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The Properties of an Edge-On Low Surface Brightness Galaxies Sample

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Abstract: We analyzed the properties of a sample of edge-on low-surface brightness galaxies, which are referred to as Cao23 EL SBGs. Cao23 EL SBGs exhibit a wide range of luminosities ($-22 < M_r < -13$) with a mean scale length of 3.19 ± 1.48 kpc. Compared to HI-rich dwarf EL SBGs, Cao23 EL SBGs display more extended disk structures and redder (g-r) colors. They are also, on average, more massive than HI-rich dwarf EL SBGs. Star formation rates (SFRs) were calculated using WISE 12 μm luminosity conversions and spectral energy distribution (SED) fitting methods, respectively. Cao23 EL SBGs fall below the main sequence with specific star formation rates (sSFRs) primarily in the range of $0.01\text{--}0.1 \text{ Gyr}^{-1}$. More massive Cao23 EL SBGs tend to have lower sSFRs. Additionally, we derived the non-parametric star formation histories (SFHs) of Cao23 EL SBGs by SED fitting, dividing the SFHs into seven look back time bins with constant SFRs assumed for each bin. Our analysis indicates that high-mass ($M_* > 10^{9.0} M_\odot$) Cao23 EL SBGs assembled their mass earlier than their lower-mass counterparts, supporting a downsizing trend for EL SBGs.

Keywords: low surface brightness galaxies; star formation; star formation history



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1. Introduction

Low surface brightness galaxies (LSBGs) are characterized by their extremely faint structure with a central surface brightness (μ_0) of the disk lower than $22.0\text{--}23.0 \text{ mag arcsec}^{-2}$ in the B-band [1–9]. LSBGs encompass various galaxy types, including dwarf LSBGs [10], ultra-diffused galaxies (UDGs) characterized by the effective surface brightness $\mu_e \geq 24 \text{ mag arcsec}^{-2}$ and the effective radius $R_e \geq 1.5 \text{ kpc}$ [11,12], and giant LSBGs (GLSBGs) with radii up to 130 kpc and stellar masses of the order of $10^{11} M_\odot$, as exemplified by Malin 1 [13–18]. The stellar masses of LSBGs exhibit a wide range, spanning from dwarf LSBGs to GLSBGs. The faint features of LSBGs are related to their low-surface stellar mass densities [19]. LSBGs are metal-poor [20–22]. In the mass-metallicity ($M_* - Z$) relation, LSBGs show a flatter trend compared to star-forming galaxies, suggesting inefficient oxygen abundance enhancement [23]. Furthermore, LSBGs display lower star formation rates (SFRs) than the main sequence galaxies [24–26].

LSBGs typically exhibit lower dust content compared to high surface brightness galaxies [27], and their far-infrared emissions are weaker than those of normal star-forming galaxies [28]. Among five GLSBGs, only UGC 6614 and UGC 6151 show $160 \mu\text{m}$ (cool) dust emission in [28] with the dust mass of UGC 6614 measured at $10^{8.42} M_\odot$ [27]. Ref. [29] have discussed the higher dust content in some extreme GLSBGs. Additionally,

LSBGs are characterized by a shortage of molecular gas [30,31]. Ref. [32] estimated the molecular gas surface density in Malin 1 to range from approximately 2 to $0.8 M_{\odot} pc^{-2}$ with a very low molecular-to-atomic gas mass ratio. Parts of LSBGs are HI-rich [33], exhibiting higher HI gas mass fractions ($f_{HI} = M_{HI}/M_{*}$) than those in the HI-selected spiral galaxies in the HI Parkes All Sky-Survey Catalogue (HICAT) and the Wide-field Infrared Survey Explorer (WISE) sample from [34]. The spiral galaxies in [34] are high surface brightness systems. Many LSBGs are late-type (Sc and later) spiral galaxies with amorphous or fragmentary and faint spiral patterns, and some are similar to irregular galaxies [33]. Some GLSBGs generally exhibit clearly defined spiral structures [35]. The differences between gas-rich and gas-poor LSBGs are not clear. Our current understanding of various LSBG properties remains limited. The origins and evolutions of these LSBGs are under debate [36–39]. The typical formation scenario is that LSBGs arise in haloes with high angular momentum under the Λ CDM framework [40,41]. Other scenarios also considered in recent research, such as ram-pressure stripping [42], extreme feedback processes [43], and mergers [22,44–47].

The star formation history (SFH) is an essential parameter tracing the stellar assembly history and thereby revealing the evolutionary pathway of galaxies. The specific star formation rate (sSFR) at different redshifts and the observed spectral energy distributions (SEDs) can provide valuable insights into SFH. The sSFR, defined as the ratio of SFR to stellar mass (M_{*}) [48], reflects the rate ratio of new stars to the assembled galaxy mass [49]. Estimating the sSFR at different redshifts [50,51] offers a deeper understanding of the galaxy's star formation history. The sSFR–stellar mass relation exhibits a steeper trend at high redshift [52] for main sequence galaxies. It indicates that the massive galaxies have assembled their stellar mass at the early time, which is a concept known as downsizing [53]. Very few studies have explored LSBGs at high redshifts [54,55]. The topic of SFH of LSBGs is a rarely mentioned area [10,25], and the relevant discussion is based on the HI-gas depletion time ($t_{dep} = M_{HI}/SFR$, [56]). Ref. [25] demonstrated that the current SFRs of their HI-detected LSBGs are close to average SFRs in Hubble time by the HI depletion time t_{dep} -sSFR relation, suggesting that most LSBGs are stable systems.

Ref. [23] presented a sample of 330 blue edge-on low-surface brightness galaxies (ELSBGs) with SDSS fiber spectra and analyzed the chemical evolution of this sample. The ELSBGs in [23] have distance information, which is often unavailable in most optically selected LSBG samples. Additionally, the ELSBGs show higher projected surface stellar mass densities than face-on LSBGs, making it possible to obtain high-quality integral field spectroscopy (IFS) data. This enables detailed investigations into their perpendicular disk structure providing insights into the formation and evolution of LSBGs through dynamical studies. For instance, ref. [22] presented IFS observations of an ELSBG (AGC 102004) from [23] and discussed evidence for a minor or mini-merger event in AGC 102004.

In this study, we investigate properties of the ELSBGs from [23], focusing on SFR, sSFR, t_{dep} , and non-parametric SFH. We give a review of ELSBGs from [23] in Section 2 and compare ELSBGs with previous ELSBG samples (HI-rich dwarf ELSBGs and super-thin galaxies) in Section 3. In Section 4, we examine the SFR of ELSBGs based on multi-band data, and in Section 5, we assess their HI gas depletion times. The SFH of ELSBGs inferred from the non-parametric model using the SED fitting code PROSPECTOR is represented in Section 6. We summarize our findings in Section 7. Throughout this paper, we utilize AB magnitudes for all measurements. We adopt a Λ CDM cosmology with $\Omega_m = 0.3$, $\Omega_{\Lambda} = 0.7$, $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$. In this paper, the stellar masses of ELSBGs are from the MPA-JHU catalog [57], and the redshifts of ELSBGs are SDSS spectroscopic redshifts. We use the Chabrier universal initial mass function (IMF, [58]) throughout the article. We convert Salpeter IMF [59] and Kroupa IMF [60] with the following conversion factors: $SFR^{cha} = SFR^{sal}/1.41$ [61–63], $SFR^{cha} = SFR^{kro} \times 0.943$ [64].

