

Article **Reliability Dynamic Analysis by Fault Trees and Binary Decision Diagrams**

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Abstract: New wind turbines are becoming more complex and reliability analysis of them rising in complexity. The systems are composed of many components. Fault tree is used as an useful tool to analyze these interrelations and provide a scheme of the wind turbine, to get a quick overview of the behavior of the system under certain conditions of the components. However, it is complicated and in some cases not possible, to identify the conditions that would generate a wind turbine failure. A quantitative and qualitative reliability analysis of the wind turbine is proposed in this study. Binary decision diagrams are employed as a suitable and operational method to facilitate this analysis and to get an analytical expression by the Boolean functions. The size of the binary decision diagram, i.e., the computational cost for solving the problem, has an important dependence on the order of the components or events considered. Different heuristic ranking methods are used to find an optimal order or one closed, and to validate the results: AND, level, top-down-left-right, deep-first search and breadth-first-search. Birnbaum and criticality importance measures are proposed to evaluate the relevance of each component. This analysis leads to classify the events according to their importance with respect to the probability of the top event. This analysis provides the basis for making medium and long-term maintenance strategies.

Keywords: fault tree; binary decision diagrams; wind turbines; maintenance management; wind energy; dynamic analysis

1. Introduction

Wind energy is one of the fasting-growing renewable energies because of the new wind turbines (WT), becoming higher and more complex, i.e., with more power electric generation [\[1\]](#page-10-0). It is expected that new installations will increase more than 55 GW every year until 2023 [\[2\]](#page-10-1), see Figure [1.](#page-1-0)

A WT is composed of static parts, e.g., tower or support, blades and nacelle and rotative or mechanical components, e.g., hubs, gearbox or generator. These components are exposed to physical efforts, e.g., stress or compression and chemical or environmental conditions such as erosion or surface degeneration [\[3\]](#page-11-0). During the operation of the installations, mechanical or electrical failures appear due to the working conditions [\[4,](#page-11-1)[5\]](#page-11-2).

Figure 1. Wind energy capacity and forecast [2]. **Figure 1.** Wind energy capacity and forecast [\[2\]](#page-10-1).

mechanical and control systems. This is leading to increased production capacity and improved competitiveness [\[1,](#page-10-0)[7\]](#page-11-4). These new strategies—together with the data available and the advanced analytics—are favoring system efficiency and cost-reduction [\[8,](#page-11-5)[9\]](#page-11-6). Good maintenance policies have been demonstrated to be a key factor in this efficiency and cost-reduction [\[10](#page-11-7)[,11\]](#page-11-8). The reliability of WTs depends on correct maintenance management $[12,13]$ $[12,13]$. The localization and the environment conditions—together with the complexity of the WTs—drives maintenance operations to become complicated [\[14\]](#page-11-11). The main maintenance tasks, preventive and corrective, required to be done over the time [\[15\]](#page-11-12) are expensive and generate risks. The maintenance costs are between 12% and 23% of the $\frac{1}{2}$ and cost-reduction $\frac{1}{2}$. Good maintenance policies have been $\frac{1}{2}$. Good maintenance policies have been $\frac{1}{2}$. Njiri and Soeffker [\[6\]](#page-11-3) showed that WTs are employing new designs, electronic, materials, electrical, total costs [\[16,](#page-11-13)[17\]](#page-11-14).

WTs are monitored to improve the efficiency of maintenance management by supervisory control and data acquisition (SCADA) systems [\[18\]](#page-11-15). SCADA integrates all measurements by sensors and measurement systems. SCADA monitors signals and alarms with a range acquisition period per minute or per ten minutes. Alarm activations display anomalies or failures detected by the sensors, though they may induce false alarms due to incorrect analysis or non-defined failures [\[19\]](#page-11-16). Since these failures $\frac{1}{2}$ reduce system accuracy, novel algorithms for false alarm detection and identification are needed [\[11\]](#page-11-8). The generation of false alarms by a SCADA system is a fundamental issue due to unnecessary stops, false interventions by the maintenance team and loss of productivity [\[20,](#page-11-17)[21\]](#page-11-18). Several researches are based on the detection and reduction of WTs false alarms by different advanced analytics [\[22,](#page-11-19)[23\]](#page-11-20). Condition monitoring system (CMS) is used to reduce the false alarms rates. CMS leads to apply predictive maintenance policies $[24]$.

