as follows:

2.2.2. Optimize the Establishment of Mathematical Model

In order to meet the design criteria of the boom suspension, the maximum sinusoidal excitation of 10 rad/s is used as the environmental excitation of the fuselage. The spray bar suspension is designed with 0~10 rad/s as the fuselage excitation, so the objective function is the minimum value of the inclination angle, then the objective function is as follows:

$$F(f) = \min(\beta) \tag{14}$$

In this study, the natural frequency of the boom suspension is set to $0.7 \sim 1.3$ rad/s with reference to the method of designing the boom suspension by Chen et al. [23]. And in order to ensure a great follow-up performance of the low-frequency environmental excitation of the boom suspension and isolation performance of the high-frequency environmental excitation, the natural frequency w_n of the boom suspension can be set to

$$\omega_n \in (0.7 \sim 1.3) \tag{15}$$

In order to ensure that the service life of the boom suspension after optimization meets the requirements, the boom suspension should meet the following requirements:

$$r \le [\sigma]$$
 (16)

where σ is the maximum stress of the boom suspension (KPa); [σ] is the allowable stress of the boom suspension (KPa).

In summary, the final optimized mathematical model of the boom suspension can be expressed as follows:

$$\begin{cases} \min(\beta) = f(L_{AD} \ L_{BC} \ L_{AB} \ d) \\ \omega_n \in (0.7 \sim 1.3) \\ \sigma \le [\sigma] \end{cases}$$
(17)

2.2.3. Construction of 3D Model of Boom Suspension

In this study, a 3D model of the two-link trapezoidal boom suspension of the 3WPYZ sprayer is constructed based on SolidWorks

The main structural parameters and the cross-sectional shape and wall thickness of each component of the boom suspension are shown in Tables 1 and 2.

Parameters	Values	Units
L_{AB}	270	mm
L_{BC}	1180	mm
L _{BC} L _{CD}	270	mm
L_{AD}	860	mm
L_G	314	mm
$rac{L_G}{ar{ heta}}$	0.63	rad
I_B	$9.89 imes 10^9$	kg∙mm ²
M_B	530.87	kg
d	4	mm

Table 1. Main structural parameters of the two-link trapezoidal boom suspension.

Table 2. The section shape and wall thickness of each component of the boom suspension.

Main Components	Section Shape	Section Shape Size (mm)	Wall Thickness (mm)
Inner boom suspension		60×40	5
Outer boom suspension		60 imes 40	5
Turning brackets		100×80	4
First stage of boom suspension		60×40	3
Second stage of boom suspension		60 imes 40	2
End stage of boom suspension		20×20	2

The constraints between the assemblies are completed according to the position relationship and motion relationship required by the design.

Most of the boom suspension is designed with a thin-walled beam structure, and its main material is Q235. In the design process, the outer boom suspension is required to isolate the vibration transmitted by the inner boom suspension, and the boom suspension and the rotating bracket on both sides should complete the deployment and folding functions of each section in the work. Cylindrical connections are used between each section of the boom and between the boom and the hydraulic cylinder; a 3D model of the two-link trapezoidal boom suspension is shown in Figure 3.

2.3. Dynamic Characterization Simulation Test Process Based on ADAMS

In this study, ADAMS 2020 (Automatic Dynamic Analysis of Mechanical Systems) software is used to simulate the influence of environmental factors on the actual working process of the boom suspension, which provides a basis for the optimization of the boom suspension. After the drawing file is imported into the ADAMS file, the base system of the units is set to MMKS and the acceleration of gravity in the X-axis direction is set to 9.8 m/s². The mass density of each component material is set to steel (the value is $7.801 \times 10^6 \text{ kg/mm}^3$, the Young's modulus of elasticity is set to $2.07 \times 10^3 \text{ N/mm}^2$, and the Poisson's ratio is set to 0.29. The virtual prototype model is obtained by adding constraints, drives, and element forces to the virtual prototype, as shown in Figure 4.

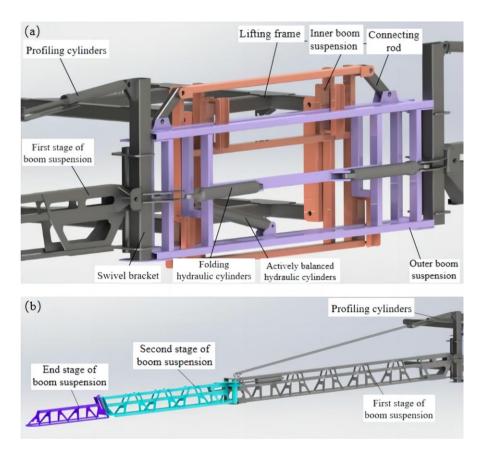


Figure 3. A 3D model of the two-link trapezoidal boom suspension. (**a**) Middle boom suspension; (**b**) single-sided boom suspension.