2. Cao23 ELSBGs

The ELSBGs' sample is drawn from [23], including 330 blue ELSBGs with SDSS spectra. The initial edge-on galaxies sample is from [65]. The ELSBGs sample are selected based on their face-on mean surface brightness in 3'' radius (μ_{3-face}) in a g-band lower than 25 mag arcsec⁻² and the projected (u-r) color in the center 3'' aperture region below the green valley upper boundary [66]. The details of conversion from edge-on to face-on surface brightness estimation are given in [23]. The final 330 ELSBGs show the face-on center surface brightness (μ_{0-face}) ranges from 22.34 to 23.75 mag arcsec⁻² and redshifts from 0.0026 to 0.14. Hereafter, we refer to the ELSBGs from [23] as "Cao23 ELSBGs".

We separate Cao23 ELSBGs into five bins according to their inclination angle and test how the inclination angle affects the surface brightness correction for edge-on galaxies with the method from [67–70] due to deviations from a 90-degree inclination angle. We show the relationship between the mean value of the scale height to scale length ratio ($-2.5 \times \log(h_s/r_s)$) and the inclination angle of Cao23 ELSBGs in Figure 1. The h_s and r_s are from the GALFIT edge-on disk model fitting [23], and the inclination angle is from [65]. It shows a weak trend that the $-2.5 \times \log(h_s/r_s)$ increases with the inclination angle increasing and $-2.5 \times \log(h_s/r_s)$ does not change too much with respect to Cao23 ELSBGs. It suggests that the inclination angle does influence the surface brightness correction, but the influence is not significant for inclination angle > 81°. The inclination angle > 81° contributes 86% of Cao23 ELSBGs which does not significantly affect the main results of the sample.

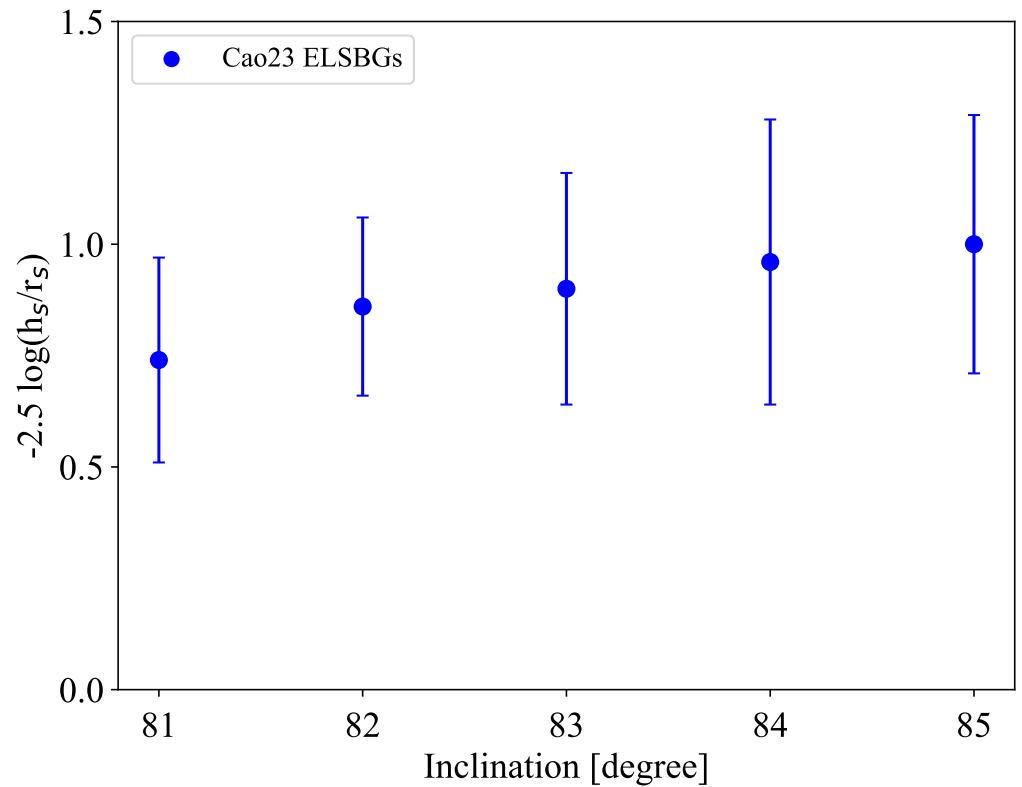


Figure 1. The relationship between the mean value of the scale height to scale length ratio ($-2.5 \times \log(h_s/r_s)$) and inclination. We note the $-2.5 \times \log(h_s/r_s)$ is the correction factor from the observed center surface brightness to face-on center surface brightness for edge-on cases [70].

The selection of the LSBG sample usually excludes those high ellipticity ($\epsilon = (1 - b/a) \geq 0.7$, a and b are the semi-major axis and semi-minor axis, respectively) targets to avoid the edge-on galaxies, high redshift, spurious artifacts, and galaxy blends [33,71,72]. It is worth noting that the surface brightness cutting sometimes does not account for inclination angle correction [71,72], which may result in parts of ELSBGs being missed in this step.

Recent studies [70] have shown that a significant portion of ELSBGs would be overlooked if inclination effects are not considered. Furthermore, the number of highly inclined galaxies is less than in other cases. These factors collectively contribute to the rarity of ELSBGs in LSBGs. This limitation may introduce biases in studies of the intrinsic morphology of LSBGs.

3. Comparison with Other ELSBG Samples

We compare the physical parameters of Cao23 ELSBGs with two other ELSBGs samples: HI-rich dwarf ELSBGs from [70] and super-thin galaxies from [73]. Both studies provide comparisons between edge-on ELSBGs and other LSBGs, concluding that ELSBGs exhibit similar properties to other LSBGs.

3.1. HI-Rich Dwarf ELSBG Sample

Ref. [70] present 281 HI-rich dwarf ELSBGs from the crossmatch between Sloan Digital Sky Survey Data Release 7 and the 40% ALFALFA catalog. They require the $b/a \leq 0.3$ in the SDSS g-band or r-band to select edge-on galaxies. They compare their ELSBGs with face-on HI-rich dwarf LSBGs from [33] and conclude that the differences between edge-on and face-on LSBGs tend to be much smaller.

We compare the physical parameters of Cao23 ELSBGs with these HI-rich dwarf ELSBGs. We use the same method with [70] to obtain $\mu_{0_{face}}$ in Figure 2a. Cao23 ELSBGs show slightly fainter $\mu_{0_{face}}$ (with the mean $\mu_{0_{face}}$ value 22.89 ± 0.51 mag arcsec⁻²) than HI-rich dwarf ELSBGs (with the mean $\mu_{0_{face}}$ value 22.67 ± 0.47 mag arcsec⁻²). The mean value of b/a of Cao23 ELSBGs and HI-rich dwarf ELSBGs is 0.20 ± 0.06 and 0.18 ± 0.08 , respectively.

The g-band absolute magnitude of HI-rich dwarf ELSBGs is much fainter than that of the Cao23 ELSBGs in Figure 2c. The mean value of M_g for Cao23 ELSBGs and HI-rich dwarf ELSBGs is -19.36 ± 0.85 mag and -16.63 ± 1.12 , respectively. Cao23 ELSBGs are selected with SDSS fiber spectra, which leads to faint targets being missed. The difference in luminosity reflects the varying mass distributions between the two samples. These HI-rich dwarf LSBGs are mainly occupied by low-mass galaxies ($<10^9 M_{\odot}$, [35]), while the Cao23 ELSBGs are, on average, more massive.

The scale length (r_s) of Cao23 ELSBGs is larger than that of HI-rich dwarf ELSBGs. The mean value of r_s of Cao23 ELSBGs is 3.19 ± 1.48 kpc, while for HI-rich dwarf ELSBGs, it is 1.84 ± 0.89 kpc. HI-rich LSBGs are primarily composed of dwarf LSBGs [33,70], indicating that they are likely small galaxies.

