

Article

Numerical Study on Improved Geometry of Outlet Pressure Ripple in Parallel 2D Piston Pumps

Yu Huang ¹ , Qianqian Lu 1,[*](https://orcid.org/0000-0003-4640-9605) , Wei Shao ¹ , Li Liu ¹ , Chuan Ding [2](https://orcid.org/0000-0002-1034-2261) and Jian Ruan ²

- ¹ School of Engineering, Zhejiang University City College, Hangzhou 310000, China
² Kay Labarataw of Sposial Dumase Equipment and Advanced Manufacturing Tech
- ² Key Laboratory of Special Purpose Equipment and Advanced Manufacturing Technology, Ministry of
- Education & Zhejiang Province, Zhejiang University of Technology, Hangzhou 310014, China

***** Correspondence: luqianqian@zucc.edu.cn

Abstract: Because the axial piston pump is often used in the aerospace and aviation fields, it is necessary to pay attention to its outlet pressure and flow characteristics. The parallel 2D piston pump proposed, based on the axial piston pump, has no structural flow ripple because it has a rail with a uniform acceleration and deceleration. Now, the pump is used in the special working conditions of the aerospace field, and it is required to meet the rated flow of 50 L/min, the rated load of 8 MPa, and an extremely low-pressure ripple. Based on CFD technology, this paper studies the pump's outlet flow and pressure ripples through numerical simulation. According to the causes of the outlet pressure ripple, an improved geometry is determined to further reduce the outlet pressure ripple. Using a high-frequency pressure sensor to measure the outlet pressure ripple of the optimized pump prototype, it was found that the outlet pressure ripple rate of the prototype was only 6%. The parallel 2D piston pump has been proved by the simulation and test that its outlet pressure ripple is extremely low. However, it is not effective to reduce the outlet flow ripple by increasing the pre-pressure and reducing the backflow. In parallel 2D piston pumps, it is still necessary to find a new method to further reduce outlet pressure and flow ripples.

Keywords: parallel 2D piston pump; pressure ripple; backflow; CFD simulation

1. Introduction

Axial piston pumps that belong to hydraulic power units are widely used in the aviation and aerospace fields for advantages, such as a high power–weight ratio, strong load capacity and high efficiency [\[1–](#page-16-0)[3\]](#page-16-1). However, in aviation and aerospace fields, the outlet pressure ripple of axial piston pumps is of particular concern because it can cause the vibration of pipelines and damage to hydraulic components, as well as endanger the stability of hydraulic systems [\[4](#page-16-2)[–6\]](#page-16-3).

In axial piston pumps, the pressure ripple is derived from flow ripples which are composed of the structural flow ripple and the compressible flow ripple [\[7](#page-16-4)[,8\]](#page-16-5). The structural flow ripple is determined by its own mechanical structure [\[9\]](#page-16-6). Under ideal conditions, the output flow curve of a single piston is a sinusoid, and the superposition of multiple sinusoids cannot form a straight line without fluctuations, so the axial piston pump cannot eliminate the structural flow ripple. The compressible flow ripple is caused by the backflow that refers to the phenomenon in which the oil flows back from the outlet to the piston chamber [\[10\]](#page-16-7). When the piston chamber is ready to discharge oil, the pressure in the chamber is lower than that of the outlet. Then, the piston chamber connects with the outlet through the valve plate, and the oil enters the piston chamber from the outlet to help the oil pressurization in the chamber $[11,12]$ $[11,12]$. When the oil pressure in the chamber is higher than the outlet, the piston chamber begins to drain oil.

There are many studies on the flow ripple, such as the work by Ma where they optimized the design of the valve plate using a mathematical model and a computational fluid

Citation: Huang, Y.; Lu, Q.; Shao, W.; Liu, L.; Ding, C.; Ruan, J. Numerical Study on Improved Geometry of Outlet Pressure Ripple in Parallel 2D Piston Pumps. *Aerospace* **2022**, *9*, 629. [https://doi.org/10.3390/](https://doi.org/10.3390/aerospace9100629) [aerospace9100629](https://doi.org/10.3390/aerospace9100629)

Received: 9 August 2022 Accepted: 20 October 2022 Published: 21 October 2022

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dynamics (CFD) simulation to reduce the compressible flow ripple [13,14]. Bergada studied leakages in four types of the friction pairs of axial piston pumps through mathematical modeling and researched the effect of leakages on the flow ripple $[15]$. In order to find the optimal design of the valve plate faster, Song proposed that the optimization procedure for the pre-compression volume and the swash-plate cross angle with a relief groove had been greatly simplified by adopting the developed parameter-selection criteria from the simula-tion results [\[4\]](#page-16-2). Zhang analyzed the flow-dynamics characteristics of an axial piston pump based on the improved CFD simulation, and test results showed that the compressible flow ripple made up 88% of the flow ripple [\[16\]](#page-16-13). Zhu came up with a solution that involved a kind of double-swash-plate hydraulic axial-piston electric-motor pump with port valves, where a cylinder rotates along with the port valves, which is different from the conventional port-valving pump, in which the swash-plate rotates and the cylinder is mounted in the casing [\[17\]](#page-16-14). The valve distribution structure can effectively reduce the backflow, thereby reducing the compressible flow ripple. Zhong used an independent metering valve-control hydraulic system (IMVCHS) to deal with the flow and pressure ripples generated by the axial piston pump and improve the stability of the fluid [\[18\]](#page-16-15). Swarnava conducted an investigation of a novel positive-displacement axial-piston machine using a bent cylinder sleeve configuration, and groove geometry was chosen primarily to reduce flow ripple [\[19\]](#page-16-16).
———————————————————— He further reduced the outlet flow and pressure ripples by combining two axial piston pumps into one and studied the influence of structural parameters on the ripples through simulation [\[20\]](#page-16-17). $\frac{1}{20!}$

mized the design of the valve plate using a mathematical model and a computational fluid

