

Article

A 3rd-Order FIR Filter Implementation Based on Time-Mode Signal Processing

Orfeas Panetas-Felouris * and Spyridon Vlassis

Electronics Laboratory, Physics Department, University of Patras, 26504 Patras, Greece; svlassis@upatras.gr

* Correspondence: o.panetasfelouris@upnet.gr

Abstract: This paper presents the hardware implementation of a 3rd-order low-pass finite impulse response (FIR) filter based on time-mode signal processing circuits. The filter topology consists of a set of novel building blocks that perform the necessary functions in time-mode including z^{-1} operation, time addition and time multiplication. The proposed time-mode low-pass FIR filter was designed in a 28 nm Samsung fully-depleted silicon-on-insulator FD-SOI process under 1 V supply voltage with 5 MHz sampling frequency. Simulation results validate the theoretical analysis. The FIR filter achieves a signal-to-noise-plus-distortion ratio (SNDR) of 38.6 dB at the input frequency of 50 KHz consuming around 200 μ W.

Keywords: time-domain circuits and systems; pulse width modulation; time-mode signal processing circuits; FIR filter implementation



Citation: Panetas-Felouris, O.; Vlassis, S. A 3rd-Order FIR Filter Implementation Based on Time-Mode Signal Processing. *Electronics* **2022**, *11*, 902. <https://doi.org/10.3390/electronics11060902>

Academic Editors: Paolo Colantonio and Alessandro Cidronali

Received: 28 January 2022

Accepted: 11 March 2022

Published: 14 March 2022

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1. Introduction

In many modern integrated circuit applications, better speed and lower power consumption are important criteria. Because of the reducing device sizes and low voltage supply, these criteria are met utilizing cutting-edge complementary metal-oxide-semiconductor (CMOS) technologies. Unfortunately, due to smaller device sizes and low power supply, many prior analog circuit architectures, such as analog-to-digital converters, are more difficult to overcome the lower voltage headroom and the lower dynamic range

The time-domain technique is a relatively recent method of processing time that utilizes time delay, time difference or pulse width rather than voltage or current, as in traditional processing methods. As a result, in time-domain circuits and systems, time is the quantity of interest [1–3]. Even for such a scaled technology, time-domain design is a very promising design method since it offers a better trade-off between dynamic range and power consumption. The advantage of time-domain systems is that they use high-speed MOS devices, which means they have a shorter time delay and so process time with more precision [4–6].

The main advantages of the time-domain design approach are improved dynamic range and time resolution when compared to analog voltage or current mode circuits under the same low-supply environment [4–6] and better power efficiency for high-speed performance because they are primarily composed of CMOS digital building blocks (gates, etc.) [1].

Signal filtering is one of the most important functions in many state-of-the-art applications, such as biomedical sensor interfacing, image processing, wireless receivers, etc. Signal filtering, which is based on finite/infinite impulse response filter implementation (FIR/IIR), belongs among the basic signal processing operations in traditional discrete-time digital signal processing (DT-DSP).

FIR/IIR implementations require some fundamental operators, such as z^{-1} operators and signal adders, along with signal multipliers, for the implementations of the filter coefficients. Traditional FIR/IIR implementations are mainly based on pure digital design

approach and, therefore, can be categorized as discrete-time/discrete-signal processing systems. The circuit realization of the basic operators is achieved using flip-flops as delay element and digital logic gates for the implementation of the digital logic adders and multipliers.

The FIR/IIR counterpart implementations in time-mode require the basic operators to work in time domain which means that z^{-1} , adders [4,7,8] and multipliers [9,10] must be able to handle time-mode quantities [11]. These systems are categorized as discrete-time/continuous signal processing (DT-CSP) systems [12].

Few works about time-mode FIR/IIR or other time-mode filter implementations have been reported in the literature. A 2nd-order Butterworth and Chebyshev Type I time-mode filters have been presented in [13]. These implementations are based on time-mode signal processing circuits, which, unfortunately, cannot be used as separate modules leading to complicate configurations. A set of time-mode building blocks used to build a sampled-data 2nd-order low-pass IIR filter along with the methodology for the construction of higher-order systems are presented in [14]. A 3-tap FIR filter and a new way of analog computation using novel time-mode operator circuitries are presented in [12].

Our work proposes the implementation of a 3rd order sampled-data low pass time-mode FIR filter which is based on the novel time-mode multiplier and time-mode adder. Both circuits are based on the modification of a simple time register topology [15,16]. A 3rd order low-pass topology offers a satisfactory trade off between high-frequency rejection, chip area and current consumption. The proposed time-mode operators feature several advantages leading to robust FIR filter implementation: (a) low circuit complexity including few transistors, (b) high accuracy in time storing (c) synchronization with the reference sampling clock and (d) modular design. The main advantage of the proposed time-mode FIR compared with aforementioned state-of-the-art works is that it can be easily realized based on the topological diagram of the traditional FIR approach in voltage mode and substituting one-by-one the voltage-mode operators with the time-mode counterpart modular operators.

The paper is organized as follows. A brief presentation about time-mode signal processing and the definition of the time-mode operators presented in Section 2. The circuit modifications of the time register in order to build the multiplier and adder operators are described in Section 3. In Section 4, the proposed time-mode modules are presented and analyzed, while the FIR filter is analyzed in Section 5. The simulation results are reported in Section 6.

2. Time-Mode Signal Processing

The time-mode circuits and systems process the time difference between two consecutive pulses or the time width of a constant frequency pulse. This work will focus on the time processing approach that handles the pulse width of a constant frequency pulse. In Figure 1, a conceptual block diagram is presented.

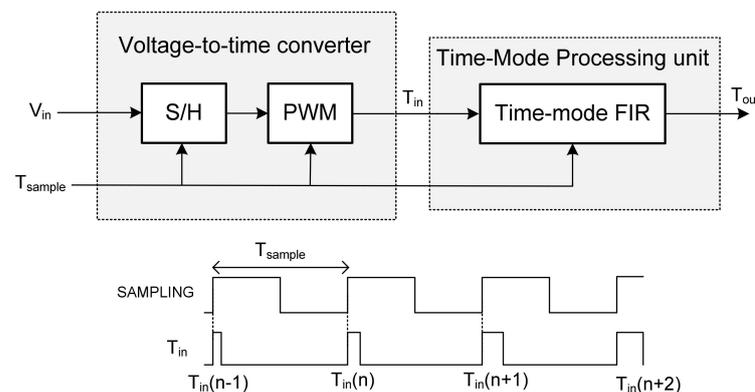


Figure 1. Block diagram of the voltage-to-time conversion followed by a time-mode processing unit.

