



# *Article* **Improved Low-Drag Pontoons for Water Bikes**

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**Abstract:** The popularity of modern water bikes increases due to the relatively high speed developed with the use of a human muscle power only. For example, the maximum speed of prototypes reaches the value 3 m/s. Similar vehicles can be used not only for recreation and fitness, but also for transportation. To increase their speed and tonnage, we recommend improving the pontoon shape and using electrical power. The underwater part of the pontoon shape was recommended to be similar to the body shape of the fastest fish in order to decrease the wave resistance and total drag. The optimal depth of the movement of corresponding shapes was calculated. The total drag and maximum speeds of the vehicles with the human muscle and electrical power are estimated. Expected success in improving the pontoon shape opens wide prospects for the use of these special-shaped hulls in shipbuilding.

**Keywords:** green transport; electrification of maritime transport; drag reduction; environment protection; unseparated shapes; wave resistance

# **1. Introduction**

A modern water bike, Explorer-1 [\[1\]](#page-9-0), can develop speeds of up to 2.7 m/s using only human muscle power at a total weight of 240 kg. This rather high speed was achieved by improving the shape of pontoons and using an effective propeller [\[1\]](#page-9-0). Similar vehicles can be used not only for recreation and fitness, but also for transportation, especially with the use of electrical power. To increase the speed and the commercial effectiveness (weightto-drag ratio) of such vehicles, special-shaped pontoons of low drag (similar to the body shape of the best swimmers) are proposed.

The maximum speed of the fastest fish can reach around 30 m/s (e.g., sailfish, swordfish, black marlin, etc., [\[2](#page-9-1)[–5\]](#page-9-2)). A very sharp nasal rostrum of these animals probably allows them to remove the boundary layer separation and avoid high pressures on the body surface as well as reduce the wave resistance when moving near the water surface. The corresponding axisymmetric bodies with concave noses have no pressure peaks on their shape and have much lower values of the vertical velocity on the water surface [\[6\]](#page-9-3). Since the reason for the waves on the water surface is the high pressure on the vessel bow and stern [\[7–](#page-9-4)[10\]](#page-9-5), these special-shaped bodies could be used to reduce wave resistance. Some other results concerning the optimization of the ship's hull can be found in [\[11–](#page-9-6)[16\]](#page-10-0).

It was shown in [\[17\]](#page-10-1) that axisymmetric bodies similar to the trunks of water animals can ensure an underwater flow pattern without boundary separation. It was proposed to use dolphin-like shapes for the underwater hulls of SWATH (Small Waterplane Area Twin Hulls) yachts and ferries [\[18\]](#page-10-2). The expected values of volumetric drag coefficient *C<sup>V</sup>* can be reduced more than twice in comparison with known shapes in the range of volumetric



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Reynolds numbers Re*<sup>V</sup>* from 1 to 10 million (see [\[17\]](#page-10-1), Figure [1\)](#page-1-0). The corresponding volumetric coefficients can be calculated as follows: Reynolds numbers Re*<sup>V</sup>* from 1 to 10 million (see [17], Figure 1). The corresponding vol-

$$
C_V = \frac{2X}{\rho U^2 V^{2/3}} \quad \text{Re}_V = \frac{U V^{\frac{1}{3}}}{v}
$$

<span id="page-1-0"></span>where V is the volume (displacement), U is speed, X is the total drag, and  $\rho$  and  $\nu$  are the density and kinematic viscosity of water, respectively. These values of  $C_V$  (shown in Figure 1 by the black solid line) are smaller than the drag on some special-shaped bodies of revolution [\[19](#page-10-3)[–21\]](#page-10-4) (se[e m](#page-1-0)arkers in Figure 1).



