

*Article*



# **Evolution of Rotating Internal Channel for Heat Transfer Enhancement in a Gas Turbine Blade**

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**Abstract:** To achieve higher thermal efficiency in a gas turbine, increasing the turbine inlet temperature is necessary. The rotor blade at the first stage tolerates the highest temperature, and the serpentine internal channel located in the middle chord of the rotor blade is vital in guaranteeing the blade's service life. Therefore, it is essential to illustrate the evolution of the rotating internal channel in a gas turbine blade. In the paper, the influence of the Coriolis force, including its mechanisms, on the conventional rotating channel are reviewed and analyzed. A way to utilize the positive heat transfer effect of the Coriolis force is proposed. Recent investigations on corresponding novel rotating channels with a channel orientation angle of 90° (called bilaterally enhanced U-channels) are illustrated. Moreover, numerical investigations about the *Re* effects on bilaterally enhanced smooth U-channels were carried out in the study. The results indicated that bilaterally enhanced U-channels can utilize the Coriolis force positive heat transfer effect on the leading and the trailing walls at the same time. *Re* and *Ro* are vital non-dimensional numbers that influence the performance of bilaterally enhanced U-channels. *Re* and *Ro* have an independent influence on the heat transfer performance of the bilaterally enhanced U-channel. *Ro* is good for the heat transfer of the bilaterally enhanced U-channel on both the leading and the trailing walls. Therefore, the bilaterally enhanced U-channel is suitable for application in the middle chord region of a turbine blade, since it can utilize the rotation effect of the rotating blade to improve the heat transfer ability of the blade and thus reduced the blade temperature. At the same *Ro*, *Re* positively affects the *Nu* on the leading and the trailing walls of the Coriolis-utilization rotating smooth U-channel, but plays a negligible role on *Nu/Nu*<sup>0</sup> .

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**Keywords:** gas turbine; blade cooling; review; rotating channel; Coriolis force utilization

### **1. Introduction**

Gas turbines possess merits such as compact size, high power output and long service life. Therefore, they are widely utilized in life and in production. Since it is crucial to achieve high thermal efficiency for the development of gas turbines, advanced gas turbines are steadily increasing their turbine inlet temperature and achieving higher efficiency. The highest gas temperature recorded exceeded 1700  $\degree$ C, which is well above the material limits of the blades [\[1\]](#page-19-0). To overcome the consequent high heat loads, especially in the first stage of the turbine blades, it is necessary to utilize an efficient blade cooling structure. A serpentine internal channel is a conventional internal cooling structure, which is widely used in the first stage of turbine rotor blades, as depicted in Figure [1](#page-1-0) [\[2\]](#page-19-1).

To achieve better cooling performance of the internal channels, many researchers have put their endeavors into this area [\[3](#page-19-2)[–12\]](#page-19-3). Furthermore, a review of the research state of the subject of gas turbine internal channels is a must to help more engineers and scholars clearly learn the research progress and provide guidelines for future study directions.

At the beginning of the 21st century, Han J. and Dutta S. [\[13\]](#page-19-4) reviewed the research development of the internal cooling of a gas turbine before the year 2000. At that time, the

operational temperature of an advanced gas turbine was in the range of 1200 ◦C to 1400 ◦C. They summarized the effect of ribs with different shapes, 180° turn regions, and combined cooling structures, such as ribs combined with dimples, on the heat transfer performance of internal cooling under non-rotation conditions. Moreover, the rotation effect on the heat transfer characteristics of smooth and ribbed channels was illustrated as well. They concluded that compared to a ribbed rotating channel, a smooth rotating channel was more sensitive to the rotation effect. The trailing or leading wall with a faster flow due to the Coriolis force had a higher heat transfer ability. Ligrani P. et al. [\[14\]](#page-19-5) provided a review of the flow and heat transfer features of the heat transfer enhancement techniques before the year 2003. These techniques included a pin-fin array structure, a dimpled surface and a ribbed channel. The heat transfer distributions and flow patterns of these cooling augmentation structures under non-rotational conditions obtained by experiments and numerical studies were presented and discussed. The results indicated that the heat transfer ability of the ribbed channel was better than the dimple–protrusion–smooth channel, while the former pressure loss was higher than the latter. Moreover, with the same pressure loss coefficient, the heat transfer of a ribbed channel was greater than the pin fin. A dimple–smooth channel had the highest thermal performance parameter, but a pin-fin channel processed the lowest. Han J. [\[15\]](#page-19-6) reviewed the research on turbine blade cooling before the year 2004. The heat transfer performance of internal channels with different aspect ratios, ribs, channel orientation angles and wall temperatures under stationary and rotating conditions were reviewed. The results showed that stationary channels with V ribs and delta-shaped ribs had superior heat transfer performance. The rotation effect was more obvious on the first channel than on the second channel, while it was less obvious on the ribbed channel than the smooth channel due to less portion contribution on heat transfer than ribs. The flow temperature distributions in a rotating channel were provided as well. What is more, turbulent models used for rotating channel performance prediction were reviewed. They concluded that the k-ε model cannot obtain correct simulation results, but that the low Reynolds number k-ω model can achieve reasonable simulation results.

<span id="page-1-0"></span>

**Figure 1.** Schematic of internal channel in rotor blade [2]. **Figure 1.** Schematic of internal channel in rotor blade [\[2\]](#page-19-1).