The input signal V_{in} is converted to time-mode by using a sample/hold stage (S/H) and pulse width modulator (PWM). S/H is necessary for high-frequency input bandwidth and can be omitted for low-frequency input signals (e.g., signal which comes from sensor interfacing circuit). Based on the PWM technique, input voltage V_{in} will correspond to an input pulse width T_{in} of a constant frequency pulse [2,17] according to the next equation:

$$T_{in}[n] = k_{VT}V_{in}[n] \tag{1}$$

where k_{VT} is the voltage-to-time conversion factor, and n is the number of sample, while the constant frequency is assumed the sampling frequency $f_{sampling}$. It is clear that T_{in} can take continuous values according to Equation (1), but the time is discrete by mean of sampling time, and the corresponding system is considered a DT-CSP system [12]. Afterward, the signal is processed by the main time-mode systems, which is capable of handling the pulse widths of a pulse train.

One of the major building blocks embedded in continuous or discrete signal processing is the filters: analog filters or FIR/IIR filters. Despite implementation, filters must be capable of filtering out all the unwanted signals/components, which are corrupted with the signal or bandwidth of interest. From the time-mode point of view, any filter implementation is similar to FIR/IIR discrete filters mainly due the use of discrete sampling time.

This study will concentrate on the implementation of time-domain FIR filters. A FIR filter is a signal processing filter whose impulse response (or response to any finite length input) has a limited duration since it settles to zero in a finite time. Each value in the output sequence for a causal discrete-time time-mode FIR filter of order N is a weighted sum of the most recent input values [18]:

$$T_{OUT}[n] = b_0T_{in}[n] + b_1T_{in}[n - 1] + \dots + b_NT_{in}[n - N] = \sum_{i=0}^N b_iT_{in}[n - i] \tag{2}$$

where

- $T_{in}[n]$ is the input pulse width;
- $T_{out}[n]$ is the output pulse width;
- N is the filter order;
- b_i is the filter’s coefficient at the i -th instant for $0 \leq i \leq N$ of an N th-order FIR filter.

Therefore, the most important operators in the corresponding time-mode FIR filters will be the time-mode z^{-1} operators, time-mode multiplier and the time-mode adders. The block diagram of these operators in the time-mode are presented in Figure 2. The circuit implementations of the aforementioned operators will be described in the next sections.

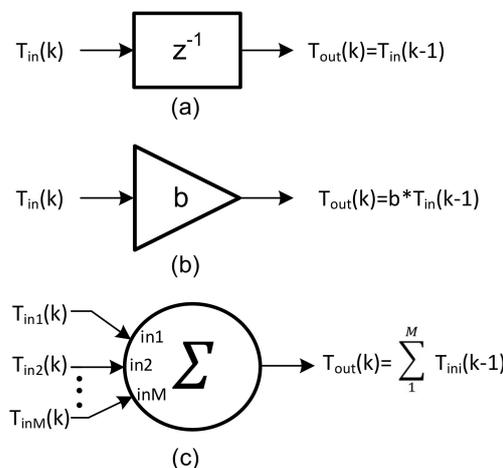


Figure 2. Time-mode operators (a) z^{-1} , (b) z^{-1} multiplier and (c) adder.

3. Multiplying and Adding Operations of the Time Register

Figure 3a shows the time register (TR), and Figure 3b shows its symbol. When $SET = 0$, transistor M_1 is turned on, and the capacitor voltage is set to V_{DD} (supply voltage). The capacitor discharges when transistor M_2 is ON, which is controlled by the OR gate. Through a digital calibration loop, the M_3 's gate voltage $CTRL$ may be utilized to calibrate the variance of the discharging slope [16]. To synchronize the output with CLK , the synchronization circuitry consists of an AND gate, a fast comparator [16] and an inverter. The comparator is designed to provide quick transient response, and its triple point voltage V_{tp} is set to match $V_{DD}/2$ [16].

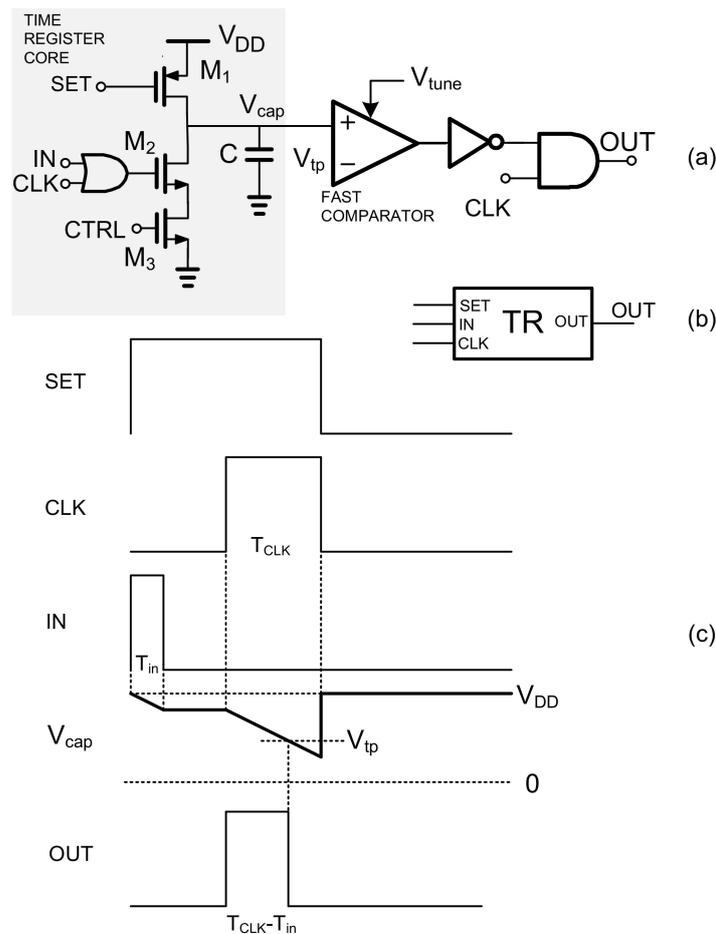


Figure 3. (a) Time register circuit, (b) symbol and (c) timing diagram.