**Figure 1.** Volumetric drag coefficient versus volumetric Reynolds number for standard (dashed **Figure 1.** Volumetric drag coefficient versus volumetric Reynolds number for standard (dashed lines) lines) and special−shaped (solid lines) bodies of revolution with different length−to−diameter ratios and special−shaped (solid lines) bodies of revolution with different length−to−diameter ratios *L/D*. *L/D*. Reproduced from [17], with permission from Igor Nesteruk, 2018. Upper dashed lines corre-Reproduced from [\[17\]](#page-10-1), with permission from Igor Nesteruk, 2018. Upper dashed lines correspond to<br>the laminar flow; lower dashed lines, the turbulent one. Drag coefficients for standard bodies are shown in dark blue for  $L/D = 4.5$ ; in blue for  $L/D = 5.9$ ; in green for  $L/D = 12.4$ ; and magenta for  $L/D$  = 33.3. Solid lines represent volumetric drag coefficients for special-shaped bodies: unseparated unclosed body UA-2 ( $L/D = 3.52$ ; red line); closed bodies UA-4.5c "Albacore" ( $L/D = 4.5$ ; dark blue line), UA-5.9c "Blue shark" ( $L/D = 5.9$ ; blue line), UA-12.4c "Sailfish" ( $L/D = 12.4$ ; green line), UA-33.3c "Largehead hairtail" ( $L/D = 33.3$ ; magenta line); and unclosed body UA-23.3 ( $L/D = 23.3$ ; brown line). Markers show the experimental data for standard ("stars", [\[19\]](#page-10-3)) and other special- $\frac{d}{dt}$  behavior ("similar"), red. "Delphin" body [20]. Thus  $\frac{d}{dt}$  charging hody [10] shaped bodies of revolution ("circles"): red—"Dolphin" body [\[20\]](#page-10-5), blue—Goldschmied body [\[19\]](#page-10-3),<br>deed to the contract the contract of the contr  $S_{\text{S}}$ dark blue—Hansen and Hoyt body [\[21\]](#page-10-4). Typical values of volumetric Reynolds numbers are shown by names.

Small disturbances of the water surface caused by the special-shaped bodies of a revolution with concave noses (similar to the rostrums of the fastest fish)  $\overline{16}$  open prospects of their use for floating vehicles. The volumetric Reynolds number for Explorer-1 is approximately 1.3 million. It means that larger and faster vehicles with special-shaped pontoons can also have a lower drag (see black solid line in Figure [1\)](#page-1-0). Since such pontoons move near the water surface, the friction and wave drags of corresponding bodies of In this paper we will concentrate on the total estimation of the total drag of specifical estimation of specifical estimations of  $\mathcal{L}$ 

In this paper we will concentrate on theoretical estimations of the total drag of specialshaped bodies of revolution moving near the water surface and will estimate the optimal depth of steady movement (Section 2). The vertical velocities on the [w](#page-2-0)ater surface will be calculated in Section 3. We will evaluate the maximum velocity of the improved water bike (Section 4) and electrical vehicles with special-shaped hulls for laminar and turbulent flow patterns (Section 5). The range of the improved electrical vehicles will be estimated in Sec[tio](#page-7-0)n 5. The problems concerned with the manufacturing of the proposed shapes will be discussed in Section [6.](#page-8-0) **Fish** 

#### <span id="page-2-0"></span>2. Friction Drag on Floating Bodies of Revolution Similar to the Shape of the **Fastest Fish** and removes the boundary layer separation. If the distance between pontoons the distance between points of the

Let us assume that the axisymmetric shape of pontoons is similar to the bodies of the Ect as assume that the axisymmetric shape of pontoons is similar to the bounds of the fastest fish and removes the boundary layer separation. If the distance between pontoons is large enough, the interference and pressure drag connected with separation can be neglected. Then, the hydrodynamic forces acting on each pontoon can be estimated as for a single hull of volume *V* and length *L*. single hull and removes the boundary  $t_{\text{reduction}}$  for the following formula formula formula formula formula formula  $V$ 

The total drag *X* on a slender axisymmetric unseparated body can be estimated with the use of the following formula for the volumetric drag coefficient in a laminar unbounded<br>flow [17] flow [\[17\]](#page-10-1):  $\overline{A}$ 

$$
C_V = \frac{4.7}{\sqrt{\text{Re}_V}}\tag{1}
$$

The solid black line represents this relationship in Figure [1.](#page-1-0) Equation (1) shows that the volumetric drag coefficient does not depend on the hull shape, provided it is slender Incording the veral comparison and the volumetric Reynolds R Formula (1) is valid only for the volumetric Reynolds  $\text{Re}_V$  numbers lower than the critical one [\[22\]](#page-10-6): *L*

$$
Re_V^* = \frac{59558\pi L^2}{V^{2/3}}
$$
 (2)

At higher Reynolds numbers, the turbulence appears in the boundary layer and in-At higher Reynolds numbers, the turbulence appears in the boundary layer and increases the friction drag. The corresponding values of the drag coefficient can be calculated with the use of the flat plate c[onc](#page-10-7)ept  $[23]$  and start to deviate from the relationship  $(1)$  (see solid lines i[n](#page-1-0) Figure 1). At supercritical Reynolds numbers, the shape peculiarities have to be taken into account and the drag coefficient is much higher ([see](#page-1-0) Figure 1). For example, at high Reynolds numbers, it can be estimated [as f](#page-10-1)[ollo](#page-10-6)ws [17,22]:

$$
C_V \approx 0.01, \ 10^7 < \text{Re}_V < 10^9 \tag{3}
$$

for the unbounded attached turbulent flow (see Figure [1\)](#page-1-0). for the unbounded attached turbulent flow (see Figure 1).