During the second decade of the 21st century, Wright L. and Han J. [\[16\]](#page-19-7) presented a review focusing on the mechanisms and approaches for heat transfer augmentation of turbine blade internal cooling in the last decade before 2013. They reviewed various turbulators used for heat transfer enhancement, including pin-fin, dimple, lattice, and continuous and broken ribs with different angles. Compound cooling approaches, such as dimples and short pins, were demonstrated as well. They concluded that stationary channels with V- and W-shaped ribs had better heat transfer performance than the channels with straight, continuous ribs and that channels with broken ribs possessed higher heat

transfer ability than the ones with continuous ribs. Moreover, stationary channels with dimples had lower heat transfer performance and pressure loss than ribbed channels. However, the channels with lattices are not be suitable for rotating blades due to the heavy weight. Meanwhile, the channels with dimples may not be appropriate for rotating blades as well, because the dimple induced light weight leads to weak material strength. A compound structure, such as lattices with dimples, is an alternative cooling approach for gas turbines. Plus, the rotation effect on the channel's heat transfer was illustrated. Channels with lattices were less affected by rotation. Studies under near-realistic engine conditions were demonstrated as well. Ligrani P. [\[17\]](#page-20-0) reviewed the heat transfer enhancement approaches for a blade's internal cooling before 2013. The structures for internal stationary channel heat transfer improvement, such as ribs, pin-fin, dimple, protrusion and a combination of them, were demonstrated. He found that the thermal performance of these structures prior to 2003 had less difference from that during 2003 to 2013. For a rotating channel, experiments of PIV were carried out to capture the vortices induced by the Coriolis force and the band region. More detailed studies on the heat transfer performance of conventional rotation channels were conducted, such as bend region heat transfer and flow characteristics, boundary layer and heat condition effects on channel heat transfer. Moreover, existing research conditions, like ranges of *Re*, *Ro*, *Buo* and inlet density ratio, were illustrated as well. Bunker R. [\[18\]](#page-20-1) wrote a piece of literature in 2017 focusing on the evolution of turbine cooling based on background, current state and prospects. He reviewed the development of turbine cooling over the last 50 years and proposed that the evolution of turbine cooling was like animal evolution. The turbine cooling technologies progressed from simple to complex structures supported by advanced manufacture and materials. Ekkad S. V. and Singh P. [\[19\]](#page-20-2) reviewed heat transfer measurement approaches and test benches for rotating internal and external cooling structures in 2020. The principles and calibrations of liquid crystal thermography and infrared thermography used for internal channels were illustrated. Lots of experimental results were provided, offering researchers guidance to design next-generation cooling concepts for gas turbines.

Nowadays, in the third decade of the 21st century, Du W. et al. [\[20\]](#page-20-3) presented an overview of the heat transfer of a trailing edge in a gas turbine blade in 2021. The internal cooling structures utilized in the trailing region, such as pin-fin, dimple, protrusions, latticework and labyrinth, were summarized. The heat transfer characteristics of these structures were illustrated as well. Yeranee K. and Yu R. [\[21\]](#page-20-4) wrote a review about the rotation effect on an internal cooling structure in 2021. Rotating effects on existing cooling structures with rib, pin-fin, jet impingement, dimple, protrusion and swirl cooling were summarized. Numerical modeling and test approaches to study the performance of rotating internal cooling structures were reviewed as well. They recommended that studies on rotating channels with ribs and pin fin at high *Re* and *Ro* should be carried out more because ribs and pin fin affected the distribution and uniformity of *Nu*, which was vital for the rotor blade to avoid local hot spots. In addition, channels with dimples were more suitable for compound cooling structures with ribs or protrusions to augment heat transfer. What is more, many correlations were summarized, while correlations for rotating channels with dimples, latticework and protrusion are fewer, and so should be further investigated.

According to a review of the literature above, heat transfer augmentations, such as ribs, dimples, protrusions and latticework for stationary internal channels have been widely researched and compared. The rotation effect, especially the Coriolis effect, on the heat transfer characteristics of a conventional rotating channel was reviewed with the conclusion of bringing heat transfer augmentation and deficit at the same time on the leading and the trailing walls. Meanwhile, the studies on conventional rotating internal channels were increasingly detailed, and more advanced experimental measurement approaches were adopted as time went on. However, rotation is a vital factor affecting the heat transfer performance of an internal rotating channel, where the Coriolis force plays a critical role. How does the rotating internal channel in a gas turbine evolve under rotating conditions? Can we eliminate unfavorable heat transfer features induced by the Coriolis force, but

utilize its beneficial heat transfer function? To solve these questions, in this paper, the influence of the Coriolis force, including its mechanisms, on conventional rotating channels is reviewed and analyzed. A way to utilize the positive heat transfer effect of the Coriolis force is proposed. Recent investigations on corresponding novel rotating channels (called bilaterally enhanced U-channels) are illustrated as well. The novelties of these channels are that their channel orientation angle is  $90^{\circ}$  to the rotating shaft and that, therefore, the direction of the Coriolis force points to the pressure and suction sides simultaneously, which eliminates the heat transfer deficit in the conventional rotating U-channel and even utilizes the positive heat transfer enhancement effect on both the pressure and the suction sides. Non-dimensional numbers *Re* and *Ro* are essential to a rotating channel's performance; however, there is less literature covering the *Re* effect on bilaterally enhanced U-channels. Thus, the *Re* effects on heat transfer and pressure loss ability are simulated and discussed in this paper.

#### **2. Influence of Coriolis Force**

Before the 1970s, the research on rotating channels mainly focused on the effect of the Coriolis force on the flow patterns and pressure loss. The purpose of the research was to understand how the Coriolis force, induced by rotation, influences the flow characteristics of the outflow fluid in the radial passage of centrifugal compressors and radial pumps, leading to different velocity profiles, pressure loss coefficients and turbomachinery efficiencies [\[22,](#page-20-5)[23\]](#page-20-6). Therefore, investigations on the flow characteristics of a rotating channel were necessary. Some study results indicated that the Coriolis force enhanced the instability of a turbulent flow. In a straight rotating channel with a rectangular cross-section, the rotation played a negative role in the pressure loss coefficient of the suction side and caused a thicker boundary layer on the leading wall [\[24\]](#page-20-7). In a straight rotating channel with a circular cross-section, the pressure loss coefficient was higher in the laminar region, but smaller in the turbulent region [\[25\]](#page-20-8). Before the 1970s, studies that focused on the heat transfer performance of a rotating channel applied in a turbine were fewer. This is because the convection heat transfer of the internal cooling structure used in the blade had only just been developed in the 1970s [\[23\]](#page-20-6). In 1979, Morris W. D. and Ayhan T. [\[26\]](#page-20-9) completed research on a straight rotating internal tube with a rectangular cross-section. The result illustrated that the influence of the Coriolis force must be considered. This is because the actual measured blade temperature would be higher without the Coriolis force being considered.