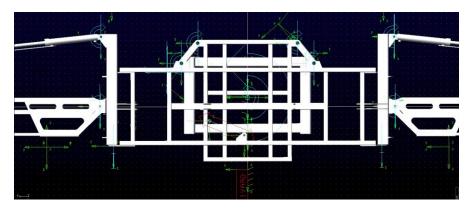


Figure 4. The virtual prototype of boom suspension based on ADAMS.

2.4. Static Analysis Simulation Test Process Based on Ansys

A 3D model of the two-link trapezoidal suspension is imported into Ansys Workbench 14.0 software and the coordinates are maintained in a directionally consistent manner. The overall structural material of the boom suspension is set to Q235. The material of the hydraulic cylinder is set to 45#. As shown in Figure 5, the automated method was chosen for model meshing. In total, 545,238 nodes and 341,139 elements were obtained after the automatic meshing process. When the grid was 300,000 to 500,000, the data varied considerably. But when the mesh count was 500,000 to 800,000, the data difference was less than 5%. Therefore, a number of grids of 500,000 was chosen in this article. The grid was tested for independence.

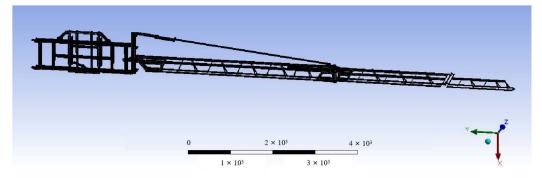


Figure 5. Construction and geometrical dimensions of specimens.

2.5. Field Dynamic Characteristic Test Process

In order to verify the operation performance of the optimized design of the boom suspension and the reliability of various parameters, combined with theoretical analysis and simulation, a WT901C485 angle sensor, produced by Shenzhen Witt Intelligent Technology Co. Ltd., was installed on the boom suspension to measure the dynamic characteristics of the boom suspension under working conditions (Figure 6), and the 3WPYZ self-propelled sprayer was used as the carrier for field experiments. The angle sensor measures acceleration with an accuracy of 0.01 g and an angular velocity of 0.05 rad/s.

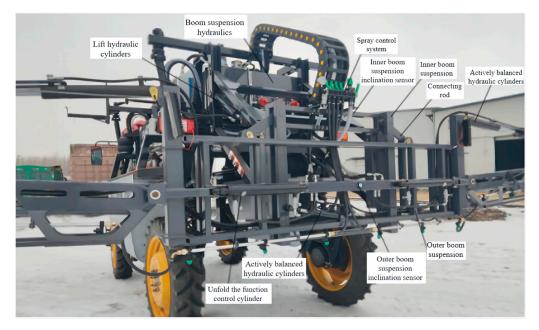


Figure 6. The dynamic characteristics test of 3WPYZ high gap self-propelled sprayer boom suspension.

The test section was set to a 125 m field section, and since the speed of the vehicle cannot be fully controlled during field operations, in order to reduce the error value, a 50 m starting road section was set, and the sensor was used to start sampling data after the speed was stable. According to the sprayer's manual, the sprayer's driving speed was set to 10 km/h for testing, and combined with the agricultural requirements of corn field operations; the ground clearance of the boom suspension was changed to 500 mm, 1200 mm, and 2500 mm. The inclination angle sensor installed on the boom suspension and the single-sided boom suspension installed in the high gap self-propelled sprayer were used to test and record the angle change in the suspension during the movement 3 times.

3. Results and Discussion

3.1. Dynamic Simulation Results and Analysis

3.1.1. Step Excitation Response Analysis

Since the step signal has the most obvious effect on the excitation of the system, the drive was first set as the step excitation signal to test the response of the boom suspension. The simulation time was set to 15 s, the simulation step was set to 500, and the driver function was set to STEP(time, 0, 0, 0.01, 1) * 5d. The diameter of the orifice d of the equivalent damper was set to five parameters for the simulation test, and 2.5° and 5° were input as amplitudes, as shown in Figure 7.