If a slender body of revolution moves horizontally at constant speed *U* at depth *h* If a slender body of revolution moves horizontally at constant speed *U* at depth *h* along its axis of symmetry *Ox* (*h* is the distance between the undisturbed water surface and along its axis of symmetry *Ox* (*h* is the distance between the undisturbed water surface the body axis of symmetry; see Figure [2\)](#page-2-1), its wave resistance must be taken into account. The case  $h < D/2$  also changes the friction drag.

<span id="page-2-1"></span>

**Figure 2.** Slender body of revolution similar to the sailfish shape near the water surface (blue line). **Figure 2.** Slender body of revolution similar to the sailfish shape near the water surface (blue line). Simulation with the use of sources and sinks. Simulation with the use of sources and sinks.

Assuming that the friction drag  $X_f$  is proportional to the submerged area  $S_f$ , the responding volumetric drag coefficient (based on the displacement *Vf*). corresponding volumetric drag coefficient (based on the displacement *V<sup>f</sup>* ).

$$
C_{Vf} = \frac{2X_f}{\rho U^2 V_f^{2/3}} \sim \frac{S_f}{V_f^{2/3}}
$$
(4)

will be proportional to  $S_f/V_f^{2/3}$  $f^{2/3}$  ( $\rho$  is the density of water). Introducing the shape coefficients  $0 \le f_s \le 1$  and  $0 \le f_V \le 1$ , corresponding to the part of the body wetted by water (i.e.,  $S_f = f_S(h)S$  and  $V_f = f_V(h)V$ , then Equations (1) and (4) yield: field  $f: \mathbb{R}^2 \to \mathbb{R}^2$   $f: \mathbb{R}^2 \to \mathbb{R}^2$  , corresponding to the part of the part of the body water of will be proportional to  $3f / V_f$  (*i)* is the density of water). Introducing the  $\frac{1}{2}$  subsets of  $\frac{1}{2}$  and  $\frac{1}{2}$  or  $\frac{1}{2}$  and  $\frac{1}{2}$  or  $\frac{1}{2}$  and  $\frac{1}{2}$  and  $\frac{1}{2}$  and  $\frac{1}{2}$  and  $\frac{1}{2}$ 

will be proportional to 200 million proportional to 200 million proportional to 200 million.<br>The proportional to 200 million proportional to 200 million proportion proportion proportion proportion propor

$$
C_{Vf} = f(h)C_V, \ f(h) = \frac{f_S(h)}{[f_V(h)]^{2/3}}
$$
(5)

In particular, at  $h = 0$ , the corresponding values  $f_s(0) = f_V(0) = 0.5$  and according to Equation (2):  $C$   $C$   $C$   $D$   $D$   $C$   $D$   $D$   $C$  and according to

$$
C_{Vf} = \frac{C_V}{2^{\frac{1}{3}}}
$$
\n<sup>(6)</sup>

Formula (6) shows that floating bodies of revolution may have a lower friction drag coefficient in comparison with the underwater ones. Nevertheless, the pressure drag connected with the waves on the water surface (even without the boundary layer separation) may yield rather high levels of total drag.

Let us calculate the values of function  $f(h)$  for the body of revolution obtained in [6] with the use of sources and sinks located on the axis of symmetry. Their intensity is given by:  $\frac{1}{2}$  dx  $\frac{1}{2}$ 

$$
q_1(x) = \begin{cases} cx^3 + dx^4, & 0 \le x \le x_* \\ a_1(x-1)^2, & x_* \le x \le 1 \end{cases}
$$
 (7)