Therefore, the Coriolis force is a dominant factor that influences the flow patterns and heat transfer features in a rotating internal cooling channel of a blade. It is an inertia force and exists when the directions of angular velocity vectors and flow velocity are not parallel. The direction of the Coriolis force is perpendicular to the plane formed by the vectors of angular velocity and flow velocity based on the right-hand rule. The Coriolis force is normalized by a dimensionless number called rotation number *Ro*.

#### <span id="page-3-0"></span>*2.1. Mechanisms of Coriolis Force Effect on Heat Transfer*

Before the 1980s, many researchers [\[26–](#page-20-9)[32\]](#page-20-10) paid more attention to the heat transfer of rotating channels with circular cross-sections. Figure [2](#page-4-0) depicts the concept of the inner channel structure of a rotor blade [\[33\]](#page-20-11). The cross-section of the internal channel near the leading edge can be modeled as a rectangle with  $AR = 1:2$ . The passage located at the middle chord can be simplified as a square cross-section with  $AR = 1:1$ . The passages close to the trailing edge are more suitable to be regarded as a wedge-shaped or rectangular cross-section with  $AR = 2:1$  or 4:1. Therefore, rotating internal channels that are square, rectangular and wedge-shaped fit the shape of the rotor blade well, attracting increasingly more researchers to focus on them [\[34](#page-20-12)[–53\]](#page-21-0). Since a smooth rotating channel has no turbulators, the mechanisms of the Coriolis force effect on the heat transfer of a rotating internal channel can be more clearly revealed.

<span id="page-4-0"></span>

channel can be more clearly revealed.

**Figure 2.** Concept of inner channel structure of a rotor blade [33]. **Figure 2.** Concept of inner channel structure of a rotor blade [\[33\]](#page-20-11).

Son et al. [\[54\]](#page-21-1) executed experiments on a rotating smooth U-duct with a square section. Counter-rotating vortices induced by the Coriolis force were observed. And the sition where the vortices impinged had a higher *Nu*. Hosseinalipour et al. [55] conducted position where the vortices impinged had a higher *Nu*. Hosseinalipour et al. [\[55\]](#page-21-2) conducted experiments on a square smooth channel with a *Ro* in the range of 0 to 0.15. The result in the range of 0 to 0.15. indicated that as the *Ro* increased, the *Nu* on the leading wall of the radial outward pass decreased, while the *Nu* on the trailing wall of the radial outward pass went up because of of the Coriolis force. Qiu et al. [56] analyzed the heat transfer of a rotating smooth two-pipe with a square cross-section. The overall *Nu* rose with a rising *Ro*. Deng et al. [\[57\]](#page-21-4) pass pipe with a square cross-section. The overall *Nu* rose with a rising *Ro*. Deng et al. [57] demonstrated that on the radial outward flow pass of a rotating smooth square U-channel, demonstrated that on the radial outward flow pass of a rotating smooth square U-channel, the heat transfer on the trailing wall was always higher than that on the leading wall. the heat transfer on the trailing wall was always higher than that on the leading wall. Moreover, a heat transfer enhancement on the trailing wall and a heat transfer deficit on Moreover, a heat transfer enhancement on the trailing wall and a heat transfer deficit on the leading wall existed when *Ro* was varied from 0 to 0.1. On the radial inward flow pass, the heat transfer of the leading wall was higher than that of the trailing wall, which showed a positive trend with a *Ro* ranging from 0 to 0.1. Meanwhile, the heat transfer of the trailing wall demonstrated a negative trend. Those heat transfer characteristics were induced by the Coriolis force effect. What is more, for the rotating passage with an irregular cross-section, Li H. et al. [\[58\]](#page-21-5) conducted experiments on a smooth U-pipe with an irregular cross-section of engine similar. They found that on the pressure side of the radial outward flow pass, the rotation augmented the *Nu* up to 4.3 times while having little influence on the other surfaces. Tao et al. [\[59\]](#page-21-6) studied a rotating wedge-shaped smooth passage. The result indicated that the *Nu* ratio of the suction to the pressure sides went down because the Coriolis force was more vertical to the pressure and the suction sides. indicated that as the *Ro* increased, the *Nu* on the leading wall of the radial outward pass the Coriolis force. Qiu et al. [\[56\]](#page-21-3) analyzed the heat transfer of a rotating smooth two-pass

It can be concluded that a conventional rotating smooth channel has higher heat transfer on the pressure side of the radial outward flow pass and suction side of the radial inward flow pass but possesses lower heat transfer on the suction side of the radial outward flow pass and pressure side of the radial inward flow pass  $[60-74]$ . The reason why these heat transfer characteristics exist is because of the influence of the Coriolis force, which can be explained based on Figure [3.](#page-5-0) According to Figure [3,](#page-5-0) the side with the Coriolis force pointing at it has Coriolis-induced secondary flow flushing and thus possesses higher heat transfer performance, while the side with Coriolis force pointing opposite has lower heat transfer because of the secondary flow leaving. Therefore, the heat transfer difference between the pressure side and the leading side of a rotating passage is significant, leading to an obvious non-uniform heat transfer distribution.

<span id="page-5-0"></span>

cant, leading to an obvious non-uniform heat transfer distribution.

Figure 3. Direction of Coriolis force in a conventional rotating internal channel of a turbine blade.

# <span id="page-5-3"></span>2.2. Interaction Mechanisms of Coriolis Force and Turbulators on Flow Pattern

<span id="page-5-1"></span>Turbulators, especially ribs, are always arranged on the leading and trailing walls of the internal serpentine channel to enhance heat transfer ability. Slanting straight ribs configured on both the leading and the trailing walls can induce secondary flow in a stationary passage, as shown in Figure 4 [75]. [A](#page-5-1) pair of vortices exist in the pass as depicted with the two black circles with arrows. The circulation direction of the secondary flow depends on the rib and main flow orientations. Moreover, in a non-rotational channel, V-ribs that are arranged on both the leading and the trailing walls cause two pairs of vortices, as depicted in plane P1 and P2 of Figure [5](#page-5-2) [\[76\]](#page-22-2). The circulation direction of the secondary flow depends on the V-rib and main flow orientations as well.