A maintenance strategy more employed is the so-called condition-based maintenance (CBM), i.e., maintenance based on the diagnosis of a WT to intervene only if the equipment requires it [\[4\]](#page-11-1). This optimizes the time employed on maintenance, additional costs to maintenance and equipment reliability [\[25](#page-11-22)[–27\]](#page-12-0). Many of these tasks involve the replacement of certain components due to the exhaustion of their estimated useful life [\[28](#page-12-1)[–30\]](#page-12-2). The strategy based on the prior analysis of the equipment condition before deciding which interventions to carry out is a successful and optimal α for equipment related to electricity conoration $\left[31,32\right]$. There are different toolniques to strategy for equipment related to electricity generation [\[31,](#page-12-3)[32\]](#page-12-4). There are different techniques to monitoring the WT performance, such as ultrasound, thermography, radiography, acoustics emissions, etc. [\[33,](#page-12-5)[34\]](#page-12-6).

The methodologies for fault detection and diagnosis in WTs are classified into model or data type [\[5](#page-11-2)[,35](#page-12-7)[,36\]](#page-12-8). The method analysis uses mathematical models developed with the comprehension of the physical behavior of the WT [\[37\]](#page-12-9). The volume and number of variables provided by the CMS involve different types of analysis for extracting the real condition of the WT [\[15\]](#page-11-12). Fault tree analysis (FTA) is a qualitative analysis for representing graphically the connections between the conditions and effects of the component faults [\[38\]](#page-12-10). Binary decision diagrams (BDD) on fault tree (FT) allow the quantitative analysis and the identification of the critical components of each WT, identifying the critical risks [\[39](#page-12-11)[,40\]](#page-12-12). BDD is data structure employed to show a Boolean function, which facilitates scalable constructions of Boolean functions using reversible logic gates [\[41\]](#page-12-13).

Quantitative techniques are obtained by mathematical models from the probabilities of the events [\[42,](#page-12-14)[43\]](#page-12-15). The analysis purposed in this study estimates the probability of the top event taking into consideration the conditions of the main components. A quantitative analysis is done employing the BDD analyzing the Boolean function. The computational cost is reduced employing the event ranking methods: top-down-left-right, level, AND, breadth-first-search and depth-first-search. The importance measures (IM) are obtained by the Birnbaum and criticality methods, i.e., the results are validated by both methods. The reliability analysis aims to achieve an efficient maintenance strategy to keep the unreliability of the system below of a desired threshold. To achieve this aim, it is essential to define two factors: when the repairs should be made and the components that should be repaired. The first one is determined by the intersection between the unreliability of the system and the threshold. The second one is obtained by IMs (IMs): Birnbaum or criticality. An iterative process is suggested to define a strategy able to ensure a correct reliability for a certain period of time.

The main novelties presented in this study are:

- An optimization of the maintenance management is employed based on IMs;
- An iterative process is suggested to define a strategy to ensure a correct reliability for a certain period of time.

Section [2](#page-2-0) introduces the FTs and BDDs. A novel dynamic analysis is proposed in Section [3.](#page-6-0) The IMs are shown and discussed in Section [4.](#page-7-0) The new procedure for maintenance is described in Section [5.](#page-9-0) Finally, Section [6](#page-10-2) presents the main conclusions.

2. FTs and BDD for Reliability Analysis

2.1. Background

FTs are a common approach for analyzing a whole system by considering all the main components that compound the system. The components, also known as elements, are related by the logical gates or logical operators "AND" and "OR". It can be also included other logical operators, but only these ones will be used in this study. The components together with the logical operators will compound the FTs [\[44\]](#page-12-16).

The top event analysis is done by quantitative evaluation, where the main methods can be classified as direct evaluation methods and methods based on the use of prime implicant (PI) sets. The conventional methods show some drawbacks, for example, the FT size and the complexity of the FT. It leads to high computational costs and some methods cannot be applied due to the complexity of the problem.