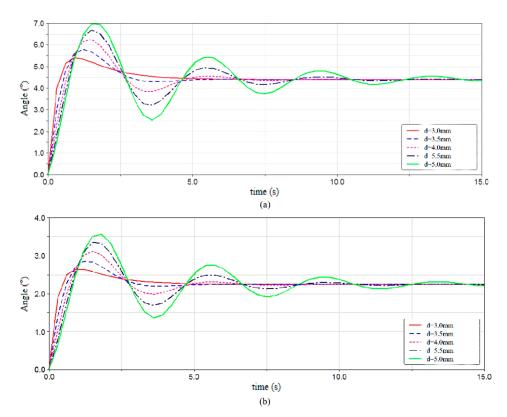


Figure 7. Time domain response diagram of boom suspension. (a) The excitation amplitude is 5° ; (b) the excitation amplitude is 25° .

As can be seen from Figure 7, the change in the equivalent damping force of the system has a great influence on the vibration of the boom suspension. When the diameter of the orifice d was increased, the damping force of the system was reduced, the peak step response of the boom suspension became larger, and the number of oscillations increased. When the diameter of the orifice d was smaller, that is, the system damping force was larger, the boom suspension was smoothed out faster and the response speed of the boom suspension was faster.

3.1.2. Sinusoidal Excitation Response Analysis

The drive was set to a sinusoidal excitation $y = A\sin\omega t$, where w is the angular frequency, A is the amplitude, and t is the time. In this study, the amplitude A was set to 5° and the angular frequency was changed to obtain the dynamic characteristics of the boom suspension at w = 0.1 rad/s, 0.5 rad/s, 5 rad/s, and 10 rad/s, as shown in Figure 8.

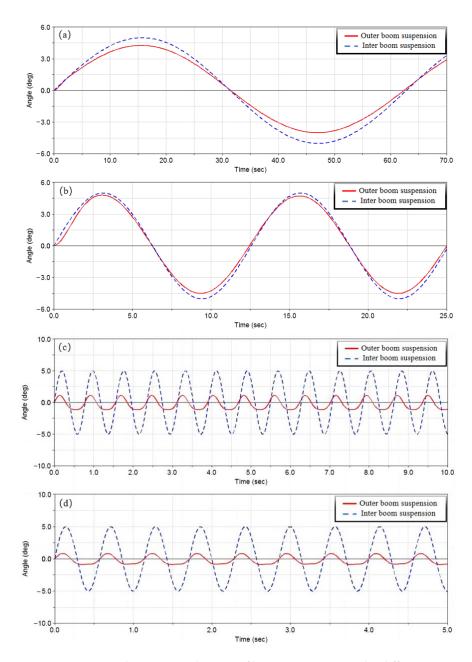


Figure 8. Dynamic characteristic diagram of boom suspension under different excitation frequencies. (a) $\omega = 0.1 \text{ rad/s}$; (b) $\omega = 0.5 \text{ rad/s}$; (c) $\omega = 5 \text{ rad/s}$; and (d) $\omega = 10 \text{ rad/s}$.

It can be seen from Figure 8 that the inner nozzle suspension was stimulated by the external low-frequency sinusoidal excitation w = 0.1 rad/s; this was w = 0.5 rad/s for sinusoidal motion and the outer boom suspension followed the inner boom suspension. When w = 10 rad/s, the maximum swing angle of the inner boom suspension was 5° , and the maximum value of the outer boom suspension was 0.877° . The spray bar suspension designed this time can follow the movement of the body when encountering low-frequency excitation and isolate the vibration transmitted by the body when encountering high-frequency excitation, but the isolation effect needs to be further improved.

3.1.3. Virtual Trials of Boom Suspensions

In order to optimize the isolation effect of the boom suspension when the locomotive encounters high-frequency excitation, ADAMS is used to perform the single factor tests of L_{AD} , L_{BC} , L_{AB} , and orifice diameter d. By changing the single influencing factor, the influence

of each influencing factor on the maximum oscillation degree and natural frequency was obtained, and the existence range of the optimal solution was determined.

(1) Change the length of the inner boom suspension rod L_{AD}

The amplitude was set to 5°, and the driving sinusoidal excitation signal was set to 0~10 rad/s. By changing the size parameters of the L_{AD} , in the range of 800~1080 mm, eight values were taken with an interval of 40 mm. The dynamic simulation analysis of different boom suspension models is shown in Figure 9.