Figure 4. Straight rib-induced secondary flow in a stationary passage [[75\]](#page-22-1).

<span id="page-5-2"></span>

**Figure 5.** V-rib-induced secondary flow in a stationary channel [\[76](#page-22-2)]. **Figure 5.** V-rib-induced secondary flow in a stationary channel [76].

The common flow characteristic of a non-rotational ribbed channel is that the secondary flow near the ribbed wall always flows along the rib and main-flow direction and dominates the whole direction of the secondary flow.

When a channel is under rotating conditions, as illustrated in Figure  $6$  [\[76\]](#page-22-2), the Coriolisinduced secondary flow near the trailing wall strengthens the secondary flow induced by the V-ribs on the trailing wall, thus enhancing the heat transfer, while weakening the by the V-ribs on the trailing wall, thus enhancing the heat transfer, while weakening the secondary flow caused by the V-ribs on the leading wall, leading to a heat transfer deficit. secondary flow caused by the V-ribs on the leading wall, leading to a heat transfer deficit. With the flow going along the passage, the rib-induced secondary flow near the leading With the flow going along the passage, the rib-induced secondary flow near the leading wall disappears, and the Coriolis-induced secondary flow merged with the rib-induced secondary flow dominates the channel flow structure. This is because the circulation direction of the rib-induced secondary flow near the trailing wall is the same as that of the Coriolis-induced secondary flow, but the rib-induced secondary flow near the leading wall Coriolis-induced secondary flow, but the rib-induced secondary flow near the leading is opposite.

<span id="page-6-0"></span>

**Figure 5.** V-rib-induced secondary flow in a stationary channel [76].

**Figure 6.** V-rib-induced secondary flow in a rotating channel [\[76](#page-22-2)]. **Figure 6.** V-rib-induced secondary flow in a rotating channel [76].

Therefore, when the circulation direction of the rib-induced secondary flow near the Therefore, when the circulation direction of the rib-induced secondary flow near the trailing or leading wall is the same as the Coriolis-induced secondary flow, the strength trailing or leading wall is the same as the Coriolis-induced secondary flow, the strength of the secondary flow can be enhanced and be good for heat transfer. Meanwhile, as the of the secondary flow can be enhanced and be good for heat transfer. Meanwhile, as the circulation direction of the rib-induced secondary flow near the trailing or leading wall is circulation direction of the rib-induced secondary flow near the trailing or leading wall is opposite to the Coriolis-induced secondary flow, the secondary flow can be weakened and opposite to the Coriolis-induced secondary flow, the secondary flow can be weakened and can even disappear, which leads to a heat transfer deficit. Consequently, the Coriolis effect brings both benefits and deficits with regard to the heat transfer of conventional ribbed brings both benefits and deficits with regard to the heat transfer of conventional ribbed rotating channels, as illustrated in Figur[e 7](#page-6-1) [77]. rotating channels, as illustrated in Figure 7 [\[77\]](#page-22-3).

<span id="page-6-1"></span>

**Figure 7.** Coriolis force effect on heat transfer of conventional, ribbed rotating channel [77]. **Figure 7.** Coriolis force effect on heat transfer of conventional, ribbed rotating channel [\[77\]](#page-22-3).

According to Sections [2.1](#page-3-0) and [2.2,](#page-5-3) under rotating conditions, the Coriolis force has both positive and negative influences on the heat transfer performance of conventional intervals. internal channels? Trowever, how can we further enhance the heat transfer ability of fotating<br>internal channels? Can we eliminate the negative heat transfer effect of the Coriolis force internal channels. Can we eliminate the negative heat transfer effect of the Coriolis force whilst also utilizing the positive heat transfer effect of the Coriolis force on the trailing and<br>leading suall simultaneously? leading wall simultaneously? internal channels. However, how can we further enhance the heat transfer ability of rotating

#### **3. Utilization of Coriolis Force**

The answer to the question above is "Yes". Many scholars [\[78–](#page-22-4)[80\]](#page-22-5) tried to weaken the Coriolis force's negative effect on the rotating internal channel. They found that when a rotating channel has a channel orientation angle with a rotation shaft as depicted in Figure [1,](#page-1-0) the Coriolis-induced secondary flow was altered in the channel. And, the Coriolis force influence on the heat transfer was weakened compared to the rotating channel without a channel orientation angle, resulting in the heat transfer on the leading wall of the radial outward flow pass being augmented [\[81\]](#page-22-6). Moreover, lately, some researchers [\[77](#page-22-3)[,82](#page-22-7)[,83\]](#page-22-8) attempted to utilize the Coriolis force positive heat transfer effect on leading and trailing walls simultaneously.

#### *3.1. Weakening the Coriolis Force's Negative Heat Transfer Effect*

If the Coriolis force's negative effect on heat transfer is weakened, the strength of the Coriolis force perpendicular to the trailing and leading walls will also decline. When a rotating channel has a channel orientation angle with a rotation shaft as depicted in Figure [1,](#page-1-0) based on the right-hand rule, the direction of the Coriolis force is not vertical to the trailing and leading walls. Hence, the Coriolis component force perpendicular to the leading and trailing wall can be reduced, leading to the Coriolis force's negative effect on heat transfer being weakened. Tao et al. [\[59\]](#page-21-6) investigated a wedge-shaped smooth channel with a rotating condition and found that the average Nu ratio of the suction to the pressure sides was prone to channel orientation. Al-Hadhrami et al. [\[83\]](#page-22-8) analyzed the channel orientation angle effect on a rotating U-duct. They revealed that the orientation angle weakened the heat transfer difference between the suction and the pressure sides induced by the Coriolis force. Li Y. et al. [\[84](#page-22-9)[–86\]](#page-22-10) studied a U-channel under rotating conditions. Two orientation angles of 22.5◦ and 45◦ were comparatively studied. A similar conclusion was obtained that since the angle existed, the heat transfer difference between the suction and the pressure sides was lower than the channel without an orientation angle.

