

Article

Rapid Evaluation of the Decay Time of a Plasma Brake-Based CubeSat

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Abstract: The plasma brake is a propellantless device conceived for de-orbiting purposes. It consists of an electrically charged thin tether that generates a Coulomb drag by interacting with the ionosphere. In essence, a plasma brake may be used to decelerate an out-of-service satellite and to ensure its atmospheric re-entry within the time limits established by the Inter-Agency Space Debris Coordination Committee. Moreover, since it only needs a small amount of electric power to work properly, the plasma brake is one of the most cost-effective systems for space debris mitigation. This paper exploits a recent plasma brake acceleration model to construct an iterative algorithm for the rapid evaluation of the decay time of a plasma-braked CubeSat, which initially traced a circular low Earth orbit. The altitude loss at the end of each iterative step was calculated using the linearized Hill–Clohessy–Wiltshire equations. It showed that the proposed algorithm, which was validated by comparing the approximate solution with the results from numerically integrating the nonlinear equations of motion, reduced computational time by up to four orders of magnitude with negligible errors in CubeSat position.

Keywords: plasma brake; relative trajectory; space debris mitigation



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1. Introduction

In recent decades, space activities have given rise to an alarming over-crowding of many geocentric orbits used for scientific, communication, and meteorological purposes [1,2]. Due to atmospheric drag, satellites experience a rapid orbital decay when they orbit below about 400 km [3]. However, the orbital radius loss associated with atmospheric friction becomes gradually smaller as the altitude increases and becomes negligible for medium-high Earth orbits [4]. The importance of keeping the geocentric regions in an acceptable condition for safe mission operation [5] has driven the scientific community to study deorbiting strategies [6–8] to meet the operational constraint according to which the residual orbital life of an out-of-service satellite should be fewer than 25 years [9–11].

Among the proposed methods to reduce the decay time of low Earth orbits (LEO) satellites, the electrostatic plasma brake [12–15] represents one of the most promising and fascinating options, as it does not require any propellant consumption, but only a tether-unreeling mechanism and a small amount of electrical power to charge that (conducting) tether. In fact, the plasma brake (PB) generates a Coulomb drag by means of a negatively charged thin tether, which electrostatically interacts with the ionized particles in the upper layers of the Earth's atmosphere [16]. The PB tether is usually so thin that a fragment taken from it should rapidly descend into the lower layers of the atmosphere without posing a threat to other spacecraft in those regions. From a conceptual point of view, the PB uses the same physical principle as the Electric Solar Wind Sail (E-sail) [17] although it is significantly smaller and less heavy because, instead of requiring an electron emitter, it uses natural charging from highly mobile electrons to maintain a negative voltage. The potential of E-sails has already been investigated in the context of a number of heliocentric mission scenarios, such as a planetary rendezvous [18–20], the more challenging in situ study of the

outer region of the solar system [21–23], or the futuristic exploration of nearby interstellar space [24,25]. On the other hand, the PB could represent a very promising option for passively deorbiting a spacecraft from a LEO. In fact, passive deorbiting systems may operate without any propellant stored onboard and after deployment are much easier to control than the other (more involved) active deorbiting strategies [26,27]. Among the passive methods, another interesting option comes from drag sails or similar drag augmentation devices that increase the area-to-mass ratio of the satellite [28,29]. Another possibility is the unreeling of an electrodynamic tether to exploit current flux and generate a magnetic field that interacts with the Earth's magnetosphere [30,31]. In this context, according to preliminary estimates [32], a PB could enable shorter deorbiting times than typical drag augmentation devices while requiring a power supply significantly smaller than that of an electrodynamic tether.

In recent years, significant efforts have been devoted to the technical development of both E-sail and PB propulsion concepts, including tether construction, overall mechanical design options, guidance and navigation strategies, and orbital simulations [33,34]. For example, Seppänen et al. [35] demonstrated the feasibility of producing a long conducting tether, while further research has been directed towards practical methods for the automatic manufacture [36,37] of such tethers. In addition, some space missions have been approved to demonstrate the feasibility of this advanced concept in a geocentric mission scenario. In particular, the Estonian 1U CubeSat ESTCube-1 [38–41], designed by the University of Tartu with the support of ESA and launched on 7 May 2013 aboard a Vega rocket, was the first ever satellite to attempt on-orbit deployment of an E-sail-charged tether. In fact ESTCube-1, with a mass of about 1 kg, was designed to deploy by centrifugal force a 10 m Heytether [37], positively charged to 500 volts with its bias maintained by two electron emitters [42].