The values of parameters  $c$ ,  $d$ ,  $a_1$ , and  $x*$  are adjusted to remove the stagnation point on the nose. The absence of the very small velocities near this point allows for a reduction in the maximum pressure on the body surface and the wave drag [6]. The black solid line in Figure 3 represents an example of such a body of revolution with a sharp concave nose, similar to the shape of sailfish. The pressure coefficient similar to the shape of sailfish. The pressure coefficient on the nose. The absence of the very small velocities near this point allows for a reduction<br>in the maximum pressure on the body surface and the wave drag [\[6\]](#page-9-3). The black solid line<br>in Figure [3](#page-3-0) represents an example of such

$$
c_p(x) = \frac{2[p(x) - p_{\infty}]}{\rho U^2}
$$

<span id="page-3-0"></span>on its surface at infinite depth is shown by the blue solid line;  $p(x)$  is the pressure on the hull of its surface at finallite depth is shown by the bide solid line,  $p(x)$  is the pressure of the fidit surface and  $p_{\infty}$  is the pressure in the ambient flow at the same depth. We see the absence of a stagnation point at nose, since  $c_p$  does not tend to 1.0 at  $x \to 0$ .



**Figure 3.** Radius (black) and pressure coefficient on the surface (blue) for the bodies of revolution **Figure 3.** Radius (black) and pressure coefficient on the surface (blue) for the bodies of revolution with the concave (solid) and convex (dashed) noses. with the concave (solid) and convex (dashed) noses.

Figure [4](#page-4-1) presents the results of the calculations of shape coefficients  $f_S$ ,  $f_V$  (dotted and dashed lines, respectively) and the friction drag coefficient  $f$  (the solid line) for the slender body of revolution similar to the sailfish shape (shown in Figure [3](#page-3-0) by the black solid line). The minimum value of  $f = 0.7782$  correspond to the dimensionless depth of steady horizontal movement  $h/D = -0.09$  and is only 2% lower than the value given by (6) and corresponding to  $h = 0$ . If we are interested in only positive values of  $h$ , the minimum friction drag can be achieved at the smallest values of depth, e.g.,  $h/D < 0.1$  (see the solid line in Figure [4\)](#page-4-1). Figure 4).

<span id="page-4-1"></span>

**Figure 4.** Shape coefficients  $f_S$ ,  $f_V$  and the friction drag coefficient  $f$  versus dimensionless depth for the axisymmetric body similar to the shape of sailfish (shown in Figur[e 3](#page-3-0) by the solid black line). the axisymmetric body similar to the shape of sailfish (shown in Figure 3 by the solid black line).

# <span id="page-4-0"></span>**3. Estimations of Vertical Velocities on the Water Surface 3. Estimations of Vertical Velocities on the Water Surface**

The wave drag caused by the hulls with a sharp concave nose (similar to the rostrum of the fastest fish [\[2](#page-9-1)[–5\]](#page-9-2) and shown in Figure [3\)](#page-3-0) can be estimated with the use of the vertical velocities on the water surface. In order to simulate the presence of the water boundary, let vecessities on the water surface in order to simulate the presence of the water boundary,  $\frac{1}{2}$  and sources and sinks with intensities  $Q_i$  located on the axis of symmetry  $Ox$  and sources and sinks of opposite intensities  $-Q_i$  located on the line  $y = 2h$ ,  $z = 0$  (see Figure [3](#page-3-0) [\[24\]](#page-10-8)). Then, the vertical velocities on the water surface at the plane of symmetry  $(y = h, z = 0)$  can  $\frac{1}{2}$  be estimated as follows [\[6\]](#page-9-3): 0) can be estimated as follows [6]: The wave drag caused by the hulls with a sharp concave nose (similar to the rostrum

$$
v_y(x, h, 0) = \frac{h}{2\pi} \sum_{i=1}^n \frac{Q_i}{\left[ (x - \xi_i)^2 + h^2 \right]^{\frac{3}{2}}}
$$
(8)

The discrete values of *Qi* corresponding to the distribution (7) have been used in The discrete values of *Q<sup>i</sup>* corresponding to the distribution (7) have been used in Equation (8) to estimate the deformation of the water surface and corresponding wave Equation (8) to estimate the deformation of the water surface and corresponding wave resistance. Solid lines in Figure [5](#page-5-0) represent the results of the calculations of the vertical velocity on the water surface upstream of the concave nose at different values of the dimensionless depth  $h/D$ . The solid lines in Fig[ur](#page-3-0)e 3 show the radius  $R(x)$  of the corresponding body with rostrum (black) and the pressure coefficient on its surface at infinite depth (blue).