However, the above studies are all for the compressible flow ripple, and there is still little research on how to reduce the structural flow ripple through mechanical designs. The
Ph 2D pump, using the guiding rail with a uniform acceleration and a uniform deceleration, was proposed by our team in order to eliminate the structural flow ripple [\[21](#page-16-18)[,22\]](#page-17-0). Figure [1a](#page-1-0) Figure 1a demonstrates the mechanical design of a parallel 2D piston pump, which condemonstrates the mechanical design of a parallel 2D piston pump, which consists of two high-speed 2D piston pumps mechanical design of a parallel 2D piston pump, which consists of two high-speed 2D piston pumps mechanically connected in series. The transmission sion mechanism of the high-speed 2D piston pump is a mechanism composed of the rollmechanism of the high-speed 2D piston pump is a mechanism composed of the rollers and
the guiding rail, as shown in Figure 1b. When the cone rollers of the driving roller and the the guiding rail, as shown in Figure [1b](#page-1-0). When the cone rollers of the driving roller and the and guiding rail, as shown in Figure 10. When the cone rollers of the driving roller and the
balancing roller are rolling on the guide rail, the driving roller and balancing roller rotates relatively folice are folling on the galacterial, the diffung folice and balancing folice folded in a reciprocating linear motion. The output flow curve of the high-speed 2D piston pump In a receptioning mean measure the output flow can be on the high-speed 22 passing pants. the a mangular carve, and the worlding principle and output for characteristics of the 2D pump have been described in detail in References [\[23,](#page-17-1)[24\]](#page-17-2) and will not be described here. parallel 2D piston pumps in the two 2D pumps in the parallel 2D piston pump have a phase difference of 45 deg, their output flow curves can compensate each other and become a straight line $[24]$. little research on the structure research on the compressible how ripple, and there is sufficiently

Figure 1. (a) The mechanical design of a parallel 2D piston pump and (b) working principle of the rollers and the guiding rail. rollers and the guiding rail.

A pump with a rated flow rate of 50 L/min , where L is the volume unit and 1 L is equal to 1 dm³, a rated load pressure of 8 MPa, and a small outlet pressure ripple is re-quired for the special working conditions of the aerospace field. A pump that meets the above requirements was designed according to the structural design of the parallel 2D piston pump shown in [F](#page-1-0)igure 1. Figure 2 [sh](#page-2-0)ows the outlet flows of the pump and the corresponding four working chambers, where 0 deg corresponds to the state of Figure 1. corresponding four working chambers, where 0 deg corresponds to the state of Figure [1.](#page-1-0) This pump needs to be further optimized because a smaller outlet pressure pulsation This pump needs to be further optimized because a smaller outlet pressure pulsation is is required. Shentu studied the outlet pressure ripple of a parallel $2D$ pump by CFD simulations and experimental studies $[24]$. However, she did not propose a method to optimize the pressure ripple, and her experiments used conventional pressure sensors instead of high-frequency pressure sensors, so the experimental results were not satisfactory. high-frequency pressure sensors, so the experimental results were not satisfactory.

Figure 2. The theoretical outlet flow of the parallel 2D piston pump. **Figure 2.** The theoretical outlet flow of the parallel 2D piston pump.

The parallel 2D piston pump, a hydraulic pump without a structural flow ripple, is great innovation, but unfortunately there is no research to measure its outlet flow and a great innovation, but unfortunately there is no research to measure its outlet flow and pressure ripples, and no solution to further reduce its ripples has been proposed [\[25\]](#page-17-3). This pressure ripples, and no solution to further reduce its ripples has been proposed [25]. This paper focuses on determining an improved geometric design to reduce the outlet pressure paper focuses on determining an improved geometric design to reduce the outlet pressure ripple of the parallel 2D piston pump by using a numerical simulation method. The CFD ripple of the parallel 2D piston pump by using a numerical simulation method. The CFD model of the parallel 2D piston pump was built, and its geometric model, grid model, model of the parallel 2D piston pump was built, and its geometric model, grid model, numerical strategy, and boundary conditions are introduced in detail. Pressure ripples numerical strategy, and boundary conditions are introduced in detail. Pressure ripples and output flow ripples of the four working chambers and parallel 2D piston pump are and output flow ripples of the four working chambers and parallel 2D piston pump are analyzed and the optimized design is determined according to the simulation. Finally, analyzed and the optimized design is determined according to the simulation. Finally, experimental results are presented as an example to verify the simulation and the improved geometric design.

2. Description of CFD Model 2. Description of CFD Model

In this chapter, the description of the CFD model is split into four parts: in order, the fluid zone's geometric model, the grid model, the numerical strategy, and the boundary conditions.

