

## Supplementary informations

**Table S1: Adsorption Kinetics parameters**

Temperature	$q_{e \text{ exp}} \text{ (mg g}^{-1}\text{)}$	Pseudo first order			Pseudo second order			
		$k_1 \text{ (min}^{-1}\text{)}$	$q_{e \text{ cal}} \text{ (mg g}^{-1}\text{)}$	$R^2$	$k_2 \text{ (min}^{-1}\text{)}$	$q_{e \text{ cal}} \text{ (mg g}^{-1}\text{)}$	$h \text{ (mg g}^{-1} \text{ min}^{-1}\text{)}$	$R^2$
298K	11.5146	0.0091	10.7894	0.9856	0.006133	13.2415	0.9298	0.9933
301K	15.9925	0.0020	14.7231	0.9376	0.002970	18.6428	0.9685	0.9907
303K	19.1910	0.0030	19.0107	0.9936	0.001454	23.5183	1.2431	0.9995
Elovich	$\alpha \text{ (mg/g min)}$	$\beta \text{ (g/mg)}$	$R^2$	Intraparticle Diffusion	$k \text{ (mg g}^{-1} \text{ min}^{-1/2}\text{)}$	$I \text{ (mg/g)}$	$R^2$	
298K	2.2234	0.3675	0.9956	298K	2.2593	0.9664	0.9628	
301K	2.0626	0.2373	0.9851	301K	1.6295	0.6964	0.9626	
303K	2.6344	0.1908	0.9986	303K	1.3677	0.5798	0.9597	

**Table.S2: Linear regression equation fit for adsorption kinetic**

System parameter	$k_2$ (g/mg min)	$q_e$ (mg/g)	$h$ (mg/g min)	$R^2$
Effect of <b>pH</b> for 153.52 ppm at 303 K.				
8	0.0111	11.9246	0.6287	0.9868
10	0.0056	13.2205	0.9819	0.9916
12	0.0014	23.5183	1.2431	0.9995
Effect of adsorbent <b>dose</b> for 153.52 ppm at 303 K.				
0.1g	0.0014	23.5183	1.2431	0.9995
0.15g	0.0053	14.4237	0.9024	0.9953
0.2g	0.0168	11.8343	0.4236	0.9827
Effect of Temperature for 153.52 ppm.				
298 K	0.0056	13.2205	0.9816	0.9961
301 K	0.0026	19.6889	1.0311	0.9922
303 K	0.0014	23.5183	1.2431	0.9995

Initial Dye concentration at 303K

51.17 ppm	0.0891	7.3051	0.2101	0.9994
102.35 ppm	0.0135	10.6997	0.6467	0.9991
128.0 ppm	0.0075	12.5015	0.8525	0.9923
153.52 ppm	0.0014	23.5183	1.2431	0.9995

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**Table S3: Adsorption equilibrium isotherm parameters**

Isotherm	Temperature	Parameters		
		$K_F$	$n$	$R^2$
Freundlich	298	0.5127	1.47732	0.98436
	301	0.28904	1.1070	0.9909
	303	0.26242	1.03032	0.9969

  

Isotherm	Temperature	Parameters		
		$K_L$ (L mg <sup>-1</sup> )	$q_m$ (mg g <sup>-1</sup> )	$R^2$
Langmuir	298	0.008109	25.6673	0.9965
	301	0.001571	136.61	0.9972
	303	0.007248	350.877	0.9988

  

Isotherm	Temperature	Parameters		
		$K_T$	$b$	$R^2$
Temkin	298	0.0857	469.45	0.9882
	301	0.0673	282.242	0.9979
	303	0.0193	232.782	0.9426

  

Isotherm	Temperature	Parameters			
		$q_m$	$\beta$	$E$ (J/mol)	$R^2$
D-R	298	11.7970	$1.34301 \times 10^{-4}$	61.0162	0.9709
	301	16.5808	$1.4059 \times 10^{-4}$	59.635	0.9780
	303	18.9891	$1.18781 \times 10^{-4}$	64.880	0.9251

Isotherm	Temperature	Parameters		
		$A_{HJ}$	$B_{HJ}$	$R^2$
H-J	298	16.7336	2.0948	0.9453
	301	18.2049	1.9632	0.9290
	303	21.3857	1.9065	0.9314
Isotherm	Temperature	Parameters		
		$K_H$	$n_H$	$R^2$
Hasley	298	0.3728	1.4775	0.9843
	301	0.2522	1.1054	0.9912
	303	0.2616	1.0307	0.9909

**Table S4 Error analysis for Isotherm models.**

S. No	Error analysis for 153.52 ppm at 303 K					
<b>1. <u>Langmuir Isotherm</u></b>						
RMSE	X <sup>2</sup>	SSE	ARE	SAE	APE	MPSD
0.492	0.0261	0.484	0.0362	0.695	0.906	13.462
<b>2. <u>Freundlich Isotherm</u></b>						
RMSE	X <sup>2</sup>	SSE	ARE	SAE	APE	MPSD
0.424	0.0193	0.359	0.0312	0.599	0.781	12.498
<b>3. <u>Temkin Isotherm</u></b>						
RMSE	X <sup>2</sup>	SSE	ARE	SAE	APE	MPSD
0.915	0.0930	1.677	0.067	1.295	1.687	18.368
<b>4. <u>D-R Isotherm</u></b>						
RMSE	X <sup>2</sup>	SSE	ARE	SAE	APE	MPSD
1.664	0.257	5.540	-0.122	-0.253	-3.066	24.763
<b>5. <u>Halsey Isotherm</u></b>						

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RMSE	$X^2$	SSE	ARE	SAE	APE	MPSD
0.399	0.030	0.319	0.029	0.565	0.736	12.139

**6. H-J Isotherm**

RMSE	$X^2$	SSE	ARE	SAE	APE	MPSD
13.273	836.702	352.310	0.978	18.769	24.451	69.930

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