Figure 3c shows a time diagram of a time register that describes the synchronization procedure. The SET signal's time interval T_{CLK} is a pulse with a fixed pulse width and a 25% duty cycle. The capacitor voltage remained constant when both IN and CLK are 0. The larger the pulse width T_{in} of the IN signal, the more discharging time due to T_{in} appeared, considering that the discharging time due to CLK stays the same.

The output is a pulse with width equal to $T_{CLK} - T_{in}$, allowing the value of T_{in} to be stored, while the output pulse is synchronized with the CLK signal.

Using the aforementioned time register circuit, the circuit can store the time interval of an input pulse and amplify the pulse width by a gain factor. The new circuit is called time amplifier and is presented in Figure 4. In this configuration, the operation of the OR gate is performed by the two-transistor branches $M_{a1}-M_{b1}$ and $M_{a2}-M_{b2}$. Transistors M_{a1} and M_{a2} have the same aspect ratio acting as switches. The aspect ratios of M_{b1} , M_{b2} are different, featuring a different discharging slope. Assuming that the channel widths of M_{b2} and M_{b1}

are $W_{b,2}$ and $W_{b,1}$, respectively, while both transistors have the same channel length. Then, intuitively, using Figure 3c, the discharging slope between T_{in} and T_{CLK} will be different. The discharging $slope_{in}$ that corresponds to T_{in} will be given by

$$slope_{in} = a * slope_{clk} \tag{3}$$

where a is the time gain and is given by

$$a = \frac{W_{b,2}}{W_{b,1}} \tag{4}$$

and $slope_{clk}$ is the discharging reference slope caused by T_{CLK} . Therefore, the output pulse width will be equal to

$$T_{OUT} = T_{CLK} - \frac{W_{b,2}}{W_{b,1}} T_{in} \tag{5}$$

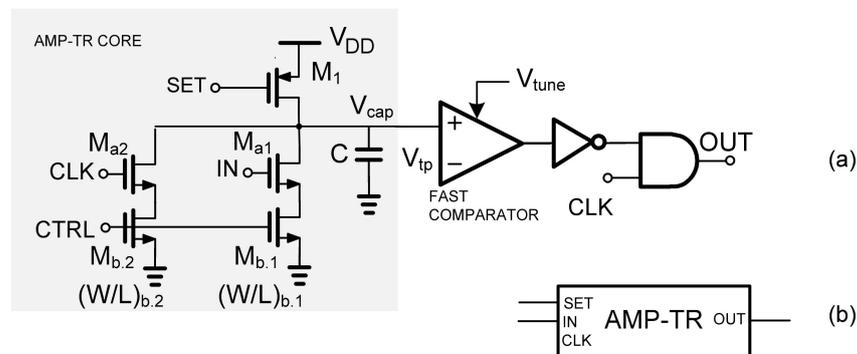


Figure 4. (a) Time amplifier based on time register circuit and (b) symbol.

A time adder circuit, which is based on the time register, is presented in Figure 5. A time adder simply adds the pulse widths $T_{in,1}, T_{in,2}, \dots, T_{in,n}$ of n number input pulses. Transistors $M_{b,1}, M_{b,2}, \dots, M_{b,n}, M_{b,n+1}$ have the same aspect ratio. Therefore, the discharging slope caused by $T_{in,1}, T_{in,2}, \dots, T_{in,n}$ will be given by

$$slope_{in,1,in,2,\dots,in,n} = slope_{in,1} + slope_{in,2} + \dots slope_{in,n} \tag{6}$$

and the output pulse width will be

$$T_{OUT} = T_{CLK} - (T_{in,1} + T_{in,2} + \dots T_{in,n}) \tag{7}$$

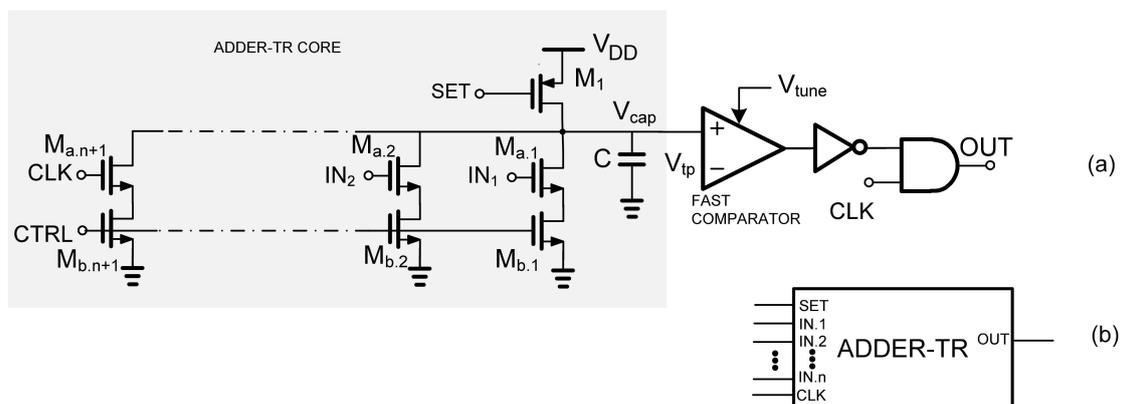


Figure 5. (a) Time adder based on time register and (b) symbol.

The main problem of the time register is the strong impact of the technology process (P) variations and chip temperature (T) variation (PT variations). The discharging slope of the capacitor voltage discharging shows variation over PT variations because of its dependency by the discharging drain current of a MOS device and the value on-chip capacitor. A digital calibration loop can be used in order to calibrate the discharging slope achieving better performance stability [16].

4. Time-Domain Modules

4.1. Time-Domain z^{-1} Circuit

The operation of the z^{-1} is to generate an output pulse with pulse width equal to T_{in} , which is synchronized with the sampling [16]. As discussed in the previous section, unfortunately a TR circuit can store the pulse width T_{in} of the input (IN) signal in the form of output pulses with pulse width equal to $T_{CLK} - T_{in}$, which is synchronized with CLK .

The proposed z^{-1} circuit is presented in Figure 6a, and the basic waveforms that explain its operation are illustrated in Figure 6b,c. A combination of four TR circuits in series realizes a z^{-1} circuit. The SAMPLING signal is assumed to be the SET1 signal of the TR1 circuit, and the input signal IN is equal to the input IN1 of TR1, while the final output signal OUT is the output of OUT4 of TR4.