2.1. Geometric Model 2.1. Geometric Model

Figure 3 shows the fluid zone extracted from the mechanical structure of the parallel 2D piston pump in Figure [1.](#page-1-0) This fluid zone is divided into 4 parts: in order, an inlet zone, 2D piston pump in Figure 1. This fluid zone is divided into 4 parts: in order, an inlet zone, an outlet zone, a left pump unit, and a right pump unit. Oil enters the pump shell through an outlet zone, a left pump unit, and a right pump unit. Oil enters the pump shell through the back cover, and then enters the right pump unit through kidney-shaped channels. The the back cover, and then enters the right pump unit through kidney-shaped channels. The remaining oil enters the cylindrical chamber in the middle through the kidney-shaped channels and the circular channels, and then enters the left pump unit through the kidneyshaped channels. Oil discharged from the left and right pump units first gathers in two annular chambers on both sides, and then flows out through the outlet in the middle. α is the outlet in the outlet in the outlet in the middle. Figure [3](#page-3-0) shows the fluid zone extracted from the mechanical structure of the parallel

Figure 3. The fluid zone of the parallel 2D piston pump.

2.2. Grid Model T_{tot} model α parallel 2D piston pump is also divided into four parallel into α

2.2. Grid Model pump units, an inlet, and an outlet, according to the geometric model of the fluid zone. Figure 4a,b show the grid models of the left and right pump units and their geometric dimensions. A pump unit is divided into four parts, which are a left chamber (LC), a left distribution part (LDP), a right distribution part (RDP), and a right chamber (RC). The LC and RC of the left pump unit shown in Figure 4a are of a medium size, while the LC and RC of the right pump unit shown in Figure 4b [ar](#page-3-1)e of maximum and minimum size, respectively. The uniteristicity marked in the rightes are in minimum recording to the working principle of 2D piston pumps, the LC and RC need to expand and contract, while the LDP pendiple of 22 places pamps, are 20 and no need to expand that conduct, while the 221 and RDP need to displace and rotate. The grid model of the parallel 2D piston pump is also divided into four parts: two respectively. The dimensions marked in the figures are in mm. According to the working

Figure 4. Grid models of (**a**) the left pump unit and (**b**) the right pump unit. **Figure 4.** Grid models of (**a**) the left pump unit and (**b**) the right pump unit.

(**a**) (**b**) pump unit as an example to describe boundary settings, as shown in Figure 5. The LC and pump unit as an example to describe boundary settings, as shown in Figure [5.](#page-4-0) The LC and **Figure 4.** Grid models of (**a**) the left pump unit and (**b**) the right pump unit. set dynamic-mesh procedure. The LC and LDP also need to set the boundaries of contact between them as an interface before they can interact with each other. This paper uses the dynamic mesh to simulate the above motion and takes the left This paper uses the dynamic mesh to simulate the above motion and takes the left RC do not rotate, but expand and contract, so their two side walls, such as the LLCMW RC do not rotate, but expand and contract, so their two side walls, such as the LLCMW and LLCI, are selected as moving walls. Because the LDP and RDP are not deformed and and LLCI, are selected as moving walls. Because the LDP and RDP are not deformed and only rotated and displaced, they are selected as rigid body zones to move according to the only rotated and displaced, they are selected as rigid body zones to move according to the

Figure 5. Boundary settings of the left pump unit. **Figure 5.** Boundary settings of the left pump unit.

Figure 6 shows the dimensions and boundary settings of the inlet fluid zone. Because study, the inlet pressure needs to increase to ensuring there is sufficient sucking oil in both the simulation and the experiment. The inlet of the inlet fluid zone is chosen as a pressure interesting the unit and the outlets are set as interfaces. It should be noted here that, taking the outlets on the left as an example, they must establish the interfaces with the contact walls of the LDP and RDP, respectively. the influence of insufficient sucking oil on the outlet flow ripple is not considered in this
indicated in this sufficient sucking oil on the outlet flow ripple is not considered in this

Figure 6. Dimensions and boundary settings of the inlet fluid zone. **Figure 6.** Dimensions and boundary settings of the inlet fluid zone.

The dimensions and boundary settings of the outlet fluid zone are similar to those of set as a pressure outlet. Because the pressure outlet can change the outlet to the set pressure, the pressure ripple cannot be detected. In order to obtain the outlet pressure ripple, an additional section of the outlet pipe is required at the outlet, as shown in Figure 7b. The outlet pipe is connected to a throttle valve. The load pressure of the pump is adjusted by
share in a throttle area of the throttle valve. The deventure ment of the throttle valve is provided with a pressure outlet. The sizes of the outlet pipe are based on the actual to provided with a pressure of the number of the state pressure of the throtten working conditions of the pump and are completely consistent with the experiment by changing the throttle area of the throttle valve. The downstream part of the throttle the inlet fluid zone, as shown in Figure 7a. However, the boundary of the outlet cannot be changing the throttle area of the throttle valve. The downstream part of the throttle valve working conditions of the pump and are completely consistent with the experiment.