Other mission requirements included using a PB to control spacecraft spin rate and de-orbiting. Unfortunately, the tether deployment failed, possibly due to a stuck reel, and the mission ended on 17 February 2015. Subsequent ground tests showed that the piezoelectric motor was damaged by launch phase vibrations [43], which meant that the failure was not due to an intrinsic flaw in the charged tether-related technology, and that the problem could have been solved with suitable spacecraft design improvements [39].

The ESTCube project is planning to launch ESTCube-2, an advanced 3U CubeSat to provide in-orbit measurements of the PB-induced Coulomb drag [32,44]. The launch is scheduled for 2023 when it is hoped that ESTCube-2 will deploy a -1 kV negatively charged 300 m tether to brake CubeSat. The latter is expected to reduce its altitude from 700 to 500 km in half a year [32]. According to conservative estimates, the conducting tether mass will be about 30 g and the mass of the whole PB system should be less than 500 g; thus, the proposed PB can be thought of as an effective, low-mass de-orbiting system.

The lesson learned from the failure of ESTCube-1 has also led to the design of Aalto-1 [45], a Finnish 3U CubeSat designed by Aalto University and launched on 23 June 2017. The Aalto-1 spacecraft has a mass of 3.9 kg and incorporates a PB device designed to perform attitude maneuvers and eventually de-orbit the CubeSat at the end of its operational lifespan [46]. The PB device consisted of a 100 m conducting tether, a reel mechanism for tether storage, a high voltage source, and electron emitters to maintain the charge [47]. After one year of technical issues (mainly concerning the communication subsystem) Aalto-1 started its planned remote sensing operations. Unfortunately, after some encouraging preliminary tests, the PB tether did not deploy, probably due to a failure in the boost converter that was supposed to maintain the nominal working voltage of the unreeling mechanism motor [48].

Recent interest in PB and Coulomb drag-based devices was also demonstrated by the private satellite AuroraSat-1, which was launched to a LEO on 2 May 2022; see Figure 1. AuroraSat-1 is a 1.5U CubeSat equipped with two payloads: a water resistojet module [49] for attitude changes and orbital adjustments and a PB module for spacecraft de-orbiting at the end of the scientific mission.

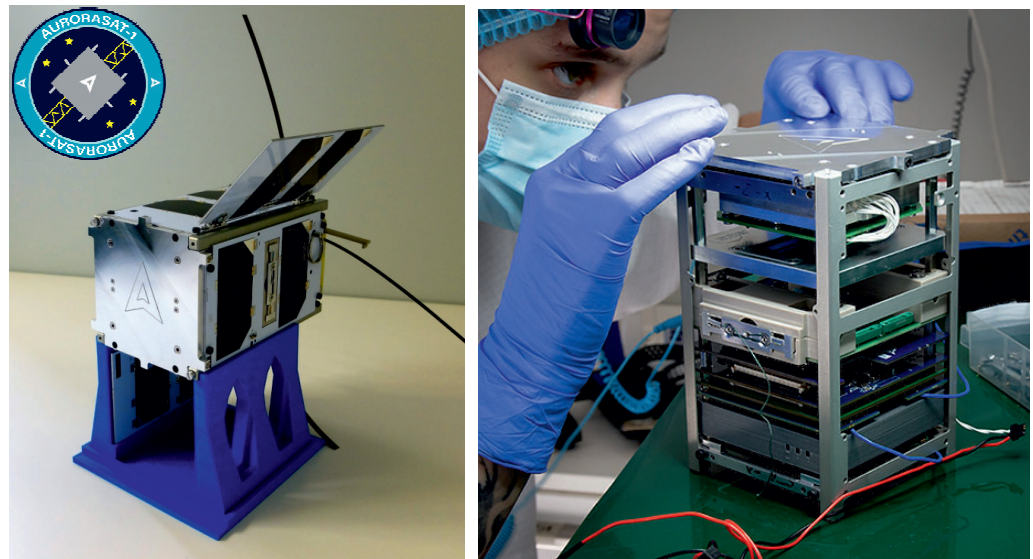


Figure 1. AuroraSat-1 includes a PB device for de-orbiting purposes at the end of its life. Image from Aurora Propulsion Technologies.

An even more recent mission that could serve as a technological demonstrator of PB technology is FORESAIL-1, the first satellite designed by the Finnish centre Of excellence in REsearch of SustAINabLe space (FORESAIL) [50]. The 3U CubeSat FORESAIL-1 was launched into a polar orbit at an altitude of 700 km on 25 May 2022. The CubeSat, which is equipped with a particle detector to provide in situ measurements required for understanding radiation belt physics, has an electrostatic PB device developed by the Finnish Meteorological Institute. It consists of a 40 m conducting tether, which will be employed for de-orbiting purposes at the end of the satellite operative life [32].