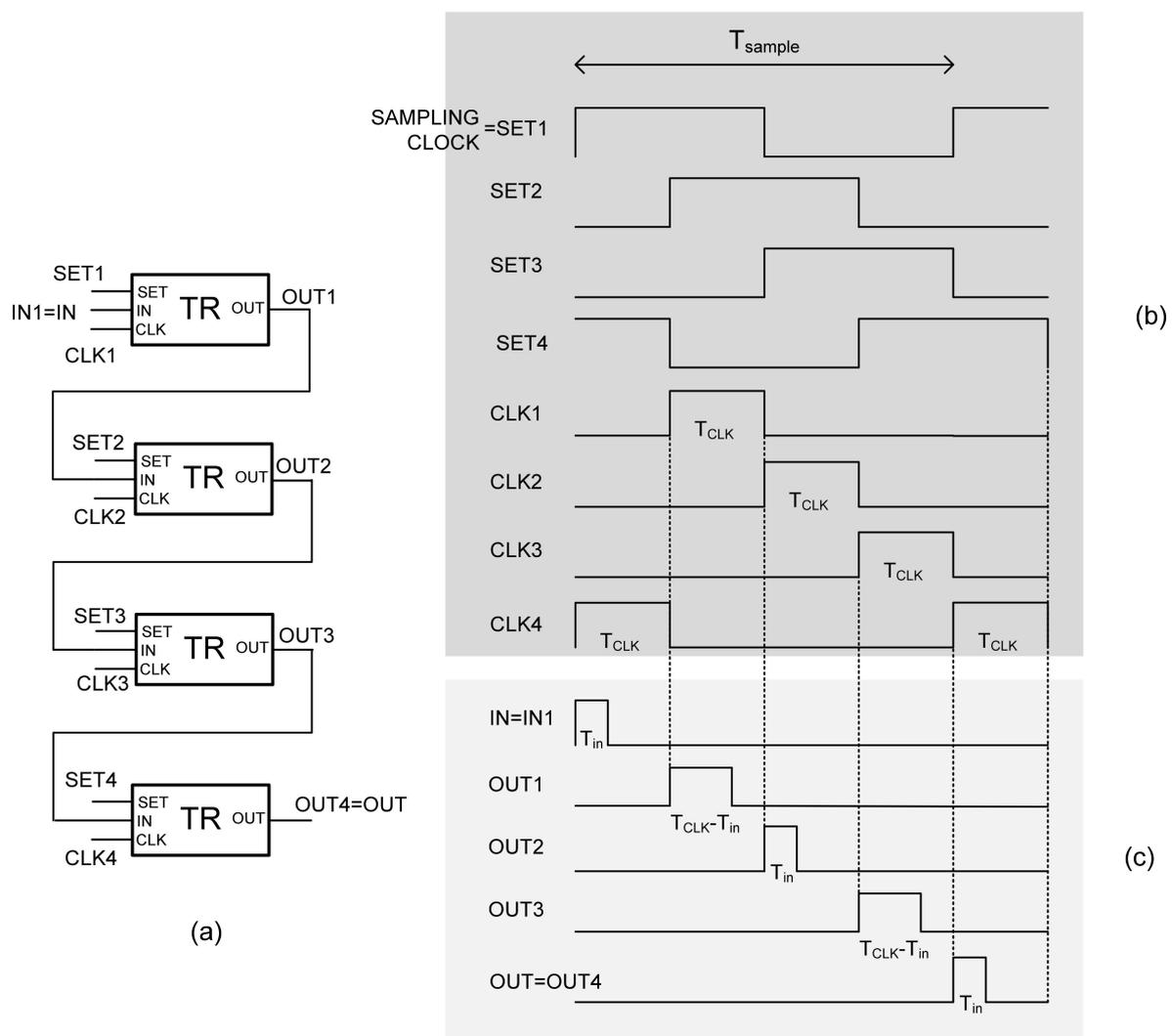


Figure 6. (a) Time-domain z^{-1} circuit, (b) clocks timing diagram and (c) pulses timing diagram.

To be synchronized with the *SET2* pulse, the *OUT1* pulse is generated at the rising edge of *CLK1*. After that, the *OUT1* was used as the TR's input. *OUT2* is synchronized with *CLK2*, and $T_{OUT2} = T_{CLK} - T_{OUT1} = T_{CLK} - (T_{CLK} + T_{in}) = T_{in}$. Therefore, *OUT2* is delayed by $T_{SAMPLING}/2$ in relation to the sampling signal. Based on the previous characteristic, the *OUT4* pulse is delayed by $T_{SAMPLING}$ and its width value is T_{in} . Taking this into account, the z^{-1} operator is produced by utilizing four TR in a cascade placement.

4.2. Time-Mode z^{-1} Multiplier

The operation of a time-mode z^{-1} multiplier is to produce an output pulse with pulse T_{out} width equal to bT_{in} , where T_{in} is the input pulse and a is the multiplication coefficient, and the output pulses will be synchronised with the sampling signal and delayed by one clock cycle.

The proposed time-mode z^{-1} multiplier is presented in Figure 7a. The pulses timing diagram that explains its operation is illustrated in Figure 7b. Moreover, the clock's timing diagram is the same as that of time-mode z^{-1} circuit as it is illustrated in Figure 6. The combination of two AMP-TR and two TR circuits series realizes a time-mode z^{-1} multiplier. The *SAMPLING* signal is assumed to be the *SET1* signal of the AMP-TR₁ circuit, and the input signal *IN* is equal to the input *IN1* of AMP-TR₂, while the final output signal *OUT* is the output of *OUT4* of TR₂. AMP-TR₁ and AMP-TR₂ generate time amplification equal to a_1 and a_2 , respectively.