We compare the observed (g-r) color for two ELSBG samples in Figure 2e. Cao23 ELSBGs are redder in (g-r) color than HI-rich dwarf ELSBGs. The mean value of (g-r) of Cao23 ELSBGs and HI-rich dwarf ELSBGs is 0.46 ± 0.16 and 0.34 ± 0.11 , respectively.

Overall, Cao23 ELSBGs show slightly fainter surface brightness, more extended disk structure, and redder color than HI-rich dwarf ELSBGs from [70]. The redder color and larger r_s of Cao23 ELSBGs are consistent with Cao23 ELSBGs being on average more massive.

3.2. Super-Thin Galaxies Sample

Ref. [73] present a sample of super-thin (ST) galaxies with b/a of 0.05–0.1 and no bulge component (the center surface brightness in B-band (μ_B) > 23.0). A comparison LSBG sample with $\mu_B > 23.0$ also is included in [73]. Ref. [73] compares the SFR of STs and LSBGs by different methods and conclude that STs and LSBs have equal intrinsic SFR, which possibly implies STs are just the LSBGs seen edge-on.

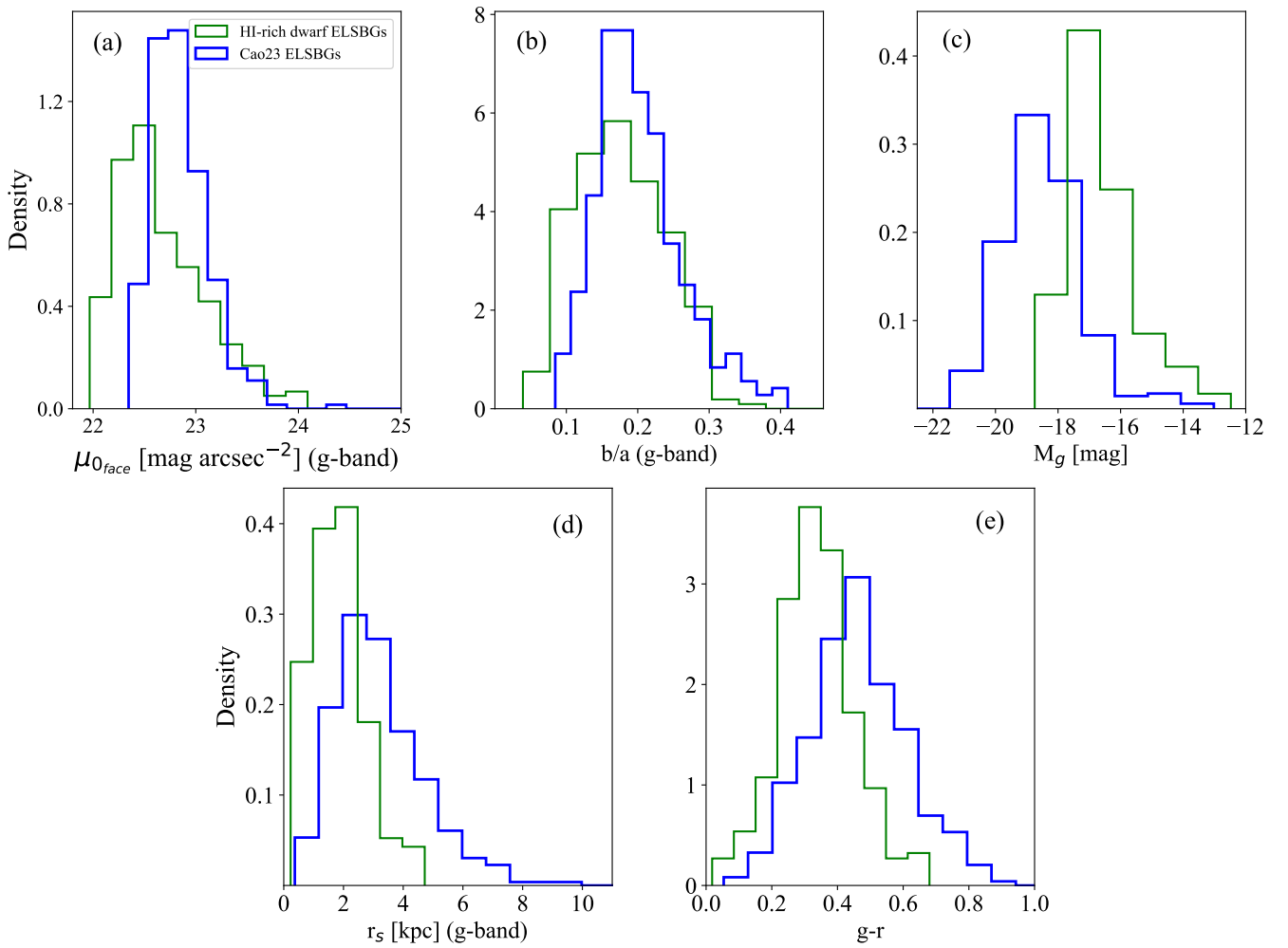


Figure 2. Panel (a): The distribution of $\mu_{0_{face}}$ in g-band. Panel (b): The distribution of axis ratio (b/a) in g-band. Panel (c): The distribution of g-band absolute magnitude. Panel (d): The distribution of scale length (r_s) of g-band in the unit of kpc. Panel (e): The distribution of (g-r) color. The blue and green line represents Cao23 ELSBGs and HI-rich dwarf ELSBGs from [70] in all panels, respectively.

Cao23 ELSBGs show a comparable distribution of M_r with the STs and LSBGs' sample for $M_r < -17$ mag in Figure 3a.

We compare the SFR of Cao23 ELSBGs with those of STs and LSBGs. We apply the same code (Multi-wavelength Analysis of Galaxy Physical Properties, MAGPHYS [74]) to obtain SFR as [73]. Ref. [73] used ten bands of photometric data from 0.15 to 2.2 μm for SED fitting. We require that Cao23 ELSBGs have observation data in GALEX: FUV, NUV, SDSS: u,g,r,i,z, and WISE: W1, W2, and a signal-to-noise ratio (SNR) larger than five in W2, and they also keep consistent the similar wavelength coverage of [73]. Overall, 192 Cao23 ELSBGs meet the requirement. We use the model magnitude associated with de Vaucouleurs and exponential model fits in each band to avoid pollution from the nearby targets. The SEDs cover the rest-frame wavelength ranges from FUV to NIR (from 0.15 to 4.6 μm) for Cao23 ELSBGs. This subsample is also used in Sections 4 and 6.

Stellar population synthesis is used to predict the observed SED [75] and model the spectral evolution of the stellar population with an IMF. The IMF is assumed [58]. The IMF and the dust attenuation of the stellar spectrum are modeled using the two-component model of [76] in MAGPHYS code. The exponentially declining SFH model is parametrized as $\text{SFR}(t) \propto \exp(-\gamma t)$, which is characterized by an age t_{gal} of the galaxy and star formation time-scale γ^{-1} , and random bursts are set to occur with equal probability at all times [77].

We show the Stellar Mass-SFR (M_* -SFR) relation in Figure 3b of 75 Cao23 ELSBGs with reduced χ^2 values smaller than five. The $\text{SFR}_{\text{MAGPHYS}}$ distribution of Cao23 ELSBGs with a median value of 0.22 ± 0.55 is consistent with that of STs ($0.2^{+0.9}_{-0.2}$). The LSBGs in Figure 3b show a wide range and have larger $\text{SFR}_{\text{MAGPHYS}}$ (with median value $0.4^{+2.2}_{-0.3}$) than that of Cao23 ELSBGs and STs on average. The range of $\text{sSFR}_{\text{MAGPHYS}}$ for Cao23 ELSBGs is from 0.01 to 0.1 Gyr^{-1} .