The aforementioned projects highlight the growing interest of the space community in PB technology. The trajectory analysis of a deorbiting satellite under Coulomb drag is therefore a subject of relevant interest. To deal with this problem, one possibility is numeric integration of Gaussian perturbation equations with a suitable model of the PB-induced Coulomb drag [14]. A viable alternative is represented by the determination of closed-form approximate models capable of estimating the decay time of a PB-equipped spacecraft (See Ref. [51]). In this context, this paper proposes a simplified mathematical model capable of estimating the decay time of a PB-based CubeSat simply and efficiently. Under the assumption that the CubeSat initially traced a circular (Keplerian) LEO, the proposed approach analyzes CubeSat motion relative to a virtual point that moves along the initial orbit at a constant speed. In other words, the virtual point represents the position of the small satellite on the circular LEO before the deployment of the PB-conducting tether. The linearized Hill–Clohessy–Wiltshire (HCW) equations [52] are used to describe the relative spacecraft motion, in which the magnitude of the PB-induced drag is a constant, while its direction is assumed to be purely circumferential; see Figure 2. The latter assumption is reasonable as long as the eccentricity of the PB-based CubeSat osculating orbit is sufficiently small, a condition that is satisfied by the very low magnitude of the Coulomb drag when compared to the Earth’s gravitational attraction. To simplify the numerical simulations to obtain conservative results, other perturbation sources such as atmospheric drag were neglected.

We showed that an analytical approximation of the spacecraft relative motion is possible, which allows the orbital decay achieved in N revolutions to be estimated with closed-form expressions. By adopting the analytical PB thrust model proposed by Orsini et al. [53], the number of revolutions within which the HCW-based approximations were valid was a function of the spacecraft’s orbital radius and the characteristics of the PB device. An iterative process was proposed to estimate the PB-based CubeSat decay time with a computational cost significantly smaller than that required by numerically integrating nonlinear

equations of motion. In particular, each cycle was characterized by constant values of PB-induced acceleration and orbital angular velocity so that the decay time was inversely proportional to the drag acceleration magnitude at the spacecraft's initial altitude. The resulting decay time was a conservative estimate, since atmospheric drag was not included in our mathematical model.

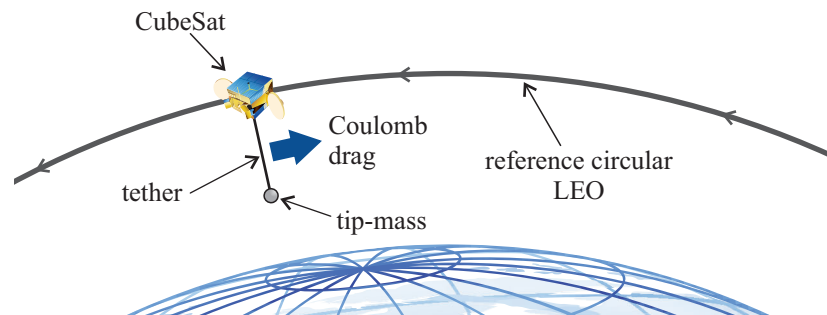


Figure 2. Plasma brake concept.

The paper is organized as follows. Section 2 deals with the approximate plasma brake trajectory and evaluates the maximum number of revolutions within which that solution is valid as a function of the spacecraft altitude, the Coulomb drag acceleration magnitude at the initial altitude, and the maximum allowable position error. Section 2 also shows a comparison of the approximate PB trajectory with reference results obtained by numerically integrating nonlinear equations of motion. Section 3 describes in detail the proposed iterative process and evaluates the decay time of three different CubeSat configurations that initially traced a circular LEO at an altitude of 1000 km above sea level. The last section contains our concluding remarks.

2. Mathematical Model

Consider a PB-based CubeSat that initially traced a circular LEO of radius r and introduced an orbital reference frame $\mathcal{T}(O; x, y)$ at origin O ; see Figure 3. The point O coincided with the CubeSat center of mass when the PB device was not deployed. Orbital perturbations were ignored, The y -axis was oriented radially from the Earth's center of mass to O , while the x -axis was tangent to the reference LEO in the opposite direction of the orbital motion.