Hence, it can be concluded that when there is a channel orientation angle for a rotating channel, the Coriolis force effect on the suction and the pressure sides is weakened, leading to heat transfer differences between the suction sides and the pressure sides going down, meaning the Coriolis force's negative effect on heat transfer is weakened. Furthermore, though the Coriolis force's negative effect on heat transfer can be weakened, the Coriolis force's positive effect on heat transfer is weakened as well due to the reduced Coriolis force strength imposed on the pressure and suction sides.

#### <span id="page-7-0"></span>*3.2. Utilizing the Coriolis Force's Positive Heat Transfer Effect*

# 3.2.1. Principle of Heat Transfer Augmentation and Study State

If the Coriolis force's positive heat transfer effect can be utilized on the leading and the trailing walls simultaneously, the direction of the Coriolis force should point to the leading and the trailing walls at the same time. Considering the rotating vector direction and the cooling flow direction by using the right-hand rule, if the cooling air only initially flows along the pressure side, goes through a bend close to the blade tip, and then enters the pass flowing along the suction side (a channel orientation angle of  $90^{\circ}$ ), then a Coriolis force pointing to the leading and trailing walls simultaneously can be achieved. The flow mechanisms of the channel with a channel orientation angle of 90◦ are illustrated in Figure [8.](#page-8-0) It should be noted that only if the main flow goes from the pass near the pressure side, and then enters the pass near the suction side, can the direction of the Coriolis force point to the leading and the trailing walls at the same time, bringing in heat transfer enhancement on both the pressure and the suction sides. However, if the flow direction is reversed, the direction of the Coriolis force would point to the partition wall, resulting in a heat transfer deficit on both the pressure and the suction sides simultaneously, which is not desirable.

<span id="page-8-0"></span>

desirable.<br>Listen desirable

**Figure 8.** Flow mechanisms induced by Coriolis force inside a rotating smooth channel with channel **Figure 8.** Flow mechanisms induced by Coriolis force inside a rotating smooth channel with channel orientation angle of 90°.

Dutta and Han [87] investigated a ribbed two-pass channel in a rotating state. The Dutta and Han [\[87\]](#page-22-11) investigated a ribbed two-pass channel in a rotating state. The orientation angle was 90°. It turned out that the rotating channel with an orientation angle of 90° achieved better heat transfer augmentation than the conventional rotating angle of 90° achieved better heat transfer augmentation than the conventional rotating channel without an orientation angle. Singh P. et al. [\[77\]](#page-22-3) studied a rotating two-pass channel with ribs. Its orientation angle was 90° as well. The result showed that the Coriolis force played a positive role in the heat transfer of both the suction and the pressure sides. Tafti D. et al. [\[88\]](#page-22-12) numerically studied a ribbed rotating channel with an orientation angle of 90°, as depicted in Figu[re](#page-8-1) 9 by LES, which revealed that compared to the stationary state, this novel rotating channel had a 10% increment of heat transfer and a 10% decrement of pressure loss. The lower pressure loss was probably because of centrifugal and buoyancy pumping. Ma Y. et al. [\[69\]](#page-21-8) simulated a smooth rotating channel with an orientation angle of  $90°$ . They demonstrated heat transfer increases on the leading and the trailing walls as *Ro* rose due to the utilization of the Coriolis force on both walls. Moreover, they optimized the bend region width between the bend wall and the tip wall and the thickness of the divider wall between the two passages. After optimization, heat transfer performances were 20.1% and 56.6% improved on the trailing wall and the leading wall, respectively. Moreover, Smirnov E. [\[4\]](#page-19-8) also achieved the optimization of a smooth rotating channel with Moreover, Smirnov E. [4] also achieved the optimization of a smooth rotating channel with reduced, matrice experimentation angle of 90°. The result illustrated that the pressure loss was significantly reduced, which is probably because of a more uniform velocity distribution at the exit of the bend area, as illustrated in Figure [10.](#page-9-0) After optimization, the pressure in the rotating the bend area, as illustrated in Figure 10. channel was smaller than that of the non-rotational channel. we can expect water convenience wall and the trailing wall and the encoderation of the trailing wall, respectively.

<span id="page-8-1"></span>

**Figure 9.** Concept view of a rotating channel with orientation angle of 90° in a rotor blade [88]. **Figure 9.** Concept view of a rotating channel with orientation angle of 90◦ in a rotor blade [\[88\]](#page-22-12).

<span id="page-9-0"></span>

**Figure 10.** Velocity distribution in a smooth rotating channel with orientation angle of 90° [\[4\]](#page-19-8) (upper: **Figure 10.** Velocity distribution in a smooth rotating channel with orientation angle of 90◦ [4] (upper: after optimization; lower: the original structure). after optimization; lower: the original structure).

Therefore, from the above pieces of literature, the rotation is good for the heat transfer Therefore, from the above pieces of literature, the rotation is good for the heat transfer on both the leading and the trailing walls of the rotating channel with an orientation angle of 90°, due to the Coriolis force effect. Moreover, the structure benefits from pressure loss reduction [89]. Pressure loss is a vital parameter for the practical internal cooling structure reduction [\[89\]](#page-22-13). Pressure loss is a vital parameter for the practical internal cooling structure design of the turbine blade because high pressure loss always leads to a high-temperature design of the turbine blade because high pressure loss always leads to a high-temperature main flow going back into the blade, resulting in blade damage. Therefore, the rotating main flow going back into the blade, resulting in blade damage. Therefore, the rotating channel with an orientation angle of  $90°$  has the advantage of less pressure loss, meaning that it is a promising structure for practical blade internal cooling design. that it is a promising structure for practical blade internal cooling design.

3.2.2. Heat Transfer Characteristics on Suction and Pressure Sides Compared with Conventional Rotating Channel

To more clearly compare the heat transfer abilities between a conventional rotating channel and a novel rotating channel with a channel orientation angle of 90°, the average *Nu/Nu*<sup>0</sup> variations along the *Ro* on the leading and trailing walls are summarized in the paper, as depicted in Figures [11–](#page-10-0)[14.](#page-11-0)

According to Figure [11,](#page-10-0) the curves with the dashed line represent the average  $Nu/Nu_0$ variations of rotating channels with an orientation angle of 90◦ on the leading wall. And the rest of the curves represent one-pass conventional rectangular rotating channels without an orientation angle. The trends of the average  $Nu/Nu_0$  on the leading wall of one-pass conventional rectangular rotating channels mainly went down as the *Ro* increased from 0 to 0.4, except for the rotating channel with matrix turbulators due to its complicated turbulator structures. However, the trends of the average  $Nu/Mu_0$  on the leading wall of the rotating channels with an orientation angle of 90◦ are opposite, going up as *Ro* increases. The reasons for this are that the Coriolis force weakens the heat transfer on the leading wall of one-pass conventional rotating channels but augments the heat transfer on the leading wall of the rotating channels with an orientation angle of 90°.