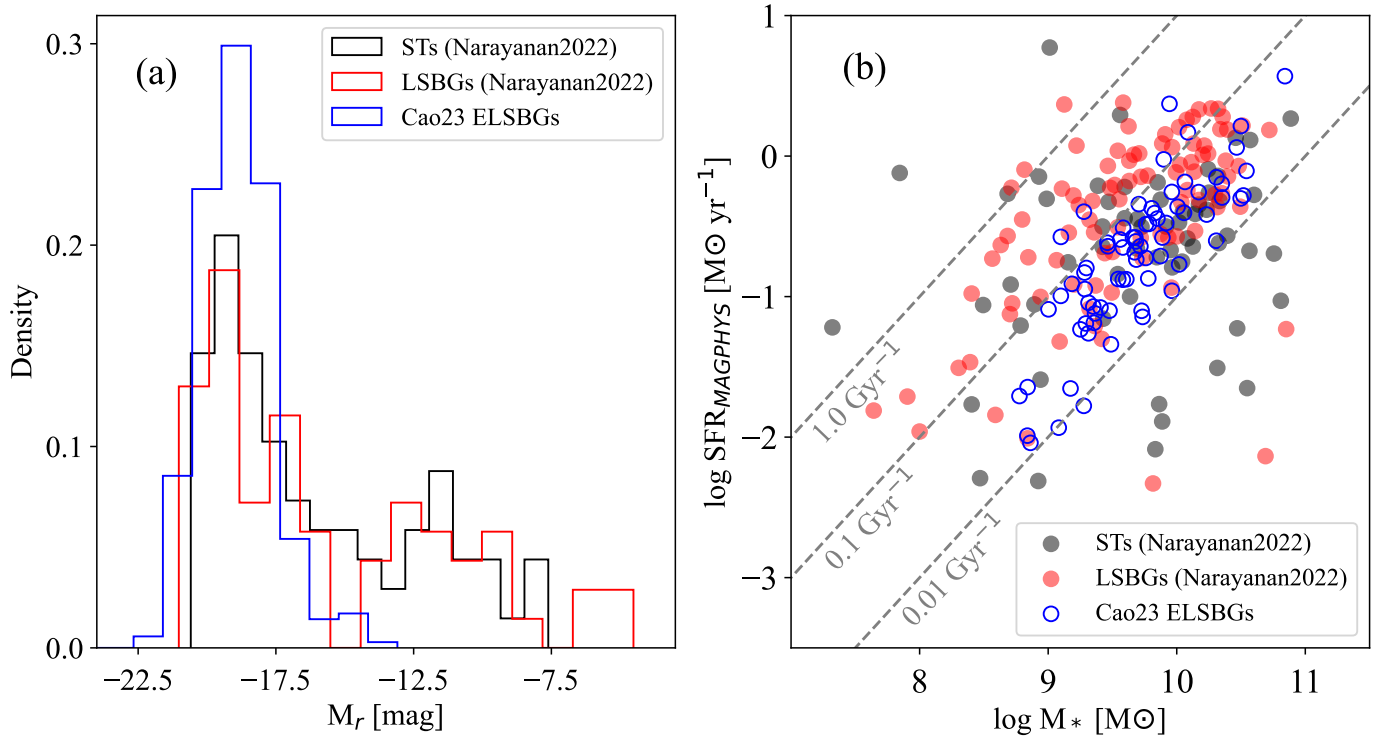


Figure 3. Panel (a): The distribution of M_r of Cao23 ELSBGs (blue line), STs (black line) [73], and LSBGs (red line) [73]. Panel (b): The M_* -SFR relation of Cao23 ELSBGs (open blue circles), STs (gray dots) [73], and LSBGs (red dots) [73]. The gray dashed lines, arranged from bottom to top, correspond to specific specific star formation rates (sSFRs) of 0.01 Gyr^{-1} , 0.1 Gyr^{-1} , and 1 Gyr^{-1} .

4. SFR of Cao23 ELSBGs

We use the infrared luminosity of WISE W3 $12 \mu\text{m}$ and the SED fitting method to estimate the SFR for Cao23 ELSBGs. The W3 luminosity traces the emission from polycyclic aromatic hydrocarbon (PAHs), which is well related with the star formation rate [78]. And W3 luminosity–SFR conversion is not affected by dust attenuation. However, since only one third of our sample has high SNR W3 photometries, we also obtain the SFRs through composite stellar population synthesis.

4.1. SFR Derived from W3 Luminosity

The 131 Cao23 ELSBGs show WISE W3 $12 \mu\text{m}$ detection with SNR values larger than three. The redshifts of Cao23 ELSBGs are smaller than 0.14, and we have ignored the k-correction. For most of our object, our treatment of observed $12 \mu\text{m}$ flux as an SFR estimator will induce less than 10% error, which is small compared with the photometric error. We derive SFR_{W3} following the formula form [79,80]:

$$\log \text{SFR}_{\text{W3}} = 0.66 \times (\log L_\nu(\text{W3}) - 22.5) + 0.16 \quad (1)$$

with $L_\nu(\text{W3})$ in W Hz^{-1} and [58] IMF.

Figure 4 shows the SFR_{W3} and sSFR_{W3} of 131 Cao23 ELSBGs. Overall, Cao23 ELSBGs deviate from the main sequence (MS) and around the 50% level of the MS line. The MS line

in Figure 4 is according to SFR_{W3} . We note that the MaNGA edge-on sample was selected based on two considerations: edge-on inclination and no clear evidence for ongoing major merging interaction [80]. The SFR_{W3} and $sSFR_{W3}$ of the MaNGA edge-on sample show a wider range than that of the Cao23 EL SBGs in Figure 4. The typical error is the mean value of the SFR_{W3} error, which is derived from the W3 band magnitude error.