The two-dimensional relative motion of the braked CubeSat after PB deployment with respect to O can be described through linearized HCW equations [52], which well approximate the actual spacecraft dynamics as long as the distance between O and the CubeSat is small compared to the orbital radius r . In the same way as in Ref. [53], the PB-induced drag acceleration is assumed to be purely circumferential, i.e., perpendicular to the local radial direction. Even though the Coulomb drag on the spacecraft depends on altitude [12], the drag acceleration magnitude a_T may be considered as roughly constant during a revolution around the Earth. This assumption is reasonable because the CubeSat orbital radius r has small variation with time due to the fact that the magnitude of the PB-induced drag is much smaller than the weight of the spacecraft. Accordingly, using the model discussed by Chobotov [54], the linearized two-dimensional HCW equations are

$$\ddot{x} - 2\omega\dot{y} = a_T \quad (1)$$

$$\ddot{y} + 2\omega\dot{x} - 3\omega^2 y = 0 \quad (2)$$

where $\omega \triangleq \sqrt{\mu_{\oplus}/r^3}$ is the constant angular velocity along the reference circular LEO, and μ_{\oplus} is the Earth's gravitational parameter. The linear HCW Equations (1) and (2) are

analytically integrated with zero initial conditions, that is, with $x(0) = y(0) = 0$ and $\dot{x}(0) = \dot{y}(0) = 0$. The solutions to Equations (1) and (2) are [54]

$$x(t) = -\frac{3 a_T t^2}{2} + \frac{4 a_T}{\omega^2} [1 - \cos(\omega t)] \tag{3}$$

$$y(t) = -\frac{2 a_T t}{\omega} \left[1 - \frac{\sin(\omega t)}{\omega t} \right] \tag{4}$$

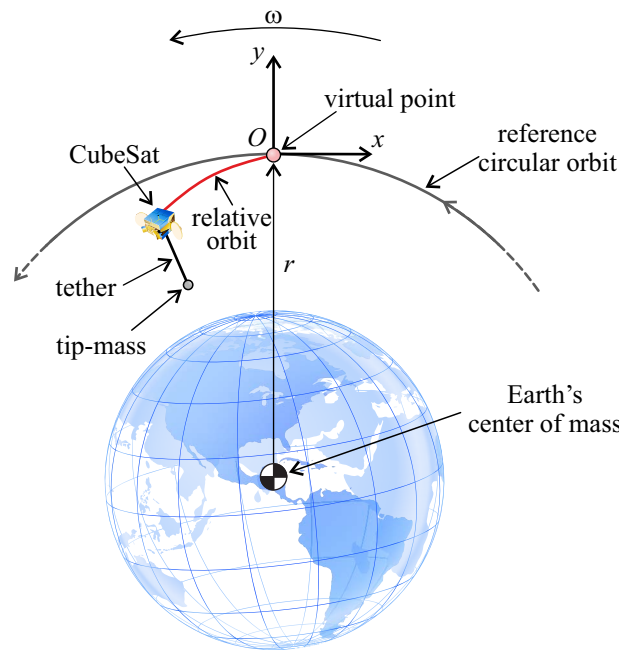


Figure 3. Rotating reference system $\mathcal{T}(O; x, y)$ and relative trajectory (solid line) of a PB-based CubeSat.

Note that the conditions $x(0) = y(0) = 0$ indicate that the virtual point O coincides with the CubeSat center of mass at initial time $t = 0$.

Starting from Equations (3) and (4), it is now possible to calculate the number N of revolutions around the Earth within which the HCW solutions can be considered valid. To this end, consider the time instant t_N corresponding to $N \in \mathbb{N}_0$ orbital periods of the virtual point O , viz.

$$t_N = \frac{2\pi}{\omega} N \tag{5}$$

The corresponding coordinates of the PB-based CubeSat in the rotating reference frame \mathcal{T} were obtained through Equations (3) and (4) as

$$x(t_N) = -\frac{6\pi^2 a_T N^2}{\omega^2} \tag{6}$$

$$y(t_N) = -\frac{4\pi a_T N}{\omega^2} \tag{7}$$

so that the distance $d(t)$ between the CubeSat and the virtual point O is

$$d(t) = \sqrt{x(t)^2 + y(t)^2} \tag{8}$$

the value of which, at $t = t_N$, is given by

$$d(t_N) = \sqrt{x(t_N)^2 + y(t_N)^2} \equiv \frac{4\pi a_T N}{\omega^2} \sqrt{1 + \frac{9\pi^2 N^2}{4}} \tag{9}$$