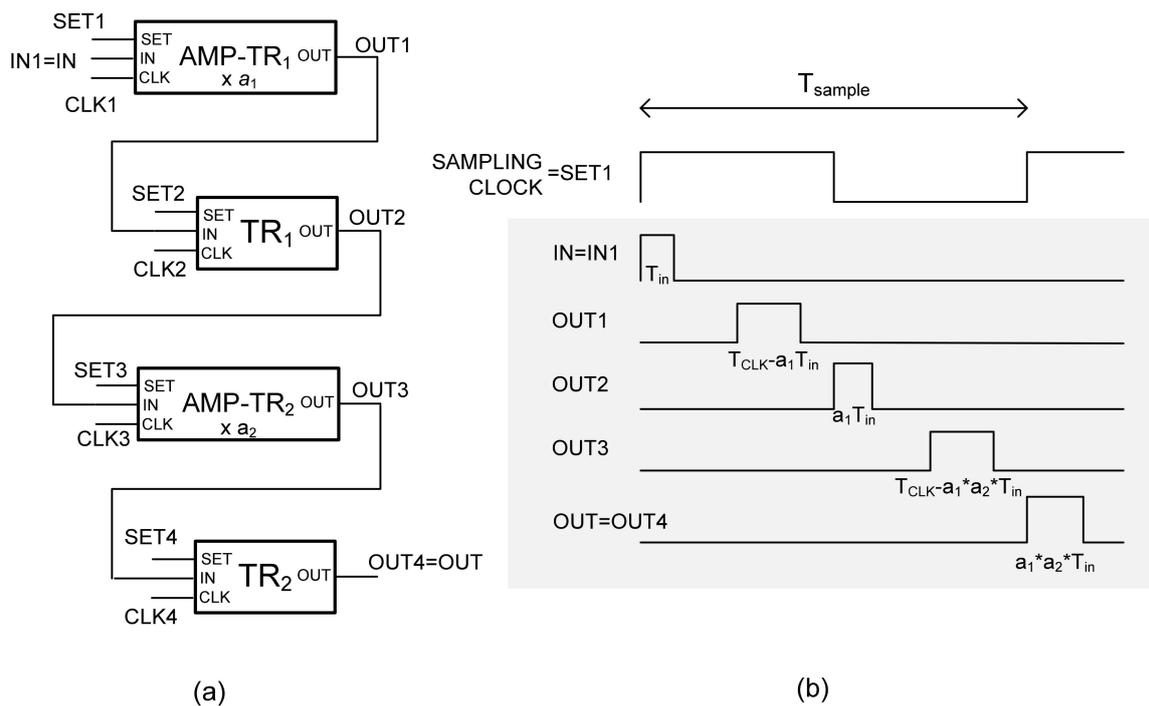


Figure 7. (a) Time-mode z^{-1} multiplier circuit, (b) pulses timing diagram.

The *OUT1* pulse is generated at the rising edge of *CLK1* in order to be synchronized with the *SET2* pulse. Afterwards the *OUT1* was used as input for the TR₁. So, $T_{OUT2} = T_{CLK} - T_{OUT1} = T_{CLK} - (T_{CLK} - a_1T_{in}) = a_1T_{in}$, and *OUT2* is synchronized with *CLK2*. Therefore, *OUT2* is delayed by $T_{SAMPLING}/2$ in relation to the sampling signal. Expanding on the previous characteristic, *OUT4* is delayed by T_{SAMPLE} , and the synchronized output pulse features a pulse width that is given by

$$T_{OUT} = bT_{in} \tag{8}$$

where the multiplication coefficient will be equal to $b = a_1a_2$.

It should be mentioned here that the use of two-time amplification operations through the standard time-mode z^{-1} multiplier operation is very important. We have more degrees of freedom for the approximation of the FIR filter coefficient by using the product of two amplifications $a_1 a_2$, compared with the single amplification a_1 or a_2 .

4.3. Time-Mode z^{-1} Adder

The time-domain z^{-1} adder can add the pulse width of several input signals and produce an output that is the sum of all the input time intervals. As an example, a two inputs time-domain z^{-1} adder is depicted in Figure 8a. The z^{-1} adder consists of ADDER-TR₁ and three time registers (TR) in series. The pulses timing diagram that explains its operation is illustrated in Figure 8b. Again, the clock's timing diagram is the same as that of the time-mode z^{-1} circuit as it is illustrated in Figure 6c.

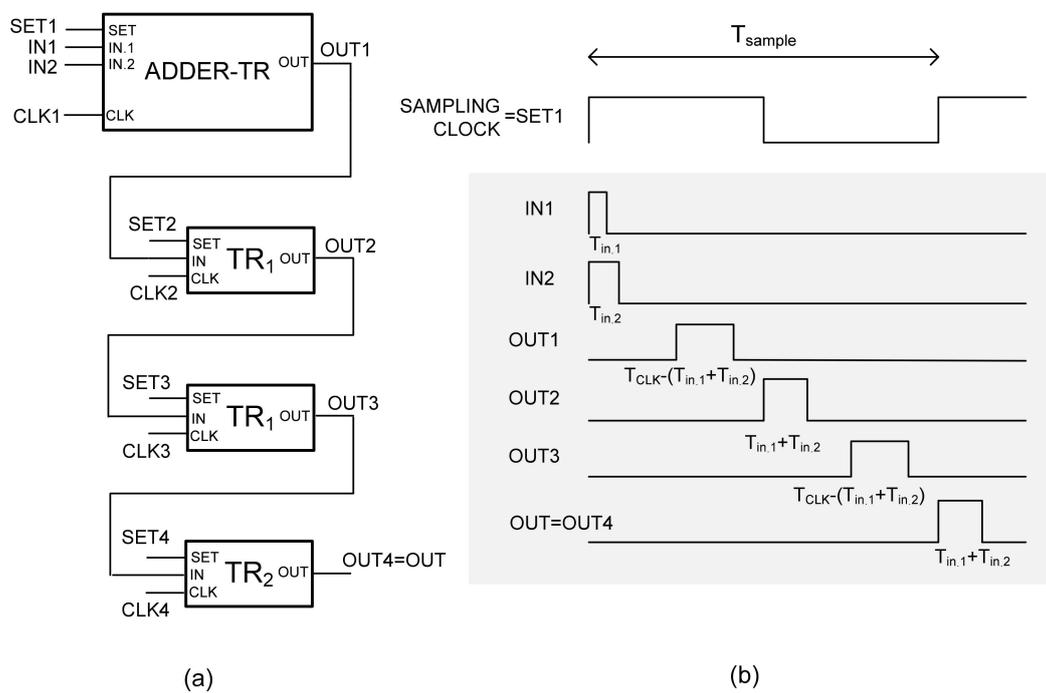


Figure 8. (a) Example of two inputs time-mode z^{-1} adder and a (b) pulses timing diagram.

The OUT1 pulse is generated at the rising edge of CLK1 in order to be synchronized with the SET2 pulse and has the value of $T_{OUT1} = T_{CLK} - (T_{in1} + T_{in2})$. Afterwards, the OUT1 was used as input for the next TR. So, $T_{OUT2} = T_{CLK} - T_{OUT1} = T_{CLK} - (T_{CLK} - (T_{in1} + T_{in2})) = T_{in1} + T_{in2}$, and OUT2 is synchronized with CLK2. Therefore, OUT2 is delayed by $T_{SAMPLING}/2$ in relation to the sampling signal. Then, the signal just passes through the next two TRs in order to acquire a delay of one cycle. The pulse width of the output pulse will be given by

$$T_{OUT} = T_{in1} + T_{in2} \tag{9}$$

and, therefore, the adding function is realized.