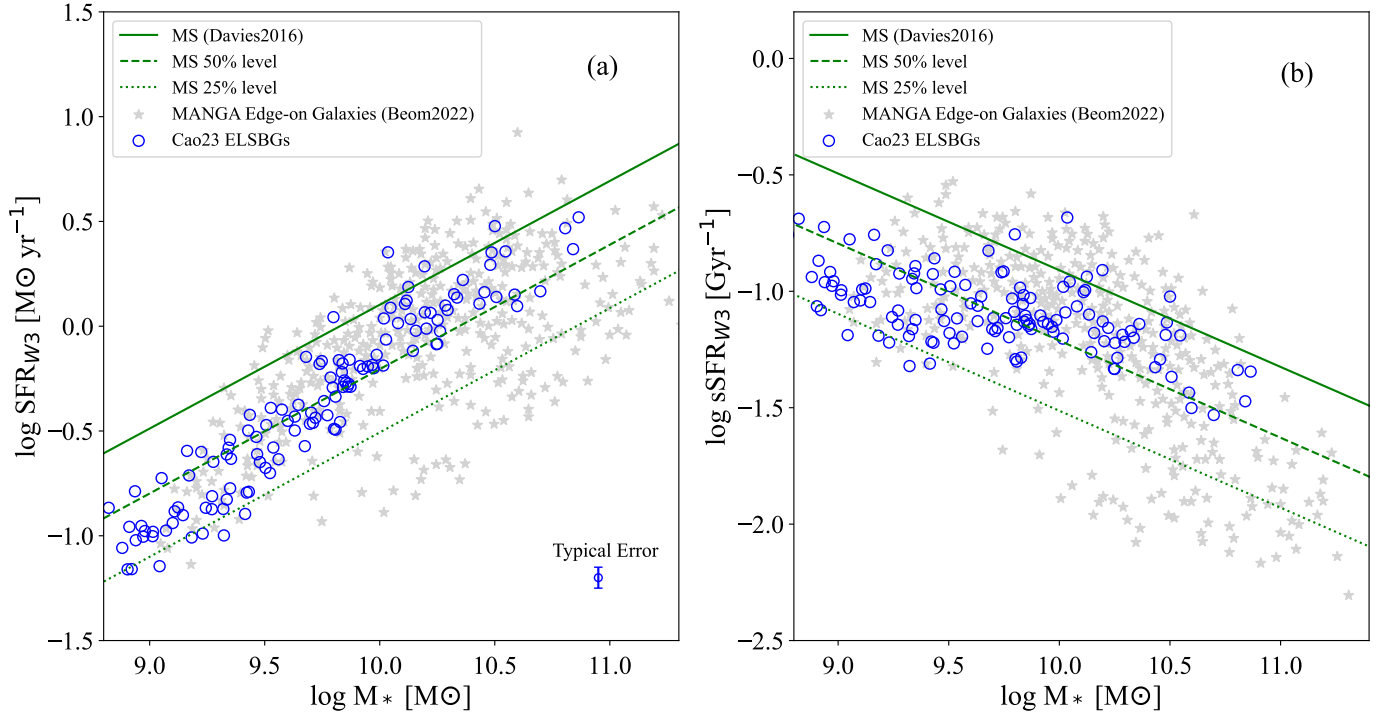


Figure 4. Panel (a): SFR_{W3} versus M_* of 131 Cao23 EL SBGs (open blue circles) and MaNGA 472 edge-on galaxies (gray stars) from [80]. The typical error is the mean value of the SFR uncertainty derived from the W3 magnitude error. Panel (b): $sSFR_{W3}$ versus M_* of 131 Cao23 EL SBGs (open blue circles) and MaNGA 472 edge-on galaxies (gray stars) from [80]. The green line represents the main sequence line for star-forming nearby galaxies with SFR derived from W3 luminosity [79,80]. The dashed and dotted lines indicate 50% and 25% levels of the main sequence lines from [80].

4.2. SFR Derived from CIGALE

We apply the Code Investigating GALaxy Emission (CIGALE, [81,82]) to perform the SED fitting and estimate SFRs of 192 Cao23 EL SBGs (multi-band data from GALEX (FUV, NUV), SDSS (u,g,r,i,z), and WISE (W1, W2)). The SEDs cover the rest-frame wavelength from 0.15 to 4.6 μm .

The stellar population synthesis models are from [75] with a [58] IMF. We set the stellar metallicities of 0.0001, 0.0004, 0.004, and 0.008. We employed the delayed star formation history (SFH) model consistent with [83]. The dust emission model is from [84] and the dust attenuation is modified [85] attenuation law. The details of the input parameters set are listed in Appendix A Table A1.

We use the likelihood-weighted mean SFR from the CIGALE results in Figure 5. The typical error is the mean value of the SFR_{cigale} error from CIGALE outputs. Cao23 EL SBGs show a distribution of $sSFR_{\text{cigale}}$ in the range of 0.01–0.1 Gyr^{-1} in Figure 5. Different types of LSBGs (UDGs, HI-rich UDGs, dwarf LSBGs and GLSBGs) are also shown in Figure 5. It shows a large scatter in the M_* -SFR relation for those LSBGs with $M_* < 10^{8.5} M_\odot$. Part of the HI-rich dwarf LSBGs from [33] shown in [35] exhibit $sSFR$ s larger than 0.1 Gyr^{-1} and show a larger SFR than Cao23 EL SBGs overall, which means those HI-rich dwarf LSBGs tend to have a larger SFR value. We note the SFR derived from different methods, and sample selection bias would induce the scatter in the M_* -SFR relation.

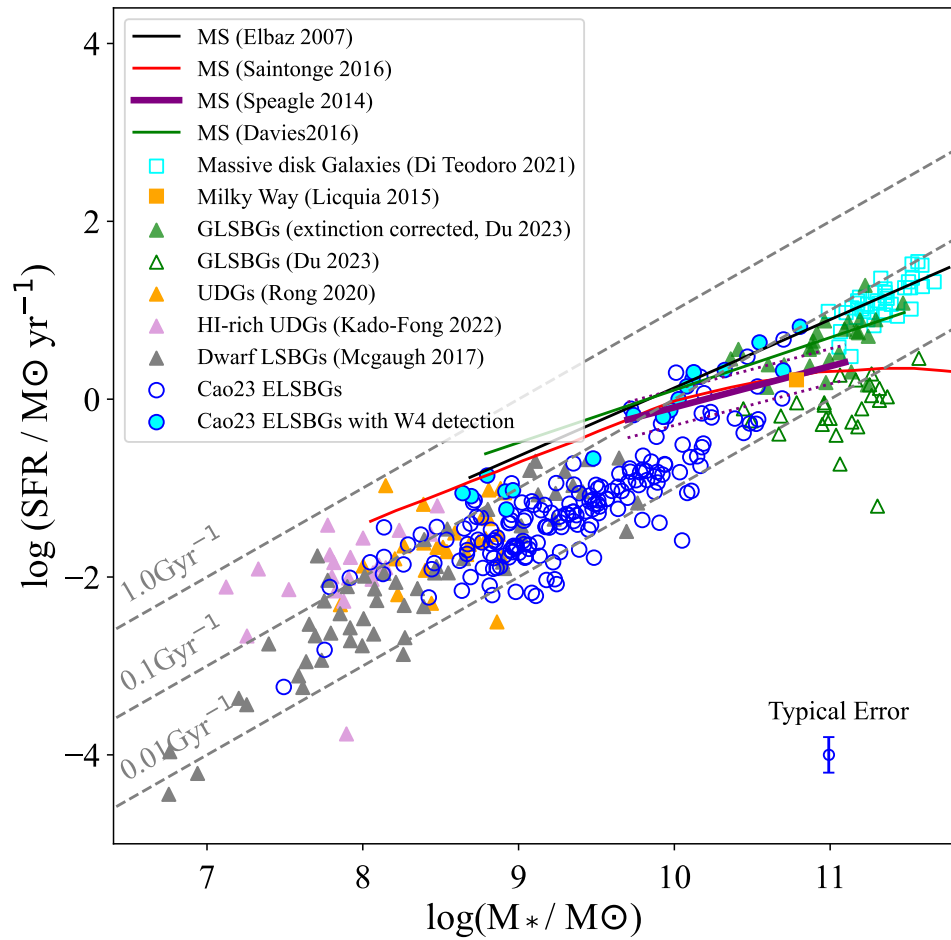


Figure 5. The M_* -SFR relation. Blue open circles denote Cao23 EL SBGs and blue open circles with filled cyan color are those Cao23 EL SBGs with W4 detection. Gray triangles represent dwarf LSBGs from [10], orange triangles distinguish UDGs from [86], and purple triangles are HI-rich UDGs from [83]. Green filled and unfilled triangles are GLSBGs from [35] with dust extinction correction and none correction, respectively. The orange and open cyan squares are the Milky Way [35] and Massive disk galaxies [87], respectively. The purple line, black line, and red line represent the main sequence from [61,88,89]. The green line represents the main sequence line for star-forming nearby galaxies with the SFR derived from W3 luminosity [79,80]. The gray dashed lines, arranged from bottom to top, correspond to specific star formation rates (sSFRs) of 0.01 Gyr^{-1} , 0.1 Gyr^{-1} , and 1 Gyr^{-1} . The typical error is the mean value of the SFR error from CIGALE. The IMF has been corrected to Chabrier IMF for all data points.