The maximum value of N (denoted by N_{\max}) is related to d_{\max} , the maximum admissible value of $d(t)$. The latter can be written as a fraction of the reference circular LEO radius r as

$$d_{\max} = \epsilon r \tag{10}$$

where $\epsilon \in (0, 1)$ is a dimensionless parameter depending on the maximum admissible error in position from the linearization process (the greater the ϵ , the greater the error). Substituting Equation (10) into Equation (9), in which $N = N_{\max}$, we obtained

$$N_{\max} = \left\lfloor \frac{\sqrt{2}}{3\pi} \sqrt{\sqrt{1 + \frac{9\epsilon^2\mu_{\oplus}^2}{16a_T^2 r^4}} - 1} \right\rfloor \equiv \left\lfloor \frac{\sqrt{2}}{3\pi} \sqrt{\sqrt{1 + \frac{9\epsilon^2\mu_{\oplus}^2}{16a_T^2 (R_{\oplus} + h)^4}} - 1} \right\rfloor \tag{11}$$

where R_{\oplus} is the Earth’s mean radius; h is the spacecraft altitude above sea level; and $\lfloor \cdot \rfloor$ is the floor function. (Recall that, by definition, N is a natural number.)

As far as the PB-induced drag acceleration is concerned, according to Orsini et al. [53] it is described by the equation

$$a_T = a_{T0} \exp \left[-\frac{m_i g_0 R_{\oplus}^2}{4k_B T} \left(\frac{r - R_{\oplus}}{r^2} - \frac{r_0 - R_{\oplus}}{r_0^2} \right) \right] \tag{12}$$

where r_0 is the initial orbital radius; $m_i = 16 \text{ u}$ is the mean molecular mass of the incoming flow (since the dominant atomic species is oxygen); g_0 is standard gravity; k_B is the Boltzmann constant; $T = 1011.5 \text{ K}$ is the (constant) ionosphere temperature (assuming mean solar activity); and a_{T0} is the plasma brake acceleration at the initial radius of the reference LEO. Accordingly, since a_T is a function of r , the maximum number of revolutions within which the solution to the HCW equations is sound is a function of ϵ and r , that is, $N_{\max} = N_{\max}(\epsilon, r)$.

Figure 4 shows the dependence of N_{\max} on h and ϵ when the PB-induced drag magnitude is $a_{T0} = 0.0024 \text{ mm/s}^2$ and the initial altitude $h_0 = 1000 \text{ km}$. The selected value of a_{T0} is consistent, for example: total spacecraft mass of 10 kg and a 300 m tether at an electric voltage of -1 kV (see Table 1). In this case, the solutions to the HCW equations may be used at an altitude between 300 and 1000 km for at least two revolutions if $\epsilon = 10^{-3}$.

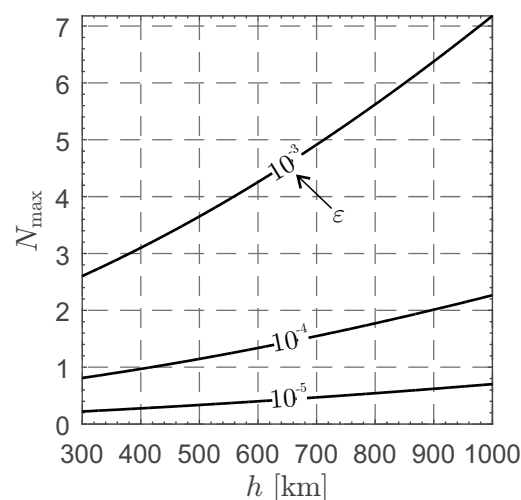


Figure 4. Variation of N_{\max} with h and ϵ when $a_{T0} = 0.0024 \text{ mm/s}^2$ and $h_0 = 1000 \text{ km}$.

Table 1. Characteristics of the satellites in the PB-enabled deorbiting simulations when $h_0 = 1000$ km.

| | m (kg) | L_t (m) | V_t (V) | a_{T0} (mm/s ²) |
|--------------|----------|-----------|-----------|-------------------------------|
| spacecraft ① | 1 | 25 | −500 | 0.0014 |
| spacecraft ② | 4 | 100 | −1000 | 0.0020 |
| spacecraft ③ | 10 | 300 | −1000 | 0.0024 |

Note that the value of N_{\max} increases either when the spacecraft total mass increases or when the Coulomb drag magnitude decreases, that is, when the value of the drag acceleration magnitude a_T falls. This aspect can be analyzed by comparing the approximate results from the analytical Equations (1) and (2) and the outputs of the numerical integration of the nonlinear equations of motion. For example, Figure 5 shows that the approximate solution differs greatly from the numerical one if $\epsilon = 10^{-2}$, while from Figure 6, the approximate solution closely follows the solution from the orbital propagator when $\epsilon = 10^{-3}$. In Figures 5 and 6, the initial value of the PB-induced drag magnitude is $a_{T0} = 0.0024$ mm/s² and the CubeSat initially covered a circular LEO of altitude $h_0 = 1000$ km.