In Figure [12,](#page-10-1) the average *Nu/Nu*<sup>0</sup> variations along the *Ro* on the leading wall of twoor three-pass conventional channels with orientation angles of  $0°$  and  $45°$  are depicted. It can be observed that the rotation effect is not obvious because the  $Nu/Nu_0$  is averaged from the leading surfaces of two or three passages.

<span id="page-10-0"></span>

**Figure 11.** Average  $Nu/Nu_0$  variations along Rø on the leading wall of one-pass channel with different cooling structures [\[69](#page-21-8)[,76,](#page-22-2)[90,](#page-22-14)[91\]](#page-22-15). **Figure 11.** Average  $Nu/Nu_0$  variation

<span id="page-10-1"></span>

**Figure 12.** Average *Nu/Nu*<sup>0</sup> variations along *Ro* on the leading wall of two- or three-pass channels with bend region with different cooling structures [\[76](#page-22-2)[,92](#page-22-16)[,93\]](#page-22-17).

<span id="page-11-1"></span>

with bend region with different cooling structures  $\mathcal{P}(\mathcal{S})$ 

**Figure 13.** Average  $Nu/Nu_0$  variations along  $Ro$  on the trailing wall of one-pass channel with different cooling structures [[69,7](#page-21-8)[6,9](#page-22-2)[0,9](#page-22-14)1]. cooling structures [69,76,90[,91\]](#page-22-15).

<span id="page-11-0"></span>

**Figure 14.** Average  $Nu/Nu_0$  variations along  $Ro$  on the trailing wall of two- or three-pass channels with bend region with different cooling structures [76,92,93]. with bend region with different cooling structures [\[76](#page-22-2)[,92](#page-22-16)[,93\]](#page-22-17).

When Figures [11](#page-10-0) and [12](#page-10-1) are comparatively analyzed, for the conventional rotating channel, rotation decreases the average heat transfer on the leading wall of one-pass conventional rectangular rotating channels, while having less effect on the average heat transfer averaged from the leading surfaces of two or three passages. Therefore, very non-uniform heat transfer induced by the Coriolis force exists on the leading walls of different passages with different flow directions when the *Ro* is smaller than 0.4. Similarly, the conclusion that very non-uniform heat transfer occurs on the trailing walls of different passages can be drawn as well, according to Figures [13](#page-11-1) and [14.](#page-11-0) However, since the  $Nu/Nu_0$ of the leading and the trailing walls in the novel rotating channel with a channel orientation angle of 90◦ rises with an increasing *Ro*, the Coriolis-induced non-uniform heat transfer effect can be avoided in the novel rotating channel. In Figure [11,](#page-10-0) the heat transfer of all the cooling rotating passages is increased as the *Ro* increases from 0 to 0.4 because of the Coriolis force-induced heat transfer augmentation, except for rotating passages with matrix turbulators due to their complicated cooling structure.

For a more focused comparison of the novel rotating channel with a channel orientation angle of 90◦ and a conventional one, the rotation effect on the heat transfer performance of the two channels is depicted in Figure [15](#page-12-0) [\[82\]](#page-22-7). Based on the Nusselt number ratio contours, the low heat transfer region in the novel channel is smaller than in the conventional rotating channel, while the low heat transfer area of the conventional rotating channel due to the heat transfer deficit induced by the Coriolis force is larger. Therefore, the Coriolis force has a negative heat transfer influence on a conventional channel. Nevertheless, the novel rotating channel avoids the negative heat transfer induced by the Coriolis force.

<span id="page-12-0"></span>

**Figure 15.** *Nu/Nu*<sup>0</sup> contours of non-rotational U-channel, conventional rotating U-channel and the **Figure 15.** *Nu/Nu*<sup>0</sup> contours of non-rotational U-channel, conventional rotating U-channel and the novel rotating U-channel [82]. novel rotating U-channel [\[82\]](#page-22-7).

Figure [16](#page-13-0) presents the rotation effect on the heat transfer ability of the novel rotating channel [\[94\]](#page-22-18). It can be clearly observed that rotation brings heat transfer enhancement on both the trailing and the leading walls, rather than a heat transfer deficit. Therefore, compared to the conventional rotating channel, the novel rotating channel does have the ability to utilize a positive rotation effect to augment the heat transfer on both the pressure and the suction sides.

<span id="page-13-0"></span>

Figure 16. Axial-average  $Nu/Nu_0$  variations along with main flow of the novel rotating channel under different *Ro* (Experiment results) [\[94\]](#page-22-18).

# **4. Reynolds Number Effect on Bilaterally Enhanced U-Channel 4. Reynolds Number Effect on Bilaterally Enhanced U-Channel**

Since a rotating channel with an orientation angle of  $90^{\circ}$  can utilize the Coriolis force heat transfer enhancement effect on both the pressure and the suction sides but has no unified name, a bilaterally enhanced U-channel is the name given to this novel rotating unified name, a bilaterally enhanced U-channel is the name given to this novel rotating paper. channel in this paper.

The non-dimensional equations for a bilaterally enhanced U-channel with incompress-ible and viscous flow are as follows [\[95\]](#page-22-19).

$$
\frac{\partial u_i}{\partial x_i} = 0 \tag{1}
$$

$$
\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} + \begin{bmatrix} -2R \cdot u_2 \\ 2R \cdot u_1 \\ 0 \end{bmatrix} = -\frac{\partial p}{\partial x_i} + \frac{1}{Re} \frac{\partial^2 u_i}{\partial x_j \partial x_j} \tag{2}
$$

Hence, based on Equations (1) and (2), *Re* and *Ro* are vital non-dimensional numbers Hence, based on Equations (1) and (2), *Re* and *Ro* are vital non-dimensional numbers that influence the performance of a bilaterally enhanced U-channel. Investigations into the that influence the performance of a bilaterally enhanced U-channel. Investigations into the effects of *Ro* and *Re* on bilaterally enhanced U-channels are essential. effects of *Ro* and *Re* on bilaterally enhanced U-channels are essential.