Figure 7. (**a**) The outlet fluid zone and (**b**) the outlet pipe. **Figure 7.** (**a**) The outlet fluid zone and (**b**) the outlet pipe. **Figure 7.** (**a**) The outlet fluid zone and (**b**) the outlet pipe. **Figure 7.** (**a**) The outlet fluid zone and (**b**) the outlet pipe.

Figur[e 8](#page-5-1) shows the grid model of the parallel 2D piston pump formed by combining the four parts. The averaged outlet pressures are compared by increasing the number of mesh elements with a similar quality of the mesh element, as shown in [F](#page-5-2)igure 9. From 2.6×10^5 mesh elements to 4.9×10^5 mesh elements, the averaged outlet pressure changes by 0.625%. From 4.9×10^5 mesh elements to 7.5×10^5 mesh elements, the averaged outlet pressure changes by 0.25%. As such, a grid with a number of 7.5 \times 10⁵ elements is chosen the computational model. as the computational model. the computational model. the computational model.

Figure 8. The grid model of the parallel 2D piston pump.

Figure 9. Relation between number of mesh elements and averaged outlet pressure.

2.3. Numerical Strategy

It is a normal choice to use the laws of mass conservation and momentum conservation for numerical strategies in the CFD simulation. These conservation laws can be described as the following equations

$$
\frac{\partial \rho}{\partial t} + \frac{\partial \rho u_x}{\partial x} + \frac{\partial \rho u_y}{\partial y} + \frac{\partial \rho u_z}{\partial z} = 0, \tag{1}
$$

$$
\frac{Du_x}{Dt} = -\frac{1}{\rho}\frac{\partial p}{\partial x} + v\left(\frac{\partial^2 u_x}{\partial x^2} + \frac{\partial^2 u_x}{\partial y^2} + \frac{\partial^2 u_x}{\partial z^2}\right) + R,\tag{2}
$$

$$
\frac{Du_y}{Dt} = -\frac{1}{\rho}\frac{\partial p}{\partial y} + v\left(\frac{\partial^2 u_y}{\partial x^2} + \frac{\partial^2 u_y}{\partial y^2} + \frac{\partial^2 u_y}{\partial z^2}\right) + T,\tag{3}
$$

$$
\frac{Du_z}{Dt} = -\frac{1}{\rho}\frac{\partial p}{\partial z} + v\left(\frac{\partial^2 u_z}{\partial x^2} + \frac{\partial^2 u_z}{\partial y^2} + \frac{\partial^2 u_z}{\partial z^2}\right) + Z,\tag{4}
$$

where *t* is the time, p , u_x , u_y , and u_z are fluid's pressure and velocities in the *xyz* directions, respectively, and *R*, *T*, and *Z* are body forces acting on the unit micelle in the *xyz* directions, respectively. *ρ* is oil density and *υ* is oil kinematic viscosity.

Due to the phenomena of backflow, pressure overshoot in the chamber, and because pressure ripples are closely related to the oil compressibility, the oil compressibility must be considered for the numerical simulation of 2D piston pumps. If the oil is incompressible, oil density is constant. This means that the transmission speed of the pressure wave is infinite, and it is unreasonable. The essence of compressible fluid is to correct the density by pressure and the elastic modulus *K*, and the relationship between them can be described as:

$$
\rho = \frac{\rho_0}{(1 - (p - p_0)/K)},
$$
\n(5)

where p_0 is an ambient pressure of 1.01 bars and ρ_0 is the corresponding density under the ambient pressure. The speed of sound *c* is calculated as

$$
c = \sqrt{\frac{K}{\rho}} = \sqrt{\frac{K - (p - p_0)}{\rho_0}},
$$
\n(6)

The renormalization group (RNG) *k*-*ε* model is used as the turbulence model for this simulation. The standard *k*-*ε* model proposed by Launder and Spalding is widely used in engineering CFD calculations because of its wide application range, ability to save computing resources, and suitable accuracy [\[26\]](#page-17-4). The RNG *k*-*ε* model is derived from the standard *k-ε* model using a statistical method called renormalization group theory [\[27\]](#page-17-5). The jet is extremely fast when the working chamber starts to discharge oil. The RNG model adds a term to its *ε* equation, improving the accuracy of high-velocity flows. This is the reason why the RNG *k-ε* model is chosen as the turbulence model.

Solution methods are required for solving the numerical calculation through the commercial software FLUENT. The coupled scheme is used for the numerical calculation. A second-order scheme is chosen for the modeling of the pressure. A second-order upwind scheme is chosen for the modeling of the density and momentum. A first-order upwind scheme is chosen for the modeling of the turbulence.

2.4. Boundary Conditions

Because the working conditions of the parallel 2D piston pump was determined, it needs to provide a flow of 50 L/min under a load of 8 MPa. The displacement of the parallel 2D piston pump is designed to be 10.24 mL/rev, so the rated rotational speed should be 5000 rpm.

One disadvantage of using a throttle valve to modulate pressure is that it cannot be accurately controlled. Therefore, the target is that the pressure of the outlet is close to 8 MPa in the simulation, and the cross-sectional area of the throttle valve is selected to be 5.3 mm^2 . The pressure inlet is consistent with the test, the pressure is 4 bars, and the pressure outlet is set to a normal pressure.