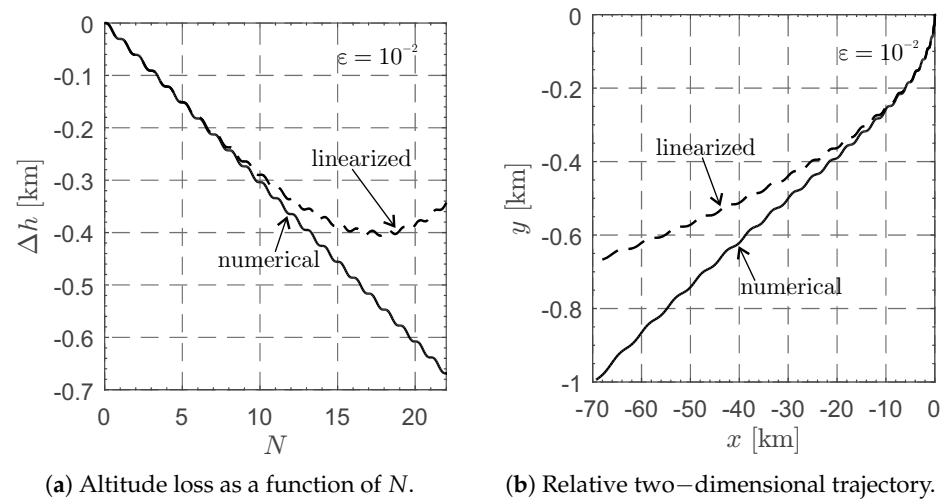


Figure 5. Comparison between the numerical (solid line) and linearized (dashed line) solutions when $a_{T0} = 0.0024$ mm/s², $h_0 = 1000$ km, and $\epsilon = 10^{-2}$.

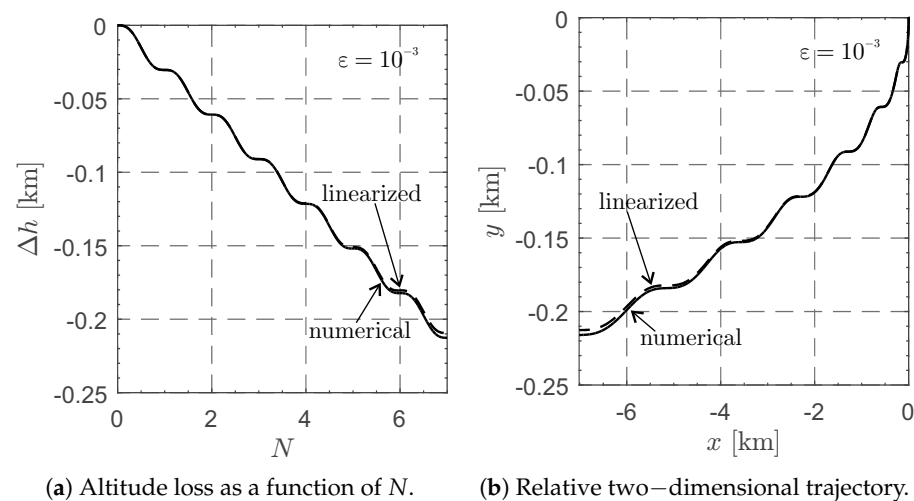


Figure 6. Comparison between the numerical (solid line) and linearized (dashed line) solutions when $a_{T0} = 0.0024$ mm/s², $h_0 = 1000$ km, and $\epsilon = 10^{-3}$.

3. Numerical Simulations and Mission Application

In this section we evaluate the orbital decay time t_d of a CubeSat by using the analytical solutions to the HCW equations from the preceding section. Three different CubeSat configurations were considered for simulation purposes. They were all consistent with a current or near-term readiness level for nanosatellites. Their main characteristics are summarized in Table 1. Note that spacecraft ③ is characterized by the greatest value of PB-induced drag acceleration; accordingly, it was used as a test case to check the soundness of the approximate (analytical) equations.

In all cases, the approximate results were compared with the solutions from the numerical integration of the (nonlinear) two-body equations of motion. The simulations were on a 1.8 GHz Intel® Core™ i7-10510U processor using the MATLAB® ode113 solver with absolute and relative errors equal to 10^{-12} and maximum step size equal to 0.01 terrestrial Canonical Time Units (about 8 s). Starting from altitude $h_0 = 1000$ km, the total decay time required for the spacecraft to reach the final altitude of 300 km, corresponding to the value of the minimum orbital radius $r_{\min} \simeq 1.0470 R_{\oplus}$, was evaluated through an iterative process, in which a_T was assumed to be constant during each cycle. The number of revolutions of the rotating reference system in each cycle came from Equation (11), with $r \in [r_{\min}, R_{\oplus} + h_0]$, where N coincided with the minimum value of N_{\max} with respect to r :

$$N = \left\lfloor \min_r \{N_{\max}(\epsilon, r, a_T(r))\} \right\rfloor \tag{13}$$

From the simulation results of the previous section, assuming a PB-induced drag acceleration of $a_{T0} = 0.0024 \text{ mm/s}^2$ at $h_0 = 1000$ km, the HCW equations gave a good approximation of the numerical results when $\epsilon = 10^{-3}$. The values of N are shown in Table 2 for each case study.