The slender bodies of revolution with convex noses have a stagnation point and a pressure peak on the surface. To illustrate this fact, we have used the source distribution: pressure peak on the surface. To illustrate this fact, we have used the source distribution:  $\frac{1}{2}$ 

$$
q_2(x) = \begin{cases} ax^2 + bx, & 0 \le x \le x_* \\ a_1(x-1)^2, & x_* \le x \le 1 \end{cases}
$$
 (9)

and a set of constant parameters  $a$ ,  $b$ ,  $a_1$ , and  $x*$  are chosen in order to calculate an example of a body of the same *L/D* ratio with a convex nose (see the black dashed line in Figure [3\)](#page-3-0),

<span id="page-5-0"></span>

**Figure 5.** Vertical velocities on the free surface of water upstream to the shapes with concave (solid **Figure 5.** Vertical velocities on the free surface of water upstream to the shapes with concave (solid lines) and convex (dashed lines) noses shown in Figure [3](#page-3-0) at different depths. lines) and convex (dashed lines) noses shown in Figure 3 at different depths.

Figure [5](#page-5-0) illustrates that the vertical velocities on the water surface upstream to the Figure 5 illustrates that the vertical velocities on the water surface upstream to the shapes with the concave nose can be significantly reduced in comparison with the similar shapes with the concave nose can be significantly reduced in comparison with the similar slender shapes with convex noses (compare corresponding solid and dashed lines). This slender shapes with convex noses (compare corresponding solid and dashed lines). This effect is especially strong at small depths (compare red and black lines) due to the absence effect is especially strong at small depths (compare red and black lines) due to the absence of high pressures on the hull. of high pressures on the hull.

Both shapes shown in Figure [3](#page-3-0) have no stagnation points (and high pressures) on the shapes shown in Figure 3 have no stagnation points (and high pressures) on the trailing edge (see blue lines at  $x = 1$ ). Thus, we can expect small magnitudes of the vertical velocities downstream to the trailing edge. Figure [6](#page-6-1) illustrates the results of for the body with a concave nose corresponding to the black solid line in Figure 3. The calculations for the body with a concave nose corresponding to the black solid line in Figure [3.](#page-3-0) The magnitudes of vertical velocities are much lower than the corresponding  $\frac{1}{2}$ to the concave nose shown in Figure 5 (compare solid lines with the same color in Figures color in Figures [5](#page-5-0) and [6\)](#page-6-1). This result can be explained by larger values of the pressure on the body surface near the concave nose in comparison with  $c_p$  values near the tail (see the the body surface near the concave nose in comparison with  $c_p$  values near the tail (see the solid blue line in Figure [3\)](#page-3-0). The pressure distributions near the tail of both bodies with the Figure 3). The pressure distributions near the tail of both bodies with the concave and concave and convex noses are very close (compare blue lines in Figure [3\)](#page-3-0). This fact yielded very similar values of the vertical velocities on the water surface downstream to the bodies very similar values of the vertical velocities on the water surface downstream to the bodies values of the vertical velocities on the water surface downstream to the bodies with conwith concave and convex noses at the same depth (compare solid and dashed curves in<br>Figure 6). values upstream to the concave nose shown in Figure [5](#page-5-0) (compare solid lines with the same Figure [6\)](#page-6-1).

It is well known that the pressure peaks on the hulls cause deformations of the water It is well known that the pressure peaks on the hulls cause deformations of the water surface and wave resistance [7–9]. To reduce this drag, the elongated wave-piercing hulls surface and wave resistance [\[7](#page-9-4)[–9\]](#page-9-7). To reduce this drag, the elongated wave-piercing hulls and bulbous bows are used [10,25–27]. The proposed shapes with very sharp concave and bulbous bows are used [\[10,](#page-9-5)[25](#page-10-9)[–27\]](#page-10-10). The proposed shapes with very sharp concave noses and tails open the prospects for a further reduction in wave resistance. Since the noses and tails open the prospects for a further reduction in wave resistance. Since the wave drag is expected to be low, Formulas (1) and (3) can be used to estimate the total wave drag is expected to be low, Formulas (1) and (3) can be used to estimate the total drag on floating special-shaped hulls with concave noses, since the smallest values of depth *h* can be recommended.

Since such hulls have never been tested (similar shapes exist only in nature—the fastest fish are used as our examples), the improved water bike pontoons provide us with a good opportunity to verify the theoretical estimations on the real vehicle. After a change of the prototype pontoon[s \(](#page-9-0)e.g., [1]) with improved ones (similar to that shown i[n F](#page-2-1)igures 2 and [3\)](#page-3-0), we could estimate the increase in the maximum speed with the use of the same human muscle power.