Accor[ding](#page-7-0) to Section 3.2, the *Ro* effect on the heat transfer of the bilaterally enhanced According to Section 3.2, the *Ro* effect on the heat transfer of the bilaterally enhanced U-channel was studied by so[me r](#page-22-12)[ese](#page-22-15)archers [88,91]. A numerical study on a bilaterally U-channel was studied by some researchers [88,91]. A numerical study on a bilaterally enhanced U-channel was carried out by our research tea[m a](#page-22-7)s well [82]. The channel structures of a conventional and novel channel with a blade are depicted [in F](#page-14-0)igure 17. The simulation results indicated that the overall heat transfer on both the leading and the ing walls of the bilaterally enhanced U-channel was better than a conventional rotating trailing walls of the bilaterally enhanced U-channel was better than a conventional rotating smooth U-channel with a *Ro* of 0.025. The Coriolis force is good for a heat transfer boost smooth U-channel with a *Ro* of 0.025. The Coriolis force is good for a heat transfer boost on both the suction and the pressure sides, leading to an improved heat transfer ability as the *Ro* increases.

<span id="page-14-0"></span>

(a) Conventional U channel (b) Bilaterally enhanced U-channel

Figure 17. Channel structures of conventional rotating U-channel and bilaterally enhanced U-channel in a blade [\[82\]](#page-22-7). channel. Consequently, to further study the *Reference of the Reference* on a smooth bilateral problem. The *Reference* of the *Reference* on a smooth bilateral problem of the *Reference* on a smooth bilateral problem. The

What is more, there is a significant gap in the bilaterally enhanced U-channel studies as there are fewer analyses on the *Re* influence on the heat transfer performance of a novel the first that the land goes of the rest minimize on the real thanks performance of a note.<br>Consequently, to further study the Re effect on a smooth bilaterally enhanced channel, simulations were carried out in this paper using a *Re* in the range of 20,000 to  $40,000$  with a constant  $Ro$  of  $0.025$  since this range is the most commonly used in many U-channel, simulations were carried out in this paper using a *Re* in the range of 20,000 to other pieces of literature [\[49,](#page-21-9)[51\]](#page-21-10). channel, simulations were carried out in this paper using a *Re* in the range of 20,000 to what is more, there is a significant gap in the bilaterally enhanced 0-channel studies other pieces of literature [49,51].

In the simulations, a structured mesh is utilized with a high mesh density near the  $\frac{1}{2}$ walls to ensure a y+ of around 1, as depicted in Figure [18.](#page-14-1) The software of FLUENT and the approach of RANS are adopted. The SST k-w model is chosen because of its good performance in predicting rotating channels [82]. For the boundary conditions, the Multi-Reference Frame method was used for rotating states. Relative to adjacent cell zone was selected in the reference frames of the inlet and outlet in the rotating channel. The inlet and outlet were set as velocity inlet and pressure outlet with zero gauges, respectively. The intervalse were seen to be computed that presence same what here gauges, respectively. The the independent velocity and the rotations with a constant heat flux of 2000 W/m<sup>2</sup> were adopted for all the walls  $\overline{\phantom{a}}$ heated wall boundary conditions with a constant heat flux of 2000 W/m<sup>2</sup> were adopted for all the walls.

<span id="page-14-1"></span>

**Figure 18.** Grid of the smooth, bilaterally enhanced U-channel. **Figure 18.** Grid of the smooth, bilaterally enhanced U-channel.

The simulation result compared with the experimental result  $[96]$  is demonstrated in Figure 19. *F* The simulation result compared with the experimental result [96] is demonstrated in Figure [19.](#page-15-0) According to the validation result, the simulation results meet the experimental  $\frac{9}{5}$  result well. result well.

<span id="page-15-0"></span>

**Figure 19.** Validation result with existing experiment [96]. **Figure 19.** Validation result with existing experiment [\[96\]](#page-22-20).

For the simulation studies, the results are demonstrated in Figures 20–23. In Figures and [21,](#page-16-0) the average *Nu* represents that the wall Nusselt number is averaged along the axial<br>direction of distribution of distribution of the major color. flow in the rotating channel. Based on Figures [20](#page-15-1) and [21,](#page-16-0) at the same Ro, all the Nu values have the same variation trend, going up as the Re increases. Thus, the Re benefits from the heat transfer ability on the leading and the trailing walls of the bilaterally enhanced U-channel. On the trailing wall presented in Figure [20,](#page-15-1) Nu is gradually reduced along the flow direction due to the development of a boundary layer in the radial outward flow pass. At  $Re = 20,000$ ,  $Nu$  is in the range of 54 to 86. At  $Re = 30,000$ ,  $Nu$  is in the range of 73 to 115. At  $Re = 40,000$ ,  $Nu$  is in the range of 91 to 142. On the leading wall, illustrated in Figure [21,](#page-16-0) the maximum  $Nu$  occurs at the location of the bend outlet because of the flow impingement of the bend outlet on the leading wall of the radial inward flow pass. Along the flow direction of the radial inward flow pass,  $Nu$  is decreased since the flow impingement at the bend outlet is gradually weakened. When  $Re$  is 20,000,  $Nu$  ranges from 73 to 146. When  $Re$  is 30,000, Nu ranges from 106 to 215. When  $Re$  is 40,000, Nu ranges from 146. When *Re* is 30,000, *Nu* ranges from 106 to 215. When *Re* is 40,000, *Nu* ranges from 133 For the simulation studies, the results are demonstrated in Figures [20–](#page-15-1)[23.](#page-17-0) In Figures [20](#page-15-1) direction, as depicted in Figure [16.](#page-13-0) The flow direction is the direction of the main coolant 133 to 230. to 230.