Table 2. Number N of revolutions of the rotating reference system corresponding to each iterative cycle, see Equation (13) with $\epsilon = 10^{-3}$.

| | Spacecraft ① | Spacecraft ② | Spacecraft ③ |
|-----|--------------|--------------|--------------|
| N | 3 | 2 | 2 |

The orbital decay Δr_i in the i -th cycle is given by

$$\Delta r_i = r_i \left[1 - \sqrt{1 + \frac{8\pi a_{Ti} N r_i^2}{\mu_{\oplus}} \left(\frac{9\pi^3 a_{Ti} N^3 r_i^2}{2\mu_{\oplus}} + \frac{2\pi a_{Ti} N r_i^2}{\mu_{\oplus}} - 1 \right)} \right] \tag{14}$$

where

$$a_{Ti} = a_T(r_i) = a_{T0} \exp \left[-\frac{m_i g_0 R_{\oplus}^2}{4k_B T} \left(\frac{r_i - R_{\oplus}}{r_i^2} - \frac{r_0 - R_{\oplus}}{r_0^2} \right) \right] \tag{15}$$

The i -th cycle was therefore characterized by a constant value of PB-induced acceleration a_{Ti} , that is, $a_T(r)$ was approximated by a step function during the whole decay, while the satellite relative position was set equal to zero at the beginning of each cycle. This amounted to modifying the position of the virtual point with respect to which the orbital decay was evaluated at each step, by updating the value of r as

$$r_{i+1} = r_i - \Delta r_i \tag{16}$$

The whole iterative process, which stopped when $r = r_{\min}$, is described in Figure 7. Note that the evaluation of N takes place on the right side of the flow chart (i.e., outside the recursive cycle), which means that the value of N is calculated globally.

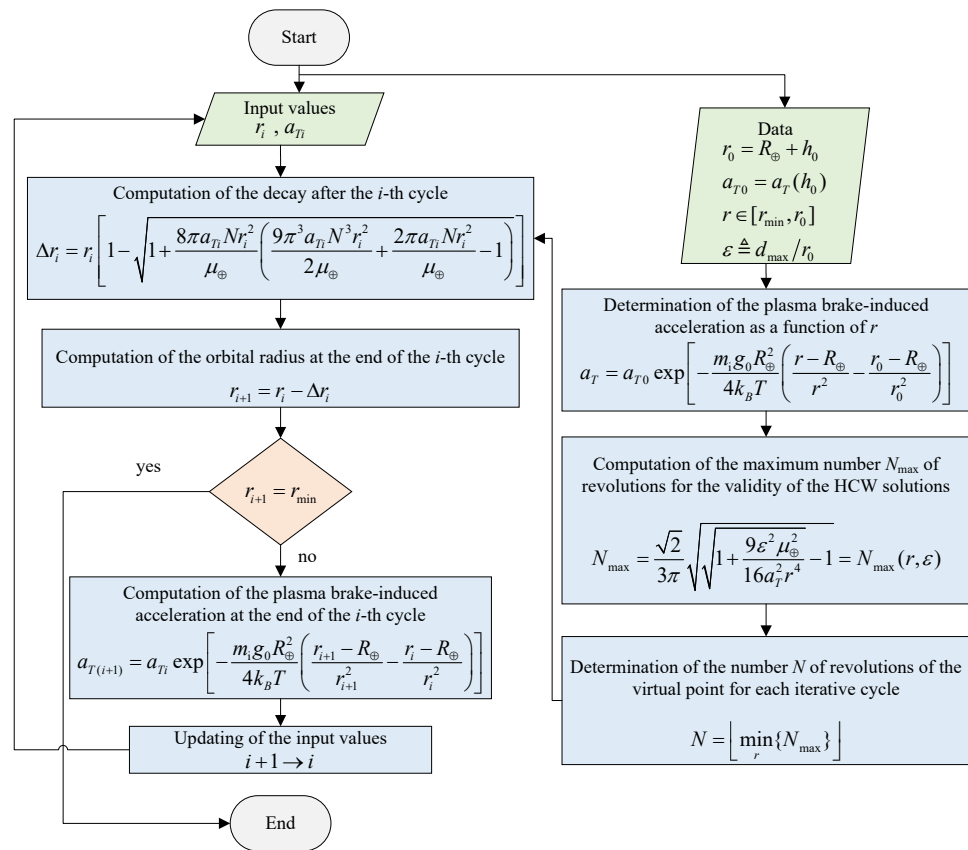


Figure 7. Flow chart of the algorithm for calculating the orbital decay.