<span id="page-6-1"></span>

**Figure 6.** Vertical velocities on the free surface of water downstream to the bodies with concave **Figure 6.** Vertical velocities on the free surface of water downstream to the bodies with concave (solid lines) and convex (dashed lines) noses shown in Figure [3.](#page-3-0) Dimensionless depths *h* and distance are based on the body length *L*.

Let us make some estimations for Explorer-1 ( $U = 2.7$  m/s; displacement 0.24 m<sup>3</sup> [[1\]](#page-9-0)). For the pontoons of an improved water bike, we can use two almost half-submerged bodies of revolution similar to that shown in Figure 3 by t[he](#page-3-0) black solid line with the volume of 0.24  $\mathrm{m}^{3}$  each. Then, the total drag can be estimated with the use of Formula (1): the volumetric Reynolds number is approximately 1.3 million ( $U = 2.7$  m/s;  $V = 0.24$  m<sup>3</sup>;  $\nu = 1.3 \cdot 10^{-6} \text{ m}^2/\text{s}$  at 10 °C) and the volumetric drag coefficient  $C_V \approx 0.0041$ . This value is more than twise lower than the drag on the Hanson and Hoyt hody [21] totad at the same volumetric Reynolds number (see Figure [1\)](#page-1-0). is more then twice lower than the drag on the Hansen and Hoyt body [\[21\]](#page-10-4) tested at the

According to Formula (1), the volumetric drag coefficients of improved water bikes can be much lower at higher subcritical Reynolds numbers. If we use the special-shaped pontoons of length *L* = 3 m (the same as for Explorer-1) and volume 0.24 m<sup>3</sup> each, then, the r<br>critical Reynolds number will be around 4.4 million (see Equation (2)). This means that even at a speed of 9 m/s, we could expect the laminar flow pattern and  $C_V \approx 0.0022$ . In the next Section, we will answer the question: Is this speed achievable with the use of human  $t$  muscle power only?

#### <span id="page-6-0"></span>**4. Estimations of Maximum Velocities**

The mechanical power *P* of a vehicle can be estimated as the product of its speed *U* by the thrust (which is equal to the total drag *X* in steady motion). Then, with the use of the volumetric drag coefficient  $C_V$ , we can obtain the following relationship:

$$
P = Xu = 0.5C_V \rho U^3 V^{2/3}
$$
\n(10)

Taking the characteristics of Explorer-1 [\[1\]](#page-9-0): the maximum speed  $U = 2.7$  m/s, the displacement *V* = 0.24 m<sup>3</sup>, and  $C_V = 0.01$  (this value was measured on the Hansen and Hoyt body [\[21\]](#page-10-4); see Figure [1\)](#page-1-0), the mechanical power can be estimated as 38 W. The corresponding<br>. human muscle power is higher since only its part is transformed into the mechanical power<br>corresponding to the corresponding to the corresponding to the mechanical power of the vehicle motion (in particular, some energy is wasted on the propeller). However,<br>if we also use only the mentals was the abtained reduced  $29. M_{\odot}$  is weak to order the limits the if we change only the pontoons, the obtained value 38 W can be used to estimate the property is a property in particular, some  $\frac{1}{2}$ maximum speed of the improved water bike.

Haximan speed of the improved water sixe. If we use the equal almost han submerged pomoths of verally variating shape.<br>Similar to the one shown in Figure [3](#page-3-0) by the black solid line, then the wave resistance can be If we use two equal almost  $\frac{1}{2}$  with the submerged point  $\frac{1}{2}$  with the shape  $\frac{1}{2}$  and  $\frac{1}{2}$ . The total due of  $\frac{1}{2}$ neglected for small values of depth, e.g., *h/D <* 0.1, see Figures [4](#page-4-1) and [5.](#page-5-0) The total drag of the improved water bike can be estimated as a friction drag on a single underwater hull of the same volume *V*.