Li et al. [\[45\]](#page-12-17) showed that there are similar approaches to FTA, such as reliability block diagrams (RBD) and Bayesian networks [\[46\]](#page-13-0). They suggest automatic transformation methods for converting the function principle graphs, e.g., Markov models [\[47\]](#page-13-1), to FTs [\[48](#page-13-2)[,49\]](#page-13-3) or RBDs [\[50\]](#page-13-4). The dynamic FT (DFT) or dynamic RBD can be transformed into a dynamic Bayesian network to estimate the reliability [\[51–](#page-13-5)[53\]](#page-13-6).

Large combinations of AND/OR gates make calculations difficult and increase the computational cost. Rauzy employed methods based on BDDs to obtain the IMs with exact results [\[54,](#page-13-7)[55\]](#page-13-8). BDDs present the following advantages [\[56\]](#page-13-9):

- The computational cost is independent of the number of PIs and the way in which the FT is built;
- All the PIs are taken into account; they provide exact qualitative and quantitative information;
- The computational speed is between 100–1000 times higher than using classic methods;
- Typical operators of Boolean algebra can be evaluated with quadratic complexity;
- The cost of the analysis using BDD depends on the FT size;
- Large Boolean functions can be represented with relatively small diagrams;
- Operations with "products" over the time are linear with respect to the BDD size;
- Great efficiency in the treatment of non-coherent FTs.

2.2. Case Study

The approach was employed to analyze the generator, electrical and electronic components that are installed inside the nacelle. Faults in generators can be the result of electrical or mechanical causes [\[57\]](#page-13-10). The main electrical faults are due to open-circuits or short-circuits in the rotor or stator [\[58\]](#page-13-11) that could cause overheating [\[37\]](#page-12-9). Previous research works have demonstrated that bearings involve a high failure rate in WTs [\[59\]](#page-13-12). The bearings failures of the generator are usually caused by cracks, asymmetry and imbalance [\[60\]](#page-13-13). Short-circuit, open-circuit and gate-drive circuit faults are the three major electrical faults of the power electronics and electric controls in WTs [\[39\]](#page-12-11). Table [1](#page-3-0) shows the main elements and failures in the generator, electrical and electronic components.

Figure [2](#page-4-0) shows the FT from Table [1](#page-3-0) for a WT. It has twelve basic components and ten non-basic components. Basic components are not possible to be broken down into simpler causes connected by the logical gates. The FT shown in Figure [2](#page-4-0) has six 'OR' gates and three 'AND' gates. A qualitative analysis can be done to the FT because the main components and their relationships are represented.

Table 1. Main faults in the converter, electrical and electronic components and generator, based on [\[37\]](#page-12-9). c1–c2 and g1–g10 are the nodes of the fault tree (FT) in Figure [2.](#page-4-0)

The quantitative analysis in this study is done by the Boolean expression given by the FT—that is obtained by the BDDs. Lee [\[61\]](#page-13-14) introduced the BDD; it was popularized by Moret [\[62\]](#page-13-15), Akers [\[63\]](#page-13-16) and Bryant [\[64\]](#page-13-17). BDDs are used to obtain the Boolean functions, leading to obtain the mathematical expression to the problem by employing, for example, the Karnaugh maps or truth tables [\[65\]](#page-13-18). BDD provides the cut-sets (CS), paths of the BDD "from the top to the one" where the unreliability of the system could be achieved from them. The computational cost is given by the size of the BDDs [\[66\]](#page-13-19).

Figure 2. Fault tree example for a wind turbine (WT) (based on [37]). **Figure 2.** Fault tree example for a wind turbine (WT) (based on [\[37\]](#page-12-9)).

It depends on the order of the events. There is not any exact method to order the events optimally. This study considers the following methods for validating the raking of the events:

- and B_0 are used to obtain the Boolean functions, leading the mathematical the mathematical the mathematical the mathematical the mathematical theorem is a set of α • The "top-down-left-right" method (TDLR) orders the events in a top-down and then left-right way in the FT to provide a ranking of the events. At each level, the events order is initialized from $\frac{1}{2}$ left to right and the events found are set in this order $[67]$;
- The "depth-first-search" method (DFS) orders from top to down of a root and each sub-tree works from left to right, being a non-recursive procedure where all new expanded nodes are added by last-input last-output process [\[68\]](#page-13-21);
- The "breadth-first-search" method (BFS) orders the events by the first-input first-output (FIFO) method; A queue list, named "open", is employed to consider the events not included by the FIFO $f(x)$ method $[69]$; $f(x)$ is order $[67]$; $f(x)$ is order $[67]$; $f(x)$ is order $[67]$; $f(x)$ is order $[x]$; $[x]$
- The "level" method orders the events regarding to the level where the events are located, being the level set by the AND gates number that there are from the event to the top event. The event that $\frac{1}{2}$ appears early in the tree will have bighest pri appears early in the tree will have highest priority in case that two or more events have the same
lovel [70] level [\[70\]](#page-14-0);
- The "AND" method assigns the order of the events according to the AND gates that the event FIFO THIS INCORDING ASSIGN THE STACK OF THE STEED AND ACCEPTAING TO THIS GATES THAT THE SYSTEM THAT THE STEED AND THE STACK OF THIS GATES IN THE SYSTEMS. Basic events with the highest number of "and" gates will be ranked at the end. In the case of duplicated basic with the highest number of "and" gates will be ranked at the end. In the case of duplicated basic events, the event with less "and" gates number that the event. The the event of the predict basic events, the event with less "and" gates has priority; Finally, basic events with the same number of t_{real} appears event appears with $\frac{1}{2}$ have $\frac{1}{2}$ have the tree will have the tree will have the tree t_{real} "and" gates can be ranked as the TDLR method approach [\[71\]](#page-14-1);

The above ranking methods were applied to the FT shown in Figure [2.](#page-4-0) The CSs obtained are presented in Table [2.](#page-5-0)

Ranking Method TLDR DFS BFS Level AND Number of CSs 38 22 23 26 23

Table 2. Number of cut-set about the FT from Figure [2.](#page-4-0)

The probability of a system is given by the sum of each analytic expression of the CSs due that the CSs are mutually exclusive, i.e., the unreliability of the system is the sum of probabilities of all the BDD paths [\[61–](#page-13-14)[63\]](#page-13-16). It can be also computed in the BDD [\[53\]](#page-13-6). The main advantage of a quantitative analysis using BDDs is the implicit formulation. Coudert (1994) proposed the use of the term "metaproducts" to develop implicit calculations of the BDDs [\[72\]](#page-14-2). Each cut set is a path from a terminal node with value 1 until the top node. The CS are mutually exclusive paths. It is necessary to consider the occurrence of some events and the non-occurrence of others to evaluate the probability of each CS. The CSs are obtained from the BDD graph, which is constructed via Shannon decomposition, where each non-terminal node has an occurrence branch (left branch) and a non-occurrence branch (right branch). These negated variables appear in those paths that go through any "non-occurrence branch" [\[73,](#page-14-3)[74\]](#page-14-4). BDD has the following probabilities of each 22 cut-sets obtained by applying the DFS method (see Table [2\)](#page-5-0), where *qi* is the probability of failure of the component *i*:

 $CS_1: q_6 q_1$

CS₂: q_7 (1– q_6) q_1 CS₃: q₁₀ (1–q₇) (1–q₆) q₁ CS₄: q₁₂ q₁₁ (1–q₁₀) (1–q₇) (1–q₆) q₁ CS₅: $q_6 q_2 (1-q_1)$ CS₆: q₇ (1−q₆) q₂ (1−q₁) CS₇: q_{10} (1– q_7) (1– q_6) q_2 (1– q_1) CS₈: q₁₂ q₁₁ (1–q₁₀) (1–q₇) (1–q₆) q₂ (1–q₁) CS₉: q₆ q₃ (1–q₂) (1–q₁) CS₁₀: q_7 (1– q_6) q_3 (1- q_2) (1- q_1) CS₁₁: q_{10} (1- q_7) (1- q_6) q_3 (1- q_2) (1- q_1) CS₁₂: q₁₂ q₁₁ (1–q₁₀) (1–q₇) (1–q₆) q₃ (1–q₂) (1–q₁) CS₁₃: q₆ q₄ (1–q₃) (1–q₂) (1–q₁) CS₁₄: q_7 (1– q_6) q_4 (1– q_3) (1– q_2) (1– q_1) CS₁₅: q_{10} (1–q₇) (1–q₆) q_4 (1–q₃) (1–q₂) (1–q₁) CS₁₆: q₁₂ q₁₁ (1-q₁₀) (1-q₇) (1-q₆) q₄ (1-q₃) (1-q₂) (1-q₁) CS₁₇: $q_{10} q_7 (1-q_4) (1-q_3) (1-q_2) (1-q_1)$ CS₁₈: q₈ (1–q₁₀) q₇ (1–q₄) (1–q₃) (1–q₂) (1–q₁) CS₁₉: q₉ (1–q₈) (1–q₁₀) q₇ (1–q₄) (1–q₃) (1–q₂) (1–q₁) CS₂₀: q₁₂ q0₁₁ (1–q₉) (1–q₈) (1–q₁₀) q₇ (1–q₄) (1–q₃) (1–q₂) (1–q₁) CS₂₁: q_{10} (1– q_{7}) (1– q_{4}) (1– q_{3}) (1– q_{7}) (1– q_{1}) CS₂₂: q₁₂ q₁₁ (1–q₁₀) (1–q₇) (1–q₄) (1–q₃) (1–q₂) (1–q₁)