The variable integrated galactic initial mass function (IGIMF) has been mentioned in [56,90,91]. The IGIMF systematically varies with the global SFR and metallicity and also affects the MS [92]. Ref. [92] shows that estimates of the SFRs for local star-forming galaxies differ by factors of approximately 10 between the IGIMF theory to the canonical universal IMF, particularly at the low-mass end. Cao23 EL SBGs primarily include massive galaxies ($M_* > 10^{9.0} M_\odot$), and the difference for those massive ones are small in [92]. Additionally, the lack of far-infrared data in the SED fitting may impact results, as noted by [93]. Ref. [94] estimated that using only stellar SEDs (sampling starlight from 0.4 to 2.2 μm) introduces an uncertainty of about 0.3 dex. However, this does not affect the main results in Figure 5, which show that Cao23 EL SBGs lie below the MS.

5. HI-Gas Content and t_{dep}

We compare the HI-gas content and depletion time t_{dep} , which characterizes the evolutionary status of star formation for HI-rich and normal dwarf LSBGs in Figure 6.

Figure 6a shows the relation between HI gas mass (M_{HI}) and M_* . The HI-rich UDGs display higher M_{HI} values than the dwarf LSBGs at similar stellar masses. Among the Cao23 ELSBGs, 75 have HI detections [23] and belong to HI-rich ones. Figure 6b presents the relation between t_{dep} and sSFR. The SFRs of both dwarf LSBGs [10] and HI-rich dwarf LSBGs [25] are derived from H α luminosities, and both share a similar stellar mass range. The parent sample of HI-rich dwarf LSBGs is from [33]. The HI-rich dwarf LSBGs exhibit higher sSFR and shorter t_{dep} than low-HI-fraction dwarf LSBGs, indicating that a higher HI gas content correlates with a higher SFR. We also show that 35 Cao23 ELSBGs with HI detection also show in Figure 6b. Additionally, 35 Cao23 ELSBGs with HI detection are located close to dwarf LSBGs but are, on average, more massive. This trend is evident in Figure 7.

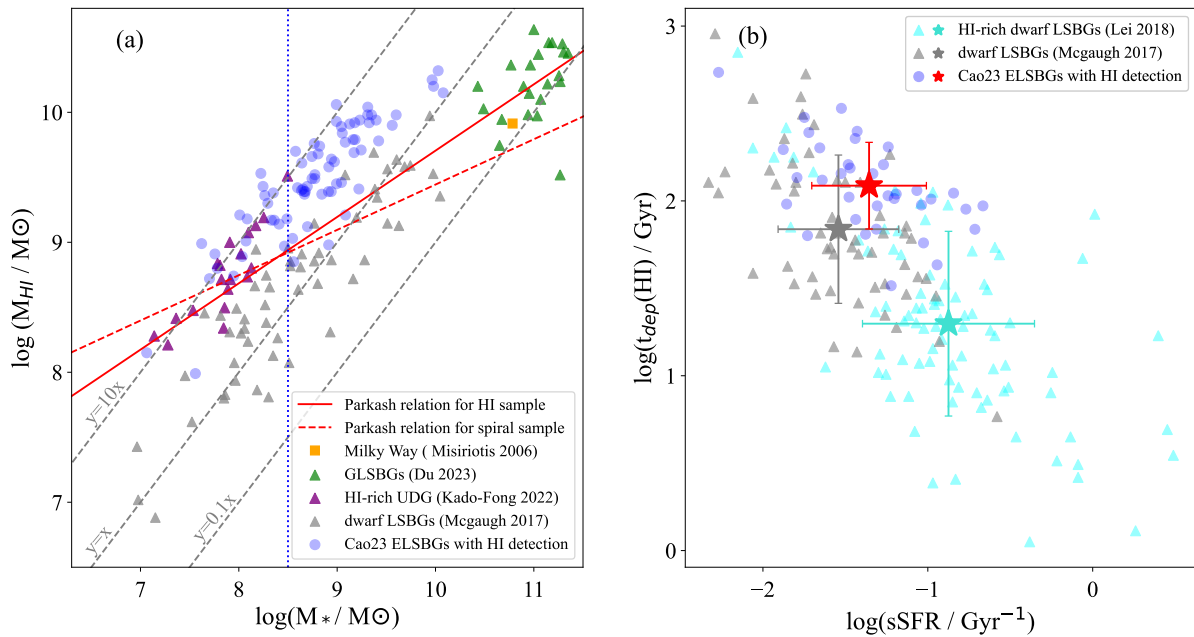


Figure 6. Panel (a): The M_{HI} - M_* relation for LSBGs. Blue filled circles denote Cao23 ELSBGs with HI detection, gray triangles represent dwarf LSBGs from [10], and purple triangles distinguish UDGs from [83]. Green filled triangles are GLSBGs from [35]. The orange square represents the Milky Way. The red solid line represents the relation followed by the HI-selected sample of galaxies with a 1σ scatter of 0.5 dex, and the red dashed line shows the relation followed by the spiral galaxies out of the M_* -selected sample with a 1σ scatter of 0.4 dex from [34]. Panel (b): The t_{dep} (HI) vs. sSFR diagram of LSBGs. Blue filled circles denote Cao23 ELSBGs with HI detection, gray triangles denote dwarf LSBGs from [10], and cyan triangles indicate HI-rich dwarf LSBGs from [25]. The red star symbol is the mean value of Cao23 ELSBGs, while the gray and cyan stars represent the mean values for dwarf LSBGs and HI-rich dwarf LSBGs, respectively.

We show the sSFR and M_* (sSFR- M_*) relation in Figure 7. The sSFR values of Cao23 ELSBGs derived from $\text{SFR}_{\text{cigale}}$. The sSFR values for the majority of Cao23 ELSBGs fall in the range of 0.1 to 0.01 Gyr^{-1} . Notably, a subset of ELSBGs exhibits higher sSFR values exceeding 0.1 Gyr^{-1} . Thirty-five Cao23 ELSBGs with HI detection show average higher sSFR values to other Cao23 ELSBGs. The sSFR shows a large scatter below $10^{8.5} M_{\odot}$ in Figure 7. The sSFR values of dwarf LSBGs [10] show a systematically lower sSFR than those of HI-rich UDGs [83] when considering stellar masses below $10^{8.5} M_{\odot}$. Specifically, the mean sSFR for dwarf LSBGs and HI-rich UDGs with $M_* < 10^{8.5} M_{\odot}$ stands at 0.04 and 0.16 Gyr^{-1} , respectively. GLSBGs and/or massive Cao23 ELSBGs on average have lower sSFR values in Figure 7.

HI-rich dwarf LSBGs exhibit higher sSFRs than the low-HI-gas fractions dwarf LSBGs at the low-mass end. The authors of [31] explored the molecular gas content in nine

HI-rich LSBGs and found that these galaxies may have higher star formation efficiency (SFE; defined as SFR/M_{H_2}) compared to typical star-forming galaxies. This suggests that HI-rich dwarf LSBGs may contain more molecular gas than low-HI-fraction dwarf LSBGs, contributing to their elevated sSFR.