MPa in the simulation, and the cross-section, and the throttle value is selected to be the throttle value is selected to be the throttle value is selected to be the throttle value of the throttle value is selected to be t

For the convenience of understanding, the left chamber of the left pump unit is denoted by the symbol LLC, and the left distribution part of the left pump unit is denoted by the symbol LLDP, and so on. The most important thing is the setting of the dynamic mesh, [and](#page-7-0) its rotation direction and boundary movement must correspond. Taking Figure 10 as an example, there are four working chambers and four distribution parts, from left to right: LLC, LLDP, LRDP, LRC, RLC, RLDP, RRDP, and RRC. The velocity of the boundary 2 s is based on the movement of the 2D piston, which has been studied in [\[28,](#page-17-6)[29\]](#page-17-7). According 2 to the Cartesian coordinate system in Figure 8, the velocity v_1 of the LLCMW and LRCMW and the velocity v_2 of LLCI, LLDP, LRDP, and LRCI can be expressed as 2 g *Thillie To Helles*
RLDP, RRDP, and R
biston, which has b KLDP, KKDP, and KKC. The velopiston, which has been studied
Figure 8, the velocity v_1 of the I 16 3 3 () guie σ , the velocity σ_1 of the EL
P, and LRCI can be expressed $\frac{2}{\pi}$ ng chambers and four distribut
RLDP, RRDP, and RRC. The vel
piston, which has been studied *v*
system in Figure
LIFPLEPP ton, which has been studied if
gure 8, the velocity v_1 of the LI
P, and LRCI can be expressed RLDP, RRDP, and RRC. The v
piston, which has been studi the 2D pisto
stem in Figu Figure 8, the velocity v_1 of the LLCMW and LRCMV RDP, and LRCI can be expressed as

$$
v_1 = -v_2 = \begin{cases} \frac{16\omega^2 L_s}{\pi^2} (\frac{\pi}{4\omega} - t) & 0 < t \le \frac{\pi}{2\omega} \\ \frac{16\omega^2 L_s}{\pi^2} (t - \frac{3\pi}{4\omega}) & \frac{\pi}{2\omega} < t \le \frac{3\pi}{4\omega} \end{cases} \tag{7}
$$

where ω is the rotational angular velocity of the 2D piston and L_s is the stroke of the 2D
piston, designed to be 2.5 mm. The velocity v_3 of RLCMW and RRCMW and the velocity piston, designed to be 2.5 mm. The velocity v_3 of RLCMW and RRCMW and the velocity v_4 of RLCI, RLDP, RRDP, and RRCI can be expressed as beity v_3 of RLCMW and RI
he expressed as $\frac{1}{2}$ is the expressed as *L*
 RRCI can be expressed as T RRCI can be expressed as $(16, 27)$

$$
v_3 = -v_4 = \begin{cases} \frac{16\omega^2 L_s}{\pi^2} t & 0 < t \le \frac{\pi}{4\omega} \\ \frac{16\omega^2 L_s}{\pi^2} (\frac{\pi}{2\omega} - t) & \frac{\pi}{4\omega} < t \le \frac{3\pi}{4\omega}, \\ \frac{16\omega^2 L_s}{\pi^2} (t - \frac{\pi}{\omega}) & \frac{3\pi}{4\omega} < t \le \frac{\pi}{\omega} \end{cases}
$$
(8)

LLDP, LRDP, RLDP, and RRDP also rotate at the angular velocity of ω that is expressed by Equation (9),

$$
\omega = -\frac{n}{60} \cdot 2\pi,\tag{9}
$$

where *n* is the rotational speed in rpm and the direction of rotation conforms to the righthand rule. hand rule.

Figure 10. Boundary settings of the two pump units. **Figure 10.** Boundary settings of the two pump units.

Aviation hydraulic oil at $40 °C$ is used as the medium. Under the ambient pressure of 1.01 bars, given liquid has a kinematic viscosity of 13.84 \times 10⁻⁶ m²/s, an elastic modulus of 1000 MPa, and a density of 850 kg/m³.

Finally, the body force *Z* is also considered to be -9.8 m/s^2 .

3. Numerical Calculation Results

Firstly, the outlet pressure ripple and flow ripple of the originally designed parallel 2D piston pump are obtained by numerical calculation. The reasons for the outlet pressure and flow ripple are analyzed by researching the output flow and chamber pressure of the four working chambers. Then, the design of the parallel 2D piston pump is optimized according working challbers. Then, the design of the parallel 2D piston pump is optimized according
to these causes, and the outlet pressure and flow ripple of the optimized 2D pump are studied and compared with those before the improved geometry. T parallel 2D piston pump has four working chambers that working chambers that work in exactly the chambers that work in exactly the chambers that work in exactly the chambers that working the chambers of the chambers o