BDD associated with the FT from Figure [2](#page-4-0) is shown in Figure [3.](#page-6-1)

Figure 3. BDD of the FT from Figure 2[, o](#page-4-0)btained by the depth-first-search (DFS) method (see Table **Figure 3.** BDD of the FT from Figure 2, obtained by the depth-first-search (DFS) method (see Table [2\)](#page-5-0).

3. Dynamic Analysis

Time-dependent unreliability functions are considered in this study to describe the behavior of the main components over the time. The aim of these models is to bring probability function of unreliability as close as possible to a real case study. The functions considered are:

- a. Constant unreliability The probability of the events or components is constant over the time. $Q(t) = K$, where K is a constant valued between 0 and 1.
	- The probability of the events or components is constant over the time. **b.** Ex**ponential increasing unreliability** The probability function assigned is defined in Equation (1):

$$
Q(t) = 1 - e^{-\lambda t},\tag{1}
$$

where λ is a parameter that takes only positive values and determines how quickly the unreliability increases.

c. Linear decreasing reliability The probability function is defined in Equation (2):

$$
Q(t) = 1 - mt,
$$
\n(2)

where *m* determines how quickly the unreliability decreases. This model could be acceptable for infant failures of those components that are in the decreasing failure rate of their lifecycle.

d. Periodic unreliability The unreliability of the components has a periodic behavior. The expression used for this assignment is given by Equation (3) : **d. Periodic unreliability**

$$
Q(t) = 1 - e^{-\lambda(t - n\alpha)}
$$
\n(3)

with $n = 1, 2, 3...$, where:

- λ is a parameter that takes only positive values and determines the velocity of the unreliability rising.
- α is a parameter that determines the size of the period

Several unreliability models were considered for each component to analyze the FT in Figure [2.](#page-4-0) The most important parameters are shown in Table [3.](#page-7-1) Several unreliability models were considered for each component to analyze the FT in Figure 2. The most important parameters are shown in Table 3.

Components	Probability Model	Parameters
Component 1	Constant	$K = 0.5$
Component 2	Exponential increasing	$\lambda = 0.2$
Component 3	Constant	$K = 0.025$
Component 4	Periodic	$\lambda = 0.51, \alpha = 2$
Component 5	Exponential increasing	$\lambda = 0.4$
Component 6	Constant	$K = 0.01$
Component 7	Exponential increasing	$\lambda = 0.25$
Component 8	Linear decreasing	$m = 0.16$
Component 9	Constant	$K = 0.09$
Component 10	Periodic	$\lambda = 0.46$, $\alpha = 1.5$
Component 11	Linear decreasing	$m = 0.16$
Component 12	Periodic	$\lambda = 0.7$, $\alpha = 0.8$

Table 3. Unreliability models. **Table 3.** Unreliability models.

Figu[re](#page-7-2) 4 shows the unreliability of each component obtained in 50 samples (units of time). Ten samples were considered for each unit of time. The methods used to perform the qualitative and quantitative analysis on the BDD are shown in reference [\[56\]](#page-13-9). The dash lines represent the unreliability of the basic components. The solid black line shows the unreliability of the global system obtained by the BDD.