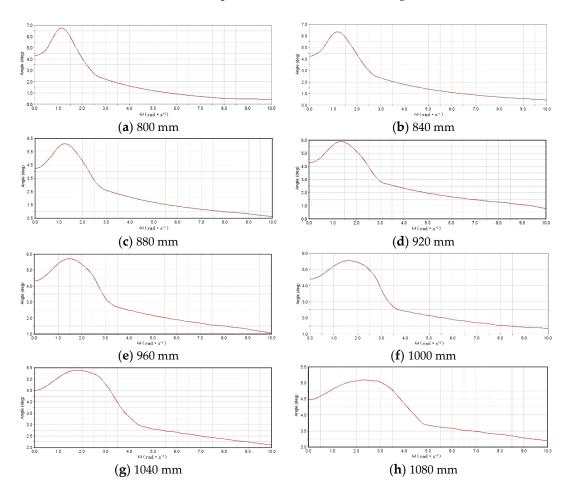


Figure 9. The relationship curve between the maximum swing angle of the external spray boom suspension and the frequency under the change in L_{AD} .

Due to the nature of natural frequencies, the highest inflection point in Figure 10a is the natural frequency. When w was less than the natural frequency, the boom suspension was able to follow the oscillation of the body. When w was greater than the natural frequency, the boom suspension began to isolate the vibration transmitted by the body and the maximum swing angle of the outer boom suspension gradually decreased as the frequency continued to increase. As can be seen from Figure 10b, with the increase in L_{AD} , the natural frequency gradually decreased, and the swing angle of the outer boom suspension at the natural frequency gradually decreased. When the size of the L_{AD} exceeded 1040 mm, the swing angle of the boom suspension changed very little, close to the swing angle of the fuselage. The results show that, when the L_{AD} of the boom suspension exceeded 1040 mm, the boom suspension followed the fuselage when stimulated by the external high frequency and low frequency, which does not meet the design requirements. Therefore, the L_{AD} was selected in the range of 840~1000 mm.

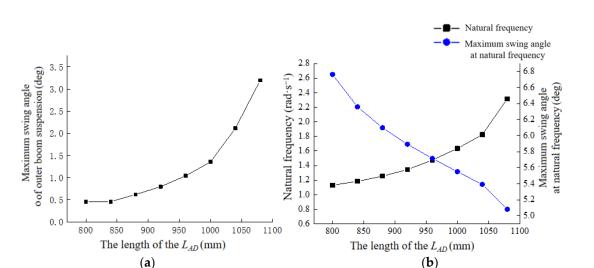


Figure 10. Relationship between boom suspension swing angle and L_{AD} . (a) The swing angle at w = 10 rad/s; (b) relation at natural frequencies.

(2) Change the length of the inner boom suspension rod L_{BC} , L_{AB} , and d

A similar method was used to perform dynamic simulation analysis by changing the length of L_{BC} , L_{AB} , and d. The amplitude was set to 5°, and the driving sinusoidal excitation signal was set to 0~10 rad/s. By changing the size parameters of the L_{BC} , in the range of 950~1300 mm, eight values were taken with an interval of 50 mm. The kinematic simulation analysis of different boom suspension models is shown in Figure 11.

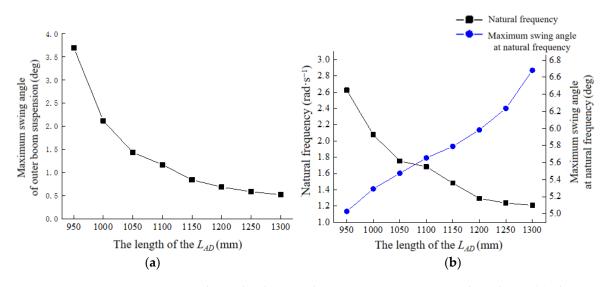


Figure 11. Relationship between boom suspension swing angle and L_{BC} . (a) The swing angle at w = 10 rad/s; (b) relation at natural frequencies.

The amplitude was set to 5° , and the driving sinusoidal excitation signal was set to $0 \sim 10 \text{ rad/s}$. By changing the size parameters of the LAD, in the range of $190 \sim 280 \text{ mm}$, seven values are taken with an interval of 15 mm. The kinematic simulation analysis of different boom suspension models is shown in Figure 12.

The amplitude was set to 5° , and the driving sinusoidal excitation signal was set to $0 \sim 10 \text{ rad/s}$. By changing the size parameters of the *d*, five values were taken with an interval of 0.5 mm. The kinematic simulation analysis of different boom suspension models is shown in Figure 13.