5. Time-Domain 3rd Order FIR Filter

In this work, a rectangular 3rd-order FIR filter had been designed in order to prove the concept of time-mode filtering using the proposed time-domain z^{-1} multiplier and adder. The realization follows the topology of Figure 9, which uses three z^{-1} operators, four z^{-1} multipliers and one 4-input z^{-1} adder. Table 1 shows the ideal filter coefficients, the approximation values and the final coefficient realizations. As was already mentioned, the use of two amplification operations can help in the better approximation of the filter

coefficients. Only three gain amplifier factors are necessary, 0.3, 0.4 and 0.7, in order to approximate the exact coefficient values of b_0 , b_1 , b_2 and b_3 . The worst-case approximation error is less than 10%.

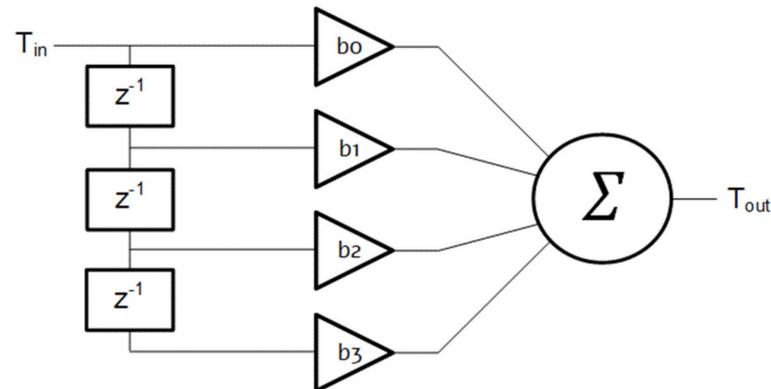


Figure 9. Implementation of 3rd order FIR filter with time-mode processing units.

Table 1. FIR filter coefficient values.

Coefficient	Exact Value	Approximate Value	Realization $\alpha_1 \times \alpha_2$
b_0	0.2330	0.21	0.3×0.7
b_1	0.2669	0.28	0.4×0.7
b_2	0.2669	0.28	0.4×0.7
b_3	0.2330	0.21	0.3×0.7

6. Results

In the following section, the performance of the proposed circuits is presented. All circuits are designed and verified by simulation in Samsung 28 nm FD-SOI CMOS technology with a supply voltage $V_{DD} = 1$ V. The voltage triple point of comparator was adjusted to be 0.5 V using an appropriate triple-point compensation circuitry [15]. Considering that the input pulse width T_{in} is varied as a sinusoid, the maximum allowable peak-to-peak amplitude $T_{in,pp,aval}$ can theoretically be equal to T_{CLK} , which is equal to 50 ns in our implementation. As long as $T_{in,pp}$ is close to T_{CLK} then shorter pulses are generated inside z^{-1} circuit increasing the signal distortion. Therefore, a maximum peak-to-peak input amplitude $T_{in,pp,max}$ of 40 ns is satisfactory, covering 80% of the maximum available range of 50 ns.

6.1. Time-Mode z^{-1} Multiplier

The operation of the z^{-1} multiplier is shown in Figure 10. Timing waveforms for a z^{-1} multiplier for a multiplying coefficient are equal to 0.28, (a) synchronization clock, (b) input pulses width with $T_{in} = 20$ ns and (c) output pulses with pulse width $T_{out} = 5.55$ ns. In Figure 10a, the synchronization clock is presented. In Figure 10b,c, the input and output pulses are presented, respectively. The input pulse width T_{in} is 20 ns, while the multiplier coefficient is chosen to be equal to 0.28. As a result, the circuit generates output pulses with a pulse width of $T_{out} = 5.55$ ns, as expected. In Figure 11, two cases of multiplication coefficient, with nominal values of 0.28 and 0.21, are presented in relation to the input pulse width. In the worst-case scenario of $T_{in,pp} = 40$ ns, the relative inaccuracy of the multiplication coefficient is less than 5%.

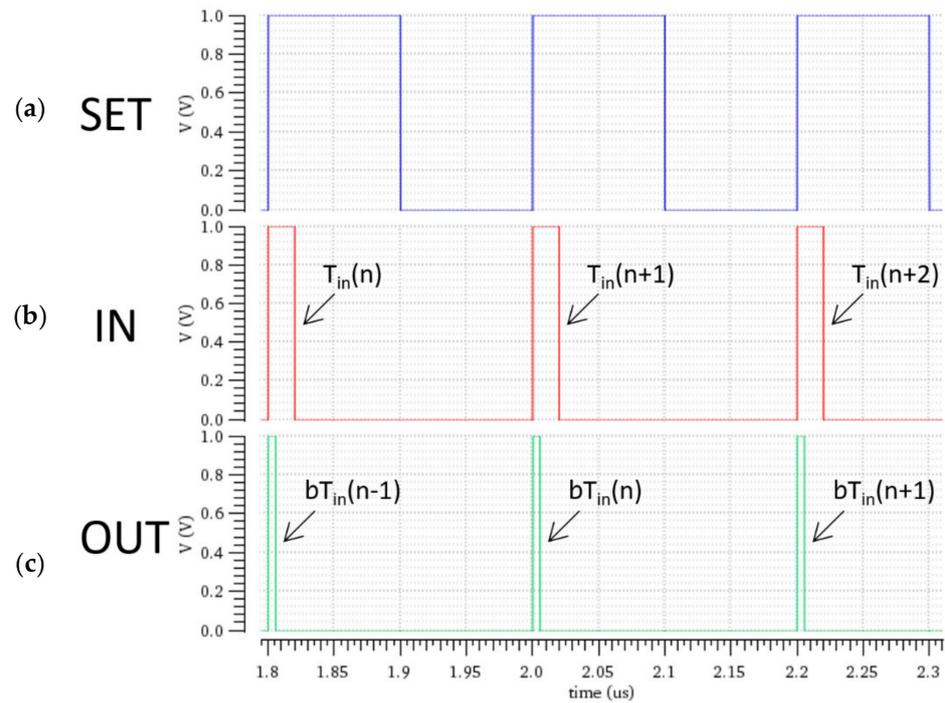


Figure 10. Timing waveforms for the z^{-1} multiplier for a multiplication coefficient equal to 0.28, (a) synchronization clock, (b) input pulses width with $T_{in} = 20$ ns and (c) output pulses with pulse width $T_{out} = 5.55$ ns.