Figure 4. Unreliability of a system. **Figure 4.** Unreliability of a system.

Figure [4](#page-7-2) also allows to obtain a first approach to the importance of components within the global Figure 4 also allows to obtain a first approach to the importance of components within the global system. It can be seen that components 12 and 10 have an important influence into the system, where a direct relation between the own unreliability of these components and the unreliability of the global system can be observed. A sudden change in the unreliability of the components causes the unreliability of the system to change abruptly. Oppositely, it can be observed that the components whose unreliability is linear decreasing (Components 8 and 11), do not have a relevant importance within the global system.

A reliable measure of the importance of each component is required to determine it quantitatively.

4. Importance Measurement

IMs are employed to set the influence of each component over the FT. There are several methods for measuring the importance of components. This study will consider the most common: Birnbaum and
We allow the intervention of the intervention of the most common: Birnbaum and criticality. Further information about these and more IMs is possible to be found in reference [\[7\]](#page-11-4).

Birnbaum IM [\[75\]](#page-14-5) gives the value associated with the direct relation between the unreliability of the system and the corresponding component. It is defined in Equation (4) as follows:

$$
I_k^{Birn} = \frac{\partial Q_{system}}{\partial Q_k},\tag{4}
$$

where: where:

- I_k^{Birn} is the Birnbaum IM value of the *k*th component;
- Q_{system}, is the unreliability of the system;
- Q_k , is the probability assigned to the *k*th component.

Figure [5](#page-8-0) shows a time-dependent Birnbaum IM for each component (event). This graph can be Figure 5 shows a time-dependent Birnbaum IM for each component (event). This graph can be useful in order to determine the most relevant component at any time. If repairs were necessary at useful in order to determine the most relevant component at any time. If repairs were necessary at a a certain moment, this solution set offers a ranking for the components that should be repaired or replaced in first place. For instance, if the unreliability of the system exceeds the established limit at placed in first place. For instance, if the unreliability of the system exceeds the established limit at sample 2, it can be observed easily that component 7 should be repaired or replaced in first place. sample 2, it can be observed easily that component 7 should be repaired or replaced in first place.

Figure 5. Time-dependent Birnbaum: time in seconds.

itself. This can lead to consider a major importance than it should be for components with a low probability of occurrence. criticality IM [76], unlike Birnbaum, has into account the probability of occurrence of the event itself. It rectifies the drawbacks presented in Birnbaum IM, balancing the values obtained. It receptions were denoted in Birnbaum IM, balancing the drawbacks presented in Birnbaum IM, balancing the drawbacks presented in Birnbaum IM, balancing the drawbacks presented in Birnbaum IM, balancing th A disadvantage of Birnbaum IM is that it does not consider the unreliability of the component

It is characterized in Equation (5):

$$
I_{k}^{Crit} = \frac{Q_{k}}{Q_{system}} \cdot \frac{\partial Q_{system}}{\partial Q_{k}} = \frac{Q_{k}}{Q_{system}} \cdot I_{k}^{Birn}
$$
(5)

where: where:

- I_k^{Crit} is the Birnbaum IM of the *k*th component;
- \bullet Q_k is the probability assigned to the *k*th component;
- \bullet \quad $\mathbf{Q}_{\text{system}}$ is the unreliability of the system.

Figure [6](#page-9-1) shows how criticality provides a different perspective than the one showed by Birnbaum IM, even though both are connected. It is important to note that there are components that had great Birnbaum Importance and Low criticality Importance. This means that mentioned components are essential for the system to work, but their unreliability values are so insignificant that no repairs are recommended upon them.

Figure 6. Time-dependent ccriticality: time in seconds.

5. Procedure for Maintenance

Applying temporary variables allows determining operational strategies that will raise the reliability of the system. It will also lead to the following issues:

- To determine the reliability of the system and its components at a certain moment;
- To identify critical operating states of the system and its components;
- To determine the optimal time to carry out a preventive task and to choose the components to be repaired or replaced; the optimal time task and to choose the components to choose the components
- \overline{a} determine the repairs $\frac{1}{\sqrt{1-\frac{1$ $f(x) = f(x)$ • To determine the repairs or replacements necessary to ensure a certain reliability of the system for a period of time.