The total decay time t_d is simply the sum of the orbital periods of each cycle multiplied by the corresponding number of revolutions of the rotating reference system, which yields

$$t_d = N \sum_i \frac{2\pi}{\omega_i} \tag{17}$$

where

$$\omega_i = \sqrt{\frac{\mu_\oplus}{r_i^3}} \tag{18}$$

The approximate solutions are shown in Table 3 along with the numerical results given by the orbital propagator. Notice that the final error is indeed very small, while in all of the three cases the computational time t_c was reduced by four orders of magnitude when compared to the simulation time required to integrate the nonlinear equations of motion numerically.

Table 3. Decay time t_d and computation time t_c for the three cases studied obtained through numerical integration (actual value) and the proposed algorithm (approximate value).

| | Numerical Integration | | Algorithm | | Error (%) |
|--------------|-----------------------|-----------|---------------|-----------|-----------|
| | t_d (Years) | t_c (s) | t_d (Years) | t_c (s) | |
| spacecraft ① | 3.5632 | 2061 | 3.5697 | 0.1 | 0.1835 |
| spacecraft ② | 2.5006 | 1356 | 2.5026 | 0.1 | 0.0794 |
| spacecraft ③ | 2.0838 | 1162 | 2.0859 | 0.1 | 0.0969 |

4. Conclusions

A plasma brake device may be used to de-orbit a small satellite from an LEO within a few years when the deceleration induced by the Coulomb drag is about 10^{-3} mm/s². The problem has been addressed using an iterative procedure in which the altitude loss of the satellite was obtained from the solutions of the two-dimensional linearized Hill–Clohessy–Wiltshire equations. Notably, the required computational time was reduced by four orders of magnitude when compared to a numerical integration of the whole equations of motion. The results turned out to be very accurate, with positional errors of only about 0.1%. When compared to more conventional approaches based on the numerical integration of the nonlinear equations of motion, the alternative method discussed in this paper for the analysis of the deorbiting trajectory demonstrated that the HCW solutions can be used effectively, under suitable assumptions, to solve the problem even if the deorbiting device interacted with the surrounding space in a complex manner, and a mathematical description of the device-induced drag force represented a difficult problem. Of course, other methods, such as those based on perturbation theories, could be equivalently and successfully used to calculate orbital decay time. However, the HCW solutions were more effective than perturbation theory because, at each iterative cycle, it allowed the spacecraft trajectory to be directly known. As a matter of fact, the knowledge of the actual spacecraft trajectory, not simply the altitude loss, was essential for predicting and preventing possible impacts with other orbiting satellites in LEOs. Future work should concentrate on a refinement of the approximate analytical model by including typical perturbation sources in a LEO.

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Abbreviations

The following abbreviations are used in this manuscript:

| | |
|------------|--|
| a_T | transverse plasma brake-induced acceleration [mm s ⁻²] |
| d | relative distance [m] |
| g_0 | standard gravity [m s ⁻²] |
| h | altitude [m] |
| i | iteration index |
| k_B | Boltzmann constant [J K ⁻¹] |
| L_t | tether length [m] |
| m | spacecraft mass [kg] |
| m_i | mean molecular mass of the incoming flow [kg] |
| N | number of revolutions of the virtual point |
| O | origin of \mathcal{T} |
| r | orbital radius [km] |
| R_\oplus | mean Earth's radius [km] |
| t | time [s] |
| T | ionosphere temperature [K] |
| V_t | tether voltage [V] |
| x | transverse relative coordinate [km] |

| | |
|-------------------|---|
| y | radial relative coordinate [km] |
| ϵ | dimensionless parameter ($\triangleq d_{\max}/r$) |
| μ_{\oplus} | Earth's gravitational parameter [$\text{km}^3 \text{s}^{-2}$] |
| \mathcal{T} | rotating reference system |
| ω | orbital angular velocity [rad/s] |
| <i>Subscripts</i> | |
| c | numerical |
| d | decay |
| max | maximum |
| min | minimum |
| N | relative to N revolutions of the virtual point |
| 0 | initial conditions |

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