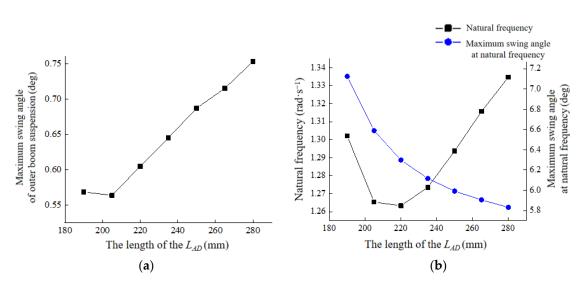


Figure 12. Relationship between boom suspension swing angle and L_{AB} . (a) The swing angle at w = 10 rad/s; (b) relation at natural frequencies.

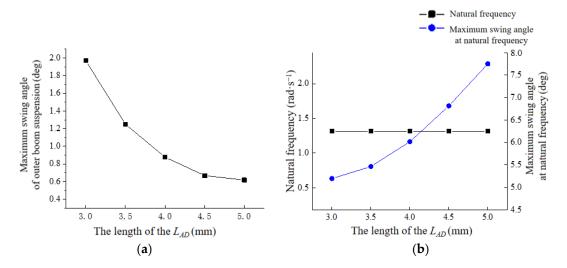


Figure 13. Relationship between boom suspension swing angle and *d*. (a) The swing angle at w = 10 rad/s; (b) relation at natural frequencies.

According to the above test results, the factor level coding table of the multivariate orthogonal test was determined, as shown in Table 3.

T 1				
Level	<i>L_{AB}</i> (mm)	<i>L_{BC}</i> (mm)	<i>LAD</i> (mm)	<i>d</i> (mm)
1	220	1050	840	3
2	235	1100	880	3.5
3	250	1150	920	4
4	265	1200	960	4.5
5	280	1250	1000	5

Table 3. Level coding table of boom suspension test factors.

In this paper, the $L_{25}(5^6)$ orthogonal table was selected for the experimental design, and the extra two factors in the table were set as empty columns to estimate the experimental error and improve the accuracy of the experiment. The test protocol and results are shown in Table 4.

Level	<i>L_{AB}</i> (mm)	L _{BC} (mm)	<i>L_{AD}</i> (mm)	<i>d</i> (mm)	E	F	Swing Angle (deg)	Natural Frequency (rad/s)
1	220	1050	840	3	1	1	1.7069	1.29
2	220	1100	880	3.5	2	2	1.21835	1.3571
3	220	1150	920	4	3	3	0.8875	1.449
4	220	1200	960	4.5	4	4	0.71315	1.5061
5	220	1250	1000	5	5	5	0.6419	1.5143
6	235	1050	880	4	4	5	1.2148	1.6265
7	235	1100	920	4.5	5	1	0.9782	1.698
8	235	1150	960	5	1	2	0.8623	1.7082
9	235	1200	1000	3	2	3	2.3001	1.502
10	235	1250	840	3.5	3	4	0.6269	1.1204
11	250	1050	920	5	2	4	1.3423	2.2286
12	250	1100	960	3	3	5	3.031	1.7449
13	250	1150	1000	3.5	4	1	2.3038	1.8163
14	250	1200	840	4	5	2	0.5226	1.1816
15	250	1250	880	4.5	1	3	0.4165	1.2245
16	265	1050	960	3.5	5	3	3.3751	2.1878
17	265	1100	1000	4	1	4	2.6797	2.2795
18	265	1150	840	4.5	2	5	0.50275	1.2939
19	265	1200	880	5	3	1	0.46155	1.3147
20	265	1250	920	3	4	2	0.6502	1.7041
21	280	1050	1000	4.5	3	2	3.827	2.713
22	280	1100	840	5	4	3	0.5654	1.4163
23	280	1150	880	3	5	4	1.6828	1.519
24	280	1200	920	3.5	1	5	1.511	1.498
25	280	1250	960	4	2	1	0.9101	1.4265

Table 4. Orthogonal test scheme and test results.

A variance analysis of the simulation data was carried out using Design-Export software 8.0.6, and the results of the ANOVA analysis of the influencing factors on the swing angle and natural frequency are shown in Tables 5 and 6.

Table 5. Swing angle variance	analysis result.
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Category	Sum of Squares	Degree of Freedom	Mean Square	F	р
Model	10.50	16	0.66	18.38	0.0001 **
$A-L_{AB}$	0.35	4	0.087	2.45	0.1307
$B-L_{BC}$	3.97	4	0.99	27.81	< 0.0001 **
$C-L_{AD}$	3.59	4	0.90	25.18	0.0001 **
d	2.58	4	0.65	18.07	0.0005 **
error	0.29	8	0.036		
sum	10.78	24			
R-squared	0.9735				

Note: ** indicates that the impact is extremely significant (p < 0.01).

 Table 6. Natural frequency variance analysis result.