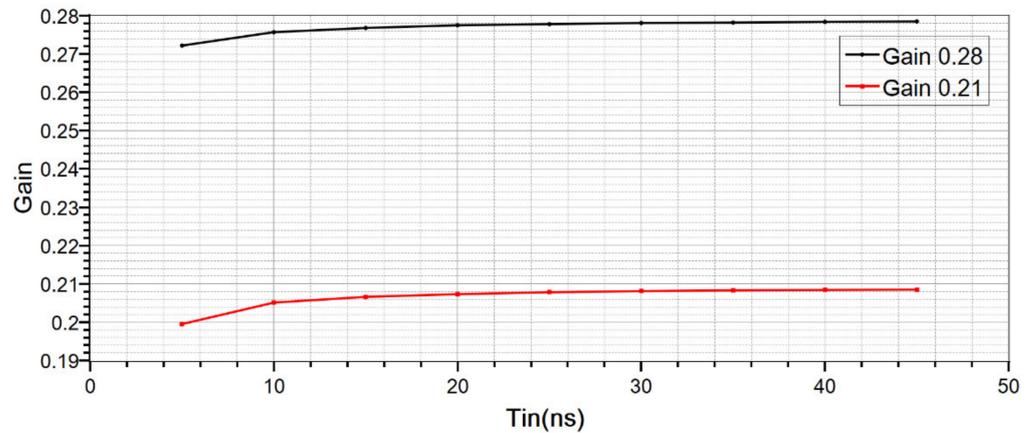


Figure 11. Two cases of multiplication coefficients with nominal values of 0.28 and 0.21 in relation to input pulse width T_{in} .

6.2. Time-Mode z^{-1} Adder

Figure 12 depicts the operation of a 2-input z^{-1} adder. The input pulse widths are 20 ns and 5 ns, respectively. The adder generates output pulses with pulse width T_{out} , which is the sum of the two preceding and equal to 25.08 ns. Figure 13 demonstrates the output pulse width of the Adder using a stable T_{in1} at 5 ns at one input, while at the second input T_{in2} ranges between 0 ns and 40 ns. It is obvious that the proposed adder can add linearly all values of the dynamic range of 40 ns.

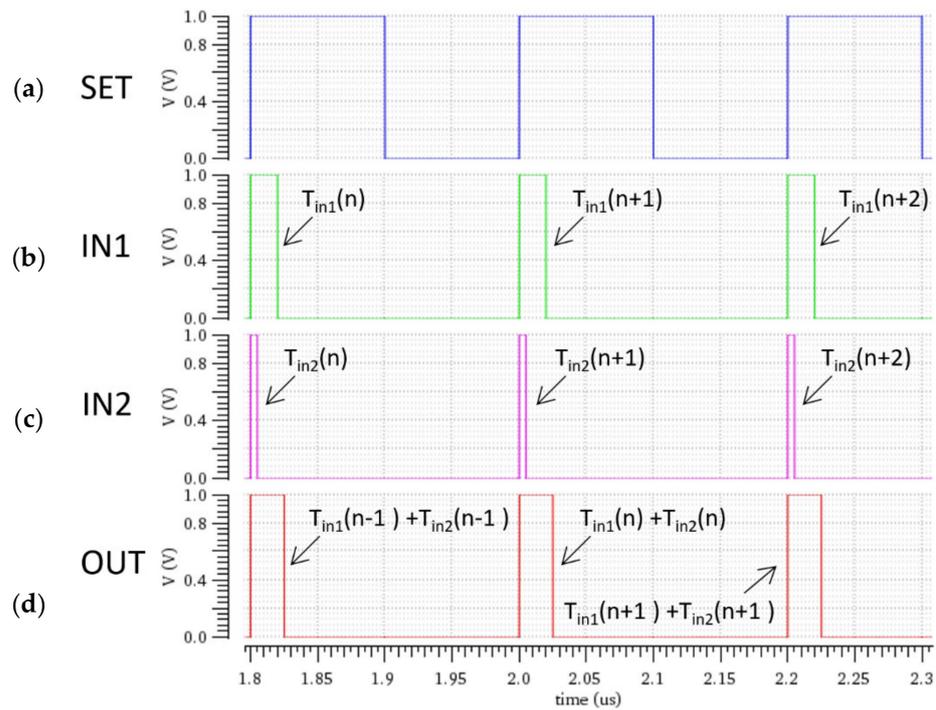


Figure 12. Timing waveforms for a 2-input z^{-1} adder, (a) synchronization clock, (b) first input pulses with pulse width $T_{in1} = 20$ ns, (c) second input pulses with pulse width $T_{in2} = 5$ ns and (d) output pulses with pulse width $T_{out} = 25.08$ ns.

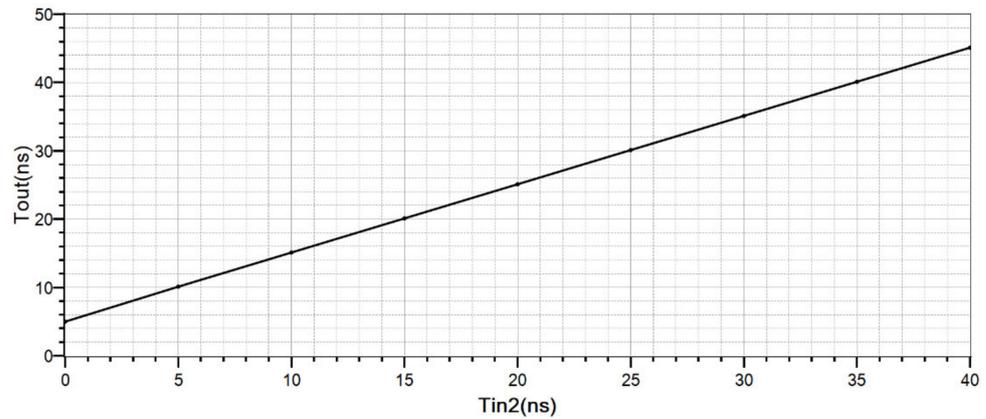


Figure 13. Input-output of a 2-input adder for a constant $T_{in1} = 5$ ns, while T_{in2} ranges between 0 and 40 ns.