For subcritical Reynolds numbers, the volumetric drag coefficient of the vehicle can be estimated with the use of Formula (1). Then, Equation (10) allows us calculating its maximum speed at a given value of mechanical power, as follows:

$$
U = \left[\frac{P}{2.35\rho\sqrt{Vv}}\right]^{0.4}
$$
 (11)

Formula (11) yields the maximum speed of 3.8 m/s for the improved water bike with the same mechanical power 38 W and the displacement  $V = 0.24 \text{ m}^3$  (the value  $\nu = 1.3 \cdot 10^{-6}$  m<sup>2</sup>/s was used for this estimation). Thus, the expected speed is almost 41% higher than for the prototype. Nevertheless, the maximum speed of 9 m/s estimated in the previous section for a laminar vehicle cannot be achieved with the use of human power only. On the other hand, an improved human-muscle-powered water bike of mass 1 t can achieve the speed of  $2.9 \text{ m/s}$ . Thus, similar improved vehicles can be also used for transportation at rather high speeds.

Significant differences in speeds of the prototype and an improved water bike can be easily registered in tests, providing us with an opportunity to estimate the efficiency of new pontoons. In the case of success, the new shapes can be recommended for rowing shells, small boats, and ships with subcritical Reynolds numbers. The new shapes could also be very useful for larger and faster vehicles since their volumetric drag coefficients are much lower then for standard hulls even at supercritical Reynolds numbers (compare solid and dashed lines in Figure [1\)](#page-1-0).

Small drag on unseparated hulls allows increasing the commercial effectiveness (weight-to-drag ratio [\[28\]](#page-10-11)). In particular, the dolphin-like underwater shapes can ensure the attached laminar flow at rather high Reynolds numbers [\[29\]](#page-10-12) and can be recommended for SWATH (Small Waterplane Area Twin Hull) yachts and ferries [\[18\]](#page-10-2). The small drag of floating hulls with a sharp nose similar to the shapes of the fastest fish could improve the commercial efficiency of common ships for both sub- and supercritical Reynolds numbers.

### <span id="page-7-0"></span>**5. Maximum Velocities and Ranges of Electrical Vehicles**

To reduce the negative impact of emissions of carbon dioxide and toxic substances (which are critical in some areas [\[30](#page-10-13)[,31\]](#page-10-14)), the use of fossil fuels has to be stopped. Electric ships are already in operation [\[32](#page-10-15)[,33\]](#page-10-16), but there is some delay in the electrification of the maritime transport (in comparison with cars and buses) connected with the higher drag in water. The low drag on the proposed hulls allows increasing the commercial efficiency of ships and range with the use of one charge.

Let us estimate the maximum speed and range of electrical vehicles with improved hulls using the power-to-weight ratio  $P_W$  and the operation time  $T$  at a given value of the power. The power-to-mass ratio for modern electrical accumulators ranges from 1.65 to 9706 W/kg  $[34]$ . Then, the corresponding power-to-weight ratios are between 0.17 and 990.4 W/N or m/s. The battery discharge time *T* can range between 0.5 and 90,000 s [\[34\]](#page-10-17).

Taking into account that only a part  $0 < k_P \leq 1$  of the accumulator power  $P_a$  is used for a steady motion (with the required mechanical power *XU*) and that the weight of accumulators  $gm_a$  is only a part  $0 < k_m \leq 1$  of a vehicle tonnage, the following formula is valid:

$$
P_W = \frac{P_a}{gm_a} = \frac{XU}{k_P k_m mg} = \frac{XU}{k_P k_m \rho Vg} = \frac{\rho C_V U^2 V^{2/3} U}{2k_P k_m \rho Vg} = \frac{C_V U^3}{2k_P k_m g V^{1/3}}
$$
(12)

Equation (12) allows for estimating the speed that can be achieved at given values of  $p_W$ ,  $k_m$ , and  $k_P$ , as follows:

$$
U = \sqrt[3]{\frac{2P_W k_P k_m g V^{1/3}}{C_V}} = \frac{k_t V^{1/9}}{C_V^{1/3}}, \ k_t = \sqrt[3]{2P_W k_P k_m g} \tag{13}
$$

Taking into account Equations (1) and (3), the following estimations for the maximum Taking into account Equations (1) and (3), the following estimations for the maximum velocity in the cases of the laminar and turbulent flows can be obtained: velocity in the cases of the laminar and turbulent flows can be obtained:

<sup>3</sup> <sup>1</sup> 2 *W Pm t <sup>P</sup> k k gV k V <sup>U</sup>*

$$
U_{lam} = 0.54 \sqrt[5]{\frac{k_t^6 V}{\nu}}, \ U_{tur} = 4.64 k_t V^{\frac{1}{9}}
$$
 (14)

= = , <sup>3</sup> 2 *t W Pm k Pkk g* = (13)