3.1. Before Improved Geometry $\begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}$

3.1. Before Improved Geometry

The parallel 2D piston pump has four working chambers that work in exactly the same
The parallel 2D piston pump has four working chambers that work in exactly the same ince parameters photon paint. The real world, a diameters and world behavior in the same way but with different phases. Therefore, the LLC is used as an example to analyze the chamber pressure and outlet flow of the working chamber. Figure 11 shows the chamber pressure in the LLC. The pressure decline marked at position 1 in Figure 10 is different from the chamber pressure of axial piston pumps. In reference [\[24\]](#page-17-2), it is believed that from the channel pressure of axial piston pumps. In reference [24], it is beneved that
this is oil shock caused by backflow, but this paper has a different explanation. Position 1 is the point at which the moving parts switch from a uniform acceleration to a uniform deceleration. When the 2D piston starts to push the oil with a uniform deceleration, the oil continues to accelerate due to inertia, resulting in the oil-pressure decline. However, this interpretation is not supported by previous simulation research of the 2D piston pump, so a single pump unit is simulated to verify this interpretation. The explanation for why the pressure increases at position 2 is that the suction and discharge oil windows are designed too small. At this time, the LLC is in a closed state and the volume of the LLC is still decreasing, causing the chamber pressure to rise. There is no immediate rise in the chamber
This is also be the U.C has in the sentent as marked strassition 2 in Figure 10. This is also pressure when the LLC begins to contract, as marked at position 3 in Figure [10.](#page-7-0) This is also presedire when the 220 degais to centrally as marked at pesition of its not consider the successive the suction and discharge oil windows are designed too small. When the 2D piston rotates close to 180 deg and the LLC is not connected to the suction oil window, the LLC is still expanding. By the time the LLC compresses, more volume needs to be compressed for the rise in chamber pressure.

Figure 11. The chamber pressure in the LLC. **Figure 11.** The chamber pressure in the LLC.

in Figure 12, and the numerical calculation results are basically consistent with the design. The reason for the small size of the inlet and outlet windows mentioned above is to let the $\overline{11}G$ ELE FIT FRESSURE SCISTE UNITED SITES OF THE INTERNATION. THE VECT, THE ELE SIMPLES OF THE INTERNATION OF THE INTERNATION OF THE INTERNATION OF THE INTERNATION OF THE INTERNATIONAL THE OF THE OF THE INTERNATIONAL STATE OF T design. A pump unit will be simulated later to explore the differences between the parallel 2D piston pump and the single pump unit. The outlet and inlet flow curves of the LLC were designed to be triangular, as shown LLC pre-pressurize before draining oil to reduce backflow. However, the LLC still has a

Figure 12. The outlet and inlet flow in the LLC.

The grid model of the pump unit is shown in Figure 13. Both the inlets and outlets set as the pressure inlet and outlet, and the set pressures are 0.4 MPa and 8 Mpa, respectively. spectively. are set as the pressure inlet and outlet, and the set pressures are 0.4 MPa and 8 Mpa, re-The grid model of the pump unit is shown in Figure [13.](#page-9-1) Both the inlets and outlets are

Pressure inlet Pressure outlet

Figure 13. The grid mesh of the pump unit. **Figure 13.** The grid mesh of the pump unit.

Figure 13. The grid mesh of the pump unit. Figure 14 shows the pressure in the left chamber and the outlet flow of the pump The pressure in the left chamber of the pump unit, and that of the LLC, are completely decline of nearly 45° , which is far less than the pressure decline in the previous parallel 2D piston pump simulation. This shows that the inertia caused by the change of acceleration is not the main reason for the pressure decline. Secondly, at the beginning of the oil discharge, higher than that of the LLC. It can be seen from Figure [14b](#page-10-0) that the backflow of the pump under this design should be very small when the load is 8 MPa. This means that the outlet pressure of the single pump unit is higher than 8 MPa in the parallel 2D piston pump. inconsistent. Firstly, the pressure fluctuation disappears, and there is only a pressure Figure [14](#page-10-0) shows the pressure in the left chamber and the outlet flow of the pump unit. the pressure has a high peak; however, at the end of the oil discharge, the pressure peak is

Figure 14. (a) The pressure in the left chamber and (b) the outlet flow of the pump unit.

In order to study the outlet load of the pump unit in the parallel 2D piston pump, the pressure distributions of the outlet flow zone are plotted as shown in Figure 1[5. In](#page-10-1) the parallel 2D piston pump, the symmetrical distribution of the left and right pump units can cause the oil to move left and right, so that the outlet load fluctuation of the pump unit can have an effect on the pressure fluctuation and pressure decline in the chamber. The influence of the symmetrical distribution of the left and right pump units on chamber pressure will continue to be a concern. pressure will continue to be a concern. pressure will continue to be a concern.

Figure 15. Pressure distributions in the outlet fluid zone when the pump rotates to (a) 7.2 deg, 10.8 deg, (**c**) 14.4 deg, and (**d**) 18 deg. 10.8 deg, (**c**) 14.4 deg, and (**d**) 18 deg. (**b**) 10.8 deg, (**c**) 14.4 deg, and (**d**) 18 deg.

The pressure distributions of the four working chambers and the pump outlet are shown in Figure [16.](#page-11-0) It is evident from the figure that there is no correlation between the shown in Figure 16. It is evident from the figure that there is no correlation between the chamber pressure and the pump outlet pressure. Their pressure declines seem to corre-chamber pressure and the pump outlet pressure. Their pressure declines seem to correspond, but this is not actually inferred from their maintained rotational angles. However, spond, but this is not actually inferred from their maintained rotational angles. However, the pressure declines in the chambers may be transmitted to the outlet and exacerbate the the pressure declines in the chambers may be transmitted to the outlet and exacerbate the outlet pressure ripple due to the compressibility. outlet pressure ripple due to the compressibility. The pressure distributions of the four working channels and the pump official mown in rigue to. It is evident from the figure that there is no correlation between the spanned pressure and the pump office pressure. Their pressure decimes seem to correthe pressure declines in the chambers may be transmitted to the outlook angles. The overver, outlet pressure ripple due to the compressibility.