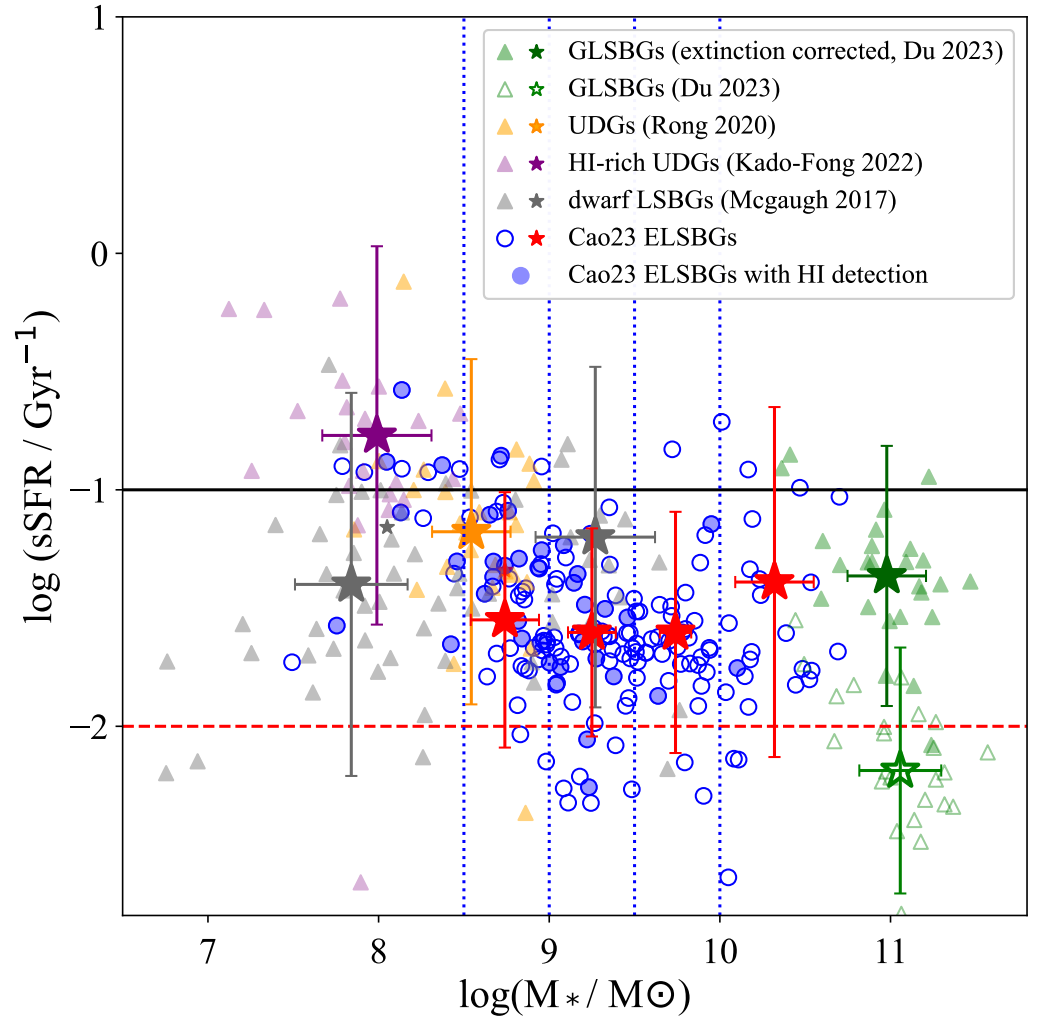


Figure 7. The sSFR- M_* relation for LSBGs. Blue open circles denote Cao23 ELSBGs, gray triangles represent dwarf LSBGs from [10], and orange triangles and plum triangles distinguish UDGs from [83,86], respectively. The blue dotted lines demarcate the boundaries of each stellar bin, with intervals of 0.5 dex in $\log(M_*/M_\odot)$ spanning from 8.5 to 10.5. Stellar masses falling below 8.5 and exceeding 10.5 are grouped into single bins, respectively. The red star symbols signify the mean values within each stellar bin. The black line is at $\log(\text{sSFR}/\text{Gyr}^{-1}) = -1.0$. Furthermore, a red dashed line at $\log(\text{sSFR}/\text{Gyr}^{-1}) = -2.0$ provides sSFR thresholds with passive galaxies typically falling below the red line. Purple and gray star symbols represent the mean values of HI-gas UDGs from [83] and dwarf LSBGs from [10] with $\log(M_*/M_\odot) < 8.5$. The IMF has been corrected to Chabrier IMF for all data points.

6. Non-Parametric Star-Formation History of Cao23 ELSBGs

Parametric models are widely employed for inferring the SFH of galaxies through the SED fitting technique [95]. However, this method relies on prior physical parameters [96,97]. The non-parametric SFH [98] assumes a constant SFR in each interval of a cosmic time grid instead of an exponential form of the SFR(t) [99–101].

We use the SED-fitting code PROSPECTOR [102] to fit the photometric data from an FUV to an NIR of 192 Cao23 ELSBGs. We adopt the non-parametric fixed-bin SFH models

preferred by [98]. The non-parametric fixed-bin SFH is described by a piecewise function where the SFR is a constant in each of the N time bins, and the edges of each time bin are fixed. The SFR in each fixed time bin is determined using the “continuity” prior, which places a Student-t prior on the log of the ratio of the SFR in adjacent bins ($\log \text{SFR}_{\text{ratio}}$). We use the same $N = 7$ time bins (the edges are 0 Gyr, 0.03 Gyr, 0.1 Gyr, 0.33 Gyr, 1.1 Gyr, 3.6 Gyr, 11.6 Gyr, 13.7 Gyr) as [98] in our non-parametric SFH and apply [58] IMF. The dust type is chosen as the default power-law curve. The free parameters of dust attenuation and stellar metallicity apply flat priors over $0 < \tau_V < 3$ and $-2 < (\log Z/Z_\odot) < 0.19$. The redshift is fixed to SDSS spectroscopic redshift. We choose an ensemble Markov chain Monte Carlo (EMCMC, [102]) sampler to fit the model.

We compare the stellar mass assembly histories in different stellar bins. We show the on-average cumulative SFH in Figure 8. The low-mass ELSBGs ($10^{7.8} \leq M_* \leq 10^{9.0} M_\odot$) exhibit a slower stellar assembly history on average compared with high-mass ELSBGs ($M_* > 10^{9.0} M_\odot$). The low-mass galaxies build 80% of their stellar mass at look back time 1.4 Gyr, while the high-mass galaxies do so at look back time 3.7 Gyr. Low-mass ELSBGs assembled their 50% and 90% stellar masses at look back time 4.0 Gyr and 0.7 Gyr, respectively. High-mass ELSBGs assembled their 50% and 90% stellar masses at look back time 6.6 Gyr and 1.9 Gyr, respectively.