If the ranges of  $k_p$  and  $k_m$  are between 0.1 and 1.0, the  $k_t$  values are located between<br>0.15 and 12.6  $\frac{2}{3}$  (a. Figure 7.11) what is the values high (14) of three different handless  $0.15$  and  $12.6$   $\mathrm{m}^{2/3}/\mathrm{s}$ . Figure  $7$  illustrates the relationships (14) at three different  $k_t$  values for laminar ("circles") and turbulent ("triangles") hulls versus displacement *V.* At high for laminar ("circles") and turbulent ("triangles") hulls versus displacement *V.* At high values of  $k_t$ , rather high speeds of electrical vehicles are possible (especially for large values values of the displacement; see blue markers in Figure [7\)](#page-8-1). Taking in  $(14)$  some average value  $k_t = 1.0 \text{ m}^{2/3}/\text{s}$ , the maximum speed of the improved electrical water bike (with  $V = 0.24 \text{ m}^3$ )  $v = 1.3 \cdot 10^{-6} \text{ m}^2/\text{s}$ ) can be estimated as 6.1 m/s for the laminar case and 4.0 m/s for the turbulent one. turbulent one.

<span id="page-8-1"></span>

**Figure 7.** Maximum speed of electrical vehicles with laminar and turbulent hulls at different values **Figure 7.** Maximum speed of electrical vehicles with laminar and turbulent hulls at different values of parameter  $k_t$  (measured in  $m^{2/3}/s$ ).

To estimate the range of the improved electrical water bike, it is enough to multiply values (14) by the battery discharge time *T*. Then, at the highest value of *T* = 90,000 s, the range of the laminar vehicle can be 549 km. This estimation looks too optimistic, since the range of the laminar vehicle can be 549 km. This estimation looks too optimistic, since the range of the laminar vehicle can be  $\mathbf{S}^k$  (can be 549 km. This estimation looks to optimize the since the  $\mathbf{S}^k$ ) contribution looks to optimize the since the since the since the since the since the since  $\mathbf{S}$ batteries with a high value of  $k_t$  (ensuring the highest speeds) have smaller discharging time  $[34]$ time [34]. time [\[34\]](#page-10-17). To estimate the range of the improved electrical water bike, it is enough to multiply

# <span id="page-8-0"></span>**6. Strength and Materials Limitations**

Formula (14) and Figure [7](#page-8-1) illustrate, that rather high speeds of electrical vehicles can be achieved at high values of the parameter  $k_t$ , especially for the laminar case. In the turbulent flow, the corresponding maximum speed is approximately twice lower. To achieve the highest speeds, special-shaped, very slender hulls must be used, which ensure the laminar-attached flow. Unfortunately, the length and volume of such hulls are limited by critical Reynolds numbers (see Formula (2)). The length-to-diameter ratio *L*/*D* must be as high as possible to increase the critical Reynolds number. In particular, taking into account the formula:

$$
\frac{V}{L^3} = \gamma \left(\frac{D}{L}\right)^2,\tag{15}
$$

where dimensionless coefficient *γ* varies from 0.23 to 0.33 for *D*/*L* from 0.02 to 0.28 [\[22\]](#page-10-6), Equation (2) can be rewritten as follows:

$$
\text{Re}_{V}^{*} = \frac{59558\pi}{\gamma^{2/3}} \left(\frac{L}{D}\right)^{4/3} \tag{16}
$$

The values of *L*/*D* range from 5 to 12 for the fastest fish, allowing them to have subcritical Reynolds numbers, a laminar flow pattern, and a low drag. Modern materials and technologies make it possible to manufacture very elongated special-shaped hulls. It is likely that modern materials can ensure that the values of *L*/*D* are higher than 33.3 (typical for the fish Largehead hairtail [\[2\]](#page-9-1)) and that the critical values of the volumetric Reynolds number are higher than 50 million (according to Equation (16)).

# **7. Conclusions**

The special-shaped bodies of revolution with the sharp concave noses (similar to the trunks of the fastest fish) moving near the water surface can ensure a low total drag and a high commercial efficiency. In particular, improved pontoon shapes can increase the speed and tonnage of water bikes using human muscle and electrical power. If the calculated significant differences in speeds of the prototype and an improved water bike are registered in tests, the new shapes can be recommended for rowing shells, small boats, and ships and probably also for larger and faster vehicles.

Modern materials and technologies open wide prospects for these special-shaped hulls in shipbuilding.

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