<span id="page-15-1"></span>

(Trailing wall,  $Ro=0.025$ )

Figure 20. Average  $Nu$  variations under different  $Re$  along the flow direction on the trailing wall.

<span id="page-16-0"></span>

Figure 21. Average Nu variations under different Re along the flow direction on the leading wall.

<span id="page-16-1"></span>

Figure 22. Average  $Nu/Nu_0$  variations under different  $Re$  along the flow direction on the trailing wall at *Ro* = 0.025. at *Ro* = 0.025.

 $Nu/Mu_0$  is in the range of 1 to 1.5. Figures [22](#page-16-1) and [23](#page-17-0) depict the average *Nu/Nu*<sup>0</sup> variations with different *Re* values along the flow direction on the trailing wall at *Ro* = 0 and 0.025. According to Figures [22](#page-16-1) and [23,](#page-17-0) at the same *Ro* condition, *Re* has less of an effect on *Nu/Nu*0. Therefore, when *Ro* is the same, *Re* plays a negligible role in heat transfer improvement (*Nu/Nu*0). Therefore, *Ro* and *Re* have an independent influence on the heat transfer performance of the bilaterally enhanced U-channel. When *Re* is in the range of 20,000 to 40,000 with non-rotational conditions, *Nu/Nu*<sup>0</sup> is between 0.9 to 1.4. When *Re* is in the range of 20,000 to 40,000 with a *Ro* of 0.025,

Figure [24](#page-17-1) demonstrates the *Re* effect on the pressure loss of the bilaterally enhanced U-channel. At the same *Ro*, the pressures of the inlet and the outlet rise with increasing *Re*. The pressure difference between the inlet and the outlet grows from 365 to 1335 Pa as the *Re* ranges from 20,000 to 40,000. The friction factor ratio *f/f* <sup>0</sup> has slightly increased from 2.37 to 2.46 with a *Re* from 20,000 to 40,000, which is probably because more viscous dissipation happens when the *Re* is higher.

<span id="page-17-0"></span>

Figure 23. Average  $Nu/Nu_0$  variations under different  $Re$  along the flow direction on the trailing wall at  $Ro = 0$ .

<span id="page-17-1"></span>

**Figure 24.** Pressure loss variations of the bilaterally enhanced U-channel along different *Re.* **Figure 24.** Pressure loss variations of the bilaterally enhanced U-channel along different *Re*.

# **5. Conclusions 5. Conclusions**

In this paper, the influence of the Coriolis force, including the mechanisms, on con-In this paper, the influence of the Coriolis force, including the mechanisms, on conventional rotating channels is reviewed and analyzed. A way to utilize the positive heat ventional rotating channels is reviewed and analyzed. A way to utilize the positive heat transfer effect of the Coriolis force is proposed. Recent investigations on corresponding transfer effect of the Coriolis force is proposed. Recent investigations on corresponding novel rotating channels called bilaterally enhanced U-channels are illustrated. Moreover, novel rotating channels called bilaterally enhanced U-channels are illustrated. Moreover, numerical investigations about the *Re* effects on bilaterally enhanced smooth U-channels numerical investigations about the *Re* effects on bilaterally enhanced smooth U-channels were carried out in the study. The relevant conclusions can be drawn as follows: were carried out in the study. The relevant conclusions can be drawn as follows:

- 1. For a conventional rotating channel, the trailing wall of the radial outward flow path performance, while the opposite walls perform lower heat transfer. This is because the leading or trailing wall with the Coriolis force pointing at it has Coriolis-induced secondary flow flushing and thus obtains heat transfer augmentation, but the opposite wall has the secondary flow leaving and thus leads to a heat transfer deficit. and the leading wall of the radial inward flow path possess higher heat transfer
- 2. Coriolis-induced secondary flow can interact with the rib-induced secondary flow, leading to heat transfer enchantment or weakened secondary flow. This is because when the circulation directions of the two-type secondary flows are the same, the secondary flow can be enhanced and thus improve heat transfer ability. However, as

the circulation directions are opposite, the secondary flow is weakened by each other

- and can even disappear. 3. The channel orientation angle can weaken the strength of the Coriolis force applied on
- the trailing or leading wall. The reason for this is that there is a component Coriolis force applied on the wall when a channel orientation angle exists and the component Coriolis force is smaller, thus the strength of the Coriolis-induced secondary flow is smaller, leading to the Coriolis force effect being weakened.
- 4. A novel rotating U-channel with a channel orientation angle of 90° (called a bilaterally enhanced U-channel) can utilize the Coriolis force positive heat transfer effect on the leading and the trailing walls at the same time. This is because, according to the right-hand rule, when the main flow goes from the pass near the pressure side and then enters the pass near the suction side, the direction of the Coriolis force can simultaneously point to the leading and trailing walls, causing heat transfer enhancement on both the pressure and the suction sides.
- 5. Based on the non-dimensional equations for a bilaterally enhanced U-channel with incompressible and viscous flow, *Re* and *Ro* are vital non-dimensional numbers that influence the performance of a bilaterally enhanced U-channel. Combined with the research results, *Ro* is good for the heat transfer of bilaterally enhanced U-channels on both the leading and the trailing walls. At the same *Ro*, *Re* positively affects the *Nu* on the leading and the trailing walls of a Coriolis-utilization rotating smooth U-channel but plays a negligible role on *Nu/Nu*0.

In different stationary cooling channels, the Coriolis force exists in the internal rotating channel due to the rotation effect, resulting in heat transfer enhancement and deficit simultaneously on the trailing or leading walls in a conventional rotating U-channel. Therefore, the heat transfer ability of the conventional rotating channel is restricted owing to the Coriolis force. However, the bilaterally enhanced U-channel with a channel orientation angle of 90◦ is promising for solving the Coriolis force-induced heat transfer deficit and even augments heat transfer performance on both the trailing and the leading walls by utilizing the rotating effect. Moreover, it has the advantage of less pressure loss, meaning that the bilaterally enhanced U-channel is an encouraging and promising internal cooling structure for real-world turbine rotating blade design.

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#### **Nomenclature**





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