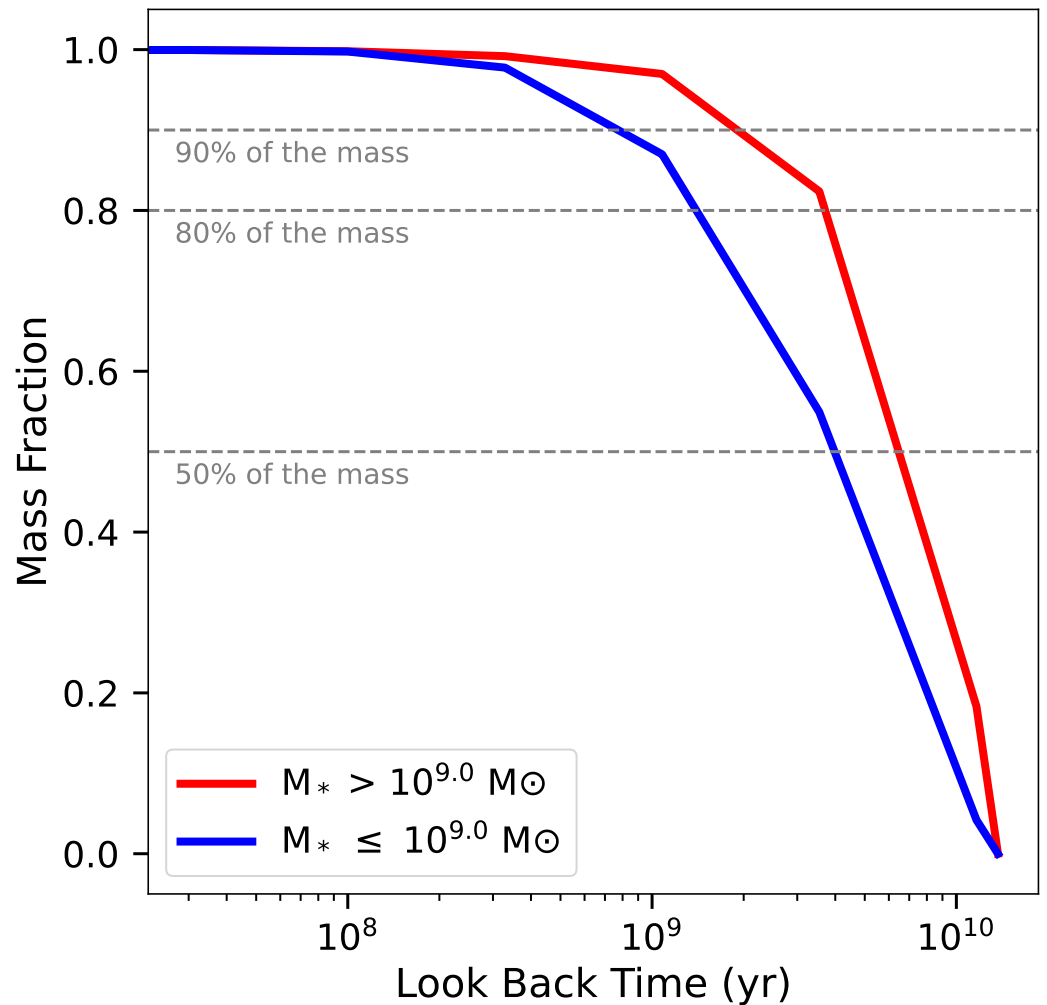


Figure 8. The mass growth curve through the look back times. The red line represents the mean value for those Cao23 ELSBGs with $M_* > 10^{9.0} M_\odot$, and the blue line represents the mean value for those Cao23 ELSBGs with $M_* \leq 10^{9.0} M_\odot$.

Figure 8 illustrates the downsizing paradigm in LSBGs. The authors of [23] analyzed the stellar population of Cao23 EL SBGs using SDSS fiber spectra, finding that more massive Cao23 EL SBGs are dominated by older stellar populations, supporting evidence for downsizing [103]. Ref. [104] noted an inverse correlation between galaxy mass and star formation duration (i.e., downsizing) by examining the $[\alpha/\text{Fe}]$ abundance with variable galaxy-wide IMF. Ref. [23] also show an α -enhancement in massive Cao23 EL SBGs, which is consistent with the downsizing trend [103,104]. Additionally, ref. [92] discussed the lower star formation efficiencies in more massive galaxies, and massive disk galaxies initiate star formation earlier than their low-mass counterparts with variable galaxy-wide IMF. The findings from Cao23 EL SBGs align with prior studies on normal spiral and elliptical galaxies [92,103–105]: massive LSBGs tend to have lower sSFRs, while low-mass EL SBGs form later than their massive counterparts. These results suggest that LSBGs share similar stellar build-up histories with normal galaxies.

7. Conclusions

This paper investigates the star formation rate and star formation history of EL SBGs from [23]. The principal outcomes are summarized as follows:

1. We compare Cao23 EL SBGs with HI-rich dwarf EL SBGs from [70] and super-thin (ST) galaxies from [73]. These EL SBGs have wide range luminosities ($-22 < M_r < -13$). The mean value of r_s for Cao23 EL SBGs is 3.19 ± 1.48 kpc, which is larger than that of HI-rich dwarf EL SBGs. Cao23 EL SBGs also show a redder (g-r) color than that of HI-rich dwarf EL SBGs. Cao23 EL SBGs are on average more massive ones compared to HI-rich dwarf LSBGs. We use the same method as [73] regarding the derived $\text{SFR}_{\text{MAGPHYS}}$. Cao23 EL SBGs and STs share a similar position in the M_* -SFR relation. The comparison results suggest that Cao23 EL SBGs share similar properties with other LSBGs.
2. We estimated the SFR by WISE W3 luminosity and SED fitting methods. SFRs of Cao23 EL SBGs are below the main sequence in the M_* -SFR relation. The sSFR of EL SBGs are mainly in the range of $0.01\text{--}0.1 \text{ Gyr}^{-1}$.
3. The HI-rich dwarf LSBGs show larger sSFR and shorter t_{dep} values than low-HI gas fraction dwarf LSBGs, which means higher HI-gas content dwarf LSBGs tend to have higher SFRs. HI-rich dwarf LSBGs likely contain more molecular gas than their low HI-gas fraction counterparts, contributing to their higher sSFR. In contrast, GLSBGs and more massive Cao23 EL SBGs tend to have lower sSFR values on the sSFR- M_* relation.
4. We acquire the non-parametric SFHs of EL SBGs by SED fitting. The SFHs are divided into seven bins of look back time, and the SFR in each bin is assumed to be constant. We find that high-mass ($M_* > 10^{9.0} M_\odot$) EL SBGs assembled mass at an earlier time than that of low-mass EL SBGs. Combined with the results from the fiber spectra in [23], we conclude that our results support a downsizing trend for LSBGs.

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Data Availability Statement: The derived data generated in this research will be shared on reasonable request to the corresponding author.

Conflicts of Interest: The authors declare no conflicts of interest.

Appendix A

We list all of the input parameters settings of CIGALE used in Section 4.2.

Table A1. Parameters setting of each module in code CIGALE.

Modules	Parameters	Values
sfhdelayedbq	tau_main	500, 750, 1100, 1700, 2600 3900, 5800, 8800, 11000 (Myr)
	age_main	2000, 4500, 7000, 9500, 12000 (Myr)
	age_bq	0.0 (Myr)
	r_sfr	0.01, 0.03, 0.1, 0.3, 1.0, 3.0, 10
	sfr_A	1.0 ($M_{\odot}\text{yr}^{-1}$)
bc03	imf	Chabrier
	metallicity	0.0001, 0.0004, 0.004, 0.008. (M_{\odot})
	separation_age	10 (Myr)
nebular	logU	−2.0
distant_modified_starburst	E_BV_lines	0.0, 0.005, 0.0075, 0.011, 0.017, 0.026, 0.038, 0.058, 0.13, 0.2, 0.44, 0.66, 1.0 (mag)
	E_BV_factor	0.25, 0.50, 0.75
	Amplitude of the UV bump	0.0
	Powerlaw_slope	0.0
	Ext_law_emission_lines	Milky Way
themis	Rv	3.1
	qhac	0.02, 0.06, 0.10, 0.17, 0.24, 0.28
	umin	0.1, 0.15, 0.3, 0.35, 0.4 0.5, 0.6, 0.7, 0.8, 1.2, 2.0
	alpha	2.0
	gamma	0.0, 0.001, 0.002, 0.004, 0.008 0.016, 0.031, 0.063, 0.13, 0.25, 0.5

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