Category	Sum of Squares	Degree of Freedom	Mean Square	F	р
Model	10.50	16	0.66	18.38	0.0001 **
$A-L_{AB}$	0.35	4	0.087	2.45	0.1307
$B-L_{BC}$	3.97	4	0.99	27.81	< 0.0001 **
$C-L_{AD}$	3.59	4	0.90	25.18	0.0001 **
d	2.58	4	0.65	18.07	0.0005 **
error	0.29	8	0.036		
sum	10.78	24			
R-squared	0.9735				

Note: ** indicates that the impact is extremely significant (p < 0.01).

From the above results, it can be seen that L_{BC} , L_{AD} , and orifice diameter d have extremely significant effects on the swing angle of the external spray bar suspension. The influence of L_{BC} and L_{AD} on the natural frequency was very significant, the orifice diameter d had little influence on the change in natural frequency, and the influence of L_{AB} on the swing angle and natural frequency was small. The influence of the four factors on the swing angle of the external boom suspension was $L_{BC}(B) > L_{AD}(C) > d(D) > L_{AB}(A)$, and the influence of the natural frequency of the boom suspension was $L_{BC}(B) > L_{AD}(C) > L_{AB}(A) > d(D)$. Using the data filtering function of the software, the minimum values of the swing angle and the natural frequency between 0.7 and 1.3 rad/s were set, and the results are shown in Table 7.

Name	Goal	Limit	Limit	Weight	Weight	Importance
A-L _{AB}	In range	220	280	1	1	3
$B-L_{BC}$	In range	1050	1250	1	1	3
C-L _{AD}	In range	840	1000	1	1	3
d	In range	3	5	1	1	3
Swing Angle	Minimize	0.1	3.827	1	1	3
Natural Frequency	In range	0.7	1.3	1	1	3

Group 1, with the smallest swing angle, was selected as the final optimal design scheme. The length of the connecting rod of the final scheme was $L_{AB} = 265$ mm, the length of the inner spray rod suspension was $L_{AD} = 840$ mm, the length of the outer spray rod suspension was $L_{BC} = 1250$ mm, and the diameter of the throttle hole was d = 4 mm.

The ADAMS model was constructed using the optimized structure size, the same constraints and drivers were set for the single-factor test to simulate the dynamic of the optimized model, and the results were analyzed; the results are shown in Figure 14.

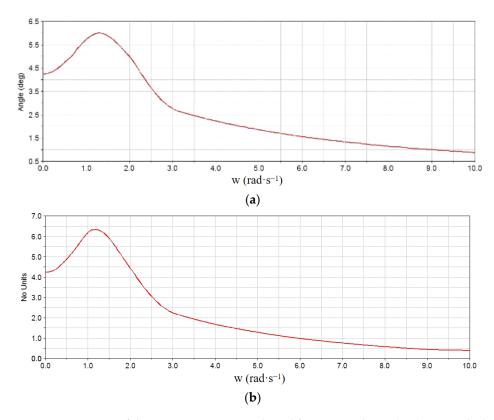


Figure 14. Diagram of the maximum swing angle and frequency relationship between the before and after of the boom suspension improvement. (**a**) Before improvement; (**b**) after improvement.

Comparing the above figure, it can be seen that the maximum swing angle and natural frequency after optimization are basically consistent with the predicted values of Design-Expert. After optimization, the maximum swing angle of the boom suspension decreased significantly, and the maximum swing angle was 0.877° before optimization $\omega = 10 \text{ rad/s}$, and the maximum swing angle was 0.412° after optimization, which decreased by 53.02% compared with that before optimization. The natural frequency was reduced from 1.3143 rad/s to 1.1826 rad/s, which met the design requirements. The optimization scheme in this study satisfies the requirements of reducing the maximum swing angle and improving the structure so that the natural frequency is between 0.7 and 1.3 rad/s.

3.2. Static Simulation Results and Analysis

As shown in Figure 15, it can be seen that the maximum stress of the connecting plate in the first section of the boom suspension was 54.97 MPa, well below the yield limit. The maximum displacement of the boom suspension was only 2 mm, close to zero. However, the maximum displacement of 35.304 mm occurred in the third section. The contact area between the inner sprayed high connecting plate and the vertical beam was small, leading to an intense local stress of 128.36 MPa. Therefore, both boom suspensions mentioned in this article need to be optimally designed. We planned to add torsion spring to the joints, which ensured the stability of the spraying process.

The first six natural frequency analysis of the boom suspension under the modal module of ANSYS 14.0 (Figure 16).