Figure 16. The outlet pressure of the parallel 2D piston pump. **Figure 16.** The outlet pressure of the parallel 2D piston pump.

Figure 17 shows the outlet flows of the four working chambers and the parallel 2D Figure [17](#page-11-1) shows the outlet flows of the four working chambers and the parallel 2D piston pump. Comparing Figures [16](#page-11-0) and [17,](#page-11-1) it is found that the curves of the outlet pressure and flow of the pump are basically the same. This means that the pump outlet pressure ripple comes from the change of the outlet flow. The outlet flow ripple of the pump comes from the backflow that occurs in the four working chambers. In order to reduce the outlet flow ripple, the backflow existing in the working chamber must be reduced. Figure 17 shows the outlet flows of the four working chambers and the parallel 2D pigure 1/ shows the outlet flows of the four working champers and the parallel 2D

Figure 17. The outlet flow of the parallel 2D piston pump. **Figure 17.** The outlet flow of the parallel 2D piston pump. **Figure 17.** The outlet flow of the parallel 2D piston pump.

The areas for improvement are summarized as follows: The areas for improvement are summarized as follows: The areas for improvement are summarized as follows:

1. The pre-pressure of the working chamber needs to be higher. 1. The pre-pressure of the working chamber needs to be higher. 1. The pre-pressure of the working chamber needs to be higher.

2. When the working chamber starts to compress, the chamber pressure should immediately. immediately. rise immediately.

3. When the working chamber finishes compression, the pressure peak in the chamber should decrease.

3.2. After Improved Geometry

Figure [18](#page-12-0) shows an optimized design for the parallel 2D piston pump. Two structures Figure 18 shows an optimized design for the parallel 2D piston pump. Two structures have been optimized: one is to increase the area of the oil inlet windows, and the other is to rotate the oil outlet windows by 2 deg towards the rotation direction of the pump.

Figure 18. The comparison of two mechanical structures before and after improved geometry.

The chamber pressure and flow of the optimized LLC are described in Figure [19.](#page-12-1) The optimized chamber pressure eliminates the pressure rise at the end of the discharging oil and reduces the flow backflow at the beginning of the discharging oil. However, when the LLC begins to discharge oil, the pressure rise is still delayed, and a pressure peak appears. The above two problems are caused by the circular window, which can cause the gradient of the increase in the connection area to be too small when it is just connected. Changing the circular window to a rectangular one can solve these problems.

Figure 19. Comparisons of (**a**) chamber pressures and (**b**) outlet and inlet flows. **Figure 19.** Comparisons of (**a**) chamber pressures and (**b**) outlet and inlet flows.

Finally, two comparisons of the outlet flows and the pressures of the pump before and after the improved geometry are shown in Figure 20. [The](#page-13-0) optimized pump has an increased output flow due to reduced backflow. The output flow and pressure ripples can be represented as the ratio of the difference between the maximum and minimum values compared
to the average value. The output flow ringle of the optimized nume abanced from 8.1% to to the average value. The output flow ripple of the optimized pump changed from 8.1% to 7%, compared with that before the improved geometry, and the pressure ripple changed from 12.5% to 11%. In the numerical calculation, the output flow and pressure ripples in ripple changed from 12.5% to 11%. In the numerical calculation, the output flow and presthe optimized parallel 2D piston pump are reduced by reducing the backflow. However, reducing the flow ripple by pre-pressurizing interferes the superposition of the output flows of the two pump units, which is the source of the outlet flow and pressure ripples.

Figure 20. Comparisons of (a) the outlet flows and (b) the outlet pressures.

4. Experiments 4. Experiments

The test system takes into account the actual application environment and sets the $\frac{1}{2}$ oil pump and an inlet pressure sensor to ensure the sufficient sucking oil of the test pump. A rotational speed sensor is installed between the motor and the test pump to monitor the rotational speed of the test pump in real time. The outlet pressure sensor is placed at the outlet of the test pump, consistent with the simulation. A throttle valve is set downstream of the hard pipe to change the load pressure of the test pump. A flowmeter is installed downstream of the throttle valve to measure the outlet flow. The oil tank is equipped with a thermometer to detect the oil temperature, in order to prevent the test results from being disturbed by the oil temperature rise. outlet as a 5 cm hard pipe, as shown in Figure 21. The test system is equipped with a supply

Figure 21. *Cont*.

Figure 21. (**a**) The test system and (**b**) the test rig. **Figure 21.** (**a**) The test system and (**b**) the test rig.