6.3. Time-Mode FIR Filter

The simulated magnitude response of the ideal and the implemented time-mode 3rd-order FIR filter is presented in Figure 14. The sampling frequency was 5 MHz. The average power consumption is 200 μ A, which includes the consumption of both actual filter circuit and digital calibration. The approximated filter coefficient values are presented in Table 1. The notch frequency of the ideal filter is selected to be around 1.31 MHz, which is close to the 1.38 MHz notch frequency of the implemented FIR filter. There is a frequency shift of 70 KHz. These frequency response discrepancies can be mainly attributed to the approximation error of the filter coefficients.

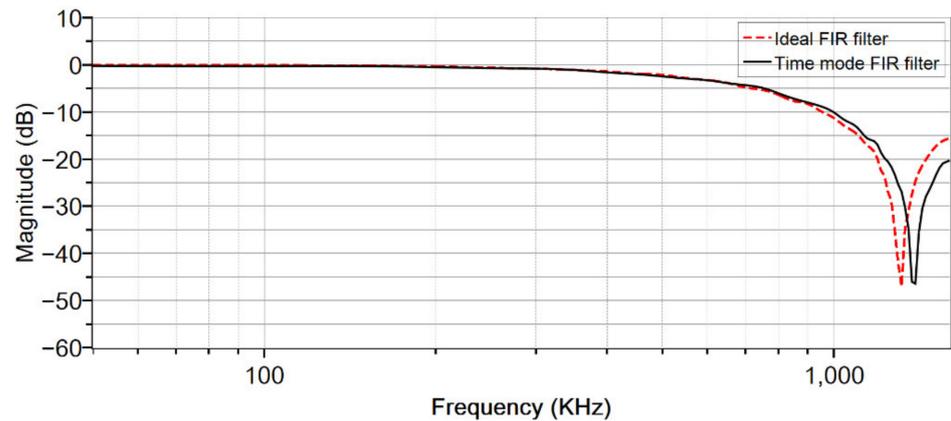


Figure 14. Ideal and time-mode FIR frequency response.

The SNDR simulated results versus $T_{in,peak}$ are reported in Figure 15, where $T_{in,peak}$ is the amplitude of a sinusoidal signal of 50 kHz. The SNDR peak is at around 38.6 dB.

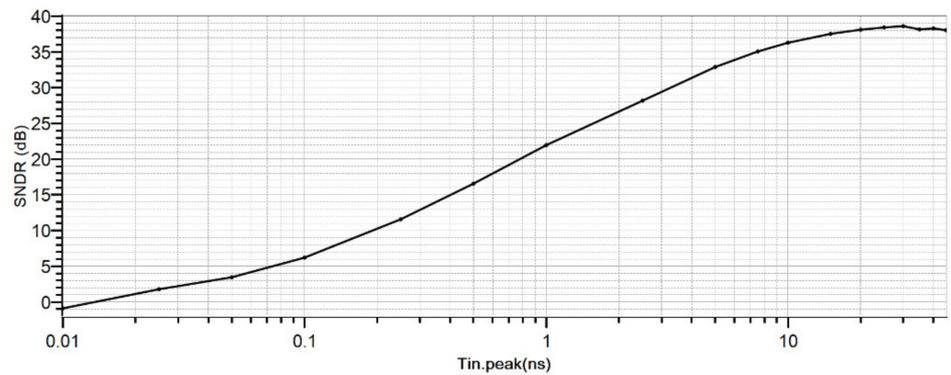


Figure 15. SNDR as function of $T_{in,peak}$ for 50 KHz.

The maximum input T_{in} is defined by the upper limit of the input signal of the z^{-1} structure, which is a bit less than 50 ns. The lower limit is mainly limited by the noise contribution of the MOS devices, which appeared as clock jitter, charge injection and leakage. Based on Figure 15, the noise level is around 10 ps.

Table 2 compares the proposed filter implementation to the state-of-the-art time-mode filters. Our implementation operates under the lowest power supply; it has relatively low power consumption for a 3rd order filter topology also using the highest sampling frequency.

Table 2. Performance comparison with the state-of-the-art time-mode low-pass filters.

	This Work	[13]	[14]	[12]	
Technology	28 nm	130 nm	180 nm	180 nm	
Supply Voltage	1 V	1.2 V	1.8 V	5 V	
Sampling Frequency	5 MHz	130 kHz	5 MHz	100 kHz	
Filter Order	3rd	2nd	2nd	3rd	
Type	FIR rectangular	Butterworth	Chebyshev	IIR Chebyshev	FIR
Peak SNDR	38.6 dB	47 dB	37 dB	44.1 dB	-
Peak SNR	-	-	-	63.6 dB	64 dB
Power Cons.	200 μ W	152 μ W	187 μ W	760 μ W	89.45 μ W

7. Discussion

The proposed time-domain 3rd-order FIR rectangular filter is based on time-mode signal processing circuits such as the z^{-1} delay, z^{-1} multiplier and z^{-1} adder. The time

register from [16] is used as a building component in all time-mode circuits in this work. The peak SNRR of the filter for a signal with frequency of 50 KHz is 38.6 dB. The average current consumption is 200 μ A for a 5 MHz sampling frequency. This filter design offers numerous inherent advantages in time-mode signal processing. First, its outputs are synchronized with the sampling frequency. Second, because the topology is modular, filters of higher order may be created by simply increasing the number of delays and multipliers on the same complexity. Finally, the compatibility with the digital circuits makes it a perfect candidate for all-digital topologies that are widely used in state-of-the-art topologies.

This technology can be utilized to produce other types of filters in the future, such as higher-order FIR or IIR filters. Time-mode controllers are also possible using this technique. The fabrication and the experimental verification of the proposed topology will be part of a future work.

Author Contributions: Conceptualization, O.P.-F. and S.V.; methodology, S.V.; validation, O.P.-F.; formal analysis, O.P.-F. and S.V.; investigation, O.P.-F. and S.V.; resources, S.V.; data curation, O.P.-F.; writing—original draft preparation, O.P.-F.; writing—review and editing, S.V.; visualization, O.P.-F. and S.V.; supervision, S.V.; project administration, S.V.; funding acquisition, O.P.-F. and S.V. All authors have read and agreed to the published version of the manuscript.

Funding: This research has been co-financed by the European regional development fund of the European union and Greek national funds through operational program competitiveness, entrepreneurship and innovation, under the call RESEARCH—CREATE—INNOVATE (project code: T1EDK-02551).

Conflicts of Interest: The authors declare no conflict of interest.

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