According to the analysis results shown in Figure 16, the natural frequencies of the first six modes of the spray suspension designed in this paper were in the range of 4.26~26.62 Hz. In the field test, even if the external ground was uneven and caused the body to sway, it could still ensure stable operation under the profiling function of the active suspension.

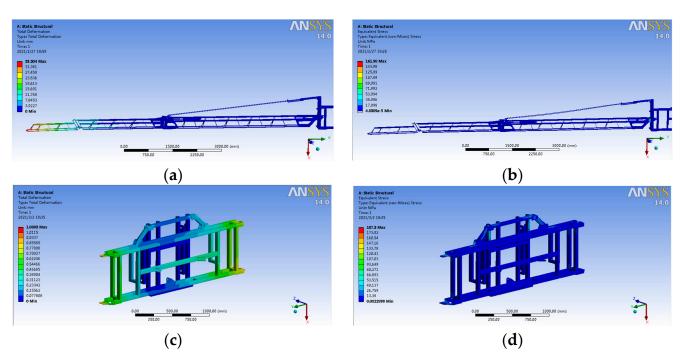


Figure 15. Displacement and stress cloud diagram boom suspension. (**a**) Displacement cloud of single-side boom; (**b**) stress cloud of single-side boom; (**c**) displacement cloud of single-side boom; and (**d**) stress cloud diagram of external boom.

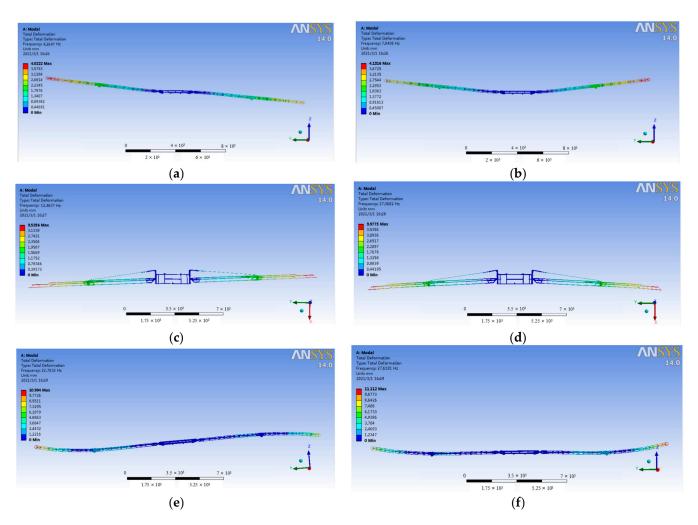


Figure 16. The first six non-rigid modes of the boom suspension. (a) First mode shape; (b) second mode shape; (c) third mode shape; (d) fourth mode shape; (e) fifth mode shape; and (f) sixth mode shape.

3.3. Field Performance Test Results and Analysis

The swing angle of the inner boom suspension and the swing angle curve of the one-side boom suspension are shown in Figure 17. Table 8 shows the maximum swing angles in the forward and reverse directions of the three suspension heights.

It can be seen from Figure 17 that the environmental excitation of the sprayer was $3.5 \sim 4^{\circ}$, and with the increase in the height of the sprayer boom suspension, the overall change curve of the inner boom suspension changed obviously, and the maximum swing angle in the forward and reverse directions was approximate. There was no obvious change in the overall curve of the single-sided boom suspension, and the height of the boom suspension increased. The angle between the hoist and the vertical direction increased first and then decreased, the maximum swing angle of the suspension increased first and the change range was about 0.2° , which proves that the mathematical model is reasonable. The maximum swing distance at the end of the 21 m boom was only 0.073 m, which ensured the stability of the pesticide application operation.

It can be seen from Table 9 that the overall change curve of the single-side boom suspension was relatively stable, and the boom suspension can realize the effect of isolating the vibration transmitted by the fuselage under different test conditions, which meets the design requirements.

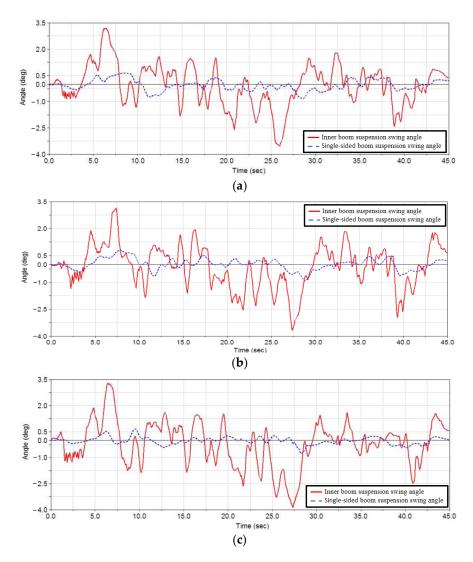


Figure 17. Boom suspension swing test results. (**a**) Height is 500 mm; (**b**) height is 1200 mm; and (**c**) height is 2500 mm.