The reason why this test cannot verify the flow ripple is that the flowmeter cannot measure the high-frequency flow [\[30](#page-17-8)[,31\]](#page-17-9), so only the outlet pressure ripple is detected for
the test nume. The least to the detection of the pressure ripple is to select a bigh-frequency. the test pump. The key to the detection of the pressure ripple is to select a high-frequency pressure sensor. In this experiment, the pressure sensor of the HM90(10 MPa)-H3-3-V2-F2 is selected, and its parameters are shown in Table [1.](#page-14-1) the test pump. The key to the detection of the pressure ripple is to select a high-frequency

F2 is selected, and its parameters are shown in Table 1. **Table 1.** Parameters of HM90(10 MPa)-H3-3-V2-F2.

| Description | Valve | Description | Valve |
|--|--------------------|--------------------------------|-----------------------|
| Pressure range | 10 MPa | Bandwidth $(-3dB)$ | 200 KHz |
| Combined non-linearity, hysteresis, and repeatability | $\pm 0.1\%$ FS | Operating temperature range | -50 °C to +120 °C |
| Thermal sensitivity shift | $\pm 0.1\%/100 °C$ | Thermal zero shift | $\pm 0.1\%$ FS/100 °C |

At a rotational speed of 5000 rpm and a load of 8 MPa, the outlet pressure ripple data of the test pump are measured through multiple tests. The original data measured by aata or the test pump are measured through multiple tests. The original data measured by
the experiment contains many interference signals, so the original data are processed by and the original data is shown in Figure [22a](#page-15-0). Then, the processed experimental data and the simulation are compared, as shown in Figure [22b](#page-15-0), and the following conclusions are drawn. Firstly, the experimental result and the numerical simulation are relatively consistent, especially in the prediction of the pressure ripple period. Secondly, after studying the amplitude–frequency characteristics of the test data and simulation result, it is found that the main frequency of the simulation result is 667 Hz, and the main frequency of the experimental data is 600 Hz. The main frequencies of the two are relatively close, but
experimental data is 600 Hz. The main frequencies of the two are relatively close, but since unipercially quite uniterest, as shown in Figure 20. Finany, are prototype of the parallel two-dimensional piston pump is tested and proves to have a low-pressure ripple
of only 6% low-pass filtering and three-point averaging. The comparison between the processed data their amplitudes are quite different, as shown in Figure [23.](#page-15-1) Finally, the prototype of the of only 6%.

However, there are also differences between the experimental data and the simulation result, especially in the magnitude of the pressure drop. Two explanations are proposed for this. The first is that the installation position of the pressure sensor in the tests is different from the measuring position of the simulation. The former is installed on the side of the pipeline, and the latter is the outlet of the pump. Secondly, the distribution windows of the prototype in the experiment are designed to be rectangular, while the distribution windows in the simulation are still circular, which also leads to a difference.

Figure 22. The comparisons (a) between the original test data with the processed test data and (b) the measured outlet pressure ripple with that obtained by numerical calculation.

Figure 23. Frequency spectrograms of the test data and simulation result.

5. Discussion and Conclusions

In this paper, the outlet pressure ripple of a parallel 2D piston pump is studied by numerical modeling and simulation. In the simulation, by analyzing the pressure and outlet flow of the working chambers, it is explained that the outlet pressure ripple of the pump comes from the flow ripple, which is derived from the backflow that occurs when the oil is discharged from the working chamber. To reduce backflow, the mechanical structures of the 2D pump have been optimized. In the end, the accuracy of the numerical simulation was testing the outlet pressure ripple of the optimized prototype. The conclusions are as follows: verified and the outlet pressure ripple rate of the parallel 2D piston pump was measured by

1. Under the operating conditions with a rotational speed of 5000 rpm and a load pressure of 8 MPa, the measured pressure ripple rate of the optimized parallel 2D piston pump prototype is only 6%. μ ump prototype is only 6%.

2. The outlet pressure ripple is indeed derived from the outlet flow ripple. The outlet flow ripple can be reduced by reducing the outlet flow ripple, so the mechanical structure of the parallel 2D piston pump, which is designed to eliminate the structural flow ripple, has a great advantage in a low outlet flow ripple. 2. The outlet pressure ripple is indeed derived from the outlet flow ripple. The outlet simulation was verified and the outlet pressure ripple.

3. By adding pre-pressure, the backflow of the working chamber can be reduced. However, in the parallel 2D piston pump, the effect on the outlet flow ripple is not significant by ing the backflow of the working chamber. 3. By adding pre-pressure, the backflow of the working chamber can be reduced. However, in the paramer 2D piston pump, the enect of reducing the backflow of the working chamber.

In future research, we will continue to maintain the advantage of the $2D$ piston μ ump and propose a 2D pisto In future research, we will continue to maintain the advantage of the 2D piston pressure of 8 MPa, the measure ripple rate of the measured pressure ripple rate of the optimization o pump and propose a 2D piston pump with an extremely low-pressure ripple under a load

pressure of 28 MPa by modifying the rail curve. In addition, through simulation, it was found that the pressure in the chamber is much higher than the load pressure when the oil is discharged from the working chamber, which greatly effects the mechanical efficiency of the pump and will be continue to be researched. Finally, measur outlet flow ripple of the parallel 2D piston pump are also in progress, and the geometry of the numerical model of the parallel 2D pump will also more closely match the geometry of the experiment.

Author Contributions: Writing—original draft preparation, Y.H. and W.S.; writing—review and editing, Q.L.; visualization, L.L.; supervision, J.R.; funding acquisition, C.D. All authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by the National Natural Science Foundation of China, grant number 51805480, by the Zhejiang Provincial Natural Science Foundation, grant number LY21E050013.

Conflicts of Interest: The authors declare no conflict of interest.

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