Firms frequently need to guarantee certain reliability for their systems or products because a reliability can lead to unprofitable situations. For instance, the image of a firm could be seriously low reliability can lead to unprofitable situations. For instance, the image of a firm could be seriously affected by unreliable products. For this reason, firms usually establish a degree of reliability for their systems or products. Figure [7](#page-10-3) shows a simple threshold (dash line) for unreliability of the WT depicted in Figure [2.](#page-4-0) The first intersection between the two lines provides the limit that the system has an acceptable unreliability rate. This point also fixes the moment in which certain repairs should be done to maintain an acceptable unreliability. Once this point was localized (time = 0.7 in Figure [7\)](#page-10-3), then next to maintain an acceptable unreliability. Once this point was localized (time = 0.7 in Figure 7), then next do maintain an acceptable unreliability. Once this point was localized (time = 0.7 in Figure 7), then next
step is to select the components to repair from the IMs obtained previously. Once components were then next step is to select the components to repair from the IMs obtained previously. Once compo-repaired or replaced, the unreliability will be acceptable again. This iterative process constitutes a good nents were repaired or replaced, the unreliability will be acceptable again. This iterative process con-strategy for ensure a certain reliability of the system for a certain period of time. Firms frequently need to guarantee certain reliability for their systems or products because a low

Moreover, the identification of maximum unreliability points allows determining the degree of criticality by evaluating the distance between these points and the corresponding threshold.

Figure 7. Unreliability threshold for a WT. **Figure 7.** Unreliability threshold for a WT.

 \mathcal{M} more ontain of maximum unreliability points allows determining the degree of \mathcal{M} **6. Conclusions**

This study presents a novel approach to facilitate quantitative reliability analysis of complex method and applied to a case study in WT. FTs are used to depict the operation of a system and the logical interrelations between its components. Building a FT requires a profound knowledge of the system, but it is a useful tool to make a previous qualitative analysis. BDDs are used for carrying out quantitative analysis, where they provide a function of the unreliability of the global system. This function depends on the unreliability of the components that compose the system. Different failure probability distributions (Section 3) are used in this study to model the behavior of these components. The reliability analysis aims to achieve an efficient maintenance strategy to keep the unreliability of the system below a desired threshold. It is necessary to define two factors to achieve this: when repairs should be made, and which components that should be repaired. The first is determined by the intersection of the unreliability of the system and the threshold. The second is obtained from IMs: Birnbaum or criticality. An iterative process is suggested to define a strategy able to ensure a correct reliability for a certain period of time. $\begin{array}{c}\n\frac{25}{120} \text{O.5} \\
\frac{25}{120} \text{O.8} \\
\frac{25}{120} \text{O.8} \\
\frac{25}{120} \text{O.9} \\
\frac{25}{120} \text{O.1} \\
\frac{25}{120} \text{O$ systems based on the qualitatively analysis. For this purpose, FTs and BDDs are presented as the

For future works, we propose considering and analyzing larger and more complex FT in WT and other systems and to study the efficiency of ranking methods employed in this study. New IM methods should be also considered. Therefore, this could improve the WT reliability assessment based Γ function Γ function Γ is Γ in Γ is a set of Γ in Γ in Γ is a set of Γ in Γ in Γ is a set of Γ in Γ i on the FTA.

and other systems and to study the efficiency of ranking methods employed in this study. New IM Author Contributions: Funding acquisition, Froject administration and Supervision, F.F.G.M., Data curation,
I.S.R. and A.P.M.; Visualization, F.P.G.M., I.S.R. and A.P.M.; Formal Analysis, Resources, F.P.G.M. and A.P.M. Investigation, F.P.G.M., I.S.R., A.P.M and B.M.-I.; Methodology, F.P.G.M., B.M.-I. and A.P.M.; Software and F.P.G.M. and B.M.-I. All authors have read and agreed to the published version of the manuscript. **Author Contributions:** Funding acquisition, Project administration and Supervision, F.P.G.M.; Data curation, Validation, A.P.M. and B.M.-I.; Writing—original draft, I.S.R., A.P.M. and B.M.-I.; Writing—review and editing,

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