Table 8. Orthogonal test simulation result value after screening.

Group	L _{AB}	L _{BC}	L _{AD}	d	E *	F *	Swing Angle	Natural Frequency	Rationality
1	265	1250	840	4	1	1	0.350971	1.17991	0.933
2	235	1250	840	4	1	1	0.356599	1.04662	0.931
3	250	1250	840	4	1	1	0.38037	1.10083	0.925
4	220	1250	880	4	1	1	0.397561	1.09559	0.920
5	235	1250	880	5	1	1	0.444582	1.16717	0.908
6	280	1250	840	5	1	1	0.45519	1.14558	0.905
7	250	1250	880	5	1	1	0.474218	1.22762	0.900
8	265	1200	840	5	1	1	0.502694	1.18974	0.892
9	235	1200	840	4.5	1	1	0.510755	1.05535	0.890
10	250	1200	840	4.5	1	1	0.544802	1.11	0.881
11	220	1150	840	4.5	1	1	0.548378	1.09873	0.880
12	280	1250	880	4.5	1	1	0.567499	1.27752	0.875
13	220	1200	880	3.5	1	1	0.569426	1.10472	0.874
14	235	1150	840	3.5	1	1	0.613237	1.17052	0.862
15	235	1200	880	3.5	1	1	0.636773	1.1769	0.856
16	280	1200	840	3.5	1	1	0.651967	1.15513	0.852
17	250	1150	840	3	1	1	0.654115	1.23114	0.851
18	250	1200	880	3	1	1	0.67922	1.23785	0.845

Note: * indicates that the impact is significant.

Structure	Suspension Height (mm)	Counterclockwise Maximum Swing Angle (deg)	Clockwise Maximum Swing Angle (deg)
Inner boom	500	3.22	3.92
	1200	3.22	3.92
suspension	2500	3.22	3.98
Cinala aidad	500	0.649	0.827
Single-sided	1200	0.818	1.01
boom suspension	2500	0.662	0.776

Table 9. Inner boom suspension and single-side boom suspension swing angle value.

4. Conclusions

Based on the 3WPYZ high gap self-propelled sprayer, this study designed a boom suspension system that can achieve the requirements of large width, low stiffness and weak damping, and vibration reduction. On the basis of considering the structural layout of the sprayer and the parameters of the boom, the dynamic characteristics and static analysis of the boom suspension system were analyzed, and the rationality of the optimization was verified by field tests. The research conclusions are as follows:

- (1) Based on the D'Alembert principle and the principle of multibody dynamics, a kinematic model of a two-link trapezoidal boom suspension was established, and the design factors affecting the stability of the boom were determined through theoretical analysis.
- (2) The results of the multi-factor test based on Design-Expert show that, when the connecting rod length L_{AB} was 265 mm, the inner boom suspension rod L_{AD} was 840 mm, the outer boom suspension rod L_{BC} was 1250 mm, and the throttle diameter d was 4 mm; the maximum swing angle of the nozzle suspension decreased by 53.02%, the natural frequency decreased from 1.3143 rad/s to 1.1826 rad/s, and the dynamic characteristics were significantly optimized.
- (3) After static optimization, the stress at the joint of the boom suspension was reduced to 22 MPa, the maximum displacement was reduced to 7 mm, and the maximum stress of the inner boom suspension was reduced to 88.07 MPa. The modal analysis results show that the optimized design of the boom suspension can effectively avoid the influence of external swing frequency on the stability of the suspension.
- (4) The angle between the hoist and the vertical direction increased first and then decreased, and the maximum swing angle of the suspension increased first and then decreased; the change range was about 0.2°, which proves that the mathematical model is reasonable. The maximum swing distance at the end of the 21 m boom was only 0.073 m, ensuring the stability of the pesticide application operation.

Author Contributions: J.H. and C.L. conceived the idea of the experiment; Y.L. and C.L. performed the field test; Y.L. and C.L. analyzed the data; and Z.Y., C.L., S.Z., Q.L. and W.Z. wrote and revised the paper. All authors have read and agreed to the published version of the manuscript.

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Conflicts of Interest: The authors declare no conflicts of interest.

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